## McMURRY FAY

# Chemistry FOURTH EDITION 



## Chapter

## Chemistry: Matter and Measurement

## Life has changed more in the past two centuries than in all the previously recorded span of human

history. The earth's population has increased more than fivefold since 1800 , and life expectancy has nearly doubled because of our ability to synthesize medicines, control diseases, and increase crop yields. Methods of transportation have changed from horses and buggies to automobiles and airplanes because of our

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In both chemistry and daily life, all kinds of measurements must be made. It's best to make them carefully!

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$\sqrt{ }$
Chemistry is an experimental science. Challenge students to sharpen their skills of observation and measurement, relating laboratory work to concepts discussed in lecture.


A Gold, one of the most valuable of elements, has been prized since antiquity for its beauty and resistance to corrosion.
ability to harness the energy in petroleum. Many goods are now made of polymers and ceramics instead of wood and metal because of our ability to manufacture materials with properties unlike any found in nature.

In one way or another, all these changes involve chemistry, the study of the composition, properties, and transformations of matter. Chemistry is deeply involved in both the changes that take place in nature and the profound social changes of the past two centuries. In addition, chemistry is central to the current revolution in molecular biology that is now exploring the details of how life is genetically controlled. No educated person today can understand the modern world without a basic knowledge of chemistry.

## 1.1 | Approaching Chemistry: Experimentation

By opening this book, you have already decided that you need to know more about chemistry. Perhaps you want to learn how medicines are made, how fertilizers and pesticides work, how living organisms function, how new hightemperature ceramics are used in space vehicles, or how microelectronic circuits are etched onto silicon chips. How do you approach chemistry?

> Modern computer chips are made by chemical etching of silicon wafers, using "masks" to produce the tiny circuitry.


One way to approach chemistry is to look around you and try to think of logical explanations for what you see. You would certainly observe, for instance, that different substances have different forms and appearances: Some substances are gases, some are liquids, and some are solids; some are hard and shiny, but others are soft and dull. You'd also observe that different substances behave differently:

Iron, though widely used as a structural material, corrodes easily.


Iron rusts but gold does not; copper conducts electricity but sulfur doesn't. How can these and a vast number of other observations be explained?

The natural world is far too complex to be understood by looking and thinking alone, so a more active approach is needed. Specific questions must be asked, and experiments must be carried out to find their answers. Only when the results of many experiments are known can we then devise an interpretation, or hypothesis, that explains the results. The hypothesis, in turn, can be used to make more predictions and to suggest more experiments until a consistent explanation, or theory, of known observations is finally arrived at.

It's important to keep in mind as you study chemistry or any other science that scientific theories are not laws of nature. All a theory does is to represent the best explanation of experimental results that we can come up with at the present time. Some currently accepted theories will eventually be modified, and others may be replaced altogether if new experiments uncover results that present theories can't explain.

## $1.2 \mid$ Chemistry and the Elements

Everything you see around you is formed from one or more of 114 presently known elements. An element is a fundamental substance that can't be chemically changed or broken down into anything simpler. Mercury, silver, and sulfur are common examples, as listed in Table 1.1.

| TABLE 1.1 | Names and Symbols of Some Common Elements |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Aluminum | Al | Chlorine | $\mathbf{C l}$ | Manganese | $\mathbf{M n}$ | Copper (cuprum) | $\mathbf{C u}$ |
| Argon | $\mathbf{A r}$ | Fluorine | $\mathbf{F}$ | Nitrogen | $\mathbf{N}$ | Iron (ferrum) | $\mathbf{F e}$ |
| Barium | $\mathbf{B a}$ | Helium | $\mathbf{H e}$ | Oxygen | $\mathbf{O}$ | Lead (plumbum) | $\mathbf{P b}$ |
| Boron | $\mathbf{B}$ | Hydrogen | $\mathbf{H}$ | Phosphorus | $\mathbf{P}$ | Mercury (hydrargyrum) | $\mathbf{H g}$ |
| Bromine | $\mathbf{B r}$ | Iodine | $\mathbf{I}$ | Silicon | $\mathbf{S i}$ | Potassium (kalium) | $\mathbf{K}$ |
| Calcium | $\mathbf{C a}$ | Lithium | $\mathbf{L i}$ | Sulfur | $\mathbf{S}$ | Silver (argentum) | $\mathbf{A g}$ |
| Carbon | $\mathbf{C}$ | Magnesium | $\mathbf{M g}$ | Zinc | $\mathbf{Z n}$ | Sodium (natrium) | $\mathbf{N a}$ |

Only about 90 of the 114 presently known elements occur naturally. The remaining ones have been produced artificially by nuclear chemists using highenergy particle accelerators. Furthermore, the 90 or so naturally occurring elements are not equally abundant. Hydrogen is thought to account for approximately $75 \%$ of the mass in the universe; oxygen and silicon together account for $75 \%$ of the earth's crust; and oxygen, carbon, and hydrogen make up more than $90 \%$ of the human body (Figure 1.1). By contrast, there is probably less than 20 grams of the element francium (Fr) dispersed over the entire earth at any one time. Francium is an unstable radioactive element, atoms of which are continually being formed and destroyed in natural radiochemical processes. (We'll discuss radioactivity in Chapter 22.)

For simplicity, chemists refer to specific elements using one- or two-letter symbols. As shown by the examples in Table 1.1, the first letter of an element's symbol is always capitalized, and the second letter, if any, is lowercase. Many of the symbols are just the first one or two letters of the element's English name: $\mathrm{H}=$ hydrogen, $\mathrm{C}=$ carbon, $\mathrm{Al}=$ aluminum, and so forth. Other symbols derive from Latin or other languages: $\mathrm{Na}=$ sodium (Latin, natrium), $\mathrm{Pb}=$ lead (Latin, plumbum), $\mathrm{W}=$ tungsten (German, wolfram). The names, symbols, and other information about all 114 elements are given inside the front cover of this book, organized in a form called the periodic table.

Elements can be broken down into simpler substances (protons, neutrons, electrons, etc.), but the energy required is greater than available under ordinary chemical conditions.


- Samples of mercury, silver, and sulfur (clockwise from top left).

P.G. Nelson, "Important Elements," J. Chem. Educ., Vol. 68, 1991, 732-737.

7. Vivi Ringes, "Origin of the Names of Chemical Elements," J. Chem. Educ., Vol. 66, 1989, 731-738.

FIGURE 1.1 Estimated elemental composition (by mass percent) of (a) the earth's crust and (b) the human body. Oxygen is the most abundant element in both. Only the major constituents are shown in each case; small amounts of many other elements are also present.

(a)

Relative abundance in the human body

(b)

- PROBLEM 1.1 Look at the alphabetical list of elements inside the front cover, and find the symbols for the following elements:
(a) Cadmium (used in batteries)
(b) Antimony (used in alloys with other metals)
(c) Americium (used in smoke detectors)
- PROBLEM 1.2 Look at the alphabetical list of elements inside the front cover, and tell what elements the following symbols represent:
(a) Ag
(b) Rh
(c) Re
(d) Cs
(e) Ar
(f) As


### 1.3 Elements and the Periodic Table

Ten elements have been known since the beginning of recorded history: antimony $(\mathrm{Sb})$, carbon $(\mathrm{C})$, copper $(\mathrm{Cu})$, gold $(\mathrm{Au})$, iron $(\mathrm{Fe})$, lead $(\mathrm{Pb})$, mercury $(\mathrm{Hg})$, silver (Ag), sulfur (S), and tin (Sn). The first "new" element to be found in several thousand years was arsenic (As), discovered in about 1250. In fact, only 24 elements were known at the time of the American Revolution, in 1776.
progression in the size of the seven periods (rows). The first period has only 2 elements, hydrogen $(\mathrm{H})$ and helium $(\mathrm{He})$; the second and third periods have 8 elements each; the fourth and fifth periods have 18 elements each; and the sixth and (incomplete) seventh periods, which include the lanthanides and actinides, have 32 elements each. We'll see in Chapter 5 that this regular progression in the periodic table reflects a similar regularity in the structure of atoms.

Notice also that not all groups (columns) in the periodic table have the same number of elements. The two larger groups on the left and the six larger groups on the right of the table are called the main groups; the ten smaller ones in the middle of the table are called the transition metal groups; and the fourteen shown separately at the bottom of the table are called the inner transition metal groups.

## 1.4 | Some Chemical Properties of the Elements

Any characteristic that can be used to describe or identify matter is called a property. Examples include size, amount, odor, color, and temperature. Still other properties include such characteristics as melting point, solubility, and chemical behavior. For example, we might list some properties of sodium chloride (table salt) by saying that it melts at $1474^{\circ} \mathrm{F}$ (or $801^{\circ} \mathrm{C}$ ), dissolves in water, and undergoes a chemical reaction when it comes into contact with a silver nitrate solution.

Properties can be classified as either intensive or extensive, depending on whether their values change with the size of the sample. Intensive properties, like temperature and melting point, have values that do not depend on the amount of sample. Thus, a small ice cube might have the same temperature as a massive iceberg. Extensive properties, like length and volume, have values that do depend on the sample size. An ice cube is much smaller than an iceberg.

Properties can also be classified as either physical or chemical, depending on whether the property involves a change in the chemical makeup of a substance. Physical properties are characteristics that do not involve a change in a sample's chemical makeup, whereas chemical properties are characteristics that do involve a change in chemical makeup. The melting point of ice, for instance, is a physical property because melting causes the water to change only in form, from solid to liquid, but not in chemical makeup. The rusting of an iron bicycle left in the rain is a chemical property, however, because iron combines with oxygen and moisture from the air to give the new substance, rust. Table 1.2 lists other examples of both physical and chemical properties.

TABLE 1.2 Some Examples of Physical and Chemical Properties

| Physical Properties |  | Chemical Properties |
| :--- | :--- | :--- |
| Temperature | Amount | Rusting (of iron) |
| Color | Odor | Combustion (of gasoline) |
| Melting point | Solubility | Tarnishing (of silver) |
| Electrical conductivity | Hardness | Hardening (of cement) |

As noted in Section 1.3, groups of elements in the periodic table often show remarkable similarities in their chemical properties. Look at the following groups, for instance, to see some examples of this behavior:

- Group 1A—Alkali metals Lithium (Li), sodium (Na), potassium (K), rubidium $(\mathrm{Rb})$, and cesium (Cs) are shiny, soft metals. All react rapidly (often violently) with water to form products that are highly alkaline, or basic-hence the name alkali metals. Because of their high reactivity, the alkali metals are never found in nature in the pure state but only in combination with other elements.

James L. Marshall, "A Living Periodic Table," J. Chem. Educ., Vol. 77, 2000, 979-983. Describes a portable and permanent collection of 87 elements.


A Addition of a solution of sodium chloride to a solution of silver nitrate yields a white precipitate of solid silver chloride.

V
While elements within the same group tend to have similar chemical properties, due to its small size the first member of each main group exhibits a chemistry that differs most from the other members of the group.


Hydrogen is a unique element. Although listed under group 1A, hydrogen is not a metal under ordinary conditions. In its ionic chemistry, hydrogen sometimes behaves as though it belongs in group 7A.


Note that hydrogen (H) is placed in group 1A even though, as a colorless gas, it is completely different in appearance and behavior from the alkali metals. We'll see the reason for this classification in Section 5.13.


A Sodium, one of the alkali metals, reacts violently with water to yield hydrogen gas and an alkaline (basic) solution.

- Group 2A—Alkaline earth metals Beryllium (Be), magnesium ( Mg ), calcium $(\mathrm{Ca})$, strontium $(\mathrm{Sr})$, barium ( Ba ), and radium ( Ra ) are also lustrous, silvery metals, but are less reactive than their neighbors in group 1A. Like the alkali metals, the alkaline earths are never found in nature in the pure state.
- Group 7A—Halogens Fluorine (F), chlorine (Cl), bromine (Br), and iodine (I), are colorful, corrosive nonmetals. They are found in nature only in combination with other elements, such as with sodium in table salt (sodium chloride, $\mathrm{NaCl})$. In fact, the group name halogen is taken from the Greek word hals, meaning "salt." Astatine (At) is also a halogen, but it exists in such tiny amounts that little is known about it.

Bromine, a halogen, is a corrosive dark red liquid at room temperature.

- Group 8A-Noble gases Helium (He), neon (Ne), argon (Ar), krypton (Kr), xenon ( Xe ), and radon ( Rn ) are gases of very low reactivity. Helium, neon, and argon don't combine with any other element; krypton and xenon combine with very few.


4 Neon, one of the noble gases, is used in neon lights and signs.

Although the resemblances aren't as pronounced as they are within a single group, neighboring groups of elements also behave similarly in some ways. Thus, as indicated in Figure 1.2, the periodic table is often divided into three major classes of elements: metals, nonmetals, and semimetals:

- Metals Metals, the largest category of elements, are found on the left side of the periodic table, bounded on the right by a zigzag line running from boron (B) at the top to astatine (At) at the bottom. The metals are easy to characterize by their appearance: All except mercury are solid at room temperature, and most have the silvery shine we normally associate with metals. In addition, metals are generally malleable rather than brittle, can be twisted and drawn into wires without breaking, and are good conductors of heat and electricity.
- Nonmetals Nonmetals are found on the right side of the periodic table and, like metals, are also easy to characterize by their appearance. Eleven of the seventeen nonmetals are gases, one is a liquid (bromine), and only five are solids at room temperature (carbon, phosphorus, sulfur, selenium, and iodine). None are silvery in appearance, and several are brightly colored. The solid nonmetals are brittle rather than malleable, and they are poor conductors of heat and electricity.


A Most metals are silvery solids that conduct electricity and can be formed into wires.


- Phosphorus, iodine, and sulfur (clockwise from top left) are typical nonmetals. All are brittle, and none conduct electricity.



B Charles W. Earley, "A Simple
Demonstration for Introducing the Metric System to Introductory Chemistry Classes," J. Chem. Educ., Vol. 76, 1999, 1215-1216.

- Semimetals Seven of the nine elements adjacent to the zigzag boundary between metals and nonmetals-boron, silicon, germanium, arsenic, antimony, tellurium, and astatine-are known as semimetals, or metalloids, because their properties are intermediate between those of their metallic and nonmetallic neighbors. Though most are silvery in appearance and all are solid at room temperature, semimetals are brittle rather than malleable and tend to be poor conductors of heat and electricity. Silicon, for example, is a widely used semiconductor, a substance whose electrical conductivity is intermediate between that of a metal and an insulator.

Computer chips are produced from wafers of silicon, a semimetal.


PROBLEM 1.3 Identify the following elements as metals, nonmetals, or semimetals:
(a) Ti
(b) Te
(c) Se
(d) Sc
(e) At
(f) Ar
-KEY CONCEPT PROBLEM 1.4 The three so-called "coinage metals" are located near the middle of the periodic table. Use the periodic table to identify them.


## 1.5 | Experimentation and Measurement

Chemistry is an experimental science. But if our experiments are to be reproducible, we must be able to describe fully the substances we're working withtheir amounts, volumes, temperatures, and so forth. Thus, one of the most important requirements in chemistry is that we have a way to measure things.

Under an international agreement concluded in 1960, scientists throughout the world now use the International System of Units for measurement, abbreviated SI for the French Système Internationale d'Unités. Based on the metric system, which is used in all industrialized countries of the world except the United States, the SI system has seven fundamental units (Table 1.3). These seven fundamental units, along with others derived from them, suffice for all scientific measurements. We'll look at three of the most common units in this chapter-those for mass, length, and temperature-and will discuss others as the need arises in later chapters.

TABLE 1.3 The Seven Fundamental SI Units of Measure

| Physical Quantity | Name of Unit | Abbreviation |
| :--- | :--- | :--- |
| Mass | kilogram | kg |
| Length | meter | m |
| Temperature | kelvin | K |
| Amount of substance | mole | mol |
| Time | second | s |
| Electric current | ampere | A |
| Luminous intensity | candela | cd |

One problem with any system of measurement is that the sizes of the units sometimes turn out to be inconveniently large or small. For example, a chemist describing the diameter of a sodium atom ( 0.000000000372 m ) would find the meter ( m ) to be inconveniently large, but an astronomer describing the average distance from the earth to the sun ( $150,000,000,000 \mathrm{~m}$ ) would find the meter to be inconveniently small. For this reason, SI units are modified through the use of prefixes when they refer to either smaller or larger quantities. Thus, the prefix millimeans one-thousandth, and a millimeter (mm) is $1 / 1000$ of 1 meter. Similarly, the prefix kilo- means one thousand, and a kilometer $(\mathrm{km})$ is 1000 meters. [Note that the SI unit for mass (kilogram) already contains the kilo- prefix.] A list of prefixes is shown in Table 1.4, with the most commonly used ones in red.

## TABLE 1.4 Some Prefixes for Multiples of SI Units

| Factor | Prefix | Symbol | Example |
| :---: | :---: | :---: | :---: |
| $1,000,000,000=10^{9}$ | giga | G | 1 gigameter (Gm) $=10^{9} \mathrm{~m}$ |
| $1,000,000=10^{6}$ | mega | M | 1 megameter $(\mathrm{Mm})=10^{6} \mathrm{~m}$ |
| $1,000=10^{3}$ | kilo | k | 1 kilogram (kg) $=10^{3} \mathrm{~g}$ |
| $100=10^{2}$ | hecto | h | 1 hectogram (hg) $=100 \mathrm{~g}$ |
| $10=10^{1}$ | deka | da | 1 dekagram (dag) $=10 \mathrm{~g}$ |
| $0.1=10^{-1}$ | deci | d | 1 decimeter $(\mathrm{dm})=0.1 \mathrm{~m}$ |
| $0.01=10^{-2}$ | centi | c | 1 centimeter $(\mathrm{cm})=0.01 \mathrm{~m}$ |
| $0.001=10^{-3}$ | milli | m | 1 milligram $(\mathrm{mg})=0.001 \mathrm{~g}$ |
| *0.000001 $=10^{-6}$ | micro | $\mu$ | 1 micrometer ( $\mu \mathrm{m}$ ) $=10^{-6} \mathrm{~m}$ |
| * $0.000000001=10^{-9}$ | nano | n | 1 nanosecond (ns) $=10^{-9} \mathrm{~s}$ |
| ${ }^{*} 0.000000000001=10^{-12}$ | pico | p | 1 picosecond (ps) $=10^{-12} \mathrm{~s}$ |

* For very small numbers, it is becoming common in scientific work to leave a thin space every three digits to the right of the decimal point.

Notice how numbers that are either very large or very small are indicated in Table 1.4 using an exponential format called scientific notation. For example, the number 55,000 is written in scientific notation as $5.5 \times 10^{4}$, and the number 0.00320 as $3.20 \times 10^{-3}$. Review Appendix A if you are uncomfortable with scientific notation or if you need to brush up on how to do mathematical manipulations on numbers with exponents.

Notice also that all measurements contain both a number and a unit label. A number alone is not much good without a unit to define it. If you asked a friend

VAll systems of measurement are based on arbitrary standards. The SI system is as arbitrary as the English system, but the relationship of one unit to another is more systematic and easier to remember in the metric system.

## -

$\nabla$
For very large or very small quantities, commonly used prefixes represent amounts that vary by three powers of 10 , for example, milli, micro, nano, and pico $\left(10^{-3}, 10^{-6}, 10^{-9}\right.$, and $10^{-12}$, respectively).

Mark L. Campbell, "Having Fun with the Metric System," J. Chem. Educ., Vol. 68, 1991, 1048. A word game.
how far it was to the nearest tennis court, the answer " 3 " alone wouldn't tell you much. 3 blocks? 3 kilometers? 3 miles?

- PROBLEM 1.5 Express the following quantities in scientific notation:
(a) The diameter of a sodium atom, 0.000000000372 m
(b) The distance from the earth to the sun, 150,000,000,000 m
- PROBLEM 1.6 What units do the following abbreviations represent?
(a) $\mu g$
(b) dm
(c) ps
(d) kA
(e) mmol


## 1.6| Measuring Mass

Mass is defined as the amount of matter in an object. Matter, in turn, is a catchall term used to describe anything with a physical presence-anything you can touch, taste, or smell. (Stated more scientifically, matter is anything that has mass.) Mass is measured in SI units by the kilogram (kg; $1 \mathrm{~kg}=2.205$ U.S. lb). Because the kilogram is too large for many purposes in chemistry, the metric gram ( $\mathbf{g}$; $1 \mathrm{~g}=0.001 \mathrm{~kg}$ ), the milligram ( $\mathbf{m g}, 1 \mathrm{mg}=0.001 \mathrm{~g}=10^{-6} \mathrm{~kg}$ ), and the micro$\operatorname{gram}\left(\boldsymbol{\mu g} ; 1 \mu \mathrm{~g}=0.001 \mathrm{mg}=10^{-6} \mathrm{~g}=10^{-9} \mathrm{~kg}\right.$ ) are more commonly used. One gram is about half the mass of a U.S. penny.

$$
\begin{gather*}
1 \mathrm{~kg}=1000 \mathrm{~g}=1,000,000 \mathrm{mg}=1,000,000,000 \mu \mathrm{~g}  \tag{2.205lb}\\
1 \mathrm{~g}=1000 \mathrm{mg}=1,000,000 \mu \mathrm{~g} \quad(0.03527 \mathrm{oz}) \\
1 \mathrm{mg}=1000 \mu \mathrm{~g}
\end{gather*}
$$

This pile of 400 pennies weighs about 1 kg .


The standard kilogram is defined as the mass of a cylindrical bar of platinumiridium alloy stored in a vault in a suburb of Paris, France. There are 40 copies of this bar distributed throughout the world, with two (Numbers 4 and 20) stored at the U.S. National Institute of Standards and Technology near Washington, D.C.

The terms "mass" and "weight," although often used interchangeably, have quite different meanings. Mass is a physical property that measures the amount of matter in an object, whereas weight measures the pull of gravity on an object by the earth or other celestial body. The mass of an object is independent of its location; your body has the same amount of matter whether you're on Earth or on the moon. The weight of an object, however, does depend on its location; if you weighed 140 lb on Earth, you would weigh only about 23 lb on the moon, which has a lower gravity than the earth.

At the same location on Earth, two objects with identical masses have identical weights; that is, the objects experience an identical pull of the earth's gravity. Thus, the mass of an object can be measured by comparing the weight of the object to the weight of a reference standard of known mass. Much of the confusion

between mass and weight is simply due to a language problem: We speak of "weighing" when we really mean that we are measuring mass by comparing two weights. Figure 1.3 shows two types of balances normally used for measuring mass in the laboratory.

## 1.7 | Measuring Length

The meter ( $\mathbf{m}$ ) is the standard unit of length in the SI system. Although originally defined in 1790 as being 1 ten-millionth of the distance from the equator to the North Pole, the meter was redefined in 1889 as the distance between two thin lines on a bar of platinum-iridium alloy stored outside Paris, France. To accommodate an increasing need for precision, the meter was redefined again in 1983 as equal to the distance traveled by light through a vacuum in $1 / 299,792,458$ second. Although this new definition isn't as easy to grasp as the distance between two scratches on a bar, it has the great advantage that it can't be lost or damaged.

One meter is 39.37 inches, about $10 \%$ longer than an English yard and much too large for most measurements in chemistry. Other, more commonly used measures of length are the centimeter ( $\mathrm{cm} ; 1 \mathrm{~cm}=0.01 \mathrm{~m}$, a bit less than half an inch), the millimeter ( $\mathbf{m m}$; $1 \mathrm{~mm}=0.001 \mathrm{~m}$, about the thickness of a U.S. dime), the micrometer ( $\mu \mathrm{m} ; 1 \mu \mathrm{~m}=10^{-6} \mathrm{~m}$ ), the nanometer ( $\mathrm{nm} ; 1 \mathrm{~nm}=10^{-9} \mathrm{~m}$ ), and the picometer ( $\mathbf{p m} ; 1 \mathrm{pm}=10^{-12} \mathrm{~m}$ ). Thus, a chemist might refer to the diameter of a sodium atom as $372 \mathrm{pm}\left(3.72 \times 10^{-10} \mathrm{~m}\right)$.

$$
\begin{gathered}
1 \mathrm{~m}=100 \mathrm{~cm}=1000 \mathrm{~mm}=1,000,000 \mu \mathrm{~m}=1,000,000,000 \mathrm{~nm} \quad(1.0936 \mathrm{yd}) \\
1 \mathrm{~cm}=10 \mathrm{~mm}=10,000 \mu \mathrm{~m}=10,000,000 \mathrm{~nm} \quad(0.3937 \mathrm{in} .) \\
1 \mathrm{~mm}=1000 \mu \mathrm{~m}=1,000,000 \mathrm{~nm}
\end{gathered}
$$

## 1.8| Measuring Temperature

Just as the kilogram and the meter are slowly replacing the pound and the yard as common units for mass and length measurement in the United States, the Celsius degree $\left({ }^{\circ} \mathrm{C}\right)$ is slowly replacing the Fahrenheit degree $\left({ }^{\circ} \mathrm{F}\right)$ as the common unit for temperature measurement. In scientific work, however, the kelvin ( $K$ ) is replacing both. (Note that we say only "kelvin," not "kelvin degree.")

For all practical purposes, the kelvin and the Celsius degree are the sameboth are one-hundredth of the interval between the freezing point of water and the boiling point of water at standard atmospheric pressure. The only real difference between the two units is that the numbers assigned to various points on the scales differ. Whereas the Celsius scale assigns a value of $0^{\circ} \mathrm{C}$ to the freezing point of water and $100^{\circ} \mathrm{C}$ to the boiling point of water, the Kelvin scale assigns a value of 0 K to the coldest possible temperature, $-273.15^{\circ} \mathrm{C}$, sometimes called absolute zero. Thus, $0 \mathrm{~K}=-273.15^{\circ} \mathrm{C}$ and $273.15 \mathrm{~K}=0^{\circ} \mathrm{C}$. For example, a warm spring day
$\measuredangle$ FIGURE 1.3 (a) The singlepan balance has a sliding counterweight that is adjusted until the weight of the object on the pan is just balanced. (b) Modern electronic balances.

© The length of these bacteria on the tip of a pin is about $5 \times 10^{-7} \mathrm{~m}$.


A Some of the hottest land temperatures on earth-up to $134^{\circ} \mathrm{F}$-have been recorded at Death Valley, California.
with a Celsius temperature of $25^{\circ} \mathrm{C}$ has a Kelvin temperature of $25+273.15$ $=298 \mathrm{~K}$.

$$
\begin{aligned}
& \text { Temperature in } \mathrm{K}=\text { Temperature in }{ }^{\circ} \mathrm{C}+273.15 \\
& \text { Temperature in }{ }^{\circ} \mathrm{C}=\text { Temperature in } \mathrm{K}-273.15
\end{aligned}
$$

In contrast to the Kelvin and Celsius scales, the common Fahrenheit scale specifies an interval of $180^{\circ}$ between the freezing point $\left(32^{\circ} \mathrm{F}\right)$ and the boiling point $\left(212^{\circ} \mathrm{F}\right)$ of water. Thus, it takes 180 Fahrenheit degrees to cover the same range as 100 Celsius degrees (or kelvins), and a Fahrenheit degree is therefore only $100 / 180=5 / 9$ as large as a Celsius degree. Figure 1.4 compares the Kelvin, Celsius, and Fahrenheit scales.

FIGURE 1.4 A comparison of the Kelvin, Celsius, and Fahrenheit temperature scales. One Fahrenheit degree is $5 / 9$ the size of a kelvin or a Celsius degree.


Two adjustments need to be made to convert between Fahrenheit and Celsius scales-one to adjust for the difference in degree size and one to adjust for the difference in zero points. The size adjustment is made using the relationship $1^{\circ} \mathrm{C}=(9 / 5)^{\circ} \mathrm{F}$ and $1^{\circ} \mathrm{F}=(5 / 9)^{\circ} \mathrm{C}$. The zero-point adjustment is made by remembering that the freezing point of water is higher by 32 on the Fahrenheit scale than on the Celsius scale. Thus, if you want to convert from Celsius to Fahrenheit, you do a size adjustment (multiply ${ }^{\circ} \mathrm{C}$ by $9 / 5$ ) and then a zero-point adjustment (add 32); if you want to convert from Fahrenheit to Celsius, you find out how many Fahrenheit degrees there are above freezing (by subtracting 32) and then do a size adjustment (multiply by 5/9). The following formulas describe the conversions, and Worked Example 1.1 shows how to do a calculation.
$\begin{array}{ll}\text { Celsius to Fahrenheit: } & \text { Fahrenheit to Celsius: } \\ { }^{\circ} \mathrm{F}=\left(\frac{9^{\circ} \mathrm{F}}{5^{\circ} \mathrm{C}} \times{ }^{\circ} \mathrm{C}\right)+32^{\circ} \mathrm{F} & { }^{\circ} \mathrm{C}=\frac{5^{\circ} \mathrm{C}}{9^{\circ} \mathrm{F}} \times\left({ }^{\circ} \mathrm{F}-32^{\circ} \mathrm{F}\right)\end{array}$

## Worked Example 1.1

The melting point of table salt is $1474^{\circ} \mathrm{F}$. What temperature is this on the Celsius and Kelvin scales?

## SOlUTION

There are two ways to do this and every other problem in chemistry. One is to think things through to be sure you understand what's going on; the other is to plug numbers into a formula and hope for the best. The thinking approach always works; the formula approach works only if you use the right equation. Let's try both ways.

The thinking approach: We're given a temperature in Fahrenheit degrees, and we need to convert to Celsius degrees. A temperature of $1474^{\circ} \mathrm{F}$ corresponds to $1474-32=1442$ Fahrenheit degrees above the freezing point of water. Since each Fahrenheit degree is only $5 / 9$ as large as a Celsius degree, 1442 Fahrenheit degrees above freezing equals $1442 \times 5 / 9=801$ Celsius degrees above freezing $\left(0^{\circ} \mathrm{C}\right)$, or $801^{\circ} \mathrm{C}$. The same number of degrees above freezing on the Kelvin scale ( 273.15 K ) corresponds to a temperature of $273.15+801=1074 \mathrm{~K}$.

The formula approach: Set up an equation using the temperature conversion formula for changing from Fahrenheit to Celsius:

$$
{ }^{\circ} \mathrm{C}=\left(\frac{5^{\circ} \mathrm{C}}{9^{\circ} \mathrm{F}}\right)\left(1474^{\circ} \mathrm{F}-32^{\circ} \mathrm{F}\right)=801^{\circ} \mathrm{C}
$$

Converting to Kelvin gives a temperature of $801^{\circ}+273.15^{\circ}=1074 \mathrm{~K}$.
Since the answers obtained by the two approaches agree, we can feel fairly confident that our thinking is following the right lines and that we understand the material. (If the answers did not agree, we'd be alerted to a misunderstanding somewhere.)

- PROBLEM 1.7 The normal body temperature of a healthy adult is $98.6^{\circ} \mathrm{F}$. What is this value on both Celsius and Kelvin scales?
- PROBLEM 1.8 Carry out the indicated temperature conversions.
(a) $-78^{\circ} \mathrm{C}=? \mathrm{~K}$
(b) $158^{\circ} \mathrm{C}=?^{\circ} \mathrm{F}$
(c) $375 \mathrm{~K}=?^{\circ} \mathrm{F}$


## 1.9 | Derived Units: Measuring Volume

Look back at the seven fundamental SI units given in Table 1.3 and you'll find that measures for such familiar quantities as area, volume, density, speed, and pressure are missing. All are examples of derived quantities rather than fundamental quantities because they can be expressed using one or more of the seven base units (Table 1.5).

| TABLE 1.5 | Some Derived Quantities |  |
| :--- | :--- | :--- |
| Quantity | Definition | Derived Unit (Name) |
| Area | Length times length | $\mathrm{m}^{2}$ |
| Volume | Area times length | $\mathrm{m}^{3}$ |
| Density | Mass per unit volume | $\mathrm{kg} / \mathrm{m}^{3}$ |
| Speed | Distance per unit time | $\mathrm{m} / \mathrm{s}$ |
| Acceleration | Change in speed per unit time | $\mathrm{m} / \mathrm{s}^{2}$ |
| Force | Mass times acceleration | $(\mathrm{kg} \cdot \mathrm{m}) / \mathrm{s}^{2}$ (newton, N) |
| Pressure | Force per unit area | $\mathrm{kg} /\left(\mathrm{m} \cdot \mathrm{s}^{2}\right)($ pascal, Pa) |
| Energy | Force times distance | $\left(\mathrm{kg} \cdot \mathrm{m}^{2}\right) / \mathrm{s}^{2}$ (joule, J) |

Volume, the amount of space occupied by an object, is measured in SI units by the cubic meter $\left(\mathbf{m}^{3}\right)$, defined as the amount of space occupied by a cube 1 meter on each edge (Figure 1.5).

A cubic meter equals 264.2 U.S. gallons, much too large a quantity for normal use in chemistry. As a result, smaller, more convenient measures are commonly employed. Both the cubic decimeter $\left(1 \mathrm{dm}^{3}=0.001 \mathrm{~m}^{3}\right)$, equal in size to the more familiar metric liter ( L ), and the cubic centimeter ( $1 \mathrm{~cm}^{3}=0.001 \mathrm{dm}^{3}=10^{-6} \mathrm{~m}^{3}$ ), equal in size to the metric milliliter ( mL ), are particularly convenient. Slightly


A The melting point of sodium chloride is $1474^{\circ} \mathrm{F}$, or $801^{\circ} \mathrm{C}$.

Remind students to raise both the measured number and unit to the appropriate power when dealing with areas and volumes. For example, $(3 \mathrm{~cm})^{3}=3^{3} \mathrm{~cm}^{3}=$ $27 \mathrm{~cm}^{3}$, not $3 \mathrm{~cm}^{3}$ or 27 cm .


- FIGURE 1.5 A cubic meter is the volume of a cube 1 meter along each edge. Each cubic meter contains 1000 cubic decimeters (liters), and each cubic decimeter contains 1000 cubic centimeters (milliliters).
larger than 1 U.S. quart, a liter has the volume of a cube 1 dm on edge. Similarly, a milliliter has the volume of a cube 1 cm on edge (Figure 1.5).

$$
\begin{aligned}
& 1 \mathrm{~m}^{3}=1000 \mathrm{dm}^{3}=1,000,000 \mathrm{~cm}^{3} \quad(264.2 \mathrm{gal}) \\
& 1 \mathrm{dm}^{3}=1 \mathrm{~L}=1000 \mathrm{~mL} \quad(1.057 \mathrm{qt})
\end{aligned}
$$

Figure 1.6 shows some of the equipment frequently used in the laboratory for measuring liquid volume.


A FIGURE 1.6 Among the most common items of laboratory equipment used for measuring liquid volume are (a) a graduated cylinder, a volumetric flask, a syringe, and (b) a buret.

### 1.10 | Derived Units: Measuring Density

The intensive physical property that relates the mass of an object to its volume is called density. Density, which is simply the mass of an object divided by its
volume, is expressed in the SI derived unit $\mathrm{g} / \mathrm{cm}^{3}$ for a solid or $\mathrm{g} / \mathrm{mL}$ for a liquid. The densities of some common materials are given in Table 1.6.

$$
\text { Density }=\frac{\text { Mass }(\mathrm{g})}{\text { Volume }\left(\mathrm{mL} \text { or } \mathrm{cm}^{3}\right)}
$$

| TABLE 1.6 | Densities of Some Common Materials |  |  |
| :--- | :--- | :--- | :--- |
| Substance | Density $\left(\mathbf{g} / \mathbf{c m}^{\mathbf{3}}\right)$ | Substance | Density $\left(\mathbf{g} / \mathbf{c m}^{\mathbf{3}}\right)$ |
| Ice $\left(0^{\circ} \mathrm{C}\right)$ | 0.917 | Human fat | 0.94 |
| Water $\left(3.98^{\circ} \mathrm{C}\right)$ | 1.0000 | Human muscle | 1.06 |
| Gold | 19.31 | Cork | $0.22-0.26$ |
| Helium $\left(25^{\circ} \mathrm{C}\right)$ | 0.000164 | Balsa wood | 0.12 |
| Air $\left(25^{\circ} \mathrm{C}\right)$ | 0.001185 | Earth | 5.54 |

Because most substances change in volume when heated or cooled, densities are temperature-dependent. At $3.98^{\circ} \mathrm{C}$, for example, a 1.0000 mL container holds exactly 1.0000 g of water (density $=1.0000 \mathrm{~g} / \mathrm{mL}$ ). As the temperature is raised, however, the volume occupied by the water expands so that only 0.9584 g fits in the 1.0000 mL container at $100^{\circ} \mathrm{C}($ density $=0.9584 \mathrm{~g} / \mathrm{mL})$. When reporting a density, the temperature must also be specified.

Although most substances expand when heated and contract when cooled, water behaves differently. Water contracts when cooled from $100^{\circ} \mathrm{C}$ to $3.98^{\circ} \mathrm{C}$, but below this temperature it begins to expand again. Thus, the density of liquid water is at its maximum of $1.0000 \mathrm{~g} / \mathrm{mL}$ at $3.98^{\circ} \mathrm{C}$, but decreases to $0.99987 \mathrm{~g} / \mathrm{mL}$ at $0^{\circ} \mathrm{C}$ (Figure 1.7). When freezing occurs, the density drops still further to a value of $0.917 \mathrm{~g} / \mathrm{cm}^{3}$ for ice at $0^{\circ} \mathrm{C}$. Ice and any other substance with a density less than that of water will float, but any substance with a density greater than that of water will sink.


Density is sometimes confused with mass. A kg of feathers weights the same as a kg of gold, but gold occupies less space because it has a greater density, the ratio of mass to volume.


A Which weighs more, the brass weight or the pillow? Actually, both have the same mass and weight, but the brass has a higher density because its volume is smaller.

vBecause students are very familiar with water they tend to use it as a standard when relating the density of a solid to the density of a liquid. Most solids sink in their liquids; water is unusual in that ice floats atop liquid water.

Kenneth E. Kolb and Doris K. Kolb, "Method for Separating or Identifying Plastics,"
J. Chem. Educ., Vol. 68, 1991, 348. A practical use of density.

FIGURE 1.7 The density of water at different temperatures. Density reaches a maximum value of $1.000 \mathrm{~g} / \mathrm{mL}$ at $3.98^{\circ} \mathrm{C}$.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Sugar in a Can of Soft Drink: A Density Exercise," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2, (American Chemical Society, Washington, DC, 1988)
pp. 126-127. Regular and diet soft drinks are identified by differences in their densities.

David. A. Franz and David Speckhard, "Densities and Miscibilities of Liquids and Liquid Mixtures," J. Chem. Educ., Vol. 68, 1991, 594. Using a graduated cylinder and electronic balance, the densities of water, dichloromethane, and petroleum ether are determined. A heavier mass of water is shown to form a layer on top of the more dense dichloromethane, but below the less dense petroleum ether. Mixtures of the miscible organic solvents are prepared with average densities above or below the density of water.

Knowing the density of a substance, particularly a liquid, can be very useful because it's often easier to measure a liquid by volume than by mass. Suppose, for example, that you needed 1.55 g of ethyl alcohol. Rather than trying to weigh exactly the right amount, it would be much easier to look up the density of ethyl alcohol $\left(0.7893 \mathrm{~g} / \mathrm{mL}\right.$ at $\left.20^{\circ} \mathrm{C}\right)$ and measure the correct volume with a syringe.

$$
\begin{aligned}
& \text { Density }=\frac{\text { Mass }}{\text { Volume } \quad \text { so } \quad \text { Volume }=\frac{\text { Mass }}{\text { Density }}} \\
& \text { Volume }=\frac{1.55 \text { gf ethyl alcohol }}{0.7893 \frac{\mathrm{~g}}{\mathrm{~mL}}}=1.96 \mathrm{~mL} \text { ethyl alcohol }
\end{aligned}
$$

A precise amount of a liquid is easily measured with a syringe if the density of the liquid is known.


## Worked Example 1.2

What is the density of the element copper (in grams per cubic centimeter) if a sample weighing 324.5 g has a volume of $36.2 \mathrm{~cm}^{3}$ ?

## Solution

Density is mass divided by volume:

$$
\text { Density }=\frac{\text { Mass }}{\text { Volume }}=\frac{324.5 \mathrm{~g}}{36.2 \mathrm{~cm}^{3}}=8.96 \mathrm{~g} / \mathrm{cm}^{3}
$$

## Worked Example 1.3

What is the volume (in cubic centimeters) of 454 g of gold?

## SOlUTION

Since density is defined as mass divided by volume, volume is mass divided by density:

$$
\text { Volume }=\frac{454 \mathrm{~g} \text { gold }}{19.31 \mathrm{~g} / \mathrm{cm}^{3}}=23.5 \mathrm{~cm}^{3} \text { gold }
$$

- PROBLEM 1.9 What is the density of glass (in grams per cubic centimeter) if a sample weighing 27.43 g has a volume of $12.40 \mathrm{~cm}^{3}$ ?
- PROBLEM 1.10 Chloroform, a substance once used as an anesthetic, has a density of $1.483 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$. How many milliliters would you use if you needed 9.37 g ?


### 1.11 Accuracy, Precision, and Significant Figures in Measurement

Any measurement is only as good as the skill of the person doing the work and the reliability of the equipment being used. You've probably noticed, for instance, that you get slightly different readings when you weigh yourself on a bathroom scale and on a scale at the doctor's office, so there's always some uncertainty about your real weight. The same is true in chemistry-there is always some uncertainty in the value of a measurement.

In talking about the degree of uncertainty in a measurement, we use the words accuracy and precision. Although most of us use the words interchangeably in daily life, there's actually an important distinction between them. Accuracy refers to how close to the true value a given measurement is, whereas precision refers to how well a number of independent measurements agree with one another. To see the difference, imagine that you weigh a tennis ball whose true mass is 54.44178 g . Assume that you take three independent measurements on each of three different types of balance to obtain the data shown in the following table.

| Measurement \# | Bathroom Scale | Lab Balance | Analytical Balance |
| :--- | :--- | :--- | :--- |
| 1 | 0.0 kg | 54.4 g | 54.4419 g |
| 2 | 0.0 kg | 54.7 g | 54.4417 g |
| 3 | 0.1 kg | 54.1 g | 54.4417 g |
| (average) | $(0.03 \mathrm{~kg})$ | $(54.4 \mathrm{~g})$ | $(54.4418 \mathrm{~g})$ |

If you use a bathroom scale, your measurement (average $=0.03 \mathrm{~kg}$ ) is neither accurate nor precise. Its accuracy is poor because it measures to only one digit that is far from the true value, and its precision is poor because any two measurements may differ substantially. If you now weigh the ball on an inexpensive single-pan balance, the value you get (average $=54.4 \mathrm{~g}$ ) has three digits and is fairly accurate, but it is still not very precise because the three readings vary from 54.1 g to 54.7 g , perhaps due to air movements in the room or to a sticky mechanism. Finally, if you weigh the ball on an expensive analytical balance like those found in research laboratories, your measurement (average $=54.4418 \mathrm{~g}$ ) is both precise and accurate. It's accurate because the measurement is very close to the true value, and it's precise because it has six digits that vary little from one reading to another.

To indicate the uncertainty in a measurement, the value you record should use all the digits you are sure of, plus one additional digit that you estimate. In reading a mercury thermometer that has a mark for each degree, for example, you could be certain about the digits of the nearest mark-say $25^{\circ} \mathrm{C}$-but you would have to estimate between two marks-say $25.3^{\circ} \mathrm{C}$.

The total number of digits in a measurement is called the number of significant figures. For example, the mass of the tennis ball as determined on the single-pan balance ( 54.4 g ) has three significant figures, whereas the mass determined on the analytical balance ( 54.4418 g ) has six significant figures. All digits but the last are certain; the final digit is only a best guess, which we generally assume to have an error of plus or minus one $( \pm 1)$.

Finding the number of significant figures in a measurement is usually easy but can be troublesome if zeros are present. Look at the following four quantities:
4.803 cm Four significant figures: 4, 8, 0, 3
0.00661 g Three significant figures: 6, 6, 1
$55.220 \mathrm{~K} \quad$ Five significant figures: 5, 5, 2, 2, 0
$34,200 \mathrm{~m} \quad$ Anywhere from three (3, 4, 2) to five (3, 4, 2, 0, 0) significant figures

Charles J. Guare, "Error, Precision and Uncertainty," J. Chem. Educ., Vol. 68, 1991, 649-652.

Thichard S. Treptow, "Precision and Accuracy in Measurements: A Tale of Four Graduated Cylinders," J. Chem. Educ., Vol. 75, 1998, 992-995.


- This tennis ball has a mass of about 54 g .

VSignificant figures tend to be abstract to students until they realize that significant figures are a shortcut to expressing the limitations of laboratory measurements.

Arden P. Zipp, "A Simple but Effective Demonstration for Illustrating Significant Figure Rules When Making Measurements and Doing Calculations," J. Chem. Educ., Vol. 69, 1992, 291.

Ben Ruekberg, "A Joke Based on Significant Figures," J. Chem. Educ., Vol. 71, 1994, 306.


Kenton B. Abel and William M. Hemmerlin, "Significant Figures," J. Chem. Educ., Vol. 67, 1990, 213.
H. Graden Kirksey and Paul Krause, "Significant Figures, A Classroom Demonstration," J. Chem. Educ., Vol. 69, 1992, 497-498.

Only measured quantities may contain a measurement error, which limits the number of significant figures. In addition to counted objects ( 7 days $=$ 1 week), numbers related by definition ( 1 in $=2.54 \mathrm{~cm}$ ) are exact numbers with an infinite number of significant figures.

© How many students are in this class, $32.9,33$, or 33.1 ?

The answer given to a series of calculations involving measured quantities is limited by the least precise measurement.

The following rules cover the different situations that can arise:

1. Zeros in the middle of a number are like any other digit; they are always significant. Thus, 4.803 cm has four significant figures.
2. Zeros at the beginning of a number are not significant; they act only to locate the decimal point. Thus, 0.00661 g has three significant figures. (Note that 0.00661 g can be rewritten as $6.61 \times 10^{-3} \mathrm{~g}$ or as 6.61 mg .)
3. Zeros at the end of a number and after the decimal point are always significant. The assumption is that these zeros would not be shown unless they were significant. Thus, 55.220 K has five significant figures. (If the value were known to only four significant figures, we would write 55.22 K .)
4. Zeros at the end of a number and before the decimal point may or may not be significant. We can't tell whether they are part of the measurement or whether they only locate the decimal point. Thus, $34,200 \mathrm{~m}$ may have three, four, or five significant figures. Often, however, a little common sense is helpful. A temperature reading of $20^{\circ} \mathrm{C}$ probably has two significant figures rather than one, since one significant figure would imply a temperature anywhere from $10-30^{\circ} \mathrm{C}$ and would be of little use. Similarly, a volume given as 300 mL probably has three significant figures. On the other hand, a figure of $93,000,000 \mathrm{mi}$ for the distance between the earth and the sun probably has only two or three significant figures.

The fourth rule shows why it's helpful to write numbers in scientific notation rather than ordinary notation. Doing so makes it possible to indicate the number of significant figures. Thus, writing the number 34,200 as $3.42 \times 10^{4}$ indicates three significant figures, but writing it as $3.4200 \times 10^{4}$ indicates five significant figures.

One further point about significant figures: Certain numbers, such as those obtained when counting objects, are exact and have an effectively infinite number of significant figures. For example, a week has exactly 7 days, not 6.9 or 7.0 or 7.1 , and a foot has exactly 12 in., not 11.9 or 12.0 or 12.1 . In addition, the power of 10 used in scientific notation is an exact number. That is, the number $10^{3}$ is exact, but the number $1 \times 10^{3}$ has one significant figure.

## Worked Example 1.4

How many significant figures does each of the following measurements have?
(a) 0.036653 m
(b) $7.2100 \times 10^{-3} \mathrm{~g}$
(c) $72,100 \mathrm{~km}$
(d) $\$ 25.03$

## Solution

(a) 5 (by rule 2 )
(b) 5 (by rule 3)
(c) 3,4 , or 5 (by rule 4 )
(d) $\$ 25.03$ is an exact number

- PROBLEM 1.11 A 1.000 mL sample of acetone, a common solvent used as a paint remover, was placed in a small bottle whose mass was known to be 38.0015 g . The following values were obtained when the acetone-filled bottle was weighed: 38.7798 g , 38.7795 g , and 38.7801 g . How would you characterize the precision and accuracy of these measurements if the actual mass of the acetone was 0.7791 g ?
- PROBLEM 1.12 How many significant figures does each of the following quantities have? Explain your answers.
(a) 76.600 kg
(b) $4.50200 \times 10^{3} \mathrm{~g}$
(c) 3000 nm
(d) 0.00300 mL
(e) 18 students
(f) $3 \times 10^{-5} \mathrm{~g}$
(g) 47.60 mL
(h) 2070 mi


### 1.12 | Rounding Numbers

It often happens, particularly when doing arithmetic on a pocket calculator, that a quantity appears to have more significant figures than are really justified. For
example, you might calculate the gas mileage of your car by finding that it takes 11.70 gallons of gasoline to drive 278 miles:

$$
\text { Mileage }=\frac{\text { Miles }}{\text { Gallons }}=\frac{278 \mathrm{mi}}{11.70 \mathrm{gal}}=23.760684 \mathrm{mi} / \mathrm{gal}(\mathrm{mpg})
$$

Although the answer on the pocket calculator has eight digits, your measurement is really not as precise as it appears. In fact, your answer is precise to only three significant figures and should be rounded off to $23.8 \mathrm{mi} / \mathrm{gal}$ by removing nonsignificant figures.

How do you decide how many figures to keep and how many to ignore? The full answer to this question involves a mathematical treatment of the data known as error analysis. For most purposes, though, a simplified procedure using just two rules is sufficient. These rules give only an approximate value of the actual error, but that approximation is often good enough:

1. In carrying out a multiplication or division, the answer can't have more significant figures than either of the original numbers. If you think about it, this rule is just common sense: If you don't know the number of miles you drove to better than three significant figures ( 278 could mean 277,278 , or 279 ), you certainly can't calculate your mileage to more than the same number of significant figures.

2. In carrying out an addition or subtraction, the answer can't have more digits to the right of the decimal point than either of the original numbers. For example, if you have 3.18 L of water and you add 0.01315 L more, you now have 3.19 L . Again, this rule is just common sense. If you don't know the volume you started with past the second decimal place (it could be 3.17, 3.18, or 3.19), you can't know the total of the combined volumes past the same decimal place.

$$
\begin{array}{r}
3.18 ? ? ? \\
+0.01315 \longleftarrow \text { Ends two places past decimal point } \\
\hline 3.19 ? ? ? \\
\hline
\end{array}
$$

Once you decide how many digits to retain for your answer, the rules for rounding off numbers are as follows:

1. If the first digit you remove is less than 5 , round down by dropping it and all following digits. Thus, 5.664525 becomes 5.66 when rounded to three significant figures because the first of the dropped digits (4) is less than 5 .
2. If the first digit you remove is 6 or greater, round up by adding 1 to the digit on the left. Thus, 5.664525 becomes 5.7 when rounded to two significant figures because the first of the dropped digits (6) is greater than 5 .
3. If the first digit you remove is 5 and there are more nonzero digits following, round up. Thus, 5.664525 becomes 5.665 when rounded to four significant figures, because there are nonzero digits $(2,5)$ after the 5 .
4. If the digit you remove is a 5 with nothing following, round down. Thus, 5.664525 becomes 5.66452 when rounded to six significant figures, because there is nothing after the 5 .


A Calculators often display more figures than are justified by the precision of the data.

VStudents can avoid round-off errors by always using one more significant figure for constants or molar masses than required by measured data and rounding off only the final answer and not intermediate ones.

Significant Figures Calculations activity; Significant Figures activity


A These runners have to convert from laps to meters to find out how far they have run.

## Dimensional analysis is also

 known as unit analysis or the factor label method.
## Worked Example 1.5

If it takes 9.25 hours to fly from London, England, to Chicago, a distance of 3952 miles, what is the average speed of the airplane in miles per hour?

## Solution

First, set up an equation dividing the number of miles flown by the number of hours:

$$
\text { Average speed }=\frac{3952 \mathrm{mi}}{9.25 \mathrm{~h}}=427.24324 \mathrm{mi} / \mathrm{h}
$$

Next, decide how many significant figures should be in your answer. Since the problem involves a division, and since one of the quantities you started with ( 9.25 h ) has only three significant figures, the answer must also have three significant figures. Finally, round off your answer. Since the first digit to be dropped (2) is less than 5 , the answer 427.24324 must be rounded off to $427 \mathrm{mi} / \mathrm{h}$.

In doing this or any other calculation, use all figures, significant or not, and then round off the final answer. Don't round off at any intermediate steps.

- PROBLEM 1.13 Round off each of the following quantities to the number of significant figures indicated in parentheses:
(a) 3.774499 L (4)
(b) $255.0974 \mathrm{~K}(3)$
(c) 55.265 kg (4)
- PROBLEM 1.14 Carry out the following calculations, expressing each result with the correct number of significant figures:
(a) $24.567 \mathrm{~g}+0.04478 \mathrm{~g}=? \mathrm{~g}$
(b) $4.6742 \mathrm{~g} \div 0.00371 \mathrm{~L}=? \mathrm{~g} / \mathrm{L}$
(c) $0.378 \mathrm{~mL}+42.3 \mathrm{~mL}-1.5833 \mathrm{~mL}=$ ? mL
- KEY CONCEPT PROBLEM 1.15 What is the temperature reading on the following Celsius thermometer? How many significant figures do you have in your answer?



### 1.13 Calculations: Converting from One Unit to Another

Many scientific activities involve numerical calculations-measuring, weighing, preparing solutions, and so forth-and it's often necessary to convert a quantity from one unit to another. Converting between units isn't difficult; we all do it every day. If you run 7.5 laps around a 200 meter track, for instance, you have to convert between the distance unit lap and the distance unit meter to find that you have run 1500 m ( 7.5 laps times 200 meters/lap). Converting from one scientific unit to another is just as easy.

$$
7.5 \text { laps } \times \frac{200 \text { meters }}{1 \text { lap }}=1500 \text { meters }
$$

The simplest way to carry out calculations that involve different units is to use the dimensional-analysis method. In this method, a quantity described in one unit is converted into an equivalent quantity with a different unit by using a conversion factor to express the relationship between units:

[^0]As an example, we know from Section 1.7 that 1 meter equals 39.37 inches. Writing this relationship as a fraction restates it in the form of a conversion factor, either meters per inch or inches per meter:

| CONVERSION FACTORS <br> BETWEEN METERS <br> AND INCHES |
| :--- |
| $\frac{1 \mathrm{~m}}{39.37 \mathrm{in} .}$ equals $\frac{39.37 \mathrm{in} .}{1 \mathrm{~m}}$ equals 1 |

Note that this and all other conversion factors are numerically equal to 1 because the value of the quantity above the division line (the numerator) is equal to the value of the quantity below the division line (the denominator). Thus, multiplying by a conversion factor is equivalent to multiplying by 1 and so does not change the value of the quantity.

$$
\begin{aligned}
& \text { These two quantities } \\
& \text { are equivalent } \unlhd \frac{1 \mathrm{~m}}{3937 \mathrm{in}} \text { or } \frac{39.37 \mathrm{in} .}{1 \mathrm{~m}}
\end{aligned} \begin{aligned}
& \text { These two quantities }
\end{aligned}
$$

The key to the dimensional-analysis method of problem solving is that units are treated like numbers and can thus be multiplied and divided (though not added or subtracted) just as numbers can. The idea when solving a problem is to set up an equation so that unwanted units cancel, leaving only the desired units. Usually it's best to start by writing what you know and then manipulating that known quantity. For example, if you know your height is 69.5 in . and want to find it in meters, you can write down the height in inches and set up an equation multiplying the height by the conversion factor in meters per inch:

$$
\text { Starting quantity } 69.5 \mathrm{in} . \times \frac{1 \mathrm{~m}}{39.37 \mathrm{iK} .}=1.77 \mathrm{~m}
$$

The unit "in." cancels from the left side of the equation because it appears both above and below the division line, and the only unit that remains is " m ."

The dimensional-analysis method gives the right answer only if the equation is set up so that the unwanted units cancel. If the equation is set up in any other way, the units won't cancel properly, and you won't get the right answer. Thus, if you were to multiply your height in inches by the incorrect conversion factor inches per meter, you would end up with an incorrect answer expressed in meaningless units:

$$
? ? \quad 69.5 \mathrm{in} . \times \frac{39.37 \mathrm{in} .}{1 \mathrm{~m}}=2,740 \mathrm{in}^{2} / \mathrm{m} \quad ? ?
$$

The main drawback to using the dimensional-analysis method is that it's easy to get the right answer without really understanding what you're doing. It's therefore best after solving a problem to think through a rough estimate, or "ballpark" solution, as a check on your work. If your ballpark check isn't close to the detailed solution, there's a misunderstanding somewhere, and you should think the problem through again. Even if you don't make an estimate, it's important to be sure that your calculated answer makes sense. If, for example, you were trying to calculate the volume of a human cell and you came up with the answer $5.3 \mathrm{~cm}^{3}$, you should realize that such an answer couldn't possibly be right; cells are too tiny to be distinguished with the naked eye, but a volume of $5.3 \mathrm{~cm}^{3}$ is about the size of a walnut.

The dimensional-analysis method and the use of ballpark checks are techniques that will help you solve problems of many kinds, not just unit conversions. Problems sometimes seem complicated, but you can usually sort out the complications by analyzing the problem properly:

- Identify the information given, including units.
- Identify the information needed in the answer, including units.

$\square$Mathematical problem solving is more difficult for most students than understanding chemistry concepts. Knowing the goal of a series of calculations and where to start is not trivial for many students. Students need to be taught a system, such as writing the units of the desired answer on the right side of the paper, writing a measurement or conversion factor containing the same units on the left, then using appropriate relationships to cancel all but the desired units.

Th Donald DeLorenzo, "Expanded Dimensional Analysis: A Blending of English and Math," J. Chem. Educ., Vol. 71, 1994, 789-791.

(1)Brian N. Akers, "Appalachian Trail Problems," J. Chem. Educ., Vol. 75, 1998, 1571-1572.


A What is the volume of a red blood cell?

Single-Step Unit
Conversion activity

Multiple-Step Unit Conversion activity

- Find a relationship between the known information and unknown answer, and plan a strategy for getting from one to the other.
- Solve the problem.
- Make a rough estimate to be sure your calculated answer is reasonable.

Examples 1.6-1.8 show how to devise strategies and use ballpark answers. To conserve space, we'll use this approach routinely in only the next few chapters, but you should make it a standard part of your problem solving.

## Worked Example 1.6

Many of the German autobahns have no speed limit, and it's not unusual to see a Porsche or Mercedes flash by at $190 \mathrm{~km} / \mathrm{h}$. What is this speed in miles per hour?

## Strategy

The known information is the speed in kilometers per hour; the unknown is the speed in miles per hour. Find the appropriate conversion factor, and use the dimensionalanalysis method to set up an equation so the km units cancel.

## Solution

$$
\frac{190 \mathrm{~km}}{1 \mathrm{~h}} \times \frac{0.6214 \mathrm{mi}}{1 \mathrm{~km}}=118 \frac{\mathrm{mi}}{\mathrm{~h}}
$$

Note that we're not completely sure of the number of significant figures in the answer because the starting value of $190 \mathrm{~km} / \mathrm{h}$ could have two or three significant figures. Three significant figures is more reasonable than two, however, since an automobile speedometer that couldn't distinguish between $180 \mathrm{~km} / \mathrm{h}$ and $200 \mathrm{~km} / \mathrm{h}$ wouldn't be of much use.
$\checkmark$ BALLPARK CHECK Common sense says that the answer is probably large, perhaps over $100 \mathrm{mi} / \mathrm{h}$. A better estimate is to realize that, since $1 \mathrm{~km}=0.6214 \mathrm{mi}$, a mile is larger than a kilometer and it takes only about $2 / 3$ as many miles as kilometers to measure the same distance. Thus, 190 km is about 120 mi , and $190 \mathrm{~km} / \mathrm{h}$ is about $120 \mathrm{mi} / \mathrm{h}$. The ballpark check agrees with the solution.

## Worked Example 1.7

The Mercedes that just went by at $190 \mathrm{~km} / \mathrm{h}$ is using gasoline at a rate of 16 L per 100 km . What does this correspond to in miles per gallon?

## Strategy

We are given a gasoline mileage in liters per kilometer (or kilometers per liter), and we need to find the mileage in miles per gallon. Thus, two conversions are necessary, one from kilometers to miles and one from liters to gallons. It's best to do multiple conversions one step at a time until you get used to working with them. First convert the distance from kilometers to miles and the fuel from liters to gallons, and then divide the distance by the amount of fuel to find the mileage.

## Solution

$$
\begin{aligned}
100 \mathrm{~km} \times \frac{0.6214 \mathrm{mi}}{1 \mathrm{~km}} & =62.14 \mathrm{mi} \quad 16 \mathrm{~L} \times \frac{1 \mathrm{gal}}{3.78 \measuredangle}=4.2328 \mathrm{gal} \\
\frac{62.14 \mathrm{mi}}{4.2328 \mathrm{gal}} & =14.68 \frac{\mathrm{mi}}{\mathrm{gal}} \quad \text { Round off to } 15 \mathrm{mi} / \mathrm{gal}
\end{aligned}
$$

Note that extra digits are carried through the intermediate calculations, and only the final answer is rounded off.

When you become more confident in working multiple conversion problems, you can set up one large equation in which all unwanted units cancel:

$$
\frac{100 \mathrm{~km}}{16 \mathrm{~L}} \times \frac{3.78 \mathrm{~K}}{1 \mathrm{gal}} \times \frac{0.6214 \mathrm{mi}}{1 \mathrm{~km}}=14.68 \frac{\mathrm{mi}}{\mathrm{gal}} \quad \text { Round off to } 15 \mathrm{mi} / \mathrm{gal}
$$

$\checkmark$ Ballpark Check The mileage is probably low, perhaps in the range of 10 to 15 $\mathrm{mi} / \mathrm{gal}$. This is a difficult problem to estimate, however, because it requires several different conversions. It's therefore best to think the problem through one step at a time, writing down the intermediate estimates:

- A distance of 100 km per 16 L is approximately $7 \mathrm{~km} / \mathrm{L}$.
- Since 1 km is about $0.6 \mathrm{mi}, 7 \mathrm{~km} / \mathrm{L}$ is about $4 \mathrm{mi} / \mathrm{L}$.
- Since 1 L is approximately 1 qt , or $1 / 4 \mathrm{gal}, 4 \mathrm{mi} / \mathrm{L}$ is about $16 \mathrm{mi} / \mathrm{gal}$.

The ballpark check agrees with the solution.

## Worked Example 1.8

The volcanic explosion that destroyed the Indonesian island of Krakatau on August 27,1883 , released an estimated 4.3 cubic miles $\left(\mathrm{mi}^{3}\right)$ of debris into the atmosphere and affected global weather for years. In SI units, how many cubic meters $\left(\mathrm{m}^{3}\right)$ of debris were released?

## Strategy

We are given a volume in cubic miles and need to convert to cubic meters. It's probably simplest to convert first from cubic miles to cubic kilometers and then from cubic kilometers to cubic meters.

## Solution

$$
\begin{array}{r}
4.3 \mathrm{mi}^{3} \times\left(\frac{1 \mathrm{~km}}{0.6214 \mathrm{mit}}\right)^{3}=17.92 \mathrm{~km}^{3} \\
\begin{aligned}
17.92 \mathrm{~km}^{3} \times\left(\frac{1000 \mathrm{~m}}{1 \mathrm{~km}}\right)^{3} & =1.792 \times 10^{10} \mathrm{~m}^{3} \\
& =1.8 \times 10^{10} \mathrm{~m}^{3} \quad \text { Rounded off }
\end{aligned}
\end{array}
$$

$\checkmark$ Ballpark Check One meter is much less than 1 mile, so it takes a large number of cubic meters to equal $1 \mathrm{mi}^{3}$, and the answer is going to be very large. In fact, $1 \mathrm{mi}^{3}$ is the volume of a cube 1 mi on each edge, and $1 \mathrm{~km}^{3}$ is the volume of a cube 1 km on each edge. Since a kilometer is about $0.6 \mathrm{mi}, 1 \mathrm{~km}^{3}$ is about $(0.6)^{3}=0.2$ times as large as $1 \mathrm{mi}^{3}$. Thus, each cubic mile contains about $5 \mathrm{~km}^{3}$, and $4.3 \mathrm{mi}^{3}$ contains about $20 \mathrm{~km}^{3}$. Each cubic kilometer, in turn, contains $(1000 \mathrm{~m})^{3}=10^{9} \mathrm{~m}^{3}$. Thus, the volume of debris from the Krakatau explosion was about $20 \times 10^{9} \mathrm{~m}^{3}$, or $2 \times 10^{10} \mathrm{~m}^{3}$. The ballpark check agrees with the solution.

- PROBLEM 1.16 Calculate answers to the following problems, and check your solutions by making ballpark estimates.
(a) The melting point of gold is $1064^{\circ} \mathrm{C}$. What is this temperature in degrees Fahrenheit?
(b) How large, in cubic centimeters, is the volume of a red blood cell if the cell has a circular shape with a diameter of $6 \times 10^{-6} \mathrm{~m}$ and a height of $2 \times 10^{-6} \mathrm{~m}$ ?

PROBLEM 1.17 Gemstones are weighed in carats, with 1 carat $=200 \mathrm{mg}$ (exactly). What is the mass in grams of the Hope Diamond, the world's largest blue diamond at 44.4 carats? What is this mass in ounces?

## Interlude Chemicals, Toxicity, and Risk

 ife is not risk-free-we all take many risks each day, often without even thinking about it. We may decide to ride a bike rather than drive, even though the likelihood per mile of being killed on a bicycle is ten times greater than in a car. We may decide to smoke cigarettes, even though smoking kills more than 400,000 people each year in the U.S.

What about risks from "chemicals"? News reports sometimes make it seem that our food is covered with pesticides and filled with dangerous additives, that our land is polluted by toxic waste dumps, and that our medicines are unsafe. How bad are the risks from chemicals, and how are the risks evaluated?

First, it's important to realize that everything, including your own body, is made of chemicals. There is no such thing as a "chem-ical-free" food, cosmetic, cleanser, or anything else. Second, there is no meaningful distinction between a "natural" substance and a "synthetic" one; a chemical is a chemical. Many naturally occurring substances-strychnine, for example-are extraordinarily toxic, and many synthetic substances-polyethylene, for exam-ple-are harmless. leukemia?

Risk evaluation of chemicals is carried out by exposing test
animals, usually mice or rats, to a chemical and then monitor-
身 ing for signs of harm. To limit the expense and time needed for testing, the amounts administered are hundreds or thousands of times larger than those a person might normally encounter. The acute chemical toxicity (as opposed to longterm toxicity) observed in animal tests is reported as an $L D_{50}$ value, the amount of a substance per kilogram of body weight that is a lethal dose for $50 \%$ of the test animals. $\mathrm{LD}_{50}$ values of various substances are shown in Table 1.7.

| TABLE 1.7 | Some $\mathrm{LD}_{50}$ Values |  |  |
| :--- | :--- | :--- | :---: |
| Substance | $\mathbf{L D}_{\mathbf{5 0}}(\mathbf{g} / \mathbf{k g})$ | Substance | $\mathbf{L D}_{\mathbf{5 0}}(\mathbf{g} / \mathbf{k g})$ |
| Strychnine | 0.005 | Iron(II) sulfate | 1.5 |
| Arsenic trioxide | 0.015 | Chloroform | 3.2 |
| DDT | 0.115 | Ethyl alcohol | 10.6 |
| Aspirin | 1.1 | Sodium cyclamate | 17 |

Even with an $\mathrm{LD}_{50}$ value established in test animals, the risk of human exposure to a given substance is still hard to assess. If a substance is harmful to rats, is it necessarily harmful to humans? How can a large dose for a small animal be translated into a small dose for a large human? All substances are toxic to some organisms to some extent, and the difference between help and harm is often a matter of degree. Vitamin A, for example, is necessary for vision, yet it can cause cancer at high doses. Arsenic trioxide is the most classic of poisons, yet recent work has shown it to be effective at inducing remissions in some types of leukemia. It is, in fact, sold for drug use under the name Trisenox. Furthermore, how we evaluate risk is strongly influenced by familiarity. Many foods contain natural ingredients far more toxic than synthetic additives or pesticide residues, but the ingredients are ignored because the foods are familiar.

All decisions involve tradeoffs. Does the benefit of a pesticide that will increase the availability of food outweigh a possible health risk to one person in 1 million? Do the beneficial effects of a new drug outweigh a potentially dangerous side effect in a small number of users? The answers aren't always obvious, but we should try to keep our responses on a factual level rather than an emotional one.

- PROBLEM 1.18 What is an $\mathrm{LD}_{50}$ value?

PROBLEM 1.19 Table salt (sodium chloride) has an $\mathrm{LD}_{50}$ of $4 \mathrm{~g} / \mathrm{kg}$ in rats. Assuming that rats and humans have the same $\mathrm{LD}_{50}$, how much salt would a typical 155 lb person have to consume to have a $50 \%$ chance of dying?

## Summary

Chemistry is the study of the composition, properties, and transformations of matter. These studies are best approached by posing questions, conducting experiments, and devising theories to interpret the experimental results.

All matter is formed from one or more of 114 presently known elements-fundamental substances that can't be chemically broken down. Elements are symbolized by one- or two-letter abbreviations and are organized into a periodic table with groups (columns) and periods (rows). Elements in the same group of the periodic table show similar chemical behavior. The two larger groups on the left and the six larger groups on the right of the table are called the main groups; the ten smaller ones in the middle of the table are called the transition metal groups; and the fourteen shown separately at the bottom of the table are called the inner transition metal groups. Elements are classified as metals, nonmetals, or semimetals.

The characteristics, or properties, that are used to describe matter can be classified in several ways. Physical properties are those that can be determined without changing the chemical composition of the sample, whereas chemical properties are those that do involve a chemical change in the sample. Intensive properties are those whose
values do not depend on the size of the sample, whereas extensive properties are those whose values do depend on sample size.

Accurate measurement is crucial to scientific experimentation. The units used are those of the Système Internationale (SI units). There are seven fundamental SI units, together with other derived units: Mass, the amount of matter an object contains, is measured in kilograms (kg); length is measured in meters (m); temperature is measured in kelvins (K); and volume is measured in cubic meters $\left(\mathbf{m}^{\mathbf{3}}\right)$. The more familiar metric liter ( $\mathbf{L}$ ) and milliliter ( $\mathbf{m L}$ ) are also still used for measuring volume, and the Celsius degree $\left({ }^{\circ} \mathrm{C}\right)$ is still used for measuring temperature. Density is an intensive physical property that relates mass to volume.

Because many experiments involve numerical calculations, it's often necessary to manipulate and convert different units of measure. The simplest way to carry out such conversions is to use the dimensional-analysis method, in which an equation is set up so that unwanted units cancel and only the desired units remain. It's also important when measuring physical quantities or carrying out calculations to indicate the precision of the measurement by rounding off the result to the correct number of significant figures.

## Key Words

## accuracy 19

alkali metal 7
alkaline earth metal 8
Celsius degree ( ${ }^{\circ} \mathrm{C}$ ) $\quad 13$
centimeter (cm) 13
chemical property 7
chemistry 2
conversion factor 22
cubic centimeter ( $\mathrm{cm}^{3}$ )
15
density 16
dimensional analysis
22
element 3
extensive property 7
gram (g) 12
group 5
halogen 8
inner transition metal
group 7
intensive property 7
kelvin (K) 13
kilogram (kg) 12
liter (L) 15
main group 7
mass 12
matter 12
metal 9
meter (m) 13
milligram (mg) 12
milliliter (mL) 15
millimeter (mm) 13
nanometer ( $\mathbf{n m}$ ) 13
noble gas 8
nonmetal 9
period 5
periodic table 5
physical property 7
picometer (pm) 13
precision 19
property 7
rounding off 21
scientific notation 11
semimetal 10
SI unit 10
significant figure 19
theory 3
transition metal
group 7

## Key Concept Summary



## Understanding Key Concepts

Exercises at the end of each chapter begin with a section called "Understanding Key Concepts." The problems in this section are visual rather than numerical and are intended to probe your understanding rather than your facility with numbers and formulas. Answers to even-numbered problems can be found at the end of the book following the appendixes. Problems 1.1-1.19 appear within the chapter.
1.20 Where on the following outline of a periodic table are the indicated elements or groups of elements?
(a) Alkali metals
(b) Halogens
(c) Alkaline earth metals
(d) Transition metals
(e) Hydrogen
(f) Helium

1.21 Where on the following outline of a periodic table does the dividing line between metals and nonmetals fall?
-

1.22 Is the element marked in red on the following periodic table likely to be a gas, a liquid, or a solid? What is the atomic number of the element in blue? Name at least one other element that is chemically similar to the element in green.


|  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

1.23 The radioactive element indicated on the following periodic table is used in smoke detectors. Identify it, give its atomic number, and tell what kind of group it's in.

1.24 Characterize each of the following dartboards according to the accuracy and precision of the results.

1.25 How many milliliters of water does the graduated cylinder in (a) contain, and how tall in centimeters is
 the paper clip in (b)? How many significant figures do you have in each answer?

(a)

(b)
1.26 Assume that you have two graduated cylinders, one with a capacity of 5 mL (a) and the other with a capacity of 50 mL (b). Draw a line in each, showing how much liquid you would add if you needed to measure 2.64 mL of water. Which cylinder will give the more accurate measurement? Explain.

1.27 The following cylinder contains three liquids that do not mix with one another: water (density $=1.0 \mathrm{~g} / \mathrm{mL}$ ), vegetable oil (density $=0.93 \mathrm{~g} / \mathrm{mL}$ ), and mercury (density $=13.5 \mathrm{~g} / \mathrm{mL}$ ). Which liquid is which?


## Additional Problems

The Additional Problems at the end of each chapter begin with sections that cover specific topics from the chapter. These problems are presented in pairs, with each even-numbered problem followed by an odd-numbered one requiring similar skills. These paired problems are followed by unpaired General Problems that draw on various parts of the chapter. Evennumbered problems are answered at the end of the book following the appendixes.

## Elements and the Periodic Table

1.28 How many elements are presently known? About how many occur naturally?
1.29 What are the rows called and what are the columns called in the periodic table?
1.30 How many groups are there in the periodic table? How are they labeled?
1.31 What common characteristics do elements within a group of the periodic table have?
1.32 Where in the periodic table are the main-group elements found? Where are the transition metal groups found?
1.33 Where in the periodic table are the metallic elements found? Where are the nonmetallic elements found?
1.34 What is a semimetal, and where in the periodic table are semimetals found?
1.35 List several general properties of the following:
(a) Alkali metals
(b) Noble gases
(c) Halogens
1.36 Without looking at a periodic table, list as many alkali metals as you can. (There are five common ones.)
1.37 Without looking at a periodic table, list as many alkaline earth metals as you can. (There are five common ones.)
1.38 Without looking at a periodic table, list as many halogens as you can. (There are four common ones.)
1.39 Without looking at a periodic table, list as many noble gases as you can. (There are six common ones.)
1.40 What are the symbols for the following elements?
(a) Gadolinium (used in color TV screens)
(b) Germanium (used in semiconductors)
(c) Technetium (used in biomedical imaging)
(d) Arsenic (used in pesticides)
1.41 What are the symbols for the following elements?
(a) Cadmium (used in rechargeable batteries)
(b) Iridium (used for hardening alloys)
(c) Beryllium (used in the space shuttle)
(d) Tungsten (used in lightbulbs)
1.42 Give the names corresponding to the following symbols:
(a) Te
(b) Re
(c) Be
(d) Ar
(e) Pu
1.43 Give the names corresponding to the following symbols:
(a) B
(b) Rh
(c) Cf
(d) Os
(e) Ga
1.44 What is wrong with each of the following statements?
(a) The symbol for tin is Ti.
(b) The symbol for manganese is Mg .
(c) The symbol for potassium is Po.
(d) The symbol for helium is HE.
1.45 What is wrong with each of the following statements?
(a) The symbol for carbon is ca.
(b) The symbol for sodium is So.
(c) The symbol for nitrogen is Ni .
(d) The symbol for chlorine is Cr .

## Units and Significant Figures

1.46 What is the difference between mass and weight?
1.47 What is the difference between a derived SI unit and a fundamental SI unit? Give an example of each.
1.48 What SI units are used for measuring the following quantities?
(a) Mass
(b) Length
(c) Temperature
(d) Volume
1.49 What SI prefixes correspond to the following multipliers?
(a) $10^{3}$
(b) $10^{-6}$
(c) $10^{9}$
(d) $10^{-12}$
(e) $10^{-2}$
1.50 Which is larger, a Fahrenheit degree or a Celsius degree? By how much?
1.51 What is the difference between a kelvin and a Celsius degree?
1.52 What is the difference between a cubic decimeter (SI) and a liter (metric)?
1.53 What is the difference between a cubic centimeter (SI) and a milliliter (metric)?
1.54 Which of the following statements use exact numbers?
(a) $1 \mathrm{ft}=12 \mathrm{in}$.
(b) The height of Mt. Everest is $29,035 \mathrm{ft}$.
(c) The world record for the 1 mile run, set by Morocco's Hicham el Guerrouj in 1999, is 3 minutes, 43.13 seconds.
1.55 What is the difference in mass between a nickel that weighs 4.8 g and a nickel that weighs 4.8673 g ?
1.56 Bottles of wine sometimes carry the notation "Volume $=75 \mathrm{cL}$. ." What does the unit cL mean?
1.57 What do the following abbreviations stand for?
(a) dL
(b) dm
(c) $\mu \mathrm{m}$
(d) nL
1.58 How many picograms are in 1 mg ? In 35 ng ?
1.59 How many microliters are in 1 L ? In 20 mL ?
1.60 Carry out the following conversions:
(a) $5 \mathrm{pm}=$ $\qquad$ $\mathrm{cm}=$ $\qquad$ nm
(b) $8.5 \mathrm{~cm}^{3}=$ $\qquad$ $\mathrm{m}^{3}=$ $\qquad$ $\mathrm{mm}^{3}$
(c) $65.2 \mathrm{mg}=\ldots \quad \mathrm{g}=\ldots \quad \mathrm{pg}$
1.61 Which is larger, and by approximately how much?
(a) A liter or a quart
(b) A mile or a kilometer
(c) A gram or an ounce
(d) A centimeter or an inch
1.62 How many significant figures are in each of the following measurements?
(a) 35.0445 g
(b) 59.0001 cm
(c) 0.03003 kg
(d) 0.00450 m
(e) $67,000 \mathrm{~m}^{2}$
(f) $3.8200 \times 10^{3} \mathrm{~L}$
1.63 How many significant figures are in each of the following measurements?
(a) $\$ 130.95$
(b) 2000.003 g
(c) 5 ft 3 in .
1.64 The Vehicle Assembly Building at the John F. Kennedy Space Center in Cape Canaveral, Florida, is the largest building in the world, with a volume of $3,666,500 \mathrm{~m}^{3}$. Express this volume in scientific notation.
1.65 The diameter of the earth at the equator is 7926.381 mi . Round off this quantity to four significant figures; to two significant figures. Express the answers in scientific notation.
1.66 Express the following measurements in scientific notation:
(a) 453.32 mg
(b) 0.0000421 mL
(c) $667,000 \mathrm{~g}$
1.67 Convert the following measurements from scientific notation to standard notation:
(a) $3.221 \times 10^{-3} \mathrm{~mm}$
(b) $8.940 \times 10^{5} \mathrm{~m}$
(c) $1.35082 \times 10^{-12} \mathrm{~m}^{3}$
(d) $6.4100 \times 10^{2} \mathrm{~km}$
1.68 Round off the following quantities to the number of significant figures indicated in parentheses:
(a) $35,670.06 \mathrm{~m}(4,6)$
(b) $68.507 \mathrm{~g}(2,3)$
(c) $4.995 \times 10^{3} \mathrm{~cm}(3)$
(d) $2.30985 \times 10^{-4} \mathrm{~kg}(5)$
1.69 Round off the following quantities to the number of significant figures indicated in parentheses:
(a) $7.0001 \mathrm{~kg}(4)$
(b) $1.605 \mathrm{~km}(3)$
(c) $13.2151 \mathrm{~g} / \mathrm{cm}^{3}(3)$
(d) $2,300,000.1$ (7)
1.70 Express the results of the following calculations with the correct number of significant figures:
(a) $4.884 \times 2.05$
(b) $94.61 \div 3.7$
(c) $3.7 \div 94.61$
(d) $5502.3+24+0.01$
(e) $86.3+1.42-0.09$
(f) $5.7 \times 2.31$
1.71 Express the results of the following calculations with the correct number of significant figures:
(a) $\frac{3.41-0.23}{5.233} \times 0.205$
(b) $\frac{5.556 \times 2.3}{4.223-0.08}$

## Unit Conversions

1.72 Carry out the following conversions:
(a) How many grams of meat are in a quarter-pound hamburger $(0.25 \mathrm{lb})$ ?
(b) How tall (in meters) is the Sears Tower in Chicago $(1454 \mathrm{ft})$ ?
(c) How large (in square meters) is the land area of Australia $\left(2,941,526 \mathrm{mi}^{2}\right)$ ?
1.73 Convert the following quantities into SI units with the correct number of significant figures:
(a) 5.4 in .
(b) 66.31 lb
(c) 0.5521 gal
(d) $65 \mathrm{mi} / \mathrm{h}$
(e) $978.3 \mathrm{yd}^{3}$
(f) $2.380 \mathrm{mi}^{2}$
1.74 The volume of water used for crop irrigation is measured in acre-feet, where 1 acre-foot is the amount of water needed to cover 1 acre of land to a depth of 1 ft .
(a) If there are 640 acres per square mile, how many cubic feet of water are in 1 acre-foot?
(b) How many acre-feet are in Lake Erie (total volume $\left.=116 \mathrm{mi}^{3}\right)$ ?
1.75 The height of a horse is usually measured in hands instead of in feet, where 1 hand equals $1 / 3 \mathrm{ft}$ (exactly).
(a) How tall (in centimeters) is a horse of 18.6 hands?
(b) What is the volume (in cubic meters) of a box measuring $6 \times 2.5 \times 15$ hands?
1.76 Amounts of substances dissolved in solution are often expressed as mass per unit volume. For example, normal human blood has a cholesterol concentration of about $200 \mathrm{mg} / 100 \mathrm{~mL}$. Express this concentration in the following units:
(a) $\mathrm{mg} / \mathrm{L}$
(b) $\mu \mathrm{g} / \mathrm{mL}$
(c) $g / L$
(d) $n g / \mu \mathrm{L}$
(e) How much total blood cholesterol (in grams) does a person have if the normal blood volume in the body is 5 L ?
1.77 Weights in England are commonly measured in stones, where 1 stone $=14 \mathrm{lb}$. What is the weight (in pounds) of a person who weighs 8.65 stones?
1.78 Among many alternative units that might be considered as a measure of time is the shake rather than the second. Based on the expression "faster than a shake of a lamb's tail," we'll define 1 shake as equal to $2.5 \times 10^{-4} \mathrm{~s}$. If a car is traveling at $55 \mathrm{mi} / \mathrm{h}$, what is its speed in $\mathrm{cm} /$ shake?
1.79 Administration of digitalis, a drug used to control atrial fibrillation in heart patients, must be carefully controlled because even a modest overdosage can be fatal. To take differences between patients into account, drug dosages are prescribed in terms of $\mathrm{mg} / \mathrm{kg}$ body weight. Thus, a child and an adult differ greatly in weight, but both receive the same dosage per kilogram of body weight. At a dosage of $20 \mu \mathrm{~g} / \mathrm{kg}$ body weight, how many milligrams of digitalis should a 160 lb patient receive?

## Temperature

1.80 The normal body temperature of a goat is $39.9^{\circ} \mathrm{C}$, and that of an Australian spiny anteater is $22.2^{\circ} \mathrm{C}$. Express these temperatures in degrees Fahrenheit.
1.81 Of the 90 or so naturally occurring elements, only four are liquid near room temperature: mercury melting point $=-38.87^{\circ} \mathrm{C}$ ), bromine (melting point $=-7.2^{\circ} \mathrm{C}$ ), cesium (melting point $=28.40^{\circ} \mathrm{C}$ ), and gallium (melting point $=29.78^{\circ} \mathrm{C}$. Convert these melting points to degrees Fahrenheit.
1.82 Tungsten, the element used to make filaments in lightbulbs, has a melting point of $6192^{\circ} \mathrm{F}$. Convert this temperature to degrees Celsius and to kelvins.
1.83 Suppose that your oven is calibrated in degrees Fahrenheit but a recipe calls for you to bake at $175^{\circ} \mathrm{C}$. What oven setting should you use?
1.84 Suppose you were dissatisfied with both Celsius and Fahrenheit units and wanted to design your own temperature scale based on ethyl alcohol (ethanol). On the Celsius scale, ethanol has a melting point of $-117.3^{\circ} \mathrm{C}$ and a boiling point of $78.5^{\circ} \mathrm{C}$, but on your new scale calibrated in units of degrees ethanol, ${ }^{\circ} \mathrm{E}$, you define ethanol to melt at $0^{\circ} \mathrm{E}$ and boil at $200^{\circ} \mathrm{E}$.
(a) How does your ethanol degree compare in size with a Celsius degree?
(b) How does an ethanol degree compare in size with a Fahrenheit degree?
(c) What are the melting and boiling points of water on the ethanol scale?
(d) What is normal human body temperature $\left(98.6^{\circ} \mathrm{F}\right)$ on the ethanol scale?
(e) If the outside thermometer reads $130^{\circ} \mathrm{E}$, how would you dress to go out?
1.85 Answer parts (a)-(d) of Problem 1.84 assuming that your new temperature scale is based on ammonia, $\mathrm{NH}_{3}$. On the Celsius scale, ammonia has a melting point of $-77.7^{\circ} \mathrm{C}$ and a boiling point of $-33.4^{\circ} \mathrm{C}$, but on your new scale calibrated in units of degrees ammonia, ${ }^{\circ} \mathrm{A}$, you define ammonia to melt at $0^{\circ} \mathrm{A}$ and boil at $100^{\circ} \mathrm{A}$.

## Density

1.86 Aspirin has a density of $1.40 \mathrm{~g} / \mathrm{cm}^{3}$. What is the volume (in cubic centimeters) of an aspirin tablet weighing 250 mg ? Of a tablet weighing 500 lb ?
1.87 Gaseous hydrogen has a density of $0.0899 \mathrm{~g} / \mathrm{L}$ at $0^{\circ} \mathrm{C}$, and gaseous chlorine has a density of $3.214 \mathrm{~g} / \mathrm{L}$ at the same temperature. How many liters of each would you need if you wanted 1.0078 g of hydrogen and 35.45 g of chlorine?
1.88 What is the density of lead (in $\mathrm{g} / \mathrm{cm}^{3}$ ) if a rectangular bar measuring 0.50 cm in height, 1.55 cm in width, and 25.00 cm in length has a mass of 220.9 g ?
1.89 What is the density of lithium metal (in $\mathrm{g} / \mathrm{cm}^{3}$ ) if a cylindrical wire with a diameter of 2.40 mm and a length of 15.0 cm has a mass of 0.3624 g ?
1.90 When an irregularly shaped chunk of silicon weighing 8.763 g was placed in a graduated cylinder containing 25.00 mL of water, the water level in the cylinder rose to 28.76 mL . What is the density of silicon in $\mathrm{g} / \mathrm{cm}^{3}$ ?
1.91 When the experiment outlined in Problem 1.90 was repeated using a chunk of sodium metal, rather than silicon, an explosion occurred. Was this due to a chemical property or a physical property of sodium?

## General Problems

1.92 Give the symbol for each of the following elements:
(a) Selenium (used in photocopiers)
(b) Rhenium (used for hardening alloys)
(c) Cobalt (used in magnets)
(d) Rhodium (used in catalytic converters)
1.93 Consider the as yet undiscovered elements with atomic numbers 115, 117, and 119.
(a) Which element is a halogen? Explain.
(b) Which element should have chemical properties similar to cesium?
(c) Is element 115 likely to be a metal or a nonmetal? What about element 117? Explain.
(d) Describe some of the properties you expect for element 119.
1.94 Sodium chloride has a melting point of 1074 K and a boiling point of 1686 K . Convert these temperatures to degrees Celsius and to degrees Fahrenheit.
1.95 The mercury in thermometers freezes at $-38.9^{\circ} \mathrm{C}$. What is this temperature in degrees Fahrenheit?
1.96 The density of chloroform, a widely used organic solvent, is $1.4832 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$. How many milliliters would you use if you wanted 112.5 g of chloroform?
1.97 The density of sulfuric acid, $\mathrm{H}_{2} \mathrm{SO}_{4}$, is $15.28 \mathrm{lb} / \mathrm{gal}$. What is the density of sulfuric acid in $\mathrm{g} / \mathrm{mL}$ ?
1.98 Sulfuric acid (Problem 1.97) is produced in a larger amount than any other chemical- $8.728 \times 10^{10} \mathrm{lb}$ in the year 2000. What is the volume of this amount in liters?
1.99 The caliber of a gun is expressed by measuring the diameter of the gun barrel in hundredths of an inch. A ". 22 " rifle, for example, has a barrel diameter of 0.22 in. What is the barrel diameter of a .22 rifle in millimeters?
1.100 Answer the following questions:
(a) An old rule of thumb in cooking says: "A pint's a pound the world around." What is the density (in $\mathrm{g} / \mathrm{mL}$ ) of a substance for which $1 \mathrm{pt}=1 \mathrm{lb}$ exactly?
(b) There are exactly 640 acres in 1 square mile. How many square meters are in 1 acre?
(c) A certain type of wood has a density of $0.40 \mathrm{~g} / \mathrm{cm}^{3}$. What is the mass of 1.0 cord of this wood (in kg ), where 1 cord is 128 cubic feet of wood?
(d) A particular sample of crude oil has a density of $0.85 \mathrm{~g} / \mathrm{mL}$. What is the mass of 1.00 barrel of this crude oil (in kg ), where a barrel of oil is exactly 42 gallons?
(e) A gallon of ice cream contains exactly 32 servings, and each serving has 165 Calories, of which $30.0 \%$ are derived from fat. How many Calories derived from fat would you consume if you ate one halfgallon of ice cream?
1.101 A 1.0 ounce piece of chocolate contains 15 mg of caffeine, and a 6.0 ounce cup of regular coffee contains 105 mg of caffeine. How much chocolate would you have to consume to get as much caffeine as you would from 2.0 cups of coffee?
1.102 A bag of Hershey's Kisses contains the following information:
Serving size: 9 pieces $=41$ grams
Calories per serving: 230
Total fat per serving: 13 g
(a) The bag contains 2.0 lbs of Hershey's Kisses. How many Kisses are in the bag?
(b) The density of a Hershey's Kiss is $1.4 \mathrm{~g} / \mathrm{mL}$. What is the volume of a single Hershey's Kiss?
(c) How many Calories are in one Hershey's Kiss?
(d) Each gram of fat yields 9 Calories when metabolized. What percent of the calories in Hershey's Kisses are derived from fat?
1.103 Vinaigrette salad dressing consists mainly of oil and vinegar. The density of olive oil is $0.918 \mathrm{~g} / \mathrm{cm}^{3}$, the density of vinegar is $1.006 \mathrm{~g} / \mathrm{cm}^{3}$, and the two do not mix. If a certain mixture of olive oil and vinegar has a total mass of 397.8 g and a total volume of $422.8 \mathrm{~cm}^{3}$, what is the volume of oil and what is the volume of vinegar in the mixture?
1.104 At a certain point, the Celsius and Fahrenheit scales "cross," giving the same numerical value on both. At what temperature does this crossover occur?
1.105 Imagine that you place a cork measuring $1.30 \mathrm{~cm} \times$ $5.50 \mathrm{~cm} \times 3.00 \mathrm{~cm}$ in a pan of water and that on top of the cork you place a small cube of lead measuring 1.15 cm on each edge. The density of cork is $0.235 \mathrm{~g} / \mathrm{cm}^{3}$, and the density of lead is $11.35 \mathrm{~g} / \mathrm{cm}^{3}$. Will the combination of cork plus lead float or sink?
1.106 A 125 mL sample of water at 293.2 K was heated for $8 \mathrm{~min}, 25 \mathrm{~s}$ so as to give a constant temperature increase of $3.0^{\circ} \mathrm{F} / \mathrm{min}$. What is the final temperature of the water in degrees Celsius?
1.107 A calibrated flask was filled to the 25.00 mL mark with ethyl alcohol. By weighing the flask before and after adding the alcohol, it was determined that the flask contained 19.7325 g of alcohol. In a second experiment, 25.0920 g of metal beads were added to the flask, and the flask was again filled to the 25.00 mL mark with ethyl alcohol. The total mass of the metal plus alcohol in the flask was determined to be 38.4704 g . What is the density of the metal in $\mathrm{g} / \mathrm{mL}$ ?
1.108 Brass is a copper-zinc alloy. What is the mass in grams of a brass cylinder having a length of 1.62 in . and a diameter of 0.514 in . if the composition of the brass is $67.0 \%$ copper and $33.0 \%$ zinc by mass? The density of copper is $8.92 \mathrm{~g} / \mathrm{cm}^{3}$, and the density of zinc is $7.14 \mathrm{~g} / \mathrm{cm}^{3}$. Assume that the density of the brass varies linearly with composition.
1.109 Ocean currents are measured in Sverdrups (sv) where $1 \mathrm{sv}=10^{9} \mathrm{~m}^{3} / \mathrm{s}$. The gulf stream off the tip of Florida, for instance, has a flow of 35 sv .
(a) What is the flow of the gulf stream in milliliters per minute?
(b) What mass of water in the gulf stream flows past a given point in 24 hours? The density of seawater is $1.025 \mathrm{~g} / \mathrm{mL}$.
(c) How much time is required for 1 petaliter (PL; $1 \mathrm{PL}=10^{15} \mathrm{~L}$ ) of seawater to flow past a given point? The density of seawater is $1.025 \mathrm{~g} / \mathrm{mL}$.
1.110 The element gallium (Ga) has the second largest liquid range of any element, melting at $29.78^{\circ} \mathrm{C}$ and boiling at $2204^{\circ} \mathrm{C}$ at atmospheric pressure.
(a) Is gallium a metal, a nonmetal, or a semimetal?
(b) Name another element whose chemical properties might be similar to those of gallium.
(c) What is the density of gallium in $\mathrm{g} / \mathrm{cm}^{3}$ at $25^{\circ} \mathrm{C}$ if a 1 in . cube has a mass of 0.2133 lb ?
(d) Assume that you construct a thermometer using gallium as the fluid instead of mercury, and that you define the melting point of gallium as $0^{\circ} \mathrm{G}$ and the boiling point of gallium as $1000^{\circ} \mathrm{G}$. What is the melting point of sodium chloride $\left(801^{\circ} \mathrm{C}\right)$ on the gallium scale?

## eMedia Problems

1.111 Use the Interactive Periodic Table (linked from eChapter 1.3) to identify each of the following elements:
(a) Discovered first after "antiquity"
(b) Largest covalent radius
(c) Lowest electronegativity
(d) Highest ionization energy
1.112 Use the Periodic Table Groups activity (eChapter 1.4) to do the following:
(a) Determine the category in the activity that contains the largest number of elements.
(b) Determine the category that contains the smallest number of elements.
1.113 In Problem 1.91 you were asked to distinguish between chemical and physical properties of sodium metal.
(a) Watch the Sodium and Potassium in Water movie (eChapter 1.4), and list the physical and chemical properties of sodium illustrated in the movie.
(b) Compare the physical and chemical properties of sodium and potassium. How are they similar? In what ways do they differ?
1.114 Use the Significant Figures activity (eChapter 1.12) to check your answers to Problems 1.70 and 1.71.
(a) Is it possible for the product of two numbers to have more significant figures than either of the original numbers? Explain. If you answered "yes," give an example.
(b) Is it possible for the sum of two numbers to have more significant figures than one of the original numbers? Explain. If you answered "yes," give an example.

## Chapter



John J. Fortman, "Analogical Demonstration," J. Chem.
Educ., Vol. 69, 1992, 323-324. Discusses the law of conservation of mass and the law of multiple proportions

Heating the red powder HgO causes it to decompose into the silvery liquid mercury and the colorless gas oxygen.
changes eventually caused Greek philosophers to think about what different materials might be composed of and led to the idea of fundamental substances that we today call elements.

At the same time philosophers were pondering the question of elements, they were also musing about related matters: What is an element made of? Is matter continuously divisible into ever smaller and smaller pieces, or is there an ultimate limit? Can you cut a piece of gold in two, take one of the pieces and cut it in two, and so on indefinitely, or is there a point at which you must stop? Although most thinkers, including Plato and Aristotle, believed that matter is continuous, the Greek philosopher Democritus (460-370 B.c.) disagreed. Democritus proposed that elements are composed of tiny particles that we now call atoms, from the Greek word atomos, meaning indivisible. Little else was learned about elements and atoms until the birth of modern experimental science some 2000 years later.

### 2.1 Conservation of Mass and the Law of Definite Proportions

The Englishman Robert Boyle (1627-1691) is generally credited with being the first person to study chemistry as a separate intellectual discipline and the first to carry out rigorous chemical experiments. Through a careful series of researches into the nature and behavior of gases, Boyle provided clear evidence for the atomic makeup of matter. In addition, Boyle was the first to clearly define an element as a substance that cannot be chemically broken down further and to suggest that a substantial number of different elements might exist.

Progress in chemistry was slow in the 100 years following Boyle, and it was not until the work of Joseph Priestley (1733-1804) and Antoine Lavoisier (1743-1794) that the next great leap was made. Priestley prepared and isolated the gas oxygen in 1774 by heating mercury(II) oxide, HgO , according to the equation we would now write as $2 \mathrm{HgO} \rightarrow 2 \mathrm{Hg}+\mathrm{O}_{2}$. Lavoisier then showed soon thereafter that oxygen is the key substance involved in combustion.


Furthermore, Lavoisier demonstrated by careful measurements that when combustion is carried out in a closed container, the mass of the combustion products exactly equals the mass of the starting reactants. For example, when hydrogen
gas burns and combines with oxygen to yield water $\left(\mathrm{H}_{2} \mathrm{O}\right)$, the mass of the water formed is equal to the mass of the hydrogen and oxygen consumed. Called the law of mass conservation, this principle is a cornerstone of chemical science.

## Law OF MASS conservation <br> Mass is neither created nor destroyed in chemical reactions.

It's easy to demonstrate the validity of the law of mass conservation by carrying out an experiment like that shown in Figure 2.1. If 3.25 g of mercury(II) nitrate $\left[\mathrm{Hg}\left(\mathrm{NO}_{3}\right)_{2}\right.$ ] and 3.32 g of potassium iodide (KI) are dissolved in water and the solutions are mixed, an immediate chemical reaction occurs, leading to formation of the insoluble orange solid mercury(II) iodide $\left(\mathrm{HgI}_{2}\right)$. Filtering the reaction mixture gives 4.55 g of mercury(II) iodide, and evaporation of the water leaves 2.02 g of potassium nitrate $\left(\mathrm{KNO}_{3}\right)$. Thus, the combined mass of the reactants $(3.25 \mathrm{~g}+3.32 \mathrm{~g}=6.57 \mathrm{~g})$ is exactly equal to the combined mass of the products $(4.55 \mathrm{~g}+2.02 \mathrm{~g}=6.57 \mathrm{~g})$.

The combined masses of these two reactants ...


V FIGURE 2.1 An illustration of the law of mass conservation. In any chemical reaction, the combined masses of the products formed equals the combined masses of the starting reactants. In this sequence of photos, (a) weighed amounts of solid KI and solid $\mathrm{Hg}\left(\mathrm{NO}_{3}\right)_{2}$ are dissolved in water. (b) The solutions are then mixed to give solid $\mathrm{HgI}_{2}$, which is removed by filtration, and the solution that remains is evaporated to yield solid $\mathrm{KNO}_{3}$. (c) When the two products are weighed, the combined masses of the reactants KI and $\mathrm{Hg}\left(\mathrm{NO}_{3}\right)_{2}$ are found to equal the combined masses of the products $\mathrm{HgI}_{2}$ and $\mathrm{KNO}_{3}$.

(a)

(b)

(c)

Further investigations in the decades following Lavoisier led the French chemist Joseph Proust (1754-1826) to formulate a second fundamental chemical principle that we now call the law of definite proportions.
law of definite Different samples of a pure chemical substance always proportions contain the same proportion of elements by mass.

Every sample of water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ contains 1 part hydrogen and 8 parts oxygen by mass; every sample of carbon dioxide $\left(\mathrm{CO}_{2}\right)$ contains 1 part carbon and 2.7 parts oxygen by mass; and so on. Elements combine in specific proportions, not in random proportions.

### 2.2 Dalton's Atomic Theory and the Law of Multiple Proportions



Electrolysis of Water movie; Electrolysis of Water activity

How can the law of mass conservation and the law of definite proportions be explained? Why do elements behave as they do? The answers to these questions


0Dalton did not know about isotopes-atoms of the same element that have different masses due to different numbers of neutrons. Challenge students to determine which of Dalton's postulates are incorrect.


- These samples of sulfur and carbon have different masses but contain the same number of atoms.

$\triangle$ Copper metal reacts with nitric acid $\left(\mathrm{HNO}_{3}\right)$ to yield the brown gas $\mathrm{NO}_{2}$.

FIGURE 2.2 An illustration of Dalton's law of multiple proportions. Atoms of nitrogen and oxygen can combine in specific proportions to make either NO or $\mathrm{NO}_{2} . \mathrm{NO}_{2}$ contains exactly twice as many atoms of oxygen per atom of nitrogen as NO does.
were provided in 1808 by the English schoolteacher John Dalton (1766-1844), who proposed a new theory of matter. Dalton reasoned as follows:

- Elements are made of tiny particles called atoms. Although Dalton didn't know what atoms were like, he nevertheless felt that they were necessary to explain why there were so many different elements.
- Each element is characterized by the mass of its atoms. Atoms of the same element have the same mass, but atoms of different elements have different masses. Dalton realized that there must be some feature that distinguishes the atoms of one element from those of another. Because Proust's law of definite proportions showed that elements always combine in specific mass ratios, Dalton reasoned that the distinguishing feature between atoms of different elements must be mass.
- Chemical combination of elements to make different substances occurs when atoms join together in small whole-number ratios. Only if whole numbers of atoms combine will different samples of a pure compound always contain the same proportion of elements by mass (the law of definite proportions). Fractional parts of atoms are never involved in chemical reactions.
- Chemical reactions only rearrange the way that atoms are combined; the atoms themselves are unchanged. Dalton realized that atoms must be chemically indestructible for the law of mass conservation to be valid. If the same numbers and kinds of atoms are present in both reactants and products, then the masses of reactants and products must also be the same.

For any theory to be successful, it must not only explain known observations, it must also predict the outcome of events yet unknown. Dalton's atomic theory does exactly this: It predicts what has come to be called the law of multiple proportions.

## - LAW OF MULTIPLE PROPORTIONS

Elements can combine in different ways to form different substances, whose mass ratios are small whole-number multiples of each other.

Read again the third statement in Dalton's atomic theory: "Chemical combination ... occurs when atoms join together in small whole-number ratios." According to this statement, it might be (and often is) possible for the same elements to combine in different ratios to give different substances. For example, nitrogen and oxygen can combine either in a 7:8 mass ratio to make a substance we know today as NO , or in a 7:16 mass ratio to make a substance we know as $\mathrm{NO}_{2}$. Clearly, the second substance contains exactly twice as much oxygen as the first.


This result makes sense only if we assume that matter is composed of discrete atoms, which combine with one another in specific and well-defined ways

(Figure 2.2). All the atoms of a particular element have the same mass, and atoms of different elements have different characteristic masses.

## Worked Example 2.1

Methane and propane are both constituents of natural gas. A sample of methane contains 5.70 g of carbon and 1.90 g of hydrogen, whereas a sample of propane contains 4.47 g of carbon and 0.993 g of hydrogen. Show that the two substances obey the law of multiple proportions.

## Strategy

Find the $\mathrm{C}: \mathrm{H}$ mass ratio in each compound, and then compare those ratios to see if they are small whole-number multiples of each other.

## Solution

$$
\begin{aligned}
& \text { Methane: } \quad \mathrm{C}: \mathrm{H} \text { mass ratio }=\frac{5.70 \mathrm{~g} \mathrm{C}}{1.90 \mathrm{~g} \mathrm{H}}=3.00 \\
& \text { Propane: } \quad \mathrm{C}: \mathrm{H} \text { mass ratio }=\frac{4.47 \mathrm{~g} \mathrm{C}}{0.993 \mathrm{~g} \mathrm{H}}=4.50 \\
& \qquad \frac{\mathrm{C}: \mathrm{H} \text { mass ratio in methane }}{\mathrm{C}: \mathrm{H} \text { mass ratio in propane }}=\frac{3.00}{4.50}=\frac{2}{3}
\end{aligned}
$$

PROBLEM 2.1 Substances A and B are colorless gases obtained by combining sulfur with oxygen. Substance A results from combining 6.00 g of sulfur with 5.99 g of oxygen, and substance B results from combining 8.60 g of sulfur with 12.88 g of oxygen. Show that the mass ratios in the two substances are simple multiples of each other.

### 2.3 The Structure of Atoms: Electrons

Dalton's atomic theory is fine as far as it goes, but it leaves unanswered the question: What is an atom made of? Dalton himself had no way of answering this question, and it was not until nearly a century later that experiments by the English physicist J. J. Thomson (1856-1940) provided some clues.

Thomson's experiments involved the use of cathode-ray tubes, early predecessors of today's television and computer displays. As illustrated in Figure 2.3, a cathode-ray tube is a glass tube from which the air has been removed and in which two thin pieces of metal, called electrodes, have been sealed. When a sufficiently high voltage is applied across the electrodes, an electric current flows through the tube from the negatively charged electrode (the cathode) to the positively charged electrode (the anode). If the tube is not fully evacuated but still contains a small amount of air or other gas, the flowing current is visible as a glow called a cathode ray. Furthermore, if the anode has a hole in it and the end of the tube is coated with a phosphorescent substance such as zinc sulfide, the rays pass through the hole and strike the end of the tube, where they are visible as a bright spot of light. (In fact, this is exactly what happens in a television set.)

Experiments by a number of physicists in the 1890s had shown that cathode rays can be deflected by bringing either a magnet or an electrically charged plate near the tube (Figure 2.3c). Because the beam is produced at a negative electrode and is deflected toward a positive plate, Thomson proposed that cathode rays must consist of tiny negatively charged particles, which we now call electrons. Furthermore, because electrons are emitted from electrodes made of many different metals, all these different substances must contain electrons.


A Sulfur burns with a bluish flame to yield colorless $\mathrm{SO}_{2}$ gas.

$\triangle$ FIGURE 2.3 (a) A drawing of a cathode-ray tube. (b),(c) An actual tube. A stream of rays (electrons) emitted from the negatively charged cathode passes through a slit, moves toward the positively charged anode, and is detected by a phosphorescent strip. The electron beam ordinarily travels in a straight line, as in (b), but it is deflected if either an electric field or a magnetic field is present, as in (c).

Millikan Oil Drop
Experiment movie

Doris Eckey, "A Millikan Oil Drop Analogy," J. Chem. Educ., Vol. 73, 1996, 237-238.

Thomson reasoned that the amount of deflection of an electron beam by a nearby magnetic or electric field must depend on three factors:

- The strength of the deflecting magnetic or electric field The stronger the magnet or the higher the voltage on the charged plate, the greater the deflection.
- The size of the negative charge on the electron The larger the charge on the particle, the greater its interaction with the magnetic or electric field and the greater the deflection.
- The mass of the electron The lighter the particle, the greater its deflection. (Just as it's easier to deflect a Ping-Pong ball than a bowling ball.)

By carefully measuring the amount of deflection caused by electric and magnetic fields of known strength, Thomson was able to calculate the ratio of the electron's electric charge to its mass-its charge-to-mass ratio, $e / m$. The modern value is

$$
\frac{e}{m}=1.758820 \times 10^{8} \mathrm{C} / \mathrm{g}
$$

where $e$ is the magnitude of the charge on the electron in coulombs ( C ) and $m$ is the mass of the electron in grams. (We'll say more about coulombs and electrical charge in Chapter 18.) Note that because $e$ is defined as a positive quantity, the actual (negative) charge on the electron is $-e$.

Thomson was able to measure only the ratio of charge to mass, not charge or mass itself, and it was left to the American R. A. Millikan (1868-1953) to devise a method for measuring the mass of an electron (Figure 2.4). In Millikan's experiment, a fine mist of oil was sprayed into a chamber, and the tiny droplets were allowed to fall between two horizontal plates. Observing the spherical drops through a telescopic eyepiece made it possible to determine how rapidly they fell through the air, which in turn allowed their masses to be calculated. The drops were then given a negative charge by irradiating them with $X$ rays. By applying a voltage to the plates, with the upper plate positive,

it was possible to counteract the downward fall of the charged drops and keep them suspended.

With the voltage on the plates and the mass of the drops known, Millikan was able to show that the charge on a given drop was always a small whole-number multiple of $e$, whose modern value is $1.602176 \times 10^{-19} \mathrm{C}$. Substituting the value of $e$ into Thomson's charge-to-mass ratio then gives the mass $m$ of the electron as $9.109382 \times 10^{-28} \mathrm{~g}$ :

$$
\begin{aligned}
\text { Because } \quad \frac{e}{m} & =1.758820 \times 10^{8} \mathrm{C} / \mathrm{g} \\
\text { then } \quad m & =\frac{e}{1.758820 \times 10^{8} \mathrm{C} / \mathrm{g}}=\frac{1.602176 \times 10^{-19} \ell}{1.758820 \times 10^{8} \frac{\ell}{\mathrm{~g}}} \\
& =9.109382 \times 10^{-28} \mathrm{~g}
\end{aligned}
$$

### 2.4 The Structure of Atoms: Protons and Neutrons

Think about the consequences of Thomson's cathode-ray experiments. Because matter is electrically neutral overall, the fact that the atoms in an electrode can give off negatively charged particles (electrons) must mean that those same atoms also contain positively charged particles. The search for those positively charged particles and for an overall picture of atomic structure led to a landmark experiment published in 1911 by the New Zealand physicist Ernest Rutherford (1871-1937).

Rutherford's work involved the use of alpha ( $\boldsymbol{\alpha}$ ) particles, a type of emission previously observed to be given off by a number of naturally occurring radioactive elements, including radium, polonium, and radon. Rutherford knew that alpha particles are about 7000 times more massive than electrons and that they have a positive charge that is twice the magnitude of the charge on an electron, but opposite in sign.

When Rutherford directed a beam of alpha particles at a thin gold foil, he found that almost all the particles passed through the foil undeflected. A very small number (about 1 of every 20,000) were deflected at an angle, however, and a few actually bounced back toward the particle source (Figure 2.5).

4 FIGURE 2.4 Millikan's oildrop experiment. The falling oil droplets are given a negative charge, which makes it possible for them to be suspended between two electrically charged plates. Knowing the mass of the drop and the voltage on the plates makes it possible to calculate the charge on the drop.

An alpha particle is a helium nucleus: $\mathrm{He}^{2+}$.


An alpha particle (relative mass $=7000$; charge $=+2 e$ )

An electron (relative mass =1; charge $=-1 e$ )



(b)

Mary V. Lorentz, "Bowling Balls and Beads, A Concrete Analogy to the Rutherford Experiment," J. Chem. Educ., Vol. 65, 1988, 1082.


A The relative size of the nucleus in an atom is roughly the same as that of a pea in the middle of this huge stadium.

Rutherford explained his results by proposing that a metal atom must be almost entirely empty space and have its mass concentrated in a tiny central core that he called the nucleus. If the nucleus contains the atom's positive charges and most of its mass, and if the electrons move in space a relatively large distance away, then it is clear why the observed scattering results are obtained: Most alpha particles encounter empty space as they fly through the foil. Only when a positive alpha particle chances to come near a small but massive positive nucleus is it repelled strongly enough to make it bounce backward (Figure 2.5b).

Modern measurements show that an atom has a diameter of roughly $10^{-10} \mathrm{~m}$ and that a nucleus has a diameter of about $10^{-15} \mathrm{~m}$. It's difficult to imagine from these numbers alone, though, just how small a nucleus really is. For comparison purposes, if an atom were the size of a large domed stadium, the nucleus would be approximately the size of a small pea in the center of the playing field.

Further experiments by Rutherford and others in the period from 1910 to 1930 showed that a nucleus is composed of two kinds of particles, called protons and neutrons. Protons have a mass of $1.672622 \times 10^{-24} \mathrm{~g}$ (about 1836 times greater than that of an electron) and are positively charged. Because the charge on a proton is opposite in sign but equal in size to that on an electron, the numbers of protons and electrons in a neutral atom are equal. Neutrons $\left(1.674927 \times 10^{-24} \mathrm{~g}\right)$ are almost identical in mass to protons but carry no charge, and the number of neutrons in a nucleus is not directly related to the numbers of protons and electrons. Table 2.1 compares the three fundamental subatomic particles, and Figure 2.6 gives an overall view of the atom.

TABLE 2.1 A Comparison of Subatomic Particles

|  | Mass |  |  | Charge |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | (Particle |  | grams |  | amu |

[^1]

## Worked Example 2.2

Ordinary "lead" pencils actually are made of a form of carbon called graphite. If a pencil line is 0.35 mm wide and the diameter of a carbon atom is $1.5 \times 10^{-10} \mathrm{~m}$, how many atoms wide is the line?

## Strategy

Begin with the known information, and set up an equation using appropriate conversion factors so that the unwanted units cancel. In the present instance, let's begin with the width of the pencil line in millimeters, then convert to meters, and then divide the line width in meters by the diameter of a single atom in meters.

## Solution

$$
\text { Atoms }=0.35 \mathrm{~mm} \times \frac{1 \mathrm{mI}}{1000 \mathrm{~mm}} \times \frac{1 \text { atom }}{1.5 \times 10^{-10} \mathrm{~m}}=2.3 \times 10^{6} \text { atoms }
$$

$\sqrt{ }$ BALLPARK CHECK A single carbon atom is about $10^{-10} \mathrm{~m}$ wide, so it takes $10^{10}$ carbon atoms placed side by side to stretch $1 \mathrm{~m}, 10^{7}$ carbon atoms to stretch 1 mm , and about $0.3 \times 10^{7}$ (or $3 \times 10^{6} ; 3$ million) carbon atoms to stretch 0.35 mm . The ballpark check agrees with the solution.

- PROBLEM 2.2 The gold foil Rutherford used in his scattering experiment had a thickness of approximately 0.0002 in. If a single gold atom has a diameter of $2.9 \times 10^{-8} \mathrm{~cm}$, how many atoms thick was Rutherford's foil?

PROBLEM 2.3 A small speck of carbon the size of a pinhead contains about $10^{19}$ atoms, the diameter of a carbon atom is $1.5 \times 10^{-10} \mathrm{~m}$, and the circumference of the earth at the equator is $40,075 \mathrm{~km}$. How many times around the earth would the atoms from this speck of carbon extend if they were laid side by side?

### 2.5 Atomic Number

Thus far, we have described atoms only in general terms and have not yet answered the most important question: What is it that makes one atom different from another? How, for example, does an atom of gold differ from an atom of carbon? The answer to this question turns out to be quite simple: Elements differ from one another according to the number of protons in their atoms, a value called the

FIGURE 2.6 A view of the atom. The protons and neutrons in the nucleus take up very little volume but contain essentially all the atom's mass. A number of electrons equal to the number of protons move around the nucleus and account for most of the atom's volume.



William Spindel and Takanobu Ishida, "Isotope Separation," J. Chem. Educ., Vol. 68, 1991, 312-318.
$\{$ Arthur B. Ellis, Edward A. Adler, and Frederick H. Juergens, "Dramatizing Isotopes: Deuterated Ice Cubes Sink," J. Chem. Educ., Vol. 67, 1990, 159-160.
element's atomic number ( $\mathbf{Z}$ ). All atoms of the same element contain the same number of protons. Hydrogen atoms, atomic number 1, all have 1 proton; helium atoms, atomic number 2 , all have 2 protons; carbon atoms, atomic number 6 , all have 6 protons; and so on. Of course, every neutral atom also contains a number of electrons equal to its number of protons.

$$
\begin{aligned}
\text { Atomic number }(\mathbf{Z}) & =\text { Number of protons in atom's nucleus } \\
& =\text { Number of electrons around atom's nucleus }
\end{aligned}
$$



A hydrogen atom (1 proton; 1 electron)


A carbon atom
(6 protons; 6 electrons)


A gold atom
(79 protons; 79 electrons)

In addition to protons, the nuclei of most atoms also contain neutrons. The sum of the number of protons $(Z)$ and the number of neutrons $(N)$ in an atom is called the atom's mass number $(A)$. That is, $A=Z+N$.

Mass number $(A)=$ Number of protons $(Z)+$ Number of neutrons $(N)$
Most hydrogen atoms have 1 proton and no neutrons, so their mass number is $A=1+0=1$. Most helium atoms have 2 protons and 2 neutrons, so their mass number is $A=2+2=4$. Most carbon atoms have 6 protons and 6 neutrons, so their mass number is $A=6+6=12$; and so on. Except for hydrogen, atoms always contain at least as many neutrons as protons, although there is no simple way to predict how many neutrons a given atom will have.

Notice in the previous paragraph that we said most hydrogen atoms have mass number 1, most helium atoms have mass number 4, and most carbon atoms have mass number 12. In fact, different atoms of the same element can have different mass numbers depending on how many neutrons they have. Atoms with identical atomic numbers but different mass numbers are called isotopes. Hydrogen, for example, has three isotopes.


Protium-one proton () and no neutrons; mass number $=1$


Deuterium-one proton ( ) and one neutron ( ); mass number $=2$


Tritium-one proton ( ) and two neutrons ( ); mass number $=3$

All hydrogen atoms have 1 proton in their nucleus (otherwise they wouldn't be hydrogen), but most ( $99.985 \%$ ) have no neutrons. These hydrogen atoms, called protium, have mass number 1 . In addition, $0.015 \%$ of hydrogen atoms, called deuterium, have 1 neutron and mass number 2 . Still other hydrogen atoms, called tritium, have 2 neutrons and mass number 3 . An unstable, radioactive isotope, tritium occurs only in trace amounts on Earth but is made artificially in nuclear reactors. As other examples, there are 13 known isotopes of carbon, only 2 of which occur commonly, and 25 known isotopes of uranium, only 3 of which occur commonly.

A given isotope is represented by showing its element symbol with mass number as a left superscript and atomic number as a left subscript. Thus, protium is represented as ${ }_{1}^{1} \mathrm{H}$, deuterium as ${ }_{1}^{2} \mathrm{H}$, and tritium as ${ }_{1}^{3} \mathrm{H}$. Similarly, the two naturally
occurring isotopes of carbon are represented as ${ }_{6}^{12} \mathrm{C}$ (spoken as "carbon- 12 ") and ${ }_{6}^{13} \mathrm{C}$ (carbon-13). Note that the number of neutrons in an isotope can be calculated simply by subtracting the atomic number (subscript) from the mass number (superscript). For example, subtracting the atomic number 6 from the mass number 12 indicates that a ${ }_{6}^{12} \mathrm{C}$ atom has 6 neutrons.


It turns out that the number of neutrons in an atom has little effect on the atom's chemical properties. The chemistry of an element is determined almost entirely by the number of electrons it has, which in turn is determined by the number of protons in its nucleus. All three isotopes of hydrogen therefore behave almost identically in their chemical reactions.

## Worked Example 2.3

The isotope of uranium used in nuclear power plants is ${ }_{92}^{235} \mathrm{U}$. How many protons, neutrons, and electrons does an atom of ${ }_{92}^{235} \mathrm{U}$ have?

## Strategy

The atomic number (subscript 92) in the symbol ${ }_{92}^{235} \mathrm{U}$ indicates the number of protons and electrons in the atom. The number of neutrons is the difference between the mass number (superscript 235) and the atomic number (92).

## Solution

An atom of ${ }_{92}^{235} \mathrm{U}$ has 92 protons, 92 electrons, and $235-92=143$ neutrons.


A Uranium-235 is used as fuel in this nuclear power plant.

## Worked Example 2.4

Element X is toxic to humans in high concentration but is essential to life at low concentrations. Identify element $X$, whose atoms contain 24 protons, and write the symbol for the isotope with 28 neutrons.

## Strategy

The number of protons in an atom's nucleus is the element's atomic number. The mass number is the sum of the atomic number and the number of neutrons.

## Solution

According to the periodic table, the element with atomic number 24 is chromium, Cr . The particular isotope of chromium in this instance has a mass number of $24+28=52$ and is written ${ }_{24}^{52} \mathrm{Cr}$.

- PROBLEM 2.4 The isotope ${ }_{34}^{75} \mathrm{Se}$ is used medically for diagnosis of pancreatic disorders. How many protons, neutrons, and electrons does an atom of ${ }_{34}^{75}$ Se have?
- PROBLEM 2.5 Chlorine, one of the elements in common table salt (sodium chloride), has two main isotopes, with mass numbers 35 and 37 . Look up the atomic number of chlorine, tell how many neutrons each isotope contains, and give the standard symbol for each.
- PROBLEM 2.6 An atom of element $X$ contains 47 protons and 62 neutrons. Identify the element, and write the symbol for the isotope in the standard format.

$\square$
The use of carbon-12 to define the amu is another example of a system of measurement based on an arbitrary standard. In earlier times the amu was based on oxygen-16 and hydrogen-1.

$\sqrt{ }$
The average atomic mass of an element is a weighted, not a simple, average.

0An effective example showing the difference between simple average and weighted average is the use of a hypothetical student's test scores of 100, 100, 100,60 . The weighted average $=90$; since there are only two different grades, 100 and 60, the simple average is 80 .

### 2.6 Atomic Mass

Atoms are so tiny that even the smallest speck of dust visible to the naked eye contains about $10^{16}$ atoms. Thus, the mass of a single atom in grams is much too small a number for convenience, and chemists therefore use a unit called an atomic mass unit (amu), also known as a dalton ( Da ). One amu is defined as exactly onetwelfth the mass of an atom of ${ }_{6}^{12} \mathrm{C}$ and is equal to $1.660539 \times 10^{-24} \mathrm{~g}$ :

$$
\begin{aligned}
\text { Mass of one }{ }_{6}^{12} \mathrm{C} \text { atom } & =12 \mathrm{amu}(\text { exactly }) \\
1 \mathrm{amu} & =\frac{\text { Mass of one }{ }_{6}^{12} \mathrm{C} \text { atom }}{12}=1.660539 \times 10^{-24} \mathrm{~g}
\end{aligned}
$$

Because the mass of an atom's electrons is negligible compared with the mass of its protons and neutrons, defining 1 amu as $1 / 12$ the mass of a ${ }_{6}^{12} \mathrm{C}$ atom means that protons and neutrons each have a mass of almost exactly 1 amu (Table 2.1). Thus, the mass of an atom in atomic mass units-called the atom's isotopic mass-is numerically close to the atom's mass number. A ${ }_{1}^{1} \mathrm{H}$ atom, for instance, has a mass of 1.007825 amu ; a ${ }_{92}^{235} \mathrm{U}$ atom has a mass of 235.043924 amu ; and so forth.

Most elements occur naturally as a mixture of different isotopes. If you look at the periodic table inside the front cover, you'll see listed below the symbol for each element a value called the element's atomic mass. (The unit amu is understood but not specified.)


An element's atomic mass is the weighted average of the isotopic masses of the element's naturally occurring isotopes. Carbon, for example, occurs on Earth as a mixture of two isotopes, ${ }_{6}^{12} \mathrm{C}$ ( $98.89 \%$ natural abundance) and ${ }_{6}^{13} \mathrm{C}(1.11 \%$ natural abundance). Although the isotopic mass of any individual carbon atom is either 12 amu (a carbon- 12 atom) or 13.0034 amu (a carbon- 13 atom), the average isotopic mass-that is, the atomic mass-of a large collection of carbon atoms is 12.011 amu . (A third carbon isotope, ${ }_{6}^{14} \mathrm{C}$, is produced in small amounts in the upper atmosphere when cosmic rays strike ${ }_{7}^{14} \mathrm{~N}$, but its abundance is so low that it can be ignored when calculating atomic mass.)

Arthur M. Last and Michael J. Webb, "Using Monetary Analogies to Teach Average Atomic Mass," J. Chem. Educ., Vol. 70, 1993, 234-235.

$$
\begin{aligned}
\text { Atomic mass of } \mathrm{C} & =\left(\text { Mass of }{ }_{6}^{12} \mathrm{C}\right)\left(\text { Abundance of }{ }_{6}^{12} \mathrm{C}\right)+\left(\text { Mass of }{ }_{6}^{13} \mathrm{C}\right)\left(\text { Abundance of }{ }_{6}^{13} \mathrm{C}\right) \\
& =(12 \mathrm{amu})(0.9889)+(13.0034 \mathrm{amu})(0.0111) \\
& =11.867 \mathrm{amu}+0.144 \mathrm{amu}=12.011 \mathrm{amu}
\end{aligned}
$$

John J. Fortman, "Pictorial Analogies IV: Relative Atomic Weights," J. Chem. Educ., Vol. 70, 1993, 235-236.

7 Josefina Arce de Sanabia, "Relative Atomic Mass and the Mole: A Concrete Analogy to Help Students Understand These Abstract Concepts," J. Chem. Educ., Vol. 70, 1993, 233-234.

The value of using atomic masses is that it allows us to count a large number of atoms by weighing a sample of the element. For instance, we can calculate that a small speck of carbon weighing $1.00 \mathrm{mg}\left(1.00 \times 10^{-3} \mathrm{~g}\right)$ contains $5.01 \times 10^{19}$ carbon atoms:

$$
1.00 \times 10^{-3} \mathrm{~g} \times \frac{1 \mathrm{amtu}}{1.6605 \times 10^{-24} \mathrm{~g}} \times \frac{1 \mathrm{C} \text { atom }}{12.011 \mathrm{amu}}=5.01 \times 10^{19} \mathrm{C} \text { atoms }
$$

We'll have many occasions in future chapters to take advantage of this relationship between mass, atomic mass, and number of atoms.

## Worked Example 2.5

Chlorine has two naturally occurring isotopes: ${ }_{17}^{35} \mathrm{Cl}$ with a natural abundance of $75.77 \%$ and an isotopic mass of 34.969 amu , and ${ }_{17}^{37} \mathrm{Cl}$ with a natural abundance of $24.23 \%$ and an isotopic mass of 36.966 amu . What is the atomic mass of chlorine?

## Strategy

The atomic mass of an element is the weighted average of the isotope masses, which equals the sum of the masses of each isotope times the natural abundance of that isotope:
Atomic mass $=\left(\right.$ Mass of $\left.{ }_{17}^{35} \mathrm{Cl}\right)\left(\right.$ Abundance of $\left.{ }_{17}^{35} \mathrm{Cl}\right)+\left(\right.$ Mass of $\left.{ }_{17}^{37} \mathrm{Cl}\right)\left(\right.$ Abundance of $\left.{ }_{17}^{37} \mathrm{Cl}\right)$

## Solution

$$
\text { Atomic mass }=(34.969 \mathrm{amu})(0.7577)+(36.966 \mathrm{amu})(0.2423)=35.45 \mathrm{amu}
$$

- PROBLEM 2.7 Copper metal has two naturally occurring isotopes: copper-63 ( $69.17 \%$; isotopic mass $=62.94 \mathrm{amu}$ ) and copper-65 ( $30.83 \%$; isotopic mass $=$ 64.93 amu ). Calculate the atomic mass of copper, and check your answer in a periodic table.
- PROBLEM 2.8 Based on your answer to Problem 2.7, how many atoms of copper are in a pure copper penny that weighs $2.15 \mathrm{~g} ?\left(1 \mathrm{amu}=1.6605 \times 10^{-24} \mathrm{~g}\right)$


## 2.7 | Compounds and Mixtures

Although only 90 elements occur naturally, there are obviously far more than 90 different kinds of matter on earth. Just look around, and you'll surely find a few hundred. All the many kinds of matter can be classified as either pure substances or mixtures, as shown in Figure 2.7. Pure substances, in turn, can be either elements or chemical compounds.


## Chemical Compounds

A chemical compound is a pure substance that is formed when atoms of two or more different elements combine and create a new material with properties completely unlike those of its constituent elements. A compound has a constant composition throughout, and its constituent units are all identical. For example, when atoms of sodium (a soft, silvery metal) combine with atoms of chlorine (a toxic, yellow-green gas), the familiar white solid called sodium chloride (table salt) is formed. Similarly, when two atoms of hydrogen combine with one atom of oxygen, water is formed. Such transformations are called chemical reactions.

A compound is written by giving its chemical formula, which lists the symbols of the individual constituent elements and indicates the number of atoms of each

FIGURE 2.7 A scheme for the classification of matter.


Mixtures and
Compounds movie;
Mixtures and Compounds activity
element with a subscript. If no subscript is given, the number 1 is understood. Thus, sodium chloride is written as NaCl , water as $\mathrm{H}_{2} \mathrm{O}$, and sucrose (table sugar) as $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$. A chemical reaction is written in a standard format called a chemical equation, in which the starting substances, or reactants, are on the left, the final substances, or products, are on the right, and an arrow is placed between them to indicate a transformation. The numbers and kinds of atoms are the same on both sides of the reaction arrow, as required by the law of mass conservation (Section 2.1).

$$
\mathrm{O}_{2}+2 \mathrm{H}_{2} \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}
$$



## Mixtures

Unlike chemical compounds, whose constituent units are identical, mixtures are simply blends of two or more substances added together in some random proportion without chemically changing the individual substances themselves. Thus, hydrogen gas and oxygen gas can be mixed in any ratio without changing them (as long as there is no flame nearby to initiate reaction), just as a spoonful of sugar and a spoonful of salt can be mixed.

The crystalline quartz sand on this beach is a pure compound $\left(\mathrm{SiO}_{2}\right)$, but the seawater is a liquid mixture of many compounds dissolved in water.


Mixtures can be further classified as either heterogeneous or homogeneous. Heterogeneous mixtures are those in which the mixing is not uniform and which therefore have regions of different composition. Sand with sugar, water with gasoline, and dust with air, are all heterogeneous mixtures. Homogeneous mixtures are those in which the mixing is uniform and which therefore have a constant composition throughout. Air is a gaseous mixture of (primarily) oxygen and nitrogen, seawater is a liquid mixture of (primarily) sodium chloride dissolved in water, and brass is a solid mixture of copper and zinc.

With liquids it's often possible to distinguish between a homogeneous mixture and a heterogeneous one simply by looking. Heterogeneous mixtures tend to be cloudy and will separate on standing, whereas homogeneous mixtures are often transparent. We'll look further at the nature and properties of liquid mixtures in Chapter 11.

## $2.8 \mid$ Molecules, Ions, and Chemical Bonds

Imagine what must happen when two atoms approach each other at the beginning of a chemical reaction. Because the electrons of an atom occupy a much greater volume than the nucleus, it's the electrons that actually make the contact when atoms collide. Thus, it's the electrons that form the connections, or chemical bonds, that join atoms together in compounds.

Chemical bonds between atoms are usually classified as either covalent or ionic. As a general rule, covalent bonds occur between nonmetal atoms while ionic bonds occur between metal and nonmetal atoms. Let's look briefly at both kinds.

## Covalent Bonds: Molecules

A covalent bond, the most common kind of chemical bond, results when two atoms share some (usually two) electrons. A simple way to think about a covalent bond is to imagine it as a tug-of-war. If two people pull on the same rope, they are effectively joined together. Neither person can escape from the other as long as both hold on. Similarly with atoms: When two atoms both hold on to some shared electrons, the atoms are bonded together (Figure 2.8).

(b)
(a)

The unit of matter that results when two or more atoms are joined by covalent bonds is called a molecule. A hydrogen chloride molecule ( HCl ) results when a hydrogen atom and a chlorine atom share two electrons. A water molecule $\left(\mathrm{H}_{2} \mathrm{O}\right)$ results when each of two hydrogen atoms shares two electrons with a single oxygen atom. An ammonia molecule $\left(\mathrm{NH}_{3}\right)$ results when three hydrogen atoms share two electrons each with a nitrogen atom, and so on. To visualize these and other molecules, it helps to imagine the individual atoms as spheres joined together to form molecules with specific three-dimensional shapes. Socalled ball-and-stick models (Figure 2.9a) specifically indicate the covalent bonds


A FIGURE 2.8 A covalent bond between atoms is analogous to a tug-of-war. (a) The two teams are joined together because both are tugging on the same rope. (b) Similarly, two atoms are joined together when both nuclei $(+)$ tug on the same electrons, represented here by dots.
< FIGURE 2.9 Molecular drawings such as these help in visualizing molecules. (a) Ball-and-stick models show individual atoms (spheres) joined together by covalent bonds (sticks). (b) Space-filling models accurately portray the overall molecular shape but do not explicitly show covalent bonds.


3D models of Methane and Water

The element oxygen is written $\mathrm{O}_{2} . \mathrm{P}_{4}$ and $\mathrm{S}_{8}$ are other examples of elements that occur as polyatomic species.
Ethyl alcohol

Name $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$

Chemical formula


Structural formula


A structural formula uses lines between atoms to indicate the covalent bonds. Thus, the two carbon atoms in ethyl alcohol are covalently bonded to each other, the oxygen atom is bonded to one of the carbon atoms, and the six hydrogen atoms are distributed three to one carbon, two to the other carbon, and one to the oxygen.

Even some elements exist as molecules rather than as atoms. Hydrogen, nitrogen, oxygen, fluorine, chlorine, bromine, and iodine all exist as diatomic (twoatom) molecules whose two atoms are held together by covalent bonds. We therefore have to write them as such when using any of these elements in a chemical equation.


## Worked Example 2.6

Propane, $\mathrm{C}_{3} \mathrm{H}_{8}$, has a structure in which the three carbon atoms are bonded in a row, each end carbon is bonded to three hydrogens, and the middle carbon is bonded to two hydrogens. Draw the structural formula, using lines between atoms to represent covalent bonds.

## Solution



Propane

## Worked Key Concept Example 2.3

Which of the following drawings represents a mixture, which a pure compound, and which an element?


## Strategy

Many people (professional chemists included) find chemistry easier to grasp when they can visualize the behavior of atoms, thereby turning symbols into pictures. The Key Concept Problems in this text are intended to help you do that, frequently representing atoms and molecules as collections of spheres. Don't take the pictures too literally; focus instead on interpreting what they represent.

## Solution

Drawing (a) represents a mixture of two diatomic elements, one composed of two red atoms and one composed of two blue atoms. Drawing (b) represents molecules of a pure diatomic element because all atoms are identical. Drawing (c) represents molecules of a pure compound composed of one red and one blue atom.

- PROBLEM 2.9 Draw the structural formula of methylamine, $\mathrm{CH}_{5} \mathrm{~N}$, a substance responsible for the odor of rotting fish. The carbon atom is bonded to the nitrogen atom and to three hydrogens. The nitrogen atom is bonded to the carbon and two hydrogens.
- KEY CONCEPT PROBLEM 2.10 Which of the following drawings represents a collection of hydrogen peroxide $\left(\mathrm{H}_{2} \mathrm{O}_{2}\right)$ molecules? The red spheres represent oxygen atoms and the ivory spheres represent hydrogen.


KEY CONCEPT PROBLEM 2.11 Adrenaline, the so-called "flight or fight" hormone, is represented by the following ball-and-stick model. What is the molecular formula of adrenaline? $($ Gray $=\mathrm{C}$, ivory $=\mathrm{H}$, red $=\mathrm{O}$, blue $=\mathrm{N})$



A Chlorine is a toxic green gas, sodium is a reactive metal, and sodium chloride is a harmless white solid.

NaCl is a simplest formula or empirical formula. It does not reveal that the compound is made up of ions $\left(\mathrm{Na}^{+} \mathrm{Cl}^{-}\right)$, nor that it is an extended system $(\mathrm{NaCl})_{x}$.


FIGURE 2.10 The arrangement of $\mathrm{Na}^{+}$ions and $\mathrm{Cl}^{-}$ions in a crystal of sodium chloride. Each $\mathrm{Na}^{+}$ion is surrounded by six neighboring $\mathrm{Cl}^{-}$ions, and each $\mathrm{Cl}^{-}$ion is surrounded by six neighboring $\mathrm{Na}^{+}$ions. Thus, there is no discrete "molecule" of NaCl . Instead, the entire crystal is an ionic solid.

Polyatomic ions are also known as molecular ions because they are molecules with a charge.


## Ionic Bonds

In contrast to a covalent bond, an ionic bond results not from a sharing of electrons but from a transfer of one or more electrons from one atom to another. As noted previously, ionic bonds generally form between a metal and a nonmetal. Metallic elements, such as sodium, magnesium, and zinc, tend to give up electrons, whereas nonmetallic elements, such as oxygen, nitrogen, and chlorine, tend to accept electrons.

To see how an ionic bond forms, imagine what happens when sodium metal comes in contact with chlorine gas. The sodium atom gives an electron to a chlorine atom, resulting in the formation of two charged particles, called ions. Because a sodium atom loses one electron, it loses one negative charge and becomes an $\mathrm{Na}^{+}$ ion with a charge of +1 . Such positive ions are called cations (cat-ions). Conversely, because a chlorine atom gains an electron, it gains a negative charge and becomes a $\mathrm{Cl}^{-}$ion with a charge of -1 . Such negative ions are called anions (an-ions).


A similar reaction takes place when magnesium and chlorine $\left(\mathrm{Cl}_{2}\right)$ come in contact to form $\mathrm{MgCl}_{2}$. Magnesium transfers two electrons to two chlorine atoms, yielding the doubly charged $\mathrm{Mg}^{2+}$ cation and two $\mathrm{Cl}^{-}$anions.

$$
\mathrm{Mg}+\mathrm{Cl}_{2} \longrightarrow \mathrm{Mg}^{2+}+\mathrm{Cl}^{-}+\mathrm{Cl}^{-} \quad\left(\mathrm{MgCl}_{2}\right)
$$

Because opposite charges attract, positively charged cations like $\mathrm{Na}^{+}$and $\mathrm{Mg}^{2+}$ experience a strong electrical attraction to negatively charged anions like $\mathrm{Cl}^{-}$, an attraction that we call an ionic bond. Unlike what happens when covalent bonds are formed, though, we can't really talk about discrete $\mathrm{Na}^{+} \mathrm{Cl}^{-}$molecules under normal conditions. We can speak only of an ionic solid, in which equal numbers of $\mathrm{Na}^{+}$ and $\mathrm{Cl}^{-}$ions are packed together in a regular way (Figure 2.10). In a crystal of table salt, for instance, each $\mathrm{Na}^{+}$ion is surrounded by six nearby $\mathrm{Cl}^{-}$ions, and each $\mathrm{Cl}^{-}$ ion is surrounded by six nearby $\mathrm{Na}^{+}$ions, but we can't specify what pairs of ions "belong" to each other as we can with atoms in covalent molecules.


Charged, covalently bonded groups of atoms, called polyatomic ions, also existfor example, ammonium ion $\left(\mathrm{NH}_{4}^{+}\right)$, hydroxide ion $\left(\mathrm{OH}^{-}\right)$, nitrate ion $\left(\mathrm{NO}_{3}^{-}\right)$, and the doubly charged sulfate ion $\left(\mathrm{SO}_{4}{ }^{2-}\right)$. You can think of these polyatomic ions as charged molecules because they consist of specific numbers and kinds of atoms joined together by covalent bonds in a definite way, with the overall unit having a positive or negative charge. When writing the formulas of substances that contain more than one of these ions, parentheses are placed around the entire polyatomic unit. The formula $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$, for instance, indicates a substance made of $\mathrm{Ba}^{2+}$ cations and $\mathrm{NO}_{3}^{-}$polyatomic anions in a 1:2 ratio. We'll say more about these ions in Section 2.10.

## Worked Example 2.8

Which of the following compounds would you expect to be ionic and which molecular?
(a) $\mathrm{BaF}_{2}$
(b) $\mathrm{SF}_{4}$
(c) $\mathrm{PH}_{3}$
(d) $\mathrm{CH}_{3} \mathrm{OH}$

## Strategy

Remember that covalent bonds generally form between nonmetal atoms, while ionic bonds form between metal and nonmetal atoms.

## Solution

Compound (a) is composed of a metal (barium) and a nonmetal (fluorine) and is likely to be ionic. Compounds (b)-(d) are composed entirely of nonmetals and therefore are probably molecular.

- PROBLEM 2.12 Which of the following compounds would you expect to be ionic and which molecular?
(a) LiBr
(b) $\mathrm{SiCl}_{4}$
(c) $\mathrm{BF}_{3}$
(d) CaO
-KEY CONCEPT PROBLEM 2.13 Which of the following drawings is most likely to represent an ionic compound, and which a molecular compound? Explain.



### 2.9 Acids and Bases

Among the many ions we'll be discussing throughout this book, two of the most important are the hydrogen cation $\left(\mathrm{H}^{+}\right)$and the hydroxide anion $\left(\mathrm{OH}^{-}\right)$. Since a hydrogen atom contains one proton and one electron, a hydrogen cation is simply a proton. A hydroxide ion, by contrast, is a polyatomic anion in which an oxygen atom is covalently bonded to a hydrogen atom. Although much of Chapter 15 is devoted to the chemistry of $\mathrm{H}^{+}$and $\mathrm{OH}^{-}$ions, it's worthwhile taking a preliminary look at these two species now.

The importance of the $\mathrm{H}^{+}$cation and $\mathrm{OH}^{-}$anion is that they are fundamental to the concept of acids and bases. In fact, one useful definition of an acid is a substance that provides $\mathrm{H}^{+}$ions when dissolved in water, and one definition of a base is a substance that provides $\mathrm{OH}^{-}$ions when dissolved in water.

```
- acid A substance that provides H}\mp@subsup{\textrm{H}}{}{+}\mathrm{ ions in water
HCl, HNO
base A substance that provides OH
NaOH, KOH, Ba(OH)
```

Hydrochloric acid $(\mathrm{HCl})$, nitric acid $\left(\mathrm{HNO}_{3}\right)$, sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$, and phosphoric acid $\left(\mathrm{H}_{3} \mathrm{PO}_{4}\right)$ are among the most common acids. When any of these substances is dissolved in water, $\mathrm{H}^{+}$ions are formed along with the corresponding anion. For example, HCl gives $\mathrm{H}^{+}$ions and $\mathrm{Cl}^{-}$ions when it dissolves in water. We sometimes attach the designation (aq) to show that the ions are present in aqueous solution. In the same way, we often attach the designation $(g)$ for gas, $(l)$ for liquid, or ( $s$ ) for solid to indicate the state of other reactants or products. For example, pure HCl is a gas, $\mathrm{HCl}(g)$, and pure $\mathrm{HNO}_{3}$ is a liquid, $\mathrm{HNO}_{3}(l)$.

Depending on their structure, different acids can provide different numbers of $\mathrm{H}^{+}$ions. Hydrochloric acid and nitric acid provide one $\mathrm{H}^{+}$ion each per molecule,

(1)Gerhard Lind, "Teaching Inorganic Nomenclature: A Systematic Approach," J. Chem. Educ., Vol. 69, 1992, 613-614.


A Morphine, a pain-killing agent found in the opium poppy, was named after Morpheus, the Greek god of dreams.
sulfuric acid can provide two $\mathrm{H}^{+}$ions per molecule, and phosphoric acid can provide three $\mathrm{H}^{+}$ions per molecule.

| Hydrochloric acid: | $\mathrm{HCl}(g)$ | $\xrightarrow{\text { Dissolve in } \mathrm{H}_{2} \mathrm{O}} \mathrm{H}^{+}(a q)+\mathrm{Cl}^{-}(a q)$ |
| :--- | :--- | :--- |
| Nitric acid: | $\mathrm{HNO}_{3}(l) \xrightarrow{\text { Dissolve in } \mathrm{H}_{2} \mathrm{O}} \mathrm{H}^{+}(a q)+\mathrm{NO}_{3}{ }^{-}(a q)$ |  |
| Sulfuric acid: | $\mathrm{H}_{2} \mathrm{SO}_{4}(l) \xrightarrow{\text { Dissolve in } \mathrm{H}_{2} \mathrm{O}} \mathrm{H}^{+}(a q)+\mathrm{HSO}_{4}{ }^{-}(a q)$ |  |
|  | $\mathrm{HSO}_{4}{ }^{-}(a q) \xrightarrow{+} \xrightarrow{+}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q)$ |  |
| Phosphoric acid: | $\mathrm{H}_{3} \mathrm{PO}_{4}(l) \xrightarrow{\text { Dissolve in } \mathrm{H}_{2} \mathrm{O}} \mathrm{H}^{+}(a q)+\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}(a q)$ |  |
|  | $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}(a q) \xrightarrow{+}(a q)+\mathrm{HPO}_{4}{ }^{2-}(a q)$ |  |
|  | $\mathrm{HPO}_{4}{ }^{2-}(a q) \xrightarrow{+}(a q)+\mathrm{PO}_{4}{ }^{3-}(a q)$ |  |

Sodium hydroxide $(\mathrm{NaOH}$; also known as lye or caustic soda), potassium hydroxide ( KOH ; also known as caustic potash), and barium hydroxide $\left[\mathrm{Ba}(\mathrm{OH})_{2}\right]$ are examples of bases. When any of these compounds dissolves in water, $\mathrm{OH}^{-}$ anions go into solution along with the corresponding metal cation. Sodium hydroxide and potassium hydroxide provide one $\mathrm{OH}^{-}$ion each, and barium hydroxide provides two $\mathrm{OH}^{-}$ions, as indicated by its formula.

| Sodium hydroxide: | $\mathrm{NaOH}(s)$ |
| :--- | :--- |
| Potassium hydroxide: $\mathrm{KOH}(s)$ | $\xrightarrow{\text { Dissolve in } \mathrm{H}_{2} \mathrm{O}} \mathrm{Na}^{+}(a q)+\mathrm{OH}^{-}(a q)$ |
| Dissolve in $\mathrm{H}_{2} \mathrm{O}$ |  |
| Barium hydroxide: | $\mathrm{Ba}(\mathrm{OH})_{2}(s) \xrightarrow{+}(a q)+\mathrm{OH}^{-}(a q)$ |
| Dissolve in $\mathrm{H}_{2} \mathrm{O}$ |  |
| $\mathrm{Ba}^{2+}(a q)+2 \mathrm{OH}^{-}(a q)$ |  |

PROBLEM 2.14 Which of the following compounds are acids, and which are bases? Explain.
(a) HF
(b) $\mathrm{Ca}(\mathrm{OH})_{2}$
(c) LiOH
(d) HCN

### 2.10 | Naming Chemical Compounds

In the early days of chemistry, when few pure substances were known, newly discovered compounds were often given fanciful names-morphine, quicklime, muriatic acid, and barbituric acid (named by its discoverer in honor of his friend Barbara)-to cite a few. Today, with more than 20 million pure compounds known, there would be chaos unless a systematic method for naming compounds were used. Every chemical compound must be given a name that not only defines it uniquely but also allows chemists (and computers) to know the compound's chemical structure.

Different kinds of compounds are named by different rules. Ordinary table salt, for instance, is named sodium chloride because of its formula NaCl , but common table sugar $\left(\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}\right)$ is named $\beta$-D-fructofuranosyl- $\alpha$-D-glucopyranoside because of special rules for carbohydrates (don't worry about it). We'll begin in this section by seeing how to name simple binary compounds-those made of only two elements-and then introduce additional rules in later chapters as the need arises.

## Naming Binary Ionic Compounds

Binary ionic compounds are named by identifying first the positive ion and then the negative ion. The positive ion takes the same name as the element; the negative ion takes the first part of its name from the element and then adds the ending -ide. For example, KBr is named potassium bromide—potassium for the $\mathrm{K}^{+}$ion, and bromide for the negative $\mathrm{Br}^{-}$ion derived from the element bromine. Figure 2.11
shows some common main-group ions, and Figure 2.12 shows some common transition metal ions.

| LiF | $\mathrm{CaBr}_{2}$ | $\mathrm{AlCl}_{3}$ |
| :---: | :---: | :---: |
| Lithium fluoride | Calcium bromide | Aluminum chloride |



There are several interesting points about Figure 2.11. Note, for instance, that metals tend to form cations and nonmetals tend to form anions, as mentioned previously in Section 2.8. Note also that elements within a given group of the periodic table form similar kinds of ions and that the charge on the ion depends on the group number. Main-group metals usually form cations whose charge is equal to the group number. Group 1A elements form monopositive ions ( $\mathrm{M}^{+}$, where M is a metal), group 2A elements form doubly positive ions $\left(\mathrm{M}^{2+}\right)$, and group 3A elements form triply positive ions $\left(\mathrm{M}^{3+}\right)$. Main-group nonmetals usually form anions whose charge is equal to the group number (U.S. system) minus eight. Thus, group 6A elements form doubly negative ions ( $6-8=-2$ ), group 7A elements form mononegative ions ( $7-$ $8=-1)$, and group 8A elements form no ions at all $(8-8=0)$.

|  | $\begin{gathered} 3 \\ 3 B \end{gathered}$ | $\begin{gathered} 4 \\ 4 \mathrm{~B} \end{gathered}$ | $\begin{gathered} 5 \\ 5 \mathrm{~B} \end{gathered}$ | $\begin{gathered} 6 \\ 6 \mathrm{~B} \end{gathered}$ | $\begin{gathered} 7 \\ 7 \mathrm{~B} \end{gathered}$ | 8 | $\begin{gathered} 9 \\ 8 B^{-} \end{gathered}$ | 10 | $\begin{gathered} 11 \\ 1 \mathrm{~B} \end{gathered}$ | $\begin{aligned} & 12 \\ & 2 B \end{aligned}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{Sc}^{3+}$ | $\mathrm{Ti}^{3+}$ | $\mathrm{V}^{3+}$ | $\begin{aligned} & \mathrm{Cr}^{2+} \\ & \mathrm{Cr}^{3+} \end{aligned}$ | $\mathrm{Mn}^{2+}$ | $\begin{aligned} & \mathrm{Fe}^{2+} \\ & \mathrm{Fe}^{3+} \end{aligned}$ | $\mathrm{Co}^{2+}$ | $\mathrm{Ni}^{2+}$ | $\mathrm{Cu}^{2+}$ | $\mathrm{Zn}^{2+}$ |  |
|  | $\mathrm{Y}^{3+}$ |  |  |  |  | $\mathrm{Ru}^{3+}$ | Rh ${ }^{3+}$ | $\mathrm{Pd}^{2+}$ | $\mathrm{Ag}^{+}$ | $\mathrm{Cd}^{2+}$ |  |
|  | $\mathrm{La}^{3+}$ |  |  |  |  |  |  |  |  | $\mathrm{Hg}^{2+}$ |  |

Notice in both Figures 2.11 and 2.12 that some metals form more than one kind of cation. Iron, for example, forms both the doubly charged $\mathrm{Fe}^{2+}$ ion and the triply charged $\mathrm{Fe}^{3+}$ ion. In naming these ions, it's necessary to distinguish between them by using a Roman numeral in parentheses to indicate the number of charges. Thus, $\mathrm{FeCl}_{2}$ is iron(II) chloride, and $\mathrm{FeCl}_{3}$ is iron(III) chloride. Alternatively, an older method distinguishes between the ions by using the Latin name of the element (ferrum) together with the ending -ous for the ion with lower charge and -ic for the ion with

4 FIGURE 2.11 Main-group cations and anions. A cation bears the same name as the element it is derived from; an anion name has an -ide ending.


FIGURE 2.12 Common transition metal ions. Only ions that exist in aqueous solution are shown.

$\square$In compounds, elements on the left of the periodic table tend to be relatively positive, and elements on the right tend to be relatively negative.


© Crystals of iron(II) chloride tetrahydrate are greenish; crystals of iron(III) chloride hexahydrate are brownish yellow.
higher charge. Thus, $\mathrm{FeCl}_{2}$ is sometimes called ferrous chloride, and $\mathrm{FeCl}_{3}$ is called ferric chloride. Though still in use, this older naming system is being phased out.

| $\mathrm{Fe}^{2+}$ |  |  | $\mathrm{Fe}^{3+}$ |
| :--- | :---: | :---: | :---: |
| Iron(II) ion | Iron(III) ion | $\mathrm{Sn}^{2+}$ | $\mathrm{Sn}^{4+}$ |
| Ferrous ion | Ferric ion | Tin(II) ion | Tin(IV) ion |
| (From the Latin ferrum $=$ iron) | Stannous ion | Stannic ion |  |
| (From the Latin stannum $=$ tin) |  |  |  |

In any neutral compound, the total number of positive charges must equal the total number of negative charges. Thus, in any binary compound, you can always figure out the number of positive charges on a cation by counting the number of negative charges on the associated anion(s). In $\mathrm{FeCl}_{2}$, for example, the iron ion must be Fe (II) because there are two $\mathrm{Cl}^{-}$ions associated with it. Similarly, in $\mathrm{AlF}_{3}$ the aluminum ion is $\mathrm{Al}(\mathrm{III})$ because there are three $\mathrm{F}^{-}$anions associated with it. As a general rule, a Roman numeral is needed for transition metal compounds to avoid ambiguity. Metals in group 1A and group 2A form only one cation, though, so Roman numerals are not needed.

## Worked Example 2.9

Give systematic names for the following compounds:
(a) $\mathrm{BaCl}_{2}$
(b) $\mathrm{CrCl}_{3}$
(c) PbS
(d) $\mathrm{Fe}_{2} \mathrm{O}_{3}$

## Strategy

Try to figure out the number of positive charges on each cation by counting the number of negative charges on the associated anion(s). Refer to Figures 2.11 and 2.12 if you are unsure.

## Solution

(a) Barium chloride
(b) Chromium(III) chloride
(c) Lead(II) sulfide
(d) Iron(III) oxide

No Roman numeral is necessary because barium, a group 2A element, forms only $\mathrm{Ba}^{2+}$.
The Roman numeral III is necessary to specify the +3 charge on chromium (a transition metal).
The sulfide anion ( $\mathrm{S}^{2-}$ ) has a double negative charge, so the lead cation must be doubly positive.
The three oxide anions $\left(\mathrm{O}^{2-}\right)$ have a total negative charge of -6 , so the two iron cations must have a total charge of +6 . Thus, each is $\mathrm{Fe}(\mathrm{III})$.

## Worked Example 2.10

Write formulas for the following compounds:
(a) Magnesium fluoride
(b) $\operatorname{Tin}(\mathrm{IV})$ oxide
(c) Iron(III) sulfide

## Strategy

For transition metal compounds, the charge on the cation is indicated by the Roman numeral in the name. Knowing the number of positive charges, you can then figure out the number of necessary negative charges for the associated anions.

## Solution

(a) $\mathrm{MgF}_{2}$ Magnesium (group 2A) forms only a $2+$ cation, so there must be two fluoride ions $\left(\mathrm{F}^{-}\right)$to balance the charge.
(b) $\mathrm{SnO}_{2} \quad \mathrm{Tin}(\mathrm{IV})$ has a +4 charge, so there must be two oxide ions $\left(\mathrm{O}^{2-}\right)$ to balance the charge.
(c) $\mathrm{Fe}_{2} \mathrm{~S}_{3} \quad$ Iron(III) has a +3 charge and sulfide ion a -2 charge $\left(\mathrm{S}^{2-}\right)$, so there must be two irons and three sulfurs.

PROBLEM 2.15 Give systematic names for the following compounds:
(a) CsF
(b) $\mathrm{K}_{2} \mathrm{O}$
(c) CuO
(d) BaS
(e) $\mathrm{BeBr}_{2}$

PROBLEM 2.16 Write formulas for the following compounds:
(a) Vanadium(III) chloride
(b) Manganese(IV) oxide
(c) Copper(II) sulfide
(d) Aluminum oxide

KEY CONCEPT PROBLEM 2.17 Three binary ionic compounds are represented on the following periodic table: red with red, green with green, and blue with blue. Name each, and tell its likely formula.


## Naming Binary Molecular Compounds

Binary molecular compounds are named by assuming that one of the two elements in the molecule is more cationlike and the other element is more anionlike. As with ionic compounds, the cationlike element takes the name of the element itself, and the anionlike element takes an -ide ending. The compound HF, for example, is called hydrogen fluoride.

HF Hydrogen is more cationlike because it is farther left in the periodic table, and fluoride is more anionlike because it is farther right. The compound is therefore named hydrogen fluoride.
We'll see a quantitative way to decide which element is more cationlike and which is more anionlike in Section 7.4 but will note for now that it's usually possible to decide by looking at the relative positions of the elements in the periodic table. The farther left and toward the bottom of the periodic table an element occurs, the more likely it is to be cationlike; the farther right and toward the top an element occurs (except for the noble gases), the more likely it is to be anionlike.


The following examples show how this generalization applies:
CO Carbon monoxide ( C is in group 4 A ; O is in group 6 A )
$\mathrm{CO}_{2}$ Carbon dioxide
$\mathrm{PCl}_{3} \quad$ Phosphorus trichloride ( P is in group $5 \mathrm{~A} ; \mathrm{Cl}$ is in group 7A)
$\mathrm{SE}_{4} \quad$ Sulfur tetrafluoride ( S is in group 6A; F is in group 7A)
$\mathrm{N}_{2} \mathrm{O}_{4}$ Dinitrogen tetroxide ( N is in group $5 \mathrm{~A} ; \mathrm{O}$ is in group 6A)
Because nonmetals often combine in different proportions to form different compounds, numerical prefixes are usually included in the names of binary molecular compounds to specify the numbers of each kind of atom present. The



| TABLE 2.2 | Numerical Prefixes for unds |
| :---: | :---: |
| Naming |  |
| Prefix | Meaning |
| mono- | 1 |
| di- | 2 |
| tri- | 3 |
| tetra- | 4 |
| penta- | 5 |
| hexa- | 6 |
| hepta- | 7 |
| octa- | 8 |

## Naming Polyatomic

 lons activity

A These blue crystals of copper sulfate pentahydrate contain the $\mathrm{Cu}^{2+}$ cation and the polyatomic $\mathrm{SO}_{4}{ }^{2-}$ anion.
compound CO , for example, is called carbon monoxide, and $\mathrm{CO}_{2}$ is called carbon dioxide. Table 2.2 lists the most common prefixes. Note that when the prefix ends in $a$ or $o$ and the anion name begins with a vowel (oxide, for instance), the $a$ or $o$ on the prefix is dropped to avoid having two vowels together in the name. Thus, we write carbon monoxide rather than carbon monooxide and dinitrogen tetroxide rather than dinitrogen tetraoxide. Note also that the mono prefix is not used for the atom named first. $\mathrm{NO}_{2}$, for instance, is called nitrogen dioxide rather than mononitrogen dioxide.

## Worked Example 2.11

Give systematic names for the following compounds:
(a) $\mathrm{PCl}_{3}$
(b) $\mathrm{N}_{2} \mathrm{O}_{3}$
(c) $\mathrm{P}_{4} \mathrm{O}_{7}$
(d) $\mathrm{BrF}_{3}$

## Strategy

Look at a periodic table to see which element in each compound is more cationlike (farther to the left or lower) and which is more anionlike (farther to the right or higher). Then name the compound using the appropriate numerical prefix.

## SOlUTION

(a) Phosphorus trichloride
(b) Dinitrogen trioxide
(c) Tetraphosphorus heptoxide
(d) Bromine trifluoride

- PROBLEM 2.18 Give systematic names for the following compounds:
(a) $\mathrm{NCl}_{3}$
(b) $\mathrm{P}_{4} \mathrm{O}_{6}$
(c) $\mathrm{S}_{2} \mathrm{~F}_{2}$
(d) $\mathrm{SeO}_{2}$
- PROBLEM 2.19 Write formulas for compounds with the following names:
(a) Disulfur dichloride
(b) Iodine monochloride
(c) Nitrogen triiodide


## Naming Compounds with Polyatomic Ions

Ionic compounds containing polyatomic ions (Section 2.8) are named in the same way as binary ionic compounds: First the cation is identified and then the anion. For example, $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$ is called barium nitrate because $\mathrm{Ba}^{2+}$ is the cation and the $\mathrm{NO}_{3}{ }^{-}$polyatomic anion has the name nitrate. Unfortunately, there is no systematic way of naming the polyatomic ions themselves, so it's necessary to memorize the names, formulas, and charges of the most common ones listed in Table 2.3. The ammonium ion $\left(\mathrm{NH}_{4}{ }^{+}\right)$is the only cation on the list; all the others are anions.

Several points about the ions in Table 2.3 need special mention. First, note that the names of most polyatomic anions end in -ite or -ate; only hydroxide $\left(\mathrm{OH}^{-}\right)$, cyanide $\left(\mathrm{CN}^{-}\right)$, and peroxide $\left(\mathrm{O}_{2}{ }^{2-}\right)$ have the -ide ending. Second, note that several of the ions form a series of oxoanions, in which an atom of a given element is combined with different numbers of oxygen atoms-hypochlorite $\left(\mathrm{ClO}^{-}\right)$, chlorite $\left(\mathrm{ClO}_{2}^{-}\right)$, chlorate $\left(\mathrm{ClO}_{3}^{-}\right)$, and perchlorate $\left(\mathrm{ClO}_{4}^{-}\right)$, for example. When there are only two oxoanions in a series, as with sulfite $\left(\mathrm{SO}_{3}{ }^{2-}\right)$ and sulfate $\left(\mathrm{SO}_{4}{ }^{2-}\right)$, the ion with fewer oxygens takes the -ite ending and the ion with more oxygens takes the -ate ending.

$$
\begin{array}{llll}
\mathrm{SO}_{3}{ }^{2-} & \text { Sulfite ion (fewer oxygens) } & \mathrm{SO}_{4}{ }^{2-} & \text { Sulfate ion (more oxygens) } \\
\mathrm{NO}_{2}^{-} & \text {Nitrite ion (fewer oxygens) } & \mathrm{NO}_{3}^{-} & \text {Nitrate ion (more oxygens) }
\end{array}
$$

When there are more than two oxoanions in a series, the prefix hypo- (meaning "less than") is used for the ion with the fewest oxygens, and the prefix per- (meaning "more than") is used for the ion with the most oxygens.

[^2]TABLE 2.3 Some Common Polyatomic lons

| Formula | Name | Formula | Name |
| :---: | :---: | :---: | :---: |
| Cation |  | Singly charged anions (continued) |  |
| $\mathrm{NH}_{4}^{+}$ | Ammonium | $\mathrm{NO}_{2}{ }^{-}$ | Nitrite |
| Singly | ged anion | $\mathrm{NO}_{3}{ }^{-}$ | Nitrate |
| $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$ | Acetate | Doubly charged anions |  |
| $\mathrm{CN}^{-}$ | Cyanide | $\mathrm{CO}_{3}{ }^{2-}$ | Carbonate |
| $\mathrm{ClO}^{-}$ | Hypochlorite | $\mathrm{CrO}_{4}{ }^{2-}$ | Chromate |
| $\mathrm{ClO}_{2}{ }^{-}$ | Chlorite | $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ | Dichromate |
| $\mathrm{ClO}_{3}{ }^{-}$ | Chlorate | $\mathrm{O}_{2}{ }^{2-}$ | Peroxide |
| $\mathrm{ClO}_{4}^{-}$ | Perchlorate | $\mathrm{HPO}_{4}{ }^{2-}$ | Hydrogen phosphate |
| $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$ | Dihydrogen phosphate | $\mathrm{SO}_{3}{ }^{2-}$ | Sulfite |
| $\mathrm{HCO}_{3}{ }^{-}$ | Hydrogen carbonate (or bicarbonate) | $\begin{aligned} & \mathrm{SO}_{4}{ }^{2-} \\ & \mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-} \end{aligned}$ | Sulfate <br> Thiosulfate |
| $\mathrm{HSO}_{4}^{-}$ | Hydrogen sulfate (or bisulfate) | Triply charged anion |  |
| $\mathrm{OH}^{-}$ | Hydroxide | $\mathrm{PO}_{4}$ | Phosphate |
| $\mathrm{MnO}_{4}{ }^{-}$ | Permanganate |  |  |

Third, note that several pairs of ions are related by the presence or absence of a hydrogen. The hydrogen carbonate anion $\left(\mathrm{HCO}_{3}^{-}\right)$differs from the carbonate anion $\left(\mathrm{CO}_{3}{ }^{2-}\right)$ by the presence of $\mathrm{H}^{+}$, and the hydrogen sulfate anion $\left(\mathrm{HSO}_{4}^{-}\right)$ differs from the sulfate anion $\left(\mathrm{SO}_{4}{ }^{2-}\right)$ by the presence of $\mathrm{H}^{+}$. The ion that has the additional hydrogen is sometimes referred to using the prefix $b i$-, although this usage is now discouraged; for example, $\mathrm{NaHCO}_{3}$ is sometimes called sodium bicarbonate.

| $\mathrm{HCO}_{3}{ }^{-}$ | Hydrogen carbonate (bicarbonate) ion | $\mathrm{CO}_{3}{ }^{2-}$ | Carbonate ion |
| :--- | :--- | :--- | :--- |
| $\mathrm{HSO}_{4}{ }^{-}$ | Hydrogen sulfate (bisulfate) ion | $\mathrm{SO}_{4}{ }^{2-}$ | Sulfate ion |

## Worked Example 2.12

Give systematic names for the following compounds:
(a) $\mathrm{LiNO}_{3}$
(b) $\mathrm{KHSO}_{4}$
(c) $\mathrm{CuCO}_{3}$
(d) $\mathrm{Fe}\left(\mathrm{ClO}_{4}\right)_{3}$

## Strategy

The names and charges of the common polyatomic ions must be memorized. Refer to Table 2.3 if you need help.

## Solution

(a) Lithium nitrate
(b) Potassium hydrogen sulfate
(c) Copper(II) carbonate
(d) Iron(III) perchlorate

Lithium (group 1A) forms only the $\mathrm{Li}^{+}$ion and does not need a Roman numeral. Potassium (group 1A) forms only the $\mathrm{K}^{+}$ion. The carbonate ion has a -2 charge, so copper must be +2 . A Roman numeral is needed because copper, a transition metal, can form more than one ion.
There are three perchlorate ions, each with a -1 charge, so the iron must have a +3 charge.

Steven J. Hawkes, "A Mnemonic for Oxy-Anions,"
J. Chem. Educ., Vol. 67, 1990, 149.

## Worked Example 2.13

Write formulas for the following compounds:
(a) Potassium hypochlorite
(b) Silver(I) chromate
(c) Iron(III) carbonate

## Solution

(a) KClO
Potassium forms only the $\mathrm{K}^{+}$ion, so only one $\mathrm{ClO}^{-}$is needed.
(b) $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$
The polyatomic chromate ion has a -2 charge, so two $\mathrm{Ag}^{+}$ions are needed.
(c) $\mathrm{Fe}_{2}\left(\mathrm{CO}_{3}\right)_{3}$
Iron(III) has a +3 charge and the polyatomic carbonate ion has a -2 charge, so there must be two iron ions and three carbonate ions. The polyatomic carbonate ion is set off in parentheses to indicate that there are three of them.

PROBLEM 2.20 Give systematic names for the following compounds:
(a) $\mathrm{Ca}(\mathrm{ClO})_{2}$
(b) $\mathrm{Ag}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$
(c) $\mathrm{NaH}_{2} \mathrm{PO}_{4}$
(d) $\mathrm{Sn}\left(\mathrm{NO}_{3}\right)_{2}$
(e) $\mathrm{Pb}\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)_{4}$
(f) $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{SO}_{4}$

PROBLEM 2.21 Write formulas for the following compounds:
(a) Lithium phosphate
(b) Magnesium hydrogen sulfate
(c) Manganese(II) nitrate
(d) Chromium(III) sulfate

- KEY CONCEPT PROBLEM 2.22 The following drawings are those of solid ionic compounds, with green spheres representing the cations and blue spheres representing the anions in each.


Which of the following formulas are consistent with each drawing?
(a) LiBr
(b) $\mathrm{NaNO}_{2}$
(c) $\mathrm{CaCl}_{2}$
(d) $\mathrm{K}_{2} \mathrm{CO}_{3}$
(e) $\mathrm{Fe}_{2}\left(\mathrm{SO}_{4}\right)_{3}$

## Naming Acids

Most acids are oxoacids; that is, they contain oxygen in addition to hydrogen and another element. When dissolved in water, an oxoacid yields one or more $\mathrm{H}^{+}$ions and a polyatomic oxoanion, such as one of those listed in Table 2.4.

The names of oxoacids are related to the names of the corresponding oxoanions described previously, with the -ite or -ate ending of the anion name replaced by -ous acid or -ic acid, respectively. In other words, the acid with fewer oxygens has an -ous ending, and the acid with more oxygens has an -ic ending. The compound $\mathrm{HNO}_{2}$, for example, is called nitrous acid because it has fewer oxygens and yields the nitrite ion $\left(\mathrm{NO}_{2}^{-}\right)$when dissolved in water. $\mathrm{HNO}_{3}$ is called nitric acid because it has more oxygens and yields the nitrate ion $\left(\mathrm{NO}_{3}^{-}\right)$when dissolved in water.

Nitrous acid gives nitrite ion

$$
\mathrm{HNO}_{2}(l) \xrightarrow{\text { Dissolve in water }} \mathrm{H}^{+}(a q)+\mathrm{NO}_{2}^{-}(a q)
$$

Nitric acid gives nitrate ion

$$
\mathrm{HNO}_{3}(l) \xrightarrow{\text { Dissolve in water }} \mathrm{H}^{+}(a q)+\mathrm{NO}_{3}^{-}(a q)
$$

TABLE 2.4 Some Common Oxoacids and Their Anions

| Oxoacid |  | Oxoanion |  |
| :--- | :--- | :--- | :--- |
| $\mathrm{HNO}_{2}$ | Nitrous acid | $\mathrm{NO}_{2}{ }^{-}$ | Nitrite ion |
| $\mathrm{HNO}_{3}$ | Nitric acid | $\mathrm{NO}_{3}{ }^{-}$ | Nitrate ion |
| $\mathrm{H}_{3} \mathrm{PO}_{4}$ | Phosphoric acid | $\mathrm{PO}_{4}{ }^{3-}$ | Phosphate ion |
| $\mathrm{H}_{2} \mathrm{SO}_{3}$ | Sulfurous acid | $\mathrm{SO}_{3}{ }^{2-}$ | Sulfite ion |
| $\mathrm{H}_{2} \mathrm{SO}_{4}$ | Sulfuric acid | $\mathrm{SO}_{4}{ }^{2-}$ | Sulfate ion |
| HClO | Hypochlorous acid | $\mathrm{ClO}^{-}$ | Hypochlorite ion |
| $\mathrm{HClO}_{2}$ | Chlorous acid | $\mathrm{ClO}_{2}^{-}$ | Chlorite ion |
| $\mathrm{HClO}_{3}$ | Chloric acid | $\mathrm{ClO}_{3}{ }^{-}$ | Chlorate ion |
| $\mathrm{HClO}_{4}$ | Perchloric acid | $\mathrm{ClO}_{4}^{-}$ | Perchlorate ion |

In a similar way, hypochlorous acid yields the hypochlorite ion, chlorous acid yields the chlorite ion, chloric acid yields the chlorate ion, and perchloric acid yields the perchlorate ion (Table 2.4).

In addition to the oxoacids, there are a small number of other acids, such as HCl , that do not contain oxygen. Although the pure, gaseous compound HCl is named hydrogen chloride according to the rules for binary compounds, the aqueous solution is named hydrochloric acid, $\mathrm{HCl}(a q)$. This example is typical of non-oxygen-containing acids: The prefix hydro- and the suffix -ic acid are used for the aqueous solution in such cases.
$\begin{array}{lll}\text { Hydrogen chloride } & \mathrm{HCl}(g) \xrightarrow{\text { Dissolve in water }} \mathrm{HCl}(a q) & \text { Hydrochloric acid } \\ \text { Hydrogen bromide } & \mathrm{HBr}(g) \xrightarrow{\text { Dissolve in water }} \mathrm{HBr}(a q) & \text { Hydrobromic acid }\end{array}$

## Worked Example 2.14

Name the following acids:
(a) $\mathrm{HBrO}(a q)$
(b) $\operatorname{HCN}(a q)$

## Strategy

To name an acid, look at the formula and decide whether the compound is an oxoacid. If so, the name must reflect the number of oxygen atoms, according to Table 2.4. If the compound is not an oxoacid, it is named using the prefix hydro- and the suffix -ic acid.

## Solution

(a) This compound is an oxoacid that yields hypobromite ion $\left(\mathrm{BrO}^{-}\right)$when dissolved in water. Its name is hypobromous acid.
(b) This compound is not an oxoacid but yields cyanide ion when dissolved in water. As a pure gas, HCN is named hydrogen cyanide. In water solution, it is called hydrocyanic acid.

- PROBLEM 2.23 Name the following acids:
(a) $\mathrm{HIO}_{4}$
(b) $\mathrm{HBrO}_{2}$
(c) $\mathrm{H}_{2} \mathrm{CrO}_{4}$


## -



- Pure HCl is a colorless gas; hydrochloric acid is an aqueous solution of HCl .


## Interlude <br> Are Atoms Real?



This image of atoms on the surface of a
nickel crystal was taken by a scanning tunnickel crystal wase.
neling microscope

The atomic theory of matter is at the heart of chemistry. Every chemical reaction and every law that describes the behavior of matter is explained by chemists in terms of atoms. But how do we know that atoms are real? The best answer to that question is that we can now actually "see" individual atoms with a remarkable device called a scanning tunneling microscope, or STM. Invented in 1981 by a research team at the IBM Corporation, this special microscope has achieved magnifications of up to 10 million, allowing chemists to look directly at individual atoms.

The principle behind the operation of an STM is shown in Figure 2.13. A sharp tungsten probe, whose tip is only one or two atoms across, is brought near the surface of the sample, and a small voltage is applied. When the tip comes within a few atomic diameters of the sample, a small electric current flows from the sample to the probe in a process called electron tunneling. The strength of the current flow is extremely sensitive to the distance between sample and probe, varying by as much as 1000 -fold over a distance of just 100 pm (about one atomic diameter.) Passing the probe across the sample while moving it up and down over individual atoms to keep current flow constant gives a two-dimensional map of the probe's path. By then moving the probe back and forth in a series of closely spaced parallel tracks, a three-dimensional image of the surface can be constructed.

The kind of image produced by scanning tunneling microscopy is quite different from the kind of image we see with our eyes. A normal visual image results when light from the sun or other source reflects off an object, strikes the retina in our eye, and is converted into electrical signals that are processed by the brain. The image obtained with a scanning tunneling microscope, by contrast, is a three-dimensional, computer-generated data plot that uses tunneling current to mimic depth perception. The nature of the computer-generated image depends on the identity of the molecules or atoms on the surface, on the precision with which the probe tip is made, on how the data are manipulated, and on other experimental variables.


A FIGURE 2.13 A scanning tunneling microscope works by moving an extremely fine probe along the surface of a sample, applying a small voltage, and measuring current flow between atoms in the sample and the atom at the tip of the probe. By raising and lowering the moving probe to keep current flow constant as the tip passes over atoms, a map of the surface can be obtained.

Most of the present uses of the scanning tunneling microscope involve studies of surface chemistry. Processes such as the deposition of monomolecular layers on smooth surfaces can be studied, the nature of industrial catalysts can be probed, and metal corrosion can be examined. The possibility also exists that complex biological structures can be determined with the STM.

PROBLEM 2.24 How does the image obtained by a scanning tunneling microscope differ from that obtained by the usual optical microscope?

## Summary

Elements are made of tiny particles called atoms, which can combine in simple numerical ratios according to the law of multiple proportions. Atoms are composed of three fundamental particles: Protons are positively charged, electrons are negatively charged, and neutrons are neutral. According to the nuclear model of an atom proposed by Ernest Rutherford, protons and neutrons are clustered into a dense core called the nucleus, while electrons move around the nucleus at a relatively large distance.

Elements differ from one another according to how many protons their atoms contain, a value called the atomic number $(Z)$ of the element. The sum of an atom's protons and neutrons is its mass number ( $A$ ). Although all atoms of a specific element have the same atomic number, different atoms of an element can have different mass numbers, depending on how many neutrons they have. Atoms with identical atomic numbers but different mass numbers are called isotopes. Atomic masses are measured using the atomic mass unit (amu), defined as $1 / 12$ the mass of a ${ }^{12} \mathrm{C}$ atom. Because both protons and neutrons have a mass of approximately 1 amu , the mass of an atom in atomic mass units (the isotopic mass) is numerically close to the atom's mass number. The element's atomic mass is a weighted mass average for naturally occurring isotope mixtures.

Most substances on Earth are chemical compounds, formed when atoms of two or more elements combine in a
chemical reaction. The atoms in a compound are held together by one of two kinds of chemical bonds. Covalent bonds form when two atoms share electrons to give a new unit of matter called a molecule. Ionic bonds form when one atom completely transfers one or more electrons to another atom, resulting in the formation of ions. Positively charged ions (cations) are strongly attracted to negatively charged ions (anions) by electrical forces.

The hydrogen ion $\left(\mathrm{H}^{+}\right)$and the polyatomic hydroxide ion $\left(\mathrm{OH}^{-}\right)$are among the most important ions in chemistry because they are fundamental to the idea of acids and bases. According to one common definition, an acid is a substance that yields $\mathrm{H}^{+}$ions when dissolved in water, and a base is a substance that yields $\mathrm{OH}^{-}$ions when dissolved in water.

All chemical compounds can be named systematically by following a series of rules. Binary ionic compounds are named by identifying first the positive ion and then the negative ion. Binary molecular compounds are similarly named by identifying the cationlike and anionlike elements. Naming compounds with polyatomic ions involves memorizing the names and formulas of the most common ones. Most acids are oxoacids, and are named according to how many oxygen atoms they contain.

## Key Words

acid 55
alpha ( $\alpha$ ) particle 43
anion 54
atom 40
atomic mass 48
atomic mass unit (amu) 48
atomic number (Z) 46
base 55
cathode ray 41
cation 54
chemical bond 51
chemical compound 49
chemical equation 50
chemical formula 49
chemical reaction 49
covalent bond 51
electron 41
element 38
heterogeneous mixture 50
homogeneous mixture 50
ion 54
ionic bond 54
ionic solid 54
isotope 46
law of definite proportions 39
law of mass
conservation 39
law of multiple proportions 40
mass number (A) 46
mixture 50
molecule 51
neutron 44
nucleus 44
oxoacid 62
oxoanion 60
polyatomic ion 54
proton 44
structural formula 52

## Key Concept Summary



## Understanding Key Concepts

Problems 2.1-2.24 appear within the chapter.
2.25 If yellow spheres represent sulfur atoms and red spheres represent oxygen atoms, which of the follow-
ing drawings shows a collection of sulfur dioxide molecules? Which drawing represents a mixture?

2.26 Assume that the mixture of substances in drawing (a) undergoes a reaction. Which of the drawings (b)-(d) represents a product mixture consistent with the law of mass conservation?

(a)


(b)

(c)

(d)
2.27 If red and blue spheres represent atoms of different elements, which two of the following drawings illustrate the law of multiple proportions?

2.28 Give molecular formulas corresponding to each of the following ball-and-stick molecular representations $($ red $=\mathrm{O}$, gray $=\mathrm{C}$, blue $=\mathrm{N}$, ivory $=\mathrm{H})$. In writing the formula, list the atoms in alphabetical order.
(a) Alanine (an amino acid)
(b) Ethylene glycol (automobile antifreeze)
(c) Acetic acid (vinegar)

2.29 Which of the following drawings represents an Na atom? $\mathrm{A} \mathrm{Ca}^{2+}$ ion? $\mathrm{An} \mathrm{F}^{-}$ion?


(a)

(b)

(c)
2.30 Indicate where in the periodic table the following elements are found:
(a) Elements that commonly form anions
(b) Elements that commonly form cations
(c) Elements that commonly form covalent bonds


## Additional Problems

## Atomic Theory

2.32 How does Dalton's atomic theory account for the law of mass conservation and the law of definite proportions?
2.33 What is the law of multiple proportions, and how is it predicted by Dalton's atomic theory?
2.34 Benzene, ethane, and ethylene are just three of a large number of hydrocarbons-compounds that contain only carbon and hydrogen. Show how the following data are consistent with the law of multiple proportions.

| Compound | Mass of Carbon <br> in $\mathbf{5 . 0 0} \mathbf{g ~ S a m p l e}$ | Mass of Hydrogen <br> in $\mathbf{5 . 0 0} \mathbf{g}$ Sample |
| :--- | :--- | :--- |
| Benzene | 4.61 g | 0.39 g |
| Ethane | 4.00 g | 1.00 g |
| Ethylene | 4.29 g | 0.71 g |

2.35 In addition to carbon monoxide ( CO ) and carbon dioxide $\left(\mathrm{CO}_{2}\right)$, there is a third compound of carbon and oxygen called carbon suboxide. If a 2.500 g sample of carbon suboxide contains 1.32 g of C and 1.18 g of O , show that the law of multiple proportions is followed.
2.31 In the following drawings, red spheres represent cations and blue spheres represent anions. Match each of the drawings (a)-(d) with the following ionic compounds:
(a) $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$
(b) $\mathrm{Li}_{2} \mathrm{CO}_{3}$
(c) $\mathrm{FeCl}_{2}$
(d) $\mathrm{MgSO}_{4}$

(a)

(c)

(b)

(d)
2.40 A binary compound of zinc and sulfur contains $67.1 \%$ zinc by mass. What is the ratio of zinc and sulfur atoms in the compound?
2.41 There are two binary compounds of titanium and chlorine. One compound contains $31.04 \%$ titanium by mass, and the other contains $74.76 \%$ chlorine by mass. What are the ratios of titanium and chlorine atoms in the two compounds?

## Elements and Atoms

2.42 What is the difference between an atom's atomic number and its mass number?
2.43 What is the difference between an element's atomic number and its atomic mass?
2.44 What is an isotope?
2.45 Carbon-14 and nitrogen-14 both have the same mass number, yet they are different elements. Explain.
2.46 The subscript giving the atomic number of an atom is often left off when writing an isotope symbol. For example, ${ }_{6}^{13} \mathrm{C}$ is often written simply as ${ }^{13} \mathrm{C}$. Why is this allowable?
2.47 Iodine has a lower atomic mass than tellurium (126.90 for iodine versus 127.60 for tellurium) even though it has a higher atomic number ( 53 for iodine versus 52 for tellurium). Explain.
2.48 Give names and symbols for the following elements:
(a) An element with atomic number 6
(b) An element with 18 protons in its nucleus
(c) An element with 23 electrons
2.49 The radioactive isotope cesium-137 was produced in large amounts in fallout from the 1985 nuclear powerplant disaster at Chernobyl, Ukraine. Write the symbol for this isotope in standard format.
2.50 Write standard symbols for the following isotopes:
(a) Radon-220
(b) Polonium-210
(c) Gold-197
2.51 Write symbols for the following isotopes:
(a) $Z=58$ and $A=140$
(b) $Z=27$ and $A=60$
2.52 How many protons, neutrons, and electrons are in each of the following atoms?
(a) ${ }_{7}^{15} \mathrm{~N}$
(b) ${ }_{27}^{60} \mathrm{Co}$
(c) ${ }_{53}^{131} \mathrm{I}$
(d) ${ }_{58}^{14} \mathrm{Ce}$
2.53 How many protons and neutrons are in the nucleus of the following atoms?
(a) ${ }^{27} \mathrm{Al}$
(b) ${ }^{32} \mathrm{~S}$
(c) ${ }^{64} \mathrm{Zn}$
(d) ${ }^{207} \mathrm{~Pb}$
2.54 Identify the following elements:
(a) ${ }_{12}^{24} X$
(b) ${ }_{28}^{58} \mathrm{X}$
(c) ${ }_{46}^{104} \mathrm{X}$
(d) ${ }_{74}^{183} x$
2.55 Identify the following elements:
(a) ${ }_{80}^{202} \mathrm{X}$
(b) ${ }_{78}^{195} \mathrm{X}$
(c) ${ }_{76}^{184} \mathrm{X}$
(d) ${ }_{83}^{209} x$
2.56 Naturally occurring boron consists of two isotopes: ${ }^{10} B$ (19.9\%) with an isotopic mass of 10.0129 amu and ${ }^{11} \mathrm{~B}$ ( $80.1 \%$ ) with an isotopic mass of 11.00931 amu . What is the atomic mass of boron? Check your answer by looking at a periodic table.
2.57 Naturally occurring silver consists of two isotopes: ${ }^{107} \mathrm{Ag}$ ( $51.84 \%$ ) with an isotopic mass of 106.9051 amu and ${ }^{109} \mathrm{Ag}(48.16 \%)$ with an isotopic mass of 108.9048 amu. What is the atomic mass of silver? Check your answer in a periodic table.
2.58 Magnesium has three naturally occurring isotopes: ${ }^{24} \mathrm{Mg}$ ( 23.985 amu ) with $78.99 \%$ abundance, ${ }^{25} \mathrm{Mg}$ ( 24.986 amu ) with $10.00 \%$ abundance, and a third with $11.01 \%$ abundance. Look up the atomic mass of magnesium, and then calculate the mass of the third isotope.
2.59 A sample of naturally occurring silicon consists of ${ }^{28} \mathrm{Si}$ (27.9769 amu), ${ }^{29} \mathrm{Si}(28.9765 \mathrm{amu})$, and ${ }^{30} \mathrm{Si}(29.9738$ amu ). If the atomic mass of silicon is 28.0855 amu and the natural abundance of ${ }^{29} \mathrm{Si}$ is $4.67 \%$, what are the natural abundances of ${ }^{28} \mathrm{Si}$ and ${ }^{30} \mathrm{Si}$ ?

## Compounds and Mixtures, Molecules and Ions

2.60 Which of the following mixtures are homogeneous and which are heterogeneous?
(a) Muddy water
(b) Concrete
(c) House paint
(d) A soft drink
2.61 Which of the following mixtures are homogeneous?
(a) 18 karat gold
(b) Window glass
(c) Tomato juice
(d) Liquefied air
2.62 What is the difference between an atom and a molecule? Give an example of each.
2.63 What is the difference between a molecule and an ion? Give an example of each.
2.64 What is the difference between a covalent bond and an ionic bond? Give an example of each.
2.65 Which of the following bonds are likely to be covalent and which ionic? Explain.
(a) $\mathrm{B}-\mathrm{Br}$
(b) $\mathrm{Na}-\mathrm{Br}$
(c) $\mathrm{Br}-\mathrm{Cl}$
(d) $\mathrm{O}-\mathrm{Br}$
2.66 The symbol CO stands for carbon monoxide, but the symbol Co stands for the element cobalt. Explain.
2.67 Correct the error in each of the following statements:
(a) The formula of ammonia is NH3.
(b) Molecules of potassium chloride have the formula KCl .
(c) $\mathrm{Cl}^{-}$is a cation.
(d) $\mathrm{CH}_{4}$ is a polyatomic ion.
2.68 How many protons and electrons are in each of the following ions?
(a) $\mathrm{Be}^{2+}$
(b) $\mathrm{Rb}^{+}$
(c) $\mathrm{Se}^{2-}$
(d) $\mathrm{Au}^{3+}$
2.69 What is the identity of the element $X$ in the following ions?
(a) $\mathrm{X}^{2+}$, a cation that has 36 electrons
(b) $\mathrm{X}^{-}$, an anion that has 36 electrons
2.70 The structural formula of isopropyl alcohol, better known as "rubbing alcohol," is shown. What is the chemical formula of isopropyl alcohol?


Isopropyl alcohol
2.71 Lactic acid, a compound found both in sour milk and in tired muscles, has the structure shown. What is its chemical formula?


Lactic acid
2.72 Butane, the fuel used in disposable lighters, has the formula $\mathrm{C}_{4} \mathrm{H}_{10}$. The carbon atoms are connected in the sequence $\mathrm{C}-\mathrm{C}-\mathrm{C}-\mathrm{C}$, and each carbon has a total of four covalent bonds. Draw a structural formula for butane.
2.73 Isooctane, the substance in gasoline from which the term octane rating derives, has the formula $\mathrm{C}_{8} \mathrm{H}_{18}$. Each carbon has a total of four covalent bonds, and the atoms are connected in the sequence shown. Draw a complete structural formula for isooctane.


## Acids and Bases

2.74 Which of the following compounds are acids and which are bases?
(a) HI
(b) CsOH
(c) $\mathrm{H}_{3} \mathrm{PO}_{4}$
(d) $\mathrm{Ba}(\mathrm{OH})_{2}$
(e) $\mathrm{H}_{2} \mathrm{CO}_{3}$
2.75 For each of the acids you identified in Problem 2.74, tell how many $\mathrm{H}^{+}$ions can be donated from one molecule of acid.
2.76 Identify the anion that results when each of the acids in Problem 2.74 dissolves in water.
2.77 Identify the cation that results when each of the bases in Problem 2.74 dissolves in water.

## Naming Compounds

2.78 Write formulas for the following binary compounds:
(a) Potassium chloride
(b) Tin(II) bromide
(c) Calcium oxide
(d) Barium chloride
(e) Aluminum hydride
2.79 Write formulas for the following compounds:
(a) Calcium acetate
(b) Iron(II) cyanide
(c) Sodium dichromate
(d) Chromium(III) sulfate
(e) Mercury(II) perchlorate
2.80 Name the following ions:
(a) $\mathrm{Ba}^{2+}$
(b) $\mathrm{Cs}^{+}$
(c) $\mathrm{V}^{3+}$
(d) $\mathrm{HCO}_{3}^{-}$
(e) $\mathrm{NH}_{4}^{+}$
(f) $\mathrm{Ni}^{2+}$
(g) $\mathrm{NO}_{2}{ }^{-}$
(h) $\mathrm{ClO}_{2}^{-}$
(i) $\mathrm{Mn}^{2+}$
(j) $\mathrm{ClO}_{4}^{-}$
2.81 Name the following binary molecular compounds:
(a) $\mathrm{CCl}_{4}$
(b) $\mathrm{ClO}_{2}$
(c) $\mathrm{N}_{2} \mathrm{O}$
(d) $\mathrm{N}_{2} \mathrm{O}_{3}$
2.82 Give the formulas and charges of the following ions:
(a) Sulfite ion
(b) Phosphate ion
(c) Zirconium(IV) ion
(d) Chromate ion
(e) Acetate ion
(f) Thiosulfate ion
2.83 What are the charges on the positive ions in the following compounds?
(a) $\mathrm{Zn}(\mathrm{CN})_{2}$
(b) $\mathrm{Fe}\left(\mathrm{NO}_{2}\right)_{3}$
(c) $\mathrm{Ti}\left(\mathrm{SO}_{4}\right)_{2}$
(d) $\mathrm{Sn}_{3}\left(\mathrm{PO}_{4}\right)_{2}$
(e) $\mathrm{Hg}_{2} \mathrm{~S}$
(f) $\mathrm{MnO}_{2}$
(g) $\mathrm{KIO}_{4}$
(h) $\mathrm{Cu}\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)_{2}$
2.84 Name each of the compounds in Problem 2.83.
2.85 Name each of the following compounds:
(a) $\mathrm{MgSO}_{3}$
(b) $\mathrm{Co}\left(\mathrm{NO}_{2}\right)_{2}$
(c) $\mathrm{Mn}\left(\mathrm{HCO}_{3}\right)_{2}$
(d) $\mathrm{ZnCrO}_{4}$
(e) $\mathrm{BaSO}_{4}$
(f) $\mathrm{KMnO}_{4}$
(g) $\mathrm{Al}_{2}\left(\mathrm{SO}_{4}\right)_{3}$
(h) $\mathrm{LiClO}_{3}$
2.86 Fill in the missing information to give formulas for the following compounds:
(a) $\mathrm{Na}_{3} \mathrm{SO}_{4}$
(b) $\mathrm{Ba}_{?}\left(\mathrm{PO}_{4}\right)$ ?
(c) $\mathrm{Ga}_{?}\left(\mathrm{SO}_{4}\right)_{\text {? }}$
2.87 Write formulas for each of the following compounds:
(a) Sodium peroxide
(b) Aluminum bromide
(c) Chromium(III) sulfate

## General Problems

2.88 Germanium has five naturally occurring isotopes: ${ }^{70} \mathrm{Ge}$, $20.5 \%, 69.924 \mathrm{amu} ;{ }^{72} \mathrm{Ge}, 27.4 \%, 71.922 \mathrm{amu} ;{ }^{73} \mathrm{Ge}, 7.8 \%$, $72.923 \mathrm{amu} ;{ }^{74} \mathrm{Ge}, 36.5 \%, 73.921 \mathrm{amu}$; and ${ }^{76} \mathrm{Ge}, 7.8 \%$, 75.921 amu . What is the atomic mass of germanium?
2.89 The best balances commonly found in laboratories can weigh amounts as small as $10^{-5} \mathrm{~g}$. If you were to count out carbon atoms at the rate of two per second, how long would it take you to count a pile of atoms large enough to weigh?
2.90 Name the following compounds:
(a) $\mathrm{NaBrO}_{3}$
(b) $\mathrm{H}_{3} \mathrm{PO}_{4}$
(c) $\mathrm{H}_{3} \mathrm{PO}_{3}$
(d) $\mathrm{V}_{2} \mathrm{O}_{5}$
2.91 Write formulas for the following compounds:
(a) Calcium hydrogen sulfate
(b) Tin(II) oxide
(c) Ruthenium(III) nitrate
(d) Ammonium carbonate
(e) Hydriodic acid
(f) Beryllium phosphate
2.92 Ammonia $\left(\mathrm{NH}_{3}\right)$ and hydrazine $\left(\mathrm{N}_{2} \mathrm{H}_{4}\right)$ are both binary compounds of nitrogen and hydrogen. Based on the law of multiple proportions, how many grams of hydrogen would you expect 2.34 g of nitrogen to combine with to yield ammonia? To yield hydrazine?
2.93 If 3.670 g of nitrogen combines with 0.5275 g of hydrogen to yield compound $X$, how many grams of nitrogen would combine with 1.575 g of hydrogen to make the same compound? Is X ammonia or hydrazine (Problem 2.92)?
2.94 Tellurium, a group 6A element, forms the oxoanions $\mathrm{TeO}_{4}{ }^{2-}$ and $\mathrm{TeO}_{3}{ }^{2-}$. What are the likely names of these ions? To what other group 6A oxoanions are they analogous?
2.95 Give the formulas and the likely names of the acids derived from the tellurium-containing oxoanions in Problem 2.94.
2.96 Identify the following atoms or ions:
(a) A halogen anion with 54 electrons
(b) A metal cation with 79 protons and 76 electrons
(c) A noble gas with $A=84$
2.97 Prior to 1961, the atomic mass unit was defined as $1 / 16$ the mass of the atomic mass of oxygen. That is, the atomic mass of oxygen was defined as exactly 16 amu . What was the mass of a ${ }^{12} \mathrm{C}$ atom prior to 1961 if the atomic mass of oxygen on today's scale is 15.9994 amu ?
2.98 What was the mass in atomic mass units of a ${ }^{40} \mathrm{Ca}$ atom prior to 1961 if its mass on today's scale is 39.9626 amu ? (See Problem 2.97.)
2.99 Analogous oxoanions of elements in the same group of the periodic table are named similarly. Based on the names of the oxoanions of phosphorus and sulfur, name the following anions:
(a) $\mathrm{AsO}_{4}{ }^{3-}$
(b) $\mathrm{SeO}_{3}{ }^{2-}$
(c) $\mathrm{SeO}_{4}{ }^{2-}$
(d) $\mathrm{HAsO}_{4}{ }^{2-}$
2.100 Identify the following atoms or ions, and where possible, write the symbol for the specific isotope. If not enough information is given to answer the question, say so.
(a) An alkaline earth metal atom with 20 protons and 20 neutrons
(b) A metal atom with 63 neutrons
(c) A 3+ cation with 23 electrons and 30 neutrons
(d) A 2- anion with 34 protons
2.101 Fluorine occurs naturally as a single isotope. How many protons, neutrons, and electrons are present in one molecule of deuterium fluoride? Is deuterium fluoride an acid or a base? (Deuterium is ${ }^{2} \mathrm{H}$.)
2.102 Hydrogen has three isotopes ( ${ }^{1} \mathrm{H},{ }^{2} \mathrm{H}$, and $\left.{ }^{3} \mathrm{H}\right)$, and chlorine has two isotopes ( ${ }^{35} \mathrm{Cl}$ and $\left.{ }^{37} \mathrm{Cl}\right)$. How many kinds of HCl molecules are there? Write the formula for each, and tell how many protons, neutrons, and electrons each contains.
2.103 Give the number of protons, neutrons, and electrons in each of the following atoms or ions:
(a) ${ }^{40} \mathrm{Ar}$
(b) ${ }^{40} \mathrm{Ca}^{2+}$
(c) ${ }^{39} \mathrm{~K}^{+}$
(d) ${ }^{35} \mathrm{Cl}^{-}$
2.104 Each of the following pairs of elements will react to form an ionic compound. Write the formula of each compound formed, and give its name.
(a) Magnesium and chlorine
(b) Calcium and oxygen
(c) Lithium and nitrogen
(d) Aluminum and oxygen
2.105 Cyclohexane, used as a paint and varnish remover, has the formula $\mathrm{C}_{6} \mathrm{H}_{12}$. In this molecule, each C atom is bonded to two H atoms and two other C atoms, and each H atom is bonded to one C atom. Write a structural formula for cyclohexane.
2.106 Pentane, a solvent that is found in petroleum, has the formula $\mathrm{C}_{5} \mathrm{H}_{12}$. In a $\mathrm{C}_{5} \mathrm{H}_{12}$ molecule, each C atom forms four bonds, and each H atom forms one bond. Write three possible structural formulas for pentane.
2.107 A 9.520 g quantity of zinc was allowed to react with 40.00 mL of sulfuric acid that had a density of 1.3028 $\mathrm{g} / \mathrm{mL}$. The reaction yielded $\mathrm{H}_{2}$ gas and a solution of zinc sulfate. The density of the gas was determined to be $0.0899 \mathrm{~g} / \mathrm{L}$, and the mass of the solution was found to be 61.338 g . How many liters of $\mathrm{H}_{2}$ were formed?
2.108 The molecular mass of a molecule is the sum of the atomic masses of all atoms in the molecule. What is the molecular mass of acetaminophen, $\mathrm{C}_{8} \mathrm{H}_{9} \mathrm{NO}_{2}$, the active ingredient in Tylenol?
2.109 The mass percent of an element in a compound is the mass of the element (total mass of the element's atoms in the molecule) divided by the mass of the compound (total mass of all atoms in the molecule) times $100 \%$. What is the mass percent of each element in acetaminophen? (See Problem 2.108.)
2.110 Aspirin contains $\mathrm{C}, \mathrm{H}$, and O in the following mass percents: C, $60.00 \%$; H, $4.48 \%$; and O, $35.52 \%$. (See Problems 2.108 and 2.109.)
(a) Is aspirin likely to be an ionic compound or a molecular compound?
(b) What is a possible formula for aspirin?
2.111 Element $X$ reacts with element $Y$ to give a product containing $\mathrm{X}^{3+}$ ions and $\mathrm{Y}^{2-}$ ions.
(a) Is element X likely to be a metal or a nonmetal? Explain.
(b) Is element Y likely to be a metal or a nonmetal? Explain.
(c) What is the formula of the product?
(d) What groups of the periodic table are elements $X$ and $Y$ likely to be in?
2.112 Zinc has atomic mass $A=65.39$ and has five naturally occurring isotopes: ${ }^{64} \mathrm{Zn}, 48.63 \%, 63.929 \mathrm{amu} ;{ }^{66} \mathrm{Zn}$, $27.90 \%$, ? amu; ${ }^{67} \mathrm{Zn}, 4.10 \%, 66.927 \mathrm{amu} ;{ }^{68} \mathrm{Zn}, 18.75 \%$, 67.925 amu ; and ${ }^{70} \mathrm{Zn}, 0.62 \%, 69.925 \mathrm{amu}$. What is the isotopic mass of ${ }^{66} \mathrm{Zn}$ ?

## eMedia Problems

2.113 After using the Multiple Proportions activity (eChapter 2.2) for NO and $\mathrm{NO}_{2}$, perform calculations similar to those in the activity to show how $\mathrm{SO}_{2}$ and $\mathrm{SO}_{3}$ also illustrate the law of multiple proportions. Draw pictures similar to those in Problem 2.25 to represent collections of $\mathrm{SO}_{2}$ and $\mathrm{SO}_{3}$ molecules.
2.114 The Rutherford Experiment movie (eChapter 2.4) shows alpha particles impinging on a thin gold foil. Describe what happens to the alpha particles and discuss how the results of this experiment shaped the modern view of atomic structure.
2.115 After using the Isotopes of Hydrogen activity (eChapter 2.5), draw pictures of the two naturally occurring isotopes of boron ( ${ }^{10} \mathrm{~B}$ and ${ }^{11} \mathrm{~B}$ ).
2.116 Use the Mixtures and Compounds activity (eChapter 2.7) to develop a flow chart for identifying substances as heterogeneous mixtures, homogeneous mixtures, compounds, or elements.
2.117 Find the names of $\mathrm{NO}_{2}^{-}$and $\mathrm{NO}_{3}^{-}$and the names of $\mathrm{SO}_{3}{ }^{2-}$ and $\mathrm{SO}_{4}{ }^{2-}$ in the Polyatomic Ions activity (eChapter 2.8). Based on these names, predict the names of the ions $\mathrm{ClO}_{3}{ }^{-}$and $\mathrm{ClO}_{4}^{-}$. Use the activity to check your names.
2.118 In the Naming Ionic Compounds activity (eChapter 2.10) there are 3 cations that form soluble compounds with all of the anions listed. Write the names and symbols for these cations. There are also 3 anions that form soluble compounds with all of the cations listed. Write the names and symbols for these anions.

## Chapter

## Formulas, Equations, and Moles

## It's sometimes possible when

 beginning the study of chemistry to forget that reactions are at the heart of the science. New words, ideas, and principles are sometimes introduced so quickly that the central concern of chemistry-the change of one substance into another-gets lost in the rush. In this chapter, we'll begin learning about how to describe chemical reactions, starting with a look at the conventions for writing chemical equations and at the necessary mass relationships between reactants and products. Because most chemical reactions are carried out using solutions rather than pure materials, we'll alsoAmmonium nitrate is so reactive that it can explode when heated.

## CONTENTS

3.1 Balancing Chemical Equations
3.2 Chemical Symbols on Different Levels
3.3 Avogadro's Number and the Mole
3.4 Stoichiometry: Chemical Arithmetic
3.5 Yields of Chemical Reactions
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3.7 Concentrations of Reactants in Solution: Molarity
3.8 Diluting Concentrated Solutions

[^3]Di William C. Herndon, "On Balancing Chemical Equations: Past and Present (A Critical Review and Annotated Bibliography)," $J$. Chem. Educ., Vol. 74, 1997, 1359-1362.

Zoltan Toth, "Balancing
Chemical Equations by Inspection," J. Chem. Educ., Vol. 74, 1997, 1363-1364.

Balancing Equations activity

VEquations may be balanced using fractions. $\mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(l)$ is a balanced equation.
discuss units for describing the concentration of a solution. Finally, we'll see how chemical formulas are determined and how molecular masses are measured.

### 3.1 Balancing Chemical Equations

The previous two chapters have provided several examples of reactions: hydrogen reacting with oxygen to yield water, sodium reacting with chlorine to yield sodium chloride, mercury(II) nitrate reacting with potassium iodide to yield mercury(II) iodide, and so forth. We can write equations for these reactions in the following format:


Look carefully at how these equations are written. Because we know from Section 2.8 that hydrogen, oxygen, and chlorine exist as covalent $\mathrm{H}_{2}, \mathrm{O}_{2}$, and $\mathrm{Cl}_{2}$ diatomic molecules rather than as isolated atoms, we must write them as such in the chemical equations. Now look at the atoms on each side of the reaction arrow. In each equation, the numbers and kinds of atoms on both sides of the arrow are identical, and the equations are therefore said to be balanced.

The requirement that an equation be balanced is a direct consequence of the mass conservation law discussed in Section 2.1: All chemical equations must balance because atoms are neither created nor destroyed in chemical reactions. The numbers and kinds of atoms must be the same in the products as in the reactants.

Balancing a chemical equation involves finding out how many formula units of each different substance take part in the reaction. A formula unit, as the name implies, is one unit-whether atom, ion, or molecule-corresponding to a given formula. One formula unit of NaCl , for example, is one $\mathrm{Na}^{+}$ion and one $\mathrm{Cl}^{-}$ion; one formula unit of $\mathrm{MgBr}_{2}$ is one $\mathrm{Mg}^{2+}$ ion and two $\mathrm{Br}^{-}$ions; and one formula unit of $\mathrm{H}_{2} \mathrm{O}$ is one $\mathrm{H}_{2} \mathrm{O}$ molecule.

Complicated equations usually need to be balanced using a systematic method, but simpler equations can often be balanced using a mixture of common sense and trial-and-error:

1. Write the unbalanced equation using the correct chemical formula for each reactant and product. In the reaction of hydrogen with oxygen to yield water, for example, we begin by writing:

$$
\mathrm{H}_{2}+\mathrm{O}_{2} \longrightarrow \mathrm{H}_{2} \mathrm{O}
$$

2. Find suitable coefficients-the numbers placed before formulas to indicate how many formula units of each substance are required to balance the equation. Only these coefficients can be changed when balancing an equation; the formulas themselves can't be changed. Again taking the reaction of hydrogen with oxygen as an example, we can balance the equation by adding a coefficient of 2 to both $\mathrm{H}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$. By so doing, we now have 4 hydrogen atoms and 2 oxygen atoms on each side of the equation:


It might seem easier at first glance to balance the equation simply by adding a subscript 2 to the oxygen atom in water, thereby changing $\mathrm{H}_{2} \mathrm{O}$ into
$\mathrm{H}_{2} \mathrm{O}_{2}$. That's not allowed, however, because the resulting equation would no longer describe the same reaction. The substances $\mathrm{H}_{2} \mathrm{O}$ (water) and $\mathrm{H}_{2} \mathrm{O}_{2}$ (hydrogen peroxide) are two entirely different compounds. Water is a substance used for drinking and swimming; hydrogen peroxide is a substance used for bleaching hair and sterilizing wounds.

$$
\mathrm{H}_{2}+\mathrm{O}_{2} \longrightarrow \mathrm{H}_{2} \mathrm{O}_{2} \begin{aligned}
& \text { NOT ALLOWED! } \\
& \text { When this subscript is added, we get } \\
& \text { a completely different reaction. }
\end{aligned}
$$

3. Reduce the coefficients to their smallest whole-number values, if necessary, by dividing them by a common divisor.
4. Check your answer by making sure that the numbers and kinds of atoms are the same on both sides of the equation.
Let's work through some additional examples to see how equations are balanced.

## Worked Example 3.1

Propane, $\mathrm{C}_{3} \mathrm{H}_{8}$, is a colorless, odorless gas often used as a heating and cooking fuel in campers and rural homes. Write a balanced equation for the combustion reaction of propane with oxygen to yield carbon dioxide and water.

## Strategy and Solution

Follow the four steps just described:
Step 1 Write the unbalanced equation using correct chemical formulas for all substances:

$$
\mathrm{C}_{3} \mathrm{H}_{8}+\mathrm{O}_{2} \longrightarrow \mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O} \quad \text { Unbalanced }
$$

Step 2 Find coefficients to balance the equation. It's usually best to start with the most complex substance-in this case $\mathrm{C}_{3} \mathrm{H}_{8}$-and to deal with one element at a time. Look first at the unbalanced equation, and note that there are 3 carbon atoms on the left side of the equation but only 1 on the right side. If we add a coefficient of 3 to $\mathrm{CO}_{2}$ on the right, the carbons balance:

$$
\mathrm{C}_{3} \mathrm{H}_{8}+\mathrm{O}_{2} \longrightarrow 3 \mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O} \quad \text { Balanced for } \mathrm{C}
$$

Next, look at the number of hydrogen atoms. There are 8 hydrogens on the left but only 2 (in $\mathrm{H}_{2} \mathrm{O}$ ) on the right. By adding a coefficient of 4 to the $\mathrm{H}_{2} \mathrm{O}$ on the right, the hydrogens balance:

$$
\mathrm{C}_{3} \mathrm{H}_{8}+\mathrm{O}_{2} \longrightarrow 3 \mathrm{CO}_{2}+4 \mathrm{H}_{2} \mathrm{O} \quad \text { Balanced for } \mathrm{C} \text { and } \mathrm{H}
$$

Finally, look at the number of oxygen atoms. There are 2 on the left but 10 on the right; by adding a coefficient of 5 to the $\mathrm{O}_{2}$ on the left, the oxygens balance:

$$
\mathrm{C}_{3} \mathrm{H}_{8}+5 \mathrm{O}_{2} \longrightarrow 3 \mathrm{CO}_{2}+4 \mathrm{H}_{2} \mathrm{O} \quad \text { Balanced for } \mathrm{C}, \mathrm{H} \text {, and } \mathrm{O}
$$

Step 3 Make sure the coefficients are reduced to their smallest whole-number values. In fact, our answer is already correct, but we might have arrived at a different answer through trial and error:

$$
2 \mathrm{C}_{3} \mathrm{H}_{8}+10 \mathrm{O}_{2} \longrightarrow 6 \mathrm{CO}_{2}+8 \mathrm{H}_{2} \mathrm{O}
$$

Although the preceding equation is balanced, the coefficients are not the smallest whole numbers. It would be necessary to divide all coefficients by 2 to reach the final equation.

Step 4 Check your answer. Count the numbers and kinds of atoms on both sides of the equation to make sure they're the same:



A Propane is used as a fuel in camp stoves and in rural homes.

## Worked Example 3.2

The major ingredient in ordinary safety matches is potassium chlorate, $\mathrm{KClO}_{3}$, a substance that can act as a source of oxygen in combustion reactions. Its reaction with ordinary table sugar (sucrose, $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$ ), for example, occurs violently to yield potassium chloride, carbon dioxide, and water. Write a balanced equation for the reaction.

## Strategy and Solution

Step 1 Write the unbalanced equation, making sure the formulas for all substances are correct:

$$
\mathrm{KClO}_{3}+\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11} \longrightarrow \mathrm{KCl}+\mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O} \quad \text { Unbalanced }
$$

Step 2 Find coefficients to balance the equation by starting with the most complex substance (sucrose) and considering one element at a time. Since there are 12 C atoms on the left and only 1 on the right, we can balance for carbon by adding a coefficient of 12 to $\mathrm{CO}_{2}$ :

$$
\mathrm{KClO}_{3}+\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11} \longrightarrow \mathrm{KCl}+12 \mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O} \quad \text { Balanced for } \mathrm{C}
$$

Since there are 22 H atoms on the left and only 2 on the right, we can balance for hydrogen by adding a coefficient of 11 to $\mathrm{H}_{2} \mathrm{O}$ :

$$
\mathrm{KClO}_{3}+\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11} \rightarrow \mathrm{KCl}+12 \mathrm{CO}_{2}+11 \mathrm{H}_{2} \mathrm{O} \quad \text { Balanced for } \mathrm{C} \text { and } \mathrm{H}
$$

Since there are now 35 O atoms on the right but only 14 on the left ( 11 in sucrose and 3 in $\mathrm{KClO}_{3}$ ), 21 oxygens must be added on the left. We can do this without disturbing the C and H balance by adding 7 more $\mathrm{KClO}_{3}{ }^{\prime}$ s, giving a coefficient of 8 for $\mathrm{KClO}_{3}$ :
$8 \mathrm{KClO}_{3}+\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11} \longrightarrow \mathrm{KCl}+12 \mathrm{CO}_{2}+11 \mathrm{H}_{2} \mathrm{O} \quad$ Balanced for $\mathrm{C}, \mathrm{H}$ and O
Potassium and chlorine can both be balanced by adding a coefficient of 8 to KCl :


Steps 3 and 4 The coefficients in the balanced equation are already reduced to their smallest whole-number values, and a check shows that the numbers and kinds of atoms are the same on both sides of the equation.


A Safety matches contain potassium chlorate, which acts as a source of oxygen for ignition.

## Worked Key Concept Example 3.3

Write a balanced equation for the reaction of element A (red spheres) with element $B$ (blue spheres) as represented below.


## Strategy

Balancing the reactions shown in graphic representations of this sort is just a matter of counting the numbers of products and reactant units. In this example, the reactant box contains three red $A_{2}$ molecules and nine blue $B_{2}$ molecules, while the product box contains six $\mathrm{AB}_{3}$ molecules with no reactant left over.

## Solution

$$
3 \mathrm{~A}_{2}+9 \mathrm{~B}_{2} \longrightarrow 6 \mathrm{AB}_{3} \quad \text { or } \quad \mathrm{A}_{2}+3 \mathrm{~B}_{2} \longrightarrow 2 \mathrm{AB}_{3}
$$

PROBLEM 3.1 Potassium chlorate, $\mathrm{KClO}_{3}$, decomposes when heated to yield potassium chloride and oxygen, a reaction used to provide oxygen for the emergency breathing masks in airliners. Balance the equation.

- PROBLEM 3.2 Balance the following equations:
(a) $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6} \rightarrow \mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}+\mathrm{CO}_{2}$ (fermentation of sugar to yield ethyl alcohol)
(b) $\mathrm{Fe}+\mathrm{O}_{2} \rightarrow \mathrm{Fe}_{2} \mathrm{O}_{3}$ (rusting of iron)
(c) $\mathrm{NH}_{3}+\mathrm{Cl}_{2} \rightarrow \mathrm{~N}_{2} \mathrm{H}_{4}+\mathrm{NH}_{4} \mathrm{Cl}$ (synthesis of hydrazine for rocket fuel)
-KEY CONCEPT PROBLEM 3.3 Write a balanced equation for the reaction of element A (red spheres) with element B (green spheres) as represented below.



## $3.2 \mid$ Chemical Symbols on Different Levels

What does it mean to write a chemical formula or equation? Answering this question isn't as easy as it sounds because a chemical symbol can have different meanings under different circumstances. Chemists use the same symbols to represent both a small-scale, microscopic level and a large-scale, macroscopic level, and they tend to slip back and forth between the two levels without realizing the confusion this can cause for newcomers to the field.

On the microscopic level, chemical symbols represent the behavior of individual atoms and molecules. Atoms and molecules are much too small to be seen, but we can nevertheless describe their microscopic behavior if we read the equation $2 \mathrm{H}_{2}+\mathrm{O}_{2} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}$ to mean "Two molecules of hydrogen react with one molecule of oxygen to yield two molecules of water." It's this microscopic world that we deal with when trying to understand how reactions occur, and it's often helpful in this regard to visualize a molecule as a collection of spheres stuck together. In trying to understand how $\mathrm{H}_{2}$ reacts with $\mathrm{O}_{2}$, for example, you might picture $\mathrm{H}_{2}$ and $\mathrm{O}_{2}$ molecules as made of two spheres pressed together and a water molecule as made of three spheres.


On the macroscopic level, formulas and equations represent the large-scale behaviors of atoms and molecules that give rise to visible properties. In other words, the symbols $\mathrm{H}_{2}, \mathrm{O}_{2}$, and $\mathrm{H}_{2} \mathrm{O}$ represent not just single molecules but vast numbers of molecules that together have a set of measurable physical properties. A single isolated $\mathrm{H}_{2} \mathrm{O}$ molecule is neither solid nor liquid nor gas, but a huge collection of $\mathrm{H}_{2} \mathrm{O}$ molecules appears to us as a colorless liquid that freezes at $0^{\circ} \mathrm{C}$ and boils at $100^{\circ} \mathrm{C}$. Clearly, it's this macroscopic behavior we deal with in the laboratory when we weigh out specific amounts of reactants, place them in a flask, and observe visible changes.

What does a chemical formula or equation mean at any particular time? It means whatever you want it to mean depending on the context. The symbol $\mathrm{H}_{2} \mathrm{O}$ can mean either one tiny, invisible molecule or a vast collection of molecules large enough to swim in.

© Ethyl chloride is often used as a spray-on anesthetic for athletic injuries.


## $3.3 \mid$ Avogadro's Number and the Mole

Imagine a laboratory experiment-perhaps the reaction of ethylene $\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)$ with hydrogen chloride $(\mathrm{HCl})$ to prepare ethyl chloride $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}\right)$, a colorless, lowboiling liquid that doctors and athletic trainers use as a spray-on anesthetic for minor injuries.


How much ethylene and how much hydrogen chloride should you use for your experiment? According to the coefficients of the balanced equation, a 1:1 numerical ratio of the two reactants is needed. But because molecules are so small and the number of molecules needed to make a visible sample is so large, your experiment must involve a vast number of ethylene molecules-say $10^{20}$ or morereacting with an equally vast number of hydrogen chloride molecules. Unfortunately, though, you can't count the reactant molecules so you have to weigh them. That is, you must convert a number ratio of reactant molecules as given by coefficients in the balanced equation into a mass ratio you can weigh to be sure you are using the right amounts.

Mass ratios are determined by using the molecular masses (also called molecular weights) of the substances involved in a reaction. Just as the atomic mass of an element is the average mass of the element's atoms, the molecular mass of a substance is the average mass of the substance's molecules. Numerically, molecular mass (or more generally formula mass) equals the sum of the atomic masses of all atoms in the molecule.

$$
\begin{array}{ll}
\text { molecular mass } & \text { Sum of atomic masses of all atoms in a molecule. } \\
\text { Formula mass } & \begin{array}{l}
\text { Sum of atomic masses of all atoms in a formula unit of } \\
\text { any compound, molecular or ionic. }
\end{array}
\end{array}
$$

As examples, the molecular mass of ethylene is 28.0 amu , the molecular mass of hydrogen chloride is 36.5 amu , the molecular mass of ethyl chloride is 64.5 amu , and the formula mass of sodium chloride is 58.5 amu . (These numbers are rounded off to one decimal place for convenience; the actual values are known more precisely.)

$$
\begin{aligned}
& \text { For ethylene, } \mathrm{C}_{2} \mathrm{H}_{4} \text { : } \\
& \text { at. mass of } 2 \mathrm{C}=2 \times 12.0 \mathrm{amu}=24.0 \mathrm{amu} \\
& \begin{array}{ll}
\text { at. mass of } 4 \mathrm{H}=4 \times 1.0 \mathrm{amu} & =4.0 \mathrm{amu} \\
\hline \text { Molec. mass of } \mathrm{C}_{2} \mathrm{H}_{4} & =28.0 \mathrm{amu}
\end{array} \\
& \text { For ethyl chloride, } \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl} \text { : } \\
& \text { at. mass of } 2 \mathrm{C}=2 \times 12.0 \mathrm{amu}=24.0 \mathrm{amu} \\
& \text { at. mass of } 5 \mathrm{H}=5 \times 1.0 \mathrm{amu}=5.0 \mathrm{amu} \\
& \text { at. mass of } \mathrm{Cl}=35.5 \mathrm{amu} \\
& \text { Molec. mass of } \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}=64.5 \mathrm{amu}
\end{aligned}
$$

For hydrogen chloride, HCl :
at. mass of $\mathrm{H}=1.0 \mathrm{amu}$
at. mass of $\mathrm{Cl}=35.5 \mathrm{amu}$
Molec. mass of $\mathrm{HCl}=36.5$
For sodium chloride, NaCl :
at. mass of $\mathrm{Na} \quad=23.0 \mathrm{amu}$
at. mass of $\mathrm{Cl}=35.5 \mathrm{amu}$
Form. mass of $\mathrm{NaCl}=58.5 \mathrm{amu}$

How do we use molecular masses? Because the mass ratio of one HCl molecule to one ethylene molecule is $36.5: 28.0$, the mass ratio of any given number of HCl molecules to the same number of ethylene molecules is always 36.5:28.0. In other words, a 36.5:28.0 mass ratio of HCl and ethylene corresponds to a 1:1 number ratio. Equal numbers of different molecules (or formula units) always have a mass ratio equal to their molecular (or formula) mass ratio (Figure 3.1).


A particularly convenient way to use this mass-number relationship is to measure amounts in grams that are numerically equal to molecular masses. If, for instance, you were to carry out your experiment with 36.5 g of HCl and 28.0 g of ethylene, you could be certain that you have the correct 1:1 number ratio of reactant molecules.

When referring to the enormous numbers of molecules or ions that take part in a visible chemical reaction, it's convenient to use a special unit called a mole, abbreviated mol. One mole of any substance is the amount whose mass-its molar mass-is equal to the molecular or formula mass of the substance in grams. One mole of ethylene has a mass of 28.0 g , one mole of HCl has a mass of 36.5 g , one mole of NaCl has a mass of 58.5 g , and so on. (To be more precise, one mole is formally defined as the amount of a substance that contains the same number of molecules or formula units as there are atoms in exactly 12 g of carbon-12.)

Just how many molecules are there in a mole? Experiments show that one mole of any substance contains $6.022 \times 10^{23}$ formula units, a value called Avogadro's number (abbreviated $N_{\mathrm{A}}$ ) after the Italian scientist who first recognized the importance of the mass/number relationship. Avogadro's number of formula units of any substance-that is, one mole-has a mass in grams equal to

A FIGURE 3.1 (a) Because one gumdrop weighs more than one jellybean, you can't get equal numbers merely by taking equal weights. The same is true for different atoms or molecules. (b) Equal numbers of HCl and ethylene molecules always have a mass ratio equal to the ratio of their molecular masses, 36.5:28.0.

$\square$Dawn M. Wakeley and Hans de Grys, "Developing an Intuitive Approach to Moles," J. Chem. Educ., Vol. 77, 2000, 1007-1009.
Di. Henk van Lubeck, "How to Visualize Avogadro's Number," J. Chem. Educ., Vol. 66, 1989 762. the molecular or formula mass of the substance.

Molec. mass of $\mathrm{HCl}=36.5 \mathrm{amu}$
Molec. mass of $\mathrm{C}_{2} \mathrm{H}_{4}=28.0 \mathrm{amu}$
Molec. mass of $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}=64.5 \mathrm{amu}$
Form. mass of $\mathrm{NaCl}=58.5 \mathrm{amu}$

Molar mass of $\mathrm{HCl}=36.5 \mathrm{~g}$
Molar mass of $\mathrm{C}_{2} \mathrm{H}_{4}=28.0 \mathrm{~g}$
Molar mass of $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}=64.5 \mathrm{~g}$
Molar mass of $\mathrm{NaCl}=58.5 \mathrm{~g}$
$1 \mathrm{~mol} \mathrm{HCl}=6.022 \times 10^{23} \mathrm{HCl}$ molecules
1 mole $\mathrm{C}_{2} \mathrm{H}_{4}=6.022 \times 10^{23} \mathrm{C}_{2} \mathrm{H}_{4}$ molecules
1 mole $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}=6.022 \times 10^{23} \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}$ molecules
1 mole $\mathrm{NaCl}=6.022 \times 10^{23} \mathrm{NaCl}$ formula units

Although it's hard to grasp the magnitude of a quantity as large as Avogadro's number, a few comparisons might give you a sense of scale:


William Laurita, "Demonstrations for Nonscience Majors: Using Common Objects to Illustrate Abstract Concepts," J. Chem. Educ., Vol. 67, 1990, 60-61. A demonstration of the measurement of Avogadro's number.

Miriam Toloudis, "The Size of a Mole," J. Chem. Educ., Vol. 73, 1996, 348.

Damon Diemente, "Demonstrations of the Enormity of Avogadro's Number," J. Chem. Educ., Vol. 75, 1998, 1565-1566.

(D]
Carmela Merlo and Kathleen E. Turner, "A Mole of M\&M's," J. Chem. Educ., Vol. 70, 1993, 453.

Sheryl Dominic, "What's a Mole For?" J. Chem. Educ., Vol. 73, 1996, 309.


A These samples of table sugar, lead shot, potassium dichromate, mercury, water, copper, sodium chloride, and sulfur each contain 1 mole. Do they have the same mass?

In effect, molar mass acts as a conversion factor between numbers of molecules and mass. If you know the mass of a sample, you can calculate how many molecules you have; if you know how many molecules you have, you can calculate their total mass. Note, though, that it's always necessary when using a molar mass to specify the formula of the substance you're talking about. For example, 1 mol of hydrogen atoms, H , has a molar mass of $1.0 \mathrm{~g} / \mathrm{mol}$, but 1 mol of hydrogen molecules, $\mathrm{H}_{2}$, has a molar mass of $2.0 \mathrm{~g} / \mathrm{mol}$.

In any balanced chemical equation, the coefficients tell how many moles of each substance are needed for the reaction. You can then use molar masses to calculate reactant masses. If you saw the following balanced equation for the industrial synthesis of ammonia, for example, you would know that 3 mol of $\mathrm{H}_{2}(3 \mathrm{~mol} \times 2.0 \mathrm{~g} / \mathrm{mol}=6.0 \mathrm{~g})$ is needed for reaction with 1 mol of $\mathrm{N}_{2}(28.0 \mathrm{~g})$ to yield 2 mol of $\mathrm{NH}_{3}(2 \mathrm{~mol} \times 17.0 \mathrm{~g} / \mathrm{mol}=34.0 \mathrm{~g})$.


## Worked Example 3.4

What is the molecular mass of sucrose, $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$ ? What is the molar mass of sucrose in grams per mole?

## Strategy

The molecular mass of a substance is the sum of the atomic masses of the constituent atoms. First, list the elements present in the molecule, and then look up the atomic mass of each (we'll round off to one decimal place for convenience):

$$
\mathrm{C}(12.0 \mathrm{amu}) ; \mathrm{H}(1.0 \mathrm{amu}) ; \mathrm{O}(16.0 \mathrm{amu})
$$

Then, multiply the atomic mass of each element by the number of times that element appears in the chemical formula, and total the results.

## Solution

$$
\begin{aligned}
\mathrm{C}_{12}(12 \times 12.0 \mathrm{amu}) & =144.0 \mathrm{amu} \\
\mathrm{H}_{22}(22 \times 1.0 \mathrm{amu}) & =22.0 \mathrm{amu} \\
\mathrm{O}_{11}(11 \times 16.0 \mathrm{amu}) & =176.0 \mathrm{amu} \\
\hline \text { Molec. mass of } \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11} & =342.0 \mathrm{amu}
\end{aligned}
$$

Since one molecule of sucrose has a mass of $342.0 \mathrm{amu}, 1 \mathrm{~mol}$ of sucrose has a mass of 342.0 grams. Thus, the molar mass of sucrose is $342.0 \mathrm{~g} / \mathrm{mol}$.

- PROBLEM 3.4 Calculate the formula mass or molecular mass of the following substances:
(a) $\mathrm{Fe}_{2} \mathrm{O}_{3}$ (rust)
(b) $\mathrm{H}_{2} \mathrm{SO}_{4}$ (sulfuric acid)
(c) $\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{7}$ (citric acid)
(d) $\mathrm{C}_{16} \mathrm{H}_{18} \mathrm{~N}_{2} \mathrm{O}_{4} \mathrm{~S}$ (penicillin G)

PROBLEM 3.5 The commercial production of iron from iron ore involves the reaction of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ with CO to yield iron metal plus carbon dioxide:

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+\mathrm{CO}(g) \longrightarrow \mathrm{Fe}(s)+\mathrm{CO}_{2}(g)
$$

Balance the equation, and predict how many moles of CO will react with 0.500 mol of $\mathrm{Fe}_{2} \mathrm{O}_{3}$.

- KEY CONCEPT PROBLEM 3.6 Methionine, an amino acid used by organisms to make proteins, can be represented by the following ball-and-stick molecular model. Give the formula for methionine, and calculate its molecular mass (red $=\mathrm{O}$, gray $=\mathrm{C}$, blue $=\mathrm{N}$, yellow $=\mathrm{S}$, ivory $=\mathrm{H}$ ).



## 3.4 | Stoichiometry: Chemical Arithmetic

We saw in Section 3.3 that the coefficients in a balanced equation tell the numbers of moles of substances in a reaction. In actual laboratory work, though, it's necessary to convert between moles and mass to be sure that the correct amounts of reactants are used. In referring to these mole-mass relationships, we use the word stoichiometry (stoy-key-ahm-uh-tree; from the Greek stoicheion, "element," and metron, "measure"). Let's look again at the reaction of ethylene with HCl to see how stoichiometric relationships are used.

$$
\mathrm{C}_{2} \mathrm{H}_{4}(g)+\mathrm{HCl}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}(g)
$$

Let's assume that we have 15.0 g of ethylene and we need to know how many grams of HCl to use in the reaction. According to the coefficients in the balanced equation, 1 mol of HCl is required for reaction with each mole of ethylene. To find out how many grams of HCl are required to react with 15.0 g of ethylene, we first have to find out how many moles of ethylene are in 15.0 g . We do

Shanthi R. Krishnan and Ann C. Howe, "The Mole Concept: Developing an Instrument to Assess Conceptual Understanding," J. Chem. Educ., Vol. 71, 1994, 635-655.

Addison Ault, "How to Say How Much: Amounts and Stoichiometry," J. Chem. Educ., Vol. 78, 2001, 1347-1348.

$\square$Richard L. Poole, "Teaching Stoichiometry: A Two-Cycle Approach," J. Chem. Educ., Vol. 66, 1989, 57.


FIGURE 3.2 A summary of conversions between moles and grams for a chemical reaction. The numbers of moles tell how many molecules of each reactant are needed, as given by the coefficients of the balanced equation; the numbers of grams tell what mass of each reactant is needed.

[^4]this gram-to-mole conversion by calculating the molar mass of ethylene and using that value as a conversion factor:

```
Molecular mass of \(\mathrm{C}_{2} \mathrm{H}_{4}=(2 \times 12.0 \mathrm{amu})+(4 \times 1.0 \mathrm{amu})=28.0 \mathrm{amu}\)
Molar mass of \(\mathrm{C}_{2} \mathrm{H}_{4}=28.0 \mathrm{~g} / \mathrm{mol}\)
Moles of \(\mathrm{C}_{2} \mathrm{H}_{4}=15.0\) g ethylene \(\times \frac{1 \mathrm{~mol} \text { ethylene }}{28.0 \text { gethylene }}=0.536\) mol ethylene
```

Now that we know how many moles of ethylene we have ( 0.536 mol ), we also know from the balanced equation how many moles of HCl we need ( 0.536 mol ), and we have to do a mole-to-gram conversion to find the mass of HCl required. Once again, the conversion is done by calculating the molecular mass of HCl and using molar mass as a conversion factor:

$$
\begin{gathered}
\text { Molecular mass of } \mathrm{HCl}=1.0 \mathrm{amu}+35.5 \mathrm{amu}=36.5 \mathrm{amu} \\
\text { Molar mass of } \mathrm{HCl}=36.5 \mathrm{~g} / \mathrm{mol} \\
\text { Grams of } \mathrm{HCl}=0.536 \mathrm{molC}_{2} \mathrm{H}_{4} \times \frac{1 \mathrm{molHCl}}{1 \mathrm{~mol}_{2} \mathrm{H}_{4}} \times \frac{36.5 \mathrm{~g} \mathrm{HCl}}{1 \mathrm{molHCl}}=19.6 \mathrm{~g} \mathrm{HCl}
\end{gathered}
$$

Thus, 19.6 g of HCl is needed to react with 15.0 g of ethylene.
Look carefully at the sequence of steps in the calculation just completed. Moles (numbers of molecules) are given by the balanced equation but grams are used to weigh reactants in the laboratory. Moles tell us how many molecules of each reactant we need; grams tell us how much mass of each reactant we need.

$$
\begin{aligned}
& \text { Moles } \longrightarrow \text { Numbers of molecules or formula units } \\
& \text { Grams } \longrightarrow \text { Mass }
\end{aligned}
$$

The flow diagram in Figure 3.2 illustrates the necessary conversions. Note again that you can't go directly from the number of grams of one reactant to the number of grams of another reactant. You must first convert to moles.

## Worked Example 3.5

How many moles of sucrose are in a tablespoon of sugar that contains 2.85 g ?

## Strategy

The problem gives the mass of sucrose and asks for a mass-to-mole conversion. Use the molar mass of sucrose as a conversion factor, and set up an equation so that the unwanted unit cancels.

## Solution

$$
\begin{aligned}
2.85 \mathrm{~g} \text { sucrose } \times \frac{1 \mathrm{~mol} \text { sucrose }}{342.0 \text { g-stuerose }} & =0.00833 \mathrm{~mol} \text { sucrose } \\
& =8.33 \times 10^{-3} \mathrm{~mol} \text { sucrose }
\end{aligned}
$$

$\checkmark$ BALLPARK CHECK Because the molecular mass of sucrose (calculated in Worked Example 3.4) is $342.0 \mathrm{amu}, 1 \mathrm{~mol}$ of sucrose has a mass of 342.0 g . Thus, 2.85 g of sucrose is a bit less than one-hundredth of a mole, or 0.01 mol . The ballpark check agrees with the solution.

## Worked Example 3.6

How many grams are in 0.0626 mol of $\mathrm{NaHCO}_{3}$, the main ingredient in Alka-Seltzer tablets?

## Strategy

The problem gives the number of moles of $\mathrm{NaHCO}_{3}$ and asks for a mole-to-mass conversion. First, calculate the formula mass and molar mass of $\mathrm{NaHCO}_{3}$. Then use molar mass as a conversion factor, and set up an equation so that the unwanted unit cancels.

## Solution

Form. mass of $\mathrm{NaHCO}_{3}=23.0 \mathrm{amu}+1.0 \mathrm{amu}+12.0 \mathrm{amu}+(3 \times 16.0 \mathrm{amu})=84.0 \mathrm{amu}$ Molar mass of $\mathrm{NaHCO}_{3}=84.0 \mathrm{~g} / \mathrm{mol}$

$$
0.0626 \mathrm{~mol} \mathrm{NaHCO}_{3} \times \frac{84.0 \mathrm{~g} \mathrm{NaHCO}_{3}}{1 \mathrm{~mol} \mathrm{NaHCO}_{3}}=5.26 \mathrm{~g} \mathrm{NaHCO}_{3}
$$

## Worked Example 3.7

Aqueous solutions of sodium hypochlorite ( NaOCl ), best known as household bleach, are prepared by reaction of sodium hydroxide with chlorine:

$$
2 \mathrm{NaOH}(a q)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{NaOCl}(a q)+\mathrm{NaCl}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

How many grams of NaOH are needed to react with 25.0 g of $\mathrm{Cl}_{2}$ ?

## Strategy

Finding the relationship between numbers of reactant formula units always requires working in moles. The general strategy was outlined in Figure 3.2 and is reproduced below:


## Solution

First, find out how many moles of $\mathrm{Cl}_{2}$ are in 25.0 g of $\mathrm{Cl}_{2}$. This gram-to-mole conversion is done in the usual way, using the molar mass of $\mathrm{Cl}_{2}(70.9 \mathrm{~g} / \mathrm{mol})$ as the conversion factor:

$$
25.0 \mathrm{~g} \mathrm{Cl}_{2} \times \frac{1 \mathrm{~mol} \mathrm{Cl}_{2}}{70.9 \mathrm{gCl}_{2}}=0.353 \mathrm{~mol} \mathrm{Cl}_{2}
$$

Next, look at the coefficients in the balanced equation. Each mole of $\mathrm{Cl}_{2}$ reacts with 2 mol of NaOH , so 0.353 mol of $\mathrm{Cl}_{2}$ reacts with $2 \times 0.353=0.706 \mathrm{~mol}$ of NaOH . With


Karla R. Krieger, "Stoogiometry: A Cognitive Approach to Teaching Stoichiometry," J. Chem. Educ., Vol. 74, 1997, 306-309.

$\square$
John J. Fortman, "Pictorial Analogies XII: Stoichiometric Calculations," J. Chem. Educ., Vol. 71, 1994, 571-572.
the number of moles of NaOH known, carry out a mole-to-gram conversion using the molar mass of $\mathrm{NaOH}(40.0 \mathrm{~g} / \mathrm{mol})$ as a conversion factor:

$$
\begin{aligned}
\text { Grams of } \mathrm{NaOH} & =0.353 \mathrm{molCl}_{2} \times \frac{2 \mathrm{~mol} \mathrm{NaOH}}{1 \mathrm{molCl}_{2}} \times \frac{40.0 \mathrm{~g} \mathrm{NaOH}}{1 \mathrm{~mol} \mathrm{NaOH}} \\
& =28.2 \mathrm{~g} \mathrm{NaOH}
\end{aligned}
$$

The problem can also be worked by combining the steps and setting up one large equation:

$$
\begin{aligned}
& \text { Grams of } \mathrm{NaOH}=25.0 \mathrm{~g} \mathrm{Cl} \\
& \mathrm{~g}
\end{aligned} \frac{1 \mathrm{molet}_{2}}{70.9 \mathrm{get}_{2}} \times \frac{2 \mathrm{~mol} \mathrm{NaOH}}{1 \mathrm{molCl}_{2}} \times \frac{40.0 \mathrm{~g} \mathrm{NaOH}}{1 \mathrm{~mol} \mathrm{NaOH}}
$$

$\sqrt{ }$ Ballpark Check The molar mass of NaOH is about half that of $\mathrm{Cl}_{2}$, and 2 mol of NaOH is needed per 1 mol of $\mathrm{Cl}_{2}$. Thus, the needed mass of NaOH will be similar to that of $\mathrm{Cl}_{2}$, about 25 g .


- PROBLEM 3.7 Aspirin has the formula $\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}_{4}$. How many moles of aspirin are in a tablet weighing 500 mg ? How many molecules?
- PROBLEM 3.8 Aspirin is prepared by reaction of salicylic acid $\left(\mathrm{C}_{7} \mathrm{H}_{6} \mathrm{O}_{3}\right)$ with acetic anhydride $\left(\mathrm{C}_{4} \mathrm{H}_{6} \mathrm{O}_{3}\right)$ according to the following equation:


How many grams of acetic anhydride are needed to react with 4.50 g of salicylic acid? How many grams of aspirin will result? How many grams of acetic acid are formed as a by-product?

## 3.5 | Yields of Chemical Reactions

In the stoichiometry examples worked out in the preceding section, we made the unstated assumption that all reactions "go to completion." That is, we assumed that all reactant molecules are converted to products. In fact, few reactions behave so nicely. Most of the time, a large majority of molecules react in the specified way, but other processes, called side reactions, also occur. Thus, the amount of product actually formed-the reaction's yield—is usually less than the amount that calculations predict.

The amount of product actually formed in a reaction divided by the amount theoretically possible and multiplied by $100 \%$ is called the reaction's percent yield. For example, if a given reaction could provide 6.9 g of a product according to its stoichiometry, but actually provides only 4.7 g , then its percent yield is $4.7 / 6.9 \times 100 \%=68 \%$.

$$
\text { Percent yield }=\frac{\text { Actual yield of product }}{\text { Theoretical yield of product }} \times 100 \%
$$

Worked Examples 3.8 and 3.9 show how to calculate and use percent yield.

## Worked Example 3.8

Methyl tert-butyl ether (MTBE, $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}$ ), a substance used as an octane booster in gasoline, can be made by reaction of isobutylene $\left(\mathrm{C}_{4} \mathrm{H}_{8}\right)$ with methanol $\left(\mathrm{CH}_{4} \mathrm{O}\right)$. What is the percent yield of the reaction if 32.8 g of methyl tert-butyl ether is obtained from reaction of 26.3 g of isobutylene with sufficient methanol?

$$
\underset{\text { Isobutylene }}{\mathrm{C}_{4} \mathrm{H}_{8}(g)}+\mathrm{CH}_{4} \mathrm{O}(l) \longrightarrow \mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}(l)
$$



Methyl tert-butyl ether

## Strategy

We need to calculate the amount of methyl tert-butyl ether that could theoretically be produced from 26.3 g of isobutylene and compare that theoretical amount to the actual amount ( 32.8 g ). As always, stoichiometry problems begin by calculating the molar masses of reactants and products. Coefficients of the balanced equation then tell mole ratios, and molar masses act as conversion factors between moles and masses.

## Solution

Isobutylene, $\mathrm{C}_{4} \mathrm{H}_{8}$ : Molec. mass $=(4 \times 12.0 \mathrm{amu})+(8 \times 1.0 \mathrm{amu})=56.0 \mathrm{amu}$
Molar mass of isobutylene $=56.0 \mathrm{~g} / \mathrm{mol}$
MTBE, $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}$ : Molec. mass $=(5 \times 12.0 \mathrm{amu})+(12 \times 1.0 \mathrm{amu})+16.0 \mathrm{amu}=88.0 \mathrm{amu}$
Molar mass of MTBE $=88.0 \mathrm{~g} / \mathrm{mol}$
To calculate the amount of MTBE that could theoretically be produced from 26.3 g of isobutylene, we first have to find the number of moles of reactant, using molar mass as the conversion factor:

$$
26.3 \mathrm{~g} \text { isobutylene } \times \frac{1 \mathrm{~mol} \text { isobutylene }}{56.0 \text { g isobutylene }}=0.470 \mathrm{~mol} \text { isobutylene }
$$

According to the balanced equation, 1 mol of product is produced per mol of reactant, so we know that 0.470 mol of isobutylene can theoretically yield 0.470 mol of MTBE. To find the mass of this MTBE, we do a mole-to-mass conversion:

$$
0.470 \mathrm{~mol} \text { isobutylene } \times \frac{1 \mathrm{~mol} \mathrm{MTBE}}{1 \mathrm{~mol} \text { isobutylene }} \times \frac{88.0 \mathrm{~g} \mathrm{MTBE}}{1 \mathrm{~mol} \mathrm{MTBE}}=41.4 \mathrm{~g} \mathrm{MTBE}
$$

Dividing the actual amount by the theoretical amount and multiplying by $100 \%$ then gives the percent yield:

$$
\frac{32.8 \mathrm{~g} \mathrm{MTBE}}{41.4 \mathrm{~g} \mathrm{MTBE}} \times 100 \%=79.2 \%
$$

## Worked Example 3.9

Diethyl ether $\left(\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}\right)$, the "ether" used medically as an anesthetic, is prepared commercially by treatment of ethyl alcohol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}\right)$ with an acid. How many grams of diethyl ether would you obtain from 40.0 g of ethyl alcohol if the percent yield of the reaction is $87 \%$ ?



Diethyl ether

## Strategy

Treat this as a typical stoichiometry problem to find the amount of diethyl ether that can theoretically be formed from 40.0 g of ethyl alcohol, and then multiply the answer by $87 \%$ to find the amount actually formed.

## Solution

First, calculate the molar masses of the reactant and product:
Ethyl alcohol, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$ : Molec. mass $=(2 \times 12.0 \mathrm{amu})+(6 \times 1.0 \mathrm{amu})+16.0 \mathrm{amu}=46.0 \mathrm{amu}$ Molar mass of ethyl alcohol $=46.0 \mathrm{~g} / \mathrm{mol}$

Diethyl ether, $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$ : Molec. mass $=(4 \times 12.0 \mathrm{amu})+(10 \times 1.0 \mathrm{amu})+16.0 \mathrm{amu}=74.0 \mathrm{amu}$ Molar mass of diethyl ether $=74.0 \mathrm{~g} / \mathrm{mol}$

Next, find how many moles of ethyl alcohol are in 40.0 g by using molar mass as a conversion factor:

$$
40.0 \text { g ethyl alcohol } \times \frac{1 \text { mol ethyl alcohol }}{46.0 \text { g ethylatcohol }}=0.870 \mathrm{~mol} \text { ethyl alcohol }
$$

Because we started with 0.870 mol of ethyl alcohol, and because the balanced equation indicates that 2 mol of ethyl alcohol yield 1 mol of diethyl ether, we can theoretically obtain 0.435 mol of product:

$$
0.870 \text { mol ethyl alcohol } \times \frac{1 \mathrm{~mol} \text { diethyl ether }}{2 \text { mol ethyl alcohol }}=0.435 \mathrm{~mol} \text { diethyl ether }
$$

We therefore need to find how many grams of diethyl ether are in 0.435 mol , using molar mass as the conversion factor:

$$
0.435 \text { mol diethyl ether } \times \frac{74.0 \mathrm{~g} \text { diethyl ether }}{1 \mathrm{~mol} \text { diethyl ether }}=32.2 \mathrm{~g} \text { diethyl ether }
$$

Finally, we have to multiply the theoretical amount of product by the observed yield $(87 \%=0.87)$ to find how much diethyl ether is actually formed:
32.2 g diethyl ether $\times 0.87=28 \mathrm{~g}$ diethyl ether


- Dichloromethane is used as a solvent to remove caffeine from coffee beans.
- PROBLEM 3.9 Ethyl alcohol is prepared industrially by the reaction of ethylene, $\mathrm{C}_{2} \mathrm{H}_{4}$, with water. What is the percent yield of the reaction if 4.6 g of ethylene gives 4.7 g of ethyl alcohol?


PROBLEM 3.10 Dichloromethane $\left(\mathrm{CH}_{2} \mathrm{Cl}_{2}\right)$, sometimes used as a solvent in the decaffeination of coffee beans, is prepared by reaction of methane $\left(\mathrm{CH}_{4}\right)$ with chlorine. How many grams of dichloromethane result from reaction of 1.85 kg of methane if the yield is $43.1 \%$ ?

## $3.6 \mid$ Reactions with Limiting Amounts of Reactants

Because chemists usually write balanced equations, it's easy to get the impression that reactions are always carried out using exactly the right proportions of reactants. In fact, this is often not the case. Many reactions are carried out using an
excess amount of one reactant-more than is actually needed according to stoichiometry. Look, for example, at the industrial synthesis of ethylene glycol, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}$, a substance used both as automobile antifreeze and as a starting material for the preparation of polyester polymers. More than 2 million tons of ethylene glycol are prepared each year in the United States by reaction of ethylene oxide, $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}$, with water at high temperature:


Because water is so cheap and so abundant, it doesn't make sense to worry about using exactly 1 mol of water for each mole of ethylene oxide. It's much easier to use an excess of water to be certain that enough is present to consume entirely the more valuable ethylene oxide reactant. Of course, when an excess of water is present, only the amount required by stoichiometry undergoes reaction. The excess water is only a spectator and is not otherwise involved.

Whenever the ratios of reactant molecules actually used in an experiment are different from those given by the coefficients of the balanced equation, a surplus of one reactant is left over after the reaction is finished. Thus, the extent to which a chemical reaction takes place depends on the reactant that is present in limiting amount-the limiting reactant. The other reactant is said to be the excess reactant.

What happens with excess reactants and limiting reactants is similar to what happens if there are five people in a room but only three chairs. Only three people can sit and the other two stand, because the number of people sitting is limited by the number of available chairs. In the same way, if 5 water molecules come in contact with 3 ethylene oxide molecules, only 3 water molecules can undergo a reaction. The other 2 water molecules are merely spectators, because the number of water molecules that react is limited by the number of available ethylene oxide molecules.


Worked Example 3.10 shows how to tell if a limiting amount of one reactant is present and how to calculate the amounts of the excess reactant consumed and remaining.

## WORKED EXAMPLE 3.10

Cisplatin, an anticancer agent used for the treatment of solid tumors, is prepared by the reaction of ammonia with potassium tetrachloroplatinate:

$$
\underset{\substack{\text { Potassium } \\ \text { tetrachloroplatinate }}}{\mathrm{K}_{2} \mathrm{PtCl}_{4}}+2 \mathrm{NH}_{3} \longrightarrow \underset{\text { Cisplatin }}{\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}}+2 \mathrm{KCl}
$$

Limiting Reactant activity; Limiting Reagent movie; and Limiting Reactant simulation

Assume that 10.0 g of $\mathrm{K}_{2} \mathrm{PtCl}_{4}$ and 10.0 g of $\mathrm{NH}_{3}$ are allowed to react.
(a) Which reactant is limiting, and which is in excess?
(b) How many grams of the excess reactant are consumed, and how many grams remain?
(c) How many grams of cisplatin are formed?

## Strategy

Complex stoichiometry problems should be worked slowly and carefully, one step at a time. When solving a problem that deals with limiting reactants, the idea is to find how many moles of all reactants are actually present and then compare the mole ratios of those actual amounts to the mole ratios required by the balanced equation. That comparison will identify the reactant there is too much of (the excess reactant) and the reactant there is too little of (the limiting reactant).

## Solution

(a) Finding the molar amounts of reactants always begins by calculating formula masses and using molar masses as conversion factors:

Form mass of $\mathrm{K}_{2} \mathrm{PtCl}_{4}=(2 \times 39.1 \mathrm{amu})+195.1 \mathrm{amu}+(4 \times 35.5 \mathrm{amu})=415.3 \mathrm{amu}$ Molar mass of $\mathrm{K}_{2} \mathrm{PtCl}_{4}=415.3 \mathrm{~g} / \mathrm{mol}$
Moles of $\mathrm{K}_{2} \mathrm{PtCl}_{4}=10.0 \mathrm{~g} \mathrm{~K}_{2} \mathrm{PtCl}_{4} \times \frac{1 \mathrm{~mol} \mathrm{~K}_{2} \mathrm{PtCl}_{4}}{415.3 \mathrm{~g} \mathrm{~K}_{2} \mathrm{PtCl}_{4}}=0.0241 \mathrm{~mol} \mathrm{~K} 2 \mathrm{PtCl}_{4}$
Molec. mass of $\mathrm{NH}_{3}=14.0 \mathrm{amu}+(3 \times 1.0 \mathrm{amu})=17.0 \mathrm{amu}$
Molar mass of $\mathrm{NH}_{3}=17.0 \mathrm{~g} / \mathrm{mol}$
Moles of $\mathrm{NH}_{3}=10.0 \mathrm{~g}_{\mathrm{g} \mathrm{NH}_{3}} \times \frac{1 \mathrm{~mol} \mathrm{NH}_{3}}{17.0 \mathrm{gNH}_{3}}=0.588 \mathrm{~mol} \mathrm{NH}_{3}$
These calculations tell us that we have 0.588 mol of ammonia and 0.0241 mol of $\mathrm{K}_{2} \mathrm{PtCl}_{4}$, or $0.588 / 0.0241=24.4$ times as much ammonia as $\mathrm{K}_{2} \mathrm{PtCl}_{4}$. The coefficients in the balanced equation, however, say that only two times as much ammonia as $\mathrm{K}_{2} \mathrm{PtCl}_{4}$ is needed. Thus, a large excess of $\mathrm{NH}_{3}$ is present, and $\mathrm{K}_{2} \mathrm{PtCl}_{4}$ is the limiting reactant.
(b) With the identities of the excess reactant and limiting reactant known, we now have to find how many moles of each undergo reaction and then carry out mole-togram conversions to find the mass of each reactant consumed. The entire amount of the limiting reactant $\left(\mathrm{K}_{2} \mathrm{PtCl}_{4}\right)$ is used up, but only the amount of the excess reactant $\left(\mathrm{NH}_{3}\right)$ required by stoichiometry undergoes reaction:

Moles of $\mathrm{K}_{2} \mathrm{PtCl}_{4}$ consumed $=0.0241 \mathrm{~mol} \mathrm{~K}{ }_{2} \mathrm{PtCl}_{4}$
Moles of $\mathrm{NH}_{3}$ consumed $=0.0241 \mathrm{~mol} \mathrm{~K}_{2} \mathrm{PtCl}_{4} \times \frac{2 \mathrm{~mol} \mathrm{NH}_{3}}{1 \mathrm{~mol} \mathrm{~K}_{2} \mathrm{PtCl}_{4}}=0.0482 \mathrm{~mol} \mathrm{NH} 3$
Grams of $\mathrm{NH}_{3}$ consumed $=0.0482 \mathrm{molNH}_{3} \times \frac{17.0 \mathrm{~g} \mathrm{NH}_{3}}{1 \mathrm{~mol} \mathrm{NH}_{3}}=0.819 \mathrm{~g} \mathrm{NH}_{3}$
Grams of $\mathrm{NH}_{3}$ not consumed $=(10.0 \mathrm{~g}-0.819 \mathrm{~g}) \mathrm{NH}_{3}=9.2 \mathrm{~g} \mathrm{NH} 3$
(c) The balanced equation shows that 1 mol of cisplatin is formed for each mole of $\mathrm{K}_{2} \mathrm{PtCl}_{4}$ consumed. Thus, 0.0241 mol of cisplatin is formed from 0.0241 mol of $\mathrm{K}_{2} \mathrm{PtCl}_{4}$. To determine the mass of cisplatin produced, we must calculate its molar mass and then carry out a mole-to-gram conversion:
Molec. mass of $\operatorname{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}=195.1 \mathrm{amu}+(2 \times 17.0 \mathrm{amu})+(2 \times 35.5 \mathrm{amu})$

$$
=300.1 \mathrm{amu}
$$

Molar mass of $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}=300.1 \mathrm{~g} / \mathrm{mol}$
Grams of $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}=0.0241 \mathrm{~mol} \mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2} \times \frac{300.1 \mathrm{~g} \mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}}{1 \mathrm{molPt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}}$

$$
=7.23 \mathrm{~g} \mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}
$$

Ernest F. Silversmith, "Limiting and Excess Reagents, Theoretical Yield," J. Chem. Educ., Vol. $62,1985,61$.
A. H. Kalantar, "Limiting Reagent Problems Made Simple for Students," J. Chem. Educ., Vol. 62, 1985, 106.

Zoltan Toth, "Limiting Reactant: An Alternative Analogy," J. Chem. Educ., Vol. 76, 1999, 934.

PROBLEM 3.11 Lithium oxide is used aboard the space shuttle to remove water from the air supply according to the equation

$$
\mathrm{Li}_{2} \mathrm{O}(s)+\mathrm{H}_{2} \mathrm{O}(g) \longrightarrow 2 \mathrm{LiOH}(s)
$$

If 80.0 kg of water is to be removed and 65 kg of $\mathrm{Li}_{2} \mathrm{O}$ is available, which reactant is limiting? How many kilograms of the excess reactant remain?

- PROBLEM 3.12 After lithium hydroxide is produced aboard the space shuttle by reaction of $\mathrm{Li}_{2} \mathrm{O}$ with $\mathrm{H}_{2} \mathrm{O}$ (Problem 3.11), it is used to remove exhaled carbon dioxide from the air supply according to the equation

$$
\mathrm{LiOH}(s)+\mathrm{CO}_{2}(g) \longrightarrow \mathrm{LiHCO}_{3}(s)
$$

How many grams of $\mathrm{CO}_{2}$ can 500.0 g of LiOH absorb?
KEY CONCEPT PROBLEM 3.13 The following diagram represents the reaction of $A$ (red spheres) with $B_{2}$ (blue spheres):

(a) Write a balanced equation for the reaction, and identify the limiting reactant.
(b) How many moles of product can be made from 1.0 mol of A and 1.0 mol of $\mathrm{B}_{2}$ ?

### 3.7 Concentrations of Reactants in Solution: Molarity

For a chemical reaction to occur, the reacting molecules or ions must come into contact. This means that the reactants must have considerable mobility, which in turn means that most chemical reactions are carried out in the liquid state or in solution rather than in the solid state. It's therefore necessary to have a standard means for describing exact quantities of reactants in solution.

As we've seen, stoichiometry calculations for chemical reactions always require working in moles. Thus, the most generally useful means of expressing a solution's concentration is molarity (M), the number of moles of a substance (the solute) dissolved in each liter of solution. For example, a solution made by dissolving $1.00 \mathrm{~mol}(58.5 \mathrm{~g})$ of NaCl in enough water to give 1.00 L of solution has a concentration of $1.00 \mathrm{~mol} / \mathrm{L}$, or 1.00 M . The molarity of any solution is found by dividing the number of moles of solute by the number of liters of solution.

$$
\operatorname{Molarity}(\mathbf{M})=\frac{\text { Moles of solute }}{\text { Liters of solution }}
$$

Note that it is the final volume of the solution that is important, not the starting volume of the solvent used. The final volume of the solution might be a bit larger than the volume of the solvent because of the additional volume of the solute. In practice, a solution of known molarity is prepared by weighing an appropriate amount of solute and placing it in a volumetric flask, as shown in Figure 3.3. Enough solvent is added to dissolve the solute, and further solvent is added until an accurately calibrated final volume is reached. The solution is then shaken until it is uniformly mixed.

Molarity can be used as a conversion factor to relate a solution's volume to the number of moles of solute. If we know the molarity and volume of a solution, we can calculate the number of moles of solute. If we know the number of moles of solute and the molarity of the solution, we can find the solution's volume. Worked Examples 3.11 and 3.12 show how such calculations are done.


$\nabla$
Molarity is moles of solute per liter of solution, not per liter of solvent. The volume of solvent used is not determined when making a solution of known molarity.



A FIGURE 3.3 Preparing a solution of known molarity. (a) A measured number of moles of solute is placed in a volumetric flask. (b) Enough solvent is added to dissolve the solute by swirling. (c) Further solvent is carefully added until the calibration mark on the neck of the flask is reached, and the solution is then shaken until uniform.

$$
\text { Molarity }=\frac{\text { Moles of solute }}{\text { Volume of solution (L) }}
$$

$\begin{gathered}\text { Moles of } \\ \text { solute }\end{gathered}=$ Molarity $\times \underset{\text { Volume of }}{\text { solution }} \quad \begin{gathered}\text { Volume of } \\ \text { solution }\end{gathered}=\frac{\text { Moles of solute }}{\text { Molarity }}$

## Worked Example 3.11

What is the molarity of a solution made by dissolving 2.355 g of sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$ in water and diluting to a final volume of 50.0 mL ?

## Strategy

Molarity is the number of moles of solute per liter of solution. Thus it's necessary to find the number of moles of sulfuric acid in 2.355 g and then divide by the volume of the solution.

## SOlUTION

Molec. mass of $\mathrm{H}_{2} \mathrm{SO}_{4}=(2 \times 1.0 \mathrm{amu})+32.1 \mathrm{amu}+(4 \times 16.0 \mathrm{amu})=98.1 \mathrm{amu}$ Molar mass of $\mathrm{H}_{2} \mathrm{SO}_{4}=98.1 \mathrm{~g} / \mathrm{mol}$

$$
\begin{aligned}
2.355 \mathrm{~g} \mathrm{H}_{2} \mathrm{SO}_{4} \times \frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}{98.1 \mathrm{~g}_{2} \mathrm{SO}_{4}} & =0.0240 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4} \\
\frac{0.0240 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}{0.0500 \mathrm{~L}} & =0.480 \mathrm{M}
\end{aligned}
$$

The solution has a sulfuric acid concentration of 0.480 M .

## Worked Example 3.12

Hydrochloric acid is sold commercially as a 12.0 M solution. How many moles of HCl are in 300.0 mL of 12.0 M solution?

## Strategy

The number of moles of solute is calculated by multiplying the molarity of the solution by its volume.

## Solution

$$
\begin{aligned}
\text { Moles of } \mathrm{HCl} & =(\text { Molarity of solution }) \times(\text { Volume of solution }) \\
& =\frac{12.0 \mathrm{~mol} \mathrm{HCl}}{1 Ł} \times 0.3000 \mathrm{~L}=3.60 \mathrm{~mol} \mathrm{HCl}
\end{aligned}
$$

There are 3.60 mol of HCl in 300.0 mL of 12.0 M solution.
$\checkmark$ Ballpark Check One liter of 12.0 M HCl solution contains 12 mol of HCl , so $300 \mathrm{~mL}(0.3 \mathrm{~L})$ of solution contains $0.3 \times 12=3.6 \mathrm{~mol}$.

- PROBLEM 3.14 How many moles of solute are present in the following solutions?
(a) 125 mL of $0.20 \mathrm{M} \mathrm{NaHCO}_{3}$
(b) 650.0 mL of $2.50 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$
- PROBLEM 3.15 How many grams of solute would you use to prepare the following solutions?
(a) 500.0 mL of 1.25 M NaOH
(b) 1.50 L of 0.250 M glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$

PROBLEM 3.16 How many milliliters of a 0.20 M glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ solution are needed to provide a total of 25.0 g of glucose?

PROBLEM 3.17 The concentration of cholesterol $\left(\mathrm{C}_{27} \mathrm{H}_{46} \mathrm{O}\right)$ in normal blood is approximately 0.005 M . How many grams of cholesterol are in 750 mL of blood?

## 3.8 | Diluting Concentrated Solutions

For convenience, chemicals are sometimes bought and stored as concentrated solutions that must be diluted before use. Aqueous hydrochloric acid, for example, is sold commercially as a 12.0 M solution, yet it is most commonly used in the laboratory after dilution with water to a final concentration of 6.0 M or 1.0 M .

$$
\text { Concentrated solution }+ \text { Solvent } \longrightarrow \text { Dilute solution }
$$

The key fact to remember when diluting a concentrated solution is that the number of moles of solute is constant; only the volume is changed by adding more solvent. Because the number of moles of solute can be calculated by multiplying molarity times volume, we can set up the following equation:

$$
\begin{aligned}
\text { Moles of solute (constant) } & =\text { Molarity } \times \text { Volume } \\
& =\mathrm{M}_{\mathrm{i}} \times V_{\mathrm{i}}=\mathrm{M}_{\mathrm{f}} \times V_{\mathrm{f}}
\end{aligned}
$$

where $\mathrm{M}_{\mathrm{i}}$ is the initial molarity, $V_{\mathrm{i}}$ is the initial volume, $\mathrm{M}_{\mathrm{f}}$ is the final molarity, and $V_{\mathrm{f}}$ is the final volume after dilution. Rearranging this equation into a more useful form shows that the molar concentration after dilution $\left(M_{f}\right)$ can be found by multiplying the initial concentration $\left(\mathrm{M}_{\mathrm{i}}\right)$ by the ratio of initial and final volumes $\left(V_{\mathrm{i}} / V_{\mathrm{f}}\right)$ :

$$
\mathrm{M}_{\mathrm{f}}=\mathrm{M}_{\mathrm{i}} \times \frac{V_{\mathrm{i}}}{V_{\mathrm{f}}}
$$

Suppose, for example, that we dilute 50.0 mL of a solution of $2.00 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ to a volume of 200.0 mL . The solution volume increases by a factor of four (from 50 mL to 200 mL ), so the concentration of the solution must decrease by a factor of four (from 2.00 M to 0.500 M ):

$$
\mathrm{M}_{\mathrm{f}}=2.00 \mathrm{M} \times \frac{50.0 \mathrm{~mL}}{200.0 \mathrm{~mL}}=0.500 \mathrm{M}
$$

$\square$Lloyd J. McElroy, "Teaching (1) Dilutions," J. Chem. Educ., Vol. 73, 1996, 765-766.


A Just as frozen orange juice concentrate must be diluted before use by adding water, many chemical solutions must also be diluted.

vThe relationship $\mathrm{M}_{\mathrm{i}} \times \mathrm{V}_{\mathrm{i}}=\mathrm{M}_{\mathrm{f}} \times \mathrm{V}_{\mathrm{f}}$ is convenient for dilutions only. Students tend to use it for solution stoichiometry problems, which only works if the stoichiometry is 1:1.


## Solution Formation by Dilution movie

 for diluting a concentrated solution. (a) The volume to be diluted is withdrawn and placed in an empty volumetric flask. (b) Solvent is added to a level just below the calibration mark, and the flask is shaken. (c) More solvent is added to reach the calibration mark, and the solution is inverted a few times to ensure mixing.

A FIGURE 3.5 A flow diagram summarizing the use of molarity as a conversion factor between moles and volume in stoichiometry calculations.

In practice, dilutions are carried out as shown in Figure 3.4. The volume to be diluted is withdrawn using a calibrated tube called a pipet, placed in an empty volumetric flask of the chosen volume, and diluted to the calibration mark on the flask.


## Worked Example 3.13

How would you prepare 500.0 mL of 0.2500 M NaOH solution starting from a concentration of 1.000 M ?

## Strategy

The problem gives initial and final concentrations ( $\mathrm{M}_{\mathrm{i}}$ and $\mathrm{M}_{\mathrm{f}}$ ) and final volume ( $V_{\mathrm{f}}$ ) and asks for the initial volume $\left(V_{\mathrm{i}}\right)$ that we need to dilute. Rewriting the equation $\mathrm{M}_{\mathrm{i}} \times V_{\mathrm{i}}=\mathrm{M}_{\mathrm{f}} \times V_{\mathrm{f}}$ as $V_{\mathrm{i}}=\left(\mathrm{M}_{\mathrm{f}} / \mathrm{M}_{\mathrm{i}}\right) \times V_{\mathrm{f}}$ gives the answer.

## Solution

$$
V_{\mathrm{i}}=\frac{\mathrm{M}_{\mathrm{f}}}{\mathrm{M}_{\mathrm{i}}} \times V_{\mathrm{f}}=\frac{0.2500 \mathrm{M}}{1.000 \mathrm{M}} \times 500.0 \mathrm{~mL}=125.0 \mathrm{~mL}
$$

We need to place 125.0 mL of 1.000 M NaOH solution in a 500.0 mL volumetric flask and fill to the mark with water.
$\checkmark$ BALLPARK CHECK Because the concentration decreases by a factor of four after dilution (from 1.000 M to 0.2500 M ), the volume must increase by a factor of four. Thus, to prepare 500.0 mL of solution, we should start with $500.0 / 4=125.0 \mathrm{~mL}$.

- PROBLEM 3.18 What is the final concentration if 75.0 mL of a 3.50 M glucose solution is diluted to a volume of 400.0 mL ?
- PROBLEM 3.19 Sulfuric acid is normally purchased at a concentration of 18.0 M . How would you prepare 250.0 mL of 0.500 M aqueous $\mathrm{H}_{2} \mathrm{SO}_{4}$ ?


## 3.9 | Solution Stoichiometry

We remarked in Section 3.7 that molarity is a conversion factor between numbers of moles of solute and the volume of a solution. If we know the volume and molarity of a solution, we can calculate the number of moles of solute. If we know the number of moles of solute and molarity, we can find the volume.

As indicated by the flow diagram in Figure 3.5, using molarity is critical for carrying out stoichiometry calculations on substances in solution. Molarity makes it possible to calculate the volume of one solution needed to react with a given volume of another solution. This sort of calculation is particularly important in acid-base chemistry, as shown in Worked Example 3.14.

## Worked Example 3.14

Stomach acid, a dilute solution of HCl in water, can be neutralized by reaction with sodium hydrogen carbonate, $\mathrm{NaHCO}_{3}$, according to the equation

$$
\mathrm{HCl}(a q)+\mathrm{NaHCO}_{3}(a q) \longrightarrow \mathrm{NaCl}(a q)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CO}_{2}(g)
$$

How many milliliters of $0.125 \mathrm{M} \mathrm{NaHCO}_{3}$ solution are needed to neutralize 18.0 mL of 0.100 M HCl ?

## Strategy

Solving stoichiometry problems always requires finding the number of moles of the first reactant, using the coefficients of the balanced equation to find the number of moles of the second reactant, and then finding the amount of the second reactant. The flow diagram in Figure 3.5 summarizes the situation.

## Solution

We first have to find how many moles of HCl are in 18.0 mL of a 0.100 M solution by multiplying volume times molarity:

$$
\text { Moles of } \mathrm{HCl}=18.0 \mathrm{~mL} \times \frac{1 \mathrm{~L}}{1000 \mathrm{~mL}} \times \frac{0.100 \mathrm{~mol}}{1 \nsucceq}=1.80 \times 10^{-3} \mathrm{~mol} \mathrm{HCl}
$$

Next, check the coefficients of the balanced equation to find that each mole of HCl reacts with 1 mol of $\mathrm{NaHCO}_{3}$, and then calculate how many milliliters of 0.125 M $\mathrm{NaHCO}_{3}$ solution contains $1.80 \times 10^{-3} \mathrm{~mol}$ :

$$
1.80 \times 10^{-3} \mathrm{molHCl} \times \frac{1 \mathrm{~mol} \mathrm{NaHCO}_{3}}{1 \mathrm{molHCl}} \times \frac{1 \mathrm{~L} \text { solution }}{0.125 \mathrm{~mol} \mathrm{NaHCO}_{3}}=0.0144 \mathrm{~L} \text { solution }
$$

Thus, $14.4 \mathrm{~mL}^{2}$ of the $0.125 \mathrm{M} \mathrm{NaHCO}_{3}$ solution is needed to neutralize 18.0 mL of the 0.100 M HCl solution.
$\checkmark$ Ballpark Check The balanced equation shows that HCl and $\mathrm{NaHCO}_{3}$ react in a 1:1 molar ratio, and we are told that the concentrations of the two solutions are about the same. Thus, the volume of the $\mathrm{NaHCO}_{3}$ solution must be about the same as that of the HCl solution.


- Neutralization of sodium hydrogen carbonate with acid leads to release of $\mathrm{CO}_{2}$ gas, visible in this fizzing solution.

PROBLEM 3.20 What volume of $0.250 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ is needed to react with 50.0 mL of 0.100 M NaOH ? The equation is

$$
\mathrm{H}_{2} \mathrm{SO}_{4}(a q)+2 \mathrm{NaOH}(a q) \longrightarrow \mathrm{Na}_{2} \mathrm{SO}_{4}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

- PROBLEM 3.21 What is the molarity of an $\mathrm{HNO}_{3}$ solution if 68.5 mL is needed to react with 25.0 mL of 0.150 M KOH solution?


### 3.10 Titration

There are two ways to make a solution of known molarity. The first way is to make the solution carefully, using an accurately weighed amount of solute dissolved in solvent to an accurately calibrated volume. Often though, it's more convenient to make up a solution quickly, using an estimated amount of solute and an estimated amount of solvent, and then determine the solution's exact molarity by titration.

Titration is a procedure for determining the concentration of a solution by allowing a carefully measured volume to react with a standard solution of another substance, whose concentration is known. By finding the volume of the standard solution that reacts with the measured volume of the first solution, the concentration of the first solution can be calculated. (It's necessary, though, that the reaction go to completion and have a yield of $100 \%$.)

Ara S. Kooser, Judith L. Jenkins, and Lawrence E. Welch, "Acid-Base Indicators: A New Look at an Old Topic," J. Chem. Educ., Vol. 78, 2001, 1504-1506.

Bassam Z. Shakhashiri, "Colorful Acid-Base Indicators," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989), pp. 33-40.


FIGURE 3.6 A flow diagram for an acid-base titration, summarizing the calculations needed to determine the concentration of an HCl solution by titration with an NaOH standard solution.

FIGURE 3.7 Titration of an acid solution of unknown concentration with a base solution of known concentration. (a) A measured volume of acid solution is placed in a flask, and phenolphthalein indicator is added. (b) A base solution of known concentration is added from a buret until the indicator changes color to signal that all the acid has reacted. Reading the volume of base solution added from the buret makes it possible to calculate the concentration of the acid solution.

To see how titration works, let's imagine that we have an HCl solution (an acid) whose concentration we want to find by allowing it to react with a base such as NaOH in what is called a neutralization reaction. (We'll learn more about acid-base neutralization reactions in the next chapter.) The balanced equation is

$$
\mathrm{NaOH}(a q)+\mathrm{HCl}(a q) \longrightarrow \mathrm{NaCl}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

We begin the titration by measuring out a known volume of the HCl solution and adding a small amount of an indicator such as phenolphthalein, a compound that is colorless in acidic solution but turns pink in basic solution. Next, we fill a calibrated glass tube called a buret with an NaOH standard solution of known concentration, and we slowly add the NaOH to the HCl until the phenolphthalein just begins to turn pink, indicating that all the HCl has reacted and that the solution is starting to become basic. By then reading from the buret to find the volume of the NaOH standard solution that has reacted with the known volume of HCl , we can calculate the concentration of the HCl . The strategy is summarized in Figure 3.6, and the procedure is shown in Figure 3.7.


Let's assume, for example, that we take 20.0 mL of the HCl solution and find that we have to add 48.6 mL of 0.100 M NaOH from a buret to obtain complete reaction. Using the molarity of the NaOH standard solution as a conversion factor, we can calculate the number of moles of NaOH undergoing reaction:

$$
\begin{aligned}
\text { Moles of } \mathrm{NaOH} & =0.0486 \mathrm{LANaOH} \times \frac{0.100 \mathrm{~mol} \mathrm{NaOH}}{1 \mathrm{LNaOH}} \\
& =0.00486 \mathrm{~mol} \mathrm{NaOH}
\end{aligned}
$$

According to the balanced equation, the number of moles of HCl is the same as that of NaOH :

$$
\text { Moles of } \mathrm{HCl}=0.00486 \mathrm{molNaOH} \times \frac{1 \mathrm{~mol} \mathrm{HCl}}{1 \mathrm{~mol} \mathrm{NaOH}}=0.00486 \mathrm{~mol} \mathrm{HCl}
$$


(a)

(b)

Dividing the number of moles of HCl by the volume then gives the molarity of the HCl :

$$
\mathrm{HCl} \text { molarity }=\frac{0.00486 \mathrm{~mol} \mathrm{HCl}}{0.0200 \mathrm{~L} \mathrm{HCl}}=0.243 \mathrm{M} \mathrm{HCl}
$$

- PROBLEM 3.22 A 25.0 mL sample of vinegar (dilute acetic acid, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ ) is titrated and found to react with 94.7 mL of 0.200 M NaOH . What is the molarity of the acetic acid solution? The reaction is

$$
\mathrm{NaOH}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q) \longrightarrow \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

### 3.11 Percent Composition and Empirical Formulas

Whenever a new compound is made in the laboratory or found in nature, it must be analyzed to find what elements it contains and how much of each element is present-that is, to find its composition. The percent composition of a compound is expressed by identifying the elements present and giving the mass percent of each. For example, we might express the percent composition of a certain colorless liquid found in gasoline by saying that it contains $84.1 \%$ carbon and $15.9 \%$ hydrogen by mass. In other words, a 100.0 g sample of the compound contains 84.1 g of carbon atoms and 15.9 g of hydrogen atoms.

Knowing a compound's percent composition makes it possible to calculate the compound's chemical formula. As shown in Figure 3.8, the strategy is to find the relative number of moles of each element in the compound and then use the numbers to establish the mole ratios of the elements. The mole ratios, in turn, give the subscripts in the chemical formula.

Let's use for our example a colorless liquid whose composition is $84.1 \%$ carbon and $15.9 \%$ hydrogen by mass. Arbitrarily taking 100 g of the substance to make the calculation easier, we find by using molar masses as conversion factors that the 100 g contains:

$$
\begin{aligned}
& 84.1 \mathrm{ge} \times \frac{1 \mathrm{~mol} \mathrm{C}}{12.01 \mathrm{gl}}=7.00 \mathrm{~mol} \mathrm{C} \\
& 15.9 \mathrm{gH} \times \frac{1 \mathrm{~mol} \mathrm{H}}{1.008 \mathrm{gH}}=15.8 \mathrm{~mol} \mathrm{H}
\end{aligned}
$$

With the relative numbers of moles of C and H known, we next find the mole ratio by dividing both by the smaller number (7.00):

$$
\mathrm{C}\left(\frac{7.00}{7.00}\right) \mathrm{H}\left(\frac{15.8}{7.00}\right)=\mathrm{C}_{1} \mathrm{H}_{2.26}
$$

The $\mathrm{C}: \mathrm{H}$ mole ratio of $1: 2.26$ means that we can write $\mathrm{C}_{1} \mathrm{H}_{2.26}$ as a temporary formula for the liquid. Multiplying the subscripts by small integers in a trial-anderror procedure until whole numbers are found then gives the final formula. In the present instance, multiplication of the subscripts by 4 is needed:

$$
\mathrm{C}_{(1 \times 4)} \mathrm{H}_{(2.26 \times 4)}=\mathrm{C}_{4} \mathrm{H}_{9}
$$

A formula such as $\mathrm{C}_{4} \mathrm{H}_{9}$, which is determined from data about percent composition, is called an empirical formula because it tells only the ratios of atoms in a compound. The molecular formula, which tells the actual numbers of atoms in a molecule, can be either the same as the empirical formula or a multiple of it, such as $\mathrm{C}_{8} \mathrm{H}_{18}$. To determine the molecular formula, it's necessary to know the molecular mass of the substance. In the present instance, the molecular mass of our compound (a substance called octane) is 114.2 amu , which is a simple multiple of the empirical molecular mass for $\mathrm{C}_{4} \mathrm{H}_{9}(57.1 \mathrm{amu})$.

George L. Gilbert, "Percentage Composition and Empirical Formula-A New View," J. Chem. Educ., Vol. 75, 1998, 851.


A FIGURE 3.8 A flow diagram for calculating the formula of a compound from its percent composition.

$\nabla$
Experimental errors in the data or calculation round-off errors usually result in mole ratios that are not whole numbers.
$\square$ Mole ratios frequently contain fractions close to $1 / 4$, $1 / 3$, or $1 / 2$ which should be multiplied by 4,3 , and 2 , respectively. Mole ratios close to whole numbers should be rounded to that number.

An easy way to remember the strategy for converting percentage composition to an empirical formula: "Percent to mass, mass to mol, divide by small, multiply 'til whole". Joel S. Thompson, "A Simple Rhyme for a Simple Formula," J. Chem. Educ., Vol. 65, 1988, 704.

## Worked Example 3.15

Vitamin C (ascorbic acid) contains $40.92 \%$ C, $4.58 \% \mathrm{H}$, and $54.50 \%$ O by mass. What is the empirical formula of ascorbic acid?

## Strategy

Assume that you have 100.00 g of ascorbic acid, and then carry out the procedure outlined in Figure 3.8.


## Solution

First, find the number of moles of each element in the sample:

$$
\begin{array}{r}
40.92 \mathrm{ge} \times \frac{1 \mathrm{~mol} \mathrm{C}}{12.0 \mathrm{~g}}=3.41 \mathrm{~mol} \mathrm{C} \\
4.58 \mathrm{gH} \times \frac{1 \mathrm{~mol} \mathrm{H}}{1.01 \mathrm{gH}}=4.53 \mathrm{~mol} \mathrm{H} \\
54.50 \mathrm{gO} \times \frac{1 \mathrm{~mol} \mathrm{O}}{16.0 \mathrm{gO}}=3.41 \mathrm{~mol} \mathrm{O}
\end{array}
$$

Dividing each of the three numbers by the smallest one ( 3.41 mol ) gives a $\mathrm{C}: \mathrm{H}: \mathrm{O}$ mole ratio of 1:1.33:1 and a temporary formula of $\mathrm{C}_{1} \mathrm{H}_{1.33} \mathrm{O}_{1}$. Multiplying the subscripts by small integers in a trial-and-error procedure until whole numbers are found then gives the empirical formula: $\mathrm{C}_{(3 \times 1)} \mathrm{H}_{(3 \times 1.33)} \mathrm{O}_{(3 \times 1)}=\mathrm{C}_{3} \mathrm{H}_{4} \mathrm{O}_{3}$.


A What is the empirical formula of vitamin C, an organic acid?

## Worked Example 3.16

Glucose, or blood sugar, has the molecular formula $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}$. What is the empirical formula, and what is the percent composition of glucose?

## Strategy and Solution

The percent composition of glucose can be calculated either from the molecular formula $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ or from the empirical formula $\left(\mathrm{CH}_{2} \mathrm{O}\right)$. Using the molecular formula, for instance, the $\mathrm{C}: \mathrm{H}: \mathrm{O}$ mole ratio of 6:12:6 can be converted into a mass ratio by assuming that we have 1 mol of compound and carrying out mole-to-gram conversions:

$$
\begin{aligned}
& 1 \text { mol glucose } \times \frac{6 \mathrm{molC}}{1 \mathrm{~mol} \text { glucose }} \times \frac{12.0 \mathrm{~g} \mathrm{C}}{1 \mathrm{molC}}=72.0 \mathrm{~g} \mathrm{C} \\
& 1 \text { mol glucose } \times \frac{12 \mathrm{molH}}{1 \text { mol glucose }} \times \frac{1.01 \mathrm{~g} \mathrm{H}}{1 \mathrm{molH}}=12.1 \mathrm{~g} \mathrm{H} \\
& 1 \mathrm{~mol} \text { glucose } \times \frac{6 \mathrm{~mol} \theta}{1 \mathrm{~mol} \text { glucose }} \times \frac{16.0 \mathrm{~g} \mathrm{O}}{1 \mathrm{mot} \theta}=96.0 \mathrm{~g} \mathrm{O}
\end{aligned}
$$


(O)

Glucose

Dividing the mass of each element by the total mass and multiplying by $100 \%$ gives the percent composition:

$$
\begin{aligned}
& \text { Total mass of } 1 \mathrm{~mol} \text { glucose }=72.0 \mathrm{~g}+12.1 \mathrm{~g}+96.0 \mathrm{~g}=180.1 \mathrm{~g} \\
& \qquad \% \mathrm{C}=\frac{7.20 \mathrm{~g} \mathrm{C}}{180.1 \mathrm{~g}} \times 100 \%=40.0 \% \\
& \% \mathrm{H}=\frac{12.1 \mathrm{~g} \mathrm{H}}{180.1 \mathrm{~g}} \times 100 \%=6.72 \% \\
& \% \mathrm{O}=\frac{96.0 \mathrm{~g} \mathrm{O}}{180.1 \mathrm{~g}} \times 100 \%=53.3 \%
\end{aligned}
$$

Note that the sum of the mass percentages is $100 \%$.

PROBLEM 3.23 What is the empirical formula, and what is the percent composition of dimethylhydrazine, $\mathrm{C}_{2} \mathrm{H}_{8} \mathrm{~N}_{2}$, a colorless liquid used as a rocket fuel?

- PROBLEM 3.24 What is the empirical formula of an ingredient in Bufferin tablets that has the percent composition C $14.25 \%$, O $56.93 \%, \mathrm{Mg} 28.83 \%$ by mass?


### 3.12 Determining Empirical Formulas: Elemental Analysis

One of the most common methods used to determine percent composition and empirical formulas, particularly for compounds containing carbon and hydrogen, is combustion analysis. In this method, a compound of unknown composition is burned with oxygen to produce the volatile combustion products $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$, which are separated and weighed by an automated instrument called a gas chromatograph. Methane $\left(\mathrm{CH}_{4}\right)$, for instance, burns according to the balanced equation

$$
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(\mathrm{~g}) \longrightarrow \mathrm{CO}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g})
$$

With the masses of the carbon-containing product $\left(\mathrm{CO}_{2}\right)$ and hydrogencontaining product $\left(\mathrm{H}_{2} \mathrm{O}\right)$ known, the strategy is to then calculate the number of moles of carbon and hydrogen in the products, from which we can find the C:H mole ratio. This information, in turn, provides the chemical formula, as outlined by the flow diagram in Figure 3.9.

As an example of how combustion analysis works, imagine that we have a sample of a pure substance-say, naphthalene (often used for household moth balls). We weigh a known amount of the sample, burn it in pure oxygen, and then analyze the products. Let's say that 0.330 g of naphthalene reacts with $\mathrm{O}_{2}$ and that 1.133 g of $\mathrm{CO}_{2}$ and 0.185 g of $\mathrm{H}_{2} \mathrm{O}$ are formed. The first thing to find out is the number of moles of carbon and hydrogen in the $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ products so that we can calculate the number of moles of each element originally present in the naphthalene sample.

$$
\begin{aligned}
\text { Moles of } \mathrm{C} \text { in } 1.133 \mathrm{~g} \mathrm{CO}_{2} & =1.133 \mathrm{gCO}_{2} \times \frac{1 \mathrm{~mol} \mathrm{CO}_{2}}{44.01 \mathrm{gCO}_{2}} \times \frac{1 \mathrm{~mol} \mathrm{C}}{1 \mathrm{molCO}_{2}} \\
& =0.02574 \mathrm{~mol} \mathrm{C} \\
\text { Moles of } \mathrm{H} \text { in } 0.185 \mathrm{~g} \mathrm{H}_{2} \mathrm{O} & =0.185 \mathrm{gH}_{2} \mathrm{O} \times \frac{1 \mathrm{molH}_{2} \mathrm{O}}{18.02 \mathrm{gH}_{2} \mathrm{O}} \times \frac{2 \mathrm{~mol} \mathrm{H}_{1 \mathrm{moH}_{2} \mathrm{O}}^{1}}{} \\
& =0.0205 \mathrm{~mol} \mathrm{H}
\end{aligned}
$$

Although it's not necessary in this instance since naphthalene contains only carbon and hydrogen, we can make sure that all the mass is accounted for and that no other elements are present. To do so, we carry out mole-to-gram conversions to find the number of grams of C and H in the starting sample:

$$
\begin{aligned}
& \text { Mass of } \mathrm{C}=0.02574 \mathrm{mot} \mathrm{C} \times \frac{12.01 \mathrm{~g} \mathrm{C}}{1 \mathrm{molC}}=0.3091 \mathrm{~g} \mathrm{C} \\
& \text { Mass of } \mathrm{H}=0.0205 \mathrm{mot} \mathrm{H} \times \frac{1.01 \mathrm{~g} \mathrm{H}}{1 \mathrm{molH}}=0.0207 \mathrm{~g} \mathrm{H} \\
& \text { Total mass of } \mathrm{C} \text { and } \mathrm{H}=0.3091 \mathrm{~g}+0.0207 \mathrm{~g}=0.3298 \mathrm{~g}
\end{aligned}
$$

Because the total mass of the C and H in the products $(0.3298 \mathrm{~g})$ is the same as the mass of the starting sample ( 0.330 g ), we know that no other elements are present in naphthalene.

With the relative number of moles of C and H in naphthalene known, divide the larger number of moles by the smaller number to get the temporary formula $\mathrm{C}_{1.26} \mathrm{H}_{1}$.

$$
\left.\mathrm{C}\left(\frac{0.0574}{0.0255}\right) \mathrm{H}_{(0.0 .025}^{0.025)}\right)=\mathrm{C}_{1.26} \mathrm{H}_{1}
$$

Multiplying the subscripts by small integers in a trial-and-error procedure until whole numbers are found gives the final formula $\mathrm{C}_{5} \mathrm{H}_{4}$. (The subscripts may not always be exact integers because of small errors in the data, but the discrepancies should be small.)

Multiply subscripts by 2: $\quad \mathrm{C}_{(1.26 \times 2)} \mathrm{H}_{(1 \times 2)}=\mathrm{C}_{2.52} \mathrm{H}_{2}$
Multiply subscripts by 3: $\quad \mathrm{C}_{(1.26 \times 3)} \mathrm{H}_{(1 \times 3)}=\mathrm{C}_{3.78} \mathrm{H}_{3}$
Multiply subscripts by 4 : $\quad \mathrm{C}_{(1.26 \times 4)} \mathrm{H}_{(1 \times 4)}=\mathrm{C}_{5.04} \mathrm{H}_{4}$
$=\mathrm{C}_{5} \mathrm{H}_{4} \quad$ Both subscripts are integers
Elemental analysis can provide only an empirical formula. To determine the molecular formula, it is also necessary to know the substance's molecular mass. In the present problem, the molecular mass of naphthalene is 128.2 amu , or twice the empirical formula mass of $\mathrm{C}_{5} \mathrm{H}_{4}(64.1 \mathrm{amu})$. Thus, the molecular formula of naphthalene is $\mathrm{C}_{(2 \times 5)} \mathrm{H}_{(2 \times 4)}$, or $\mathrm{C}_{10} \mathrm{H}_{8}$.

Worked Example 3.18 shows a combustion analysis when the sample contains oxygen in addition to carbon and hydrogen. Because oxygen yields no combustion products, its presence in a molecule can't be directly detected by this method. Rather, the presence of oxygen must be inferred by subtracting the calculated masses of C and H from the total mass of the sample.

## Worked Example 3.17

We calculated in Worked Example 3.15 that ascorbic acid (vitamin C) has the empirical formula $\mathrm{C}_{3} \mathrm{H}_{4} \mathrm{O}_{3}$. If the molecular mass of ascorbic acid is 176 amu , what is its molecular formula?

## Strategy

Calculate a formula mass corresponding to the empirical formula, and compare it with the molecular mass of ascorbic acid.

## Solution

$$
\begin{aligned}
\text { Form. mass of } \mathrm{C}_{3} \mathrm{H}_{4} \mathrm{O}_{3} & =(3 \times 12.0 \mathrm{amu})+(4 \times 1.0 \mathrm{amu})+(3 \times 16.0 \mathrm{amu}) \\
& =88.0 \mathrm{amu}
\end{aligned}
$$

The empirical formula mass ( 88.0 amu ) is half the molecular mass of ascorbic acid ( 176 amu ), so the subscripts in the empirical formula must be multiplied by 2 : $\mathrm{C}_{(2 \times 3)} \mathrm{H}_{(2 \times 4)} \mathrm{O}_{(2 \times 3)}=\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{6}$

-
Naphthalene

Combustion analysis can be used to determine the empirical formula of a compound containing carbon, hydrogen, and any third element. Frequently the third element is oxygen.

## Worked Example 3.18

Caproic acid, the substance responsible for the aroma of dirty gym socks and running shoes, contains carbon, hydrogen, and oxygen. On combustion analysis, a 0.450 g sample of caproic acid gives 0.418 g of $\mathrm{H}_{2} \mathrm{O}$ and 1.023 g of $\mathrm{CO}_{2}$. What is the empirical formula of caproic acid? If the molecular mass of caproic acid is 116.2 amu , what is the molecular formula?

## Strategy

Using the steps outlined in Figure 3.9, find the empirical formula of caproic acid, calculate a formula mass, and compare with the known molecular mass.

## Solution

First, find the molar amounts of C and H in the sample:

$$
\begin{aligned}
& \text { Moles of } \mathrm{C}=1.023 \mathrm{~g} \mathrm{CO}_{2} \times \frac{1 \mathrm{molCO}_{2}}{44.01 \mathrm{gCO}_{2}} \times \frac{1 \mathrm{~mol} \mathrm{C}}{1 \mathrm{~mol} \mathrm{H}_{2}}=0.02324 \mathrm{~mol} \mathrm{C} \\
& \text { Moles of } \mathrm{H}=0.418 \mathrm{~g} \mathrm{H}_{2} \mathrm{O} \times \frac{1 \mathrm{molH}_{2} \mathrm{O}}{18.02 \mathrm{gH}_{2} \mathrm{O}} \times \frac{2 \mathrm{~mol} \mathrm{H}^{2}}{1 \mathrm{molH}_{2} \mathrm{O}}=0.0464 \mathrm{~mol} \mathrm{H}
\end{aligned}
$$



Caproic acid

Next, find the number of grams of C and H in the sample:

$$
\begin{aligned}
& \text { Mass of } \mathrm{C}=0.02324 \mathrm{mot} \mathrm{C} \times \frac{12.01 \mathrm{~g} \mathrm{C}}{1 \mathrm{molC}}=0.2791 \mathrm{~g} \mathrm{C} \\
& \text { Mass of } \mathrm{H}=0.0464 \mathrm{molH} \times \frac{1.01 \mathrm{~g} \mathrm{H}}{1 \mathrm{molH}}=0.0469 \mathrm{~g} \mathrm{H}
\end{aligned}
$$

Subtracting the masses of C and H from the mass of the starting sample indicates that 0.124 g is unaccounted for:

$$
0.450 \mathrm{~g}-(0.2791 \mathrm{~g}+0.0469 \mathrm{~g})=0.124 \mathrm{~g}
$$

Because we are told that oxygen is also present in the sample, the "missing" mass must be due to oxygen, which can't be detected by combustion. We therefore need to find the number of moles of oxygen in the sample:

$$
\text { Moles of } \mathrm{O}=0.124 \mathrm{~g} \theta \times \frac{1 \mathrm{~mol} \mathrm{O}}{16.00 \mathrm{~g} \theta}=0.00775 \mathrm{~mol} \mathrm{O}
$$

Knowing the relative numbers of moles of all three elements, $\mathrm{C}, \mathrm{H}$, and O , we divide the three numbers of moles by the smallest number ( 0.00775 mol of oxygen) to arrive at a $\mathrm{C}: \mathrm{H}: \mathrm{O}$ ratio of $3: 6: 1$.

$$
\mathrm{C}\left(\frac{0.022324}{0.00775}\right) \mathrm{H}_{\left(\frac{0.0464}{0.00775}\right)} \mathrm{O}_{\left(\frac{0.00775}{0.00775}\right)}=\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}
$$

The empirical formula of caproic acid is therefore $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}$, and the empirical formula mass is 58.1 amu . Since the molecular mass of caproic acid is 116.2 , or twice the empirical formula mass, the molecular formula of caproic acid must be $\mathrm{C}_{(2 \times 3)} \mathrm{H}_{(2 \times 6)} \mathrm{O}_{(2 \times 1)}$, or $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$.

When doing combustion analysis problems, students frequently try to determine the amount of oxygen in a sample from the amounts of water and carbon dioxide produced. This is not possible because the compound is burned in oxygen, which makes up part of the water and carbon dioxide produced.


an evacuated chamber, where it is bombarded with a beam of high-energy electrons. The electron beam knocks other electrons from the sample molecules, which become positively charged ions. Some of these ionized molecules survive, and others fragment into smaller ions. The various ions of different masses are then accelerated by an electric field and passed between the poles of a strong magnet, which deflects them through a curved, evacuated pipe.

The radius of deflection of a charged ion $\mathrm{M}^{+}$as it passes between the magnet poles depends on its mass, with lighter ions deflected more strongly than heavier ones. By varying the strength of the magnetic field, it's possible to focus ions of different masses through a slit and onto a detector assembly. The mass spectrum that results is plotted as a graph of ion mass versus intensity-that is, as the molecular masses of the various ions versus the relative number of those ions produced in the instrument.

Although a typical mass spectrum contains ions of many different masses, the heaviest ion is generally due to the ionized molecule itself. By measuring the mass of this ion, the molecular mass of the molecule can be determined. The naphthalene sample discussed in the previous section, for example, gives rise to an intense peak at mass 128 amu in its spectrum, consistent with its molecular formula of $\mathrm{C}_{10} \mathrm{H}_{8}$ (Figure 3.10b).

Modern mass spectrometers are so precise that molecular masses can often be measured to seven significant figures. $\mathrm{A}^{12} \mathrm{C}_{10}{ }^{1} \mathrm{H}_{8}$ molecule of naphthalene, for example, has a molecular mass of 128.0626 amu as measured by mass spectrometry.
re

FIGURE 3.10 (a) Schematic illustration of a mass spectrometer. Sample molecules are ionized by collision with a high-energy electron beam, and the resulting ions are then passed between the poles of a magnet, where they are deflected according to their mass-to-charge ratio. The deflected ions pass through a slit into a detector assembly. (b) A mass spectrum of naphthalene, molec. mass $=128$, showing peaks of different masses on the horizontal axis.

## Interlude

## Did Ben Franklin Have Avogadro's Number? A Ballpark Calculation

At length being at Clapham, where there is on the common


What did these two have in common?


Benjamin Franklin, author and renowned statesman, was also an inventor and a scientist. Every schoolchild knows of Franklin's experiment with a kite and a key, demonstrating that lightning is electricity. Less well known is that his measurement of the extent to which oil spreads on water makes possible a simple estimate of molecular size and Avogadro's number.

The calculation goes like this: Avogadro's number is the number of molecules in a mole. So, if we can estimate both the number of molecules and the number of moles in Franklin's teaspoon of oil, we can calculate Avogadro's number. Let's start by calculating the number of molecules in the oil.

1. The volume $(V)$ of oil Franklin used was $1 \mathrm{tsp}=4.9 \mathrm{~cm}^{3}$, and the area $(A)$ covered by the oil was $1 / 2$ acre $=2.0 \times 10^{7} \mathrm{~cm}^{2}$. Let's assume that the oil molecules are tiny cubes that pack closely together and form a layer only one molecule thick. As shown in the accompanying figure, the volume of the oil

equals the surface area of the layer times the length $(l)$ of the side of one molecule: $V=A \times l$. Rearranging this equation to find the length then gives us an estimate of molecular size:

$$
l=\frac{V}{A}=\frac{4.9 \mathrm{~cm}^{3}}{2.0 \times 10^{7} \mathrm{~cm}^{2}}=2.4 \times 10^{-7} \mathrm{~cm}
$$

2. The area of the oil layer is the area of the side of one molecule $\left(l^{2}\right)$ times the number of molecules ( $N$ ) of oil: $A=l^{2} \times N$. Rearranging this equation gives the number of molecules:

$$
N=\frac{A}{l^{2}}=\frac{2.0 \times 10^{7} \mathrm{~cm}^{2}}{\left(2.4 \times 10^{-7} \mathrm{~cm}\right)^{2}}=3.5 \times 10^{20} \text { molecules }
$$

3. To calculate the number of moles, we first need to know the mass ( $m$ ) of the oil. This could have been determined by weighing, but Franklin neglected to do so. Let's therefore estimate the mass by multiplying the volume ( $V$ ) of the oil by the density $(D)$ of a typical oil, $0.95 \mathrm{~g} / \mathrm{cm}^{3}$. [Since oil floats on water, the density of oil must be a bit less than the density of water $\left(1.00 \mathrm{~g} / \mathrm{cm}^{3}\right)$.]

$$
m=V \times D=4.9 \mathrm{~cm}^{3} \times 0.95 \frac{\mathrm{~g}}{\mathrm{~cm}^{3}}=4.7 \mathrm{~g}
$$

4. We now have to make one final assumption about the molecular mass of the oil before completing the calculation. Assuming that a typical oil has molec. mass $=200 \mathrm{amu}$, then the mass of 1 mol of oil is 200 g . Dividing the mass of the oil by the mass of one mole gives the number of moles of oil:

$$
\text { Moles of oil }=\frac{4.7 \mathrm{~g}}{200 \mathrm{~g} / \mathrm{mol}}=0.024 \mathrm{~mol}
$$

5. Finally, the number of molecules per mole-Avogadro's number-can be obtained:

$$
\text { Avogadro's number }=\frac{3.5 \times 10^{20} \text { molecules }}{0.024 \mathrm{~mol}}=1.5 \times 10^{22}
$$

The calculation is not very accurate, but Ben wasn't really intending for us to calculate Avogadro's number when he made a rough estimate of how much his oil spread out. Nevertheless, the result isn't too bad for such a simple experiment.

- PROBLEM 3.28 What do you think are the main sources of error in calculating Avogadro's number by spreading oil on a pond?
- PROBLEM 3.29 Recalculate Avogadro's number assuming that the oil molecules are tall rectangular boxes rather than cubes, with two edges of equal length and the third edge four times the length of the other two. Assume also that the molecules stand on end in the water.

Summary

Because mass is neither created nor destroyed in reactions, all chemical equations must be balanced-that is, the numbers and kinds of atoms on both sides of the reaction arrow must be the same. A balanced equation tells the number ratio of reactant and product formula units in a reaction.

Just as atomic mass is the mass of an atom, molecular mass is the mass of a molecule. The analogous term formula mass is used for ionic and other nonmolecular substances. Molecular mass is the sum of the atomic masses of all atoms in the molecule. When referring to the large numbers of molecules or ions that take part in a visible chemical reaction, it's convenient to use a unit called the mole, abbreviated mol. One mole of any object, atom, molecule, or ion contains Avogadro's number of formula units, $6.022 \times 10^{23}$.

For work in the laboratory, it's necessary to weigh reactants rather than just know numbers of moles. Thus, it's necessary to convert between numbers of moles and numbers of grams by using molar mass as the conversion factor. The molar mass of any substance is the amount in grams numerically equal to the substance's molecular or formula mass. Carrying out chemical calculations using these relationships is called stoichiometry.

The amount of product actually formed in a reaction (the reaction's yield) is often less than the amount theoretically possible. Dividing the actual amount by the theoretical amount and multiplying by $100 \%$ gives the reaction's percent
yield. Often, reactions are carried out with an excess of one reactant beyond that called for by the balanced equation. In such cases, the extent to which the reaction takes place depends on the reactant present in limiting amount, the limiting reactant.

The concentration of a substance in solution is usually expressed as molarity (M), defined as the number of moles of a substance (the solute) dissolved per liter of solution. A solution's molarity acts as a conversion factor between solution volume and number of moles of solute, making it possible to carry out stoichiometry calculations on solutions. Often, chemicals are stored as concentrated aqueous solutions that are diluted before use. When carrying out a dilution, only the volume is changed by adding solvent; the amount of solute is unchanged. A solution's exact concentration can often be determined by titration.

The chemical makeup of a substance is described by its percent composition-the percentage of the substance's mass due to each of its constituent elements. Elemental analysis is used to calculate a substance's empirical formula, which gives the smallest whole-number ratio of atoms of the elements in the compound. To determine the molecular formula, which may be a simple multiple of the empirical formula, it's also necessary to know the substance's molecular mass. Molecular masses are usually determined by mass spectrometry.

## Key Words

Avogadro's number $\left(N_{\mathrm{A}}\right) 82$
balanced 76
coefficient 77
empirical formula 99
formula mass 81
formula unit 76
limiting reactant 90
molar mass 82
molarity (M) 92
mole 82
molecular formula 99
molecular mass 81
percent composition 98
percent yield 97
solute 92
stoichiometry 84
titration 97
yield 97

## Key Concept Summary



## Understanding Key Concepts

Problems 3.1-3.29 appear within the chapter.
3.30 Box (a) represents 1.0 mL of a solution of particles at a given concentration. Which of the boxes (b)-(d) represents 1.0 mL of the solution that results after (a) has been diluted by doubling the volume of its solvent?

(a)

(b)

(c)

(d)
3.31 Reaction of A (green spheres) with B (blue spheres) is shown schematically in the following diagram:


Which equation best describes the stoichiometry of the reaction?
(a) $\mathrm{A}_{2}+2 \mathrm{~B} \rightarrow \mathrm{~A}_{2} \mathrm{~B}_{2}$
(b) $10 \mathrm{~A}+5 \mathrm{~B}_{2} \rightarrow 5 \mathrm{~A}_{2} \mathrm{~B}_{2}$
(c) $2 \mathrm{~A}+\mathrm{B}_{2} \rightarrow \mathrm{~A}_{2} \mathrm{~B}_{2}$
(d) $5 \mathrm{~A}+5 \mathrm{~B}_{2} \rightarrow 5 \mathrm{~A}_{2} \mathrm{~B}_{2}$
3.32 Cytosine, a constituent of deoxyribonucleic acid (DNA) can be represented by the molecular model at the top of the next column. If 0.001 mol of cytosine is submitted to combustion analysis, how many moles of $\mathrm{CO}_{2}$ and how many moles of $\mathrm{H}_{2} \mathrm{O}$ would be formed?

3.33 If blue spheres represent nitrogen atoms and red spheres represent oxygen atoms, which box represents reactants and which represents products for the reaction $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{NO}_{2}(g)$ ?

(a)

(c)

(b)

(d)
3.34 Fluoxetine, marketed as an antidepressant under the name Prozac, can be represented by the following ball-and-stick molecular model. Write the molecular formula for fluoxetine, and calculate its molecular mass (red $=\mathrm{O}$, gray $=\mathrm{C}$, blue $=\mathrm{N}$, yellow-green $=\mathrm{F}$, ivory $=\mathrm{H}$ ).

3.35 Assume that the buret contains $\mathrm{H}^{+}$ions, the flask contains $\mathrm{OH}^{-}$ions, and you are carrying out a titration of the base with the acid. If the volumes in the buret and the flask are identical and the concentration of the acid in the buret is 1.00 M , what is the concentration of base in the flask?

$+$

3.36 The following diagram represents the reaction of $\mathrm{A}_{2}$ (red spheres) with $\mathrm{B}_{2}$ (blue spheres):

(a) Write a balanced equation for the reaction, and identify the limiting reactant.
(b) How many moles of product can be made from 1.0 mol of $\mathrm{A}_{2}$ and 1.0 mol of $\mathrm{B}_{2}$ ?
3.37 A hydrocarbon of unknown formula $\mathrm{C}_{\mathrm{x}} \mathrm{H}_{\mathrm{y}}$ was submitted to combustion analysis with the following results.
What is the empirical formula of the hydrocarbon?


## Additional Problems

## Balancing Equations

3.38 Which of the following equations are balanced?
(a) The development reaction in photography:

$$
\begin{aligned}
2 \mathrm{AgBr}+2 \mathrm{NaOH}+\mathrm{C}_{6} \mathrm{H}_{6} \mathrm{O}_{2} \longrightarrow \\
2 \mathrm{Ag}+\mathrm{H}_{2} \mathrm{O}+2 \mathrm{NaBr}+\mathrm{C}_{6} \mathrm{H}_{4} \mathrm{O}_{2}
\end{aligned}
$$

(b) Preparation of household bleach:

$$
2 \mathrm{NaOH}+\mathrm{Cl}_{2} \longrightarrow \mathrm{NaOCl}+\mathrm{NaCl}+\mathrm{H}_{2} \mathrm{O}
$$

3.39 Which of the following equations are balanced? Balance any that need it.
(a) The thermite reaction, used in welding:

$$
\mathrm{Al}+\mathrm{Fe}_{2} \mathrm{O}_{3} \longrightarrow \mathrm{Al}_{2} \mathrm{O}_{3}+\mathrm{Fe}
$$

(b) The photosynthesis of glucose from $\mathrm{CO}_{2}$ :

$$
6 \mathrm{CO}_{2}+6 \mathrm{H}_{2} \mathrm{O} \longrightarrow \mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}+6 \mathrm{O}_{2}
$$

(c) The separation of gold from its ore:

$$
\mathrm{Au}+2 \mathrm{NaCN}+\mathrm{O}_{2}+\mathrm{H}_{2} \mathrm{O} \longrightarrow \mathrm{NaAu}(\mathrm{CN})_{2}+3 \mathrm{NaOH}
$$

3.40 Balance the following equations:
(a) $\mathrm{Mg}+\mathrm{HNO}_{3} \rightarrow \mathrm{H}_{2}+\mathrm{Mg}\left(\mathrm{NO}_{3}\right)_{2}$
(b) $\mathrm{CaC}_{2}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{Ca}(\mathrm{OH})_{2}+\mathrm{C}_{2} \mathrm{H}_{2}$
(c) $\mathrm{S}+\mathrm{O}_{2} \rightarrow \mathrm{SO}_{3}$
(d) $\mathrm{UO}_{2}+\mathrm{HF} \rightarrow \mathrm{UF}_{4}+\mathrm{H}_{2} \mathrm{O}$
3.41 Balance the following equations:
(a) The explosion of ammonium nitrate:

$$
\mathrm{NH}_{4} \mathrm{NO}_{3} \longrightarrow \mathrm{~N}_{2}+\mathrm{O}_{2}+\mathrm{H}_{2} \mathrm{O}
$$

(b) The spoilage of wine into vinegar:

$$
\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}+\mathrm{O}_{2} \longrightarrow \mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}_{2}+\mathrm{H}_{2} \mathrm{O}
$$

(c) The burning of rocket fuel:

$$
\mathrm{C}_{2} \mathrm{H}_{8} \mathrm{~N}_{2}+\mathrm{N}_{2} \mathrm{O}_{4} \longrightarrow \mathrm{~N}_{2}+\mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O}
$$

## Molecular Masses and Moles

3.42 What are the molecular (formula) masses of the following substances?
(a) $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$ (calomel, used at one time as a bowel purgative)
(b) $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$ (butyric acid, responsible for the odor of rancid butter)
(c) $\mathrm{CF}_{2} \mathrm{Cl}_{2}$ (a chlorofluorocarbon that destroys the stratospheric ozone layer)
3.43 What are the formulas of the following substances?
(a) $\mathrm{PCl}_{3}$; Molec. mass $=137.3 \mathrm{amu}$
(b) Nicotine, $\mathrm{C}_{10} \mathrm{H}_{14} \mathrm{~N}_{3} ;$ Molec. mass $=162.2 \mathrm{amu}$
3.44 How many grams are in a mole of each of the following substances?
(a) Ti
(b) $\mathrm{Br}_{2}$
(c) Hg
(d) $\mathrm{H}_{2} \mathrm{O}$
3.45 How many moles are in a gram of each of the following substances?
(a) Cr
(b) $\mathrm{Cl}_{2}$
(c) Au
(d) $\mathrm{NH}_{3}$
3.46 How many moles of ions are in 2.5 mol of NaCl ?
3.47 How many moles of cations are in 1.45 mol of $\mathrm{K}_{2} \mathrm{SO}_{4}$ ?
3.48 How many moles of ions are in 27.5 g of $\mathrm{MgCl}_{2}$ ?
3.49 How many moles of anions are in 35.6 g of $\mathrm{AlF}_{3}$ ?
3.50 What is the molecular mass of chloroform if 0.0275 mol weighs 3.28 g ?
3.51 What is the molecular mass of cholesterol if 0.5731 mol weighs 221.6 g ?
3.52 Iron(II) sulfate, $\mathrm{FeSO}_{4}$, is prescribed for the treatment of anemia. How many moles of $\mathrm{FeSO}_{4}$ are present in a standard 300 mg tablet? How many iron(II) ions?
3.53 The "lead" in lead pencils is actually almost pure carbon, and the mass of a period mark made by a lead pencil is about 0.0001 g . How many carbon atoms are in the period?
3.54 An average cup of coffee contains about 125 mg of caffeine, $\mathrm{C}_{8} \mathrm{H}_{10} \mathrm{~N}_{4} \mathrm{O}_{2}$. How many moles of caffeine are in a cup? How many molecules of caffeine?
3.55 Let's say that an average egg has a mass of 45 g . What mass would a mole of eggs have?
3.56 How many moles does each of the following samples contain?
(a) 1.0 g of lithium
(b) 1.0 g of gold
(c) 1.0 g of penicillin G potassium, $\mathrm{C}_{16} \mathrm{H}_{17} \mathrm{~N}_{2} \mathrm{O}_{4} \mathrm{SK}$
3.57 What is the mass in grams of each of the following samples?
(a) 0.0015 mol of sodium
(b) 0.0015 mol of lead
(c) 0.0015 mol of diazepam (Valium), $\mathrm{C}_{16} \mathrm{H}_{13} \mathrm{ClN}_{2} \mathrm{O}$

## Stoichiometry Calculations

3.58 Titanium metal is obtained from the mineral rutile, $\mathrm{TiO}_{2}$. How many kilograms of rutile are needed to produce 100.0 kg of Ti?
3.59 Iron metal can be produced from the mineral hematite, $\mathrm{Fe}_{2} \mathrm{O}_{3}$, by reaction with carbon. How many kilograms of iron are present in 105 kg of hematite?
3.60 In the preparation of iron from hematite (Problem 3.59), $\mathrm{Fe}_{2} \mathrm{O}_{3}$ reacts with carbon:

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}+\mathrm{C} \longrightarrow \mathrm{Fe}+\mathrm{CO}_{2} \quad \text { Unbalanced }
$$

(a) Balance the equation.
(b) How many moles of carbon are needed to react with 525 g of hematite?
(c) How many grams of carbon are needed to react with 525 g of hematite?
3.61 An alternative method for preparing pure iron from $\mathrm{Fe}_{2} \mathrm{O}_{3}$ (Problem 3.59) is by reaction with carbon monoxide:

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}+\mathrm{CO} \longrightarrow \mathrm{Fe}+\mathrm{CO}_{2} \quad \text { Unbalanced }
$$

(a) Balance the equation.
(b) How many grams of CO are needed to react with 3.02 g of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ ?
(c) How many grams of CO are needed to react with 1.68 mol of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ ?
3.62 Magnesium metal burns in oxygen to form magnesium oxide, MgO .
(a) Write a balanced equation for the reaction.
(b) How many grams of oxygen are needed to react with 25.0 g of Mg ? How many grams of MgO will result?
(c) How many grams of Mg are needed to react with 25.0 g of $\mathrm{O}_{2}$ ? How many grams of MgO will result?
3.63 Ethylene gas, $\mathrm{C}_{2} \mathrm{H}_{4}$, reacts with water at high temperature to yield ethyl alcohol, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$.
(a) How many grams of ethylene are needed to react with 0.133 mol of $\mathrm{H}_{2} \mathrm{O}$ ? How many grams of ethyl alcohol will result?
(b) How many grams of water are needed to react with 0.371 mol of ethylene? How many grams of ethyl alcohol will result?
3.64 Pure oxygen was first made by heating mercury(II) oxide:

$$
\mathrm{HgO} \xrightarrow{\text { Heat }} \mathrm{Hg}+\mathrm{O}_{2} \quad \text { Unbalanced }
$$

(a) Balance the equation.
(b) How many grams of mercury and how many grams of oxygen are formed from 45.5 g of HgO ?
(c) How many grams of HgO would you need to obtain 33.3 g of $\mathrm{O}_{2}$ ?
3.65 Titanium dioxide $\left(\mathrm{TiO}_{2}\right)$, the substance used as the pigment in white paint, is prepared industrially by reaction of $\mathrm{TiCl}_{4}$ with $\mathrm{O}_{2}$ at high temperature.

$$
\mathrm{TiCl}_{4}+\mathrm{O}_{2} \xrightarrow{\text { Heat }} \mathrm{TiO}_{2}+2 \mathrm{Cl}_{2}
$$

How many kilograms of $\mathrm{TiO}_{2}$ can be prepared from 5.60 kg of $\mathrm{TiCl}_{4}$ ?
3.66 Silver metal reacts with chlorine $\left(\mathrm{Cl}_{2}\right)$ to yield silver chloride. If 2.00 g of Ag reacts with 0.657 g of $\mathrm{Cl}_{2}$, what is the empirical formula of silver chloride?
3.67 Aluminum reacts with oxygen to yield aluminum oxide. If 5.0 g of Al reacts with 4.45 g of $\mathrm{O}_{2}$, what is the empirical formula of aluminum oxide?

## Limiting Reactants and Reaction Yield

3.68 Assume that you have 1.39 mol of $\mathrm{H}_{2}$ and 3.44 mol of $\mathrm{N}_{2}$. How many grams of ammonia $\left(\mathrm{NH}_{3}\right)$ can you make, and how many grams of which reactant will be left over?

$$
3 \mathrm{H}_{2}+\mathrm{N}_{2} \longrightarrow 2 \mathrm{NH}_{3}
$$

3.69 Hydrogen and chlorine react to yield hydrogen chloride: $\mathrm{H}_{2}+\mathrm{Cl}_{2} \rightarrow 2 \mathrm{HCl}$. How many grams of HCl are formed from reaction of 3.56 g of $\mathrm{H}_{2}$ with 8.94 g of $\mathrm{Cl}_{2}$ ? Which reactant is limiting?
3.70 How many grams of the dry-cleaning solvent ethylene chloride, $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Cl}_{2}$, can be prepared by reaction of 15.4 g of ethylene, $\mathrm{C}_{2} \mathrm{H}_{4}$, with 3.74 g of $\mathrm{Cl}_{2}$ ?

$$
\mathrm{C}_{2} \mathrm{H}_{4}+\mathrm{Cl}_{2} \longrightarrow \mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Cl}_{2}
$$

3.71 How many grams of each product result from the following reactions, and how many grams of which reactant is left over?
(a) $(1.3 \mathrm{~g} \mathrm{NaCl})+\left(3.5 \mathrm{~g} \mathrm{AgNO}_{3}\right) \longrightarrow$
$(x \mathrm{~g} \mathrm{AgCl})+\left(y \mathrm{~g} \mathrm{NaNO}_{3}\right)$
(b) $\left(2.65 \mathrm{~g} \mathrm{BaCl}_{2}\right)+\left(6.78 \mathrm{~g} \mathrm{H}_{2} \mathrm{SO}_{4}\right) \longrightarrow$

$$
\left(x \mathrm{~g} \mathrm{BaSO}_{4}\right)+(y \mathrm{~g} \mathrm{HCl})
$$

3.72 Limestone $\left(\mathrm{CaCO}_{3}\right)$ reacts with hydrochloric acid according to the equation $\mathrm{CaCO}_{3}+2 \mathrm{HCl} \rightarrow$ $\mathrm{CaCl}_{2}+\mathrm{H}_{2} \mathrm{O}+\mathrm{CO}_{2}$. If 1.00 mol of $\mathrm{CO}_{2}$ has a volume of 22.4 L under the reaction conditions, how many liters of gas can be formed by reaction of 2.35 g of $\mathrm{CaCO}_{3}$ with 2.35 g of HCl ? Which reactant is limiting?
3.73 Sodium azide $\left(\mathrm{NaN}_{3}\right)$ yields $\mathrm{N}_{2}$ gas when heated to $300^{\circ} \mathrm{C}$, a reaction used in automobile air bags. If 1.00 mol of $\mathrm{N}_{2}$ has a volume of 47.0 L under the reaction conditions, how many liters of gas can be formed by heating 38.5 g of $\mathrm{NaN}_{3}$ ? The reaction is:

$$
2 \mathrm{NaN}_{3} \longrightarrow 3 \mathrm{~N}_{2}(g)+2 \mathrm{Na}
$$

3.74 Acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$ reacts with isopentyl alcohol $\left(\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}\right)$ to yield isopentyl acetate $\left(\mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}\right)$, a fragrant substance with the odor of bananas. If the yield from the reaction of acetic acid with isopentyl alcohol is $45 \%$, how many grams of isopentyl acetate are formed from 3.58 g of acetic acid and 4.75 g of isopentyl alcohol? The reaction is:

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}+\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O} \longrightarrow \mathrm{C}_{7} \mathrm{H}_{14} \mathrm{O}_{2}+\mathrm{H}_{2} \mathrm{O}
$$

3.75 Cisplatin $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}\right]$, a compound used in cancer treatment, is prepared by reaction of ammonia with potassium tetrachloroplatinate:

$$
\mathrm{K}_{2} \mathrm{PtCl}_{4}+2 \mathrm{NH}_{3} \rightarrow 2 \mathrm{KCl}+\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}
$$

How many grams of cisplatin are formed from 55.8 g of $\mathrm{K}_{2} \mathrm{PtCl}_{4}$ and 35.6 g of $\mathrm{NH}_{3}$ if the reaction takes place in $95 \%$ yield based on the limiting reactant?
3.76 If 1.87 g of acetic acid reacts with 2.31 g of isopentyl alcohol to give 2.96 g of isopentyl acetate (Problem 3.74), what is the percent yield of the reaction?
3.77 If 3.42 g of $\mathrm{K}_{2} \mathrm{PtCl}_{4}$ and 1.61 g of $\mathrm{NH}_{3}$ give 2.08 g of cisplatin (Problem 3.75), what is the percent yield of the reaction?

## Molarity, Solution Stoichiometry, Dilution, and Titration

3.78 How many moles of solute are present in each of the following solutions?
(a) 35.0 mL of $1.200 \mathrm{M} \mathrm{HNO}_{3}$
(b) 175 mL of 0.67 M glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$
3.79 How many grams of solute would you use to prepare each of the following solutions?
(a) 250.0 mL of 0.600 M ethyl alcohol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}\right)$
(b) 167 mL of 0.200 M boric acid $\left(\mathrm{H}_{3} \mathrm{BO}_{3}\right)$
3.80 How many milliliters of a $0.45 \mathrm{M} \mathrm{BaCl}_{2}$ solution contain 15.0 g of $\mathrm{BaCl}_{2}$ ?
3.81 How many milliliters of a 0.350 M KOH solution contain 0.0171 mol of KOH ?
3.82 The sterile saline solution used to rinse contact lenses can be made by dissolving 400 mg of NaCl in sterile water and diluting to 100 mL . What is the molarity of the solution?
3.83 The concentration of glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ in normal blood is approximately 90 mg per 100 mL . What is the molarity of the glucose?
3.84 Ringer's solution, used in the treatment of burns and wounds, is prepared by dissolving 4.30 g of NaCl , 0.150 g of KCl , and 0.165 g of $\mathrm{CaCl}_{2}$ in water and diluting to a volume of 500.0 mL . What is the molarity of each of the component ions in the solution?
3.85 Copper reacts with dilute nitric acid according to the following equation:

$$
\begin{aligned}
& 3 \mathrm{Cu}(s)+8 \mathrm{HNO}_{3}(a q) \longrightarrow \\
& \quad 3 \mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}(a q)+2 \mathrm{NO}(g)+4 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

If a copper penny weighing 3.045 g is dissolved in a small amount of nitric acid and the resultant solution is diluted to 50.0 mL with water, what is the molarity of the $\mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}$ ?
3.86 A bottle of 12.0 M hydrochloric acid has only 35.7 mL left in it. What will the HCl concentration be if the solution is diluted to 250.0 mL ?
3.87 What is the volume of the solution that would result by diluting 70.00 mL of 0.0913 M NaOH to a concentration of 0.0150 M ?
3.88 A flask containing 450 mL of 0.500 M HBr was accidentally knocked to the floor. How many grams of $\mathrm{K}_{2} \mathrm{CO}_{3}$ would you need to put on the spill to neutralize the acid according to the following equation?

$$
\left.\begin{array}{rl}
2 \mathrm{HBr}(a q)+\mathrm{K}_{2} \mathrm{CO}_{3}(a q) & \longrightarrow \\
2 \mathrm{KBr}(a q)
\end{array}\right) \mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
$$

3.89 The odor of skunks is caused by chemical compounds called thiols. These compounds, of which butanethiol $\left(\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{~S}\right)$ is a representative example, can be deodorized by reaction with household bleach ( NaOCl ) according to the following equation:

$$
2 \mathrm{C}_{4} \mathrm{H}_{10} \mathrm{~S}+\mathrm{NaOCl}(a q) \longrightarrow \mathrm{C}_{8} \mathrm{H}_{18} \mathrm{~S}_{2}+\mathrm{NaCl}(a q)+\mathrm{H}_{2} \mathrm{O}(a q)
$$

How many grams of butanethiol can be deodorized by reaction with 5.00 mL of 0.0985 M NaOCl ?
3.90 Potassium permanganate $\left(\mathrm{KMnO}_{4}\right)$ reacts with oxalic acid $\left(\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$ in aqueous sulfuric acid according to the following equation:

$$
\begin{aligned}
& 2 \mathrm{KMnO}_{4}+5 \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}+3 \mathrm{H}_{2} \mathrm{SO}_{4} \longrightarrow \\
& \longrightarrow \mathrm{MnSO}_{4}+10 \mathrm{CO}_{2}+8 \mathrm{H}_{2} \mathrm{O}+\mathrm{K}_{2} \mathrm{SO}_{4}
\end{aligned}
$$

How many milliliters of a $0.250 \mathrm{M} \mathrm{KMnO}_{4}$ solution are needed to react completely with 3.225 g of oxalic acid?
3.91 Oxalic acid, $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, is a toxic substance found in spinach leaves. What is the molarity of a solution made by dissolving 12.0 g of oxalic acid in enough water to give 400.0 mL of solution? How many milliliters of 0.100 M KOH would you need to titrate 25.0 mL of the oxalic acid solution according to the following equation?

$$
\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}(a q)+2 \mathrm{KOH}(a q) \longrightarrow \mathrm{K}_{2} \mathrm{C}_{2} \mathrm{O}_{4}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

## Formulas and Elemental Analysis

3.92 Urea, a substance commonly used as a fertilizer, has the formula $\mathrm{CH}_{4} \mathrm{~N}_{2} \mathrm{O}$. What is its percent composition by mass?
3.93 Calculate the mass percent composition of each of the following substances:
(a) Malachite, a green copper-containing mineral: $\mathrm{Cu}_{2}(\mathrm{OH})_{2} \mathrm{CO}_{3}$
(b) Acetaminophen, a headache remedy: $\mathrm{C}_{8} \mathrm{H}_{9} \mathrm{NO}_{2}$
(c) Prussian blue, an ink pigment: $\mathrm{Fe}_{4}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]_{3}$
3.94 What is the empirical formula of stannous fluoride, the first fluoride compound added to toothpaste to protect teeth against decay? Its mass percent composition is 24.25\% F, 75.75\% Sn.
3.95 What are the empirical formulas of each of the following substances?
(a) Ibuprofen, a headache remedy:
$75.69 \% \mathrm{C}, 15.51 \% \mathrm{O}, 8.80 \% \mathrm{H}$
(b) Tetraethyllead, the "lead" in gasoline:
$29.71 \% \mathrm{C}, 64.06 \% \mathrm{~Pb}, 6.23 \% \mathrm{H}$
(c) Zircon, a diamondlike mineral:
$34.91 \% \mathrm{O}, 15.32 \% \mathrm{Si}, 49.76 \% \mathrm{Zr}$
3.96 Combustion analysis of 45.62 mg of toluene, a commonly used solvent, gives 35.67 mg of $\mathrm{H}_{2} \mathrm{O}$ and 152.5 mg of $\mathrm{CO}_{2}$. What is the empirical formula of toluene?
3.97 Coniine, a toxic substance isolated from poison hemlock, contains only carbon, hydrogen, and nitrogen. Combustion analysis of a 5.024 mg sample yields 13.90 mg of $\mathrm{CO}_{2}$ and 6.048 mg of $\mathrm{H}_{2} \mathrm{O}$. What is the empirical formula of coniine?
3.98 Cytochrome $c$ is an iron-containing enzyme found in the cells of all aerobic organisms. If cytochrome $c$ is $0.43 \%$ Fe by mass, what is its minimum molecular mass?
3.99 Nitrogen fixation in the root nodules of peas and other leguminous plants is carried out by the molybdenumcontaining enzyme nitrogenase. What is the molecular mass of nitrogenase if the enzyme contains two molybdenum atoms and is $0.0872 \%$ Mo by mass?
3.100 Disilane, $\mathrm{Si}_{2} \mathrm{H}_{x}$, is analyzed and found to contain $90.28 \%$ silicon by mass. What is the value of $x$ ?
3.101 A certain metal sulfide, $\mathrm{MS}_{2}$, is used extensively as a high-temperature lubricant. If $\mathrm{MS}_{2}$ is $40.06 \%$ sulfur by mass, what is the identity of the metal M ?

## General Problems

3.102 Give the percent composition of each of the following substances:
(a) Glucose, $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}$
(b) Sulfuric acid, $\mathrm{H}_{2} \mathrm{SO}_{4}$
(c) Potassium permanganate, $\mathrm{KMnO}_{4}$
(d) Saccharin, $\mathrm{C}_{7} \mathrm{H}_{5} \mathrm{NO}_{3} \mathrm{~S}$
3.103 What are the empirical formulas of substances with the following mass percent compositions?
(a) Aspirin: $4.48 \% \mathrm{H}, 60.00 \% \mathrm{C}, 35.52 \% \mathrm{O}$
(b) Ilmenite (a titanium-containing ore):
$31.63 \% \mathrm{O}, 31.56 \% \mathrm{Ti}, 36.81 \% \mathrm{Fe}$
(c) Sodium thiosulfate (photographic "fixer"):
$30.36 \%$ O, 29.08\% Na, $40.56 \%$ S
3.104 Balance the following equations:
(a) $\mathrm{SiCl}_{4}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{SiO}_{2}+\mathrm{HCl}$
(b) $\mathrm{P}_{4} \mathrm{O}_{10}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{H}_{3} \mathrm{PO}_{4}$
(c) $\mathrm{CaCN}_{2}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{CaCO}_{3}+\mathrm{NH}_{3}$
(d) $\mathrm{NO}_{2}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{HNO}_{3}+\mathrm{NO}$
3.105 Sodium borohydride, $\mathrm{NaBH}_{4}$, a substance used in the synthesis of many pharmaceutical agents, can be prepared by reaction of NaH with $\mathrm{B}_{2} \mathrm{H}_{6}$ according to the equation $2 \mathrm{NaH}+\mathrm{B}_{2} \mathrm{H}_{6} \rightarrow 2 \mathrm{NaBH}_{4}$. How many grams of $\mathrm{NaBH}_{4}$ can be prepared by reaction between 8.55 g of NaH and 6.75 g of $\mathrm{B}_{2} \mathrm{H}_{6}$ ? Which reactant is limiting, and how many grams of the excess reactant will be left over?
3.106 Ferrocene, a substance proposed for use as a gasoline additive, has the percent composition $5.42 \% \mathrm{H}$, $64.56 \% \mathrm{C}$, and $30.02 \% \mathrm{Fe}$. What is the empirical formula of ferrocene?
3.107 The molar mass of HCl is $36.5 \mathrm{~g} / \mathrm{mol}$, and the average mass per HCl molecule is 36.5 amu . Use the fact that $1 \mathrm{amu}=1.6605 \times 10^{-24} \mathrm{~g}$ to calculate Avogadro's number.
3.108 What is the molarity of each ion in a solution prepared by dissolving 0.550 g of $\mathrm{Na}_{2} \mathrm{SO}_{4}, 1.188 \mathrm{~g}$ of $\mathrm{Na}_{3} \mathrm{PO}_{4}$, and $0.223 \mathrm{~g}^{2}$ of $\mathrm{Li}_{2} \mathrm{SO}_{4}$ in water and diluting to a volume of 100.00 mL ?
3.109 Ethylene glycol, commonly used as automobile antifreeze, contains only carbon, hydrogen, and oxygen. Combustion analysis of a 23.46 mg sample yields 20.42 mg of $\mathrm{H}_{2} \mathrm{O}$ and 33.27 mg of $\mathrm{CO}_{2}$. What is the empirical formula of ethylene glycol? What is its molecular formula if it has a molecular mass of 62.0 amu ?
3.110 The molecular mass of ethylene glycol (Problem 3.109) is 62.0689 amu when calculated using the atomic masses found in a standard periodic table, yet the molecular mass determined experimentally by high-resolution mass spectrometry is 62.0368 amu . Explain the discrepancy.
3.111 Balance the following equations:
(a) $\mathrm{CO}\left(\mathrm{NH}_{2}\right)_{2}(a q)+\mathrm{HOCl}(a q) \rightarrow$

$$
\mathrm{NCl}_{3}(a q)+\mathrm{CO}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

(b) $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}(s)+\mathrm{SiO}_{2}(s)+\mathrm{C}(s) \rightarrow$

$$
\mathrm{P}_{4}(g)+\mathrm{CaSiO}_{3}(l)+\mathrm{CO}(g)
$$

3.112 How many pounds of $\mathrm{CO}_{2}$ are produced from the complete combustion of 1.00 gal of gasoline. Assume that gasoline has the formula $\mathrm{C}_{8} \mathrm{H}_{18}$ and has a density of $0.703 \mathrm{~g} / \mathrm{mL}$.
3.113 A sample of $\mathrm{CaCO}_{3}$ with a mass of 6.35 g is placed in 500.0 mL of 0.31 M HCl , forming $\mathrm{CaCl}_{2}, \mathrm{H}_{2} \mathrm{O}$, and $\mathrm{CO}_{2}$. What mass in grams of $\mathrm{CO}_{2}$ is produced?
3.114 Compound X contains only carbon, hydrogen, nitrogen, and chlorine. When 1.00 g of X is dissolved in water and allowed to react with excess $\mathrm{AgNO}_{3}$, all the chlorine in X precipitates and 1.95 g of AgCl is collected. When 1.00 g of X undergoes complete combustion, 0.900 g of $\mathrm{CO}_{2}$ and 0.735 g of $\mathrm{H}_{2} \mathrm{O}$ are formed. What is the empirical formula of $X$ ?
3.115 A pulverized rock sample believed to be pure calcium carbonate is subjected to chemical analysis and found to contain $51.3 \% \mathrm{Ca}, 7.7 \% \mathrm{C}$, and $41.0 \% \mathrm{O}$ by mass. Why can't this rock sample be pure $\mathrm{CaCO}_{3}$ ?
3.116 Salicylic acid, used in the manufacture of aspirin, contains only the elements $\mathrm{C}, \mathrm{H}$, and O and has only one acidic hydrogen. When 1.00 g of salicylic acid undergoes complete combustion, $2.23 \mathrm{~g} \mathrm{CO}_{2}$ and $0.39 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}$ are obtained. When 1.00 g of salicylic acid is titrated with $0.100 \mathrm{M} \mathrm{NaOH}, 72.4 \mathrm{~mL}$ of base is needed for complete reaction. What are the empirical and molecular formulas of salicylic acid?
3.117 Compound $X$ contains only the elements $\mathrm{C}, \mathrm{H}, \mathrm{O}$, and S. A 5.00 g sample undergoes complete combustion to give 4.83 g of $\mathrm{CO}_{2}, 1.48 \mathrm{~g}$ of $\mathrm{H}_{2} \mathrm{O}$, and a certain amount of $\mathrm{SO}_{2}$ that is further oxidized to $\mathrm{SO}_{3}$ and dissolved in water to form $\mathrm{H}_{2} \mathrm{SO}_{4}$. On titration of the $\mathrm{H}_{2} \mathrm{SO}_{4}, 109.8 \mathrm{~mL}$ of 1.00 M NaOH is needed for complete reaction.
(a) What is the empirical formula of X ?
(b) When 5.00 g of X is titrated with NaOH , it is found that $X$ has two acidic hydrogens and that 54.9 mL of 1.00 M NaOH is required to completely neutralize the sample. What is the molecular formula of $X$ ?
3.118 Assume that you have 1.00 g of a mixture of benzoic acid (molec. mass $=122 \mathrm{amu}$ ) and gallic acid (molec. mass $=170 \mathrm{amu}$ ), both of which contain one
acidic hydrogen. On titrating the mixture with 0.500 M $\mathrm{NaOH}, 14.7 \mathrm{~mL}$ of base is needed to completely neutralize both acids. What mass (in grams) of each acid is present in the original mixture?
3.119 A certain alcoholic beverage contains only ethanol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}\right)$ and water. When a sample of this beverage undergoes combustion, the ethanol burns but the water simply evaporates and is collected along with the water produced by combustion. The combustion reaction is:

$$
\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}(l)+3 \mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{CO}_{2}(g)+3 \mathrm{H}_{2} \mathrm{O}(g)
$$

When a 10.00 g sample of this beverage is burned, 11.27 g of water is collected. What is the mass (in grams) of ethanol and what is the mass of water in the original sample?
3.120 A mixture of FeO and $\mathrm{Fe}_{2} \mathrm{O}_{3}$ with a mass of 10.0 g is converted to 7.43 g of pure Fe metal. What are the amounts (in grams) of FeO and $\mathrm{Fe}_{2} \mathrm{O}_{3}$ in the original sample?
3.121 A compound of formula $\mathrm{XCl}_{3}$ reacts with aqueous $\mathrm{AgNO}_{3}$ to yield a precipitate of solid AgCl according to the following equation:

$$
\mathrm{XCl}_{3}(a q)+3 \mathrm{AgNO}_{3}(a q) \longrightarrow \mathrm{X}\left(\mathrm{NO}_{3}\right)_{3}(a q)+3 \mathrm{AgCl}(s)
$$

When a solution containing 0.634 g of $\mathrm{XCl}_{3}$ was allowed to react with an excess of aqueous $\mathrm{AgNO}_{3}, 1.68$ g of solid AgCl was formed. What is the identity of the atom X ?
3.122 When eaten, dietary carbohydrates are digested to yield glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$, which is then metabolized to yield carbon dioxide and water:

$$
\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}+\mathrm{O}_{2} \longrightarrow \mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O} \quad \text { Unbalanced }
$$

Balance the equation, and calculate both the mass in grams and the volume in liters of the $\mathrm{CO}_{2}$ produced from 66.3 g of glucose, assuming that 1 mol of $\mathrm{CO}_{2}$ has a volume of 25.4 L at normal body temperature.
3.123 Other kinds of titrations are possible in addition to acid-base titrations. For example, the concentration of a solution of potassium permanganate, $\mathrm{KMnO}_{4}$, can be determined by titration against a known amount of oxalic acid, $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, according to the following equation:

$$
\begin{aligned}
& 5 \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}(a q)+2 \mathrm{KMnO}_{4}(a q)+3 \mathrm{H}_{2} \mathrm{SO}_{4}(a q) \longrightarrow \\
& 10 \mathrm{CO}_{2}(g)+2 \mathrm{MnSO}_{4}(a q)+\mathrm{K}_{2} \mathrm{SO}_{4}(a q)+8 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

What is the concentration of a $\mathrm{KMnO}_{4}$ solution if 22.35 mL reacts with 0.5170 g of oxalic acid?
3.124 A copper wire having a mass of 2.196 g was allowed to react with an excess of sulfur. The excess sulfur was then burned, yielding $\mathrm{SO}_{2}$ gas. The mass of the copper sulfide produced was 2.748 g .
(a) What is the percent composition of copper sulfide?
(b) What is its empirical formula?
(c) Calculate the number of copper ions per cubic centimeter if the density of the copper sulfide is $5.6 \mathrm{~g} / \mathrm{cm}^{3}$.
3.125 Element $X$, a member of group 5 A , forms two chlorides, $\mathrm{XCl}_{3}$ and $\mathrm{XCl}_{5}$. Reaction of an excess of $\mathrm{Cl}_{2}$ with 8.729 g of $\mathrm{XCl}_{3}$ yields 13.233 g of $\mathrm{XCl}_{5}$. What is the atomic mass and the identity of the element $X$ ?
3.126 A mixture of $\mathrm{XCl}_{3}$ and $\mathrm{XCl}_{5}$ (see Problem 3.125) weighing 10.00 g contains $81.04 \% \mathrm{Cl}$ by mass. How many grams of $\mathrm{XCl}_{3}$ and how many grams of $\mathrm{XCl}_{5}$ are present in the mixture?
3.127 A 1.268 g sample of a metal carbonate $\mathrm{MCO}_{3}$ was treated with 100.00 mL of $0.1083 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$, yielding $\mathrm{CO}_{2}$ gas and an aqueous solution of the metal sulfate. The solution was boiled to remove all the dissolved $\mathrm{CO}_{2}$ and was then titrated with 0.1241 M NaOH . A 71.02 mL volume of NaOH was required to neutralize the excess $\mathrm{H}_{2} \mathrm{SO}_{4}$.
(a) What is the identity of the metal M ?
(b) How many liters of $\mathrm{CO}_{2}$ gas were produced if the density of $\mathrm{CO}_{2}$ is $1.799 \mathrm{~g} / \mathrm{L}$ ?
3.128 Ammonium nitrate, a potential ingredient of terrorist bombs, can be made nonexplosive by addition of diammonium hydrogen phosphate, $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}$. Analysis of a such a $\mathrm{NH}_{4} \mathrm{NO}_{3}-\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}$ mixture
showed the mass percent of nitrogen to be $30.43 \%$. What is the mass ratio of the two components in the mixture?
3.129 Window glass is typically made by mixing soda ash $\left(\mathrm{Na}_{2} \mathrm{CO}_{3}\right)$, limestone $\left(\mathrm{CaCO}_{3}\right)$, and silica sand $\left(\mathrm{SiO}_{2}\right)$ and then heating to $1500^{\circ} \mathrm{C}$ to drive off $\mathrm{CO}_{2}$ from the $\mathrm{Na}_{2} \mathrm{CO}_{3}$ and $\mathrm{CaCO}_{3}$. The resultant glass consists of about $12 \% \mathrm{Na}_{2} \mathrm{O}$ by mass, $13 \% \mathrm{CaO}$ by mass, and $75 \%$ $\mathrm{SiO}_{2}$ by mass. How much of each reactant would you start with to prepare 0.35 kg of glass?
3.130 An unidentified metal M reacts with an unidentified halogen X to form a compound $\mathrm{MX}_{2}$. When heated, the compound decomposes by the reaction:

$$
2 \mathrm{MX}_{2}(s) \longrightarrow 2 \mathrm{MX}(s)+\mathrm{X}_{2}(g)
$$

When 1.12 g of $\mathrm{MX}_{2}$ is heated, 0.720 g of MX is obtained, along with 56.0 mL of $\mathrm{X}_{2}$ gas. Under the conditions used, 1.00 mol of the gas has a volume of 22.41 L .
(a) What is the atomic mass and identity of the halogen $X$ ?
(b) What is the atomic mass and identity of the metal M?

## eMedia Problems

3.131 The Balancing Equations activity (eChapter 3.1) allows you to balance three different chemical equations.
(a) In the activity, select the Decomposition reaction and balance it.
(b) Rewrite the equation such that ammonium nitrate reacts to yield only elements ( $\mathrm{N}_{2}, \mathrm{H}_{2}$, and $\mathrm{O}_{2}$ ), and balance this new equation.
(c) Draw diagrams similar to those in Question 1 (eChapter 3.1) to represent the decomposition of 2 ammonium nitrate particles according to the balanced equations in (a) and (b).
(d) Explain how it is possible for the number of product molecules to be different in parts (a) and (b).
(e) Is it also possible for the number of product atoms to be different in parts (a) and (b)? Explain.
3.132 Using the Mole Diagram in eChapter 3.4, write out the steps required to determine the mass of NaOH required to react completely with 20.5 g of $\mathrm{H}_{2} \mathrm{SO}_{4}$. Determine the mass of water produced when 17.4 g of $\mathrm{Na}_{2} \mathrm{SO}_{4}$ is generated.
3.133 Using the Limiting Reagents (Stoichiometry) simulation (eChapter 3.6), perform the redox reaction between magnesium metal and oxygen gas by combining equal masses of both reactants.
(a) Which reactant is the limiting reactant?
(b) Explain how it is possible for there to be a limiting reactant when both are present in equal mass.
(c) Convert the mass you selected to moles for each reactant.
(d) Explain how it is possible for the reactant present in the greatest number of moles to be the limiting reactant.
3.134 Calculate the volume of a solution that
(a) contains 25.0 g of sulfuric acid and is 0.073 M in sulfuric acid;
(b) contains 40.0 g of potassium chloride and is 0.101 M in potassium chloride;
(c) Use the Molarity activity (eChapter 3.7) to verify your answers in (a) and (b).
(d) Use the Molarity activity to determine the mass of NaCl required to make 2.5 L of a 0.151 M solution of NaCl . Would it require a larger or smaller mass of HCl to make 2.5 L of a 0.151 M solution? Explain.
3.135 The Acid-Base Titration activity (eChapter 3.10) allows you to simulate the titration of five acids, A through E. Assuming that the acids can all provide one hydrogen, perform simulated titrations and determine the concentration of all five acids.
3.136 Using the Mole Diagram in eChapter 3.10, write out the calculations required to determine the concentration of an HCl solution by titration with a 0.134 M NaOH solution. What volume of this solution would be required to titrate 20.00 L of a 3.18 M HCl solution?
3.137 Calculate the percent composition of each of the following compounds
(a) $\mathrm{H}_{2} \mathrm{O}_{2}$ (hydrogen peroxide, an antiseptic)
(b) $\mathrm{Mg}(\mathrm{OH})_{2}$ (milk of magnesia, an antacid)
(c) $\mathrm{N}_{2} \mathrm{O}$ (laughing gas, an anesthetic)
(c) Use the Molecular Mass and Percent Composition activity (eChapter 3.11) to verify your answers.
(e) Look at the percent composition of water. Explain how it can be $88.8 \%$ oxygen when there are twice as many hydrogen atoms as oxygen atoms.

## Chapter

## Reactions in Aqueous Solution

## Ours is a world based on water.

Approximately $71 \%$ of the earth's surface is covered by water, and another $3 \%$ is covered by ice; $66 \%$ of an adult human
body is water, and water is needed to sustain all living organisms. It's therefore not surprising that a large amount of important chemistry takes place in water-that is, in aqueous solution.

We saw in the previous chapter how chemical reactions are described and how certain mass relationships must be obeyed when reactions occur. In this chapter,

## CONTENTS

The corrosion evident on this anchor from a sunken ship occurs by a typical oxidation-reduction reaction of the kind discussed in this chapter.
4.1 Some Ways that Chemical Reactions Occur
4.2 Electrolytes in Aqueous Solution
4.3 Aqueous Reactions and Net Ionic Equations
4.4 Precipitation Reactions and Solubility Rules
4.5 Acids, Bases, and Neutralization Reactions
4.6 Oxidation-Reduction (Redox) Reactions
4.7 Identifying Redox Reactions
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4.10 Balancing Redox Reactions: The Half-Reaction Method
4.11 Redox Titrations
4.12 Some Applications of Redox Reactions

- Interlude-Photography: A Series of Redox Reactions

$\triangle$ Reaction of aqueous $\mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}$ with aqueous KI gives a yellow precipitate of $\mathrm{PbI}_{2}$.
we'll continue our study of chemical reactions by seeing how different reactions can be classified and by learning some of the general ways reactions take place.


### 4.1 Some Ways that Chemical Reactions Occur

Every chemical reaction occurs for a reason-a reason that involves the energies of reactants and products and that we'll explore in more depth in Chapter 8. Without going into detail at present, it's often convenient to think of reactions as being "driven" from reactants to products by some energetic "driving force" that pushes them along.

Aqueous reactions can be grouped into three general categories, each with its own kind of driving force: precipitation reactions, acid-base neutralization reactions, and oxidation-reduction reactions. Let's look briefly at an example of each before studying them in more detail in subsequent sections.

- Precipitation reactions are processes in which soluble reactants yield an insoluble solid product that drops out of the solution. Formation of this stable product removes material from the aqueous solution and provides the driving force for the reaction. Most precipitations take place when the anions and cations of two ionic compounds change partners. For example, an aqueous solution of lead(II) nitrate reacts with an aqueous solution of potassium iodide to yield an aqueous solution of potassium nitrate plus an insoluble yellow precipitate of lead iodide:

$$
\mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}(a q)+2 \mathrm{KI}(a q) \longrightarrow 2 \mathrm{KNO}_{3}(a q)+\mathrm{PbI}_{2}(s)
$$

- Acid-base neutralization reactions are processes in which an acid reacts with a base to yield water plus an ionic compound called a salt. You might recall from Section 2.9 that we defined acids as compounds that produce $\mathrm{H}^{+}$ions when dissolved in water and bases as compounds that produce $\mathrm{OH}^{-}$ions when dissolved in water. Thus, the driving force behind a neutralization reaction is the production of the stable covalent water molecule by removal of $\mathrm{H}^{+}$ and $\mathrm{OH}^{-}$ions from solution. The reaction between hydrochloric acid and aqueous sodium hydroxide to yield water plus aqueous sodium chloride is a typical example:

$$
\mathrm{HCl}(a q)+\mathrm{NaOH}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{NaCl}(a q)
$$

- Oxidation-reduction reactions, or redox reactions, are processes in which one or more electrons are transferred between reaction partners (atoms, molecules, or ions). The driving force is a decrease in electrical potential, analogous to what happens when a live electrical wire is grounded and electrons flow from the wire to the ground. As a result of this transfer of electrons, charges on atoms in the various reactants change. When metallic magnesium reacts with iodine vapor, for instance, a magnesium atom gives an electron to each of two iodine atoms, forming an $\mathrm{Mg}^{2+}$ ion and two $\mathrm{I}^{-}$ ions. The charge on the magnesium changes from 0 to +2 , and the charge on each iodine changes from 0 to -1 :

$$
\mathrm{Mg}(s)+\mathrm{I}_{2}(g) \longrightarrow \operatorname{MgI}_{2}(s)
$$

- PROBLEM 4.1 Classify each of the following processes as a precipitation, acid-base neutralization, or redox reaction:
(a) $\mathrm{AgNO}_{3}(a q)+\mathrm{KCl}(a q) \rightarrow \mathrm{AgCl}(s)+\mathrm{KNO}_{3}(a q)$
(b) $2 \mathrm{P}(s)+3 \mathrm{Br}_{2}(l) \rightarrow 2 \mathrm{PBr}_{3}(l)$
(c) $\mathrm{Ca}(\mathrm{OH})_{2}(a q)+2 \mathrm{HNO}_{3}(a q) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{Ca}\left(\mathrm{NO}_{3}\right)_{2}(a q)$


### 4.2 Electrolytes in Aqueous Solution

We all know from experience that both sugar (sucrose) and table salt ( NaCl ) dissolve in water. The solutions that result, though, are quite different. When sucrose, a molecular substance, dissolves in water, the solution that results contains neutral sucrose molecules surrounded by water. When NaCl , an ionic substance, dissolves in water, the solution contains separate $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions surrounded by water. Because of the presence of the ions, the NaCl solution conducts electricity, but the sucrose solution does not.

$$
\begin{aligned}
& \underset{\substack{\text { Sucrose }}}{\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}(s)} \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}(a q) \\
& \quad \mathrm{NaCl}(s) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{Na}^{+}(a q)+\mathrm{Cl}^{-}(a q)
\end{aligned}
$$

The electrical conductivity of an aqueous NaCl solution is easy to demonstrate using a battery, a lightbulb, and several pieces of wire, connected as shown in Figure 4.1. When the wires are dipped into an aqueous NaCl solution, the positively charged $\mathrm{Na}^{+}$ions move through the solution toward the wire connected to the negatively charged terminal of the battery. At the same time, the negatively charged $\mathrm{Cl}^{-}$ions move toward the wire connected to the positively charged terminal of the battery. The resulting movement of ions allows a current to flow, so the bulb lights. When the wires are dipped into an aqueous sucrose solution, however, there are no ions to carry the current, so the bulb remains dark.

Substances such as NaCl or KBr , which dissolve in water to produce conducting solutions of ions, are called electrolytes. Substances such as sucrose or ethyl alcohol, which do not produce ions in aqueous solution, are called nonelectrolytes. Most electrolytes are ionic compounds, but some are molecular. Hydrogen


vRelating properties to structure is an important skill. Later in this text it will be shown that species that are soluble in water are either ionic or polar, like water, as indicated in the rule of thumb "Like dissolves like." Showing that water, sucrose, methyl alcohol, and ethyl alcohol all contain-OH groups will demonstrate their "likeness."

Bassam Z. Shakhashiri, "Conductivity and Extent of Dissociation of Acids in Aqueous Solution," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 140-145. Universal indicator and a conductivity probe are used to explore the relative acidity and conductivity of a series of aqueous acids.

[] ${ }^{\mathrm{J}}$
John J. Fortman, "Pictorial Analogies X: Solutions of Electrolytes," J. Chem. Educ., Vol. 71, 1994, 27-28.

$\nabla$Dissociation is the fragmentation of a neutral species into ionic species.

FIGURE 4.1 A simple device to demonstrate the electrical conductivity of an ionic solution. (a) A solution of NaCl conducts electricity because of the movement of charged particles (ions), thereby completing the circuit and allowing the bulb to light. (b) A solution of sucrose does not conduct electricity or complete the circuit because it has no charged particles. The bulb therefore remains dark.


Electrolytes and Nonelectrolytes movie

Albert Kowalak, "When is a Strong Electrolyte Strong?" J. Chem. Educ., Vol. 65, 1988, 607.


Strong electrolytes are usually soluble ionic compounds or strong acids. Weak electrolytes are typically weak acids or weak bases. Common nonelectrolytes are water, alcohols, and sugars.

0Note that $\mathrm{HCl}, \mathrm{HBr}$, and HI are strong electrolytes, but HF is a weak electrolyte. This is an example of how the properties of the first element in a group (fluorine) differ from those of the other members of the group.
chloride, for example, is a molecular compound when pure but dissociates (splits apart) to give $\mathrm{H}^{+}$and $\mathrm{Cl}^{-}$ions when it dissolves in water.

$$
\mathrm{HCl}(g) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{H}^{+}(a q)+\mathrm{Cl}^{-}(a q)
$$

Compounds that dissociate to a large extent (70-100\%) into ions when dissolved in water are said to be strong electrolytes, while compounds that dissociate to only a small extent are weak electrolytes. Potassium chloride and most other ionic compounds, for instance, are largely dissociated in dilute solution and are thus strong electrolytes. Acetic acid, by contrast, dissociates to the extent of about $1.3 \%$ in a 0.10 M solution and is a weak electrolyte. As a result, a 0.10 M solution of acetic acid is only weakly conducting.


Note that when we write a dissociation, we use a forward-and-backward double arrow $\rightleftharpoons$ to indicate that the reaction takes place simultaneously in both directions. That is, a dissociation is a dynamic process in which an equilibrium is established between the forward and reverse reactions. The balance between the two opposing reactions defines the exact concentrations of the various species in solution. We'll learn much more about chemical equilibria in subsequent chapters.

A brief list of some common substances classified according to their electrolyte strength is given in Table 4.1. Note that pure water is classified as a nonelectrolyte because it does not dissociate appreciably into $\mathrm{H}^{+}$and $\mathrm{OH}^{-}$ions. We'll explore the dissociation of water in more detail in Chapter 15.

TABLE 4.1 Electrolyte Classification of Some Common Substances

| Strong Electrolytes | Weak Electrolytes | Nonelectrolytes |
| :--- | :--- | :--- |
| $\mathrm{HCl}, \mathrm{HBr}, \mathrm{HI}$ | $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ | $\mathrm{H}_{2} \mathrm{O}$ |
| $\mathrm{HClO}_{4}$ | HF | $\mathrm{CH}_{3} \mathrm{OH}$ (methyl alcohol) |
| $\mathrm{HNO}_{3}$ |  | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ (ethyl alcohol) |
| $\mathrm{H}_{2} \mathrm{SO}_{4}$ |  | $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$ (sucrose) |
| KBr | Most compounds of carbon |  |
| NaCl | (organic compounds) |  |
| $\mathrm{NaOH}, \mathrm{KOH}$ |  |  |
| Other soluble ionic <br> $\quad$ compounds |  |  |

## Worked Example 4.1

What is the total molar concentration of ions in a 0.350 M solution of the strong electrolyte $\mathrm{Na}_{2} \mathrm{SO}_{4}$, assuming complete dissociation?

## Strategy

First, we need to know how many ions are produced by dissociation of $\mathrm{Na}_{2} \mathrm{SO}_{4}$. Writing the equation for dissolving $\mathrm{Na}_{2} \mathrm{SO}_{4}$ in water shows that 3 moles of ions are formed- 2 moles of $\mathrm{Na}^{+}$and 1 mole of $\mathrm{SO}_{4}{ }^{2-}$

$$
\mathrm{Na}_{2} \mathrm{SO}_{4}(s) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} 2 \mathrm{Na}^{+}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q)
$$

## Solution

The total molar concentration of ions is three times the molarity of $\mathrm{Na}_{2} \mathrm{SO}_{4}$, or 1.05 M .

$$
\frac{0.350 \mathrm{~mol} \mathrm{Na}_{2} \mathrm{SO}_{4}^{-}}{1 \mathrm{~L}} \times \frac{3 \mathrm{molions}}{1 \mathrm{~mol} \mathrm{Na}_{2} \mathrm{SO}_{4}^{-}}=1.05 \mathrm{M}
$$

- PROBLEM 4.2 What is the molar concentration of $\mathrm{Br}^{-}$ions in a 0.225 M aqueous solution of $\mathrm{FeBr}_{3}$, assuming complete dissociation?
- KEY CONCEPT PROBLEM 4.3 Three different substances $\mathrm{A}_{2} \mathrm{X}, \mathrm{A}_{2} \mathrm{Y}$, and $\mathrm{A}_{2} \mathrm{Z}$ were dissolved in water, with the following results. (Water molecules are omitted for clarity.) Which of the substances is the strongest electrolyte, and which the weakest? Explain.

$\mathrm{A}_{2} \mathrm{X}$

$\mathrm{A}_{2} \mathrm{Y}$



## 4.3 | Aqueous Reactions and Net Ionic Equations

The equations we've been writing up to this point have all been molecular equations. That is, all the substances involved in reactions have been written using their full formulas as if they were molecules. In Section 4.1, for example, we wrote the precipitation reaction of lead(II) nitrate with potassium iodide to yield solid $\mathrm{PbI}_{2}$ using only the parenthetical $(a q)$ to indicate that the reaction takes place in aqueous solution. Nowhere was it indicated that ions are involved:

## A MOLECULAR EQUATION

$$
\mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}(a q)+2 \mathrm{KI}(a q) \longrightarrow 2 \mathrm{KNO}_{3}(a q)+\mathrm{PbI}_{2}(s)
$$

In fact, lead nitrate, potassium iodide, and potassium nitrate are strong electrolytes that dissolve in water to yield solutions of ions. Thus, it's more accurate to write the reaction as an ionic equation, in which all the ions are explicitly shown:

AN IONIC EQUATION

$$
\mathrm{Pb}^{2+}(a q)+2 \mathrm{NO}_{3}^{-}(a q)+2 \mathrm{~K}^{+}(a q)+2 \mathrm{I}^{-}(a q) \longrightarrow 2 \mathrm{~K}^{+}(a q)+2 \mathrm{NO}_{3}^{-}(a q)+\mathrm{PbI}_{2}(s)
$$

A look at this ionic equation shows that the $\mathrm{NO}_{3}{ }^{-}$and $\mathrm{K}^{+}$ions undergo no change during the reaction. Instead, they appear on both sides of the reaction arrow and act merely as spectator ions, whose only role is to balance the charge. The actual reaction, when stripped to its essentials, can be described more simply by writing a net ionic equation, in which only the ions undergoing change are shown-the $\mathrm{Pb}^{2+}$ and $\mathrm{I}^{-}$ions in this instance. The spectator ions are not shown.

$\square$
A molecular equation shows complete formulas of reactants and products; an ionic equation shows which substances are present as ions; a net ionic equation shows only those ions and molecules that react.

AN IONIC EQUATION

$$
\mathrm{Pb}^{2+}(a q)+2 \mathrm{NO}_{3}^{-}(a q)+2 \mathrm{~K}^{+}(a q)+2 \mathrm{I}^{-}(a q) \longrightarrow 2 \mathrm{~K}^{+}(a q)+2 \mathrm{NO}_{3}^{-}(a q)+\mathrm{PbI}_{2}(s)
$$

## A NET IONIC EQUATION

$$
\mathrm{Pb}^{2+}(a q)+2 \mathrm{I}^{-}(a q) \longrightarrow \mathrm{PbI}_{2}(s)
$$

v
While not included in the net ionic equation, spectator ions are present in solution and must be included in the computation of the molar mass of the compound dissolved.

Betty J. Wruck, "Reinforcing Net Ionic Equation Writing," J. Chem. Educ., Vol. 73, 1996, 149-150.

Leaving the spectator ions out of a net ionic equation does not imply that their presence is irrelevant. Certainly, if a reaction occurs by mixing a solution of $\mathrm{Pb}^{2+}$ ions with a solution of $\mathrm{I}^{-}$ions, then those solutions must also contain additional ions to balance the charge in each: The $\mathrm{Pb}^{2+}$ solution must contain an anion, and the $\mathrm{I}^{-}$solution must contain a cation. Leaving these other ions out of the net ionic equation merely implies that the specific identity of the spectator ions is not important; any nonreactive ions could fill the same role.

## Worked Example 4.2

Aqueous hydrochloric acid reacts with zinc metal to yield hydrogen gas and aqueous zinc chloride. Write a net ionic equation for the process.

$$
2 \mathrm{HCl}(a q)+\mathrm{Zn}(s) \longrightarrow \mathrm{H}_{2}(g)+\mathrm{ZnCl}_{2}(a q)
$$

## Strategy

First, write the ionic equation, listing all the species present in solution. Both HCl (a molecular compound; Table 4.1) and $\mathrm{ZnCl}_{2}$ (an ionic compound) are strong electrolytes that exist as ions in solution. Then, find the ions that are present on both sides of the reaction arrow (the spectator ions) and cancel them, leaving the net ionic equation.

## Solution

## IONIC EQUATION

$$
2 \mathrm{H}^{+}(a q)+2 \mathrm{Cl}^{-}(a q)+\mathrm{Zn}(s) \longrightarrow \mathrm{H}_{2}(g)+\mathrm{Zn}^{2+}(a q)+2 \mathrm{Cl}^{-}(a q)
$$

## NET IONIC EQUATION

$$
2 \mathrm{H}^{+}(a q)+\mathrm{Zn}(s) \longrightarrow \mathrm{H}_{2}(g)+\mathrm{Zn}^{2+}(a q)
$$



A Zinc metal reacts with aqueous hydrochloric acid to give hydrogen gas and aqueous $\mathrm{Zn}^{2+}$ ions.

$C w n W$Ionic Compounds activity; Precipitation Reactions movie

[^5]- PROBLEM 4.4 Write net ionic equations for the following reactions:
(a) $2 \mathrm{AgNO}_{3}(a q)+\mathrm{Na}_{2} \mathrm{CrO}_{4}(a q) \rightarrow \mathrm{Ag}_{2} \mathrm{CrO}_{4}(s)+2 \mathrm{NaNO}_{3}(a q)$
(b) $\mathrm{H}_{2} \mathrm{SO}_{4}(a q)+\mathrm{MgCO}_{3}(s) \rightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CO}_{2}(g)+\mathrm{MgSO}_{4}(a q)$
(c) $\mathrm{Hg}_{2}\left(\mathrm{NO}_{3}\right)_{2}(a q)+2 \mathrm{NH}_{4} \mathrm{Cl}(a q) \rightarrow \mathrm{Hg}_{2} \mathrm{Cl}_{2}(s)+2 \mathrm{NH}_{4} \mathrm{NO}_{3}(a q)$


### 4.4 Precipitation Reactions and Solubility Rules

To predict whether a precipitation reaction will occur on mixing aqueous solutions of two substances, you must know the solubility of each potential product-that is, how much of each compound will dissolve in a given amount of solvent at a given temperature. If a substance has a low solubility in water, it is likely to precipitate from an aqueous solution. If a substance has a high solubility in water, no precipitate will form.

Solubility is a complex matter, and it's not always possible to make correct predictions. In addition, solubilities depend on the concentrations of the reactant ions, and the very words "soluble" and "insoluble" are imprecise. As a rule of thumb, though, a compound is probably soluble if it meets either (or both) of the following criteria:

1. A compound is probably soluble if it contains one of the following cations:

- Group 1A cation: $\mathrm{Li}^{+}, \mathrm{Na}^{+}, \mathrm{K}^{+}, \mathrm{Rb}^{+}, \mathrm{Cs}^{+}$
- Ammonium ion: $\mathrm{NH}_{4}^{+}$

2. A compound is probably soluble if it contains one of the following anions:

- Halide: $\mathrm{Cl}^{-}, \mathrm{Br}^{-}, \mathrm{I}^{-}$except $\mathrm{Ag}^{+}, \mathrm{Hg}_{2}{ }^{2+}$, and $\mathrm{Pb}^{2+}$ compounds
- Nitrate $\left(\mathrm{NO}_{3}^{-}\right)$, perchlorate $\left(\mathrm{ClO}_{4}^{-}\right)$, acetate $\left(\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right)$, sulfate $\left(\mathrm{SO}_{4}{ }^{2-}\right)$ except $\mathrm{Ba}^{2+}, \mathrm{Hg}_{2}{ }^{2+}$, and $\mathrm{Pb}^{2+}$ sulfates

A compound that does not contain one of the ions listed above is probably not soluble. Thus, NaOH , which contains a group 1 A cation, and $\mathrm{BaCl}_{2}$, which contains a halide anion, are both soluble. A compound such as $\mathrm{CaCO}_{3}$, however, contains neither a group 1A cation nor any of the anions on the list and is therefore not soluble.

Using these guidelines not only makes it possible to predict whether a precipitate will form when solutions of two ionic compounds are mixed but also makes it possible to prepare a specific compound by purposefully carrying out a precipitation. If, for example, you wanted to prepare a sample of silver carbonate, $\mathrm{Ag}_{2} \mathrm{CO}_{3}$, you could mix a solution of $\mathrm{AgNO}_{3}$ with a solution of $\mathrm{Na}_{2} \mathrm{CO}_{3}$. Both starting compounds are soluble in water, as is $\mathrm{NaNO}_{3}$. Silver carbonate is the only insoluble combination of ions and will therefore precipitate from solution.

$$
2 \mathrm{AgNO}_{3}(a q)+\mathrm{Na}_{2} \mathrm{CO}_{3}(a q) \longrightarrow \mathrm{Ag}_{2} \mathrm{CO}_{3}(s)+2 \mathrm{NaNO}_{3}(a q)
$$

## Worked Example 4.3

Predict whether a precipitation reaction will occur when aqueous solutions of $\mathrm{CdCl}_{2}$ and $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{~S}$ are mixed. Write the net ionic equation.

## Strategy

Write the possible reaction, identify the two potential products, and predict the solubility of each. In the present instance, $\mathrm{CdCl}_{2}$ and $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{~S}$ might give CdS and $2 \mathrm{NH}_{4} \mathrm{Cl}$ :

$$
\text { ?? } \quad \mathrm{CdCl}_{2}(a q)+\left(\mathrm{NH}_{4}\right)_{2} \mathrm{~S}(a q) \longrightarrow \mathrm{CdS}+2 \mathrm{NH}_{4} \mathrm{Cl} \text { ?? }
$$

## Solution

Of the two possible products, the solubility guidelines predict that CdS , a sulfide, is insoluble and that $\mathrm{NH}_{4} \mathrm{Cl}$, an ammonium compound, is soluble. Thus, a precipitation reaction will occur:

$$
\mathrm{Cd}^{2+}(a q)+\mathrm{S}^{2-}(a q) \longrightarrow \mathrm{CdS}(s)
$$

## Worked Example 4.4

How might you use a precipitation reaction to prepare a sample of $\mathrm{CuCO}_{3}$ ? Write the net ionic equation.

## Strategy

To prepare a precipitate of $\mathrm{CuCO}_{3}$, a soluble $\mathrm{Cu}^{2+}$ compound must react with a soluble $\mathrm{CO}_{3}{ }^{2-}$ compound.

## Solution

A look at the solubility guidelines suggests that $\mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}$ and $\mathrm{Na}_{2} \mathrm{CO}_{3}$ (among many other possibilities) might work:

$$
\begin{gathered}
\mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}(a q)+\mathrm{Na}_{2} \mathrm{CO}_{3}(a q) \longrightarrow 2 \mathrm{NaNO}_{3}(a q)+\mathrm{CuCO}_{3}(s) \\
\mathrm{Cu}^{2+}(a q)+\mathrm{CO}_{3}{ }^{2-}(a q) \longrightarrow \mathrm{CuCO}_{3}(s)
\end{gathered}
$$

v$\mathrm{Hg}_{2}{ }^{2+}$ is a polyatomic ion with Hg in the +1 oxidation state.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Solubility of Some Silver Compounds," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 83-85. The solubility of a series of silver salts and complexes is explored in this demonstration.


- Reaction of aqueous $\mathrm{AgNO}_{3}$ with aqueous $\mathrm{Na}_{2} \mathrm{CO}_{3}$ gives a white precipitate of $\mathrm{Ag}_{2} \mathrm{CO}_{3}$.
L. R. Summerlin, C. L.

Borgford, and J. B. Ealy, "Name That Precipitate," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 121-123. Blue, brown, red, white, and yellow precipitates are formed when solutions containing +2 cations of mercury , nickel, lead, and barium are mixed with solutions containing carbonate, chloride, iodide, and sulfate anions. Students are asked to name and determine the formula of each precipitate and to write an ionic equation for each reaction.

## Worked Key Concept Example 4.5

An aqueous solution of an anion, represented by blue spheres, is added to a solution of a cation, represented by red spheres, and the following result is obtained. Which cations and anions, chosen from the following lists, are compatible with the observed results?


## Strategy

The process represented in the drawing is a precipitation reaction because ions in solution fall to the bottom of the container in an ordered arrangement. Counting the spheres shows that the cation and anion react in equal numbers ( 8 of each), so they must have the same number of charges-either both singly charged or both doubly charged. (There is no triply charged cation in the list.) Look at all the possible combinations, and decide which are soluble and which would precipitate.

## Solution

Possible combinations of singly charged ions: $\mathrm{AgNO}_{3}, \mathrm{KNO}_{3}, \mathrm{AgCl}, \mathrm{KCl}$
Possible combinations of doubly charged ions: $\mathrm{CaCO}_{3}, \mathrm{CdCO}_{3}$
Of the possible combinations, $\mathrm{AgCl}, \mathrm{CaCO}_{3}$, and $\mathrm{CdCO}_{3}$ are insoluble, so the anion might be $\mathrm{Cl}^{-}$or $\mathrm{CO}_{3}{ }^{2-}$, and the cation might be $\mathrm{Ag}^{+}$or $\mathrm{Cd}^{2+}$.

- PROBLEM 4.5 Predict the solubility of each of the following compounds:
(a) $\mathrm{CdCO}_{3}$
(b) MgO
(c) $\mathrm{Na}_{2} \mathrm{~S}$
(d) $\mathrm{PbSO}_{4}$
(e) $\left(\mathrm{NH}_{4}\right)_{3} \mathrm{PO}_{4}$
(f) $\mathrm{HgCl}_{2}$

PROBLEM 4.6 Predict whether a precipitation reaction will occur in each of the following situations. Write a net ionic equation for each reaction that does occur.
(a) $\mathrm{NiCl}_{2}(a q)+\left(\mathrm{NH}_{4}\right)_{2} \mathrm{~S}(a q) \rightarrow$
(b) $\mathrm{Na}_{2} \mathrm{CrO}_{4}(a q)+\mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}(a q) \rightarrow$
(c) $\mathrm{AgClO}_{4}(a q)+\mathrm{CaBr}_{2}(a q) \rightarrow$
(d) $\mathrm{ZnCl}_{2}(a q)+\mathrm{K}_{2} \mathrm{CO}_{3}(a q) \rightarrow$

PROBLEM 4.7 How might you use a precipitation reaction to prepare a sample of $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$ ? Write the net ionic equation.

- KEY CONCEPT PROBLEM 4.8 An aqueous solution of an anion, represented by blue spheres, is added to a solution of a cation, represented by green spheres, and the following result is obtained. Which cations and anions, chosen from the following lists, are compatible with the observed results?



### 4.5 Acids, Bases, and Neutralization Reactions

We've mentioned acids and bases on several previous occasions, but now let's look at both more carefully. In 1777 the French chemist Antoine Lavoisier proposed that all acids contain a common element: oxygen. In fact, the word "oxygen" is derived from a Greek phrase meaning "acid former." Lavoisier's idea had to be modified, however, when the English chemist Sir Humphrey Davy (1778-1829) showed in 1810 that muriatic acid (now called hydrochloric acid) contains only hydrogen and chlorine but no oxygen. Davy's studies thus suggested that the common element in acids is hydrogen, not oxygen.

The relation between acidic behavior and the presence of hydrogen in a compound was clarified in 1887 by the Swedish chemist Svante Arrhenius (1859-1927). Arrhenius proposed that acids are substances that dissociate in water to produce hydrogen ions $\left(\mathrm{H}^{+}\right)$and that bases are substances that dissociate in water to yield hydroxide ions $\left(\mathrm{OH}^{-}\right)$:

$$
\left.\begin{array}{rl}
\begin{array}{r}
\mathrm{HA}(a q) \\
\text { An acid }
\end{array} & \longrightarrow \mathrm{H}^{+}(a q)+\mathrm{A}^{-}(a q) \\
\mathrm{MOH}(a q) & \longrightarrow \mathrm{M}^{+}(a q)+\mathrm{OH}^{-}(a q) \\
\text { A base }
\end{array}\right)
$$

In these equations, HA is a general formula for an acid—for example, HCl or $\mathrm{HNO}_{3}$-and MOH is a general formula for a metal hydroxide-for example, NaOH or KOH .

Although convenient to use in equations, the symbol $\mathrm{H}^{+}(a q)$ does not really represent the structure of the ion present in aqueous solution. As a bare hydrogen nucleus (proton) with no electron nearby, $\mathrm{H}^{+}$is much too reactive to exist by itself. Rather, the $\mathrm{H}^{+}$attaches to a water molecule, giving the more stable hydronium ion, $\mathrm{H}_{3} \mathrm{O}^{+}$. We'll sometimes write $\mathrm{H}^{+}(a q)$ for convenience, particularly when balancing equations, but will more often write $\mathrm{H}_{3} \mathrm{O}^{+}(a q)$ to represent an aqueous acid solution. Hydrogen chloride, for instance, gives $\mathrm{Cl}^{-}(a q)$ and $\mathrm{H}_{3} \mathrm{O}^{+}(a q)$ when it dissolves in water.


Different acids dissociate to different extents in aqueous solution. Those acids that dissociate to a large extent are strong electrolytes and strong acids; those acids that dissociate only to a small extent are weak electrolytes and weak acids. We've already seen in Table 4.1, for example, that $\mathrm{HCl}, \mathrm{HClO}_{4}, \mathrm{HNO}_{3}$, and $\mathrm{H}_{2} \mathrm{SO}_{4}$ are strong electrolytes and therefore strong acids, whereas $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ and HF are weak electrolytes and therefore weak acids.

Recall from Section 2.9 that different acids have different numbers of acidic hydrogens and yield different numbers of $\mathrm{H}_{3} \mathrm{O}^{+}$ions in solution. Sulfuric acid, for instance, can dissociate twice, and phosphoric acid can dissociate three times. In the case of sulfuric acid, the first dissociation of an $\mathrm{H}^{+}$is complete-all $\mathrm{H}_{2} \mathrm{SO}_{4}$ molecules lose one $\mathrm{H}^{+}$-but the second dissociation is incomplete, as indicated by the double arrow below. In the case of phosphoric acid, none of the three dissociations is complete.
Sulfuric acid:

$$
\begin{aligned}
& \mathrm{H}_{2} \mathrm{SO}_{4}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{HSO}_{4}^{-}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q) \\
& \mathrm{HSO}_{4}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{SO}_{4}^{2-}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q)
\end{aligned}
$$

Phosphoric acid:

$$
\begin{aligned}
& \mathrm{H}_{3} \mathrm{PO}_{4}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q) \\
& \mathrm{H}_{2} \mathrm{PO}_{4}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HPO}_{4}{ }^{-2}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q) \\
& \mathrm{HPO}_{4}{ }^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{PO}_{4}{ }^{3-}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q)
\end{aligned}
$$



Introduction to Aqueous Acids movie; Introduction to Aqueous Bases movie

VAll compounds that contain H are not acids. $\mathrm{NH}_{3}$ is a base and $\mathrm{CH}_{4}$ is neither an acid nor a base. All compounds that contain OH are not bases. $\mathrm{SO}_{2}(\mathrm{OH})_{2}$ (usually written as $\mathrm{H}_{2} \mathrm{SO}_{4}$ ) is an acid.

$\nabla$$\mathrm{H}^{+}(a q)$ and $\mathrm{H}_{3} \mathrm{O}^{+}(a q)$ are both representations of a proton dissolved in water. The actual species present is a complex mixture of hydrates, including $\mathrm{H}_{9} \mathrm{O}_{4}{ }^{+}$.

VAcidity is a function of both the solute and the solvent. HCl is a strong acid in water, a weak acid in glacial acetic acid, and remains undissociated in benzene. Arrhenius theory pertains to aqueous solutions.

quH. van Lubeck, "Significance, Concentration Calculations, Weak and Strong Acids," J. Chem. Educ., Vol. 60, 1983, 189.

vAcids with one, two, and three dissociable protons are called monoprotic, diprotic, and triprotic, respectively.

vAmmonium hydroxide and aqueous ammonia are the same substance:
$\mathrm{NH}_{3}(g)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons$ $\mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q)$. There is no evidence for the undissociated species $\mathrm{NH}_{4} \mathrm{OH}$.


A Why should this bottle be labeled "Aqueous Ammonia" rather than "Ammonium Hydroxide?"


Due to economic considerations NaOH and KOH are the only two common strong bases with group 1A metal ions. The others ( $\mathrm{LiOH}, \mathrm{RbOH}, \mathrm{CsOH}$ ) are equally strong bases.

Bases, like acids, can also be either strong or weak, depending on the extent to which they dissociate and produce $\mathrm{OH}^{-}$ions in aqueous solution. Most metal hydroxides, such as NaOH and $\mathrm{Ba}(\mathrm{OH})_{2}$, are strong electrolytes and strong bases, but ammonia $\left(\mathrm{NH}_{3}\right)$ is a weak electrolyte and a weak base. Ammonia is weakly basic because it reacts to a small extent with water to yield $\mathrm{NH}_{4}^{+}$and $\mathrm{OH}^{-}$ions. In fact, aqueous solutions of ammonia are often called "ammonium hydroxide," although this is really a misnomer since the concentrations of $\mathrm{NH}_{4}^{+}$and $\mathrm{OH}^{-}$ions are low.

$$
\mathrm{NH}_{3}(g)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

As with the dissociation of acetic acid discussed in Section 4.2, the reaction of ammonia with water takes place only to a small extent (about $1 \%$ ). Most of the ammonia remains unreacted, and we therefore write the reaction with a double arrow to show that a dynamic equilibrium exists between forward and reverse reactions.

Table 4.2 summarizes the names, formulas, and classification of some common acids and bases.

| TABLE 4.2 Some Common Acids and Bases |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Strong acid | $\begin{aligned} & \mathrm{HClO}_{4} \\ & \mathrm{H}_{2} \mathrm{SO}_{4} \\ & \mathrm{HBr} \\ & \mathrm{HCl} \\ & \mathrm{HNO}_{3} \end{aligned}$ | Perchloric acid <br> Sulfuric acid <br> Hydrobromic acid Hydrochloric acid Nitric acid | NaOH <br> KOH <br> $\mathrm{Ba}(\mathrm{OH})_{2}$ <br> $\mathrm{Ca}(\mathrm{OH})_{2}$ | Sodium hydroxide Potassium hydroxide Barium hydroxide Calcium hydroxide | Strong base |
| Weak acid | $\begin{aligned} & \mathrm{H}_{3} \mathrm{PO}_{4} \\ & \mathrm{HF} \\ & \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H} \end{aligned}$ | Phosphoric acid Hydrofluoric acid Acetic acid | $\mathrm{NH}_{3}$ | Ammonia | Weak base |

When an acid and a base are mixed in the right stoichiometric proportion, both acidic and basic properties disappear because of a neutralization reaction, which produces water and a salt. The anion of the salt $\left(\mathrm{A}^{-}\right)$comes from the acid, and the cation of the salt $\left(\mathrm{M}^{+}\right)$comes from the base:

## A NEUTRALIZATION REACTION



Because salts are generally strong electrolytes in aqueous solution, we can write the neutralization reaction of a strong acid with a strong base as an ionic equation:

$$
\mathrm{H}^{+}(a q)+\mathrm{A}^{-}(a q)+\mathrm{M}^{+}(a q)+\mathrm{OH}^{-}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{M}^{+}(a q)+\mathrm{A}^{-}(a q)
$$

Canceling the ions that appear on both sides of the ionic equation gives the net ionic equation, which holds for the reaction of any strong acid with any strong base in water:

$$
\begin{aligned}
\mathrm{H}^{+}(a q)+\mathrm{A}^{-}(a q)+\mathrm{M}^{+}(a q)+\mathrm{OH}^{-}(a q) & \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{M}^{+}(a q)+\mathrm{A}^{-}(a q) \\
\mathrm{H}^{+}(a q)+\mathrm{OH}^{-}(a q) & \longrightarrow \mathrm{H}_{2} \mathrm{O}(l) \\
\text { or } \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) & \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

For the reaction of a weak acid with a strong base, a similar neutralization occurs, but we must write the molecular formula of the acid rather than simply $\mathrm{H}^{+}(a q)$, because the dissociation of the acid in water is incomplete. Instead, the acid exists primarily as the neutral molecule. In the reaction of HF with KOH , for example, we write the net ionic equation as

$$
\mathrm{HF}(a q)+\mathrm{OH}^{-}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{F}^{-}(a q)
$$

## Worked Example 4.6

Write both an ionic equation and a net ionic equation for the neutralization reaction of aqueous HBr and aqueous $\mathrm{Ba}(\mathrm{OH})_{2}$.

## Strategy

Hydrogen bromide is a strong acid whose aqueous solution contains $\mathrm{H}^{+}$ions and $\mathrm{Br}^{-}$ ions. Barium hydroxide is a strong base whose aqueous solution contains $\mathrm{Ba}^{2+}$ and $\mathrm{OH}^{-}$ions. Thus, we have a mixture of four different ions on the reactant side. Write the neutralization reaction as an ionic equation, and then cancel spectator ions to give the net ionic equation.

## Solution

## IONIC EQUATION

$$
2 \mathrm{H}^{+}(a q)+2 \mathrm{Br}^{-}(a q)+\mathrm{Ba}^{2+}(a q)+2 \mathrm{OH}^{-}(a q) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{Br}^{-}(a q)+\mathrm{Ba}^{2+}(a q)
$$

## NET IONIC EQUATION

$$
\begin{aligned}
& 2 \mathrm{H}^{+}(a q)+2 \mathrm{OH}^{-}(a q) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l) \\
& \text { or } \mathrm{H}^{+}(a q)+\mathrm{OH}^{-}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

The reaction of HBr with $\mathrm{Ba}(\mathrm{OH})_{2}$ involves the combination of a proton $\left(\mathrm{H}^{+}\right)$from the acid with $\mathrm{OH}^{-}$from the base to yield water and a salt $\left(\mathrm{BaBr}_{2}\right)$.

- PROBLEM 4.9 Write a balanced ionic equation and net ionic equation for each of the following acid-base reactions:
(a) $2 \mathrm{CsOH}(a q)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \rightarrow$
(b) $\mathrm{Ca}(\mathrm{OH})_{2}(a q)+2 \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q) \rightarrow$
- KEY CONCEPT PROBLEM 4.10 The following pictures represent aqueous solutions of three acids HA ( $\mathrm{A}=\mathrm{X}, \mathrm{Y}$, or Z ), with water molecules omitted for clarity. Which of the three is the strongest acid, and which is the weakest?



## 4.6 | Oxidation-Reduction (Redox) Reactions

Magnesium metal burns in air with an intense white light to form solid magnesium oxide. Red phosphorus reacts with liquid bromine to form liquid phosphorus tribromide. Purple aqueous permanganate ion, $\mathrm{MnO}_{4}^{-}$, reacts with aqueous $\mathrm{Fe}^{2+}$ ion to yield $\mathrm{Fe}^{3+}$ and pale pink $\mathrm{Mn}^{2+}$. Although these and many thousands of other reactions appear unrelated, all are oxidation-reduction reactions.


$$
\begin{aligned}
2 \mathrm{Mg}(s)+\mathrm{O}_{2}(g) & \longrightarrow 2 \mathrm{MgO}(s) \\
2 \mathrm{P}(s)+3 \mathrm{Br}_{2}(l) & \longrightarrow 2 \mathrm{PBr}_{3}(l) \\
\mathrm{MnO}_{4}^{-}(a q)+5 \mathrm{Fe}^{2+}(a q)+8 \mathrm{H}^{+}(a q) & \longrightarrow \mathrm{Mn}^{2+}(a q)+5 \mathrm{Fe}^{3+}(a q)+4 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$


© Magnesium metal burns in air to give MgO .


A Elemental phosphorus reacts spectacularly with bromine to give $\mathrm{PBr}_{3}$.

© Aqueous potassium permanganate is frequently used as an oxidizing agent, as described in the text.

.C. E. Ophardt, "Redox Demonstrations and Descriptive Chemistry: Part I. Metals," J. Chem. Educ., Vol. 64, 1987, 716. Redox reactions of iron(III) with thiosulfate, iron(II) with permanganate, and tin(II) with mercury(I) are used to show how an abbreviated table of standard reduction potentials is used to predict the products of these reactions from the relative positions of the oxidizing agents and reducing agents in the table.

Historically, the word oxidation referred to the combination of an element with oxygen to yield an oxide, and the word reduction referred to the removal of oxygen from an oxide to yield the element. Such oxidation-reduction processes have been crucial to the development of human civilization and still have enormous commercial value. The oxidation (rusting) of iron metal by reaction with moist air has been known for millennia and is still a serious problem that causes enormous damage to buildings, bridges, and automobiles. The reduction of iron ore $\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)$ with charcoal $(\mathrm{C})$ to make iron metal has been carried out since prehistoric times and is still used today in the initial stages of steelmaking.

| $4 \mathrm{Fe}(s)+3 \mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{Fe}_{2} \mathrm{O}_{3}(s)$ | Rusting of iron: an oxidation of Fe |
| :--- | :--- |
| $2 \mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{C}(s) \longrightarrow 4 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(g)$ | Manufacture of iron: a reduction of Fe |

vTwo commonly used redox reaction memorization aids are: 1) LEO the lion goes GER (Lose Electrons Oxidation, Gain Electrons Reduction); and OIL RIG (Oxidation Involves Loss of electrons, Reduction Involves Gain of electrons).

Gion Calzaferri, "Oxidation Numbers," J. Chem. Educ., Vol. 76, 1999, 362-363.

0Oxidation numbers of atoms in a compound are the charges the atoms would have if the compound were ionic.

Today, the words oxidation and reduction have taken on a much broader meaning. An oxidation is now defined as the loss of one or more electrons by a substance-element, compound, or ion-and a reduction is the gain of one or more electrons by a substance. Thus, an oxidation-reduction reaction, or redox reaction, is a process in which electrons are transferred from one substance to another.


How can you tell when a redox reaction is taking place? The answer is that we assign to each atom in a substance a value called an oxidation number (or oxidation state), which indicates whether the atom is neutral, electron-rich, or electron-poor. By comparing the oxidation number of an atom before and after reaction, we can tell whether the atom has gained or lost electrons. Note that oxidation numbers don't necessarily imply ionic charges. They are simply a convenient device to help keep track of electrons in redox reactions.

The rules for assigning oxidation numbers are as follows:

1. An atom in its elemental state has an oxidation number of 0 . For example:

2. An atom in a monatomic ion has an oxidation number identical to its charge. (Review Section 2.10 to see the charges on some common ions.) For example:





3. An atom in a polyatomic ion or in a molecular compound usually has the same oxidation number it would have if it were a monatomic ion. In the hydroxide ion $\left(\mathrm{OH}^{-}\right)$, for example, the oxygen atom has an oxidation number of -2 , as if it were a monatomic $\mathrm{O}^{2-}$ ion, and the hydrogen atom has an oxidation number of +1 , as if it were $\mathrm{H}^{+}$.




In general, the farther left an element is in the periodic table, the more likely it is that the atom will be "cationlike." Metals, therefore, usually have positive oxidation numbers. The farther right an element is in the periodic table, the more likely it is that the atom will be "anionlike." Nonmetals, such as O, N, and the halogens, usually have negative oxidation numbers. We'll see the reasons for this trend in Sections 6.3-6.5.

a. Hydrogen can be either +1 or $\mathbf{- 1}$. When bonded to a metal, such as Na or Ca , hydrogen has an oxidation number of -1 . When bonded to a nonmetal, such as $\mathrm{C}, \mathrm{N}, \mathrm{O}$, or Cl , hydrogen has an oxidation number of +1 .

b. Oxygen usually has an oxidation number of $\mathbf{- 2}$. The major exception is in compounds called peroxides, which contain either the $\mathrm{O}_{2}{ }^{2-}$ ion or an $\mathrm{O}-\mathrm{O}$ covalent bond in a molecule. Each oxygen atom in a peroxide has an oxidation number of -1 .




Oxidation Numbers activity

Oxygen has an oxidation number of -2 except when it is bonded to itself or to fluorine. The oxidation number of oxygen is 0 in $\mathrm{O}_{2},-1 / 2$ on $\mathrm{O}_{2}^{-}$(superoxide), and -1 in $\mathrm{O}_{2}{ }^{2-}$ (peroxide).

©
A useful rule of thumb: For any main group element, maximum oxidation number $=$ group number; minimum oxidation number = group number -8 .

Lee R. Summerlin and James L. Ealy, Jr., "Oxidation States of Manganese: $\mathrm{Mn}^{7+}, \mathrm{Mn}^{6+}, \mathrm{Mn}^{4+}$, and $\mathrm{Mn}^{2+}$, , Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), pp. 133-134.
c. Halogens usually have an oxidation number of $\mathbf{- 1}$. The major exception is in compounds of chlorine, bromine, or iodine in which the halogen atom is bonded to oxygen. In such cases, the oxygen has an oxidation number of -2 , and the halogen has a positive oxidation number. $\operatorname{In} \mathrm{Cl}_{2} \mathrm{O}$, for example, the O atom has an oxidation number of -2 and each Cl atom has an oxidation number of +1 .


4. The sum of the oxidation numbers is 0 for a neutral compound and is equal to the net charge for a polyatomic ion. This rule is particularly useful for finding the oxidation number of an atom in difficult cases. The general idea is to assign oxidation numbers to the "easy" atoms first and then find the oxidation number of the "difficult" atom by subtraction. For example, suppose we need to know the oxidation number of the sulfur atom in sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$. Since each H atom is +1 and each O atom is -2 , the S atom must have an oxidation number of +6 for the compound to have no net charge:


$$
\begin{aligned}
& 2(+1)+(?)+4(-2)=0 \text { net charge } \\
& ?=0-2(+1)-4(-2)=+6
\end{aligned}
$$

To find the oxidation number of the chlorine atom in the perchlorate anion $\left(\mathrm{ClO}_{4}^{-}\right)$, we know that each oxygen is -2 , so the Cl atom must have an oxidation number of +7 for there to be a net charge of -1 :


$$
?+4(-2)=-1 \text { net charge }
$$

$$
?=-1-4(-2)=+7
$$

To find the oxidation number of the nitrogen atom in the ammonium cation $\left(\mathrm{NH}_{4}{ }^{+}\right)$, we know that each H atom is +1 , so the N atom must have an oxidation number of -3 for there to be a net charge of +1 :


$$
\begin{aligned}
& ?+4(+1)=+1 \text { net charge } \\
& ?=+1-4(+1)=-3
\end{aligned}
$$

## Worked Example 4.7

Assign oxidation numbers to each atom in the following substances:
(a) CdS
(b) $\mathrm{AlH}_{3}$
(c) $\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}$
(d) $\mathrm{Na}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$

## Strategy

(a) The sulfur atom in $\mathrm{S}^{2-}$ has an oxidation number of -2 , so Cd must be +2 .
(b) H bonded to a metal has the oxidation number -1 , so Al must be +3 .
(c) O usually has the oxidation number -2 , so $S$ must be +2 for the anion to have a net charge of -2 : for $\left(2 \mathrm{~S}^{+2}\right)\left(3 \mathrm{O}^{-2}\right), 2(+2)+3(-2)=-2$ net charge.
(d) Na is always +1 , and oxygen is -2 , so Cr must be +6 for the compound to be neutral: for $\left(2 \mathrm{Na}^{+}\right)\left(2 \mathrm{Cr}^{+6}\right)\left(7 \mathrm{O}^{-2}\right), 2(+1)+2(+6)+7(-2)=0$ net charge.

## Solution

(a) CdS $\uparrow \uparrow$
(b) $\mathrm{AlH}_{3}$
$\uparrow \uparrow$
(c) $\underset{\uparrow}{\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}-1}$
(d) $\underset{\uparrow}{\mathrm{Na}} \mathrm{N}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$
$+2-2$
$+3-1$
$+2-2$
$+1+6 \quad-2$

- PROBLEM 4.11 Assign an oxidation number to each atom in the following compounds:
(a) $\mathrm{SnCl}_{4}$
(b) $\mathrm{CrO}_{3}$
(c) $\mathrm{VOCl}_{3}$
(d) $\mathrm{V}_{2} \mathrm{O}_{3}$
(e) $\mathrm{HNO}_{3}$
(f) $\mathrm{FeSO}_{4}$


## 4.7 | Identifying Redox Reactions

Once oxidation numbers are assigned, it's clear why the reactions mentioned in the previous section are all redox processes. Take the rusting of iron, for example. Two of the reactants, Fe and $\mathrm{O}_{2}$, are elements, and both therefore have an oxidation number of 0 . In the product, however, the oxygen atoms have an oxidation number of -2 , and the iron atoms have an oxidation number of +3 . Thus, Fe has undergone a change from 0 to +3 (a loss of electrons, or oxidation), and O has undergone a change from 0 to -2 (a gain of electrons, or reduction). Note that the total number of electrons given up by the atoms being oxidized $(4 \mathrm{Fe} \times$ 3 electrons $/ \mathrm{Fe}=12$ electrons) is the same as the number gained by the atoms being reduced ( $6 \mathrm{O} \times 2$ electrons $/ \mathrm{O}=12$ electrons).


A similar analysis can be carried out for the production of iron metal from its ore. The iron atom is reduced because it goes from an oxidation number of +3 in the reactant $\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)$ to 0 in the product $(\mathrm{Fe})$. At the same time, the carbon atom is oxidized because it goes from an oxidation number of 0 in the reactant $(\mathrm{C})$ to +4 in the product $\left(\mathrm{CO}_{2}\right)$. The oxygen atoms undergo no change because they have an oxidation number of -2 in both reactant and product. The total number of electrons given up by the atoms being oxidized ( $3 \mathrm{C} \times 4$ electrons $/ \mathrm{C}=12$ electrons) is the same as the number gained by the atoms being reduced ( $4 \mathrm{Fe} \times 3$ electrons $/ \mathrm{Fe}=12$ electrons).


As these examples show, oxidations and reductions always occur together. Whenever one atom loses one or more electrons (is oxidized), another atom must gain those electrons (be reduced). The substance that causes a reduction by giving up electrons-the iron atom in the reaction of Fe with $\mathrm{O}_{2}$ and the carbon atom in the reaction of C with $\mathrm{Fe}_{2} \mathrm{O}_{3}$-is called a reducing agent. The substance that causes an oxidation by accepting electrons-the oxygen atom in the reaction of Fe with $\mathrm{O}_{2}$ and the iron atom in the reaction of C with $\mathrm{Fe}_{2} \mathrm{O}_{3}$-is called an oxidizing agent. The reducing agent is itself oxidized when it gives up electrons, and the oxidizing agent is itself reduced when it accepts electrons.

[^6]

- The iron used for this prehistoric ax was made by the reduction of iron ore with charcoal.

and Zinc movie

We'll see in later chapters that redox reactions are common for almost every element in the periodic table except for the noble gas elements of group 8A. In general, metals act as reducing agents, and reactive nonmetals such as $\mathrm{O}_{2}$ and the halogens act as oxidizing agents.


Different metals can give up different numbers of electrons in redox reactions. Lithium, sodium, and the other group 1A elements give up only one electron and become monopositive ions with oxidation numbers of +1 . Beryllium, magnesium, and the other group 2A elements, however, typically give up two electrons and become dipositive ions. The transition metals in the middle of the periodic table can give up a variable number of electrons to yield more than one kind of ion depending on the exact reaction. Titanium, for example, can react with chlorine to yield either $\mathrm{TiCl}_{3}$ or $\mathrm{TiCl}_{4}$. Because a chloride ion has a -1 oxidation number, the titanium atom in $\mathrm{TiCl}_{3}$ must have a +3 oxidation number and the titanium atom in $\mathrm{TiCl}_{4}$ must be +4 .

## Worked Example 4.8

Assign oxidation numbers to all atoms, tell in each case which substance is undergoing oxidation and which reduction, and identify the oxidizing and reducing agents.
(a) $\mathrm{Ca}(s)+2 \mathrm{H}^{+}(a q) \rightarrow \mathrm{Ca}^{2+}(a q)+\mathrm{H}_{2}(g)$
(b) $2 \mathrm{Fe}^{2+}(a q)+\mathrm{Cl}_{2}(a q) \rightarrow 2 \mathrm{Fe}^{3+}(a q)+2 \mathrm{Cl}^{-}(a q)$

## Strategy and Solution

(a) The neutral elements Ca and $\mathrm{H}_{2}$ have oxidation numbers of $0 ; \mathrm{Ca}^{2+}$ is +2 and $\mathrm{H}^{+}$ is +1 :


Ca is oxidized because its oxidation number increases from 0 to +2 , and $\mathrm{H}^{+}$is reduced because its oxidation number decreases from +1 to 0 . The reducing agent is the substance that gives away electrons, thereby going to a higher oxidation number, and the oxidizing agent is the substance that accepts electrons, thereby going to a lower oxidation number. In the present case, calcium is the reducing agent, and $\mathrm{H}^{+}$is the oxidizing agent.
(b) Atoms of the neutral element $\mathrm{Cl}_{2}$ have an oxidation number of 0 ; the monatomic ions have oxidation numbers equal to their charge:

$$
\underset{\uparrow}{2 \mathrm{Fe}^{2+}(a q)}+\underset{\substack{\uparrow_{2} \\ \mathrm{Cl}_{2} \\+2}}{0} \underset{\uparrow}{2 \mathrm{Fe}^{3+}}(a q)+\underset{\uparrow}{2 \mathrm{Cl}^{-}(a q)}
$$

$\mathrm{Fe}^{2+}$ is oxidized (its oxidation number increases from +2 to +3 ); $\mathrm{Cl}_{2}$ is reduced (its oxidation number decreases from 0 to -1$). \mathrm{Fe}^{2+}$ is the reducing agent, and $\mathrm{Cl}_{2}$ is the oxidizing agent.

PROBLEM 4.12 Aqueous copper(II) ion reacts with aqueous iodide ion to yield solid copper(I) iodide and aqueous iodine. Write the balanced net ionic equation, assign oxidation numbers to all species present, and identify the oxidizing and reducing agents.

- PROBLEM 4.13 Tell in each of the following reactions which substance is undergoing an oxidation and which a reduction, and identify the oxidizing and reducing agents.
(a) $\mathrm{SnO}_{2}(s)+2 \mathrm{C}(s) \rightarrow \mathrm{Sn}(s)+2 \mathrm{CO}(g)$
(b) $\mathrm{Sn}^{2+}(a q)+2 \mathrm{Fe}^{3+}(a q) \rightarrow \mathrm{Sn}^{4+}(a q)+2 \mathrm{Fe}^{2+}(a q)$
(c) $4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \rightarrow 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(l)$


### 4.8 The Activity Series of the Elements

The reaction of an aqueous cation, usually a metal ion, with a free element is among the simplest of all redox processes. The products are a different ion and a different element. Iron metal reacts with aqueous copper(II) ion, for example, to give iron(II) ion and copper metal (Figure 4.2):

$$
\mathrm{Fe}(s)+\mathrm{Cu}^{2+}(a q) \longrightarrow \mathrm{Fe}^{2+}(a q)+\mathrm{Cu}(s)
$$



A FIGURE 4.2 The iron nail reduces the $\mathrm{Cu}^{2+}$ ions and becomes coated with metallic Cu . At the same time, the intensity of the blue color diminishes due to loss of $\mathrm{Cu}^{2+}$ ions from solution.

Similarly, magnesium metal reacts with aqueous acid to yield magnesium ion and hydrogen gas:

$$
\mathrm{Mg}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Mg}^{2+}(a q)+\mathrm{H}_{2}(g)
$$

Bassam Z. Shakhashiri, "Reactions of Metals and Hydrochloric Acid," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983) pp. 25-26. Reactions of iron, zinc, and magnesium with hydrochloric acid produce aqueous solutions of the +2 -metal ions and hydrogen gas.


A Magnesium metal reacts with aqueous acid to give bubbles of hydrogen gas and $\mathrm{Mg}^{2+}$ ion.

The activity series can be roughly divided into three groups based on periodic table location: 1) active metals from Groups 1A, 2A, and Al; 2) lighter transition metals ( $\mathrm{Cr}, \mathrm{Mn}, \mathrm{Fe}, \mathrm{Co}$, $\mathrm{Ni}, \mathrm{Zn}), \mathrm{Sn}$ and $\mathrm{Pb} ; 3) \mathrm{Cu}$ and heavier transition metals (Ag, Pt, $\mathrm{Au}, \mathrm{Hg})$.

A memorization aid: the elements below hydrogen in the periodic table form an upside-down T on the periodic table:

$$
\begin{gathered}
\mathrm{Cu} \\
\mathrm{Ag} \\
\mathrm{Pt} \mathrm{AuHg}
\end{gathered}
$$

Lee R. Summerlin and James L. Ealy, Jr., "Activity Series for Some Metals," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), p. 150. An overhead projector demonstration showing hydrogen gas generated by a redox reaction.

Whether a reaction occurs between a given ion and a given element depends on the relative ease with which the various species gain or lose electrons-that is, on how easily each species is reduced or oxidized. By noting the results from a succession of different reactions, it's possible to organize an activity series, which ranks the elements in order of their reducing ability in aqueous solution (Table 4.3).

TABLE 4.3 A Partial Activity Series of the Elements

## Oxidation Reaction



Those elements at the top of Table 4.3 give up electrons readily and are stronger reducing agents, whereas those elements at the bottom give up electrons less readily and are weaker reducing agents. As a result, any element higher in the activity series will reduce the ion of any element lower in the activity series. Because copper is above silver, for example, copper metal can give electrons to $\mathrm{Ag}^{+}$ions:

$$
\mathrm{Cu}(s)+2 \mathrm{Ag}^{+}(a q) \longrightarrow \mathrm{Cu}^{2+}(a q)+2 \mathrm{Ag}(s)
$$

Conversely, because gold is below silver in the activity series, gold metal does not give electrons to $\mathrm{Ag}^{+}$ions:

$$
\mathrm{Au}(s)+3 \mathrm{Ag}^{+}(a q) \nrightarrow \mathrm{Au}^{3+}(a q)+3 \mathrm{Ag}(s) \quad \text { Does not occur }
$$

The position of hydrogen in the activity series is particularly important because it indicates which metals react with aqueous acid $\left(\mathrm{H}^{+}\right)$to release $\mathrm{H}_{2}$ gas. The metals at the top of the series-the alkali metals of group 1A and alkaline earth metals of group 2A—are such powerful reducing agents that they react even with pure water, in which the concentration of $\mathrm{H}^{+}$is very low:



By contrast, the metals in the middle of the series react with aqueous acid but not with water, and the metals at the bottom of the series react with neither aqueous acid nor water:

$$
\begin{aligned}
\mathrm{Fe}(s)+2 \mathrm{H}^{+}(a q) & \longrightarrow \mathrm{Fe}^{2+}(a q)+\mathrm{H}_{2}(g) \\
\mathrm{Cu}(s)+\mathrm{H}^{+}(a q) & \longrightarrow \text { No reaction }
\end{aligned}
$$

Notice that the most reactive metals (the top of the activity series) are on the left of the periodic table, whereas the least reactive metals (the bottom of the activity series) are in the transition metal groups closer to the right side of the table. We'll see the reasons for this behavior in Chapter 6.


## Worked Example 4.9

Predict whether the following reactions will occur:
(a) $\mathrm{Hg}^{2+}(a q)+\mathrm{Zn}(s) \rightarrow \mathrm{Hg}(l)+\mathrm{Zn}^{2+}(a q)$
(b) $2 \mathrm{H}^{+}(a q)+2 \mathrm{Ag}(s) \rightarrow \mathrm{H}_{2}(g)+2 \mathrm{Ag}^{+}(a q)$
(a) The copper wire reduces aqueous $\mathrm{Ag}^{+}$ion and (b) becomes coated with metallic silver. Note the blue color due to $\mathrm{Cu}^{2+}$ ions in the solution.

Bassam Z. Shakhashiri, "An Activity Series: Zinc, Copper, and Silver Half Cells," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 4 (The University of Wisconsin Press, Madison, 1992) pp. 101-106.


A Iron reacts only slowly with aqueous acid at room temperature.


Formation of Silver Crystals movie

Precipitation, Redox and Neutralization Reactions activity

Marten J. ten Hoor, "Redox Balancing Without Puzzling," J. Chem. Educ., Vol. 74, 1997, 1368-1376.

Addition of aqueous $\mathrm{Br}^{-}$to a solution of $\mathrm{MnO}_{4}^{-}$causes a reduction of the permanganate ion, discharging the intense purple color.

## Strategy

Look at Table 4.3 to find the relative reactivities of the elements.

## Solution

(a) Zinc is above mercury in the activity series, so this reaction will occur.
(b) Silver is below hydrogen in the activity series, so this reaction will not occur.

- PROBLEM 4.14 Predict whether the following reactions will occur:
(a) $2 \mathrm{H}^{+}(a q)+\mathrm{Pt}(s) \rightarrow \mathrm{H}_{2}(g)+\mathrm{Pt}^{2+}(a q)$
(b) $\mathrm{Ca}^{2+}(a q)+\mathrm{Mg}(s) \rightarrow \mathrm{Ca}(s)+\mathrm{Mg}^{2+}(a q)$

PROBLEM 4.15 Element B will reduce the cation of element $\mathrm{A}\left(\mathrm{A}^{+}\right)$, but will not reduce the cation of element $C\left(C^{+}\right)$. Will element $C$ reduce the cation of element $A$ ? Explain.

### 4.9 Balancing Redox Reactions: The Oxidation-Number Method

Simple redox reactions can be balanced by the trial-and-error method described in Section 3.1, but other reactions are so complex that a more systematic approach is needed. There are two such systematic approaches often used for balancing redox reactions: the oxidation-number method and the half-reaction method. Different people prefer different methods, so we'll discuss both. The oxidation-number method is useful because it makes you focus on the chemical changes involved; the halfreaction method (discussed in the next section) is useful because it makes you focus on the transfer of electrons, a subject of particular interest when discussing batteries and other aspects of electrochemistry (Chapter 18).

The key to the oxidation-number method of balancing redox equations is to realize that the net change in the total of all oxidation numbers must be zero. That is, any increase in oxidation number for the oxidized atoms must be matched by a corresponding decrease in oxidation number for the reduced atoms. Take the reaction of potassium permanganate $\left(\mathrm{KMnO}_{4}\right)$ with sodium bromide in aqueous acid, for example. An aqueous acidic solution of the purple permanganate anion $\left(\mathrm{MnO}_{4}^{-}\right)$is reduced by $\mathrm{Br}^{-}$to yield the nearly colorless $\mathrm{Mn}^{2+}$ ion, while $\mathrm{Br}^{-}$is oxidized to $\mathrm{Br}_{2}$. The unbalanced net ionic equation for the process is

$$
\mathrm{MnO}_{4}^{-}(a q)+\mathrm{Br}^{-}(a q) \longrightarrow \mathrm{Mn}^{2+}(a q)+\mathrm{Br}_{2}(a q) \quad \text { Unbalanced }
$$



The first step is to balance the equation for all atoms other than O and H . In the present instance, a coefficient of 2 is needed for $\mathrm{Br}^{-}$on the left:


Next, assign oxidation numbers to all atoms, including O and H if present, in both reactants and products:


Now, decide which of the atoms have changed their oxidation number and have thus been either oxidized or reduced. In the present instance, manganese has been reduced from +7 to +2 (gaining five electrons), and bromine has been oxidized from -1 to 0 (losing one electron).


The next step is to find the net increase in oxidation number for the oxidized atoms and the net decrease in oxidation number for the reduced atoms. Then, multiply the net increase and the net decrease by suitable factors so that the two become equal. In the present instance, the net increase in oxidation number is 2 (as two $\mathrm{Br}^{-}$ions go from -1 to 0 ), and the net decrease in oxidation number is 5 (as Mn goes from +7 to +2 ). Multiplying the net increase by 5 and the net decrease by 2 will make them equal at 10 . Thus, we must multiply the coefficients of the manganese species by 2 and the coefficients of the Br species by 5 .


Finally, because the reaction is occurring in acidic solution, we balance the equation for oxygen by adding $\mathrm{H}_{2} \mathrm{O}$ to the side with less O and then balance for hydrogen by adding $\mathrm{H}^{+}$to the side with less H . In this example, $8 \mathrm{H}_{2} \mathrm{O}$ must be added to the right side to balance for O , and $16 \mathrm{H}^{+}$must then be added to the left side to balance for $H$. If everything has been done correctly, the final net ionic equation will result. The answer can be checked by noting that the equation is balanced both for atoms and for charge, with +4 on both sides.


FIGURE 4.3 The procedure for balancing redox equations by the oxidation-number method.

To summarize, balancing a redox reaction in acidic solution by the oxidationnumber method is a six-step process, followed by a check of the answer (Figure 4.3.)


Worked Example 4.10 shows how the oxidation-number method is used to balance a reaction carried out in basic solution. The procedure is exactly the same as that used for balancing a reaction in acidic solution, but $\mathrm{OH}^{-}$ions are added as the final step to neutralize any $\mathrm{H}^{+}$ions that appear in the equation. This simply reflects the fact that basic solutions contain negligibly small amounts of $\mathrm{H}^{+}$but large amounts of $\mathrm{OH}^{-}$.

## Worked Example 4.10

A purple solution of aqueous potassium permanganate $\left(\mathrm{KMnO}_{4}\right)$ reacts with aqueous sodium sulfite $\left(\mathrm{Na}_{2} \mathrm{SO}_{3}\right)$ in basic solution to yield the green manganate ion $\left(\mathrm{MnO}_{4}{ }^{2-}\right)$ and sulfate ion $\left(\mathrm{SO}_{4}{ }^{2-}\right)$. The unbalanced net ionic equation is

$$
\mathrm{MnO}_{4}^{-}(a q)+\mathrm{SO}_{3}{ }^{2-}(a q) \longrightarrow \mathrm{MnO}_{4}{ }^{2-}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q) \quad \text { Unbalanced }
$$

## Reduction of the purple

 $\mathrm{MnO}_{4}^{-}$ion with $\mathrm{SO}_{3}^{2-}$ in basic solution yields the deep green $\mathrm{MnO}_{4}{ }^{2-}$ ion.

Balance the equation by the oxidation-number method.

## Strategy

Follow the series of steps outlined in Figure 4.3.

## Solution

Steps 1 and 2. The initial equation is already balanced for atoms other than O and H .
Step 3. Assign oxidation numbers to all atoms:


Step 4. Decide which atoms have changed oxidation number and by how much. Manganese has been reduced from +7 to +6 (gaining one electron), and sulfur has been oxidized from +4 to +6 (losing two electrons):


Step 5. Find the total net increase in oxidation number for the oxidized atoms and the total net decrease in oxidation number for the reduced atoms:

Increase in oxidation number: $S(+4) \longrightarrow S(+6) \quad$ Net increase $=+2$
Decrease in oxidation number: $\mathrm{Mn}(+7) \longrightarrow \mathrm{Mn}(+6) \quad$ Net decrease $=-1$
Now, choose coefficients that make the net increase equal to the net decrease. In this case, the net decrease must be multiplied by 2 , so a coefficient of 2 is needed for both Mn species:


Step 6. Balance the equation for O by adding $1 \mathrm{H}_{2} \mathrm{O}$ on the left, and then balance for H by adding $2 \mathrm{H}^{+}$on the right.


At this point, the equation is fully balanced. Even so, it's not correct because it assumes an acidic solution (the $2 \mathrm{H}^{+}$on the right), while we were told that the reaction occurs in basic solution. We can correct the situation by adding $2 \mathrm{OH}^{-}$ions to each side of the equation. The $2 \mathrm{OH}^{-}$on the right will "neutralize" the $2 \mathrm{H}^{+}$ions, giving $2 \mathrm{H}_{2} \mathrm{O}$ :


Finally, we can cancel one $\mathrm{H}_{2} \mathrm{O}$ molecule that occurs on both sides of the equation, giving the final balanced net ionic equation that is balanced both for atoms and for charge:

```
\(2 \mathrm{MnO}_{4}{ }^{-}(a q)+\mathrm{SO}_{3}{ }^{2-}(a q)+2 \mathrm{OH}^{-}(a q) \longrightarrow 2 \mathrm{MnO}_{4}{ }^{2-}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)\)
    Charge: \((2 \times-1)+(-2)+(2 \times-1)=-6 \quad\) Charge: \((2 \times-2)+(-2)=-6\)
```



- The orange dichromate ion is reduced by addition of $\mathrm{Cl}^{-}$ to give the green $\mathrm{Cr}^{3+}$ ion.


Stepwise Balancing of Redox Equations-Acidic activity

PROBLEM 4.16 Balance the following net ionic equation by the oxidationnumber method. The reaction takes place in acidic solution.

$$
\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+\mathrm{I}^{-}(a q) \longrightarrow \mathrm{Cr}^{3+}(a q)+\mathrm{IO}_{3}^{-}(a q)
$$

- PROBLEM 4.17 Balance the following net ionic equation by the oxidationnumber method. The reaction takes place in basic solution.

$$
\mathrm{MnO}_{4}^{-}(a q)+\mathrm{Br}^{-}(a q) \longrightarrow \mathrm{MnO}_{2}(s)+\mathrm{BrO}_{3}^{-}(a q)
$$

### 4.10 Balancing Redox Reactions: The Half-Reaction Method

An alternative to the oxidation-number method for balancing redox reactions is the half-reaction method. The key to this method is to realize that the overall reaction can be broken into two parts, or half-reactions. One half-reaction describes the oxidation part of the process, and the other half-reaction describes the reduction part. Each half is balanced separately, and the two halves are then added to obtain the final equation. Let's look at the reaction of aqueous potassium dichromate $\left(\mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}\right)$ with aqueous NaCl to see how the method works. The reaction occurs in acidic solution according to the unbalanced net ionic equation

$$
\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+\mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{Cr}^{3+}(a q)+\mathrm{Cl}_{2}(a q) \quad \text { Unbalanced }
$$

The first step is to decide which atoms have been oxidized and which have been reduced. In the present case, the chloride ion is oxidized (from -1 to 0 ), and the chromium atom is reduced (from +6 to +3 ). Thus, we can write two unbalanced half-reactions that show the separate steps:

$$
\begin{array}{ll}
\text { Oxidation half-reaction: } & \mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{Cl}_{2}(a q) \\
\text { Reduction half-reaction: } & \mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q) \longrightarrow \mathrm{Cr}^{3+}{ }_{(a q)}
\end{array}
$$

With the two half-reactions identified, each is balanced separately. Begin by balancing for all atoms other than H and O . The oxidation half-reaction needs a coefficient of 2 before the $\mathrm{Cl}^{-}$, and the reduction half-reaction needs a coefficient of 2 before the $\mathrm{Cr}^{3+}$.


Next, balance both half-reactions for oxygen by adding $\mathrm{H}_{2} \mathrm{O}$ to the side with less O , and balance for hydrogen by adding $\mathrm{H}^{+}$to the side with less H . The oxidation half-reaction has no H or O , but the reduction reaction needs $7 \mathrm{H}_{2} \mathrm{O}$ on the product side to balance for O and $14 \mathrm{H}^{+}$on the reactant side to balance for H :

Oxidation: $2 \mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{Cl}_{2}(a q)$


Now, balance both half-reactions for charge by adding electrons ( $\mathrm{e}^{-}$) to the side with the greater positive charge. The oxidation half-reaction must have $2 \mathrm{e}^{-}$ added to the product side, and the reduction half-reaction must have $6 \mathrm{e}^{-}$added to the reactant side:


$$
\text { Reduction: } \quad \mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \xrightarrow{\text { Add these electrons to }} \text { balance for charge. }
$$

With both half-reactions now balanced, we need to multiply by suitable coefficients so that the number of electrons released in the oxidation half-reaction is the same as the number consumed in the reduction half-reaction. Since the reduction half-reaction has $6 \mathrm{e}^{-}$but the oxidation half-reaction has only $2 \mathrm{e}^{-}$, the entire oxidation half-reaction must be multiplied by 3 :
Multiply by this coefficient to
equalize the numbers of electrons
in the two half-reactions.
Oxidation: $\quad 3 \times\left[2 \mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{Cl}_{2}(a q)+2 \mathrm{e}^{-}\right]$

$$
\text { or } \quad 6 \mathrm{Cl}^{-}(a q) \longrightarrow 3 \mathrm{Cl}_{2}(a q)+6 \mathrm{e}^{-}
$$

Reduction: $\quad \mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l)$

Adding the two half-reactions together and canceling the species that occur on both sides (only the electrons in this example) then gives the final balanced equation. Check the answer to make sure it is balanced both for atoms and for charge.

$$
\begin{aligned}
& 6 \mathrm{Cl}^{-}(a q) \longrightarrow 3 \mathrm{Cl}_{2}(a q)+6 \mathrm{e}^{-} \\
& \mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l) \\
& \hline \mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{Cl}^{-}(a q) \longrightarrow 3 \mathrm{Cl}_{2}(a q)+2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l) \\
& \text { Charge: }(-2)+(+14)+(6 \times-1)=+6 \text { Charge: }(2 \times+3)=+6
\end{aligned}
$$

To summarize, balancing a redox reaction in acidic solution by the half-reaction method is a six-step process, followed by a check of the answer (Figure 4.4.)

Worked Example 4.12 shows how to use the method for balancing a reaction
that takes place in basic solution. As in the oxidation-number method, we first balance the reaction for an acidic solution and then add $\mathrm{OH}^{-}$ions in a final step to neutralize $\mathrm{H}^{+}$.

$\square$The most common error that students make when balancing redox reactions by the half-reaction method is to miscount charges, which results in an incorrect number of electrons used to balance the half-reaction.

VBalancing a redox equation by the half-reaction method will reveal that a half-reaction is an oxidation when electrons appear on the right and a reduction when electrons appear on the left of the arrow.

$\nabla$The number of electrons used to balance the half-reaction should agree with the change in oxidation number of the element undergoing oxidation or reduction.

FIGURE 4.4 The procedure for balancing redo aquations by the half-reaction method.

Step 1. Write the unbalanced net ionic equation.


Step 2. Decide which atoms are oxidized and which are reduced, and write the two unbalanced half-reactions.


Step 3. Balance both half-reactions for all atoms except O and H .


Step 4. Balance each half-reaction for O by adding water to the side with less O , and balance for H by adding $\mathrm{H}^{+}$to the side with less H .

## $\downarrow$

Step 5. Balance each half-reaction for charge by adding electrons to the side with greater positive charge, and then multiply by suitable factors to make the electron count the same in both half-reactions.


Step 6. Add the two balanced half-reactions together, and cancel electrons and other species that appear on both sides of the equation.

Check your answer by making sure the equation is balanced both for atoms and for charge.

## Worked Example 4.11

Write unbalanced half-reactions for the following net ionic equations:
(a) $\mathrm{Mn}^{2+}(a q)+\mathrm{ClO}_{3}^{-}(a q) \longrightarrow \mathrm{MnO}_{2}(s)+\mathrm{ClO}_{2}(a q)$
(b) $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+\mathrm{Fe}^{2+}(a q) \longrightarrow \mathrm{Cr}^{3+}(a q)+\mathrm{Fe}^{3+}(a q)$

## Strategy

Look at each equation to see which atoms are being oxidized (increasing in oxidation number) and which are being reduced (decreasing in oxidation number).

## Solution

(a) Oxidation: $\mathrm{Mn}^{2+}(a q) \rightarrow \mathrm{MnO}_{2}(s) \quad \mathrm{Mn}$ goes from +2 to +4

Reduction: $\mathrm{ClO}_{3}{ }^{-}(a q) \rightarrow \mathrm{ClO}_{2}(a q) \quad \mathrm{Cl}$ goes from +5 to +4
(b) Oxidation: $\mathrm{Fe}^{2+}(a q) \rightarrow \mathrm{Fe}^{3+}(a q) \quad$ Fe goes from +2 to +3

Reduction: $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q) \rightarrow \mathrm{Cr}^{3+}(a q) \quad \mathrm{Cr}$ goes from +6 to +3

## Worked Example 4.12

Aqueous sodium hypochlorite ( NaOCl ; household bleach) is a strong oxidizing agent that reacts with chromite ion $\left[\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}\right]$in basic solution to yield chromate ion $\left(\mathrm{CrO}_{4}^{2-}\right)$ and chloride ion. The net ionic equation is

$$
\mathrm{ClO}^{-}(a q)+\mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q) \longrightarrow \mathrm{CrO}_{4}{ }^{2-}(a q)+\mathrm{Cl}^{-}(a q) \quad \text { Unbalanced }
$$

Balance the equation using the half-reaction method.

## Strategy

Follow the steps outlined in Figure 4.4.

## Solution

Steps 1 and 2. The unbalanced net ionic equation shows that chromium is oxidized (from +3 to +6 ) and chlorine is reduced (from +1 to -1 ). Thus, we can write the following two half-reactions:

$$
\begin{array}{ll}
\text { Oxidation half-reaction: } & \mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q) \longrightarrow \mathrm{CrO}_{4}{ }^{2-}(a q) \\
\text { Reduction half-reaction: } & \mathrm{ClO}^{-}(a q) \longrightarrow \mathrm{Cl}^{-}(a q)
\end{array}
$$

Step 3. The half-reactions are already balanced for atoms other than O and H .
Step 4. Balance both half-reactions for O by adding $\mathrm{H}_{2} \mathrm{O}$ to the sides that have less O , and then balance both for H by adding $\mathrm{H}^{+}$to the sides that have less H :

$$
\begin{array}{ll}
\text { Oxidation: } & \mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q) \longrightarrow \mathrm{CrO}_{4}{ }^{2-}(a q)+4 \mathrm{H}^{+}(a q) \\
\text { Reduction: } & \mathrm{ClO}^{-}(a q)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Cl}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
\end{array}
$$

Step 5. Balance both half-reactions for charge by adding electrons to the sides with the greater positive charge:

Oxidation: $\quad \mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}(a q) \longrightarrow \mathrm{CrO}_{4}{ }^{2-}(a q)+4 \mathrm{H}^{+}(a q)+3 \mathrm{e}^{-}$
Reduction: $\quad \mathrm{ClO}^{-}(a q)+2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cl}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)$
Next, multiply the half-reactions by factors that make the electron count in each the same. The oxidation half-reaction must be multiplied by 2 , and the reduction half-reaction must be multiplied by 3 :

Oxidation:

$$
2 \times\left[\mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q) \longrightarrow \mathrm{CrO}_{4}^{2-}(a q)+4 \mathrm{H}^{+}(a q)+3 \mathrm{e}^{-}\right]
$$

or $\quad 2 \mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q) \longrightarrow 2 \mathrm{CrO}_{4}{ }^{2-}(a q)+8 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-}$
Reduction: $\quad 3 \times\left[\mathrm{ClO}^{-}(a q)+2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cl}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)\right]$
or $\quad 3 \mathrm{ClO}^{-}(a q)+6 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 3 \mathrm{Cl}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)$
Step 6. Add the balanced half-reactions:

$$
\begin{aligned}
& 2 \mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q) \longrightarrow 2 \mathrm{CrO}_{4}^{2-}(a q)+8 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \\
& 3 \mathrm{ClO}^{-}(a q)+6 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 3 \mathrm{Cl}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l) \\
& \hline 2 \mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q)+3 \mathrm{ClO}^{-}(a q)+6 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow \\
& 2 \mathrm{CrO}_{4}{ }^{2-}(a q)+3 \mathrm{Cl}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)+8 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-}
\end{aligned}
$$

Now, cancel the species that appear on both sides of the equation:

$$
2 \mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q)+3 \mathrm{ClO}^{-}(a q) \longrightarrow 2 \mathrm{CrO}_{4}^{2-}(a q)+3 \mathrm{Cl}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{H}^{+}(a q)
$$

Finally, since we know that the reaction takes place in basic solution, we must add $2 \mathrm{OH}^{-}$ions to both sides of the equation to neutralize the $2 \mathrm{H}^{+}$ions on the right. The final net ionic equation, balanced for both atoms and charge, is

$$
\begin{gathered}
2 \mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q)+3 \mathrm{ClO}^{-}(a q)+2 \mathrm{OH}^{-}(a q) \longrightarrow 2 \mathrm{CrO}_{4}{ }^{2-}(a q)+3 \mathrm{Cl}^{-}(a q)+5 \mathrm{H}_{2} \mathrm{O}(l) \\
\text { Charge: }(2 \times-1)+(3 \times-1)+(2 \times-1)=-7 r
\end{gathered}
$$

PROBLEM 4.18 Write unbalanced half-reactions for the following net ionic equations:
(a) $\mathrm{MnO}_{4}^{-}(a q)+\mathrm{IO}_{3}^{-}(a q) \rightarrow \mathrm{MnO}_{2}(s)+\mathrm{IO}_{4}^{-}(a q)$
(b) $\mathrm{NO}_{3}{ }^{-}(a q)+\mathrm{SO}_{2}(a q) \rightarrow \mathrm{SO}_{4}{ }^{2-}(a q)+\mathrm{NO}_{2}(g)$

- PROBLEM 4.19 Balance the following net ionic equation by the half-reaction method. The reaction takes place in acidic solution.

$$
\mathrm{NO}_{3}^{-}(a q)+\mathrm{Cu}(s) \longrightarrow \mathrm{NO}(g)+\mathrm{Cu}^{2+}(a q) \quad \text { Unbalanced }
$$

- PROBLEM 4.20 Balance the following equation by the half-reaction method. The reaction takes place in basic solution.

$$
\mathrm{Fe}(\mathrm{OH})_{2}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{Fe}(\mathrm{OH})_{3}(s) \quad \text { Unbalanced }
$$

### 4.11 Redox Titrations

We saw in Section 3.10 that the concentration of an acid or base solution can be determined by titration. A measured volume of an acid (or base) solution of unknown concentration is placed in a flask, and a base (or acid) solution of known concentration is slowly added from a buret. By measuring the volume of the added solution needed for a complete reaction, as signaled by an indicator, the unknown concentration can be calculated.

A similar procedure can be carried out to determine the concentration of many oxidizing or reducing agents using a redox titration. All that's necessary is that the substance whose concentration you want to determine undergo an oxidation or reduction reaction in $100 \%$ yield and that there be some means, such as a color change, to tell when the reaction is complete. The color change might be due to one of the substances undergoing reaction or to some added redox indicator. Let's imagine, for instance, that we have a potassium permanganate solution whose concentration we want to find. Aqueous $\mathrm{KMnO}_{4}$ reacts with oxalic acid, $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, in acidic solution according to the net ionic equation

$$
\begin{aligned}
& 5 \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}(a q)+2 \mathrm{MnO}_{4}^{-}(a q)+6 \mathrm{H}^{+}(a q) \longrightarrow \\
& 10 \mathrm{CO}_{2}(g)+2 \mathrm{Mn}^{2+}(a q)+8 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

The reaction takes place in $100 \%$ yield and is accompanied by a sharp color change when the intense purple color of the $\mathrm{MnO}_{4}^{-}$ion disappears.

The strategy used for this and other redox titrations is outlined in Figure 4.5. As with acid-base titrations, the general idea is to measure a known amount of one substance-in this case, $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$-and use mole ratios from the balanced equation to find the number of moles of the second substance-in this case, $\mathrm{KMnO}_{4}$-necessary for complete reaction. With the molar amount of $\mathrm{KMnO}_{4}$ thus

FIGURE 4.5 A flow diagram for a redox titration, summarizing the calculations needed to determine the concentration of a $\mathrm{KMnO}_{4}$ solution by titration of a known mass of $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$.

known, titration gives the volume of solution containing that amount. Dividing the number of moles by the volume gives the concentration.

As an example of how this redox titration works, let's carefully weigh an amount of $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$-say, 0.2585 g -and dissolve it in approximately 100 mL of $0.5 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$. The exact volume isn't important because we're concerned only with the amount of dissolved $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, not with its concentration. Next, we place an aqueous $\mathrm{KMnO}_{4}$ solution of unknown concentration in a buret and slowly add it to the $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ solution. The purple color of $\mathrm{MnO}_{4}^{-}$initially disappears as reaction occurs, but we continue the addition until a faint color persists, indicating that all the $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ has reacted and that $\mathrm{MnO}_{4}^{-}$ion is no longer being reduced. At this point, we might find that 22.35 mL of the $\mathrm{KMnO}_{4}$ solution has been added (Figure 4.6).


To calculate the molarity of the $\mathrm{KMnO}_{4}$ solution, we need to find the number of moles of $\mathrm{KMnO}_{4}$ present in the 22.35 mL of solution used for titration. We do this by first calculating the number of moles of oxalic acid that react with the permanganate ion, using a gram-to-mole conversion with the molar mass of $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ as the conversion factor:

$$
\text { Moles of } \begin{aligned}
\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4} & =0.2585 \mathrm{~g} \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4} \times \frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}}{90.04 \mathrm{gH}_{2} \mathrm{C}_{2} \mathrm{O}_{4}} \\
& =2.871 \times 10^{-3} \mathrm{~mol} \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}
\end{aligned}
$$

According to the balanced equation, 5 mol of oxalic acid react with 2 mol of permanganate ion. Thus, we can calculate the number of moles of $\mathrm{KMnO}_{4}$ that react with $2.871 \times 10^{-3} \mathrm{~mol}$ of $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ :

$$
\begin{aligned}
\text { Moles of } \mathrm{KMnO}_{4} & =2.871 \times 10^{-3} \mathrm{molH}_{2} \mathrm{C}_{2} \mathrm{O}_{4} \times \frac{2 \mathrm{~mol} \mathrm{KMnO}_{4}}{5 \mathrm{molH}_{2} \mathrm{C}_{2} \mathrm{O}_{4}} \\
& =1.148 \times 10^{-3} \mathrm{~mol} \mathrm{KMnO}_{4}
\end{aligned}
$$

Knowing both the number of moles of $\mathrm{KMnO}_{4}$ that react ( $1.148 \times 10^{-3} \mathrm{~mol}$ ) and the volume of the $\mathrm{KMnO}_{4}$ solution ( 22.35 mL ) then makes it possible to calculate the molarity:

$$
\text { Molarity }=\frac{1.148 \times 10^{-3} \mathrm{~mol} \mathrm{KMnO}_{4}}{22.35 \mathrm{mE}} \times \frac{1000 \mathrm{mZ}}{1 \mathrm{~L}}=0.05136 \mathrm{M}
$$

The molarity of the $\mathrm{KMnO}_{4}$ solution as determined by redox titration is 0.05136 M .

4 FIGURE 4.6 The redox titration of oxalic acid, $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, with $\mathrm{KMnO}_{4}$. (a) A precise amount of oxalic acid is weighed and dissolved in aqueous sulfuric acid. (b) Aqueous $\mathrm{KMnO}_{4}$ of unknown concentration is then added from a buret until (c) the purple color persists, indicating that all the $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ has been oxidized.

## Worked Example 4.13

The concentration of an aqueous $\mathrm{I}_{3}{ }^{-}$solution can be determined by titration with aqueous sodium thiosulfate, $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$, in the presence of a starch indicator, which turns from deep blue to colorless when all the $\mathrm{I}_{3}{ }^{-}$has reacted. What is the molar concentration of $\mathrm{I}_{3}{ }^{-}$if 24.55 mL of $0.102 \mathrm{M} \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ is needed for complete reaction with 10.00 mL of the $\mathrm{I}_{3}{ }^{-}$solution? The net ionic equation is

$$
2 \mathrm{~S}_{2} \mathrm{O}_{3}{ }^{2-}(a q)+\mathrm{I}_{3}^{-}(a q) \longrightarrow \mathrm{S}_{4} \mathrm{O}_{6}^{2-}(a q)+3 \mathrm{I}^{-}(a q)
$$

## Strategy and Solution

The procedure is similar to that outlined in Figure 4.5. We first need to find the number of moles of thiosulfate ion used for the titration:

$$
24.55 \mathrm{~mL} \times \frac{1 \mathrm{~L}}{1000 \mathrm{mt}} \times \frac{0.102 \mathrm{~mol} \mathrm{~S}_{2} \mathrm{O}_{3}{ }^{2-}}{1 \mathrm{~L}}=2.50 \times 10^{-3} \mathrm{~mol} \mathrm{~S}_{2} \mathrm{O}_{3}{ }^{2-}
$$

According to the balanced equation, 2 mol of $\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}$ ion react with 1 mol of $\mathrm{I}_{3}{ }^{-}$ion. Thus, we can find the number of moles of $\mathrm{I}_{3}{ }^{-}$ion:

$$
2.50 \times 10^{-3} \mathrm{molS}_{2} \mathrm{O}_{3}{ }^{2-} \times \frac{1 \mathrm{~mol} \mathrm{I}_{3}^{-}}{2 \mathrm{molS}_{2} \mathrm{O}_{3}{ }^{2-}}=1.25 \times 10^{-3} \mathrm{~mol} \mathrm{I}_{3}^{-}
$$

Knowing both the number of moles $\left(1.25 \times 10^{-3} \mathrm{~mol}\right)$ and the volume $(10.00 \mathrm{~mL})$ then lets us calculate molarity:

$$
\frac{1.25 \times 10^{-3} \mathrm{~mol} \mathrm{I}_{3}^{-}}{10.00 \mathrm{~mL}} \times \frac{10^{3} \mathrm{mt}}{1 \mathrm{~L}}=0.125 \mathrm{M}
$$

The molarity of the $\mathrm{I}_{3}{ }^{-}$solution is 0.125 M .
$\checkmark$ Ballpark Check According to the balanced equation, the amount of $\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}$ needed for the reaction ( 2 mol ) is twice the amount of $\mathrm{I}_{3}{ }^{-}(1 \mathrm{~mol})$. The titration results indicate that the volume of the $\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}$ solution ( 24.55 mL ) is a little over twice the volume of the $\mathrm{I}_{3}{ }^{-}$solution ( 10.00 mL ). Thus, the concentrations of the two solutions must be about the same-approximately 0.1 M .


A The red $\mathrm{I}_{3}{ }^{-}$solution turns a deep blue color when it is added to a solution containing a small amount of starch.

PROBLEM 4.21 The concentration of $\mathrm{Fe}^{2+}$ ion in aqueous solution can be determined by redox titration with bromate ion, $\mathrm{BrO}_{3}{ }^{-}$, according to the net ionic equation

$$
6 \mathrm{Fe}^{2+}(a q)+\mathrm{BrO}_{3}^{-}(a q)+6 \mathrm{H}^{+}(a q) \longrightarrow 6 \mathrm{Fe}^{3+}(a q)+\mathrm{Br}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)
$$

What is the molar concentration of $\mathrm{Fe}^{2+}$ if 31.50 mL of $0.105 \mathrm{M} \mathrm{KBrO}_{3}$ is required for complete reaction with 10.00 mL of the $\mathrm{Fe}^{2+}$ solution?

### 4.12 Some Applications of Redox Reactions

Redox reactions take place with almost every element in the periodic table and occur in a vast number of processes throughout nature, biology, and industry. Here are just a few examples:

- Combustion is the burning of a fuel by oxidation with oxygen in air. Gasoline, fuel oil, natural gas, wood, paper, and other organic substances of carbon and hydrogen are the most common fuels. Even some metals, such as magnesium and calcium, will burn in air.

$$
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

Methane (natural gas)

- Bleaching uses redox reactions to decolorize or lighten colored materials. Dark hair is bleached to turn it blond, clothes are bleached to remove stains, wood pulp is bleached to make white paper, and so on. The exact oxidizing agent used depends on the situation: hydrogen peroxide $\left(\mathrm{H}_{2} \mathrm{O}_{2}\right)$ is used for hair, sodium hypochlorite $(\mathrm{NaOCl})$ is used for clothes, and elemental chlorine is used for wood pulp, but the principle is always the same. In all cases, colored impurities are destroyed by reaction with a strong oxidizing agent.
- Batteries, although they come in many types and sizes, are all based on redox reactions. In a typical redox reaction carried out in the laboratory-say, the reaction of zinc metal with $\mathrm{Ag}^{+}$to yield $\mathrm{Zn}^{2+}$ and silver metal-the reactants are simply mixed in a flask and electrons are transferred by direct contact between the reactants. In a battery, however, the two reactants are kept in separate compartments and the electrons are transferred through a wire running between them.

The common household battery found in flashlights and radios uses a can of zinc metal as one reactant and a paste of solid manganese dioxide as the other. A graphite rod sticks into the $\mathrm{MnO}_{2}$ paste to provide electrical contact, and a moist paste of ammonium chloride separates the two reactants. When the zinc can and the graphite rod are connected by a wire, zinc sends electrons flowing through the wire toward the $\mathrm{MnO}_{2}$ in a redox reaction. The resultant electrical current can be used to light a bulb or power a radio. The reaction is

$$
\mathrm{Zn}(s)+2 \mathrm{MnO}_{2}(s)+2 \mathrm{NH}_{4} \mathrm{Cl}(s) \longrightarrow \mathrm{ZnCl}_{2}(a q)+\mathrm{Mn}_{2} \mathrm{O}_{3}(s)+2 \mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

- Metallurgy, the science of extracting and purifying metals from their ores, makes use of numerous redox processes. We'll see in Section 21.2, for example, that metallic zinc is prepared by reduction of ZnO with coke, a form of carbon:

$$
\mathrm{ZnO}(s)+\mathrm{C}(s) \longrightarrow \mathrm{Zn}(s)+\mathrm{CO}(g)
$$

- Corrosion is the deterioration of a metal by oxidation, such as the rusting of iron in moist air. The economic consequences of rusting are enormous: It has been estimated that up to one-fourth of the iron produced in the United States is used to replace bridges, buildings, and other structures that have been destroyed by corrosion. (The raised dot in the formula $\mathrm{Fe}_{2} \mathrm{O}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ for rust indicates that one water molecule is associated with each $\mathrm{Fe}_{2} \mathrm{O}_{3}$ in an undefined way.)

$$
4 \mathrm{Fe}(s)+3 \mathrm{O}_{2}(g) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} 2 \mathrm{Fe}_{2} \mathrm{O}_{3} \cdot \mathrm{H}_{2} \mathrm{O}(s)
$$

- Respiration is the process of breathing and using oxygen for the many biological redox reactions that provide the energy needed by living organisms. The energy is released from food molecules slowly and in complex, multistep pathways, but the overall result of respiration is similar to that of a combustion reaction. For example, the simple sugar glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ reacts with $\mathrm{O}_{2}$ to give $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ according to the following equation:

$$
\begin{aligned}
& \quad \mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}+6 \mathrm{O}_{2} \longrightarrow 6 \mathrm{CO}_{2}+6 \mathrm{H}_{2} \mathrm{O}+\text { energy } \\
& \quad \begin{array}{l}
\text { Glucose } \\
\text { (a carbohydrate) }
\end{array}
\end{aligned}
$$

## Interlude Photography: A Series of Redox Reactions

 hotography is so common that most people never give a moment's thought to how remarkable the process is. Ordinary black-and-white photographic film consists of a celluloid strip that has been coated with a gelatin emulsion containing very tiny crystals, or "grains," of a silver halide, usually AgBr . There is a considerable amount of art as well as science to making the film, and the recipes used by major manufacturers are well-guarded secrets. When exposed to light, the surfaces of the AgBr grains turn dark because of a light-induced redox reaction in which $\mathrm{Br}^{-}$transfers an electron to $\mathrm{Ag}^{+}$, producing atoms of elemental silver and $\mathrm{Br}_{2}$, which reacts with the gelatin emulsion (Figure 4.7). Those areas of the film exposed to the brightest light have the largest number of silver atoms, and those areas exposed to the least light have the smallest number.

$$
2 \mathrm{AgBr} \xrightarrow{\text { Light }} 2 \mathrm{Ag}+\mathrm{Br}_{2}
$$

Perhaps surprisingly in view of what a finished photograph looks like, only a few hundred out of many trillions of $\mathrm{Ag}^{+}$ions in each grain are reduced to Ag atoms, and the latent image produced on the film is still invisible at this point. The key to silver halide photography is the developing process, in which the latent image is amplified.

By mechanisms still not understood in detail, the presence of a relatively tiny number of Ag atoms on the surface of an
AgBr grain sensitizes the remaining $\mathrm{Ag}^{+}$ions in the grain
toward further reduction when the film is exposed to the organic reducing agent hydroquinone. Those grains that have
been exposed to the strongest light-and thus have more Ag atoms-reduce and darken quickly, while those grains with fewer Ag atoms reduce and darken more slowly. By carefully monitoring the amount of time allowed for reduction of the AgBr grains with hydroquinone, it's possible to amplify the latent image on the exposed film and make it visible.

(a)

(b)

Once the image is fully formed, the film is fixed by washing away the remaining unreduced AgBr so that the film is no longer sensitive to light. Although pure AgBr is insoluble in water, it is made soluble by reaction with a solution of sodium thiosulfate, $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$, called hypo by photographers.

$$
\mathrm{AgBr}(s)+2 \mathrm{~S}_{2} \mathrm{O}_{3}^{2-}(a q) \longrightarrow \mathrm{Ag}\left(\mathrm{~S}_{2} \mathrm{O}_{3}\right)_{2}^{3-}(a q)+\mathrm{Br}^{-}(a q)
$$

At this point, the film contains a negative image formed by a layer of black, finely divided silver metal, a layer that is denser and darker in those areas exposed to the most light but lighter in those areas exposed to the least light. To convert this negative image into the final printed photograph, the entire photographic procedure is repeated a second time. Light is passed through the negative image onto special photographic paper that is coated with the same kind of gelatin -AgBr emulsion used on the original film. Developing the photographic paper with hydroquinone and fixing the image with sodium thiosulfate reverses the negative image, and a final, positive image is produced. The whole process from film to print is carried out billions of times and consumes over 3 million pounds of silver each year.

- PROBLEM 4.22 What is the purpose of $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$, or hypo, in the photographic process?

PROBLEM 4.23 The image produced on photographic film is a negative one, with dark objects appearing light, and light objects appearing dark. Explain how this negative image is converted to a positive image when printed.

(c)

A FIGURE 4.7 (a) When the paper clip sitting on powdered AgCl crystals is exposed to a bright light, (b) the crystals around the clip darken to provide an image of the clip (c).

Summary

Many reactions, particularly those that involve ionic compounds, take place in aqueous solution. Substances whose aqueous solutions contain ions and therefore conduct electricity are called electrolytes. Ionic compounds, such as NaCl , and molecular compounds that dissociate substantially into ions when dissolved in water are strong electrolytes. Substances that dissociate to only a small extent are weak electrolytes, and substances that do not produce ions in aqueous solution are nonelectrolytes. Acids dissociate in aqueous solutions to yield an anion and a hydronium ion, $\mathrm{H}_{3} \mathrm{O}^{+}$. Those acids that dissociate to a large extent are strong acids; those acids that dissociate to a small extent are weak acids.

There are three important classes of aqueous reactions. Precipitation reactions occur when solutions of two ionic substances are mixed and a precipitate falls from solution. To predict whether a precipitate will form, you must know the solubility of each potential product. Acid-base neutralization reactions occur when an acid is mixed with a base, yielding water and a salt. The neutralization of a strong acid with a strong base can be written as a net ionic equation, in which nonparticipating, spectator ions are not specified:

$$
\mathrm{H}^{+}(a q)+\mathrm{OH}^{-}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)
$$

Oxidation-reduction reactions, or redox reactions, are processes in which one or more electrons are transferred
between reaction partners. An oxidation is the loss of one or more electrons; a reduction is the gain of one or more electrons. Redox reactions can be identified by assigning to each atom in a substance an oxidation number, which provides a measure of whether the atom is neutral, electron-rich, or electron-poor. Comparing the oxidation numbers of an atom before and after reaction shows whether the atom has gained or lost electrons.

Oxidations and reductions must occur together. Whenever one substance loses one or more electrons (is oxidized), another substance gains those electrons (is reduced). The substance that causes a reduction by giving up electrons is called a reducing agent. The substance that causes an oxidation by accepting electrons is called an oxidizing agent. The reducing agent is itself oxidized when it gives up electrons, and the oxidizing agent is itself reduced when it accepts electrons.

Among the simplest of redox processes is the reaction of an aqueous cation, usually a metal ion, with a free element to give a different ion and a different element. Noting the results from a succession of different reactions makes it possible to organize an activity series, which ranks the elements in order of their reducing ability in aqueous solution.

Redox reactions can be balanced using either the oxidation-number method or the half-reaction method. The concentration of an oxidizing agent or a reducing agent in solution can be determined by a redox titration.

## Key Words

acid-base neutralization reaction 116
activity series 132
dissociate 118
electrolyte 117
half-reaction 138
half-reaction method 138
hydronium ion $\mathrm{H}_{3} \mathrm{O}^{+}$ 123
ionic equation 119
molecular equation 119
net ionic equation 119
nonelectrolyte 117
oxidation 126
oxidation number 126
oxidation-number method 134
oxidation-reduction reaction 116
oxidizing agent 129
precipitation reaction 116
redox reaction 116
redox titration 142
reducing agent 129
reduction 126
salt 116
solubility 120
spectator ion 119
strong acid 123
strong base 124
strong electrolyte 118
weak acid 123
weak base 124
weak electrolyte 118

## Key Concept Summary



## Understanding Key Concepts

Problems 4.1-4.23 appear within the chapter.
4.24 Assume that an aqueous solution of a cation, represented as a red sphere, is allowed to mix with a solution of an anion, represented as a yellow sphere. Three possible outcomes are represented by boxes (1)-(3):


Which outcome corresponds to each of the following reactions?
(a) $2 \mathrm{Na}^{+}(a q)+\mathrm{CO}_{3}{ }^{2-}(a q) \rightarrow$
(b) $\mathrm{Ba}^{2+}(a q)+\mathrm{CrO}_{4}{ }^{2-}(a q) \rightarrow$
(c) $2 \mathrm{Ag}^{+}(a q)+\mathrm{SO}_{3}{ }^{2-}(a q) \rightarrow$
4.25 Assume that an aqueous solution of a cation, represented as a blue sphere, is allowed to mix with a solution of an anion, represented as a green sphere, and that the following result is obtained:


Which combinations of cation and anion, chosen from the following lists, are compatible with the observed results? Explain.
Cations: $\mathrm{Na}^{+}, \mathrm{Ca}^{2+}, \mathrm{Ag}^{+}, \mathrm{Ni}^{2+}$
Anions: $\mathrm{Cl}^{-}, \mathrm{CO}_{3}{ }^{2-}, \mathrm{CrO}_{4}{ }^{2-}, \mathrm{NO}_{3}{ }^{-}$
4.26 Assume that an aqueous solution of $\mathrm{OH}^{-}$, represented as a blue sphere, is allowed to mix with a solution of an acid $\mathrm{H}_{n} \mathrm{~A}$, represented as a red sphere. Three possible outcomes are depicted by boxes (1)-(3), where the green spheres represent $\mathrm{A}^{n-}$, the anion of the acid:

(1)

(3)

Which outcome corresponds to each of the following reactions?
(a) $\mathrm{HF}+\mathrm{OH}^{-} \rightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{F}^{-}$
(b) $\mathrm{H}_{2} \mathrm{SO}_{3}+2 \mathrm{OH}^{-} \rightarrow 2 \mathrm{H}_{2} \mathrm{O}+\mathrm{SO}_{3}{ }^{2-}$
(c) $\mathrm{H}_{3} \mathrm{PO}_{4}+3 \mathrm{OH}^{-} \rightarrow 3 \mathrm{H}_{2} \mathrm{O}+\mathrm{PO}_{4}{ }^{3-}$
4.27 The concentration of an aqueous solution of NaOCl (sodium hypochlorite; the active ingredient in household bleach) can be determined by a redox titration with iodide ion in acidic solution:

$$
\begin{aligned}
& \mathrm{OCl}^{-}(a q)+2 \mathrm{I}^{-}(a q)+2 \mathrm{H}^{+}(a q) \longrightarrow \\
& \mathrm{Cl}^{-}(a q)+\mathrm{I}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

Assume that the blue spheres in the buret represent $\mathrm{I}^{-}$ ions, the red spheres in the flask represent $\mathrm{OCl}^{-}$ions, the concentration of the $\mathrm{I}^{-}$ions in the buret is 0.120 M , and the volumes in the buret and the flask are identical. What is the concentration of NaOCl in the flask? What percentage of the $\mathrm{I}^{-}$solution in the buret must be added to the flask to react with all the $\mathrm{OCl}^{-}$ions?

4.28 Assume that the conductivity of a solution depends on the total concentration of dissolved ions and that you measure the conductivity of three different solutions while carrying out titration procedures:
(a) Begin with 1.00 L of 0.100 M KCl , and titrate by addition of $0.100 \mathrm{M} \mathrm{AgNO}_{3}$.
(b) Begin with 1.00 L of 0.100 M HF , and titrate by addition of 0.100 M KOH .
(c) Begin with 1.00 L of $0.100 \mathrm{M} \mathrm{BaCl}_{2}$, and titrate by addition of $0.100 \mathrm{M} \mathrm{Na}_{2} \mathrm{SO}_{4}$.
Which of the following graphs corresponds to which titration?

(1)

(2)

(3)
4.29 Based on the positions in the periodic table, which of the following reactions would you expect to occur?
(a) Red $^{+}+$Green $\rightarrow$ Red + Green ${ }^{+}$
(b) Blue + Green $^{+} \rightarrow$ Blue $^{+}+$Green
(c) Red + Blue $^{+} \rightarrow$ Red $^{+}+$Blue


## Additional Problems

## Aqueous Reactions and Net Ionic Equations

4.30 Classify each of the following reactions as a precipitation, acid-base neutralization, or oxidation-reduction:
(a) $\mathrm{Hg}\left(\mathrm{NO}_{3}\right)_{2}(a q)+2 \mathrm{NaI}(a q) \longrightarrow$

$$
2 \mathrm{NaNO}_{3}(a q)+\mathrm{HgI}_{2}(s)
$$

(b) $2 \mathrm{HgO}(s) \xrightarrow{\text { Heat }} 2 \mathrm{Hg}(l)+\mathrm{O}_{2}(g)$
(c) $\mathrm{H}_{3} \mathrm{PO}_{4}(a q)+3 \mathrm{KOH}(a q) \longrightarrow$

$$
\mathrm{K}_{3} \mathrm{PO}_{4}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)
$$

4.31 Classify each of the following reactions as a precipitation, acid-base neutralization, or oxidation-reduction:
(a) $\mathrm{S}_{8}(\mathrm{~s})+8 \mathrm{O}_{2}(g) \longrightarrow 8 \mathrm{SO}_{2}(g)$
(b) $\mathrm{NiCl}_{2}(a q)+\mathrm{Na}_{2} \mathrm{~S}(a q) \longrightarrow \mathrm{NiS}(s)+2 \mathrm{NaCl}(a q)$
(c) $2 \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{Ba}(\mathrm{OH})_{2}(a q) \longrightarrow$ $\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)_{2} \mathrm{Ba}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)$
4.32 Write net ionic equations for the reactions listed in Problem 4.30.
4.33 Write net ionic equations for the reactions listed in Problem 4.31.
4.34 Individual solutions of $\mathrm{Ba}(\mathrm{OH})_{2}$ and $\mathrm{H}_{2} \mathrm{SO}_{4}$ both conduct electricity, but the conductivity disappears when equal molar amounts of the solutions are mixed. Explain.
4.35 A solution of HCl in water conducts electricity but a solution of HCl in chloroform, $\mathrm{CHCl}_{3}$, does not. What does this observation tell you about the way HCl exists in water and the way it exists in chloroform?
4.36 Classify each of the following substances as either a strong electrolyte, weak electrolyte, or nonelectrolyte:
(a) HBr
(b) HF
(c) $\mathrm{NaClO}_{4}$
(d) $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$
(e) $\mathrm{NH}_{3}$
(f) Ethyl alcohol
4.37 Is it possible for a molecular substance to be a strong electrolyte? Explain.
4.38 What is the total molar concentration of ions in each of the following solutions, assuming complete dissociation?
(a) A 0.750 M solution of $\mathrm{K}_{2} \mathrm{CO}_{3}$
(b) A 0.355 M solution of $\mathrm{AlCl}_{3}$
4.39 What is the total molar concentration of ions in each of the following solutions?
(a) A 1.250 M solution of $\mathrm{CH}_{3} \mathrm{OH}$
(b) A 0.225 M solution of $\mathrm{HClO}_{4}$

## Precipitation Reactions and Solubility Rules

4.40 Which of the following substances are likely to be soluble in water?
(a) $\mathrm{Ag}_{2} \mathrm{O}$
(b) $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$
(c) $\mathrm{SnCO}_{3}$
(d) $\mathrm{Fe}_{2} \mathrm{O}_{3}$
4.41 Which of the following substances are likely to be soluble in water?
(a) ZnS
(b) $\mathrm{Au}_{2}\left(\mathrm{CO}_{3}\right)_{3}$
(c) $\mathrm{PbCl}_{2}$
(d) $\mathrm{MnO}_{2}$
4.42 Predict whether a precipitation reaction will occur when aqueous solutions of the following substances are mixed:
(a) $\mathrm{NaOH}+\mathrm{HClO}_{4}$
(b) $\mathrm{FeCl}_{2}+\mathrm{KOH}$
(c) $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{SO}_{4}+\mathrm{NiCl}_{2}$
(d) $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}+\mathrm{HCl}$
4.43 Predict whether a precipitation reaction will occur when aqueous solutions of the following substances are mixed:
(a) $\mathrm{MnCl}_{2}+\mathrm{Na}_{2} \mathrm{~S}$
(b) $\mathrm{HNO}_{3}+\mathrm{CuSO}_{4}$
(c) $\mathrm{Hg}\left(\mathrm{NO}_{3}\right)_{2}+\mathrm{Na}_{3} \mathrm{PO}_{4}$
(d) $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}+\mathrm{KOH}$
4.44 How would you prepare the following substances by a precipitation reaction?
(a) $\mathrm{PbSO}_{4}$
(b) $\mathrm{Mg}_{3}\left(\mathrm{PO}_{4}\right)_{2}$
(c) $\mathrm{ZnCrO}_{4}$
4.45 How would you prepare the following substances by a precipitation reaction?
(a) $\mathrm{Al}(\mathrm{OH})_{3}$
(b) FeS
(c) $\mathrm{CoCO}_{3}$
4.46 Assume that you have an aqueous mixture of $\mathrm{NaNO}_{3}$ and $\mathrm{AgNO}_{3}$. How could you use a precipitation reaction to separate the two metal ions?
4.47 Assume that you have an aqueous mixture of $\mathrm{BaCl}_{2}$ and $\mathrm{CuCl}_{2}$. How could you use a precipitation reaction to separate the two metal ions?
4.48 Assume that you have an aqueous solution of an unknown salt. Treatment of the solution with dilute $\mathrm{NaOH}, \mathrm{Na}_{2} \mathrm{SO}_{4}$, and KCl produces no precipitate. Which of the following cations might the solution contain?
(a) $\mathrm{Ag}^{+}$
(b) $\mathrm{Cs}^{+}$
(c) $\mathrm{Ba}^{2+}$
(d) $\mathrm{NH}_{4}^{+}$
4.49 Assume that you have an aqueous solution of an unknown salt. Treatment of the solution with dilute $\mathrm{BaCl}_{2}, \mathrm{AgNO}_{3}$, and $\mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}$ produces no precipitate. Which of the following anions might the solution contain?
(a) $\mathrm{Cl}^{-}$
(b) $\mathrm{NO}_{3}{ }^{-}$
(c) $\mathrm{OH}^{-}$
(d) $\mathrm{SO}_{4}{ }^{2-}$

## Acids, Bases, and Neutralization Reactions

4.50 Assume that you are given a solution of an unknown acid or base. How can you tell whether the unknown substance is acidic or basic?
4.51 Why do we use a double arrow $(\rightleftharpoons)$ to show the dissociation of a weak acid or weak base in aqueous solution?
4.52 Write balanced ionic equations for the following reactions:
(a) Aqueous perchloric acid is neutralized by aqueous calcium hydroxide.
(b) Aqueous sodium hydroxide is neutralized by aqueous acetic acid.
4.53 Write balanced ionic equations for the following reactions:
(a) Aqueous hydrofluoric acid is neutralized by aqueous calcium hydroxide.
(b) Aqueous magnesium hydroxide is neutralized by aqueous nitric acid.
4.54 Write balanced net ionic equations for the following reactions:
(a) $\mathrm{LiOH}(a q)+\mathrm{HI}(a q) \rightarrow$
(b) $\mathrm{HBr}(a q)+\mathrm{Ca}(\mathrm{OH})_{2}(a q) \rightarrow$
4.55 Write balanced net ionic equations for the following reactions: (Note: $\mathrm{HClO}_{3}$ is a strong acid.)
(a) $\mathrm{Fe}(\mathrm{OH})_{3}(s)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \rightarrow$
(b) $\mathrm{HClO}_{3}(a q)+\mathrm{NaOH}(a q) \rightarrow$

## Redox Reactions and Oxidation Numbers

4.56 Where in the periodic table are the best reducing agents found? The best oxidizing agents?
4.57 Where in the periodic table are the most easily reduced elements found? The most easily oxidized?
4.58 Tell in each of the following instances whether the substance gains electrons or loses electrons in a redox reaction:
(a) An oxidizing agent
(b) A reducing agent
(c) A substance undergoing oxidation
(d) A substance undergoing reduction
4.59 Tell for each of the following substances whether the oxidation number increases or decreases in a redox reaction:
(a) An oxidizing agent
(b) A reducing agent
(c) A substance undergoing oxidation
(d) A substance undergoing reduction
4.60 Assign oxidation numbers to each element in the following compounds:
(a) $\mathrm{NO}_{2}$
(b) $\mathrm{SO}_{3}$
(c) $\mathrm{COCl}_{2}$
(d) $\mathrm{CH}_{2} \mathrm{Cl}_{2}$
(e) $\mathrm{KClO}_{3}$
(f) $\mathrm{HNO}_{3}$
4.61 Assign oxidation numbers to each element in the following compounds:
(a) $\mathrm{VOCl}_{3}$
(b) $\mathrm{CuSO}_{4}$
(c) $\mathrm{CH}_{2} \mathrm{O}$
(d) $\mathrm{Mn}_{2} \mathrm{O}_{7}$
(e) $\mathrm{OsO}_{4}$
(f) $\mathrm{H}_{2} \mathrm{PtCl}_{6}$
4.62 Assign oxidation numbers to each element in the following ions:
(a) $\mathrm{ClO}_{3}{ }^{-}$
(b) $\mathrm{SO}_{3}{ }^{2-}$
(c) $\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}$
(d) $\mathrm{NO}_{2}{ }^{-}$
(e) $\mathrm{BrO}^{-}$
(f) $\mathrm{AsO}_{4}{ }^{3-}$
4.63 Assign oxidation numbers to each element in the following ions:
(a) $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}$
(b) $\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}$
(c) $\mathrm{NO}_{3}^{-}$
(d) $\mathrm{MnO}_{4}{ }^{2-}$
(e) $\mathrm{HPO}_{4}{ }^{2-}$
(f) $\mathrm{V}_{2} \mathrm{O}_{7}{ }^{4-}$
4.64 Which element is oxidized and which is reduced in each of the following reactions?
(a) $\mathrm{Ca}(s)+\mathrm{Sn}^{2+}(a q) \rightarrow \mathrm{Ca}^{2+}(a q)+\mathrm{Sn}(s)$
(b) $\mathrm{ICl}(s)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow \mathrm{HCl}(a q)+\mathrm{HOI}(a q)$
4.65 Which element is oxidized and which is reduced in each of the following reactions?
(a) $\mathrm{Si}(s)+2 \mathrm{Cl}_{2}(g) \rightarrow \mathrm{SiCl}_{4}(l)$
(b) $\mathrm{Cl}_{2}(g)+2 \mathrm{NaBr}(a q) \rightarrow \mathrm{Br}_{2}(a q)+2 \mathrm{NaCl}(a q)$
4.66 Use the activity series of metals (Table 4.3) to predict the outcome of each of the following reactions. If no reaction occurs, write N.R.
(a) $\mathrm{Na}^{+}(a q)+\mathrm{Zn}(s) \rightarrow$
(b) $\mathrm{HCl}(a q)+\mathrm{Pt}(s) \rightarrow$
(c) $\mathrm{Ag}^{+}(a q)+\mathrm{Au}(s) \rightarrow$
(d) $\mathrm{Au}^{3+}(a q)+\mathrm{Ag}(s) \rightarrow$
4.67 Neither strontium ( Sr ) nor antimony $(\mathrm{Sb})$ is shown in the activity series of Table 4.3. Based on their positions in the periodic table, which would you expect to be the better reducing agent? Will the following reaction occur? Explain.

$$
2 \mathrm{Sb}^{3+}(a q)+3 \mathrm{Sr}(s) \longrightarrow 2 \mathrm{Sb}(s)+3 \mathrm{Sr}^{2+}(a q)
$$

4.68 (a) Use the following reactions to arrange the elements $A, B, C$, and $D$ in order of their redox activity:

$$
\begin{array}{ll}
\mathrm{A}+\mathrm{B}^{+} \longrightarrow \mathrm{A}^{+}+\mathrm{B} & \mathrm{C}^{+}+\mathrm{D} \longrightarrow \text { no reaction } \\
\mathrm{B}+\mathrm{D}^{+} \longrightarrow \mathrm{B}^{+}+\mathrm{D} & \mathrm{~B}+\mathrm{C}^{+} \longrightarrow \mathrm{B}^{+}+\mathrm{C}
\end{array}
$$

(b) Which of the following reactions would you expect to occur according to the activity series you established in part (a)?
(1) $\mathrm{A}^{+}+\mathrm{C} \longrightarrow \mathrm{A}+\mathrm{C}^{+}$
(2) $\mathrm{A}^{+}+\mathrm{D} \longrightarrow \mathrm{A}+\mathrm{D}^{+}$
4.69 (a) Use the following reactions to arrange the elements $\mathrm{A}, \mathrm{B}, \mathrm{C}$, and D in order of their redox activity:
$2 \mathrm{~A}+\mathrm{B}^{2+} \longrightarrow 2 \mathrm{~A}^{+}+\mathrm{B} \quad \mathrm{B}+\mathrm{D}^{2+} \longrightarrow \mathrm{B}^{2+}+\mathrm{D}$ $\mathrm{A}^{+}+\mathrm{C} \longrightarrow$ no reaction $\quad 2 \mathrm{C}+\mathrm{B}^{2+} \longrightarrow 2 \mathrm{C}^{+}+\mathrm{B}$
(b) Which of the following reactions would you expect to occur according to the activity series you established in part (a)?

$$
\text { (1) } 2 \mathrm{~A}^{+}+\mathrm{D} \longrightarrow 2 \mathrm{~A}+\mathrm{D}^{2+}
$$

$$
\text { (2) } \mathrm{D}^{2+}+2 \mathrm{C} \longrightarrow \mathrm{D}+2 \mathrm{C}^{+}
$$

## Balancing Redox Reactions

4.70 Classify each of the following unbalanced halfreactions as either an oxidation or a reduction:
(a) $\mathrm{NO}_{3}^{-}(a q) \rightarrow \mathrm{NO}(g)$
(b) $\mathrm{Zn}(s) \rightarrow \mathrm{Zn}^{2+}(a q)$
(c) $\mathrm{Ti}^{3+}(a q) \rightarrow \mathrm{TiO}_{2}(s)$
(d) $\mathrm{Sn}^{4+}(a q) \rightarrow \mathrm{Sn}^{2+}(a q)$
4.71 Classify each of the following unbalanced halfreactions as either an oxidation or a reduction:
(a) $\mathrm{O}_{2}(g) \rightarrow \mathrm{OH}^{-}(a q)$
(b) $\mathrm{H}_{2} \mathrm{O}_{2}(a q) \rightarrow \mathrm{O}_{2}(g)$
(c) $\mathrm{MnO}_{4}^{-}(a q) \rightarrow \mathrm{MnO}_{4}{ }^{2-}(a q)$
(d) $\mathrm{CH}_{3} \mathrm{OH}(a q) \rightarrow \mathrm{CH}_{2} \mathrm{O}(a q)$
4.72 Balance the half-reactions in Problem 4.70, assuming that they occur in acidic solution.
4.73 Balance the half-reactions in Problem 4.71, assuming that they occur in basic solution.
4.74 Write unbalanced oxidation and reduction halfreactions for the following processes:
(a) $\mathrm{Te}(s)+\mathrm{NO}_{3}^{-}(a q) \rightarrow \mathrm{TeO}_{2}(s)+\mathrm{NO}(g)$
(b) $\mathrm{H}_{2} \mathrm{O}_{2}(a q)+\mathrm{Fe}^{2+}(a q) \rightarrow \mathrm{Fe}^{3+}(a q)+\mathrm{H}_{2} \mathrm{O}(l)$
4.75 Write unbalanced oxidation and reduction halfreactions for the following processes:
(a) $\mathrm{Mn}(s)+\mathrm{NO}_{3}^{-}(a q) \rightarrow \mathrm{Mn}^{2+}(a q)+\mathrm{NO}_{2}(g)$
(b) $\mathrm{Mn}^{3+}(a q) \rightarrow \mathrm{MnO}_{2}(s)+\mathrm{Mn}^{2+}(a q)$
4.76 Balance the following half-reactions:
(a) (acidic) $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q) \rightarrow \mathrm{Cr}^{3+}(a q)$
(b) (basic) $\mathrm{CrO}_{4}{ }^{2-}(a q) \rightarrow \mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}(a q)$
(c) (basic) $\mathrm{Bi}^{3+}{ }^{+}$aq $) \rightarrow \mathrm{BiO}_{3}{ }^{-}($aq $)$
(d) (basic) $\mathrm{ClO}^{-}(a q) \rightarrow \mathrm{Cl}^{-}(a q)$
4.77 Balance the following half-reactions:
(a) (acidic) $\mathrm{VO}^{2+}(a q) \rightarrow \mathrm{V}^{3+}(a q)$
(b) (basic) $\mathrm{Ni}(\mathrm{OH})_{2}(s) \rightarrow \mathrm{Ni}_{2} \mathrm{O}_{3}(s)$
(c) (acidic) $\mathrm{NO}_{3}^{-}(a q) \rightarrow \mathrm{NO}_{2}(a q)$
(d) (basic) $\mathrm{Br}_{2}(\mathrm{aq}) \rightarrow \mathrm{BrO}_{3}^{-}(\mathrm{aq})$
4.78 Write balanced net ionic equations for the following reactions in basic solution:
(a) $\mathrm{MnO}_{4}^{-}(a q)+\mathrm{IO}_{3}^{-}(a q) \rightarrow \mathrm{MnO}_{2}(s)+\mathrm{IO}_{4}^{-}(a q)$
(b) $\mathrm{Cu}(\mathrm{OH})_{2}(s)+\mathrm{N}_{2} \mathrm{H}_{4}(a q) \rightarrow \mathrm{Cu}(s)+\mathrm{N}_{2}(g)$
(c) $\mathrm{Fe}(\mathrm{OH})_{2}(s)+\mathrm{CrO}_{4}{ }^{2-}(a q) \rightarrow$

$$
\mathrm{Fe}(\mathrm{OH})_{3}(s)+\mathrm{Cr}(\mathrm{OH})_{4}^{-}(a q)
$$

(d) $\mathrm{H}_{2} \mathrm{O}_{2}(a q)+\mathrm{ClO}_{4}^{-}(a q) \rightarrow \mathrm{ClO}_{2}^{-}(a q)+\mathrm{O}_{2}(g)$
4.79 Write balanced net ionic equations for the following reactions in basic solution:
(a) $\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}(a q)+\mathrm{I}_{2}(a q) \rightarrow \mathrm{S}_{4} \mathrm{O}_{6}{ }^{2-}(a q)+\mathrm{I}^{-}(a q)$
(b) $\mathrm{Mn}^{2+}(a q)+\mathrm{H}_{2} \mathrm{O}_{2}(a q) \rightarrow \mathrm{MnO}_{2}(s)+\mathrm{H}_{2} \mathrm{O}(l)$
(c) $\mathrm{Zn}(s)+\mathrm{NO}_{3}{ }^{-}(\mathrm{aq}) \rightarrow \mathrm{NH}_{3}(\mathrm{aq})+\mathrm{Zn}(\mathrm{OH})_{4}{ }^{2-}(a q)$
(d) $\mathrm{Bi}(\mathrm{OH})_{3}(s)+\mathrm{Sn}(\mathrm{OH})_{3}{ }^{-}(a q) \rightarrow$

$$
\mathrm{Bi}(s)+\mathrm{Sn}(\mathrm{OH})_{6}{ }^{2-}(a q)
$$

4.80 Write balanced net ionic equations for the following reactions in acidic solution:
(a) $\mathrm{Zn}(s)+\mathrm{VO}^{2+}(a q) \rightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{V}^{3+}(a q)$
(b) $\mathrm{Ag}(s)+\mathrm{NO}_{3}^{-}(a q) \rightarrow \mathrm{Ag}^{+}(a q)+\mathrm{NO}_{2}(g)$
(c) $\mathrm{Mg}(s)+\mathrm{VO}_{4}{ }^{3-}(a q) \rightarrow \mathrm{Mg}^{2+}(a q)+\mathrm{V}^{2+}(a q)$
(d) $\mathrm{I}^{-}(a q)+\mathrm{IO}_{3}^{-}(a q) \rightarrow \mathrm{I}_{3}^{-}(a q)$
4.81 Write balanced net ionic equations for the following reactions in acidic solution:
(a) $\mathrm{MnO}_{4}^{-}(a q)+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(a q) \rightarrow$

$$
\mathrm{Mn}^{2+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)
$$

(b) $\mathrm{H}_{2} \mathrm{O}_{2}(a q)+\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q) \rightarrow \mathrm{O}_{2}(g)+\mathrm{Cr}^{3+}(a q)$
(c) $\mathrm{Sn}^{2+}(a q)+\mathrm{IO}_{4}{ }^{-}(a q) \rightarrow \mathrm{Sn}^{4+}(a q)+\mathrm{I}^{-}(a q)$
(d) $\mathrm{PbO}_{2}(s)+\mathrm{Cl}^{-}(a q) \rightarrow \mathrm{PbCl}_{2}(s)+\mathrm{O}_{2}(g)$

## Redox Titrations

4.82 Iodine, $\mathrm{I}_{2}$, reacts with aqueous thiosulfate ion in neutral solution according to the balanced equation

$$
\mathrm{I}_{2}(a q)+2 \mathrm{~S}_{2} \mathrm{O}_{3}{ }^{2-}(a q) \longrightarrow \mathrm{S}_{4} \mathrm{O}_{6}{ }^{2-}(a q)+2 \mathrm{I}^{-}(a q)
$$

How many grams of $\mathrm{I}_{2}$ are present in a solution if 35.20 mL of $0.150 \mathrm{M} \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ solution is needed to titrate the $\mathrm{I}_{2}$ solution?
4.83 How many milliliters of $0.250 \mathrm{M} \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ solution are needed to titrate 2.486 g of $\mathrm{I}_{2}$ according to the equation in Problem 4.82?
4.84 Titration with solutions of potassium bromate, $\mathrm{KBrO}_{3}$, can be used to determine the concentration of $\mathrm{As}(\mathrm{III})$. What is the molar concentration of $\mathrm{As}(\mathrm{III})$ in a solution if 22.35 mL of $0.100 \mathrm{M} \mathrm{KBrO}_{3}$ is needed to titrate 50.00 mL of the $\mathrm{As}(\mathrm{III})$ solution? The balanced equation is

$$
3 \mathrm{H}_{3} \mathrm{AsO}_{3}(a q)+\mathrm{BrO}_{3}^{-}(a q) \longrightarrow \mathrm{Br}^{-}(a q)+3 \mathrm{H}_{3} \mathrm{AsO}_{4}(a q)
$$

4.85 Standardized solutions of $\mathrm{KBrO}_{3}$ are frequently used in redox titrations. The necessary solution can be made by dissolving $\mathrm{KBrO}_{3}$ in water and then titrating it with an $\mathrm{As}(\mathrm{III})$ solution. What is the molar concentration of a $\mathrm{KBrO}_{3}$ solution if 28.55 mL of the solution is needed to titrate 1.550 g of $\mathrm{As}_{2} \mathrm{O}_{3}$ ? See Problem 4.84 for the balanced equation $\left(\mathrm{As}_{2} \mathrm{O}_{3}\right.$ dissolves in aqueous acid solution to yield $\mathrm{H}_{3} \mathrm{AsO}_{3}: \mathrm{As}_{2} \mathrm{O}_{3}+3 \mathrm{H}_{2} \mathrm{O} \rightarrow 2 \mathrm{H}_{3} \mathrm{AsO}_{3}$ ).
4.86 The metal content of iron in ores can be determined by a redox procedure in which the sample is first oxidized with $\mathrm{Br}_{2}$ to convert all the iron to $\mathrm{Fe}^{3+}$ and then titrated with $\mathrm{Sn}^{2+}$ to reduce the $\mathrm{Fe}^{3+}$ to $\mathrm{Fe}^{2+}$. The balanced equation is

$$
2 \mathrm{Fe}^{3+}(a q)+\mathrm{Sn}^{2+}(a q) \longrightarrow 2 \mathrm{Fe}^{2+}(a q)+\mathrm{Sn}^{4+}(a q)
$$

What is the mass percent Fe in a 0.1875 g sample if 13.28 mL of a $0.1015 \mathrm{M} \mathrm{Sn}^{2+}$ solution is needed to titrate the $\mathrm{Fe}^{3+}$ ?
4.87 The $\mathrm{Sn}^{2+}$ solution used in Problem 4.86 can be standardized by titrating it with a known amount of $\mathrm{Fe}^{3+}$. What is the molar concentration of an $\mathrm{Sn}^{2+}$ solution if 23.84 mL is required to titrate 1.4855 g of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ ?
4.88 Alcohol levels in blood can be determined by a redox titration with potassium dichromate according to the balanced equation

$$
\begin{array}{r}
\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(a q)+2 \mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+16 \mathrm{H}^{+}(a q) \longrightarrow \\
2 \mathrm{CO}_{2}(g)+4 \mathrm{Cr}^{3+}(a q)+11 \mathrm{H}_{2} \mathrm{O}(l)
\end{array}
$$

What is the blood alcohol level in mass percent if 8.76 mL of $0.04988 \mathrm{M} \mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ is required for titration of a 10.002 g sample of blood?
4.89 Calcium levels in blood can be determined by adding oxalate ion to precipitate calcium oxalate, $\mathrm{CaC}_{2} \mathrm{O}_{4}$, followed by dissolving the precipitate in aqueous acid and titrating the resulting oxalic acid $\left(\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$ with $\mathrm{KMnO}_{4}$ :

$$
\begin{aligned}
5 \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}(a q)+ & 2 \mathrm{MnO}_{4}^{-}(a q)+6 \mathrm{H}^{+}(a q) \longrightarrow \\
& 10 \mathrm{CO}_{2}(g)+2 \mathrm{Mn}^{2+}(a q)+8 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

How many milligrams of $\mathrm{Ca}^{2+}$ are present in 10.0 mL of blood if 21.08 mL of $0.000988 \mathrm{M} \mathrm{KMnO}_{4}$ solution is needed for the titration?

## General Problems

4.90 Balance the equations for the following reactions in basic solution:
(a) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}(a q)+\mathrm{N}_{2} \mathrm{H}_{4}(a q) \rightarrow$

$$
\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4-}(a q)+\mathrm{N}_{2}(g)
$$

(b) $\mathrm{SeO}_{3}{ }^{2-}(a q)+\mathrm{Cl}_{2}(g) \rightarrow \mathrm{SeO}_{4}{ }^{2-}(a q)+\mathrm{Cl}^{-}(a q)$
(c) $\mathrm{CoCl}_{2}(a q)+\mathrm{HO}_{2}^{-}(a q) \rightarrow$

$$
\mathrm{Co}(\mathrm{OH})_{3}(a q)+\mathrm{Cl}^{-}(a q)
$$

4.91 An alternative procedure to that given in Problem 4.86 for determining the amount of iron in a sample is to convert the iron to $\mathrm{Fe}^{2+}$ and then titrate with a solution of $\mathrm{Ce}\left(\mathrm{NH}_{4}\right)_{2}\left(\mathrm{NO}_{3}\right)_{6}$ :

$$
\mathrm{Fe}^{2+}(a q)+\mathrm{Ce}^{4+}(a q) \longrightarrow \mathrm{Fe}^{3+}(a q)+\mathrm{Ce}^{3+}(a q)
$$

What is the mass percentage of iron in a sample if titration of 1.2284 g of the sample requires 57.91 mL of $0.1018 \mathrm{M} \mathrm{Ce}\left(\mathrm{NH}_{4}\right)_{2}\left(\mathrm{NO}_{3}\right)_{6}$ ?
4.92 Assign oxidation numbers to each atom in the following substances:
(a) Ethane, $\mathrm{C}_{2} \mathrm{H}_{6}$, a constituent of natural gas
(b) Borax, $\mathrm{Na}_{2} \mathrm{~B}_{4} \mathrm{O}_{7}$, a mineral used in laundry detergents
(c) $\mathrm{Mg}_{2} \mathrm{Si}_{2} \mathrm{O}_{6}$, a silicate mineral
4.93 Balance the equations for the following reactions in acidic solution:
(a) $\mathrm{PbO}_{2}(s)+\mathrm{Mn}^{2+}(a q) \rightarrow \mathrm{Pb}^{2+}(a q)+\mathrm{MnO}_{4}^{-}(a q)$
(b) $\mathrm{As}_{2} \mathrm{O}_{3}(s)+\mathrm{NO}_{3}^{-}(a q) \rightarrow$

$$
\mathrm{H}_{3} \mathrm{AsO}_{4}(a q)+\mathrm{HNO}_{2}(a q)
$$

(c) $\mathrm{Br}_{2}(a q)+\mathrm{SO}_{2}(g) \rightarrow \mathrm{Br}^{-}(a q)+\mathrm{HSO}_{4}^{-}(a q)$
(d) $\mathrm{NO}_{2}^{-}(a q)+\mathrm{I}^{-}(a q) \rightarrow \mathrm{I}_{2}(s)+\mathrm{NO}(g)$
4.94 (a) Use the following reactions to arrange the elements A, B, C, and D in order of their decreasing ability as reducing agents:
$\mathrm{C}+\mathrm{B}^{+} \longrightarrow \mathrm{C}^{+}+\mathrm{B} \quad \mathrm{A}^{+}+\mathrm{D} \longrightarrow$ No reaction
$\mathrm{C}^{+}+\mathrm{A} \longrightarrow$ No reaction $\mathrm{D}+\mathrm{B}^{+} \longrightarrow \mathrm{D}^{+}+\mathrm{B}$
(b) Which of the following reactions would you expect to occur according to the activity series you established in part (a)?
(1) $\mathrm{A}^{+}+\mathrm{C} \longrightarrow \mathrm{A}+\mathrm{C}^{+}$
(2) $\mathrm{A}^{+}+\mathrm{B} \longrightarrow \mathrm{A}+\mathrm{B}^{+}$
4.95 The solubility of an ionic compound can be described quantitatively by a value called the solubility product constant, $K_{\text {sp }}$. For the general solubility process $\mathrm{A}_{a} \mathrm{~B}_{b} \rightleftharpoons a \mathrm{~A}^{n+}+b \mathrm{~B}^{m-}, K_{\mathrm{sp}}=\left[\mathrm{A}^{n+}\right]^{a}\left[\mathrm{~B}^{m-}\right]^{b}$. The brackets refer to concentrations in moles per liter.
(a) Write the expression for the solubility product constant of $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$.
(b) If $K_{\text {sp }}=1.1 \times 10^{-12}$ for $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$, what are the molar concentrations of $\mathrm{Ag}^{+}$and $\mathrm{CrO}_{4}{ }^{2-}$ in a saturated solution?
4.96 Write the expression for the solubility product constant of $\mathrm{MgF}_{2}$ (see Problem 4.95). If $\left[\mathrm{Mg}^{2+}\right]=2.6 \times 10^{-4} \mathrm{~mol} / \mathrm{L}$ in a saturated solution, what is the value of $K_{\mathrm{sp}}$ ?
4.97 Succinic acid, an intermediate in the metabolism of food molecules, has molecular mass $=118.1 \mathrm{amu}$. When 1.926 g of succinic acid was dissolved in water and titrated, 65.20 mL of 0.5000 M NaOH solution was required to neutralize the acid. How many acidic hydrogens are there in a molecule of succinic acid?
4.98 How could you use a precipitation reaction to separate each of the following pairs of cations? Write the formula for each reactant you would add, and write a balanced net ionic equation for each reaction.
(a) $\mathrm{K}^{+}$and $\mathrm{Hg}_{2}{ }^{2+}$
(b) $\mathrm{Pb}^{2+}$ and $\mathrm{Ni}^{2+}$
(c) $\mathrm{Ca}^{2+}$ and $\mathrm{NH}_{4}{ }^{+}$
(d) $\mathrm{Fe}^{2+}$ and $\mathrm{Ba}^{2+}$
4.99 How could you use a precipitation reaction to separate each of the following pairs of anions? Write the formula for each reactant you would add, and write a balanced net ionic equation for each reaction.
(a) $\mathrm{Cl}^{-}$and $\mathrm{NO}_{3}^{-}$
(b) $\mathrm{S}^{2-}$ and $\mathrm{SO}_{4}{ }^{2-}$
(c) $\mathrm{SO}_{4}{ }^{2-}$ and $\mathrm{CO}_{3}{ }^{2-}$
(d) $\mathrm{OH}^{-}$and $\mathrm{ClO}_{4}^{-}$
4.100 Write a balanced net ionic equation for each of the following reactions in either acidic or basic solution:
(a) $\mathrm{Mn}(\mathrm{OH})_{2}(s)+\mathrm{H}_{2} \mathrm{O}_{2}(a q) \xrightarrow{\text { Base }} \mathrm{Mn}(\mathrm{OH})_{3}(s)$
(b) $\mathrm{MnO}_{4}{ }^{2-}(a q) \xrightarrow{\text { Acid }} \mathrm{MnO}_{2}(s)+\mathrm{MnO}_{4}^{-}(a q)$
(c) $\mathrm{IO}_{3}^{-}(a q)+\mathrm{I}^{-}(a q) \xrightarrow{\text { Acid }} \mathrm{I}_{3}{ }^{-}(a q)$
(d) $\mathrm{P}(s)+\mathrm{PO}_{4}^{3-}(a q) \xrightarrow{\text { Base }} \mathrm{HPO}_{3}{ }^{2-}(a q)$
4.101 A 100.0 mL solution containing aqueous HCl and HBr was titrated with 0.1235 M NaOH . The volume of base required to neutralize the acid was 47.14 mL . Aqueous $\mathrm{AgNO}_{3}$ was then added to precipitate the $\mathrm{Cl}^{-}$and $\mathrm{Br}^{-}$ ions as AgCl and AgBr . The mass of the silver halides obtained was 0.9974 g . What are the molarities of the HCl and HBr in the original solution?
4.102 Write balanced net ionic equations for the following reactions in acidic solution:
(a) $\mathrm{S}_{4} \mathrm{O}_{6}{ }^{2-}(a q)+\mathrm{Al}(s) \rightarrow \mathrm{H}_{2} \mathrm{~S}(a q)+\mathrm{Al}^{3+}(a q)$
(b) $\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}(a q)+\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q) \rightarrow$

$$
\mathrm{S}_{4} \mathrm{O}_{6}{ }^{2-}(a q)+\mathrm{Cr}^{3+}(a q)
$$

(c) $\mathrm{ClO}_{3}^{-}(a q)+\mathrm{As}_{2} \mathrm{~S}_{3}(s) \rightarrow$

$$
\mathrm{Cl}^{-}(a q)+\mathrm{H}_{2} \mathrm{AsO}_{4}^{-}(a q)+\mathrm{HSO}_{4}^{-}(a q)
$$

(d) $\mathrm{IO}_{3}^{-}(a q)+\operatorname{Re}(s) \rightarrow \mathrm{ReO}_{4}^{-}(a q)+\mathrm{I}^{-}(a q)$
(e) $\mathrm{HSO}_{4}^{-}(a q)+\mathrm{As}_{4}(s)+\mathrm{Pb}_{3} \mathrm{O}_{4}(s) \rightarrow$

$$
\mathrm{PbSO}_{4}(s)+\mathrm{H}_{2} \mathrm{AsO}_{4}^{-}(a q)
$$

(f) $\mathrm{HNO}_{2}(a q) \rightarrow \mathrm{NO}_{3}^{-}(a q)+\mathrm{NO}(g)$
4.103 Write balanced net ionic equations for the following reactions in basic solution:
(a) $\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{O}_{6}{ }^{2-}(a q)+\mathrm{ClO}_{3}{ }^{-}(a q) \rightarrow$

$$
\mathrm{CO}_{3}^{2-}(a q)+\mathrm{Cl}^{-}(a q)
$$

(b) $\mathrm{Al}(s)+\mathrm{BiONO}_{3}(s) \rightarrow$

$$
\mathrm{Bi}(s)+\mathrm{NH}_{3}(a q)+\mathrm{Al}(\mathrm{OH})_{4}^{-}(a q)
$$

(c) $\mathrm{H}_{2} \mathrm{O}_{2}(a q)+\mathrm{Cl}_{2} \mathrm{O}_{7}(a q) \rightarrow \mathrm{ClO}_{2}^{-}(a q)+\mathrm{O}_{2}(g)$
(d) $\mathrm{Tl}_{2} \mathrm{O}_{3}(s)+\mathrm{NH}_{2} \mathrm{OH}(a q) \rightarrow \mathrm{TlOH}(s)+\mathrm{N}_{2}(g)$
(e) $\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}(a q)+\mathrm{S}_{2} \mathrm{O}_{4}{ }^{2-}(a q) \rightarrow$

$$
\mathrm{SO}_{3}{ }^{2-}(a q)+\mathrm{Cu}(s)+\mathrm{NH}_{3}(a q)
$$

(f) $\mathrm{Mn}(\mathrm{OH})_{2}(s)+\mathrm{MnO}_{4}^{-}(a q) \rightarrow \mathrm{MnO}_{2}(s)$
4.104 A mixture of CuO and $\mathrm{Cu}_{2} \mathrm{O}$ with a mass of 10.50 g is reduced to give 8.66 g of pure Cu metal. What are the amounts (in grams) of CuO and $\mathrm{Cu}_{2} \mathrm{O}$ in the original mixture?
4.105 When 75.0 mL of a 0.100 M lead(II) nitrate solution is mixed with 100.0 mL of a 0.190 M potassium iodide solution, a yellow-orange precipitate of lead(II) iodide is formed.
(a) What mass (in grams) of lead(II) iodide is formed, assuming the reaction goes to completion?
(b) What is the molarity of each of the ions $\mathrm{Pb}^{2+}$, $\mathrm{K}^{+}, \mathrm{NO}_{3}^{-}$, and $\mathrm{I}^{-}$in the resulting solution?

## Multi-Concept Problems

4.106 Assume that you dissolve 10.0 g of a mixture of NaOH and $\mathrm{Ba}(\mathrm{OH})_{2}$ in 250.0 mL of water and titrate with 1.50 M hydrochloric acid. The titration is complete after 108.9 mL of the acid has been added. What is the mass (in grams) of each substance in the mixture?
4.107 The following three solutions are mixed: 100.0 mL of $0.100 \mathrm{M} \mathrm{Na}_{2} \mathrm{SO}_{4}, 50.0 \mathrm{~mL}$ of $0.300 \mathrm{M} \mathrm{ZnCl}_{2}$, and 100.0 mL of $0.200 \mathrm{M} \mathrm{Ba}(\mathrm{CN})_{2}$.
(a) What ionic compounds will precipitate out of solution?
(b) What is the molarity of each ion remaining in the solution, assuming complete precipitation of all insoluble compounds?
4.108 A 250.0 g sample of a white solid is known to be a mixture of $\mathrm{KNO}_{3}, \mathrm{BaCl}_{2}$, and NaCl . When 100.0 g of this mixture is dissolved in water and allowed to react with excess $\mathrm{H}_{2} \mathrm{SO}_{4}, 67.3 \mathrm{~g}$ of a white precipitate is collected. When the remaining 150.0 g of the mixture is dissolved in water and allowed to react with excess $\mathrm{AgNO}_{3}, 197.6 \mathrm{~g}$ of a second precipitate is collected.
(a) What are the formulas of the two precipitates?
(b) What is the mass of each substance in the original 250 g mixture?
4.109 Four solutions are prepared and mixed together in the following order:
(1) Start with 100.0 mL of $0.100 \mathrm{M} \mathrm{BaCl}_{2}$
(2) Add 50.0 mL of $0.100 \mathrm{M} \mathrm{AgNO}_{3}$
(3) Add 50.0 mL of $0.100 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$
(4) Add 250.0 mL of $0.100 \mathrm{M} \mathrm{NH}_{3}$

Write an equation for any reaction that occurs after each step, and calculate the concentrations of $\mathrm{Ba}^{2+}, \mathrm{Cl}^{-}, \mathrm{NO}_{3}{ }^{-}, \mathrm{NH}_{3}$, and $\mathrm{NH}_{4}{ }^{+}$in the final solution, assuming that all reactions go to completion.
4.110 To 100.0 mL of a solution that contains 0.120 M $\mathrm{Cr}\left(\mathrm{NO}_{3}\right)_{2}$ and $0.500 \mathrm{M} \mathrm{HNO}_{3}$ is added 20.0 mL of 0.250 $\mathrm{M} \mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$. The dichromate and chromium(II) ions react to give chromium(III) ions.
(a) Write a balanced net ionic equation for the reaction.
(b) Calculate the concentrations of all ions in the solution after reaction. Check your concentrations to make sure that the solution is electrically neutral.
4.111 Sodium nitrite, $\mathrm{NaNO}_{2}$, is frequently added to processed meats as a preservative. The amount of nitrite ion in a sample can be determined by acidifying to form nitrous acid $\left(\mathrm{HNO}_{2}\right)$, letting the nitrous acid react with an excess of iodide ion, and then titrating the
$\mathrm{I}_{3}{ }^{-}$ion that results with thiosulfate solution in the presence of a starch indicator. The unbalanced equations are
(1) $\mathrm{HNO}_{2}+\mathrm{I}^{-} \longrightarrow \mathrm{NO}+\mathrm{I}_{3}^{-}$(in acidic solution)
(2) $\mathrm{I}_{3}{ }^{-}+\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-} \longrightarrow \mathrm{I}^{-}+\mathrm{S}_{4} \mathrm{O}_{6}{ }^{2-}$
(a) Balance the two redox equations.
(b) When a nitrite-containing sample with a mass of 2.935 g was analyzed, 18.77 mL of 0.1500 M $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ solution was needed for the titration. What is the mass percentage of $\mathrm{NO}_{2}{ }^{-}$ion in the sample?
4.112 Brass is an approximately $4: 1$ alloy of copper and zinc, along with small amounts of tin, lead, and iron. The mass percents of copper and zinc can be determined by a procedure that begins with dissolving the brass in hot nitric acid. The resulting solution of $\mathrm{Cu}^{2+}$ and $\mathrm{Zn}^{2+}$ ions is then treated with aqueous ammonia to lower its acidity, followed by addition of sodium thiocyanate ( NaSCN ) and sulfurous acid $\left(\mathrm{H}_{2} \mathrm{SO}_{3}\right)$ to precipitate copper(I) thiocyanate (CuSCN). The solid CuSCN is collected, dissolved in aqueous acid, and treated with potassium iodate $\left(\mathrm{KIO}_{3}\right)$ to give iodine, which is then titrated with aqueous sodium thiosulfate $\left(\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}\right)$. The filtrate remaining after CuSCN has been removed is neutralized by addition of aqueous ammonia, and a solution of diammonium hydrogen phosphate $\left[\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}\right]$ is added to yield a precipitate of zinc ammonium phosphate $\left(\mathrm{ZnNH}_{4} \mathrm{PO}_{4}\right)$. Heating the precipitate to $900^{\circ} \mathrm{C}$ converts it to zinc pyrophosphate $\left(\mathrm{Zn}_{2} \mathrm{P}_{2} \mathrm{O}_{7}\right)$, which is weighed. The equations are
(1) $\mathrm{Cu}(s)+\mathrm{NO}_{3}^{-}(a q) \rightarrow \mathrm{Cu}^{2+}(a q)+\mathrm{NO}(g) \quad$ (in acid)
(2) $\mathrm{Cu}^{2+}(a q)+\mathrm{SCN}^{-}(a q)+\mathrm{HSO}_{3}{ }^{-}(a q) \rightarrow$

$$
\mathrm{CuSCN}(s)+\mathrm{HSO}_{4}^{-}(a q) \quad \text { (in acid) }
$$

(3) $\mathrm{Cu}^{+}(a q)+\mathrm{IO}_{3}{ }^{-}(a q) \rightarrow \mathrm{Cu}^{2+}(a q)+\mathrm{I}_{2}(a q) \quad$ (in acid)
(4) $\mathrm{I}_{2}(a q)+\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}(a q) \rightarrow \mathrm{I}^{-}(a q)+\mathrm{S}_{4} \mathrm{O}_{6}{ }^{2-}(a q) \quad$ (in acid)
(5) $\mathrm{ZnNH}_{4} \mathrm{PO}_{4} \rightarrow \mathrm{Zn}_{2} \mathrm{P}_{2} \mathrm{O}_{7}+\mathrm{H}_{2} \mathrm{O}+\mathrm{NH}_{3}$
(a) Balance all equations.
(b) When a brass sample with a mass of 0.544 g was subjected to the above analysis, 10.82 mL of 0.1220 M sodium thiosulfate was required for the iodine titration. What is the mass percent copper in the brass?
(c) The brass sample in (b) yielded 0.246 g of $\mathrm{Zn}_{2} \mathrm{P}_{2} \mathrm{O}_{7}$. What is the mass percent zinc in the brass?
4.113 A certain metal sulfide, $\mathrm{MS}_{n}$ (where $n$ is a small integer), is widely used as a high-temperature lubricant. The substance is prepared by reaction of the metal pentachloride $\left(\mathrm{MCl}_{5}\right)$ with sodium sulfide $\left(\mathrm{Na}_{2} \mathrm{~S}\right)$. Heating the metal sulfide to $700^{\circ} \mathrm{C}$ in air gives the metal trioxide $\left(\mathrm{MO}_{3}\right)$ and sulfur dioxide $\left(\mathrm{SO}_{2}\right)$, which reacts with $\mathrm{Fe}^{3+}$ ion under aqueous acidic conditions to give sulfate ion $\left(\mathrm{SO}_{4}{ }^{2-}\right)$. Addition of aqueous $\mathrm{BaCl}_{2}$ then forms a precipitate of $\mathrm{BaSO}_{4}$. The unbalanced equations are:
(1) $\mathrm{MCl}_{5}(s)+\mathrm{Na}_{2} \mathrm{~S}(s) \longrightarrow \mathrm{MS}_{n}(s)+\mathrm{S}(l)+\mathrm{NaCl}(s)$
(2) $\mathrm{MS}_{n}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{MO}_{3}(s)+\mathrm{SO}_{2}(g)$
(3) $\mathrm{SO}_{2}(g)+\mathrm{Fe}^{3+}(a q) \longrightarrow$

$$
\mathrm{Fe}^{2+}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q) \quad \text { (in acid) }
$$

(4) $\mathrm{SO}_{4}{ }^{2-}(a q)+\mathrm{Ba}^{2+}(a q) \longrightarrow \mathrm{BaSO}_{4}(s)$

Assume that you begin with 4.61 g of $\mathrm{MCl}_{5}$ and that reaction (1) proceeds in $91.3 \%$ yield. After oxidation of the $\mathrm{MS}_{n}$ product, oxidation of $\mathrm{SO}_{2}$, and precipitation of sulfate ion, 7.19 g of $\mathrm{BaSO}_{4}(s)$ is obtained.
(a) How many moles of sulfur are present in the $\mathrm{MS}_{n}$ sample?
(b) Assuming several possible values for $n$ ( $n=$ $1,2,3 \ldots$ ), what is the atomic mass of M in each case?
(c) What is the likely identity of the metal $M$, and what is the formula of the metal sulfide $\mathrm{MS}_{n}$ ?
(d) Balance all equations.

## eMedia Problems

4.114 After watching the Strong and Weak Electrolytes movie (eChapter 4.2), draw two pictures (similar to those in Key Concept Problem 4.3, page 119) to represent the two solutions in the movie. Use different colored spheres to represent the hydronium, chloride, and acetate ions.
4.115 After working through the Net Ionic Equation activity (eChapter 4.3), explain the difference between the equations in each step of the process.
4.116 Use the Ionic Compounds activity (eChapter 4.4) to determine the formula of each of the insoluble iron(III) salts. Then, using your knowledge of the solubility rules, write a molecular, ionic, and net ionic equation for an aqueous reaction that would produce each salt.
4.117 Together, the Oxidation-Reduction Reactions-Part I and Oxidation-Reduction Reactions-Part II movies (eChapters 4.6 and 4.7) show three different reactions in which zinc metal is oxidized.
(a) Write the molecular, ionic, and net ionic equation corresponding to each of the three reactions.
(b) Explain how the products of the three reactions are different.
(c) Explain how they are the same.
4.118 Choose one of the reactions in the Precipitation, Redox, and Neutralization Reactions activity in eChapter 4.8, and draw the pictures used to represent it. Eliminate the spectator ions by crossing them out of the picture, and then write the net ionic equation. Draw similar pictures for the reaction $\mathrm{NaCl}(a q)+\mathrm{NH}_{4} \mathrm{NO}_{3}(a q) \rightarrow$ $\mathrm{NaNO}_{3}(a q)+\mathrm{NH}_{4} \mathrm{Cl}(a q)$, and eliminate the spectator ions. What does this indicate about the reaction?

## Chapter

## Periodicity and Atomic Structure

## The periodic table is the most important organizing principle in

 chemistry. If you know the properties of any one element in a group, or column, of the periodic table, you can make a good guess at the properties of every other element in the same group and even the elements in neighboring groups.To see why it's called the periodic table, look at the graph of atomic radius versus atomic number in

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Periodicity-the presence of regularly repeating patterns- is found throughout nature.

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FIGURE 5.1 A graph of atomic radius in picometers ( pm ) versus atomic number shows a rise-and-fall pattern of periodicity. The maxima occur for atoms of group 1A elements ( $\mathrm{Li}, \mathrm{Na}, \mathrm{K}, \mathrm{Rb}, \mathrm{Cs}, \mathrm{Fr}$ ); the minima occur for atoms of the group 7A elements. Accurate data are not available for the group 8A elements.


Interactive Periodic Table

FIGURE 5.2 A portion of Mendeleev's periodic table, giving the atomic masses known at the time and showing some of the "holes" representing unknown elements. There is an unknown element (which turned out to be gallium, Ga ) beneath aluminum (Al) and another one (which turned out to be germanium, $\mathrm{Ge})$ beneath silicon $(\mathrm{Si})$.

Figure 5.1. The graph shows a periodic rise-and-fall pattern. Beginning on the left with atomic number 1 (hydrogen), the size of the atoms increases to a maximum at atomic number 3 (lithium), then decreases to a minimum, then increases again to a maximum at atomic number 11 (sodium), then decreases, and so on. It turns out that all the maxima occur for atoms of group 1A elements- Li (atomic number, $Z=3), \mathrm{Na}(Z=11), \mathrm{K}(Z=19), \mathrm{Rb}(Z=37), \mathrm{Cs}(Z=55)$, and $\operatorname{Fr}(Z=87)$-and that the minima occur for atoms of the group 7A elements.


There's nothing unique about the periodicity of atomic radii shown in Figure 5.1. Any of several dozen other physical or chemical properties can be plotted in a similar way with similar results. We'll look at several examples of such periodicity in this chapter and the next.

## 5.1| Development of the Periodic Table

In many ways, the creation of the periodic table by Dmitri Mendeleev in 1869 is an ideal example of how a scientific theory develops. At first there is only random information-a large number of elements and many observations about their properties and behavior. As more and more facts become known, people try to organize the data in ways that make sense, until ultimately a consistent hypothesis emerges.

Any good hypothesis must do two things: It must explain known facts, and it must make predictions about phenomena yet unknown. If the predictions are tested and found true, then the hypothesis is a good one and will stand until additional facts require that it be modified or discarded. Mendeleev's hypothesis about how known chemical information could be organized passed all tests. Not only did the periodic table arrange data in a useful and consistent way to explain known facts about chemical reactivity, it also led to several remarkable predictions that were later found to be accurate.

Taking the chemistry of the elements as his primary organizing principle, Mendeleev arranged the known elements by atomic mass and grouped them together according to their chemical reactivity. On so doing, he realized that there were several "holes" in the table, some of which are shown in Figure 5.2. The

chemical behavior of aluminum (atomic mass $\approx 27.3$ ) is similar to that of boron (atomic mass $\approx 11$ ), but there was no element known at the time that fit into the slot below aluminum. In the same way, silicon (atomic mass $\approx 28$ ) is similar in many respects to carbon (atomic mass $\approx 12$ ), but there was no element known that fit below silicon.

Looking at the holes in the table, Mendeleev predicted that two then-unknown elements existed and might be found at some future time. Furthermore, he predicted with remarkable accuracy what the properties of these unknown elements would be. The element immediately below aluminum, which he called ekaaluminum from a Sanskrit word meaning "first," would have an atomic mass near 68, would have a low melting point, and would react with chlorine to form a trichloride $\mathrm{XCl}_{3}$. Gallium, discovered in 1875, has exactly these predicted properties. The element below silicon, which Mendeleev called eka-silicon, would have an atomic mass near 72 , would be dark gray in color, and would form an oxide with the formula $\mathrm{XO}_{2}$. Germanium, discovered in 1886, fits the description perfectly (Table 5.1).
tABLE 5.1 A Comparison of Predicted and Observed Properties for Gallium (eka-Aluminum) and Germanium (eka-Silicon)

|  |  | Mendeleev's <br> Prediction | Observed <br> Property |
| :--- | :--- | :--- | :--- |
|  | Atomic mass | 68 amu | 69.72 amu |
| Gallium |  |  |  |
| (eka-Aluminum) | Density | $5.9 \mathrm{~g} / \mathrm{cm}$ | $5.91 \mathrm{~g} / \mathrm{cm}^{3}$ |
|  | Melting point | Low | $29.8^{\circ} \mathrm{C}$ |
|  | Formula of oxide | $\mathrm{X}_{2} \mathrm{O}_{3}$ | $\mathrm{Ga}_{2} \mathrm{O}_{3}$ |
|  | Formula of chloride | $\mathrm{XCl}_{3}$ | $\mathrm{GaCl}_{3}$ |
|  | Atomic mass | 72 amu | 72.61 amu |
| Germanium |  |  |  |
| (eka-Silicon) | Density | $5.5 \mathrm{~g} / \mathrm{cm}^{3}$ | $5.35 \mathrm{~g} / \mathrm{cm}^{3}$ |
|  | Color | $\mathrm{Dark} \mathrm{gray}^{\mathrm{XO}_{2}}$ | Light gray |
|  | Formula of oxide | $\mathrm{GeO}_{2}$ |  |
|  | Formula of chloride | $\mathrm{XCl}_{4}$ | $\mathrm{GeCl}_{4}$ |
|  |  |  |  |



The success of these and other predictions convinced chemists of the usefulness of Mendeleev's periodic table and led to its wide acceptance. Even Mendeleev made some mistakes, though. He was completely unaware of the existence of the group 8A elements- $\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}, \mathrm{Kr}, \mathrm{Xe}$, and Rn -because none were known at the time. All are colorless, odorless gases with little or no chemical reactivity, and none were discovered until 1894, when argon was first isolated.

Gallium (left) is a shiny, low-melting metal; germanium (right) is a hard, gray semimetal.

0Radiation refers to any form of energy that travels in all directions from a single source, such as light from the sun.

FIGURE 5.3 The electromagnetic spectrum consists of a continuous range of wavelengths and frequencies, from radio waves at the lowfrequency end to gamma rays at the high-frequency end. The familiar visible region accounts for only a small portion near the middle of the spectrum. Note that waves in the X-ray region have a length that is approximately the same as the diameter of an atom $\left(10^{-10} \mathrm{~m}\right)$.


$\square$Many students associate radiation only with nuclear decay processes and their negative connotations. This form of radiation represents only a small segment of the electromagnetic radiation spectrum.

0Wavelength can be related to colors of the spectrum ranging from 400 nm (violet) to 700 nm (red) using the acronym ROY G BIV (Red, Orange, Yellow, Green, Blue, Indigo, Violet).

vStudents best relate some wave properties to radio waves: the frequency of a favorite radio station and loudness (amplitude).

## $5.2 \mid$ Light and the Electromagnetic Spectrum

What fundamental property of atoms is responsible for the periodic variations we observe in atomic radii and in so many other characteristics of the elements? This question occupied the thoughts of chemists for more than 50 years after Mendeleev, and it was not until well into the 1920s that the answer was established. To understand how the answer slowly emerged, it's necessary to look first at the nature of visible light and other forms of radiant energy. Historically, studies of the interaction of radiant energy with matter have provided immense insight into atomic and molecular structure.

Although they appear quite different to our senses, visible light, infrared radiation, microwaves, radio waves, $X$ rays, and other forms of radiant energy are all different kinds of electromagnetic radiation. Collectively, they make up the electromagnetic spectrum, shown in Figure 5.3.


Electromagnetic radiation traveling through a vacuum behaves in some ways like ocean waves traveling through water. Like ocean waves, electromagnetic radiation is characterized by a frequency, a wavelength, and an amplitude. If you could stand in one place and look at a sideways, cutaway view of an ocean wave moving through the water, you would see a regular rise-and-fall pattern (Figure 5.4). The frequency ( $\nu$, Greek nu) of a wave is simply the number of wave peaks that pass by a given point per unit time, usually expressed in units of reciprocal seconds $\left(1 / \mathrm{s}\right.$ or $\left.^{-1}\right)$, or hertz $\left(\mathbf{H z} ; 1 \mathrm{~Hz}=1 \mathrm{~s}^{-1}\right)$. The wavelength ( $\boldsymbol{\lambda}$, Greek lambda) of the wave is the distance from one wave peak to the next, and the amplitude of the

Like electromagnetic waves, ocean waves are characterized by a wavelength, a frequency, and an amplitude.


(b)
wave is the height, measured from the center line between peak and trough. Physically, what we perceive as the intensity of radiant energy is proportional to the square of the wave amplitude. A very feeble beam and a blinding glare of light may have the same wavelength and frequency, but they will differ greatly in amplitude.

Multiplying the wavelength of a wave in meters ( $\mathrm{m} \mathrm{)} \mathrm{by} \mathrm{its} \mathrm{frequency} \mathrm{in} \mathrm{recip-}$ rocal seconds $\left(\mathrm{s}^{-1}\right)$ gives the speed of the wave in meters per second ( $\mathrm{m} / \mathrm{s}$ ). The rate of travel of all electromagnetic radiation in a vacuum is a constant value, commonly called the speed of light and abbreviated $c$. It's numerical value is defined as exactly $2.99792458 \times 10^{8} \mathrm{~m} / \mathrm{s}$, usually rounded off to $3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}$ :

$$
\begin{aligned}
& \text { Wavelength } \times \text { Frequency }=\text { Speed } \\
& \quad \lambda(\mathrm{m}) \times \nu\left(\mathrm{s}^{-1}\right)=c(\mathrm{~m} / \mathrm{s})
\end{aligned}
$$

which can be rewritten as:

$$
\lambda=\frac{c}{\nu} \quad \text { or } \quad \nu=\frac{c}{\lambda}
$$

This equation says that frequency and wavelength are inversely related: Electromagnetic radiation with a long wavelength has a low frequency, and radiation with a short wavelength has a high frequency.

## Worked Example 5.1

The light blue glow given off by mercury streetlamps has a wavelength of 436 nm . What is its frequency in hertz?

## Strategy

We are given a wavelength and need to find the corresponding frequency. Wavelength and frequency are inversely related by the equation $\lambda \nu=c$, which can be solved for $\nu$. Don't forget to convert from nanometers to meters.

## Solution

$$
\begin{aligned}
\nu=\frac{c}{\lambda} & =\frac{\left(3.00 \times 10^{8} \frac{\mathrm{~K}}{\mathrm{~s}}\right)\left(\frac{10^{9} \mathrm{ntI}}{\mathrm{gK}}\right)}{436 \mathrm{~mm}} \\
& =6.88 \times 10^{14} \mathrm{~s}^{-1}=6.88 \times 10^{14} \mathrm{~Hz}
\end{aligned}
$$

The frequency of the light is $6.88 \times 10^{14} \mathrm{~s}^{-1}$, or $6.88 \times 10^{14} \mathrm{~Hz}$.

4 FIGURE 5.4
Electromagnetic waves are characterized by a wavelength, a frequency, and an amplitude. (a) Wavelength $(\lambda)$ is the distance between two successive wave peaks, and frequency $(\nu)$ is the number of wave peaks that pass a fixed point per unit time. Amplitude is the height of the maximum measured from the center line. (b) What we perceive as different kinds of electromagnetic radiation are simply waves with different wavelengths and frequencies.

FIGURE 5.5 (a) When a narrow beam of ordinary white light is passed through a glass prism, different wavelengths travel through the glass at different rates and appear as different colors. A similar effect occurs when light passes through water droplets in the air, forming a rainbow, or (b) through ice crystals in clouds, causing an unusual weather phenomenon called a sundog.

[^7]- PROBLEM 5.1 What is the frequency of a gamma ray with $\lambda=3.56 \times 10^{-11} \mathrm{~m}$ ? Of a radar wave with $\lambda=10.3 \mathrm{~cm}$ ?

PROBLEM 5.2 What is the wavelength (in meters) of an FM radio wave with frequency $\nu=102.5 \mathrm{MHz}$ ? Of a medical X ray with $\nu=9.55 \times 10^{17} \mathrm{~Hz}$ ?
-KEY CONCEPT PROBLEM 5.3 Two electromagnetic waves are represented below.
(a) Which wave has the higher frequency?
(b) Which wave represents a more intense beam of light?
(c) Which wave represents blue light, and which represents red light?

(a)

(b)

### 5.3 Electromagnetic Radiation and Atomic Spectra

The light that we see from the sun or from a typical lightbulb is "white" light, meaning that it consists of an essentially continuous distribution of all possible wavelengths spanning the entire visible region of the electromagnetic spectrum. When a narrow beam of white light is passed through a glass prism, the different wavelengths travel through the glass at different rates. As a result, the white light is separated into its component colors, ranging from red at the long-wavelength end of the spectrum ( 700 nm ) to violet at the short-wavelength end ( 400 nm ) (Figure 5.5a). This separation into colors is similar to what occurs when light travels through water droplets in the air, forming a rainbow.


What do visible light and other kinds of electromagnetic radiation have to do with atomic structure? It turns out that atoms give off light when heated or otherwise excited energetically, thereby providing a clue to their atomic makeup. Unlike the white light from the sun, though, the light given off by an energetically excited atom is not a continuous distribution of all possible wavelengths. When passed first through a narrow slit and then through a prism, the light emitted by an excited atom is found to consist of only a few wavelengths rather than a full rainbow of colors, giving a series of discrete lines separated by blank areas-a line spectrum. Excited sodium atoms, produced by heating NaCl or some other
sodium salt in the flame of a Bunsen burner, give off yellow light (Figure 5.6a); hydrogen atoms give off a bluish light made of several different colors (Figure 5.6b); and so on. In fact, the brilliant colors of fireworks are produced by mixtures of metal atoms that have been heated by explosive powder.


Soon after the discovery that energetic atoms emit light of specific wavelengths, chemists began cataloging the line spectra of various elements. They rapidly found that each element has its own unique spectral "signature," and they began using the results to identify the elements present in minerals and other substances. Not until the work of the Swiss schoolteacher Johann Balmer in 1885, though, was a pattern discovered in atomic line spectra. It was known at the time that hydrogen produced a spectrum with four lines, as shown in Figure 5.6b. The wavelengths of the four lines are 656.3 nm (red), 486.1 nm (blue-green), 434.0 nm (blue), and 410.1 nm (indigo).

Thinking about the hydrogen spectrum and trying by trial-and-error to organize the data in various ways, Balmer discovered that the wavelengths of the four lines in the hydrogen spectrum can be expressed by the equation

$$
\frac{1}{\lambda}=R\left(\frac{1}{2^{2}}-\frac{1}{n^{2}}\right) \quad \text { or } \quad \nu=R \cdot c\left(\frac{1}{2^{2}}-\frac{1}{n^{2}}\right)
$$

where $R$ is a constant (now called the Rydberg constant) equal to $1.097 \times 10^{-2} \mathrm{~nm}^{-1}$ and $n$ is an integer greater than 2 . The red spectral line at 656.3 nm , for example, results from Balmer's equation when $n=3$ :

$$
\begin{aligned}
& \frac{1}{\lambda}=\left(1.097 \times 10^{-2} \mathrm{~nm}^{-1}\right)\left(\frac{1}{2^{2}}-\frac{1}{3^{2}}\right)=1.524 \times 10^{-3} \mathrm{~nm}^{-1} \\
& \lambda=\frac{1}{1.524 \times 10^{-3} \mathrm{~nm}^{-1}}=656.3 \mathrm{~nm}
\end{aligned}
$$

Similarly, a value of $n=4$ gives the blue-green line at 486.1 nm , a value of $n=5$ gives the blue line at 434.0 nm , and so on. Solve Balmer's equation yourself to make sure.

Subsequent to the discovery of the Balmer series of lines in the visible region of the electromagnetic spectrum, it was found that many other spectral lines are also present in nonvisible regions of the electromagnetic spectrum. Hydrogen, for example, shows a series of spectral lines called the Lyman series in the ultraviolet region and still other series (the Paschen, Brackett, and Pfund series) in the infrared region.

By adapting Balmer's equation, the Swedish physicist Johannes Rydberg was able to show that every line in the entire spectrum of hydrogen can be fit by a generalized Balmer-Rydberg equation:

- BALMER-RYDBERG EQUATION $\quad \frac{1}{\lambda}=R\left[\frac{1}{m^{2}}-\frac{1}{n^{2}}\right] \quad$ or $\quad \nu=R \cdot c\left[\frac{1}{m^{2}}-\frac{1}{n^{2}}\right]$
where $m$ and $n$ represent integers with $n>m$. If $m=1$, then the Lyman series of lines results. If $m=2$, then Balmer's series of visible lines results. If $m=3$, then


FIGURE 5.6 (a) The visible line spectrum of energetically excited sodium atoms consists of a closely spaced pair of yellow lines. (b) The visible line spectrum of excited hydrogen atoms consists of four lines, from indigo at 410 nm to red at 656 nm .

© Excited hydrogen atoms give off a bluish light; excited neon atoms emit orange light.
the Paschen series is described, and so forth for still larger values of $m$. Some of these other spectral lines are calculated in Worked Example 5.2.

We'll look further at the Balmer-Rydberg equation and see what the integers $m$ and $n$ represent in Section 5.9.

## Worked Example 5.2

What are the two longest-wavelength lines (in nanometers) in the Lyman series of the hydrogen spectrum?

## Strategy

The Lyman series is given by the Balmer-Rydberg equation with $m=1$ and $n>1$. The wavelength $\lambda$ is greatest when $n$ is smallest; that is, when $n=2$ and $n=3$.

$$
\frac{1}{\lambda}=R\left(\frac{1}{m^{2}}-\frac{1}{n^{2}}\right) \quad \text { where } m=1
$$

## SOlUTION

Solving the equation first for $n=2$ gives

$$
\frac{1}{\lambda}=R\left(\frac{1}{1^{2}}-\frac{1}{2^{2}}\right)=\left(1.097 \times 10^{-2} \mathrm{~nm}^{-1}\right)\left(1-\frac{1}{4}\right)=8.228 \times 10^{-3} \mathrm{~nm}^{-1}
$$

$$
\text { or } \quad \lambda=\frac{1}{8.228 \times 10^{-3} \mathrm{~nm}^{-1}}=121.5 \mathrm{~nm}
$$

Solving the equation next for $n=3$ gives

$$
\begin{aligned}
\frac{1}{\lambda} & =R\left(\frac{1}{1^{2}}-\frac{1}{3^{2}}\right)=\left(1.097 \times 10^{-2} \mathrm{~nm}^{-1}\right)\left(1-\frac{1}{9}\right)=9.751 \times 10^{-3} \mathrm{~nm}^{-1} \\
\text { or } \quad \lambda & =\frac{1}{9.751 \times 10^{-3} \mathrm{~nm}^{-1}}=102.6 \mathrm{~nm}
\end{aligned}
$$

The two longest-wavelength lines in the Lyman series are at 121.5 nm and 102.6 nm .

## Worked Example 5.3

What is the shortest-wavelength line (in nanometers) in the Lyman series of the hydrogen spectrum?

## Strategy

The Lyman series is given by the Balmer-Rydberg equation with $m=1$ and $n>1$. The shortest-wavelength line occurs when $n$ is infinitely large so that $1 / n^{2}$ is zero. That is, if $n=\infty$, then $1 / n^{2}=0$.

## Solution

$$
\begin{aligned}
\frac{1}{\lambda} & =R\left(\frac{1}{1^{2}}-\frac{1}{\infty^{2}}\right)=\left(1.097 \times 10^{-2} \mathrm{~nm}^{-1}\right)(1-0)=1.097 \times 10^{-2} \mathrm{~nm}^{-1} \\
\text { or } \quad \lambda & =\frac{1}{1.097 \times 10^{-2} \mathrm{~nm}^{-1}}=91.2 \mathrm{~nm}
\end{aligned}
$$

PROBLEM 5.4 The Balmer equation can be extended beyond the visible portion of the electromagnetic spectrum to include lines in the ultraviolet. What is the wavelength (in nanometers) of ultraviolet light in the Balmer series corresponding to a value of $n=7$ ?

- PROBLEM 5.5 What is the longest-wavelength line (in nanometers) in the Paschen series for hydrogen?
- PROBLEM 5.6 What is the shortest-wavelength line (in nanometers) in the Paschen series for hydrogen?


### 5.4 Particlelike Properties of Electromagnetic Radiation: The Planck Equation

The existence of atomic line spectra and the fit of the visible hydrogen spectrum to the Balmer-Rydberg equation imply the existence of a general underlying principle about atomic structure, yet it was many years before that principle was found. One of the key discoveries came in 1900, when the German physicist Max Planck (1858-1947) proposed a theory to explain a seemingly unrelated phenomenon called blackbody radiation-the visible glow that solid objects give off when heated. The reddish glow from the heating element in an electric stove and the white light emitted by the hot filament in a lightbulb are two examples of blackbody radiation.

Experimentally, it's found that the intensity of blackbody radiation varies with the wavelength of the emitted light. When an object such as an iron bar is heated, it first begins to glow a dull red but then changes to a brighter orange and ultimately to a blinding white glare as its temperature increases. Thus, longer wavelengths (red) have a lower intensity, and shorter wavelengths have a higher intensity. If this trend were to continue, the intensity would keep rising indefinitely as the wavelength becomes ever shorter and enters the ultraviolet region. In fact, though, the intensity of blackbody radiation does not continue rising indefinitely. Instead, the intensity reaches a maximum and then falls rapidly at wavelengths shorter than about 500 nm (Figure 5.7).


To explain the observation that the intensity of blackbody radiation does not continue to rise indefinitely as the wavelength decreases, Planck concluded that the energy radiated by a heated object can't be continuously variable. Instead the energy is emitted only in discrete amounts, or quanta. An analogy from daily life is that of stairs versus a ramp. A ramp changes height continuously, but stairs change height only in discrete amounts and are thus quantized.

The amount of energy, $E$, associated with a quantum of radiant energy depends on the frequency of the radiation, $\nu$, according to the equation
$\begin{array}{ll}\text { or, since } \nu=\frac{c}{\lambda^{\prime}}, & E=\frac{h c}{\lambda}\end{array}$

The symbol $h$ represents a fundamental physical constant that we now call Planck's constant; $h=6.626 \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s}$. For example, one quantum of red light
\& FIGURE 5.7 The dependence of the intensity of blackbody radiation on wavelength at two different temperatures. Intensity increases from right to left on the curve as wavelength decreases. As the wavelength continues to decrease, intensity reaches a maximum and then drops off to zero.



- This glass window can be broken by a single baseball, but a thousand Ping-Pong balls would only bounce off.
with a frequency $\nu=4.62 \times 10^{14} \mathrm{~s}^{-1}$ (wavelength $\lambda=649 \mathrm{~nm}$ ) has an energy in joules of $3.06 \times 10^{-19} \mathrm{~J}$.

$$
E=h \nu=\left(6.626 \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s}\right)\left(4.62 \times 10^{14} \mathrm{~s}^{-1}\right)=3.06 \times 10^{-19} \mathrm{~J}
$$

The SI energy unit joule ( $1 \mathrm{~J}=1 \mathrm{~kg} \cdot \mathrm{~m}^{2} / \mathrm{s}^{2}$ ) is actually a fairly small amount of energy-it takes 100 J to light a 100 watt lightbulb for 1 second.

Higher frequencies and shorter wavelengths correspond to higher energy radiation, while lower frequencies and longer wavelengths correspond to lower energy. Blue light ( $\lambda \approx 450 \mathrm{~nm}$ ), for instance, has a shorter wavelength and is more energetic than red light $(\lambda \approx 650 \mathrm{~nm})$. Similarly, an $X$ ray $(\lambda \approx 1 \mathrm{~nm})$ has a shorter wavelength and is more energetic than an FM radio wave ( $\lambda \approx 10^{10} \mathrm{~nm}$, or 10 m ).


The idea that electromagnetic energy is quantized rather than continuous received further support in 1905, when Albert Einstein (1879-1955) used it to explain the photoelectric effect. Scientists had known since the late 1800s that irradiating a clean metal surface with light causes electrons to be ejected from the metal. Furthermore, the frequency of the light used for the irradiation must be above some threshold value, which is different for every metal. Blue light ( $\nu \approx$ $6.7 \times 10^{14} \mathrm{~Hz}$ ) causes metallic sodium to emit electrons, for example, but red light $\left(\nu \approx 4.0 \times 10^{14} \mathrm{~Hz}\right)$ has no effect on sodium.

Einstein explained the photoelectric effect by assuming that a beam of light behaves as if it were composed of a stream of small particles, called photons, whose energy $(E)$ is related to their frequency $(\nu)$ by the Planck equation, $E=h \nu$. If the frequency (or energy) of the photon striking a metal is below a minimum value, no electron is ejected. Above the threshold level, however, sufficient energy is transferred from the photon for an electron to overcome the attractive forces holding it to the metal (Figure 5.8).

FIGURE 5.8 The photoelectric effect. A plot of the number of electrons ejected from a metal surface versus light frequency shows a threshold value. Increasing the intensity of the light while keeping the frequency the same increases the number of electrons ejected but does not change the threshold value.
©


Note that the energy of an individual photon depends only on its frequency, not on the intensity of the light beam. The intensity of a light beam is a measure of the number of photons in the beam, not of the energies of those photons. A lowintensity beam of high-energy photons might easily knock a few electrons loose from a metal, but a high-intensity beam of low-energy photons might not be able to knock loose a single electron.

As a rough analogy, think of throwing balls of different masses at a glass window. A thousand Ping-Pong balls (lower energy) would only bounce off the window, but a single baseball (higher energy) would break the glass. In the same way, low-energy photons bounce off the metal surface, but a single photon at or above a certain threshold energy can "break" the metal and dislodge an electron.

The main conclusion from both Planck's and Einstein's work was that the behavior of light and other forms of electromagnetic radiation is more complex than had been formerly believed. In addition to behaving as waves, light energy can also behave as small particles. The idea isn't really so strange if you think of light as analogous to matter. The amount of energy corresponding to one quantum of light is almost inconceivably small, just as the amount of matter in one atom is inconceivably small, but the principle is the same: Both matter and energy occur only in discrete units. Just as there can be either 1 or 2 hydrogen atoms but not 1.5 or 1.8, there can be 1 or 2 photons of light but not 1.5 or 1.8.

Once the quantized nature of electromagnetic radiation is accepted, part of the puzzle of atomic line spectra is explained. Energetically excited atoms are unable to emit light of continuously varying wavelengths and therefore don't give a continuous spectrum. The atoms are constrained to emit light quanta (photons) of only a few specific energies, and they therefore give a line spectrum. Why atoms should be thus constrained is the next question to answer.

## Worked Example 5.4

What is the energy (in kilojoules per mole) of photons of radar waves with $\nu=$ $3.35 \times 10^{8} \mathrm{~Hz}$ ?

## Strategy

The energy of a photon with frequency $\nu$ can be calculated with the Planck equation $E=h \nu$. To find the energy per mole of photons, the energy of one photon must be multiplied by Avogadro's number.

## Solution

$$
\begin{aligned}
E=h \nu=\left(6.626 \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s}\right)\left(3.35 \times 10^{8} \mathrm{~s}^{-1}\right) & =2.22 \times 10^{-25} \mathrm{~J} \\
\left(2.22 \times 10^{-25} \frac{\mathrm{~J}}{\text { photon }}\right)\left(6.022 \times 10^{23} \frac{\text { photon }}{\mathrm{mol}}\right) & =0.134 \mathrm{~J} / \mathrm{mol} \\
& =1.34 \times 10^{-4} \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

- PROBLEM 5.7 What is the energy (in kilojoules per mole) of photons corresponding to the shortest-wavelength line in the Lyman series for hydrogen (Worked Example 5.3)?
- PROBLEM 5.8 The biological effects of a given dose of electromagnetic radiation generally become more serious as the energy of the radiation increases: Infrared radiation has a pleasant warming effect; ultraviolet radiation causes tanning and burning; and $X$ rays can cause considerable tissue damage. What energies (in kilojoules per mole) are associated with the following wavelengths: infrared radiation with $\lambda=1.55 \times 10^{-6} \mathrm{~m}$, ultraviolet light with $\lambda=250 \mathrm{~nm}$, and $X$ rays with $\lambda=5.49 \mathrm{~nm}$ ?


### 5.5 Wavelike Properties of Matter: The de Broglie Equation

The analogy between matter and radiant energy developed by Planck and Einstein in the early 1900s was further extended in 1924 by the French physicist Louis de Broglie (1892-1987). De Broglie suggested that if light can behave in some respects like matter, then perhaps matter can behave in some respects like light. That is, perhaps both light and matter are wavelike as well as particlelike.

To help construct his argument about the wavelike behavior of matter, de Broglie used the now-famous equation $E=m c^{2}$, which had been proposed in 1905 by Einstein as part of his special theory of relativity.

$$
\text { Since } E=m c^{2} \quad \text { then } \quad m=\frac{E}{c^{2}}
$$

VWave-particle duality does not mean that energy is sometimes a wave and other times a particle; it means we must use both wave and particle theories to describe energy.

V
A photon is a quantum of light energy.

Because $E=h c / \lambda$ according to the Planck equation, it's possible to substitute for $E$ to derive a relationship between mass and wavelength:

$$
m=\frac{E}{c^{2}}=\frac{h c / \lambda}{c^{2}}=\frac{h}{\lambda c}
$$

De Broglie suggested that a similar equation might be applied to an electron by replacing the speed of light (c) by the speed of the electron (v). The resultant de Broglie equation thus allows calculation of a "wavelength" of an electron or of any other particle or object of mass $m$ moving at velocity $v$ :

- De Broglie equation $\quad m=\frac{h}{\lambda v} \quad$ or $\quad \lambda=\frac{h}{m v}$

For example, the mass of an electron is $9.11 \times 10^{-31} \mathrm{~kg}$, and the velocity $v$ of an electron in a hydrogen atom is $2.2 \times 10^{6} \mathrm{~m} / \mathrm{s}$ (about $1 \%$ of the speed of light). Thus, the de Broglie wavelength of an electron in a hydrogen atom is $3.3 \times$ $10^{-10} \mathrm{~m}$, or 330 pm :

$$
\lambda=\frac{h}{m v}=\frac{6.626 \times 10^{-34} \frac{\mathrm{~kg} \cdot \mathrm{~m}^{2}}{\delta}}{\left(9.11 \times 10^{-31} \mathrm{~kg}\right)\left(2.2 \times 10^{6} \frac{\mathrm{~m}}{\mathrm{~g}}\right)}=3.3 \times 10^{-10} \mathrm{~m}
$$

Note that Planck's constant, which is usually expressed in units of joule seconds $(\mathrm{J} \cdot \mathrm{s})$, is expressed for the present purposes in units of $\left(\mathrm{kg} \cdot \mathrm{m}^{2}\right) / \mathrm{s}$ $\left[1 \mathrm{~J}=1\left(\mathrm{~kg} \cdot \mathrm{~m}^{2}\right) / \mathrm{s}^{2}\right]$.

What does it mean to say that light and matter act both as waves and as particles? The answer is "not much," at least not on the everyday human scale. The problem in trying to understand the dual wave/particle description of light and matter is that our common sense isn't up to the task. Our intuition has been developed from personal experiences, using our eyes and other senses to tell us how light and matter are "supposed" to behave. We have no personal experience on the atomic scale, though, and thus have no common-sense way of dealing with the behavior of light and matter at that level. On the atomic scale, where distances and masses are so tiny, light and matter behave in a manner different from what we're used to.

The dual wave/particle description of light and matter is really just a mathematical model. Since we can't see atoms and observe their behavior directly, the best we can do is to construct a set of mathematical equations that correctly account for atomic properties and behavior. The wave/particle description does this extremely well, even though it is not easily understood using day-to-day experience.

## Worked Example 5.5

What is the de Broglie wavelength (in meters) of a pitched baseball with a mass of 120 g and a speed of $100 \mathrm{mph}(44.7 \mathrm{~m} / \mathrm{s})$ ?

## Strategy

The de Broglie relationship says that the wavelength $\lambda$ of an object with mass $m$ moving at a velocity $v$ can be calculated by the equation $\lambda=h / m v$.

## Solution

$$
\lambda=\frac{h}{m v}=\frac{6.626 \times 10^{-34} \frac{\mathrm{~kg} \cdot \mathrm{~m}^{2}}{\mathrm{~g}}}{(0.120 \mathrm{~kg})\left(44.7 \frac{\hbar t}{\mathrm{~g}}\right)}=1.24 \times 10^{-34} \mathrm{~m}
$$

The de Broglie wavelength of the baseball is $1.24 \times 10^{-34} \mathrm{~m}$, far smaller than the diameter of an atom.

- PROBLEM 5.9 What is the de Broglie wavelength (in meters) of a small car with a mass of 1150 kg traveling at a speed of $55.0 \mathrm{mi} / \mathrm{h}(24.6 \mathrm{~m} / \mathrm{s})$ ?


### 5.6 Quantum Mechanics and the Heisenberg Uncertainty Principle

With the particlelike nature of energy and the wavelike nature of matter now established, let's return to the problem of atomic structure. Several models of atomic structure were proposed in the late nineteenth and early twentieth centuries. A model proposed in 1914 by the Danish physicist Niels Bohr (1885-1962), for example, described the hydrogen atom as a nucleus with an electron circling around it, much as a planet orbits the sun. Furthermore, said Bohr, only certain specific orbits corresponding to certain specific energy levels for the electron are available. The Bohr model was extremely important historically because of its conclusion that electrons have only specific energy levels available to them, but the model fails for atoms with more than one electron.

The breakthrough in understanding atomic structure came in 1926, when the Austrian physicist Erwin Schrödinger (1887-1961) proposed what has come to be called the quantum mechanical model of the atom. The fundamental idea behind the model is that it's best to abandon the notion of an electron as a small particle moving around the nucleus in a defined path and to concentrate instead on the electron's wavelike properties. In fact, it was shown in 1927 by Werner Heisenberg (1901-1976) that it is impossible to know precisely where an electron is and what path it follows-a statement called the Heisenberg uncertainty principle.

The Heisenberg uncertainty principle can be understood by imagining what would happen if we tried to determine the position of an electron at a given moment. For us to "see" the electron, light photons of an appropriate frequency would have to interact with and bounce off the electron. But such an interaction would transfer energy from the photon to the electron, thereby increasing the energy of the electron and making it move faster. Thus, the very act of determining the electron's position would make that position change.

In mathematical terms, Heisenberg's principle states that the uncertainty in the electron's position, $\Delta x$, times the uncertainty in its momentum, $\Delta m v$, is equal to or greater than the quantity $h / 4 \pi$ :

Heisenberg uncertainty principle $\quad(\Delta x)(\Delta m v) \geq \frac{h}{4 \pi}$
According to this equation, we can never know both the position and the velocity of an electron (or of any other object) beyond a certain level of precision. If we know the velocity with a high degree of certainty ( $\Delta m v$ is small), then the position of the electron must be uncertain ( $\Delta x$ must be large). Conversely, if we know the position of the electron exactly ( $\Delta x$ is small), then we can't know its velocity ( $\Delta m v$ must be large). As a result, an electron will always appear as something of a blur whenever we attempt to make any physical measurements of its position and velocity.

A brief calculation can help make the conclusions of the uncertainty principle clearer. As mentioned in the previous section, the mass $m$ of an electron is $9.11 \times 10^{-31} \mathrm{~kg}$ and the velocity $v$ of an electron in a hydrogen atom is $2.2 \times 10^{6} \mathrm{~m} / \mathrm{s}$. If we assume that the velocity is known to within $10 \%$, or

Bianca L. Haendler, "Presenting the Bohr Atom," J. Chem. Educ., Vol. 59, 1982, 372-376.

Oliver G. Ludwig, "On a Relation Between the Heisenberg and de Broglie Principles," J. Chem. Educ., Vol. 70, 1993, 28.


A Werner Heisenberg. Where is he? His whereabouts aren't known with certainty.

[^8]did Lawrence S. Bartell, "Perspectives on the Uncertainty Principle and Quantum Reality," J. Chem. Educ., Vol. 62, 1985, 192-196.


A Even the motion of very fast objects can be captured in daily life. On the atomic scale, however, velocity and position can't both be known precisely. Photograph by Dr. Harold E. Edgerton. © Harold \& Esther Edgerton Foundation, 2003, courtesy of Palm Press, Inc.

Ngai Ling Ma, "Quantum Analogies on Campus," J. Chem. Educ., Vol. 73, 1996, 1016-1017
$0.2 \times 10^{6} \mathrm{~m} / \mathrm{s}$, then the uncertainty in the electron's position in a hydrogen atom is greater than $3 \times 10^{-10} \mathrm{~m}$, or 300 pm :

$$
\begin{aligned}
& \text { If }(\Delta x)(\Delta m v) \geq \frac{h}{4 \pi} \text { then }(\Delta x) \geq \frac{h}{(4 \pi)(\Delta m v)} \\
& \Delta x \geq \frac{6.626 \times 10^{-34} \frac{\mathrm{~kg} \cdot \mathrm{~m}^{\chi}}{\mathrm{g}}}{(4)(3.1416)\left(9.11 \times 10^{-31} \mathrm{~kg}\right)\left(0.2 \times 10^{6} \frac{\mathrm{mg}}{\mathrm{~s}}\right)} \\
& \Delta x \geq 3 \times 10^{-10} \mathrm{~m} \text { or } 300 \mathrm{pm}
\end{aligned}
$$

But since the diameter of a hydrogen atom is only 240 pm , the uncertainty in the electron's position is similar in size to the atom itself!

When the mass $m$ of an object is relatively large, as is true in daily life, then both $\Delta x$ and $\Delta v$ in the Heisenberg relationship can be very small. We therefore have no apparent problem in measuring both position and velocity for visible objects. The problem arises only on the atomic scale. Worked Example 5.6 gives a sample calculation.

## Worked Example 5.6

Assume that you are traveling at a speed of $90 \mathrm{~km} / \mathrm{h}$ in a small car with a mass of 1250 kg . If the uncertainty in the velocity of the car is $1 \%(\Delta v=0.9 \mathrm{~km} / \mathrm{h})$, what is the uncertainty (in meters) in the position of the car? How does this compare with the uncertainty in the position of an electron in a hydrogen atom?

## Strategy

The Heisenberg relationship says that the uncertainty in an object's position, $\Delta x$, times the uncertainty in its momentum, $\Delta m v$, is equal to or greater than the quantity $h / 4 \pi$.

## Solution

In the present instance, we need to find $\Delta x$ when $\Delta v$ is known:

$$
\begin{aligned}
& \Delta x \geq \frac{h}{(4 \pi)(\Delta m v)} \\
& \Delta x \geq \frac{6.626 \times 10^{-34} \frac{\mathrm{~kg} \cdot \mathrm{~m}^{2}}{8}}{(4)(3.1416)(1250 \mathrm{~kg})\left(0.9 \frac{\mathrm{~km}}{\mathrm{k}}\right)\left(\frac{1 \mathrm{~K}}{36008}\right)\left(\frac{1000 \mathrm{kT}}{1 \mathrm{~km}}\right)} \\
& \Delta x \geq 2 \times 10^{-37} \mathrm{~m}
\end{aligned}
$$

The uncertainty in the position of the car is far smaller than the uncertainty in the position of an electron in a hydrogen atom ( $3 \times 10^{-10} \mathrm{~m}$ ) and far too small a value to have any measurable consequences.

PROBLEM 5.10 Calculate the uncertainty (in meters) in the position of a 120 g baseball thrown at a velocity of $45 \mathrm{~m} / \mathrm{s}$ if the uncertainty in the velocity is $2 \%$.

## 5.7 | Wave Functions and Quantum Numbers

Schrödinger's quantum mechanical model of atomic structure is framed in the form of a wave equation, a mathematical equation similar in form to that used to describe the motion of ordinary waves in fluids. The solutions (there are many) to the wave equation are called wave functions, or orbitals, and are represented by
the symbol $\psi$ (Greek psi). The best way to think about a wave function is to regard it as an expression whose square, $\psi^{2}$, defines the probability of finding the electron within a given volume of space around the nucleus. As Heisenberg showed, we can never be completely certain about an electron's position. A wave function, however, tells where the electron will most probably be found.

$\underset{\text { equation }}{\text { Wave }} \xrightarrow{\text { Solve }}$| Wave function |
| :---: |
| or orbital $(\psi)$ |$\longrightarrow$| Probability of finding |
| :---: |
| electron in a region |
| of space $\left(\psi^{2}\right)$ |

A wave function contains three variables called quantum numbers, represented as $n, l$, and $m_{l}$, which describe the energy level of the orbital and the threedimensional shape of the region in space occupied by a given electron.

- The principal quantum number $(n)$ is a positive integer $(n=1,2,3,4, \ldots)$ on which the size and energy level of the orbital primarily depend. For hydrogen and other one-electron atoms, such as $\mathrm{He}^{+}$, the energy of an orbital depends only on $n$. For atoms with more than one electron, the energy level of an orbital depends both on $n$ and on the $l$ quantum number.

As the value of $n$ increases, the number of allowed orbitals increases and the size of those orbitals becomes larger, thus allowing an electron to be farther from the nucleus. Because it takes energy to separate a negative charge from a positive charge, this increased distance between the electron and the nucleus means that the energy of the electron in the orbital increases as the quantum number $n$ increases.

We often speak of orbitals as being grouped according to the principal quantum number $n$ into successive layers, or shells, around the atom. Those orbitals with $n=3$, for example, are said to be in the third shell.

- The angular-momentum quantum number $(\boldsymbol{l})$ defines the three-dimensional shape of the orbital. For an orbital whose principal quantum number is $n$, the angular-momentum quantum number $l$ can have any integral value from 0 to $n-1$. Thus, within each shell, there are $n$ different shapes for orbitals.

$$
\begin{aligned}
& \text { If } n=1 \text {, then } l=0 \\
& \text { If } n=2, \text { then } l=0 \text { or } 1 \\
& \text { If } n=3, \text { then } l=0,1, \text { or } 2 \\
& \ldots \text { and so forth }
\end{aligned}
$$

Just as it's convenient to think of orbitals as being grouped into shells according to the principal quantum number $n$, we often speak of orbitals as being grouped into subshells according to the angular-momentum quantum number $l$. Different subshells are usually referred to by letter rather than by number, following the order $s, p, d, f, g$. (Historically, the letters $s, p, d$, and $f$ arose from the use of the words sharp, principal, diffuse, and fundamental to describe various lines in atomic spectra.) After $f$, successive subshells are designated alphabetically: $g, h$, and so on.

| Quantum number $l:$ | 0 | 1 | 2 | 3 | $4 \ldots$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Subshell notation: | $s$ | $p$ | $d$ | $f$ | $g \ldots$ |

As an example, an orbital with $n=3$ and $l=2$ is a $3 d$ orbital: 3 to represent the third shell and $d$ to represent the $l=2$ subshell.

- The magnetic quantum number $\left(m_{l}\right)$ defines the spatial orientation of the orbital with respect to a standard set of coordinate axes. For an orbital whose angular-momentum quantum number is $l$, the magnetic quantum number $m_{l}$


Mali Yin and Raymond S. Ochs, "The Mole, The Periodic Table, and Quantum Numbers: An Introductory Trio," J. Chem. Educ., Vol. 78, 2001, 1345-1347.

Geoff Raynner-Canham, "A
Student's Travels, Close Dancing, Bathtubs, and the Shopping Mall: More Analogies in Teaching Introductory Chemistry," J. Chem. Educ., Vol. 71, 1994, 943-944.

John J. Fortman, "Pictorial
Analogies VII: Quantum Numbers and Orbitals," J. Chem. Educ., Vol. 70, 1993, 649-650.

$\checkmark$Quantum number $m_{l}$ defines the different orientations an orbital of a given shape may assume. This gives the number of orbitals of a given type: $s$ orbital (one), $p$ orbital (three), $d$ orbital (five), $f$ orbital (seven).
can have any integral value from $-l$ to $+l$. Thus, within each subshell (orbitals with the same shape, or value of $l$ ), there are $2 l+1$ different spatial orientations for those orbitals. We'll explore this point further in the next section.

$$
\begin{aligned}
& \text { If } l=0, \text { then } m_{l}=0 \\
& \text { If } l=1, \text { then } m_{l}=-1,0, \text { or }+1 \\
& \text { If } l=2, \text { then } m_{l}=-2,-1,0,+1, \text { or }+2 \\
& \ldots \text { and so forth }
\end{aligned}
$$

A summary of the allowed combinations of quantum numbers for the first four shells is given in Table 5.2.

|  | 5.2 | Allowed Combination First Four Shells | Quantum | umbers $n, I$, and | for the |
| :---: | :---: | :---: | :---: | :---: | :---: |
| n | 1 | $\boldsymbol{m}_{\boldsymbol{l}}$ | Orbital <br> Notation | Number of Orbitals in Subshell | Number of Orbitals in Shell |
| 1 | 0 | 0 | 1 s | 1 | 1 |
| 2 | 0 | 0 | $2 s$ | 1 |  |
| 2 | 1 | $-1,0,+1$ | $2 p$ | 3 | 4 |
|  | 0 | 0 | 3s | 1 |  |
| 3 | 1 | -1, $0,+1$ | $3 p$ | 3 | 9 |
|  | 2 | -2, -1, $0,+1,+2$ | 3d | 5 |  |
|  | 0 | 0 | $4 s$ | 1 |  |
|  | 1 | -1, $0,+1$ | $4 p$ | 3 |  |
| 4 | 2 | -2, -1, $0,+1,+2$ | $4 d$ | 5 | 16 |
|  | 3 | -3, $-2,-1,0,+1,+2,+3$ | $4 f$ | 7 |  |

The energy levels of various orbitals are shown in Figure 5.9. As noted earlier in this section, the energy levels of different orbitals in a hydrogen atom depend only on the principal quantum number $n$, but the energy levels of orbitals in multielectron atoms depend on both $n$ and $l$. In other words, orbitals in a given subshell have the same energy for hydrogen but have slightly different energies for other atoms. In fact, there is even some crossover of energies from one shell to another. A 3d orbital in some multielectron atoms has a higher energy than a $4 s$ orbital, for instance.

FIGURE 5.9 Orbital energy levels for (a) hydrogen and (b) a typical multielectron atom. The differences between energies of various subshells in (b) are exaggerated for clarity. Note that there is some crossover of energies from one shell to another. In some atoms, a $3 d$ orbital has a higher energy than a $4 s$ orbital, for instance.

(a) Hydrogen
(b) Multielectron atoms

## Worked Example 5.7

Identify the shell and subshell of an orbital with the quantum numbers $n=3$, $l=1, m_{l}=1$.

## Strategy

The principal quantum number $n$ gives the shell number, and the angular-momentum quantum number $l$ gives the subshell designation. The magnetic quantum number $m_{l}$ is related to the spatial orientation of the orbital.

## Solution

A value of $n=3$ indicates that the orbital is in the third shell, and a value of $l=1$ indicates that the orbital is of the $p$ type. Thus, the orbital has the designation $3 p$.

## Worked Example 5.8

Give the possible combinations of quantum numbers for a $4 p$ orbital.

## Strategy

The designation $4 p$ indicates that the orbital has a principal quantum number $n=4$ and an angular-momentum quantum number $l=1$. The magnetic quantum number $m_{l}$ can have any of the three values $-1,0$, or +1 .

## Solution

The allowable combinations are

$$
n=4, l=1, m_{l}=-1 \quad n=4, l=1, m_{l}=0 \quad n=4, l=1, m_{l}=+1
$$

- PROBLEM 5.11 Extend Table 5.2 to show allowed combinations of quantum numbers when $n=5$. How many orbitals are in the fifth shell?
- PROBLEM 5.12 Give orbital notations for electrons in orbitals with the following quantum numbers:
(a) $n=2, l=1, m_{l}=1$
(b) $n=4, l=3, m_{l}=-2$
(c) $n=3, l=2, m_{l}=-1$
- PROBLEM 5.13 Give the possible combinations of quantum numbers for the following orbitals:
(a) A $3 s$ orbital
(b) A $2 p$ orbital
(c) A $4 d$ orbital


### 5.8 The Shapes of Orbitals

We said in the previous section that a wave function, or orbital, describes the probability of finding the electron within a specific region of space. The shape of a given orbital is defined by the angular-momentum quantum number $l$, with $l=0$ called an $s$ orbital, $l=1$ a $p$ orbital, $l=2$ a $d$ orbital, and so forth. Of the various possibilities, $s, p, d$, and $f$ orbitals are the most important because these are the only ones actually occupied in known elements. Let's look at each of the four individually.

## $s$ Orbitals

All $s$ orbitals are spherical, meaning that the probability of finding an $s$ electron depends only on distance from the nucleus, not on direction. Furthermore, because there is only one possible orientation of a sphere in space, an $s$ orbital has $m_{l}=0$ and there is only one $s$ orbital per shell.

$\square$Some students believe that the shape of an orbital shows how the electron moves about the atom. An orbital defines the region in which the electron moves with an indeterminable motion.

FIGURE 5.10 Representations of (a) 1 s , (b) $2 s$, and (c) $3 s$ orbitals. Slices through these spherical orbitals are shown on the top and cutaway views on the bottom, with the probability of finding an electron represented by the density of the shading. Note that the 2 s orbital has buried within it a spherical surface of zero probability (a node), and the 3 s orbital has within it two spherical surfaces of zero probability. The different colors of different regions in the $2 s$ and $3 s$ orbitals correspond to different algebraic signs of the wave function, analogous to the different phases of a wave, as explained in the text.

An electron's orbital is a wave theory concept. Since a wave exists simultaneously on both sides of a node, an electron does not "move" from one lobe of an orbital to another according to this mathematical model.

7 FIGURE 5.11 (a) When a rope is fixed at one end and vibrated rapidly at the other, a standing wave is generated. (b) The wave has two phases of different algebraic sign, + and -, separated by zero-amplitude regions called nodes.

As shown in Figure 5.10, the value of $\psi^{2}$ for an $s$ orbital is greatest near the nucleus and then drops off rapidly as distance from the nucleus increases, although it never goes all the way to zero, even at a large distance. As a result, there is no definite boundary to the atom and no definite "size." For purposes like that of Figure 5.10, however, we usually imagine a boundary surface enclosing the volume where an electron spends most (say, $95 \%$ ) of its time.


Although all $s$ orbitals are spherical, there are significant differences among the $s$ orbitals in different shells. For one thing, the size of the $s$ orbital increases in successively higher shells, implying that an electron in an outer-shell $s$ orbital is farther from the nucleus on average than an electron in an inner-shell $s$ orbital. For another thing, the electron distribution in an outer-shell $s$ orbital has several regions of high probability. As shown in Figure 5.10b, a $2 s$ orbital is essentially a sphere within a sphere. There are two regions of high probability, separated by a surface of zero probability called a node. Similarly, a $3 s$ orbital has three regions of high probability and two spherical nodes (Figure 5.10c).

The concept of an orbital node-a surface of zero electron probability separating regions of nonzero probability-is difficult to grasp because it raises the question "How does an electron get from one region of the orbital to another if it's not allowed to be at the node?" The question is misleading, though, because it assumes particlelike behavior for the electron rather than wavelike behavior. In fact, nodes are an intrinsic property of waves, from moving waves of water in the ocean to the stationary, or standing, wave generated by vibrating a rope (Figure 5.11). A node simply

corresponds to the zero-amplitude part of the wave. On either side of the node is a nonzero wave amplitude. Note that a wave has two phases-peaks above the zero line and troughs below-corresponding to different algebraic signs, + and - . Similarly, the different regions of $2 s$ and $3 s$ orbitals have different phases, + and - , as indicated in Figure 5.10 by different colors.

## $p$ Orbitals

The $p$ orbitals are dumbbell-shaped rather than spherical, with their electron distribution concentrated in identical lobes on either side of the nucleus and separated by a planar node cutting through the nucleus. As a result, the probability of finding a $p$ electron near the nucleus is zero. The two lobes of a $p$ orbital have different phases, as indicated in Figure 5.12 by different shading. We'll see in Chapter 7 that these phases are crucial for bonding because only lobes of the same phase can interact in forming covalent chemical bonds.


There are three allowable values of $m_{1}$ when $l=1$, so each shell beginning with the second has three $p$ orbitals, which are oriented in space at $90^{\circ}$ angles to one another along the three coordinate axes $x, y$, and $z$. The three $p$ orbitals in the second shell, for example, are designated $2 p_{x}, 2 p_{y}$, and $2 p_{z}$. As you might expect, $p$ orbitals in the third and higher shells are larger than those in the second shell and extend farther from the nucleus. Their shape is roughly the same, however.

## $d$ and $f$ Orbitals

The third and higher shells each contain five $d$ orbitals, which differ from their $s$ and $p$ counterparts because they have two different shapes. Four of the five $d$ orbitals are cloverleaf-shaped and have four lobes of maximum electron probability separated by two nodal planes through the nucleus (Figure $5.13 \mathrm{a}-\mathrm{d}$ ). The fifth $d$ orbital is similar in shape to a $p_{z}$ orbital but has an additional donut-shaped region of electron probability centered in the $x y$ plane (Figure 5.13e). In spite of their different shapes, all five $d$ orbitals in a given shell have the same energy. As with $p$ orbitals, alternating lobes of the $d$ orbitals have different phases.

You may have noticed that both the number of nodal planes through the nucleus and the overall geometric complexity of the orbitals increases with the $l$ quantum number of the subshell: $s$ orbitals have one lobe and no nodal plane through the nucleus; $p$ orbitals have two lobes and one nodal plane; $d$ orbitals have four lobes and two nodal planes. The seven $f$ orbitals are more complex still, having eight lobes of maximum electron probability separated by three nodal planes through the nucleus. (Figure 5.13 f shows one of the seven $4 f$ orbitals.) Most of the elements we'll deal with in the following chapters don't use $f$ orbitals in bonding, however, so we won't worry about them.

## r

4 FIGURE 5.12
Representations of the three $2 p$ orbitals, each of which is dumbbell-shaped and oriented in space along one of the three coordinate axes $x, y$, or $z$. Each $p$ orbital has two lobes of high electron probability separated by a nodal plane passing through the nucleus. The different shadings of the lobes reflect different algebraic signs analogous to the different phases of a wave.


- FIGURE 5.13

Representations of the five $3 d$ orbitals. Four of the orbitals are shaped like a cloverleaf (a-d), and the fifth is shaped like an elongated dumbbell inside a donut (e). Also shown is one of the seven $4 f$ orbitals ( $\mathbf{f}$ ). As with $p$ orbitals in Figure 5.12, the different shadings of the lobes reflect different phases.

Elvin Hughes, Jr., and Arnold George, "Suitable Light
Sources and Spectroscopes for Student Observation of Emission Spectra in Lecture Halls," J. Chem. Educ., Vol. 61, 1984, 908-909.

PROBLEM 5.14 How many nodal planes through the nucleus do you think a $g$ orbital has?

- KEY CONCEPT PROBLEM 5.15 Give a possible combination of $n$ and $l$ quantum numbers for the following fourth-shell orbital:



### 5.9 Quantum Mechanics and Atomic Spectra

Now that we've seen how atomic structure is described according to the quantum mechanical model, let's return briefly to the subject of atomic line spectra first mentioned in Section 5.3. How does the quantum mechanical model account for the discrete wavelengths of light found in a line spectrum?

Each electron in an atom occupies an orbital, and each orbital has a specific energy level. Thus, the energies available to electrons are quantized and can have only the specific values associated with the orbitals they occupy. When an atom is heated in a flame or electric discharge, the heat energy causes an electron to jump from a lower-energy orbital to a higher-energy orbital. In a hydrogen atom, for
example, the electron might jump from the $1 s$ orbital to a second-shell orbital, to a third-shell orbital, or to any higher-shell orbital, depending on the amount of energy added. But the energetically excited atom is relatively unstable, and the electron rapidly returns to a lower-energy level accompanied by emission of energy equal to the difference between the higher and lower orbitals. Since the energies of the orbitals are quantized, the amount of energy emitted is also quantized. Thus, we observe the emission of only specific frequencies of radiation (Figure 5.14). By measuring the frequencies emitted by excited hydrogen atoms, we can calculate the energy differences between orbitals.

(a)

(b)

The variables $m$ and $n$ in the Balmer-Rydberg equation for hydrogen (Section 5.3) represent the principal quantum numbers of the two orbitals involved in the electronic transition. The variable $n$ corresponds to the principal quantum number of the higher-energy, outer-shell orbital that the transition is from, and the variable $m$ corresponds to the principal quantum number of the lower-energy, inner-shell orbital that the transition is to. When $m=1$ (the Lyman series), for example, the frequencies of emitted light correspond to energy differences between various outer-shell orbitals and the first-shell orbital. When $m=2$ (the Balmer series), the frequencies correspond to energy differences between outer-shell orbitals and the second-shell orbitals (Figure 5.14b).


Notice in Figure 5.14b that as $n$ becomes larger and approaches infinity, the energy difference between the $n$ shell and the first shell converges to a value of $1312 \mathrm{~kJ} / \mathrm{mol}$. That is, 1312 kJ is released when electrons come from a great distance (the "infinite" shell) and add to $\mathrm{H}^{+}$to give a mole of hydrogen atoms, each with an electron in its first shell:

$$
\mathrm{H}^{+}+\mathrm{e}^{-} \longrightarrow \mathrm{H}+\text { Energy } \quad(1312 \mathrm{~kJ} / \mathrm{mol})
$$

Because the energy released on adding an electron to $\mathrm{H}^{+}$is equal to the energy absorbed on removing an electron from a hydrogen atom, we can also say that $1312 \mathrm{~kJ} / \mathrm{mol}$ is required to remove the electron from a hydrogen atom. We'll see in the

A FIGURE 5.14 The origin of atomic line spectra. (a) When an electron falls from a higherenergy outer-shell orbital to a lower-energy inner-shell orbital, it emits electromagnetic radiation whose frequency corresponds to the energy difference between the two orbitals. (The orbital radii are not drawn to scale.) (b) The different spectral series correspond to electronic transitions from outer-shell orbitals to different inner-shell orbitals.

$\sqrt{ }$
The closer an electron is brought to the nucleus of an atom, the greater the energy of the photon emitted and the lower the energy of the electron.

The Planck equation is for a single photon or single electron energy. On a macroscopic scale it is useful to convert to energy per mole of photons or electrons by multiplying by Avogadro's number.

vIf a beam of atoms having one unpaired electron (such as atoms of silver) pass through a magnetic field, half are attracted to one pole and half to the other pole of the magnet.

$m_{s}=+\frac{1}{2}$

$m_{s}=-\frac{1}{2}$

A FIGURE 5.15 Electrons behave in some respects as if they were tiny charged spheres spinning around an axis. This spin (blue arrow) gives rise to a tiny magnetic field (green arrow) and to a fourth quantum number, $m_{s}$, which can have a value of either $+1 / 2$ or $-1 / 2$.
next chapter that the amount of energy necessary to remove an electron from an element provides an important clue about the element's chemical reactivity.

What is true for hydrogen is also true for all other atoms: All atoms show atomic line spectra when energetically excited electrons fall from higher-energy orbitals in outer shells to lower-energy orbitals in inner shells. As you might expect, though, these spectra become very complex for multielectron atoms in which different orbitals within a shell no longer have identical energies and in which a large number of electronic transitions are possible.

## Worked Example 5.9

What is the energy difference (in kilojoules per mole) between the first and second shells of the hydrogen atom if the first emission in the Lyman series occurs at $\lambda=121.5 \mathrm{~nm}$ ?

## Strategy

The first line in the Lyman series corresponds to the emission of light as an electron falls from the second shell to the first shell, and the energy of that light equals the energy difference between shells. Knowing the wavelength of the light, we can calculate the energy of one photon using the Planck equation, $E=h c / \lambda$, and then multiply by Avogadro's number to find the answer in joules (or kilojoules) per mole:

## SOlUTION

$$
\begin{aligned}
E=\frac{h c N_{\mathrm{A}}}{\lambda} & =\frac{\left(6.626 \times 10^{-34} \mathrm{~J} \cdot \delta\right)\left(3.00 \times 10^{8} \frac{\mathrm{~m}}{\delta}\right)\left(10^{9} \frac{\mathrm{~nm}}{\mathrm{~m}}\right)\left(6.022 \times 10^{23} \mathrm{~mol}^{-1}\right)}{121.5 \mathrm{~nm}} \\
& =9.85 \times 10^{5} \mathrm{~J} / \mathrm{mol}=985 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

The energy difference between the first and second shells of the hydrogen atom is $985 \mathrm{~kJ} / \mathrm{mol}$.

PROBLEM 5.16 Calculate (in kilojoules per mole) the energy necessary to remove an electron from the first shell of a hydrogen atom $\left(R=1.097 \times 10^{-2} \mathrm{~nm}^{-1}\right)$.

### 5.10 Electron Spin and the Pauli Exclusion Principle

The three quantum numbers $n, l$, and $m_{l}$ discussed in Section 5.7 define the energy, shape, and spatial orientation of orbitals, but they don't quite tell the whole story. When the line spectra of many multielectron atoms are studied in detail, it turns out that some lines actually occur as very closely spaced pairs. (You can see this pairing if you look closely at the visible spectrum of sodium in Figure 5.6.) Thus, there are more energy levels than simple quantum mechanics predicts, and a fourth quantum number is required. Denoted $m_{s}$, this fourth quantum number is related to a property called electron spin.

In certain respects, electrons behave as if they were spinning around an axis, much as the earth spins daily. Unlike the earth, though, electrons are free to spin in either a clockwise or a counterclockwise direction. This spinning charge gives rise to a tiny magnetic field and to a spin quantum number ( $m_{s}$ ), which can have either of two values, $+1 / 2$ or $-1 / 2$ (Figure 5.15 ). A spin of $+1 / 2$ is usually represented by an up arrow $(\uparrow)$, and a spin of $-1 / 2$ is represented by a down arrow $(\downarrow)$. Note that the value of $m_{s}$ is independent of the other three quantum numbers, unlike the values of $n, l$, and $m_{l}$, which are interrelated.

The importance of the spin quantum number comes when electrons occupy specific orbitals in multielectron atoms. According to the Pauli exclusion principle,
proposed in 1925 by the Austrian physicist Wolfgang Pauli (1900-1958), no two electrons in an atom can have the same four quantum numbers. In other words, the set of four quantum numbers associated with an electron acts as a unique "address" for that electron in an atom, and no two electrons can have the same address.

Pauli exclusion principle No two electrons in an atom can have the same four quantum numbers.
Think about the consequences of the Pauli exclusion principle. Electrons that occupy the same orbital have the same three quantum numbers, $n, l$, and $m_{l}$. But if they have the same values for $n, l$, and $m_{l}$, they must have different values for the fourth quantum number: either $m_{s}=+1 / 2$ or $m_{s}=-1 / 2$. Thus, an orbital can hold only two electrons, which must have opposite spins. An atom with $x$ number of electrons therefore has at least $x / 2$ occupied orbitals (though it might have more if some of its orbitals are only half-filled).

### 5.11| Orbital Energy Levels in Multielectron Atoms

We said in Section 5.7 that the energy level of an orbital in a hydrogen atom is determined by its principal quantum number $n$. Within a shell, all hydrogen orbitals have the same energy, independent of their other quantum numbers. The situation is different in multielectron atoms, however, where the energy level of a given orbital depends not only on the shell but also on the subshell. The $s, p, d$, and $f$ orbitals within a given shell have slightly different energies in a multielectron atom, as shown previously in Figure 5.9, and there is even some crossover of energies between orbitals in different shells.

The difference in energy between subshells in multielectron atoms results from electron-electron repulsions. In hydrogen, the only electrical interaction is the attraction of the positive nucleus for the negative electron, but in multielectron atoms there are many different interactions to consider. Not only are there the attractions of the nucleus for each electron, there are also the repulsions between every electron and each of its neighboring electrons.

The repulsion of outer-shell electrons by inner-shell electrons is particularly important because the outer-shell electrons are pushed farther away from the nucleus and are thus held less tightly. Part of the attraction of the nucleus for an outer electron is thereby canceled, an effect we describe by saying that the outer electrons are shielded from the nucleus by the inner electrons (Figure 5.16). The net nuclear charge actually felt by an electron, called the effective nuclear charge, $Z_{\text {eff }}$, is often substantially lower than the actual nuclear charge $Z$.

- effective nuclear charge $\quad Z_{\text {eff }}=Z_{\text {actual }}$ - Electron shielding


FIGURE 5.16 The origin of electron shielding and $Z_{\text {eff }}$. Outer electrons are attracted toward the nucleus by the nuclear charge but are pushed away by the repulsion of inner electrons. As a result, the nuclear attraction actually felt by outer electrons is diminished, and we say that the outer electrons are shielded from the full charge of the nucleus by the inner electrons.

How does electron shielding lead to energy differences among orbitals within a shell? The answer is a consequence of the differences in orbital shapes. Compare a $2 s$ orbital with a $2 p$ orbital, for instance. The $2 s$ orbital is spherical and has a large
probability density near the nucleus, while the $2 p$ orbitals are dumbbell-shaped and have a node at the nucleus (Section 5.8). An electron in a $2 s$ orbital therefore spends more time closer to the nucleus than an electron in a $2 p$ orbital does and is less shielded. A $2 s$ electron thus feels a higher $Z_{\text {eff }}$, is more tightly held by the nucleus, and is lower in energy than a $2 p$ electron. In the same way, a $3 p$ electron is closer to the nucleus on average, feels a higher $Z_{\text {eff }}$, and has a lower energy than a $3 d$ electron. More generally, within any given shell $n$, a lower value of the angularmomentum quantum number $l$ corresponds to a higher $Z_{\text {eff }}$ and to a lower energy for the electron.


The idea that electrons in different orbitals are shielded differently and feel different values of $Z_{\text {eff }}$ is a very useful one that we'll return to on several occasions to explain various chemical phenomena.

### 5.12 Electron Configurations of Multielectron Atoms

All the parts are now in place to provide a complete electronic description for every element. Knowing the relative energies of the various orbitals, we can predict for each element which orbitals are occupied by electrons-the element's electron configuration.

A set of three rules called the aufbau principle (from the German word for "building up") guides the filling order of orbitals. In general, each successive electron added to an atom occupies the lowest-energy orbital available. The resultant lowest-energy electron configuration is called the ground-state configuration of the atom. It may happen, of course, that several orbitals will have the same energy level-for example, the three $p$ orbitals or the five $d$ orbitals in a given subshell. Orbitals that have the same energy level are said to be degenerate.

## Rules of the aufbau principle

1. Lower-energy orbitals fill before higher-energy orbitals. (The ordering of energy levels for orbitals is shown in Figure 5.9.)
2. An orbital can hold only two electrons, which must have opposite spins. This is just a restatement of the Pauli exclusion principle (Section 5.10), emphasizing that no two electrons in an atom can have the same four quantum numbers.
3. If two or more degenerate orbitals are available, one electron goes into each until all are half-full, a statement called Hund's rule. Only then does a second electron fill one of the orbitals. Furthermore, the electrons in each of the singly occupied orbitals must have the same value for their spin quantum number.

- Hund's rule If two or more orbitals with the same energy are available, one electron goes in each until all are half-full. The electrons in the half-filled orbitals all have the same value of their spin quantum number.

Hund's rule results from the fact that electrons repel one another and therefore remain as far apart as possible. Not surprisingly, they can remain farther apart and be lower in energy if they are in different orbitals describing different spatial regions than if they are in the same orbital occupying the same region.

Let's look at some examples to see how the rules of the aufbau principle are applied.

- Hydrogen: Hydrogen has only one electron, which must go into the lowestenergy, 1 s orbital. Thus, we say that the ground-state electron configuration of hydrogen is $1 s^{1}$, where the superscript indicates the number of electrons in the specified orbital.

$$
\mathbf{H}: 1 s^{1}
$$

- Helium: Helium has two electrons, both of which fit into the lowest-energy, 1 s orbital. The two electrons have opposite spins.

$$
\mathrm{He}: 1 s^{2}
$$

- Lithium and beryllium: With the $1 s$ orbital full, both the third and fourth electrons go into the next available, $2 s$ orbital.

$$
\mathbf{L i}: 1 s^{2} 2 s^{1} \quad \mathbf{B e}: 1 s^{2} 2 s^{2}
$$

- Boron through neon: The six elements from boron through neon have their three $2 p$ orbitals filled successively. Because these three $2 p$ orbitals have the same energy, they are degenerate and are filled according to Hund's rule. In carbon, for instance, the two $2 p$ electrons are in different orbitals, which can be arbitrarily specified as $2 p_{x}, 2 p_{y}$, or $2 p_{z}$ when writing the electron configuration. Similarly for nitrogen, whose three $2 p$ electrons must be in three different orbitals. Although not usually noted in the written electron configuration, the electrons in each of the singly occupied carbon and nitrogen $2 p$ orbitals must have the same value of the spin quantum numbereither $+1 / 2$ or $-1 / 2$.

For clarity, we sometimes specify electron configurations using orbitalfilling diagrams, in which electrons are represented by arrows. The two values of the spin quantum numbers are indicated by having the arrow point either up or down. An up-down pair indicates that an orbital is filled, while a single up (or down) arrow indicates that an orbital is half-filled. Note in the diagrams for carbon and nitrogen that the degenerate $2 p$ orbitals are halffilled rather than filled, according to Hund's rule, and that the electron spin is the same in each.

| B: $1 s^{2} 2 s^{2} 2 p^{1}$ | or | $\frac{\downarrow \uparrow}{1 s}$ | $\frac{\downarrow \uparrow}{2 s}$ | $-\uparrow$ |
| :--- | :--- | :--- | :--- | :--- |
| C: $1 s^{2} 2 s^{2} 2 p_{x}{ }^{1} 2 p_{y}{ }^{1}$ | or | $\frac{\downarrow \uparrow}{1 s}$ | $\frac{\downarrow \uparrow}{2 s}$ | $-\uparrow \frac{\uparrow}{2 p}-$ |
| N: $1 s^{2} 2 s^{2} 2 p_{x}{ }^{1} 2 p_{y}{ }^{1} 2 p_{z}{ }^{1}$ | or | $\frac{\downarrow \uparrow}{1 s}$ | $\frac{\downarrow \uparrow}{2 s}$ | $-\uparrow \frac{\uparrow}{2 p}-$ |

From oxygen through neon, the three $2 p$ orbitals are successively filled. For fluorine and neon, it's no longer necessary to distinguish among the different $2 p$ orbitals, so we can simply write $2 p^{5}$ and $2 p^{6}$.
O: $\quad 1 s^{2} 2 s^{2} 2 p_{x}{ }^{2} 2 p_{y}{ }^{1} 2 p_{z}{ }^{1}$
or $\quad \frac{\downarrow \uparrow}{1 s} \quad \frac{\downarrow \uparrow}{2 s}$
$\frac{\downarrow \uparrow}{2 p} \frac{\uparrow}{2}$
F: $\quad 1 s^{2} 2 s^{2} 2 p^{5}$
or
$\frac{\downarrow \uparrow}{1 s} \quad \frac{\downarrow \uparrow}{2 s}$
$\frac{\downarrow \uparrow}{2 p} \frac{\downarrow \uparrow}{2}-$
Ne: $1 s^{2} 2 s^{2} 2 p^{6}$
or
$\frac{\downarrow \uparrow}{1 s} \quad \frac{\downarrow \uparrow}{2 s}$
$\frac{\downarrow \uparrow}{} \frac{\downarrow \uparrow}{2 p} \frac{\downarrow \uparrow}{}$

Ronald J. Gillespie, James N. Spencer, and Richard S. Moog, "Demystifying Introductory Chemistry; Part 1. Electron Configurations from Experiment," J. Chem. Educ., Vol. 73, 1996, 617-622.

(1)
Anthony Garofalo, "Housing Electrons: Relating Quantum Numbers, Energy Levels, and Electron Configurations," J. Chem. Educ., Vol. 74, 1997, 709-719.

DIJ M. Bonneau, "The Quantum Shoe Store and Electron Structure," J. Chem. Educ., Vol. 68, 1991, 837.


vElectron orbital-filling diagrams explicitly show the number of unpaired electrons; electron configurations do not. Students who ignore the use of orbital-filling diagrams are prone to say that all electrons are paired on an atom with an electron configuration such as $1 s^{2} 2 s^{2} 2 p^{2}$.

Judith A. Strong, "The Periodic Table and Electron Configurations," J. Chem. Educ., Vol. 63, 1986, 834.

## TABLE 5.3 Valence-

 ShellElectron Configurations of Main-Group Elements

| Group | Valence-Shell <br> Electron <br> Configuration |  |
| :--- | :--- | ---: |
| 1 A | $n s^{1}$ | $(1$ total $)$ |
| 2 A | $n s^{2}$ | $(2$ total $)$ |
| 3 A | $n s^{2} n p^{1}$ | $(3$ total $)$ |
| 4 A | $n s^{2} n p^{2}$ | $(4$ total $)$ |
| 5 A | $n s^{2} n p^{3}$ | $(5$ total) |
| 6 A | $n s^{2} n p^{4}$ | $(6$ total $)$ |
| 7 A | $n s^{2} n p^{5}$ | $(7$ total) |
| 8 A | $n s^{2} n p^{6}$ | $(8$ total) |

- Sodium and magnesium: The $3 s$ orbital is filled next, giving sodium and magnesium the ground-state electron configurations shown. Note that we often write the configurations in a shorthand version by giving the symbol of the noble gas in the previous row to indicate electrons in filled shells and then specifying only those electrons in unfilled shells.

- Aluminum through argon: The $3 p$ orbitals are now filled according to the same rules used previously for filling the $2 p$ orbitals of boron through neon. Rather than explicitly identify which of the degenerate $3 p$ orbitals are occupied in Si , P, and S, we'll simplify the writing by giving just the total number of electrons in the subshell. For example, we'll write $3 p^{2}$ for silicon rather than $3 p_{x}{ }^{1} 3 p_{y}{ }^{1}$.

$$
\begin{array}{lll}
\text { Al: }[\mathrm{Ne}] 3 s^{2} 3 p^{1} & \mathbf{S i}:[\mathrm{Ne}] 3 s^{2} 3 p^{2} & \mathbf{P}:[\mathrm{Ne}] 3 s^{2} 3 p^{3} \\
\text { S: }[\mathrm{Ne}] 3 s^{2} 3 p^{4} & \mathbf{C l}:[\mathrm{Ne}] 3 s^{2} 3 p^{5} & \text { Ar: }[\mathrm{Ne}] 3 s^{2} 3 p^{6}
\end{array}
$$

- Elements past argon: Following the filling of the $3 p$ subshell in argon, the first crossover in the orbital filling order is encountered. Rather than continue filling the third shell by populating the $3 d$ orbitals, the next two electrons in potassium and calcium go into the $4 s$ subshell. Only then does filling of the $3 d$ subshell occur to give the first transition metal series from scandium through zinc.

$$
\mathbf{K}:\left[\begin{array}{lll}
{[A r}
\end{array} 4 s^{1} \quad \mathbf{C a}:[\mathrm{Ar}] 4 s^{2} \quad \mathbf{S c}:[\mathrm{Ar}] 4 s^{2} 3 d^{1} \longrightarrow \mathbf{Z n}:[\mathrm{Ar}] 4 s^{2} 3 d^{10}\right.
$$

The experimentally determined ground-state electron configurations of the elements are shown in Figure 5.17.

### 5.13 Electron Configurations and the Periodic Table

Why are electron configurations so important, and what do they have to do with the periodic table? The answers emerge when you look closely at Figure 5.17. Focusing only on the electrons in the outermost shell, called the valence shell, all the elements in a given group of the periodic table have similar valence-shell electron configurations (Table 5.3). The group 1A elements, for example, all have an $s^{1}$ valence-shell configuration; the group 2A elements have an $s^{2}$ valenceshell configuration; the group 3A elements have an $s^{2} p^{1}$ valence-shell configuration; and so on across every group of the periodic table (except for a small number of anomalies). Furthermore, because the valence-shell electrons are the most loosely held, they are the most important for determining an element's properties, thus explaining why the elements in a given group of the periodic table have similar chemical behavior.

The periodic table can be divided into four regions, or blocks, of elements according to the orbitals being filled (Figure 5.18). The group 1A and 2A elements on the left side of the table are called the s-block elements because they result from the filling of an $s$ orbital; the group 3A-8A elements on the right side of the table are the $p$-block elements because they result from the filling of $p$ orbitals; the transition metal $d$-block elements in the middle of the table result from the filling of $d$ orbitals; and the lanthanide/actinide $f$-block elements detached at the bottom of the table result from the filling of $f$ orbitals.


|  | $\begin{gathered} 59 \\ \operatorname{Pr} \\ 6 s^{2} 4 f^{3} \end{gathered}$ | 60 <br> Nd <br> $6 s^{2} 4 f^{4}$ | $\begin{gathered} 61 \\ \mathrm{Pm} \\ 6 s^{2} 4 f^{5} \end{gathered}$ | $\begin{gathered} 62 \\ \mathrm{Sm} \\ 6 s^{2} 4 f^{6} \end{gathered}$ | $\begin{gathered} 63 \\ \text { Eu } \\ 6 s^{2} 4 f^{7} \end{gathered}$ |  | $\begin{gathered} 65 \\ \mathrm{~Tb} \\ 6 s^{2} 4 f^{9} \end{gathered}$ | $66$ <br> Dy $6 s^{2} 4 f^{10}$ | $\begin{gathered} 67 \\ \text { Ho } \\ 6 s^{2} 4 f^{11} \end{gathered}$ | $\begin{gathered} 68 \\ \mathrm{Er} \\ 6 s^{2} 4 f^{12} \end{gathered}$ | $\begin{gathered} 69 \\ \mathrm{Tm} \\ 6 s^{2} 4 f^{13} \end{gathered}$ | $\begin{gathered} 70 \\ \mathrm{Yb} \\ 6 s^{2} 4 f^{14} \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} 90 \\ \text { Th } \\ 7 s^{2} 6 d^{2} \end{gathered}$ | $\begin{gathered} 91 \\ \mathrm{~Pa} \\ 7 s^{2} 5 f^{2} 6 d^{1} \end{gathered}$ | $\begin{gathered} 92 \\ \mathrm{U} \\ 7 s^{2} 5 f^{3} 6 d^{1} \end{gathered}$ | $\begin{gathered} 93 \\ \mathrm{~Np} \\ 7 \mathrm{~s}^{2} 5 f^{4} 6 d^{1} \end{gathered}$ | $\begin{gathered} 94 \\ \mathrm{Pu} \\ 7 \mathrm{~s}^{2} 5 f^{6} \end{gathered}$ | $\begin{gathered} 95 \\ \mathrm{Am} \\ 7 s^{2} 2 f^{7} \end{gathered}$ | $\begin{gathered} 96 \\ C m \\ 7 s^{2} 5 f^{7} 6 d^{1} \end{gathered}$ | $\begin{gathered} 97 \\ \mathrm{Bk} \\ 7 s^{2} 5 f^{9} \end{gathered}$ | $\begin{gathered} 98 \\ \mathrm{Cf} \\ 7 \mathrm{~s}^{2} 5 f^{10} \end{gathered}$ | $\begin{gathered} 99 \\ \text { Es } \\ 7 s^{2} 5 f^{11} \end{gathered}$ | $\begin{gathered} 100 \\ \mathrm{Fm} \\ 7 \mathrm{~s}^{2} 5 f^{12} \end{gathered}$ | $\begin{gathered} 101 \\ \mathrm{Md} \\ 7 \mathrm{~s}^{2} 5 f^{13} \end{gathered}$ | $\begin{gathered} 102 \\ \text { No } \\ 7 s^{2} 5 f^{14} \end{gathered}$ | $\begin{gathered} 103 \\ \mathrm{Lr} \\ 7 \mathrm{~s}^{2} 5 f^{14} 6 d^{1} \end{gathered}$ |




A FIGURE 5.18 Blocks of the periodic table, corresponding to filling the different kinds of orbitals. Beginning at the top left and going across successive rows of the periodic table provides a method for remembering the order of orbital filling: $1 s \rightarrow 2 s \rightarrow 2 p \rightarrow 3 s \rightarrow 3 p \rightarrow$ $4 s \rightarrow 3 d \rightarrow 4 p$, and so on.

Thinking of the periodic table as outlined in Figure 5.18 provides a useful way to remember the order of orbital filling. Beginning at the top left corner of the periodic table and going across successive rows gives the correct orbitalfilling order automatically. The first row of the periodic table, for instance, contains only the two $s$-block elements H and He , so the first available $s$ orbital (1s) is filled first. The second row begins with two $s$-block elements ( Li and Be ) and continues with six $p$-block elements ( B through Ne ), so the next available $s$ orbital (2s) and then the first available $p$ orbitals ( $2 p$ ) are filled. The third row is similar to the second row, so the $3 s$ and $3 p$ orbitals are filled. The fourth row again starts with two $s$-block elements ( K and Ca ) but is then followed by ten $d$-block elements ( Sc through Zn ) and six $p$-block elements ( Ga through Kr ). Thus, the order of orbital filling is $4 s$ followed by the first available $d$ orbitals (3d) followed by $4 p$. Continuing through successive rows of the periodic table gives the entire filling order:

$$
\begin{aligned}
& 1 s \rightarrow 2 s \rightarrow 2 p \rightarrow 3 s \rightarrow 3 p \rightarrow 4 s \rightarrow 3 d \rightarrow 4 p \rightarrow 5 s \rightarrow 4 d \rightarrow \\
& 5 p \rightarrow 6 s \rightarrow 4 f \rightarrow 5 d \rightarrow 6 p \rightarrow 7 s \rightarrow 5 f \rightarrow 6 d \rightarrow 7 p
\end{aligned}
$$

## Worked Example 5.10

Give the ground-state electron configuration of arsenic, $Z=33$, and draw an orbitalfilling diagram, indicating the electrons as up or down arrows.

## Strategy

Think of the periodic table as having $s, p, d$, and $f$ blocks of elements, as shown in Figure 5.18. Start with hydrogen at the upper left, and fill orbitals until 33 electrons have been added. Remember that only two electrons can go into an orbital and that each one of a set of degenerate orbitals must be half-filled before any one can be completely filled.

## Solution

$$
\text { As: } 1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6} 4 s^{2} 3 d^{10} 4 p^{3} \text { or }[\mathrm{Ar}] 4 s^{2} 3 d^{10} 4 p^{3}
$$

An orbital-filling diagram indicates the electrons in each orbital as arrows. Note that the three $4 p$ electrons all have the same spin:


## Worked Key Concept Example 5.11

Identify the atom with the following ground-state electron configuration:


## Strategy

One way to do this problem is to identify the electron configuration and decide which atom has that configuration. Alternatively, it's simpler to just count the electrons, thereby finding the atomic number of the atom.

## Solution

The atom whose ground-state electron configuration is depicted is in the fifth row because it follows krypton. It has the configuration $5 s^{2} 4 d^{5}$, which identifies it as technetium. Alternatively, it has $36+7=43$ electrons and is the element with $Z=43$.

PROBLEM 5.17 Give expected ground-state electron configurations for the following atoms, and draw orbital-filling diagrams for parts (a)-(c).
(a) $\mathrm{Ti}(Z=22)$
(b) $\mathrm{Zn}(Z=30)$
(c) $\operatorname{Sn}(Z=50)$
(d) $\mathrm{Pb}(Z=82)$

PROBLEM 5.18 What is a likely ground-state electron configuration for the sodium ion, $\mathrm{Na}^{+}$, formed by loss of an electron from a neutral sodium atom? What is a likely ground-state electron configuration for the chloride ion, $\mathrm{Cl}^{-}$, formed by adding an electron to a neutral chlorine atom?

KEY CONCEPT PROBLEM 5.19 Identify the atom with the following groundstate electron configuration:


### 5.14 | Some Anomalous Electron Configurations

The guidelines discussed in the previous section for determining ground-state electron configurations work well but are not completely accurate. As shown in Figure 5.17, 90 electron configurations are correctly accounted for by the rules, but 19 of the predicted configurations are incorrect.

The reasons for the anomalies generally have to do with the unusual stability of both half-filled and fully filled subshells. Chromium, for example, which we would predict to have the configuration [Ar] $4 s^{2} 3 d^{4}$, actually has the configuration [Ar] $4 s^{1} 3 d^{5}$. By moving an electron from the $4 s$ orbital to an energetically similar $3 d$ orbital, chromium trades one filled subshell $\left(4 s^{2}\right)$ for two half-filled subshells $\left(4 s^{1} 3 d^{5}\right)$. In the same way, copper, which we would predict to have the configuration [Ar] $4 s^{2} 3 d^{9}$, actually has the configuration [Ar] $4 s^{1} 3 d^{10}$. By transferring an electron from the $4 s$ orbital to a $3 d$ orbital, copper trades one filled subshell $\left(4 s^{2}\right)$ for a different filled subshell $\left(3 d^{10}\right)$ and gains a half-filled subshell $\left(4 s^{1}\right)$.

Most of the anomalous electron configurations shown in Figure 5.17 occur in elements with atomic numbers greater than $Z=40$, where the energy differences between subshells are small. In all cases, the transfer of an electron from one subshell to another lowers the total energy of the atom because of a decrease in electronelectron repulsions.

- PROBLEM 5.20 Look at the electron configurations in Figure 5.17, and identify the 19 anomalous ones.

Periodic Trends: Atomic Radii movie
eractive Periodic Table

FIGURE 5.19 Atomic radii of the elements in picometers.

### 5.15 Electron Configurations and Periodic Properties: Atomic Radii

One of the many periodic properties of the elements that can be explained by electron configurations is size, or atomic radius. You might wonder, though, how we can talk about a definite "size" for an atom, having said in Section 5.8 that the electron clouds around atoms have no specific boundaries. What's usually done is to define an atom's radius as being half the distance between the nuclei of two identical atoms when they are bonded together. In the $\mathrm{Cl}_{2}$ molecule, for example, the distance between the two chlorine nuclei is 198 pm ; in diamond (elemental carbon), the distance between two carbon nuclei is 154 pm . Thus, we say that the atomic radius of chlorine is half the $\mathrm{Cl}-\mathrm{Cl}$ distance, or 99 pm , and the atomic radius of carbon is half the $\mathrm{C}-\mathrm{C}$ distance, or 77 pm .

It's possible to check the accuracy of atomic radii by making sure that the assigned values are additive. For instance, since the atomic radius of Cl is 99 pm and the atomic radius of C is 77 pm , the distance between Cl and C nuclei when those two atoms are bonded together ought to be roughly $99 \mathrm{pm}+77 \mathrm{pm}$, or 176 pm . In fact, the measured distance between chlorine and carbon in the chloromethane molecule $\left(\mathrm{CH}_{3} \mathrm{Cl}\right)$ is 178 pm , remarkably close to the expected value.

it's the fourth one $\left(4 s^{1}\right)$; and so on through $\mathrm{Rb}\left(5 s^{1}\right), \mathrm{Cs}\left(6 s^{1}\right)$, and $\mathrm{Fr}\left(7 s^{1}\right)$. Because larger shells are occupied, the atomic radii are also larger.

The decrease in radius from left to right across the periodic table occurs because of an increase in effective nuclear charge for the valence-shell electrons. As we saw in Section $5.11, Z_{\text {eff }}$, the effective nuclear charge actually felt by an electron, is lower than the true nuclear charge $Z$ because of shielding by other electrons in the atom. The amount of shielding felt by an electron depends on both the shell and subshell of the other electrons with which it is interacting. As a general rule, a valence-shell electron is

- Strongly shielded by electrons in inner shells, which are closer to the nucleus
- Less strongly shielded by other electrons in the same shell, according to the order $s>p>d>f$
- Only weakly shielded by other electrons in the same subshell, which are at the same distance from the nucleus
On going across the third period from Na to Ar , for example, each additional electron adds to the same shell (from $3 s^{1}$ for Na to $3 s^{2} 3 p^{6}$ for Ar). Because electrons in the same shell are at approximately the same distance from the nucleus, they are relatively ineffective at shielding one another. At the same time, though, the nuclear charge Z increases from +11 for Na to +18 for Ar. Thus, the effective nuclear charge for the valence-shell electrons increases across the period from 2.20 for Na to 6.75 for Ar, drawing all the valence-shell electrons closer to the nucleus and progressively shrinking the atomic radii (Figure 5.20).

- PROBLEM 5.21 Which atom in each of the following pairs would you expect to be larger? Explain.
(a) Mg or Ba
(b) W or Au
(c) Si or Sn
(d) Ce or Lu

$\sigma$
Core electron configuration does have some effect on the chemistry of an element. Due to filling of the $d$ orbitals, $p$-block elements in period 4 have an additional 10 core electrons relative to elements in period 3. This influences some properties, such as atomic radius. A similar and more dramatic effect, called the lanthanide contraction, caused by $f$ orbital filling, occurs for period $6 d$-block and $p$-block elements.

FIGURE 5.20 Plots of atomic radius and $Z_{\text {eff }}$ for the highest-energy electron versus atomic number. As $Z_{\text {eff }}$ increases, the valence-shell electrons are attracted more strongly to the nucleus, and the atomic radius therefore decreases.

## Interlude The Aurora Borealis: Atomic Spectra on a Grand Scale

Every so often on a clear evening, residents of Alaska, Canada, and other far-northern parts of the world are treated to a breathtaking display of celestial fireworks-the so-called northern lights, or aurora borealis. The lights appear in many different forms-as curtains, arcs, rays, and gauzy patches-and in many different colors. All, however, result from the emission of light by energetically excited atoms, ions, and molecules in the upper atmosphere, the same kind of phenomenon that gives rise to atomic line spectra.

The aurora borealis is caused by a chain of events that begins on the surface of the sun with a massive solar flare. These flares eject a solar "gas" of energetic protons and electrons that reach Earth after about 2 days and are then attracted toward the north and south magnetic poles. (The Southern Hemisphere has its own display of lights called the aurora australis.) The energetic electrons are deflected by the earth's magnetic field into a series of sheetlike beams, much as iron filings scattered around a magnet are deflected into a series of lines by the magnet's field of force. The electrons then collide with $\mathrm{O}_{2}$ and $\mathrm{N}_{2}$ molecules in the upper atmosphere, exciting them, ionizing them, and breaking them apart into O and N atoms.

The energetically excited atoms, ions, and molecules generated by collisions with electrons emit energy of characteristic wavelengths when they decay to their ground states. The $\mathrm{O}_{2}{ }^{+}$ions emit a red light around $630 \mathrm{~nm} ; \mathrm{N}_{2}{ }^{+}$ions emit violet and blue light at 391.4 nm and 470.0 nm ; and O atoms emit a greenish-yellow light at 557.7 nm and a deep red light at 630.0 nm .

Protons in the solar gas are also responsible for part of the auroral display as they too collide with oxygen atoms when they descend into the upper atmosphere. The protons pull electrons from the oxygen atoms, yielding excited $\mathrm{O}^{+}$ions and H atoms that give off still more colors when they return to their ground states. The hydrogen atoms, in particular, emit all the wavelengths of visible light in the Balmer series.

Northern lights are seen almost every night by observers within about 2000 km of the north magnetic pole and are visible in the northern parts of the United States several times a year. They have even been seen as far south as Mexico during times of massive solar disturbances.

- PROBLEM 5.22 Why are the auroras seen primarily near the north and south poles rather than elsewhere on earth?

Understanding the nature of atoms and molecules begins with an understanding of light and other kinds of electromagnetic radiation that make up the electromagnetic spectrum. An electromagnetic wave travels through a vacuum at the speed of light (c) and is characterized by its frequency ( $\nu$ ), wavelength ( $\boldsymbol{\lambda}$ ), and amplitude. Unlike the white light of the sun, which consists of a nearly continuous distribution of wavelengths, the light emitted by an excited atom consists of only a few discrete wavelengths, a so-called line spectrum. The observed wavelengths correspond to the specific energy differences between energies of different orbitals.

Atomic line spectra arise because electromagnetic radiation occurs only in discrete units, or quanta. Just as light behaves in some respects like a stream of small particles (photons), so electrons and other tiny units of matter behave in some respects like waves. The wavelength of a particle of mass $m$ traveling at a velocity $v$ is given by the de Broglie equation, $\lambda=h / m v$, where $h$ is Planck's constant.

The quantum mechanical model proposed in 1926 by Erwin Schrödinger describes an atom by a mathematical equation similar to that used to describe wave motion. The behavior of each electron in an atom is characterized by a wave function, or orbital, the square of which defines the probability of finding the electron in a given volume of space. Each wave function has a set of three variables, called quantum numbers. The principal quantum number $n$ defines the size of the orbital; the angular-momentum quantum number $l$ defines the shape of the orbital; and the magnetic quantum number $m_{l}$ defines the spatial orientation of the orbital. In a hydrogen atom, which contains only one electron, the
energy of an orbital depends only on $n$. In a multielectron atom, the energy of an orbital depends on both $n$ and $l$. In addition, the spin quantum number $m_{s}$ specifies the electron spin as either $+1 / 2$ or $-1 / 2$.

Orbitals can be grouped into successive layers, or shells, according to their principal quantum number $n$. Within a shell, orbitals are grouped into $s, p, d$, and $f$ subshells according to their angular-momentum quantum numbers $l$. An orbital in an $s$ subshell is spherical, an orbital in a $p$ subshell is dumbbell-shaped, and four of the five orbitals in a $d$ subshell are cloverleaf-shaped.

The ground-state electron configuration of a multielectron atom is arrived at by following a series of rules called the aufbau principle.

1. The lowest-energy orbitals fill first.
2. Only two electrons of opposite spin go into any one orbital (the Pauli exclusion principle).
3. If two or more orbitals are equal in energy (degenerate), each is half-filled before any one of them is completely filled (Hund's rule).
The periodic table is the most important organizing principle of chemistry. It is successful because elements in each group of the periodic table have similar valence-shell electron configurations and therefore have similar properties. For example, atomic radii of elements show a periodic rise-andfall pattern according to their position in the table. Atomic radii increase going down a group because $n$ increases, and they decrease from left to right across a period because the effective nuclear charge ( $Z_{\text {eff }}$ ) increases.

## Key Words

amplitude 162
angular-momentum quantum number ( $l$ ) 173
aufbau principle 182
Balmer-Rydberg
equation 165
d-block element 185
de Broglie equation 170
degenerate 182
effective nuclear charge ( $\mathrm{Z}_{\text {eff }}$ ) 181
electromagnetic radiation 162
electromagnetic spectrum 162
electron configuration 182
f-block element 185
frequency ( $\nu$ ) 162
ground-state configuration 182
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Hund's rule 182
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magnetic quantum number $\left(m_{1}\right) \quad 173$<br>node 176<br>orbital 172<br>p-block element 185<br>Pauli exclusion principle 180<br>photon 168<br>principal quantum number ( $n$ ) 173<br>quanta 167<br>quantum mechanical model 171

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( $\boldsymbol{m}_{\boldsymbol{s}}$ ) 180
subshell 173
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wave function 172
wavelength ( $\boldsymbol{\lambda}$ ) 162

## Key Concept Summary

- 





## Understanding Key Concepts

Problems 5.1-5.22 appear within the chapter.
5.23 Where on the blank outline of the periodic table do elements that meet the following descriptions appear?
(a) Elements with the valence-shell ground-state electron configuration $n s^{2} n p^{5}$
(b) An element whose fourth shell contains two $p$ electrons
(c) An element with the ground-state electron configuration [Ar] $4 s^{2} 3 d^{10} 4 p^{5}$

5.24 Where on the periodic table do elements that meet the following descriptions appear?
(a) Elements with electrons whose largest principal quantum number is $n=4$
(b) Elements with the valence-shell ground-state electron configuration $n s^{2} n p^{3}$
(c) Elements that have only one unpaired $p$ electron
(d) The $d$-block elements
(e) The $p$-block elements

5.25 Two electromagnetic waves are represented below.
(a) Which wave has the greater intensity?
(b) Which wave corresponds to higher-energy radiation?
(c) Which wave represents yellow light, and which represents infrared radiation?

(a)

(b)
5.26 What atom has the following orbital-filling diagram?

$$
[A r] \quad \frac{\downarrow \uparrow}{4 s} \quad \underline{\downarrow \uparrow} \frac{\downarrow \uparrow}{} \frac{\downarrow \uparrow}{3 d} \underline{\downarrow \uparrow} \underline{\downarrow \uparrow} \quad-\uparrow \frac{}{4 p}-
$$

5.27 The following orbital-filling diagram represents an excited state rather than the ground state of an atom. Identify the atom, and give it's ground-state electron configuration.

$$
[A r] \quad \frac{\downarrow \uparrow}{4 s} \quad \underline{\downarrow \uparrow} \frac{\downarrow \uparrow}{} \frac{\downarrow \uparrow}{3 d} \underline{\downarrow \uparrow} \underline{\downarrow \uparrow} \quad \underline{\downarrow \uparrow} \frac{\downarrow \uparrow}{4 p}-
$$

5.28 Which of the following three spheres represents a Ca atom, which an Sr atom, and which a Br atom?

5.29 Identify each of the following orbitals, and give $n$ and $l$ quantum numbers for each.

(in third shell)
(a)

(in fourth shell)
(b)

## Additional Problems

## Electromagnetic Radiation

5.30 Which has the higher frequency, red light or violet light? Which has the longer wavelength? Which has the greater energy?
5.31 Which has the higher frequency, infrared light or ultraviolet light? Which has the longer wavelength? Which has the greater energy?
5.32 What is the wavelength (in meters) of ultraviolet light with $\nu=5.5 \times 10^{15} \mathrm{~s}^{-1}$ ?
5.33 What is the frequency of a microwave with $\lambda=4.33 \times$ $10^{-3} \mathrm{~m}$ ?
5.34 Calculate the energies of the following waves (in kilojoules per mole), and tell which member of each pair has the higher value.
(a) An FM radio wave at 99.5 MHz and an AM radio wave at 1150 kHz
(b) An X ray with $\lambda=3.44 \times 10^{-9} \mathrm{~m}$ and a microwave with $\lambda=6.71 \times 10^{-2} \mathrm{~m}$
5.35 The MRI (magnetic resonance imaging) body scanners used in hospitals operate with 400 MHz radiofrequency energy. How much energy does this correspond to in kilojoules per mole?
5.36 What is the wavelength (in meters) of photons with the following energies? In what region of the electromagnetic spectrum does each appear?
(a) $90.5 \mathrm{~kJ} / \mathrm{mol}$
(b) $8.05 \times 10^{-4} \mathrm{~kJ} / \mathrm{mol}$
(c) $1.83 \times 10^{3} \mathrm{~kJ} / \mathrm{mol}$
5.37 What is the energy of each of the following photons in kilojoules per mole?
(a) $\nu=5.97 \times 10^{19} \mathrm{~s}^{-1}$
(b) $\nu=1.26 \times 10^{6} \mathrm{~s}^{-1}$
(c) $\lambda=2.57 \times 10^{2} \mathrm{~m}$
5.38 Protons and electrons can be given very high energies in particle accelerators. What is the wavelength (in meters) of an electron (mass $=9.11 \times 10^{-31} \mathrm{~kg}$ ) that has been accelerated to $99 \%$ of the speed of light? In what region of the electromagnetic spectrum is this wavelength?
5.39 What is the wavelength (in meters) of a proton (mass $=1.673 \times 10^{-24} \mathrm{~g}$ ) that has been accelerated to $25 \%$ of the speed of light? In what region of the electromagnetic spectrum is this wavelength?
5.40 What is the de Broglie wavelength (in meters) of a baseball weighing 145 g and traveling at $156 \mathrm{~km} / \mathrm{h}$ ?
5.41 What is the de Broglie wavelength (in meters) of a mosquito weighing 1.55 mg and flying at $1.38 \mathrm{~m} / \mathrm{s}$ ?
5.42 At what speed (in meters per second) must a 145 g baseball be traveling to have a de Broglie wavelength of 0.500 nm ?
5.43 What velocity would an electron (mass $=9.11 \times$ $10^{-31} \mathrm{~kg}$ ) need for its de Broglie wavelength to be that of red light ( 750 nm )?

## Atomic Spectra

5.44 According to the equation for the Balmer line spectrum of hydrogen, a value of $n=3$ gives a red spectral line at 656.3 nm , a value of $n=4$ gives a green line at 486.1 nm , and a value of $n=5$ gives a blue line at 434.0 nm . Calculate the energy (in kilojoules per mole) of the radiation corresponding to each of these spectral lines.
5.45 According to the values cited in Problem 5.44, the wavelength differences between lines in the Balmer series become smaller as $n$ becomes larger. In other words, the wavelengths converge toward a minimum value as $n$ becomes very large. At what wavelength (in nanometers) do the lines converge?
5.46 The wavelength of light at which the Balmer series converges (Problem 5.45) corresponds to the amount of energy required to completely remove an electron from the second shell of a hydrogen atom. Calculate this energy in kilojoules per mole.
5.47 Lines in the Brackett series of the hydrogen spectrum are caused by emission of energy accompanying the fall of an electron from outer shells to the fourth shell. The lines can be calculated using the Balmer-Rydberg equation:

$$
\frac{1}{\lambda}=R\left(\frac{1}{m^{2}}-\frac{1}{n^{2}}\right)
$$

where $m=4, R=1.097 \times 10^{-2} \mathrm{~nm}^{-1}$, and $n$ is an integer greater than 4 . Calculate the wavelengths (in nanometers) and energies (in kilojoules per mole) of the first two lines in the Brackett series. In what region of the electromagnetic spectrum do they fall?
5.48 Sodium atoms emit light with a wavelength of 330 nm when an electron moves from a $4 p$ orbital to a $3 s$ orbital. What is the energy difference between the orbitals in kilojoules per mole?
5.49 Excited rubidium atoms emit red light with $\lambda=795 \mathrm{~nm}$. What is the energy difference (in kilojoules per mole) between orbitals that give rise to this emission?

## Orbitals and Quantum Numbers

5.50 What are the four quantum numbers, and what does each specify?
5.51 What is the Heisenberg uncertainty principle, and how does it affect our description of atomic structure?
5.52 Why do we have to use an arbitrary value such as $95 \%$ to determine the spatial limitations of an orbital?
5.53 How many nodal surfaces does a $4 s$ orbital have? Draw a cutaway representation of a $4 s$ orbital showing the nodes and the regions of maximum electron probability.
5.54 What is meant by the term effective nuclear charge, $Z_{\text {eff }}$, and what is it due to?
5.55 How does electron shielding in multielectron atoms give rise to energy differences among $3 s, 3 p$, and $3 d$ orbitals?
5.56 Give the allowable combinations of quantum numbers for each of the following electrons:
(a) A $4 s$ electron
(b) A $3 p$ electron
(c) A $5 f$ electron
(d) A 5d electron
5.57 Give the orbital designations of electrons with the following quantum numbers:
(a) $n=3, l=0, m_{l}=0$
(b) $n=2, l=1, m_{l}=-1$
(c) $n=4, l=3, m_{l}=-2$
(d) $n=4, l=2, m_{l}=0$
5.58 Tell which of the following combinations of quantum numbers are not allowed. Explain your answers.
(a) $n=3, l=0, m_{l}=-1$
(b) $n=3, l=1, m_{l}=1$
(c) $n=4, l=4, m_{l}=0$
5.59 Which of the following combinations of quantum numbers can refer to an electron in a ground-state cobalt atom ( $Z=27$ )?
(a) $n=3, l=0, m_{l}=2$
(b) $n=4, l=2, m_{l}=-2$
(c) $n=3, l=1, m_{l}=0$
5.60 What is the maximum number of electrons in an atom whose highest-energy electrons have the principal quantum number $n=5$ ?
5.61 What is the maximum number of electrons in an atom whose highest-energy electrons have the principal quantum number $n=4$ and the angular-momentum quantum number $l=0$ ?
5.62 Use the Heisenberg uncertainty principle to calculate the uncertainty (in meters) in the position of a honeybee weighing 0.68 g and traveling at a velocity of $0.85 \mathrm{~m} / \mathrm{s}$. Assume that the uncertainty in the velocity is $0.1 \mathrm{~m} / \mathrm{s}$.
5.63 The mass of a helium atom is 4.0026 amu , and its average velocity at $25^{\circ} \mathrm{C}$ is $1.36 \times 10^{3} \mathrm{~m} / \mathrm{s}$. What is the uncertainty (in meters) in the position of a helium atom if the uncertainty in its velocity is $1 \%$ ?

## Electron Configurations

5.64 Why does the number of elements in successive periods of the periodic table increase by the progression 2, $8,18,32$ ?
5.65 Which two of the four quantum numbers determine the energy level of an orbital in a multielectron atom?
5.66 Which orbital in each of the following pairs is higher in energy?
(a) $5 p$ or $5 d$
(b) $4 s$ or $3 p$
(c) $6 s$ or $4 d$
5.67 Order the orbitals for a multielectron atom in each of the following lists according to increasing energy:
(a) $4 d, 3 p, 2 p, 5 s$
(b) $2 s, 4 s, 3 d, 4 p$
(c) $6 s, 5 p, 3 d, 4 p$
5.68 According to the aufbau principle, which orbital is filled immediately after each of the following in a multielectron atom?
(a) $4 s$
(b) $3 d$
(c) $5 f$
(d) $5 p$
5.69 According to the aufbau principle, which orbital is filled immediately before each of the following?
(a) $3 p$
(b) $4 p$
(c) $4 f$
(d) $5 d$
5.70 Give the expected ground-state electron configurations for the following elements:
(a) Ti
(b) Ru
(c) Sn
(d) Sr
(e) Se
5.71 Give the expected ground-state electron configurations for atoms with the following atomic numbers:
(a) $Z=55$
(b) $Z=40$
(c) $Z=80$
(d) $Z=62$
5.72 Draw orbital-filling diagrams for the following atoms. Show each electron as an up or down arrow, and use the abbreviation of the preceding noble gas to represent inner-shell electrons.
(a) Rb
(b) W
(c) Ge
(d) Zr
5.73 Draw orbital-filling diagrams for atoms with the following atomic numbers. Show each electron as an up or down arrow, and use the abbreviation of the preceding noble gas to represent inner-shell electrons.
(a) $Z=25$
(b) $Z=56$
(c) $Z=28$
(d) $Z=47$
5.74 Order the electrons in the following orbitals according to their shielding ability: $4 s, 4 d, 4 f$.
5.75 Order the following elements according to increasing $Z_{\text {eff }}: \mathrm{Ca}, \mathrm{Se}, \mathrm{Kr}, \mathrm{K}$.
5.76 What is the expected ground-state electron configuration of the recently discovered element with $Z=116$ ?
5.77 What is the atomic number and expected ground-state electron configuration of the yet undiscovered element directly below Fr in the periodic table?
5.78 How many unpaired electrons are present in each of the following ground-state atoms?
(a) O
(b) Si
(c) K
(d) As
5.79 Identify the following atoms:
(a) It has the ground-state electron configuration [Ar] $3 d^{10} 4 s^{2} 4 p^{1}$.
(b) It has the ground-state electron configuration $[\mathrm{Kr}] 4 d^{10}$.
5.80 At what atomic number is the filling of a $g$ orbital likely to begin?
5.81 Assuming that $g$ orbitals fill according to Hund's rule, what is the atomic number of the first element to have a filled $g$ orbital?

## Atomic Radii and Periodic Properties

5.82 Why do atomic radii increase going down a group of the periodic table?
5.83 Why do atomic radii decrease from left to right across a period of the periodic table?
5.84 Order the following atoms according to increasing atomic radius: $\mathrm{S}, \mathrm{F}, \mathrm{O}$.
5.85 Which atom in each of the following pairs has a larger radius?
(a) Na or K
(b) V or Ta
(c) V or Zn
(d) Li or Ba
5.86 The amount of energy that must be added to remove an electron from a neutral atom to give a cation is called the atom's ionization energy. Which would you expect to have the larger ionization energy, Na or Mg ? Explain.
5.87 The amount of energy released when an electron adds to a neutral atom to give an anion is called the atom's electron affinity. Which would you expect to have the larger electron affinity, C or F? Explain.

## General Problems

5.88 Use the Balmer equation to calculate the wavelength (in nanometers) of the spectral line for hydrogen when $n=6$. What is the energy (in kilojoules per mole) of the radiation corresponding to this line?
5.89 Lines in the Pfund series of the hydrogen spectrum are caused by emission of energy accompanying the fall of an electron from outer shells to the fifth shell. Use the Balmer-Rydberg equation to calculate the wavelengths (in nanometers) and energies (in kilojoules per mole) of the two longest-wavelength lines in the Pfund series. In what region of the electromagnetic spectrum do they fall?
5.90 What is the shortest wavelength (in nanometers) in the Pfund series (Problem 5.89) for hydrogen?
5.91 What is the wavelength (in meters) of photons with the following energies? In what region of the electromagnetic spectrum does each appear?
(a) $142 \mathrm{~kJ} / \mathrm{mol}$
(b) $4.55 \times 10^{-2} \mathrm{~kJ} / \mathrm{mol}$
(c) $4.81 \times 10^{4} \mathrm{~kJ} / \mathrm{mol}$
5.92 What is the energy of each of the following photons in kilojoules per mole?
(a) $\nu=3.79 \times 10^{11} \mathrm{~s}^{-1}$
(b) $\nu=5.45 \times 10^{4} \mathrm{~s}^{-1}$
(c) $\lambda=4.11 \times 10^{-5} \mathrm{~m}$
5.93 The second in the SI system is defined as the duration of $9,192,631,770$ periods of radiation corresponding to the transition between two energy levels of a cesium-133 atom. What is the energy difference between the two levels in kilojoules per mole?
5.94 Write the symbol, give the ground-state electron configuration, and draw an orbital-filling diagram for each
of the following atoms. Use the abbreviation of the preceding noble gas to represent the inner-shell electrons.
(a) The heaviest alkaline earth metal
(b) The lightest transition metal
(c) The heaviest actinide metal
(d) The lightest semimetal
(e) The group 6A element in the fifth period
5.95 Imagine a universe in which the four quantum numbers can have the same possible values as in our universe except that the angular-momentum quantum number $l$ can have integral values of $0,1,2, \ldots, n+1$ (instead of $0,1,2, \ldots, n-1$ ).
(a) How many elements would be in the first two rows of the periodic table in this universe?
(b) What would be the atomic number of the element in the second row and fifth column?
(c) Draw an orbital-filling diagram for the element with atomic number 12.
5.96 Cesium metal is frequently used in photoelectric cells because the amount of energy necessary to eject electrons from a cesium surface is relatively small-only $206.5 \mathrm{~kJ} / \mathrm{mol}$. What wavelength of light (in nanometers) does this correspond to?
5.97 The laser light used in compact disc players has $\lambda=780 \mathrm{~nm}$. In what region of the electromagnetic spectrum does this light appear? What is the energy of this light in kilojoules per mole?
5.98 Draw orbital-filling diagrams for the following atoms. Show each electron as an up or down arrow, and use the abbreviation of the preceding noble gas to represent inner-shell electrons.
(a) Sr
(b) Cd
(c) $\mathrm{Has} \mathrm{Z}=22$
(d) Has $Z=34$
5.99 The atomic radii of $\mathrm{Y}(180 \mathrm{pm})$ and $\mathrm{La}(187 \mathrm{pm})$ are significantly different, but the radii of $\mathrm{Zr}(160 \mathrm{pm})$ and Hf ( 159 pm ) are essentially identical. Explain.
5.100 One method for calculating $Z_{\text {eff }}$ is to use the equation

$$
Z_{\mathrm{eff}}=\sqrt{\frac{(E)\left(n^{2}\right)}{1312 \mathrm{~kJ} / \mathrm{mol}}}
$$

where $E$ is the energy necessary to remove an electron from an atom and $n$ is the principal quantum number of the electron. Use this equation to calculate $Z_{\text {eff }}$ values for the highest-energy electrons in potassium ( $E=$ $418.8 \mathrm{~kJ} / \mathrm{mol}$ ) and krypton ( $E=1350.7 \mathrm{~kJ} / \mathrm{mol}$ ).
5.101 One watt (W) is equal to $1 \mathrm{~J} / \mathrm{s}$. Assuming that $5.0 \%$ of the energy output of a 75 W lightbulb is visible light and that the average wavelength of the light is 550 nm , how many photons are emitted by the lightbulb each second?
5.102 Microwave ovens work by irradiating food with microwave radiation, which is absorbed and converted into heat. Assuming that radiation with $\lambda=15.0 \mathrm{~cm}$ is used, that all the energy is converted to heat, and that 4.184 J is needed to raise the temperature of 1.00 g of water by $1.00^{\circ} \mathrm{C}$, how many photons are necessary to raise the temperature of a 350 mL cup of water from $20^{\circ} \mathrm{C}$ to $95^{\circ} \mathrm{C}$ ?
5.103 Photochromic sunglasses, which darken when exposed to light, contain a small amount of colorless $\mathrm{AgCl}(\mathrm{s})$ embedded in the glass. When irradiated with light, metallic silver atoms are produced and the glass darkens: $\mathrm{AgCl}(s) \rightarrow \mathrm{Ag}(s)+\mathrm{Cl}$. Escape of the chlorine atoms is prevented by the rigid structure of the glass, and the reaction therefore reverses as soon as the light is removed. If $310 \mathrm{~kJ} / \mathrm{mol}$ of energy is required to make the reaction proceed, what wavelength of light is necessary?
5.104 The amount of energy necessary to remove an electron from an atom is a quantity called the ionization energy, $E_{i}$. This energy can be measured by a technique called photoelectron spectroscopy, in which light of wavelength $\lambda$ is directed at an atom, causing an electron to be ejected. The kinetic energy of the ejected electron $\left(E_{\mathrm{k}}\right)$ is measured by determining its velocity, $v\left(E_{\mathrm{k}}=m v^{2} / 2\right)$, and $E_{\mathrm{i}}$ is then calculated using the conservation of energy principle. That is, the energy of the incident light equals $E_{\mathrm{i}}$ plus $E_{\mathrm{k}}$. What is the ionization energy of selenium atoms (in kilojoules per mole) if light with $\lambda=48.2 \mathrm{~nm}$ produces electrons with a velocity of $2.371 \times 10^{6} \mathrm{~m} / \mathrm{s}$ ? The mass, $m$, of an electron is $9.109 \times 10^{-31} \mathrm{~kg}$.
5.105 X rays with a wavelength of $1.54 \times 10^{-10} \mathrm{~m}$ are produced when a copper metal target is bombarded with high-energy electrons that have been accelerated by a voltage difference of $30,000 \mathrm{~V}$. The kinetic energy of the electrons equals the product of the voltage difference and the electronic charge in coulombs, where 1 volt-coulomb $=1 \mathrm{~J}$.
(a) What is the kinetic energy (in joules) and the de Broglie wavelength (in meters) of an electron that has been accelerated by a voltage difference of $30,000 \mathrm{~V}$ ?
(b) What is the energy (in joules) of the X rays emitted by the copper target?
5.106 In the Bohr model of atomic structure, electrons are constrained to orbit a nucleus at specific distances, given by the equation

$$
r=\frac{n^{2} a_{0}}{Z}
$$

where $r$ is the radius of the orbit, $Z$ is the charge on the nucleus, $a_{0}$ is the Bohr radius and has a value of $5.292 \times 10^{-11} \mathrm{~m}$, and $n$ is a positive integer ( $n=$ $1,2,3, \ldots$ ) like the principal quantum number in the Schrödinger wave equation. Furthermore, Bohr concluded that the energy level $E$ of an electron in a given orbit is

$$
E=\frac{-Z e^{2}}{2 r}
$$

where $e$ is the charge on an electron. Derive an equation that will let you calculate the difference $\Delta E$ between any two energy levels. What relation does your equation have to the Balmer-Rydberg equation?
5.107 Assume that the rules for quantum numbers are different and that the spin quantum number $m_{\mathrm{s}}$ can have any of three values, $m_{\mathrm{s}}=-1 / 2,0,+1 / 2$, while all other rules remain the same.
(a) Draw an orbital-filling diagram for the element with $Z=25$, showing the individual electrons in the outermost subshell as up arrows, down arrows, or 0 . How many partially filled orbitals does the element have?
(b) What is the atomic number of the element in the 3 rd column of the 4th row under these new rules? What block does it belong to ( $s, p, d$, or $f$ )?
5.108 Given the subshells $1 s, 2 s, 2 p, 3 s, 3 p$, and $3 d$, identify those that meet the following descriptions:
(a) Has $l=2$
(b) Can have $m_{1}=-1$
(c) Is empty in a nitrogen atom
(d) Is full in a carbon atom
(e) Contains the outermost electrons in a beryllium atom
(f) Can contain two electrons, both with spin $m_{\mathrm{s}}=+1 / 2$
5.109 A hydrogen atom with an electron in the first shell ( $n=1$ ) absorbs ultraviolet light with a wavelength of $1.03 \times 10^{-7} \mathrm{~m}$. To what shell does the electron jump?
5.110 A minimum energy of $7.21 \times 10^{-19} \mathrm{~J}$ is required to produce the photoelectric effect in chromium metal.
(a) What is the minimum frequency of light needed to remove an electron from chromium?
(b) Light with a wavelength of $2.50 \times 10^{-7} \mathrm{~m}$ falls on a piece of chromium in an evacuated glass tube. What is the minimum de Broglie wavelength of the emitted electrons? (Note that the energy of the incident light must be conserved; that is, the photon's energy must equal the sum of the energy needed to eject the electron plus the kinetic energy of the electron.)

## Multi-Concept Problems

5.111 A photon produced by an X-ray machine has an energy of $4.70 \times 10^{-16} \mathrm{~J}$.
(a) What is the frequency of the photon?
(b) What is the wavelength of radiation of frequency (a)?
(c) What is the velocity of an electron with a de Broglie wavelength equal to (b)?
(d) What is the kinetic energy of an electron traveling at velocity (c)?
5.112 An energetically excited hydrogen atom has its electron in a $5 f$ subshell. The electron drops down to the $3 d$ subshell, releasing a photon in the process.
(a) Give the $n$ and $l$ quantum numbers for both subshells, and give the range of possible $m_{1}$ quantum numbers.
(b) What wavelength of light is emitted by the process?
(c) The hydrogen atom now has a single electron in the $3 d$ subshell. What is the energy (in $\mathrm{kJ} / \mathrm{mol}$ ) required to remove this electron?
5.113 Consider the noble gas xenon.
(a) Write the electron configuration of xenon using the abbreviation of the previous noble gas.
(b) When xenon absorbs $801 \mathrm{~kJ} / \mathrm{mol}$ of energy, it is excited into a higher-energy state in which the outermost electron has been promoted to the next available subshell. Write the electron configuration for this excited xenon.
(c) The energy required to completely remove the outermost electron from the excited xenon atom is $369 \mathrm{~kJ} / \mathrm{mol}$, almost identical to that of cesium ( $376 \mathrm{~kJ} / \mathrm{mol}$ ). Explain.
5.114 A 1.000 g sample of alkaline earth metal M reacts completely with 0.8092 g of chlorine gas $\left(\mathrm{Cl}_{2}\right)$ to yield an ionic product with the formula $\mathrm{MCl}_{2}$. In the process, 9.46 kJ of heat is released.
(a) What is the molecular mass and identity of the metal M?
(b) How much heat (in kilojoules) would be released by reaction of 1.000 mol of M with a stoichiometric amount of $\mathrm{Cl}_{2}$ ?
5.115 A certain semimetal $M$ emits electrons only when struck by radiation with a minimum frequency of $9.07 \times 10^{14} \mathrm{~s}^{-1}$. On heating a 0.200 g sample of the semimetal in air, the corresponding oxide $\mathrm{M}_{2} \mathrm{O}_{3}$ was obtained. When the oxide was dissolved in aqueous acid and titrated with $\mathrm{KMnO}_{4}, 10.7 \mathrm{~mL}$ of 0.100 M $\mathrm{MnO}_{4}^{-}$was required to reach an equivalence point. The unbalanced equation is

$$
\begin{aligned}
\mathrm{H}_{3} \mathrm{MO}_{3}(a q)+ & \mathrm{MnO}_{4}^{-}(a q) \\
& \longrightarrow \\
\mathrm{H}_{3} \mathrm{MO}_{4}(a q)+\mathrm{Mn}^{2+} & (\text { In acid })
\end{aligned}
$$

(a) Balance the equation.
(b) How many moles of oxide were formed, and how many moles of semimetal were in the initial 0.200 g sample?
(c) What is the identity of the semimetal M?
(d) What is the minimum energy (in kilojoules per mole) required to cause the semimetal to emit electrons?

## eMedia Problems

5.116 The Electromagnetic Spectrum activity (eChapter 5.2) allows you to determine the frequency and wavelength of any color of visible light.
(a) Use the activity to determine the range of wavelengths (in nm ) for red light, yellow light, and blue light.
(b) For each color in part (a), determine the range of frequencies (in s ${ }^{-1}$ ) and the range of photon energies (in $\mathrm{kJ} / \mathrm{mol}$ ).
(c) What happens to the value of the frequency as the wavelength increases?
(d) What happens to the value of the energy of the photon as the wavelength increases?
5.117 According to the Photoelectric Effect movie (eChapter 5.4), photons must have sufficient energy to cause the electrode to release electrons. What determines the energy of the photons? What does the intensity of the light determine?
5.118 View the electron density plots for the noble gases helium, neon, and argon in the Radial Electron Distribution movie (eChapter 5.8).
(a) What do maxima in the distribution represent? Which quantum number determines this characteristic?
(b) Why is the first maximum for helium at such a greater distance from the nucleus than are the first maxima for neon and argon?
(c) Even though neon has a greater nuclear charge than does helium, its outermost maximum is farther from the nucleus than the outermost maximum of helium. What accounts for the increased relative size of the neon atom? Does the Effective Nuclear Charge movie (eChapter 5.11) confirm your answer?
5.119 Use the Electron Configuration activity in eChapter 5.12 to determine the subshell being filled as you move across a period in each of the following groups of elements:
(a) Groups 1A and 2A
(b) Groups 3A through 8A
(c) The transition metals
(d) The inner transition metals
5.120 Use the Interactive Periodic Table in eChapter 5.15 to determine the trend in atomic radius as you move across a period and as you move down a group. Explain the factors that account for these trends.

## Chapter

## 6

## Ionic Bonds and Some Main-Group Chemistry

## What holds atoms together in chemical compounds? Cer-

 tainly, there must be some force holding them together; otherwise, they would simply fly apart. As we saw briefly in Section 2.8, the forces that hold atoms together are called chemical bonds and are of two types-ionic bonds and covalent bonds. In this and the next two chapters, we'll look at the nature of chemical bonds and at the energy changes that accompany their formation
## CONTENTS

This beautiful chandelier was carved entirely out of salt by miners in the 900 year old Wieliczka salt mine in Poland.
$\begin{array}{cl}\text { 6.1 } & \text { Ions and Their Electron } \\ & \text { Configurations } \\ \text { 6.2 } & \text { Ionic Radii } \\ 6.3 & \text { Ionization Energy } \\ 6.4 & \text { Higher Ionization Energies } \\ 6.5 & \text { Electron Affinity } \\ 6.6 & \text { Ionic Bonds and the Formation of } \\ & \text { Ionic Solids } \\ \text { 6.7 } & \text { The Alkali Metals (Group 1A) }\end{array}$
6.8 The Alkaline Earth Metals (Group 2A)
6.9 The Group 3A Elements: Aluminum
6.10 The Halogens (Group 7A)
6.11 The Noble Gases (Group 8A)
6.12 The Octet Rule

- Interlude-Salt


Electrons are always lost from orbitals having the highest value of the principal quantum number, $n$, before they are lost from orbitals with lower values of $n$.
and breakage. We'll begin in the present chapter with a look at ions and the ionic bonds formed between halogens and main-group metals.

### 6.1 Ions and Their Electron Configurations

We've seen on numerous occasions that metallic elements on the left side of the periodic table have a tendency to give up electrons and form cations, while the halogens and a few other nonmetallic elements on the right side of the table have a tendency to accept electrons and form anions. What are the ground-state electron configurations of the resultant ions?

For main-group elements, the electrons given up by a metal in forming a cation come from the highest-energy occupied orbital, while the electrons that are accepted by a nonmetal in forming an anion go into the lowest-energy unoccupied orbital according to the aufbau principle (Section 5.12). When a sodium atom ( $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{1}$ ) gives up an electron, for example, the valence-shell $3 s$ electron is lost, giving an $\mathrm{Na}^{+}$ion with the stable, noble gas electron configuration of neon ( $1 s^{2} 2 s^{2} 2 p^{6}$ ). Similarly, when a chlorine atom ( $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{5}$ ) accepts an electron, the electron fills the remaining vacancy in the $3 p$ subshell to give a $\mathrm{Cl}^{-}$ion with the noble gas electron configuration of argon $\left(1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6}\right)$.

$$
\begin{gathered}
\text { Na: } 1 s^{2} 2 s^{2} 2 p^{6} 3 s^{1} \xrightarrow{-e^{-}} \mathbf{N a}^{+}: 1 s^{2} 2 s^{2} 2 p^{6} \\
\mathbf{C l}: 1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{5} \xrightarrow{+e^{-}} \mathbf{C l}^{-}: 1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6}
\end{gathered}
$$

What is true for sodium is also true for the other elements in group 1A: All form positive ions by losing their valence-shell $s$ electron, and all the resultant ions have noble gas electron configurations. Similarly for the elements in group 2A: All form a doubly positive ion by losing both their valence-shell $s$ electrons. An Mg atom ( $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2}$ ), for example, goes to an $\mathrm{Mg}^{2+}$ ion with the neon configuration $1 s^{2} 2 s^{2} 2 p^{6}$ by loss of its two $3 s$ electrons.

Group 1A atom: [Noble gas] $n s^{1} \xrightarrow{-\mathrm{e}^{-}}$Group 1A ion ${ }^{+}$: [Noble gas]
Group 2A atom: [Noble gas] $n s^{2} \xrightarrow{-2 \mathrm{e}^{-}}$Group 2A ion $^{2+}$ : [Noble gas]
Just as the group 1A and 2A metals lose the appropriate number of electrons to yield ions with noble gas configurations, the group 6A and group 7A nonmetals gain the appropriate number of electrons. The halogens in group 7A gain one electron to form singly charged anions with noble gas configurations, and the elements in group 6A gain two electrons to form doubly charged anions with noble gas configurations. Oxygen $\left(1 s^{2} 2 s^{2} 2 p^{4}\right)$, for example, becomes the $\mathrm{O}^{2-}$ ion with the neon configuration $\left(1 s^{2} 2 s^{2} 2 p^{6}\right)$.
Group 6A atom: [Noble gas] $n s^{2} n p^{4} \xrightarrow{+2 e^{-}}$Group 6A ion ${ }^{2-}$ : [Noble gas] $n s^{2} n p^{6}$
Group 7A atom: [Noble gas] $n s^{2} n p^{5} \xrightarrow{+e^{-}}$Group 7A ion ${ }^{-}$: [Noble gas] $n s^{2} n p^{6}$
The formulas and electron configurations of the most common main-group ions are listed in Table 6.1.

The situation is a bit different for the formation of ions from the transition metal elements than it is for the main-group elements. Transition metals form cations by first losing their valence-shell $s$ electrons and then losing $d$ electrons. As a result, all the remaining valence electrons in transition metal cations occupy $d$ orbitals. Iron, for instance, forms the $\mathrm{Fe}^{2+}$ ion by losing its two $4 s$ electrons and forms the $\mathrm{Fe}^{3+}$ ion by losing two $4 s$ electrons and one $3 d$ electron:

$$
\begin{aligned}
& \text { Fe: }[\mathrm{Ar}] 4 s^{2} 3 d^{6} \xrightarrow{-2 e^{-}} \mathbf{F e}^{2+}:[\mathrm{Ar}] 3 d^{6} \\
& \text { Fe: }[\mathrm{Ar}] 4 s^{2} 3 d^{6} \xrightarrow{-3 e^{-}} \mathbf{F e}^{3+}:[\mathrm{Ar}] 3 d^{5}
\end{aligned}
$$

| TABLE 6.1 | Some Common Main-Group Ions and Their Noble Gas Electron Configurations |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Group 1A | Group $2 \mathrm{~A}$ | Group $\mathbf{3 A}$ | Group 6A | Group 7A | Electron Configuration |
| $\mathrm{H}^{+}$ |  |  |  |  | [None] |
| $\mathrm{H}^{-}$ |  |  |  |  | [He] |
| $\mathrm{Li}^{+}$ | $\mathrm{Be}^{2+}$ |  |  |  | [He] |
| $\mathrm{Na}^{+}$ | $\mathrm{Mg}^{2+}$ | $\mathrm{Al}^{3+}$ | $\mathrm{O}^{2-}$ | $\mathrm{F}^{-}$ | [ Ne ] |
| $\mathrm{K}^{+}$ | $\mathrm{Ca}^{2+}$ | *Ga ${ }^{3+}$ | $\mathrm{S}^{2-}$ | $\mathrm{Cl}^{-}$ | [Ar] |
| $\mathrm{Rb}^{+}$ | $\mathrm{Sr}^{2+}$ | ${ }^{*} \mathrm{In}^{3+}$ | $\mathrm{Se}^{2-}$ | $\mathrm{Br}^{-}$ | [Kr] |
| $\mathrm{Cs}^{+}$ | $\mathrm{Ba}^{2+}$ | ${ }^{*} \mathrm{Tl}^{3+}$ | Te ${ }^{2-}$ | $\mathrm{I}^{-}$ | [Xe] |

*These ions do not have a true noble gas electron configuration because they have an additional filled $d$ subshell.

It may seem strange that building up the periodic table adds the $3 d$ electrons after the $4 s$ electrons, whereas ion formation from a transition metal removes the 4 s electrons before the $3 d$ electrons. Note, though, that the two processes are not the reverse of each other, so they can't be compared directly. Building up the periodic table adds one electron to the valence shell and also adds one positive charge to the nucleus, whereas ion formation removes an electron from the valence shell but does not alter the nucleus.

PROBLEM 6.1 Predict the ground-state electron configuration for each of the following ions, and explain your answers.
(a) $\mathrm{Ra}^{2+}$
(b) $\mathrm{La}^{3+}$
(c) $\mathrm{Ti}^{4+}$
(d) $\mathrm{N}^{3-}$

- PROBLEM 6.2 What doubly positive ion has the following ground-state electron configuration? $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6} 3 d^{10}$


### 6.2 Ionic Radii

Just as there are systematic differences in the sizes of atoms (Section 5.15), there are also systematic differences in the sizes of ions. As shown in Figure 6.1 for the elements of groups 1 A and 2 A , atoms shrink dramatically when an electron is removed to form a cation. The radius of an Na atom, for example, is 186 pm , while that of an $\mathrm{Na}^{+}$cation is 102 pm . Similarly, the radius of an Mg atom is 160 pm , and that of an $\mathrm{Mg}^{2+}$ cation is 72 pm .

The cation that results when an electron is removed from a neutral atom is smaller than the atom both because the electron is removed from a large, valenceshell orbital and because there is an increase in $Z_{\text {eff }}$ (Section 5.11). On going from a neutral Na atom to a charged $\mathrm{Na}^{+}$cation, for example, the electron configuration

- FIGURE 6.1 Radii of (a) group 1 A atoms and their cations; (b) group 2A atoms and their cations. The cations are smaller than the neutral atoms both because the principal quantum number of the valence-shell electrons is smaller for the cations and because $Z_{\text {eff }}$ is larger.


The larger the proton-toelectron ratio, the greater the attraction of the nucleus for the valence electrons and the smaller the size of the ion.
changes from $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{1}$ to $1 s^{2} 2 s^{2} 2 p^{6}$. The valence shell of the Na atom is the third shell, but the valence shell of the $\mathrm{Na}^{+}$cation is the second shell. Thus, the $\mathrm{Na}^{+}$ ion has a smaller valence shell than the Na atom and therefore a smaller size. In addition, the effective nuclear charge felt by the valence-shell electrons is greater in the $\mathrm{Na}^{+}$cation than in the neutral atom. The Na atom has 11 protons and 11 electrons, but the $\mathrm{Na}^{+}$cation has 11 protons and only 10 electrons. The smaller number of electrons in the cation means that they shield one another to a lesser extent and therefore feel a stronger pull toward the nucleus.

The same effects felt by the group 1A elements when a single electron is lost are felt by the group 2 A elements when two electrons are lost. For example, loss of two valence-shell electrons from an Mg atom $\left(1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2}\right)$ gives the $\mathrm{Mg}^{2+}$ cation $\left(1 s^{2} 2 s^{2} 2 p^{6}\right)$. The smaller valence shell of the $\mathrm{Mg}^{2+}$ cation and the increase in effective nuclear charge combine to cause a dramatic shrinkage. In the same way, a similar shrinkage is encountered whenever any of the metal atoms on the left-hand two-thirds of the periodic table is converted into a cation.

Just as atoms shrink when converted to cations by loss of an electron, they expand when converted to anions by gain of an electron. As shown in Figure 6.2 for the group 7A elements (halogens), the expansion is dramatic. Chlorine, for example, nearly doubles in size, from 99 pm for the neutral atom to 184 pm for the chloride anion.

FIGURE 6.2 Radii of the group 7A atoms (halogens) and their anions. The anions are larger than the neutral atoms because of additional electron-electron repulsions and a decrease in $\mathrm{Z}_{\text {eff }}$.

## s



The expansion that occurs when a group 7A atom gains an electron to yield an anion can't be accounted for by a change in the quantum number of the valence shell, because the added electron simply completes an already occupied $p$ subshell: [ Ne ] $3 s^{2} 3 p^{5}$ for a Cl atom becomes $[\mathrm{Ne}] 3 s^{2} 3 p^{6}$ for a $\mathrm{Cl}^{-}$anion, for example. Thus, the expansion is due entirely to the decrease in effective nuclear charge and the increase in electron-electron repulsions that occurs when an extra electron is added.

- PROBLEM 6.3 Which atom or ion in each of the following pairs would you expect to be larger? Explain.
(a) $\mathrm{O}_{\text {or }} \mathrm{O}^{2-}$
(b) O or S
(c) Fe or $\mathrm{Fe}^{3+}$
(d) $\mathrm{H}_{\mathrm{H}}$ or $\mathrm{H}^{-}$
-KEY CONCEPT PROBLEM 6.4 Which of the following spheres represents a $\mathrm{K}^{+}$ ion, which a K atom, and which a $\mathrm{Cl}^{-}$ion?



## 6.3 | Ionization Energy

We saw in the previous chapter that the absorption of light energy by an atom leads to a change in electron configuration. A valence-shell electron is promoted from a lower-energy orbital to a higher-energy one with a larger principal quantum
number $n$. If enough energy is absorbed, the electron can be removed completely from the atom, leaving behind an ion. The amount of energy necessary to remove the highest-energy electron from an isolated neutral atom in the gaseous state is called the atom's ionization energy, abbreviated $E_{i}$. For hydrogen atoms, $1312.0 \mathrm{~kJ} / \mathrm{mol}$ is needed.


As shown by the plot in Figure 6.3, ionization energies differ widely, from a low of $375.7 \mathrm{~kJ} / \mathrm{mol}$ for cesium to a high of $2372.3 \mathrm{~kJ} / \mathrm{mol}$ for helium. Furthermore, there is a clear periodicity to the data. The minimum $E_{\mathrm{i}}$ values correspond to the group 1A elements (alkali metals), the maximum $E_{i}$ values correspond to the group 8A elements (noble gases), and a gradual increase in $E_{\mathrm{i}}$ occurs from left to right across a row of the periodic table-from Na to Ar, for example. Note that all the values are positive, meaning that energy is always required to remove an electron from an atom.


The periodicity evident in Figure 6.3 can be explained by looking at electron configurations. Atoms of the group 8A elements have filled valence subshells, either $s$ (for helium) or both $s$ and $p$ (for the other noble gases). As we saw in Section 5.15, an electron in a filled valence subshell feels a relatively high $Z_{\text {eff }}$ because electrons within the same subshell don't shield one another very strongly. As a result, the electrons are held tightly to the nucleus, the radius of the atom is small, and the energy necessary to remove an electron is relatively large. Atoms of group 1A elements, by contrast, have only a single $s$ electron in their valence shell. This single valence electron is well shielded from the nucleus by all the inner-shell electrons, called the core electrons, resulting in a low $Z_{\text {eff }}$. The valence electron is thus held loosely, and the energy necessary to remove it is relatively small.

The three-dimensional display of ionization energies in Figure 6.4 shows that there are other trends in the data beyond the periodicity. One such trend is that ionization energies gradually decrease going down a group in the periodic table, from Li to Fr and from He to Rn , for example. As atomic number increases going down a group, both the principal quantum number of the valence-shell electrons and their average distance from the nucleus also increase. As a result, the valence-shell electrons are less tightly held, and $E_{\mathrm{i}}$ is smaller.


4 FIGURE 6.3 Ionization energies of the first 92 elements. There is a clear periodicity to the data, with maximum values for the noble gas elements and minimum values for the alkali metals.

## r

- 

Core electrons shield valence electrons effectively; electrons in the same shell shield one another less effectively.

$\square$
The closer an electron is to the nucleus, the higher its ionization energy. Hence, small atoms have high ionization energies. Due to its small size, the first element in every group tends to differ significantly from the other elements in the same group.

FIGURE 6.4 A threedimensional display showing how ionization energies increase from left to right across a row and decrease from top to bottom down a group of the periodic table. The elements at the lower left therefore have the smallest $E_{i}$ values, and the elements at the upper right have the largest.

FIGURE 6.5 Ionization energies of the first 20 elements. The group 2A elements ( $\mathrm{Be}, \mathrm{Mg}$, and Ca ) have slightly larger $E_{\mathrm{i}}$ values than might be expected, and the group 6A elements ( $O$ and S) have slightly smaller values than might be expected.


Still another feature of the $E_{\mathrm{i}}$ data is that minor irregularities occur across a row of the periodic table. As shown by the close-up look at $E_{\mathrm{i}}$ values of the first 20 elements (Figure 6.5), the $E_{\mathrm{i}}$ of beryllium is larger than that of its neighbor boron, and the $E_{\mathrm{i}}$ of nitrogen is larger than that of its neighbor oxygen. Similarly, magnesium has a larger $E_{\mathrm{i}}$ than aluminum, and phosphorus has a slightly larger $E_{\mathrm{i}}$ than sulfur.


The unusually large $E_{\mathrm{i}}$ values for the group 2A elements $\mathrm{Be}, \mathrm{Mg}$, and so forth can be explained by their electron configurations. Compare beryllium with boron, for example. A $2 s$ electron is removed on ionization of beryllium, but a $2 p$ electron is removed on ionization of boron:


Because a $2 s$ electron is on average closer to the nucleus than a $2 p$ electron, it is held more tightly and is harder to remove. Thus, the $E_{\mathrm{i}}$ of beryllium is larger than that of boron. An alternative way of saying the same thing is to note that the $2 p$ electron of boron is shielded somewhat by the $2 s$ electrons, feels a smaller $Z_{\text {eff }}$, and is thus more easily removed than a $2 s$ electron of beryllium.

The unusually low $E_{\mathrm{i}}$ values for atoms of group 6A elements can also be explained by their electron configurations. In comparing nitrogen with oxygen, for example, the nitrogen electron is removed from a half-filled orbital, whereas the oxygen electron is removed from a filled orbital:


Because electrons repel one another and tend to stay as far apart as possible, electrons that are forced together in a filled orbital are slightly higher in energy than those in a half-filled orbital, so it is slightly easier to remove one. Thus, oxygen has a smaller $E_{\mathrm{i}}$ than nitrogen.

## Worked Example 6.1

Arrange the elements $\mathrm{Se}, \mathrm{Cl}$, and S in order of increasing ionization energy.

## Strategy

Ionization energy generally increases from left to right across a row of the periodic table and decreases from top to bottom down a group. Chlorine should have a larger $E_{\mathrm{i}}$ than its neighbor sulfur, and selenium should have a smaller $E_{\mathrm{i}}$ than sulfur.

## Solution

The order is $\mathrm{Se}<\mathrm{S}<\mathrm{Cl}$.

- PROBLEM 6.5 Using the periodic table as your guide, predict which element in each of the following pairs has the larger ionization energy:
(a) K or Br
(b) S or Te
(c) Ga or Se
(d) Ne or Sr


## 6.4 | Higher Ionization Energies

Ionization is not limited to the removal of a single electron from an atom. Two, three, or even more electrons can be removed sequentially from an atom, and the amount of energy associated with each step can be measured.

$$
\begin{array}{ll}
\mathrm{M}+\text { Energy } \longrightarrow \mathrm{M}^{+}+\mathrm{e}^{-} & \text {First ionization energy }\left(E_{\mathrm{i} 1}\right) \\
\mathrm{M}^{+}+\text {Energy } \longrightarrow \mathrm{M}^{2+}+\mathrm{e}^{-} & \begin{array}{l}
\text { Second ionization energy }\left(E_{\mathrm{i} 2}\right) \\
\mathrm{M}^{2+}+\text { Energy } \longrightarrow \mathrm{M}^{3+}+\mathrm{e}^{-} \\
\text {And so forth } \ldots
\end{array}
\end{array}
$$

As you might expect, successively larger amounts of energy are required for each successive ionization step because it is much harder to remove a negatively charged electron from a positively charged ion than from a neutral atom. Interestingly, though, the energy differences between successive steps vary dramatically from one element to another. Removing the second electron from sodium takes nearly ten times as much energy as removing the first one ( 4562 versus $496 \mathrm{~kJ} / \mathrm{mol}$ ), but removing the second electron from magnesium takes only twice as much energy as removing the first one ( 1451 versus $738 \mathrm{~kJ} / \mathrm{mol}$ ). Large jumps similar to that for sodium are also found for other elements, as can be seen by following the zigzag line in Table 6.2. Magnesium has a large jump between its second and third ionization energies, aluminum has a large jump between its third and fourth ionization energies, silicon has a large jump between its fourth and fifth ionization energies, and so on.

TABLE 6.2 Higher Ionization Energies (kJ/mol) for Third-Row Elements

| $\boldsymbol{E}_{\mathbf{i}}$ |  |  |  | $\mathbf{M}$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{N u m b e r}$ | $\mathbf{N a}$ | $\mathbf{M g}$ | $\mathbf{A l}$ | $\mathbf{S i}$ | $\mathbf{P}$ | $\mathbf{S}$ | $\mathbf{C l}$ | $\mathbf{A r}$ |
| $E_{\mathrm{i} 1}$ | 496 | 738 | 578 | 787 | 1,012 | 1,000 | 1,251 | 1,520 |
| $E_{\mathrm{i} 2}$ | 4,562 | 1,451 | 1,817 | 1,577 | 1,903 | 2,251 | 2,297 | 2,665 |
| $E_{\mathrm{i} 3}$ | 6,912 | 7,733 | 2,745 | 3,231 | 2,912 | 3,361 | 3,822 | 3,931 |
| $E_{\mathrm{i} 4}$ | 9,543 | 10,540 | 11,575 | 4,356 | 4,956 | 4,564 | 5,158 | 5,770 |
| $E_{\mathrm{i} 5}$ | 13,353 | 13,630 | 14,830 | 16,091 | 6,273 | 7,013 | 6,540 | 7,238 |
| $E_{\mathrm{i} 6}$ | 16,610 | 17,995 | 18,376 | 19,784 | 22,233 | 8,495 | 9,458 | 8,781 |
| $E_{\mathrm{i} 7}$ | 20,114 | 21,703 | 23,293 | 23,783 | 25,397 | 27,106 | 11,020 | 11,995 |

The large increases in ionization energies that follow the zigzag line in Table 6.2 are yet another consequence of electron configuration. It's relatively easy to remove an electron from a partially filled valence shell, where $Z_{\text {eff }}$ is lower, but it's relatively difficult to remove an electron from a filled valence shell, where $Z_{\text {eff }}$ is higher. In other words, there is a large amount of stability associated with filled $s$ and $p$ subshells (a noble gas electron configuration), which corresponds to having eight electrons (an octet) in the valence shell of an atom or ion. Sodium ([Ne] $3 s^{1}$ ) loses only one electron easily, magnesium ( $[\mathrm{Ne}] 3 s^{2}$ ) loses only two electrons easily, aluminum ( $[\mathrm{Ne}] 3 s^{2} 3 p^{1}$ ) loses only three electrons easily, and so on across the row. We'll further explore the stability of valence-shell electron octets in Section 6.12.

$$
\begin{array}{ll} 
& \begin{array}{c}
8 \text { electrons in } \\
\text { outer (2nd) shell }
\end{array} \\
\mathrm{Na}\left(1 s^{2} 2 s^{2} 2 p^{6} 3 s^{1}\right) & \mathrm{Na}^{+}\left(1 s^{2} 2 s^{2} 2 p^{6}\right)+\mathrm{e}^{-} \\
\mathrm{Mg}\left(1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2}\right) & \mathrm{Mg}^{2+}\left(1 s^{2} 2 s^{2} 2 p^{6}\right)+2 \mathrm{e}^{-} \\
\mathrm{Al}\left(1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{1}\right) \longrightarrow \mathrm{Al}^{3+}\left(1 s^{2} 2 s^{2} 2 p^{6}\right)+3 \mathrm{e}^{-} \\
\cdot & \cdot \\
\cdot \\
\cdot \\
\mathrm{Cl}\left(1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{5}\right) \longrightarrow \mathrm{Cl}^{7+}\left(1 s^{2} 2 s^{2} 2 p^{6}\right)+7 \mathrm{e}^{-}
\end{array}
$$

Just as valence-shell electrons rather than core electrons are the most easily lost during ionization, they are also the most easily lost or shared during chemical reactions. We'll see repeatedly in later chapters that the valence-shell electron configuration of an atom controls the atom's chemistry.

## Worked Example 6.2

Which has the larger fifth ionization energy, Ge or As?

## Strategy

Look at their positions in the periodic table. The group 4A element germanium has four valence-shell electrons and thus has four relatively low ionization energies, whereas the group 5A element arsenic has five valence-shell electrons and has five low ionization energies.

## Solution

Germanium has a larger $E_{\mathrm{i} 5}$ than arsenic.

- PROBLEM 6.6
(a) Which has the larger third ionization energy, Be or N ?
(b) Which has the larger fourth ionization energy, Ga or Ge?

PROBLEM 6.7 Three atoms have the following electron configurations:
(a) $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{1}$
(b) $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{5}$
(c) $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6} 4 s^{1}$

Which of the three has the largest $E_{\mathrm{i} 1}$ ? Which has the smallest $E_{\mathrm{i} 4}$ ?
-KEY CONCEPT PROBLEM 6.8 Order the indicated three elements according to the ease with which each is likely to lose its third electron:


### 6.5 Electron Affinity

Just as it's possible to measure the energy change on removing an electron from an atom to form a cation, it's also possible to measure the energy change on adding an electron to an atom to form an anion. An element's electron affinity, abbreviated $E_{\text {ea }}$, is the energy change that occurs when an electron is added to an isolated atom in the gaseous state.

Ionization energies (Section 6.3) are always positive because energy must always be added to remove an electron from an atom. Electron affinities, however, are generally negative because energy is usually released when a neutral atom adds an electron.* We'll see in Chapter 8 that this same sign convention is used throughout chemistry: A positive energy change means energy is absorbed, and a negative energy change means energy is released.

The more negative the $E_{\text {ea, }}$, the greater the tendency of the atom to accept an electron and the more stable the anion that results. By contrast, an atom that forms an unstable anion by addition of an electron has, in principle, a positive value of $E_{\text {ea }}$, but no experimental measurement can be made in such circumstances. All we can say is that the $E_{\text {ea }}$ for such an atom is greater than zero. The $E_{\text {ea }}$ of hydrogen, for instance, is $-72.8 \mathrm{~kJ} / \mathrm{mol}$, meaning that energy is released and the $\mathrm{H}^{-}$anion is stable. The $E_{\text {ea }}$ of neon, however, is greater than $0 \mathrm{~kJ} / \mathrm{mol}$, meaning that Ne does not add an electron and the $\mathrm{Ne}^{-}$anion is unstable.

$$
\begin{array}{ll}
\mathrm{H}\left(1 s^{1}\right)+\mathrm{e}^{-} \longrightarrow \mathrm{H}^{-}\left(1 s^{2}\right)+72.8 \mathrm{~kJ} / \mathrm{mol} & E_{\text {ea }}=-72.8 \mathrm{~kJ} / \mathrm{mol} \\
\mathrm{Ne}\left(1 s^{2} 2 s^{2} 2 p^{6}\right)+\mathrm{e}^{-}+\text {Energy } \longrightarrow \mathrm{Ne}^{-}\left(1 s^{2} 2 s^{2} 2 p^{6} 3 s^{1}\right) & E_{\text {ea }}>0 \mathrm{~kJ} / \mathrm{mol}
\end{array}
$$

As with ionization energies, electron affinities show a periodicity that is related to the electron configurations of the elements. The data in Figure 6.6 indicate that group 7A elements have the most negative electron affinities, corresponding to the largest release of energy, while group 2A and group 8A elements have near-zero or positive electron affinities, corresponding to an absorption of energy.

[^9]aElectron affinity is defined for isolated, gaseous-state atoms. Other factors, such as lattice energy or solvation energy must be considered when forming ions in a condensed state.

$\nabla$Just as there are successive ionization energies: $E_{i 1}, E_{i 2}, E_{i 3}, \ldots$, there are successive electron affinities: $E_{\text {ea1 }}, E_{\text {ea2 }}, E_{\text {ea3 }}, \ldots$ While energy is generally released on addition of one electron, energy is always required to add two or more electrons to a neutral gaseous atom.

FIGURE 6.6 Electron affinities for elements 1-57 and $72-86$. A negative value means that energy is released when an electron adds to an atom, while a value of zero means that energy is absorbed but the exact amount can't be measured. Note that the group 2A elements (alkaline earths) and the group 8A elements (noble gases) have $E_{\text {ea }}$ values near zero, while the group 7A elements (halogens) have large negative $E_{\text {ea }}$ 's. Accurate electron affinities are not known for elements 58-71.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Halogens Compete for Electrons," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 60-61. The relative tendency of halogens to gain or lose electrons is demonstrated.


The value of an element's electron affinity is due to an interplay of several offsetting factors. Attraction between the additional electron and the atomic nucleus favors a negative $E_{\text {ea }}$, but the increase in electron-electron repulsions that result from addition of the extra electron favors a positive $E_{\text {ea }}$.

Large negative $E_{\text {ea }}$ 's are found for the halogens $(\mathrm{F}, \mathrm{Cl}, \mathrm{Br}, \mathrm{I})$ because each of these elements has both a high $Z_{\text {eff }}$ and room in its valence shell for an additional electron. Halide anions have a noble gas electron configuration with filled $s$ and $p$ sublevels, and the attraction between the additional electron and the atomic nucleus is high. Positive $E_{\text {ea }}$ 's are found for the noble gas elements ( $\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}, \mathrm{Kr}, \mathrm{Xe}$ ) because the $s$ and $p$ sublevels in these elements are full, and the additional electron must therefore go into the next higher shell, where it is shielded from the nucleus and feels a relatively low $Z_{\text {eff. }}$. The attraction of the nucleus for the added electron is therefore small and is outweighed by the additional electron-electron repulsions.
$\begin{array}{lll}\text { A halogen: } & \mathrm{Cl}\left(\ldots 3 s^{2} 3 p^{5}\right)+\mathrm{e}^{-} \longrightarrow \mathrm{Cl}^{-}\left(\ldots 3 s^{2} 3 p^{6}\right) & E_{\mathrm{ea}}=-348.6 \mathrm{~kJ} / \mathrm{mol} \\ \text { A noble gas: } & \mathrm{Ar}\left(\ldots 3 s^{2} 3 p^{6}\right)+\mathrm{e}^{-} \longrightarrow \mathrm{Ar}^{-}\left(\ldots 3 s^{2} 3 p^{6} 4 s^{1}\right) & E_{\mathrm{ea}}>0 \mathrm{~kJ} / \mathrm{mol}\end{array}$
A noble gas: $\quad \operatorname{Ar}\left(\ldots 3 s^{2} 3 p^{6}\right)+\mathrm{e}^{-} \longrightarrow \mathrm{Ar}^{-}\left(\ldots 3 s^{2} 3 p^{6} 4 s^{1}\right) \quad E_{\text {ea }}>0 \mathrm{~kJ} / \mathrm{mol}$
In looking for other trends in the data of Figure 6.6, the near-zero $E_{\mathrm{ea}}$ 's of the alkaline earth metals ( $\mathrm{Be}, \mathrm{Mg}, \mathrm{Ca}, \mathrm{Sr}, \mathrm{Ba}$ ) are particularly striking. Atoms of these elements have filled $s$ subshells, which means that the additional electron must go into a $p$ subshell. The higher energy of the $p$ subshell, together with a relatively low $Z_{\text {eff }}$ for elements on the left side of the periodic table, means that alkaline earth atoms accept an electron reluctantly and have $E_{\text {ea }}$ values near zero.
An alkaline earth: $\mathrm{Mg}\left(\ldots 3 s^{2}\right)+\mathrm{e}^{-} \longrightarrow \mathrm{Mg}^{-}\left(\ldots 3 s^{2} 3 p^{1}\right) \quad E_{\text {ea }} \approx 0 \mathrm{~kJ} / \mathrm{mol}$

## Worked Example 6.3

Why does nitrogen have a less favorable (more positive) $E_{\text {ea }}$ than its neighbors on either side, C and O ?

## Strategy and Solution

The magnitude of an element's $E_{\text {ea }}$ depends on the element's valence-shell electron configuration. The electron configurations of $\mathrm{N}, \mathrm{C}$, and O are

$$
\begin{aligned}
& \text { Carbon: } 1 s^{2} 2 s^{2} 2 p_{x}{ }^{1} 2 p_{\mathrm{y}}{ }^{1} \\
& \text { Oxygen: } 1 s^{2} 2 s^{2} 2 p_{x}{ }^{2} 2 p_{y}{ }^{1} 2 p_{z}{ }^{1}
\end{aligned}
$$

Carbon has only two electrons in its $2 p$ subshell and can readily accept another in its vacant $2 p_{z}$ orbital. Nitrogen, however, has a half-filled $2 p$ subshell, and the additional electron must pair up in a $2 p$ orbital, where it feels a repulsion from the electron already present. Thus, the $E_{\text {ea }}$ of nitrogen is less favorable than that of carbon. Oxygen
also must add an electron to an orbital that already has one electron, but the additional stabilizing effect of increased $Z_{\text {eff }}$ across the periodic table counteracts the effect of electron repulsion, resulting in a more favorable $E_{\text {ea }}$ for O than for N .

- PROBLEM 6.9 Explain why manganese (atomic number 25) has a less favorable $E_{\text {ea }}$ than its neighbors on either side.
- KEY CONCEPT PROBLEM 6.10 Which of the indicated three elements has the least favorable $E_{\mathrm{ea}}$, and which has the most favorable $E_{\mathrm{ea}}$ ?



### 6.6 Ionic Bonds and the Formation of Ionic Solids

What would happen if an element that gives up an electron easily (that is, has a small ionization energy) were to come in contact with an element that accepts an electron easily (that is, has a large negative electron affinity)? The element with the small $E_{\mathrm{i}}$ might transfer an electron to the element with the negative $E_{\text {ea }}$, yielding a cation and an anion. Sodium, for example, reacts with chlorine to give $\mathrm{Na}^{+}$ions and $\mathrm{Cl}^{-}$ions:


The oppositely charged $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions that result when sodium transfers an electron to chlorine are attracted to one another by electrostatic forces, and we say that they are joined by an ionic bond. The crystalline substance that results is said to be an ionic solid. A visible crystal of sodium chloride does not consist of individual pairs of $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions, however. Instead, solid NaCl consists of a vast three-dimensional network of ions in which each $\mathrm{Na}^{+}$is surrounded by and attracted to many $\mathrm{Cl}^{-}$ions, and each $\mathrm{Cl}^{-}$is surrounded by and attracted to many $\mathrm{Na}^{+}$ions (Figure 6.7).

-


A Sodium metal burns in a chlorine atmosphere to yield solid sodium chloride.

FIGURE 6.7 When sodium atoms transfer electrons to chlorine atoms, crystals of the ionic solid sodium chloride are formed. In the sodium chloride crystal, each $\mathrm{Na}^{+}$ion is surrounded by six nearestneighbor $\mathrm{Cl}^{-}$ions, and each $\mathrm{Cl}^{-}$ion is surrounded by six nearest-neighbor $\mathrm{Na}^{+}$ions.

$\square$
Formulas for ionic compounds are empirical formulas giving the relative number of cations and anions. Although the formula for sodium chloride is NaCl , molecules of NaCl do not exist under ordinary laboratory conditions.


v
Because the sum of ionization energy and electron affinity is always positive, obtaining noble gas electron configurations upon formation of ions is not the driving force behind the formation of an ionic compound. The ions must be stabilized by strong forces arising from electrostatic attraction.

What about the energy change, $\Delta E$, that occurs when sodium and chlorine react to yield $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions? It's apparent from $E_{\mathrm{i}}$ and $E_{\text {ea }}$ values that the amount of energy released when a chlorine atom accepts an electron ( $E_{\mathrm{ea}}=$ $-348.6 \mathrm{~kJ} / \mathrm{mol}$ ) is insufficient to offset the amount absorbed when a sodium atom loses an electron ( $\left.E_{\mathrm{i}}=+495.8 \mathrm{~kJ} / \mathrm{mol}\right)$ :

$$
\begin{aligned}
E_{\mathrm{i}} \text { for } \mathrm{Na}=+495.8 \mathrm{~kJ} / \mathrm{mol} & \text { (Unfavorable) } \\
E_{\mathrm{ea}} \text { for } \mathrm{Cl}=-348.6 \mathrm{~kJ} / \mathrm{mol} & \text { (Favorable) } \\
\hline \Delta E=+147.2 \mathrm{~kJ} / \mathrm{mol} & \text { (Unfavorable) }
\end{aligned}
$$

The net energy change $\Delta E$ for the reaction of sodium and chlorine atoms would be unfavorable by $+147.2 \mathrm{~kJ} / \mathrm{mol}$, and no reaction would occur unless some other factor were involved. This additional factor, which overcomes the unfavorable energy change of electron transfer, is the large gain in stability due to the formation of ionic bonds. (The Greek capital letter delta, $\Delta$, is used to represent a change in the indicated quantity, in this case, $\Delta E$.)

The actual reaction of sodium with chlorine occurs all at once rather than in a stepwise manner, but energy calculations can be made more easily if we imagine a series of hypothetical steps for which experimentally measured energy values can be obtained. There are five contributions that must be taken into account to calculate the overall energy change during the formation of solid NaCl from solid sodium metal and gaseous chlorine molecules:

$$
\mathrm{Na}(s)+1 / 2 \mathrm{Cl}_{2}(g) \longrightarrow \mathrm{NaCl}(s)
$$

Step 1. The conversion of solid Na metal into isolated gaseous Na atoms, a process called sublimation. Since energy must be added to disrupt the forces holding atoms together in a solid, the heat required for sublimation has a positive value: $107.3 \mathrm{~kJ} / \mathrm{mol}$ for Na .
Step 2. The dissociation of gaseous $\mathrm{Cl}_{2}$ molecules into individual Cl atoms. Energy must be added to break molecules apart before reaction can occur, and the energy required for bond breaking therefore has a positive value: $243 \mathrm{~kJ} / \mathrm{mol}$ for $\mathrm{Cl}_{2}$ (or $122 \mathrm{~kJ} / \mathrm{mol}$ for $1 / 2 \mathrm{Cl}_{2}$ ). We'll look further into the energetics of bond dissociation in Section 8.11.
Step 3. The ionization of isolated Na atoms into $\mathrm{Na}^{+}$ ions plus electrons. The energy required is simply the first ionization energy of sodium and has a positive value: $495.8 \mathrm{~kJ} / \mathrm{mol}$.
Step 4. The formation of $\mathrm{Cl}^{-}$ions from Cl atoms by addition of an electron. The energy required is simply the electron affinity of chlorine and has a negative value: $-348.6 \mathrm{~kJ} / \mathrm{mol}$.
Step 5. The formation of solid NaCl from isolated $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions. The energy change for this step is a measure of the overall electrostatic interactions between ions in the solid. It is the amount of energy released when isolated ions condense to form a solid, and it has a negative value: $-787 \mathrm{~kJ} / \mathrm{mol}$ for NaCl .

Net reaction:
Net energy change:

$$
\mathrm{Na}(s) \longrightarrow \mathrm{Na}(g)
$$

$$
+107.3 \mathrm{~kJ} / \mathrm{mol}
$$

$$
\begin{gathered}
1 / 2 \mathrm{Cl}_{2}(g) \longrightarrow \mathrm{Cl}(g) \\
+122 \mathrm{~kJ} / \mathrm{mol}
\end{gathered}
$$

$$
\begin{aligned}
\mathrm{Na}(g) & \longrightarrow \mathrm{Na}^{+}(g)+\mathrm{e}^{-} \\
+ & 495.8 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

$$
\begin{gathered}
\mathrm{Cl}(g)+\mathrm{e}^{-} \longrightarrow \mathrm{Cl}^{-}(g) \\
-348.6 \mathrm{~kJ} / \mathrm{mol}
\end{gathered}
$$

$$
\begin{gathered}
\mathrm{Na}^{+}(g)+\mathrm{Cl}^{-}(g) \longrightarrow \mathrm{NaCl}(s) \\
-787 \mathrm{~kJ} / \mathrm{mol}
\end{gathered}
$$

$$
\begin{aligned}
\mathbf{N a}(s)+ & \mathbf{1} / \mathbf{2} \mathbf{C l}_{\mathbf{2}}(g) \longrightarrow \mathbf{N a C l}(\mathrm{s}) \\
& -411 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

A pictorial representation of the five hypothetical steps in the reaction between sodium and chlorine is shown in Figure 6.8. Called a Born-Haber cycle, the figure shows how each step contributes to the overall energy change and how the net process is the sum of the individual steps. As indicated in the diagram, steps 1, 2, and 3 absorb energy (have positive values), while steps 4 and 5 release energy (have negative values). The largest contribution is step 5, which takes into account the electrostatic interactions between ions in the solid product. Were it not for this large amount of stabilization of the solid due to ionic bonding, no reaction would take place.


## Lattice Energy

The sum of the electrostatic interaction energies between ions in a crystal—and thus the measure of the strength of the crystal's ionic bonds-is called the lattice energy $(U)$. By convention, lattice energy is the amount of energy that must be supplied to break up an ionic solid into its individual gaseous ions. It therefore has a positive value because energy is required to separate the electrical charges. The formation of a crystal from ions is the reverse of the breakup, however, and step 5 in the Born-Haber cycle of Figure 6.8 therefore has the value $-U$.

$$
\begin{array}{lrl}
\mathrm{NaCl}(s) \longrightarrow \mathrm{Na}^{+}(g)+\mathrm{Cl}^{-}(g) & U=+787 \mathrm{~kJ} / \mathrm{mol} & \text { (Energy absorbed) } \\
\mathrm{Na}^{+}(g)+\mathrm{Cl}^{-}(g) \longrightarrow \mathrm{NaCl}(s) & -U=-787 \mathrm{~kJ} / \mathrm{mol} & \text { (Energy released) }
\end{array}
$$

The force $F$ that results from the interaction of electric charges is described by Coulomb's law and is equal to a constant $k$ times the charges on the ions, $z_{1}$ and $z_{2}$, divided by the square of the distance $d$ between their centers:

- COULOMB'S LAW $F=k \times \frac{z_{1} z_{2}}{d^{2}}$

But because energy is equal to force times distance, the negative of the lattice energy equals

$$
-U=F \times d=k \times \frac{z_{1} z_{2}}{d}
$$

The value of the constant $k$ depends on the arrangement of the ions in the specific compound and is different for different substances.

Lattice energies are largest when the distance $d$ between ions is small and when the charges $z_{1}$ and $z_{2}$ are large. A small distance $d$ means that the ions are close together, which means that they have small ionic radii. Thus, if $z_{1}$ and $z_{2}$ are

VThe Born-Haber cycle is an example of Hess's law, introduced in Chapter 8. It is used to calculate properties that are impossible to measure directly.

4 FIGURE 6.8 A Born-Haber cycle for the formation of $\mathrm{NaCl}(\mathrm{s})$ from $\mathrm{Na}(\mathrm{s})$ and $\mathrm{Cl}_{2}(g)$. The sum of the individual energy changes for the five steps equals the net energy change for the overall reaction. Note that the most favorable step is the formation of solid NaCl from gaseous $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions (step 5).


An ionic compound will form when an element from the far left-hand side combines with an element from the far right-hand side of the periodic table (a notable exception being $\mathrm{BeCl}_{2}$ ). Compounds encountered in a general chemistry course are usually ionic if formed from reaction of a metal with a nonmetal.
held constant, the largest lattice energies belong to compounds formed from the smallest ions, as listed in Table 6.3. Within a series of compounds that have the same anion but different cations, lattice energy increases as the cation becomes smaller. Comparing $\mathrm{LiF}, \mathrm{NaF}$, and KF , for example, cation size follows the order $\mathrm{K}^{+}>\mathrm{Na}^{+}>\mathrm{Li}^{+}$, so lattice energies follow the order $\mathrm{LiF}>\mathrm{NaF}>\mathrm{KF}$. Similarly, within a series of compounds that have the same cation but different anions, lattice energy increases as anion size decreases. Comparing $\mathrm{LiF}, \mathrm{LiCl}, \mathrm{LiBr}$, and LiI , for example, anion size follows the order $\mathrm{I}^{-}>\mathrm{Br}^{-}>\mathrm{Cl}^{-}>\mathrm{F}^{-}$, so lattice energies follow the reverse order $\mathrm{LiF}>\mathrm{LiCl}>\mathrm{LiBr}>\mathrm{LiI}$.

| TABLE 6.3 | Lattice Energies of Some Ionic Solids (kJ/mol) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Cation | Anion |  |  |  |  |
|  | $\mathbf{F}^{-}$ | $\mathrm{Cl}^{-}$ | $\mathbf{B r}^{-}$ | $\mathbf{I}^{-}$ | $\mathbf{O}^{2-}$ |
| $\mathrm{Li}^{+}$ | 1036 | 853 | 807 | 757 | 2925 |
| $\mathrm{Na}^{+}$ | 923 | 787 | 747 | 704 | 2695 |
| $\mathrm{K}^{+}$ | 821 | 715 | 682 | 649 | 2360 |
| $\mathrm{Be}^{2+}$ | 3505 | 3020 | 2914 | 2800 | 4443 |
| $\mathrm{Mg}^{2+}$ | 2957 | 2524 | 2440 | 2327 | 3791 |
| $\mathrm{Ca}^{2+}$ | 2630 | 2258 | 2176 | 2074 | 3401 |
| $\mathrm{Al}^{3+}$ | 5215 | 5492 | 5361 | 5218 | 15,916 |

Table 6.3 also shows that compounds of ions with higher charges have larger lattice energies than compounds of ions with lower charges. In comparing NaI , $\mathrm{MgI}_{2}$, and $\mathrm{AlI}_{3}$, for example, the order of charges on the cations is $\mathrm{Al}^{3+}>$ $\mathrm{Mg}^{2+}>\mathrm{Na}^{+}$, and the order of lattice energies is $\mathrm{AlI}_{3}>\mathrm{MgI}_{2}>\mathrm{NaI}$.

## Worked Example 6.4

Which has the larger lattice energy, NaCl or CsI?

## Strategy

The magnitude of a substance's lattice energy is affected both by the charges on its constituent ions and by the sizes of those ions. The higher the charges on the ions and the smaller the sizes of the ions, the larger the lattice energy. All four ions, $\mathrm{Na}^{+}, \mathrm{Cs}^{+}, \mathrm{Cl}^{-}$, and $\mathrm{I}^{-}$, are singly charged, but they differ in size.

## Solution

Since $\mathrm{Na}^{+}$is smaller than $\mathrm{Cs}^{+}$and $\mathrm{Cl}^{-}$is smaller than $\mathrm{I}^{-}$, the distance between ions is smaller in NaCl than in CsI. Thus, NaCl has the larger lattice energy.

## Worked Key Concept Example 6.5

Which of the following alkaline earth oxides has the larger lattice energy, and which has the smaller lattice energy? Explain.

(a)

(b)

## Strategy

The magnitude of a lattice energy depends directly on the charge on the ions and inversely on the distance between ions (that is, on the radii of the ions). In this instance, all the ions in both drawings are doubly charged, either $\mathrm{M}^{2+}$ or $\mathrm{O}^{2-}$, so only the size of the ions is important.

## Solution

The ions in drawing (b) are smaller than those in drawing (a), so (b) has the larger lattice energy.

PROBLEM 6.11 Which substance in each of the following pairs has the larger lattice energy?
(a) KCl or RbCl
(b) $\mathrm{CaF}_{2}$ or $\mathrm{BaF}_{2}$
(c) CaO or KI

PROBLEM 6.12 Calculate the net energy change (in kilojoules per mole) that takes place on formation of $\mathrm{KF}(s)$ from the elements: $\mathrm{K}(s)+1 / 2 \mathrm{~F}_{2}(g) \rightarrow \mathrm{KF}(s)$. The following information is needed:

$$
\begin{array}{ll}
\text { Heat of sublimation for } K=89.2 \mathrm{~kJ} / \mathrm{mol} & E_{\text {ea }} \text { for } F=-328 \mathrm{~kJ} / \mathrm{mol} \\
\text { Bond dissociation energy for } F_{2}=158 \mathrm{~kJ} / \mathrm{mol} & E_{\mathrm{i}} \text { for } \mathrm{K}=418.8 \mathrm{~kJ} / \mathrm{mol}
\end{array}
$$

Lattice energy for $\mathrm{KF}=821 \mathrm{~kJ} / \mathrm{mol}$
-KEY CONCEPT PROBLEM 6.13 One of the following pictures represents NaCl and one represents MgO . Which is which, and which has the larger lattice energy?


## 6.7 | The Alkali Metals (Group 1A)

Now that we know something about ionization energies, electron affinities, and ionic bonding, let's look at the chemistry of some of the elements that form ionic bonds. The alkali metals in group $1 \mathrm{~A}-\mathrm{Li}, \mathrm{Na}, \mathrm{K}, \mathrm{Rb}, \mathrm{Cs}$, and Fr -have the smallest ionization energies of all the elements because of their valence-shell $n s^{1}$ electron configurations (Figure 6.3). They therefore lose this $n s^{1}$ electron easily in chemical reactions to yield +1 ions and are thus among the most powerful reducing agents in the periodic table (Sections 4.6-4.8). In fact, the entire chemistry of the alkali metals is dominated by their ability to donate an electron to other elements or compounds.

As their group name implies, the alkali metals are metallic. They have a bright, silvery appearance, are malleable, and are good conductors of electricity. Unlike the more common metals such as iron, though, the alkali metals are all soft enough to cut with a dull knife, have low melting points and densities, and are so reactive that they must be stored under oil to prevent their instantaneous reaction with oxygen and water. None is found in the elemental state in nature; they occur only in salts. Their properties are summarized in Table 6.4.


Kristin A. Johnson, Rodney Schreiner, and Jon Loring, "A Dramatic Flame Test Demonstration," J. Chem. Educ., Vol. 78, 2001, 640-641.

| TABLE 6.4 | Properties of Alkali Metals |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name | Melting <br> Point ( ${ }^{\circ} \mathbf{C}$ ) | Boiling <br> Point ( ${ }^{\circ} \mathbf{C}$ ) | Density <br> (g/cm ${ }^{3}$ ) | First Ionization <br> Energy (kJ/mol) | Abundance on Earth (\%) | Atomic <br> Radius (pm) | Ionic ( $\mathbf{M}^{+}$) <br> Radius (pm) |
| Lithium | 180.5 | 1342 | 0.534 | 520.2 | 0.0020 | 152 | 68 |
| Sodium | 97.7 | 883 | 0.971 | 495.8 | 2.36 | 186 | 102 |
| Potassium | 63.3 | 759 | 0.862 | 418.8 | 2.09 | 227 | 138 |
| Rubidium | 39.3 | 688 | 1.532 | 403.0 | 0.0090 | 248 | 147 |
| Cesium | 28.4 | 671 | 1.873 | 375.7 | 0.00010 | 265 | 167 |
| Francium | - | - | - | $\approx 400$ | Trace | - | - |

## Occurrence and Uses of Alkali Metals

Lithium First isolated in 1817 from the mineral petalite, $\mathrm{LiAlSi}_{4} \mathrm{O}_{10}$, lithium was named from the Greek word lithos, meaning stone, because of its common occurrence in rocks. Most lithium today is obtained from the mineral spodumene, $\mathrm{LiAlSi}_{2} \mathrm{O}_{6}$, large deposits of which occur scattered throughout the world in the United States, Canada, Brazil, and the former USSR. The major industrial use of lithium is in all-purpose automotive greases, but lithium salts such as $\mathrm{Li}_{2} \mathrm{CO}_{3}$ also have a variety of specialized applications, including use as a pharmaceutical agent for the treatment of manic-depressive behavior.

A sample of lithium metal.


Sodium Sodium, the sixth most abundant element in the earth's crust, was first prepared in 1807 from caustic soda $(\mathrm{NaOH})$, after which it was named. Sodium occurs throughout the world in vast deposits of NaCl (halite, or rock salt), $\mathrm{NaNO}_{3}$ (Chile saltpeter), $\mathrm{Na}_{2} \mathrm{CO}_{3} \cdot \mathrm{NaHCO}_{3} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ (trona), and $\mathrm{Na}_{2} \mathrm{SO}_{4} \cdot 10 \mathrm{H}_{2} \mathrm{O}$ (mirabilite), all laid down by evaporation of ancient seas. In addition, the world's oceans are approximately $3 \%$ by mass NaCl . Uses of sodium and its salts span nearly the entire range of processes in the modern chemical industry. Glass, rubber, pharmaceutical agents, and many other substances use sodium or its salts in their production. [Note that the formulas of trona $\left(\mathrm{Na}_{2} \mathrm{CO}_{3} \cdot \mathrm{NaHCO}_{3} \cdot 2 \mathrm{H}_{2} \mathrm{O}\right)$ and mirabilite $\left(\mathrm{Na}_{2} \mathrm{SO}_{4} \cdot 10 \mathrm{H}_{2} \mathrm{O}\right)$ are written with raised dots to specify the overall composition of the substances without indicating exactly how the various parts separated by the dots are bonded together.]
Potassium Potassium, the eighth most abundant element in the earth's crust, was first prepared in 1807 at the same time as sodium. The name of the element is derived from potash, a made-up word for $\mathrm{K}_{2} \mathrm{CO}_{3}$, which had been isolated from the "pot ashes" left over from wood fires. (Today, the term potash is used as a general name for all water-soluble, potassium-containing minerals, and the
A A sample of potassium metal.
name caustic potash is used for KOH.) Potassium is found primarily in deposits of $\mathrm{KNO}_{3}$ (saltpeter), KCl (sylvite), and $\mathrm{KCl} \cdot \mathrm{MgCl}_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}$ (carnalite), most of which are in Canada and the former USSR. The major use of potassium salts is as a plant fertilizer.

Rubidium, Cesium Rubidium and cesium, the two most chemically reactive of the common alkali metals, were both detected as impurities in other substances by chance observation of their characteristic colored spectral lines (Section 5.3). Rubidium, named from the Latin rubidius (deepest red), occurs as an impurity in the mineral lepidolite, $\mathrm{K}_{2} \mathrm{Li}_{3} \mathrm{Al}_{5} \mathrm{Si}_{6} \mathrm{O}_{20}(\mathrm{OH}, \mathrm{F})_{4}$, and is obtained as a byproduct of lithium manufacture. Cesium, named from the Latin caesius (sky blue), also occurs with lithium in many minerals and is found in pollucite $\left(\mathrm{Cs}_{4} \mathrm{Al}_{4} \mathrm{Si}_{9} \mathrm{O}_{26} \cdot \mathrm{H}_{2} \mathrm{O}\right)$. Neither rubidium nor cesium has any major commercial importance.

Francium Francium, the heaviest of the group 1A elements, is highly radioactive, and no visible amount of the element has ever been prepared. Little is known about its properties from direct observation, but its behavior would presumably be similar to that of the other alkali metals.

## Production of Alkali Metals

Alkali metals are produced commercially by reduction of their chloride salts, although the exact procedure differs for each element. Both lithium metal and sodium metal are produced by electrolysis, a process in which an electric current is passed through the molten salt. The details of the process won't be discussed until Sections 18.11 and 18.12, but the fundamental idea is simply to use electrical energy to break down an ionic compound into its elements. A high reaction temperature is necessary to keep the salt liquid.

$$
2 \mathrm{LiCl}(l) \xrightarrow[\substack{450^{\circ} \mathrm{C}}]{\substack{\text { Electrolysis } \\ \text { in KCl } \\ \text { Electroysis } \\ \text { in Call }}} 2 \mathrm{Li}(l)+\mathrm{Cl}_{2}(g)
$$

Potassium, rubidium, and cesium metals are produced by chemical reduction rather than by electrolysis. Sodium is the reducing agent used in potassium production, and calcium is the reducing agent used for preparing rubidium and cesium.

$$
\begin{aligned}
\mathrm{KCl}(l)+\mathrm{Na}(l) & \stackrel{850^{\circ} \mathrm{C}}{\rightleftharpoons} \mathrm{~K}(g)+\mathrm{NaCl}(l) \\
2 \mathrm{RbCl}(l)+\mathrm{Ca}(l) & \stackrel{750^{\circ} \mathrm{C}}{\rightleftharpoons} 2 \mathrm{Rb}(g)+\mathrm{CaCl}_{2}(l) \\
2 \mathrm{CsCl}(l)+\mathrm{Ca}(l) & \stackrel{750^{\circ} \mathrm{C}}{\rightleftharpoons} 2 \mathrm{Cs}(g)+\mathrm{CaCl}_{2}(l)
\end{aligned}
$$

All three of the above reductions appear contrary to the activity series described in Section 4.8, according to which sodium is not a strong enough reducing agent to react with $\mathrm{K}^{+}$, and calcium is not a strong enough reducing agent to react with either $\mathrm{Rb}^{+}$or $\mathrm{Cs}^{+}$. At high reaction temperatures, however, equilibria are established in which small amounts of the products are formed. These products are then removed from the reaction mixture by distillation, thereby driving the reactions toward more product formation. We'll explore the general nature of such chemical equilibria in Chapter 13.


A Samples of rubidium and cesium, sealed in glass to protect them from the atmosphere.

## Reactions of Alkali Metals

Reaction with Halogens The alkali metals react rapidly with the group 7A elements (halogens) to yield colorless, crystalline ionic salts called halides:

$$
2 \mathrm{M}(s)+\mathrm{X}_{2} \longrightarrow 2 \mathrm{MX}(s)
$$

$$
\text { where } \mathrm{M}=\text { Alkali metal ( } \mathrm{Li}, \mathrm{Na}, \mathrm{~K}, \mathrm{Rb}, \text { or } \mathrm{Cs} \text { ) }
$$

$$
X=\operatorname{Halogen}(F, C l, B r, \text { or } I)
$$

The reactivity of an alkali metal increases as its ionization energy decreases, giving a reactivity order $\mathrm{Cs}>\mathrm{Rb}>\mathrm{K}>\mathrm{Na}>\mathrm{Li}$. Cesium is the most reactive, combining almost explosively with the halogens.

Reaction with Hydrogen and Nitrogen Alkali metals react with hydrogen gas to form a series of white crystalline compounds called hydrides, MH, in which the hydrogen has an oxidation number of -1 . The reaction is slow at room temperature and requires heating to melt the alkali metal before reaction takes place.

$$
2 \mathrm{M}(s)+\mathrm{H}_{2}(g) \xrightarrow[\text { A metal hydride }]{\text { Heat }} 2 \mathrm{MH}(s)
$$

where $\mathrm{M}=$ Alkali metal (Li, $\mathrm{Na}, \mathrm{K}, \mathrm{Rb}$, or Cs )
A similar reaction takes place between lithium and nitrogen gas to form lithium nitride, $\mathrm{Li}_{3} \mathrm{~N}$, but the other alkali metals do not react with nitrogen.

$$
6 \mathrm{Li}(s)+\mathrm{N}_{2}(g) \xrightarrow{\text { Heat }} 2 \mathrm{Li}_{3} \mathrm{~N}(s)
$$

Reaction with Oxygen All the alkali metals react rapidly with oxygen, but they give different kinds of products. Lithium reacts with $\mathrm{O}_{2}$ to yield the oxide, $\mathrm{Li}_{2} \mathrm{O}$; sodium reacts to yield the peroxide, $\mathrm{Na}_{2} \mathrm{O}_{2}$; and the remaining alkali metals, $\mathrm{K}, \mathrm{Rb}$, and Cs , form either peroxides or superoxides, $\mathrm{MO}_{2}$, depending on the reaction conditions and on how much oxygen is present. The reasons for the differences have to do largely with the differences in stability of the various products and with the way in which the ions pack together in crystals. The alkali metal cations have a +1 oxidation number in all cases, but the oxidation numbers of the oxygen atoms in the $\mathrm{O}^{2-}, \mathrm{O}_{2}{ }^{2-}$, and $\mathrm{O}_{2}^{-}$anions vary from -2 to $-1 / 2$.
$4 \mathrm{Li}(s)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{Li}_{2} \mathrm{O}(s) \quad$ An oxide; oxidation number of $\mathrm{O}=-2$
$2 \mathrm{Na}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{Na}_{2} \mathrm{O}_{2}(s) \quad$ A peroxide; oxidation number of $\mathrm{O}=-1$
$\mathrm{K}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{KO}_{2}(s) \quad$ A superoxide; oxidation number of $\mathrm{O}=-1 / 2$
Potassium superoxide, $\mathrm{KO}_{2}$, is a particularly valuable compound because of its use in spacecraft and in self-contained breathing devices to remove moisture
M. D. Alexander, "Reactions of
the Alkali Metals with Water: A Novel Demonstration," J. Chem. Educ., Vol. 69, 1992, 418. The reaction of sodium metal with water to produce an aqueous solution of sodium hydroxide and hydrogen gas is performed at the interface between paint thinner and the more dense water. Periodically, bubbles of hydrogen gas carry the sodium metal into the organic layer, temporarily stopping the reaction. The presence of the aqueous layer is shown by a phenolphthalein indicator color change.
and $\mathrm{CO}_{2}$ from exhaled air, generating oxygen in the process:

$$
\begin{aligned}
2 \mathrm{KO}_{2}(s)+\mathrm{H}_{2} \mathrm{O}(g) & \longrightarrow \mathrm{KOH}(s)+\mathrm{KO}_{2} \mathrm{H}(s)+\mathrm{O}_{2}(g) \\
4 \mathrm{KO}_{2}(s)+2 \mathrm{CO}_{2}(g) & \longrightarrow 2 \mathrm{~K}_{2} \mathrm{CO}_{3}(s)+3 \mathrm{O}_{2}(g)
\end{aligned}
$$

Reaction with Water The most well-known and dramatic reaction of the alkali metals is with water to yield hydrogen gas and an alkali metal hydroxide, MOH . In fact, it's this reaction that gives the elements their group name: The solution of metal hydroxide that results from adding an alkali metal to water is alkaline, or basic.

$$
\begin{gathered}
2 \mathrm{M}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{M}^{+}(a q)+2 \mathrm{OH}^{-}(a q)+\mathrm{H}_{2}(g) \\
\text { where } \mathrm{M}=\mathrm{Li}, \mathrm{Na}, \mathrm{~K}, \mathrm{Rb}, \mathrm{Cs}
\end{gathered}
$$

Lithium undergoes the reaction with vigorous bubbling as hydrogen is released, sodium reacts rapidly with evolution of heat, and potassium reacts so violently that the hydrogen produced bursts instantly into flame. Rubidium and cesium react almost explosively.


Like all reactions of the alkali metals, the reaction with water is a redox process in which the metal M loses an electron and is oxidized to $\mathrm{M}^{+}$. At the same time, a hydrogen from water gains an electron and is reduced to $\mathrm{H}_{2}$ gas, as can be seen by assigning oxidation numbers to the various substances in the usual way. Note that not all hydrogens are reduced; those in the $\mathrm{OH}^{-}$product remain in the +1 oxidation state.


Reaction with Ammonia The alkali metals react with ammonia to yield $\mathrm{H}_{2}$ gas plus a metal amide, $\mathrm{MNH}_{2}$. The reaction is exactly analogous to that between an alkali metal and water.

$$
\begin{gathered}
2 \mathrm{M}(s)+2 \mathrm{NH}_{3}(l) \longrightarrow 2 \mathrm{M}^{+}(\operatorname{soln})+2 \mathrm{NH}_{2}^{-}(\operatorname{soln})+\mathrm{H}_{2}(g) \\
\text { where } \mathrm{M}=\mathrm{Li}, \mathrm{Na}, \mathrm{~K}, \mathrm{Rb}, \mathrm{Cs}
\end{gathered}
$$

The reaction is so slow at low temperature that it's possible for the alkali metals to dissolve in liquid ammonia at $-33^{\circ} \mathrm{C}$, forming deep blue solutions of metal cations and dissolved electrons. These solutions have extremely powerful reducing properties.

$$
\begin{gathered}
\mathrm{M}(s) \xrightarrow[\text { solvent }]{\text { Liquid } \mathrm{NH}_{3}} \mathrm{M}^{+}(\text {soln })+\mathrm{e}^{-}(\text {soln }) \\
\text { where } \mathrm{M}=\mathrm{Li}, \mathrm{Na}, \mathrm{~K}, \mathrm{Rb}, \text { or } \mathrm{Cs}
\end{gathered}
$$



All the alkali metals react with water to generate $\mathrm{H}_{2}$ gas. (a) Lithium reacts vigorously with bubbling, (b) sodium reacts violently, and (c) potassium reacts almost explosively.
$\nabla$ Sodium metal dissolves in liquid ammonia to yield a blue solution of $\mathrm{Na}^{+}$ions and solvent-surrounded electrons.



FIGURE 6.9 A Born-Haber cycle for the formation of $\mathrm{MgCl}_{2}$ from the elements. The large contribution from ionic bonding in the solid (step 5) provides more than enough energy to remove two electrons from magnesium (step 3).

- PROBLEM 6.14 Assign oxidation numbers to the oxygen atoms in the following compounds:
(a) $\mathrm{Li}_{2} \mathrm{O}$
(b) $\mathrm{K}_{2} \mathrm{O}_{2}$
(c) $\mathrm{CsO}_{2}$
- PROBLEM 6.15 Complete and balance the following equations. If no reaction takes place, write N.R.
(a) $\mathrm{Cs}(s)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow$ ?
(b) $\mathrm{Na}(s)+\mathrm{N}_{2}(g) \rightarrow$ ?
(c) $\mathrm{Rb}(s)+\mathrm{O}_{2}(g) \rightarrow$ ?
(d) $\mathrm{K}(s)+\mathrm{NH}_{3}(g) \rightarrow$ ?
(e) $\mathrm{Rb}(\mathrm{s})+\mathrm{H}_{2}(g) \rightarrow$ ?


### 6.8 The Alkaline Earth Metals (Group 2A)

The alkaline earth elements in group $2 \mathrm{~A}-\mathrm{Be}, \mathrm{Mg}, \mathrm{Ca}, \mathrm{Sr}, \mathrm{Ba}$, and Ra -are similar to the alkali metals in many respects. They differ, however, in that they have $n s^{2}$ valence-shell electron configurations and can therefore lose two electrons in redox reactions. Alkaline earth metals are thus powerful reducing agents and form ions with a +2 charge.

The Born-Haber cycle in Figure 6.9 for the reaction of magnesium with chlorine provides a graphic representation of the energy changes involved in the redox reaction of an alkaline earth element. As in the reaction of sodium and chlorine to form NaCl shown previously in Figure 6.8, there are five contributions to the overall energy change in the reaction of magnesium with chlorine to form $\mathrm{MgCl}_{2}$. First, solid magnesium metal must be converted into isolated gaseous magnesium atoms (sublimation). Second, the bond in $\mathrm{Cl}_{2}$ molecules must be broken to yield two chlorine atoms. Third, each magnesium atom must lose two electrons to form the dipositive $\mathrm{Mg}^{2+}$ ion. Fourth, the two chlorine atoms formed in step 2 must accept electrons to form two $\mathrm{Cl}^{-}$ions. Fifth, the gaseous ions must combine to form the ionic solid, $\mathrm{MgCl}_{2}$. As the Born-Haber cycle indicates, it is the large contribution from ionic bonds (the negative of the lattice energy) that releases enough energy to drive the entire process.


Though harder than their neighbors in group 1A, the alkaline earth elements are still relatively soft, silvery metals. They tend, however, to have higher melting points and densities than alkali metals, as listed in Table 6.5. Alkaline earth elements

TABLE 6.5 Properties of Alkaline Earth Metals

| Name | Melting <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | Boiling <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | Density <br> $\left(\mathbf{g} / \mathbf{c m}^{3}\right)$ | First Ionization <br> Energy $(\mathbf{k J / m o l})$ | Abundance <br> on Earth $(\%)$ | Atomic <br> Radius (pm) | Ionic (Madius $(\mathbf{p m})$ <br> Rad) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: |
| Beryllium | 1287 | 2471 | 1.848 | 899.4 | 0.00028 | 112 | 44 |
| Magnesium | 650 | 1090 | 1.738 | 737.7 | 2.33 | 160 | 66 |
| Calcium | 842 | 1484 | 1.55 | 589.8 | 4.15 | 197 | 99 |
| Strontium | 777 | 1382 | 2.54 | 549.5 | 0.038 | 215 | 112 |
| Barium | 727 | 1897 | 3.51 | 502.9 | 0.042 | 222 | 134 |
| Radium | 700 | 1140 | $\approx 5.0$ | 509.3 | Trace | 223 | 143 |

are less reactive toward oxygen and water than alkali metals but are nevertheless found in nature only in salts, not in the elemental state.

## Occurrence and Uses of Alkaline Earth Metals

Beryllium Beryllium was first detected in 1798 in the gemstones beryl and emerald ( $\mathrm{Be}_{3} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{18}$ ) and was subsequently prepared in pure form in 1828 by the reduction of $\mathrm{BeCl}_{2}$ with potassium. It is obtained today from large commercial deposits of beryl in Brazil and southern Africa. Though beryllium compounds are extremely toxic, particularly when inhaled as dust, the metal is nevertheless useful in forming alloys. Addition of a few percent beryllium to copper or nickel results in hard, cor-rosion-resistant alloys that are used in airplane engines and precision instruments.
Magnesium Compounds of magnesium, the seventh most abundant element in the earth's crust, have been known since ancient times, although the pure metal was not prepared until 1808. The element is named after the Magnesia district in Thessaly, Greece, where large deposits of talc $\left[\mathrm{Mg}_{3} \mathrm{Si}_{4} \mathrm{O}_{10}(\mathrm{OH})_{2}\right]$ are found. There are many magnesium-containing minerals, including dolomite $\left(\mathrm{CaCO}_{3} \cdot \mathrm{MgCO}_{3}\right)$ and magnesite $\left(\mathrm{MgCO}_{3}\right)$, and the world's oceans provide a nearly infinite supply, since seawater is $0.13 \% \mathrm{Mg}$. When alloyed with aluminum, magnesium is used widely as a structural material because of its high strength, low density, and ease in machining. Airplane fuselages, automobile engines, and a great many other products are made of magnesium alloys.


Calcium Calcium is the fifth most abundant element in the earth's crust, owing largely to the presence of huge $\mathrm{CaSO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$ (gypsum) and $\mathrm{CaCO}_{3}$ deposits in ancient seabeds. Limestone, marble, chalk, and coral are all slightly different forms of $\mathrm{CaCO}_{3}$. Though the metal was not obtained in a pure form until 1808 , compounds of calcium have been known for millennia. Lime ( CaO ), for example, was prepared by the Romans by heating $\mathrm{CaCO}_{3}$ and was used as a mortar in their constructions. In fact, the name calcium is derived from the Latin word calx, meaning "lime."


A The gemstones beryl and emerald both contain beryllium.


A A sample of calcium.

The primary industrial use of calcium metal is as an alloying agent to harden aluminum. Calcium compounds such as lime and gypsum are used for many purposes throughout the chemical and construction industries. Portland cement, for example, contains approximately $70 \% \mathrm{CaO}$. In addition, calcium is the primary constituent of teeth and bones.

Strontium, Barium Strontium was discovered near, and named after, the small town of Strontian, Scotland, in 1787. There are no commercial uses for the pure metal, but the carbonate salt, $\mathrm{SrCO}_{3}$, is used in the manufacture of glass for color TV picture tubes. Barium is found principally in the minerals witherite $\left(\mathrm{BaCO}_{3}\right)$ and barite $\left(\mathrm{BaSO}_{4}\right)$, after which it is named. Though water-soluble salts of barium are extremely toxic, barium sulfate is so insoluble that it is used in medicine as a contrast medium for stomach and intestinal $X$ rays. Like strontium, barium metal has no commercial uses, but various compounds are used in glass manufacture and in drilling oil wells.

Radium Radium, the heaviest of the group 2A elements, occurs with uranium and was isolated as its chloride salt from the mineral pitchblende by Marie and Pierre Curie in 1898. Radium is highly radioactive, and no more than a few kilograms of the pure metal have ever been produced. Though used for many years as a radiation source for cancer radiotherapy, better sources are now available, and there are no longer any commercial uses for radium.

## Production of Alkaline Earth Metals

Like the alkali metals, the pure alkaline earth elements are produced commercially by reduction of their salts, either chemically or through electrolysis. Beryllium is prepared by reduction of $\mathrm{BeF}_{2}$ with magnesium, and magnesium is prepared by electrolysis of its molten chloride.

$$
\begin{array}{r}
\mathrm{BeF}_{2}(l)+\mathrm{Mg}(l) \xrightarrow{1300^{\circ} \mathrm{C}} \mathrm{Be}(l)+\mathrm{MgF}_{2}(l) \\
\mathrm{MgCl}_{2}(l) \xrightarrow[750^{\circ} \mathrm{C}]{\text { Electrolysis }} \mathrm{Mg}(l)+\mathrm{Cl}_{2}(g)
\end{array}
$$

Calcium, strontium, and barium are all made by high-temperature reduction of their oxides with aluminum metal.

$$
\begin{gathered}
3 \mathrm{MO}(l)+2 \mathrm{Al}(l) \xrightarrow{\text { High temp }} 3 \mathrm{M}(l)+\mathrm{Al}_{2} \mathrm{O}_{3}(s) \\
\text { where } \mathrm{M}=\mathrm{Ca}, \mathrm{Sr}, \mathrm{Ba}
\end{gathered}
$$

## Reactions of Alkaline Earth Metals

The alkaline earth metals undergo the same kinds of redox reactions that the alkali metals do, but they lose two electrons rather than one to yield dipositive ions, $\mathrm{M}^{2+}$. Because their first ionization energy is larger than that of alkali metals (Figure 6.3), the group 2A metals tend to be somewhat less reactive than alkali metals. The general reactivity trend is $\mathrm{Ba}>\mathrm{Sr}>\mathrm{Ca}>\mathrm{Mg}>\mathrm{Be}$.

Alkaline earth metals react with halogens to yield ionic halide salts, $\mathrm{MX}_{2}$, and with oxygen to form oxides, MO:

$$
\begin{aligned}
\mathrm{M}+\mathrm{X}_{2} \longrightarrow \mathrm{MX}_{2} & \text { where } \mathrm{M} \\
& =\mathrm{Be}, \mathrm{Mg}, \mathrm{Ca}, \mathrm{Sr}, \text { or } \mathrm{Ba} \\
\mathrm{X} & =\mathrm{F}, \mathrm{Cl}, \mathrm{Br}, \text { or } \mathrm{I}
\end{aligned}
$$

Beryllium and magnesium are relatively unreactive toward oxygen at room temperature, but both burn with a brilliant white glare when ignited by a flame. Calcium,
strontium, and barium are reactive enough that they are best stored under oil to keep them from contact with air. Like the heavier alkali metals, strontium and barium form peroxides, $\mathrm{MO}_{2}$.

With the exception of beryllium, the alkaline earth elements react with water to yield metal hydroxides, $\mathrm{M}(\mathrm{OH})_{2}$. Magnesium undergoes reaction only at temperatures above $100^{\circ} \mathrm{C}$; calcium and strontium react slowly with liquid water at room temperature. Only barium reacts vigorously.

$$
\begin{gathered}
\mathrm{M}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{M}^{2+}(a q)+2 \mathrm{OH}^{-}(a q)+\mathrm{H}_{2}(g) \\
\text { where } \mathrm{M}=\mathrm{Mg}, \mathrm{Ca}, \mathrm{Sr}, \text { or } \mathrm{Ba}
\end{gathered}
$$

## Worked Example 6.6

Calcium metal reacts with hydrogen gas at high temperature to give calcium hydride. Predict the formula of the product, and write the balanced equation.

## Strategy

Metal hydrides contain hydrogen with a -1 oxidation number. Since calcium always has $\mathrm{a}+2$ oxidation number, there must be two $\mathrm{H}^{-}$ions per $\mathrm{Ca}^{2+}$ ion.

## Solution

The formula of calcium hydride is $\mathrm{CaH}_{2}$.

$$
\mathrm{Ca}(s)+\mathrm{H}_{2}(g) \longrightarrow \mathrm{CaH}_{2}(s)
$$

- PROBLEM 6.16 Predict the products of the following reactions, and balance the equations:
(a) $\operatorname{Be}(s)+\mathrm{Br}_{2}(l) \rightarrow$ ?
(b) $\mathrm{Sr}(s)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow$ ?
(c) $\mathrm{Mg}(s)+\mathrm{O}_{2}(g) \rightarrow$ ?
- PROBLEM 6.17 Write a balanced equation for the preparation of beryllium metal by the reduction of beryllium chloride with potassium.
- PROBLEM 6.18 What product do you think is formed by reaction of magnesium with sulfur, a group 6A element? What is the oxidation number of sulfur in the product?


## 6.9 | The Group 3A Elements: Aluminum

The elements in group $3 \mathrm{~A}-\mathrm{B}, \mathrm{Al}, \mathrm{Ga}$, In, and Tl -are the first of the $p$-block elements (Section 5.12) and have the valence-shell electron configuration $n s^{2} n p^{1}$. With the exception of boron, which behaves as a semimetal rather than a metal, the group 3A elements are silvery in appearance, good conductors of electricity, and relatively soft. Gallium, in fact, has a melting point of only $29.8^{\circ} \mathrm{C}$. Although properties of the entire group are listed in Table 6.6, we'll concentrate for now on the most common element, aluminum, and look at the others in Chapter 19.

Lee R. Summerlin, Christie L.
Borgford, and Julie B. Ealy, "Producing Hydrogen Gas from Calcium Metal," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 51-52.


A Calcium metal reacts very slowly with water at room temperature.

TABLE 6.6 Properties of Group 3A Elements

| Name | Melting <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | Boiling <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | Density <br> $\left(\mathbf{g} / \mathbf{c m}^{3}\right)$ | First Ionization <br> Energy (kJ/mol) | Abundance <br> on Earth $(\%)$ | Atomic <br> Radius (pm) | Ionic (Madius $(\mathbf{M +})$ <br> Rm) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Boron | 2075 | 4000 | 2.34 | 800.6 | 0.001 | 83 | - |
| Aluminum | 660 | 2519 | 2.699 | 577.6 | 8.32 | 143 | 51 |
| Gallium | 29.8 | 2204 | 5.904 | 578.8 | 0.0015 | 135 | 62 |
| Indium | 157 | 2072 | 7.31 | 558.3 | 0.00001 | 167 | 81 |
| Thallium | 304 | 1473 | 11.85 | 589.3 | 0.00004 | 170 | 95 |


© When completed in 1884, the Washington Monument was capped with a pyramid of pure aluminum, a precious metal at the time.


A Aluminum metal reacts with liquid bromine in a spectacular display of sparks.

Aluminum, the most abundant metal in the earth's crust at $8.3 \%$, takes its name from alum, $\mathrm{KAl}\left(\mathrm{SO}_{4}\right)_{2} \cdot 12 \mathrm{H}_{2} \mathrm{O}$, a salt that has been used medicinally since Roman times. In spite of its abundance, the metal nevertheless proved difficult to isolate in pure form. It was such a precious substance in the midnineteenth century, in fact, that aluminum cutlery was sometimes used for elegant dinners, and the Washington Monument was capped by a pyramid of pure aluminum. Not until 1886 did an economical manufacturing process become available.

Aluminum occurs in many common minerals and clays, as well as in gemstones. Sapphire and ruby are both impure forms of $\mathrm{Al}_{2} \mathrm{O}_{3}$ and receive their color from the presence of small amounts of other elements ( Cr in ruby; Fe and Ti in sapphire). Most aluminum is currently obtained from bauxite, $\mathrm{Al}_{2} \mathrm{O}_{3} \cdot x \mathrm{H}_{2} \mathrm{O}$, which occurs in large deposits in Australia, the United States, Jamaica, and elsewhere. The preparation of Al from ores is extremely energyintensive, requiring high temperatures and large amounts of electric current to carry out the electrolysis of $\mathrm{Al}_{2} \mathrm{O}_{3}$. We'll examine the process in more detail in Section 18.12.

$$
2 \mathrm{Al}_{2} \mathrm{O}_{3}(\text { soln }) \xrightarrow[980^{\circ} \mathrm{C}]{\substack{\text { Electrolysis } \\ \text { in } \mathrm{Na}_{3} \mathrm{AlF}_{6}}} 4 \mathrm{Al}(l)+3 \mathrm{O}_{2}(g)
$$

Continuing the trend established by the group 1A and group 2A metals, aluminum is a reducing agent that undergoes redox reactions by losing all three valence-shell electrons to yield $\mathrm{Al}^{3+}$ ions. For example, it reacts with the halogens to yield colorless halides, $\mathrm{AlX}_{3}$, with oxygen to yield an oxide, $\mathrm{Al}_{2} \mathrm{O}_{3}$, and with nitrogen to yield a nitride, AlN:

$$
\begin{aligned}
2 \mathrm{Al}+3 \mathrm{X}_{2} & \longrightarrow 2 \mathrm{AlX}_{3} \quad \text { where } \mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{Br}, \text { or } \mathrm{I} \\
4 \mathrm{Al}+3 \mathrm{O}_{2} & \longrightarrow 2 \mathrm{Al}_{2} \mathrm{O}_{3} \\
2 \mathrm{Al}+\mathrm{N}_{2} & \longrightarrow 2 \mathrm{AlN}
\end{aligned}
$$

Reactions with the halogens occur vigorously at room temperature and release large amounts of heat. Reaction with oxygen is also vigorous at room temperature, yet aluminum can be used in a huge array of consumer products without evident corrosion from the air. The explanation for this apparent inconsistency is that aluminum metal reacts rapidly with oxygen only on its surface. In so doing, it forms a thin, hard, oxide coating that does not flake off and that protects the underlying metal from contact with air.

Aluminum is less reactive than the group 1 A and 2 A metals and does not normally react with water because of the oxide coating mentioned previously. It does, however, react with both acidic and basic solutions to give $\mathrm{Al}^{3+}$ ions and release $\mathrm{H}_{2}$ gas.

Acid solution:

$$
\begin{aligned}
2 \mathrm{Al}(s)+6 \mathrm{H}^{+}(a q) & \longrightarrow 2 \mathrm{Al}^{3+}(a q)+3 \mathrm{H}_{2}(g) \\
2 \mathrm{Al}(s)+2 \mathrm{OH}^{-}(a q)+6 \mathrm{H}_{2} \mathrm{O}(l) & \longrightarrow 2 \mathrm{Al}(\mathrm{OH})_{4}^{-}(a q)+3 \mathrm{H}_{2}(g)
\end{aligned}
$$

Basic solution:

PROBLEM 6.19 Identify the oxidizing agent and the reducing agent in the reaction of aluminum metal with $\mathrm{H}^{+}(a q)$.

- PROBLEM 6.20 Aluminum reacts with sulfur to give a sulfide in the same way that it reacts with oxygen to give an oxide. Identify the product, and write a balanced equation for the reaction.


### 6.10 | The Halogens (Group 7A)

The halogens in group 7A-F, Cl, Br, I, and At—are completely different from the elements we've been discussing up to this point. The halogens are nonmetals rather than metals, they exist as diatomic molecules rather than as individual atoms, and they have a tendency to gain rather than lose electrons when they enter into redox reactions because of their $n s^{2} n p^{5}$ electron configurations. In other words, the halogens are powerful oxidizing agents, characterized by large negative electron affinities and large positive ionization energies. Some of their properties are listed in Table 6.7.


TABLE 6.7 Properties of Halogens

| Name | Melting <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | Boiling <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | Density <br> $\left(\mathbf{g} / \mathbf{c m}^{3}\right)$ | Electron <br> Affinity $(\mathbf{k J} / \mathbf{m o l})$ | Abundance <br> on Earth $(\%)$ | Atomic <br> Radius $(\mathbf{p m})$ | Ionic $\left(\mathbf{X}^{-}\right)$ <br> Radius (pm) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Fluorine | -220 | -188 | $1.50(l)$ | -328 | 0.062 | 72 | 133 |
| Chlorine | -101 | -34 | $2.03(l)$ | -349 | 0.013 | 99 | 181 |
| Bromine | -7 | 59 | $3.12(l)$ | -325 | 0.0003 | 114 | 196 |
| Iodine | 114 | 184 | $4.930(s)$ | -295 | 0.00005 | 133 | 220 |
| Astatine | - | - | - | -270 | Trace | - | - |

Halogens are too reactive to occur in nature as free elements. Instead, they are found only as their anions in various salts and minerals. Even the name "halogen" implies reactivity, since it comes from the Greek words hals (salt) and gennan (to form). Thus, a halogen is literally a "salt former."

## Occurrence and Uses of Halogens

Fluorine Fluorine, a corrosive, pale-yellow gas, is the thirteenth most abundant element in the earth's crust, more common than such well-known elements as sulfur (16th), carbon (17th), and copper (26th). It is found in several common minerals including fluorspar, or fluorite $\left(\mathrm{CaF}_{2}\right)$, and fluorapatite $\left[\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{~F}\right]$. (Note that fluorine is spelled with the $u$ first as in $f l u$ rather than with the $o$ first as in flour.)

In spite of its toxicity and extreme reactivity, fluorine is widely used for the manufacture of polymers such as Teflon, $\left(\mathrm{C}_{2} \mathrm{~F}_{4}\right)_{n}$. Fluorine is also important in the production of $\mathrm{UF}_{6}$, used in the separation of uranium isotopes for nuclear power plants, and fluoride ion is added to toothpaste in the form of NaF to help prevent tooth decay.

Chlorine Chlorine is a toxic, reactive, greenish-yellow gas that must be handled with great care. Though chlorine is only the twentieth most abundant element in crustal rocks, there are vast additional amounts of chloride ion in the world's oceans ( $1.9 \%$ by mass). The free element was first prepared in 1774 by oxidation of NaCl with $\mathrm{MnO}_{2}$, although not until 1810 was it recognized that the product of the reaction was indeed a new element rather than a compound.

$$
\mathrm{MnO}_{2}(s)+2 \mathrm{Cl}^{-}(a q)+4 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Mn}^{2+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{Cl}_{2}(g)
$$

Industrial applications of chlorine center around its uses for the preparation of numerous chlorinated organic chemicals, including PVC [poly(vinyl chloride)] plastic and the solvents chloroform $\left(\mathrm{CHCl}_{3}\right)$, methylene chloride $\left(\mathrm{CH}_{2} \mathrm{Cl}_{2}\right)$, and ethylene dichloride $\left(\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Cl}_{2}\right)$. Large amounts of chlorine are also used as a bleach during paper manufacture and as a disinfectant for swimming pools and municipal water supplies.


- Chlorine and chlorinereleasing compounds are frequently added as a disinfectant to the water in swimming pools.

Bromine Bromine, a fourth-row element, is a volatile, reddish liquid rather than a gas like fluorine and chlorine. Its fumes are quite toxic, however, and it causes extremely painful burns when spilled on bare skin. Bromine was first isolated in 1826 by the 23 -year-old French chemist A.-J. Balard by oxidation of KBr with $\mathrm{MnO}_{2}$ in a manner similar to that used for the synthesis of chlorine.

$$
\mathrm{MnO}_{2}(s)+2 \mathrm{Br}^{-}(a q)+4 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Mn}^{2+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{Br}_{2}(a q)
$$

The primary uses of bromine are as its silver salt, AgBr , in photographic emulsions and as a reactant for preparing brominated organic compounds. Fuel additives, pesticides, fungicides, and flame retardants are a few of the many kinds of compounds manufactured from bromine.
lodine Iodine is a volatile purple-black solid with a beautiful metallic sheen. As the least reactive halogen, iodine is safe to handle and is widely used as a skin disinfectant. It was first prepared in 1811 from seaweed ash, but commercially useful deposits of the iodine-containing minerals lautarite $\left(\mathrm{CaIO}_{3}\right)$ and dietzeite [ $7 \mathrm{Ca}\left(\mathrm{IO}_{3}\right)_{2} \cdot 8 \mathrm{CaCrO}_{4}$ ] were subsequently found in Chile. Iodine is used in the preparation of numerous organic compounds, including dyes and pharmaceutical agents, but there is no one single use of major importance.
Astatine Astatine, like francium in group 1 A , is a radioactive element that occurs only in minute amounts in nature. No more than about $5 \times 10^{-8} \mathrm{~g}$ has ever been prepared at one time, and little is known about its chemistry.

## Production of Halogens

All the free halogens are produced commercially by oxidation of their anions. Fluorine and chlorine are both produced by electrolysis: fluorine from a molten 1:2 mixture of KF and HF , and chlorine from molten NaCl .

$$
\begin{gathered}
2 \mathrm{HF}(l) \xrightarrow[100^{\circ} \mathrm{C}]{\text { Electrols }} \mathrm{H}_{2}(g)+\mathrm{F}_{2}(g) \\
2 \mathrm{NaCl}(l) \xrightarrow[580^{\circ} \mathrm{C}]{\text { Electys }} 2 \mathrm{Na}(l)+\mathrm{Cl}_{2}(g)
\end{gathered}
$$

Bromine and iodine are both prepared by oxidation of the corresponding halide ion with chlorine. Naturally occurring aqueous solutions of bromide ion with concentrations of up to 5000 ppm are found in Arkansas and in the Dead Sea in Israel. Iodide ion solutions of up to 100 ppm concentration are found in Oklahoma and Michigan.

$$
\left.\begin{array}{rl}
2 \mathrm{Br}^{-}(a q) & +\mathrm{Cl}_{2}(g)
\end{array}>\mathrm{Br}_{2}(l)+2 \mathrm{Cl}^{-}(a q)\right) ~=\mathrm{I}^{-}(a q)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{I}_{2}(s)+2 \mathrm{Cl}^{-}(a q)
$$

## Reactions of Halogens

Halogens are among the most reactive elements in the periodic table. Fluorine, in fact, forms compounds with every element except the noble gases $\mathrm{He}, \mathrm{Ne}$, and Ar . As noted previously, the dominant reaction of halogens is as strong oxidizing agents in redox reactions. That is, their large negative electron affinities allow halogens to accept electrons from other atoms to yield halide anions, $\mathrm{X}^{-}$.

Reaction with Metals Halogens react with every metal in the periodic table to yield metal halides. With the alkali and alkaline earth metals, the formula of the halide product is easily predictable. With transition metals, though, more than one product can sometimes form depending on the reaction conditions and the amounts
of reactants present. Iron, for example, can react with $\mathrm{Cl}_{2}$ to form either $\mathrm{FeCl}_{2}$ or $\mathrm{FeCl}_{3}$. Without knowing a good deal more about transition-metal chemistry, it's not possible to make predictions at this point. The reaction can be generalized as

$$
\begin{aligned}
2 \mathrm{M}+n \mathrm{X}_{2} \longrightarrow 2 \mathrm{MX}_{n} \quad \text { where } \mathrm{M} & =\text { Metal } \\
\mathrm{X} & =\mathrm{F}, \mathrm{Cl}, \mathrm{Br}, \mathrm{I}
\end{aligned}
$$

Unlike the metallic elements, halogens become less reactive going down the periodic table because of their generally decreasing electron affinity. Thus, their reactivity order is $\mathrm{F}_{2}>\mathrm{Cl}_{2}>\mathrm{Br}_{2}>\mathrm{I}_{2}$. Fluorine often reacts violently, chlorine and bromine somewhat less so, and iodine often sluggishly.
Reaction with Hydrogen Halogens react with hydrogen gas to yield hydrogen halides, HX:

$$
\mathrm{H}_{2}(g)+\mathrm{X}_{2} \longrightarrow 2 \mathrm{HX}(g) \quad \text { where } \mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{Br}, \mathrm{I}
$$

Fluorine reacts explosively with hydrogen as soon as the two gases come in contact. Chlorine also reacts explosively once the reaction is initiated by a spark or by ultraviolet light, but the mixture of gases is stable in the dark. Bromine and iodine react more slowly.

The hydrogen halides are valuable because they behave as acids when dissolved in water. Hydrogen fluoride is a weak acid, dissociating only to a small extent in aqueous solution, but the other hydrogen halides are strong acids. As one of the few substances that reacts with glass, HF is frequently used for the etching or fogging of glass. The aqueous solution of HCl , called hydrochloric acid or muriatic acid, is used throughout the chemical industry in a vast number of processes, from pickling steel (removing its iron oxide coating) to dissolving animal bones for producing gelatin.

$$
\mathrm{HX} \xrightarrow[\text { in } \mathrm{H}_{2} \mathrm{O}]{\text { Dissolve }} \mathrm{H}^{+}(a q)+\mathrm{X}^{-}(a q)
$$

Reaction with Other Halogens Since all the halogens are diatomic molecules $\mathrm{X}_{2}$, it's not too surprising that a variety of covalent interhalogen compounds $X Y$ also exist, where $X$ and $Y$ are different halogens. Iodine reacts with chlorine, for example, to yield iodine monochloride ( ICl ), and bromine reacts with fluorine to yield bromine monofluoride ( BrF ). These reactions can be thought of as redox processes in which the lighter, more reactive element is the oxidizing agent and the heavier, less reactive element is the reducing agent. In the reaction of iodine with chlorine, for example, $\mathrm{Cl}_{2}$ acts as the oxidizing agent and is reduced to a -1 oxidation state, while $I_{2}$ acts as the reducing agent and is oxidized to a +1 oxidation state.


As a general rule, the properties of interhalogen compounds are intermediate between those of their parent elements. For example, ICl is a red solid that melts near room temperature, and BrF is a brownish gas that condenses to a liquid near room temperature. All six possible diatomic interhalogen compounds are known, and all act as strong oxidizing agents in redox reactions.

$\Delta$ Gaseous HF is one of the few substances that reacts with and etches glass $\left(\mathrm{SiO}_{2}\right)$, according to the equation $\mathrm{SiO}_{2}(s)+4 \mathrm{HF}(g) \rightarrow$ $\mathrm{SiF}_{4}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)$.

In addition to the diatomic interhalogen compounds, a number of polyatomic substances with formulas $X Y_{3}, X Y_{5}$, and $X Y_{7}$ are also known. Typical examples are $\mathrm{ClF}_{3}, \mathrm{BrF}_{5}$, and $\mathrm{IF}_{7}$. Once again, the less reactive halogen has a positive oxidation number and the more reactive halogen has a negative oxidation number. In $\mathrm{BrF}_{5}$, for example, the oxidation number of Br is +5 and that of each F is -1 .

## Worked Example 6.7

The $\mathrm{UF}_{6}$ used in producing nuclear fuels is prepared by reaction of uranium metal with chlorine trifluoride. Tell which atoms have been oxidized and which reduced, and balance the equation.

$$
\mathrm{U}(s)+\mathrm{ClF}_{3}(l) \longrightarrow \mathrm{UF}_{6}(l)+\mathrm{ClF}(g) \quad \text { Unbalanced }
$$

## Strategy

Assign oxidation numbers to the various elements, and then decide which atoms have undergone a change. Those that have increased in oxidation number have been oxidized, and those that have decreased in oxidation number have been reduced.

## SOlution

Uranium is oxidized from 0 to +6 , and chlorine is reduced from +3 to +1 .


Balance the equation, either by inspection or by one of the methods discussed in Sections 4.9 and 4.10.

$$
\mathrm{U}(s)+3 \mathrm{ClF}_{3}(l) \longrightarrow \mathrm{UF}_{6}(l)+3 \mathrm{ClF}(g)
$$

- PROBLEM 6.21 Write the products of the following reactions, and balance the equations:
(a) $\mathrm{Br}_{2}(l)+\mathrm{Cl}_{2}(g) \rightarrow$ ?
(b) $\mathrm{Al}(s)+\mathrm{F}_{2}(g) \rightarrow$ ?
(c) $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(s) \rightarrow$ ?
- PROBLEM 6.22 Bromine reacts with sodium iodide to yield iodine and sodium bromide. Identify the oxidizing and reducing agents, and write the balanced equation.


### 6.11 The Noble Gases (Group 8A)


-

The noble gases in group $8 \mathrm{~A}-\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}, \mathrm{Kr}, \mathrm{Xe}$, and Rn —are completely different from the other elements we've been discussing. They are neither metals like most elements nor reactive nonmetals like the halogens; rather, they are colorless, odorless, unreactive gases. Their $1 s^{2}$ (for He) and $n s^{2} n p^{6}$ (for the others) valence-shell electron configurations make it difficult for the noble gases to either gain or lose electrons, so the elements don't normally enter into redox reactions.

Though sometimes referred to as "rare gases" or "inert gases," these older names are not really accurate because the group 8A elements are neither rare nor completely inert. Argon, for instance, makes up nearly $1 \%$ by volume of dry air, and there are several dozen known compounds of krypton and xenon, although none occur naturally. Some properties of the noble gases are listed in Table 6.8.

TABLE 6.8 Properties of Noble Gases

| Name | Melting <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | Boiling <br> Point $\left({ }^{\circ} \mathbf{C}\right)$ | First Ionization <br> Energy $(\mathbf{k J / m o l})$ | Abundance <br> in Dry Air (Vol \%) |
| :--- | :--- | :--- | :--- | :--- |
| Helium | -272.2 | -268.9 | 2372.3 | $5.2 \times 10^{-4}$ |
| Neon | -248.6 | -246.1 | 2080.6 | $1.8 \times 10^{-3}$ |
| Argon | -189.3 | -185.9 | 1520.4 | 0.93 |
| Krypton | -157.4 | -153.2 | 1350.7 | $1.1 \times 10^{-4}$ |
| Xenon | -111.8 | -108.0 | 1170.4 | $9 \times 10^{-6}$ |
| Radon | -71 | -61.7 | 1037 | Trace |

## Occurrence and Uses of Noble Gases

The natural abundance of the noble gas elements depends on where you look. In the universe, helium is the second most abundant element, accounting for about $25 \%$ of the total mass (hydrogen accounts for the other 75\%). On Earth, though, the fact that they're gases means that the abundance of the group 8A elements in crustal rocks is very low. Helium occurs as a minor constituent of natural gas, and argon makes up about $1 \%$ of the volume of dry air. The remaining noble gases occur in small amounts in the air (Table 6.8), from which they are obtained by liquefaction and distillation.

Their relative lack of reactivity means that the main commercial uses of the noble gases are in applications that require an inert (unreactive) atmosphere. Argon, for example, is used as the gas in lightbulbs and to protect the metal from oxygen during arc welding. Liquid helium is used in scientific research as a cooling agent for extremely low-temperature studies because it has the lowest boiling point (4.2 K) of any substance. Helium is also used in deep-sea diving gas.

Radon, the heaviest of the noble gases, has been much publicized in recent years because of a fear that low-level exposures increase the risk of cancer. Like astatine and francium, its neighbors in the periodic table, radon is a radioactive element with only a minute natural abundance. It is produced by radioactive decay of the radium present in small amounts in many granitic rocks, and it can slowly seep into basements, where it remains unless vented. If breathed into the lungs, it can cause radiation damage.

## Reactions of Noble Gases

Helium, neon, and argon undergo no chemical reactions and form no known compounds; krypton and xenon react only with fluorine. Depending on the reaction conditions and on the amounts of reactants present, xenon can form three different fluorides, $\mathrm{XeF}_{2}, \mathrm{XeF}_{4}$, and $\mathrm{XeF}_{6}$. All three xenon fluorides are powerful oxidizing agents and undergo a wide variety of redox reactions.

$$
\begin{aligned}
\mathrm{Xe}(g)+\mathrm{F}_{2}(g) & \longrightarrow \mathrm{XeF}_{2}(s) \\
\mathrm{Xe}(g)+2 \mathrm{~F}_{2}(g) & \longrightarrow \mathrm{XeF}_{4}(s) \\
\mathrm{Xe}(g)+3 \mathrm{~F}_{2}(g) & \longrightarrow \mathrm{XeF}_{6}(s)
\end{aligned}
$$

The lack of reactivity of the noble gases is a consequence of their unusually large ionization energies (Figure 6.3) and their unusually small electron affinities (Figure 6.6), which result from their valence-shell electron configurations.

- PROBLEM 6.23 Assign oxidation numbers to the elements in the following compounds of xenon:
(a) $\mathrm{XeF}_{2}$
(b) $\mathrm{XeF}_{4}$
(c) $\mathrm{XeOF}_{4}$


A A helium-oxygen mixture is used in diving gas instead of compressed air (nitrogenoxygen). If air were used, nitrogen would dissolve in the diver's blood at the high underwater pressures and would be released as painful bubbles when the diver returned to the surface.

$\mathrm{XeF}_{6}$

### 6.12 | The Octet Rule

Let's list some general conclusions about main-group elements that we can draw from the information in Sections 6-7-6.11:

- Group 1A elements tend to lose their $n s^{1}$ valence-shell electron, thereby adopting the electron configuration of the noble gas element in the previous row of the periodic table.
- Group 2A elements tend to lose both of their $n s^{2}$ valence-shell electrons and adopt a noble gas electron configuration.
- Group 3A elements tend to lose all three of their $n s^{2} n p^{1}$ valence-shell electrons and adopt a noble gas electron configuration.
- Group 7A elements tend to gain one electron, changing from $n s^{2} n p^{5}$ to $n s^{2} n p^{6}$, thereby adopting the configuration of the neighboring noble gas element in the same row.
- Group 8A (noble gas) elements are essentially inert; they rarely gain or lose electrons.

All these observations can be gathered into a single statement called the octet rule:
octet rule Main-group elements tend to undergo reactions that leave them with eight outer-shell electrons. That is, main-group elements react so that they attain a noble gas electron configuration with filled $s$ and $p$ sublevels in their valence electron shell.

There are many exceptions to the octet rule-after all, it's called the octet rule, not the octet law-but it is nevertheless useful for making predictions and for providing insights about chemical bonding.

Why does the octet rule work? What factors determine whether an atom is likely to gain or to lose electrons? Clearly, electrons are most likely to be lost if they are held loosely in the first place-that is, if they feel a relatively low effective nuclear charge, $Z_{\text {eff, }}$ and therefore have small ionization energies. Valence-shell electrons in the group 1A, 2A, and 3A metals, for example, are shielded from the nucleus by core electrons. They feel a low $Z_{\text {eff }}$, and they are therefore lost relatively easily. Once the next lower noble gas configuration is reached, though, loss of an additional electron is much more difficult because it must come from an inner shell where it feels a high $Z_{\text {eff }}$.

Conversely, electrons are most likely to be gained if they can be held tightly by a high $Z_{\text {eff }}$. Valence-shell electrons in the group 6A and 7A elements, for example, are poorly shielded. They feel high values of $Z_{\text {eff }}$, and they aren't lost easily. The high $Z_{\text {eff }}$ thus makes possible the gain of one or more additional electrons into vacant valence-shell orbitals. Once the noble gas configuration is reached, though, there are no longer any low-energy orbitals available. An additional electron would have to be placed in a higher-energy orbital, where it would feel only a low $Z_{\text {eff }}$.

Eight is therefore the "magic number" for valence-shell electrons. Taking electrons from a filled octet is difficult because they are tightly held by a high $\mathrm{Z}_{\text {eff }}$; adding more electrons to a filled octet is difficult because, with $s$ and $p$ sublevels full, there is no low-energy orbital available.

$$
\left.\begin{array}{cll}
\frac{\downarrow \uparrow}{(n-1) s^{2}} & \frac{\downarrow \uparrow}{(n-1) p^{6}} & \frac{\downarrow \uparrow}{n s^{1}}
\end{array} \begin{array}{l}
\text { Strongly shielded; low } Z_{\text {eff }} ; \\
\text { easy to remove }
\end{array}\right] \begin{aligned}
& \text { Poorly shielded; high } Z_{\text {eff; }} \\
& \frac{\downarrow \uparrow}{n s^{2}}
\end{aligned}
$$

$$
\begin{array}{lll}
\frac{\downarrow \uparrow}{n s^{2}} & \frac{\downarrow \uparrow}{n p^{6}} \frac{\downarrow \uparrow}{(n+1) s} & \begin{array}{l}
\text { Strongly shielded; low } Z_{\text {eff }} \\
\text { hard to add }
\end{array} \\
\frac{\downarrow \uparrow}{n s^{2}} & \frac{\downarrow \uparrow}{n p^{5}} \frac{\downarrow \uparrow}{} \frac{\downarrow}{(n+1) s} & \begin{array}{l}
\text { Poorly shielded; high } Z_{\text {effi }} \\
\text { easy to add }
\end{array}
\end{array}
$$

When the octet rule fails, it generally does so for elements toward the right side of the periodic table (groups $3 \mathrm{~A}-8 \mathrm{~A}$ ) that are in the third row and lower (Figure 6.10). The reason has to do with the electron configurations of these elements: With few exceptions, the main-group elements that occasionally break the octet rule have vacant, low-energy $d$ orbitals, which allow them to accommodate additional electrons. Phosphorus, for example, has the electron configuration $[\mathrm{Ne}]$ $3 s^{2} 3 p^{3}$ and has a vacant $3 d$ subshell that is only slightly higher in energy than the $3 s$ and $3 p$ levels. As a result, phosphorus is occasionally able to add more than the three electrons predicted by the octet rule.


## Worked Example 6.8

We saw in Section 6.7 that lithium reacts with nitrogen to yield $\mathrm{Li}_{3} \mathrm{~N}$. What noble gas configuration does the nitrogen atom in $\mathrm{Li}_{3} \mathrm{~N}$ have?

## Solution

The nitrogen atom in $\mathrm{Li}_{3} \mathrm{~N}$ has an oxidation number of -3 and has gained three electrons over the neutral atom, giving it a valence-shell octet with the neon configuration:

N configuration: $\left(1 s^{2} 2 s^{2} 2 p^{3}\right) \quad \mathrm{N}^{3-}$ configuration: $\left(1 s^{2} 2 s^{2} 2 p^{6}\right)$

PROBLEM 6.24 What noble gas configurations are the following elements likely to adopt in redox reactions?
(a) Rb
(b) Ba
(c) Ga
(d) F

PROBLEM 6.25 Although we haven't talked about group 6A elements in this chapter, what are they likely to do in redox reactions-gain or lose electrons? How many?

FIGURE 6.10 The octet rule occasionally fails for the shaded main-group elements. These elements, all of which are in the third row or lower, can use low-energy unfilled $d$ orbitals to expand their valence shell beyond the normal octet.

## Interlude Salt

 Wieliczka mine is 101 meters below the surface and is over 50 meters long, 15 meters wide, and 12 meters high.
f you're like most people, you probably feel a little guilty about reaching for the saltshaker at mealtime. The notion that high salt intake and high blood pressure go hand in hand is surely among the most highly publicized pieces of nutritional lore to appear in recent decades.

Salt has not always been held in such disrepute. Historically, salt has been prized since the earliest recorded times as a seasoning and a food preservative. Words and phrases in many languages reflect the importance of salt as a life-giving and life-sustaining substance. We refer to a kind and generous person as "the salt of the earth," for instance, and we speak of being "worth one's salt." In Roman times, soldiers were paid in salt; the English word "salary" is derived from the Latin word for paying salt wages (salarium).

Salt is perhaps the easiest of all minerals to obtain and purify. The simplest method, used for thousands of years throughout the world in coastal climates where sunshine is abundant and rainfall is scarce, is to evaporate seawater. Though the exact amount varies depending on the source, seawater contains an average of about $3.5 \%$ by mass of dissolved substances, most of which is sodium chloride. It has been estimated that evaporation of all the world's oceans would yield approximately 4.5 million cubic miles of NaCl .

Only about $10 \%$ of current world salt production comes from evaporation of seawater. Most salt is obtained by mining the vast deposits of halite, or rock salt, formed by evaporation of ancient inland seas. These salt beds vary in thickness up to hundreds of meters and vary in depth from a few meters to thousands of meters below the earth's surface. Salt mining has gone on for at least 3400 years, and the Wieliczka mine in Galicia, Poland, has been worked continuously from A.D. 1000 to the present.

Let's get back now to the dinner table. What about the link between dietary salt intake and high blood pressure? There's no doubt that most people in industrialized nations have a relatively high salt intake, and there's no doubt that high blood pressure among industrialized populations is on the rise. What's not so clear is how the two observations are related.

The case against salt has been made largely by comparing widely diverse populations with different dietary salt intakes-by comparing the health of modern Americans with that of inhabitants of the Amazon rain forest, for example. Obviously, though, industrialization brings with it far more changes than simply an increase in dietary salt intake, and many of these other changes may be much more important than salt in contributing to hypertension.

In a study called the DASH-Sodium study, published in 2001, a strong correlation was found between a change in salt intake and a change in blood pressure. When volunteers cut back their salt intake from 8.3 g per day-roughly what Americans typically consume-to 3.8 g per day, significant drops in blood pressure were found. The largest reduction in blood pressure was seen in people already diagnosed with hypertension, but subjects with normal blood pressure also lowered their readings by several percent.

What should an individual do? The best answer, as in so many things, is to use moderation and common sense. People with hypertension should make a strong effort to lower their sodium intake; others might be well advised to choose unsalted snacks, use less salt in preparing food, and read nutrition labels for sodium content.

- PROBLEM 6.26 How is salt obtained commercially?


## Summary

Metallic elements on the left side of the periodic table have a tendency to give up electrons to form cations, while the halogens and a few other nonmetallic elements on the right side of the table have a tendency to accept electrons to form anions. The electrons given up by a main-group metal in forming a cation come from the highest-energy occupied orbital, while the electrons that are accepted by a nonmetal in forming an anion go into the lowest-energy unoccupied orbital. Sodium metal, for instance, loses its valence-shell $3 s$ electron to form an $\mathrm{Na}^{+}$ion with the electron configuration of neon, while chlorine gains a $3 p$ electron to form a $\mathrm{Cl}^{-}$anion with the electron configuration of argon.

The amount of energy necessary to remove a valence electron from an isolated neutral atom is called the atom's ionization energy ( $E_{i}$ ). Ionization energies are smallest for metallic elements on the left side of the periodic table and largest for nonmetallic elements on the right side. As a result, metals can act as electron donors (reducing agents) in chemical reactions.

Ionization is not limited to the removal of a single electron from an atom. Two, three, or even more electrons can be removed sequentially from an atom, although larger amounts of energy are required for each successive ionization step. In general, valence-shell electrons are much more easily removed than core electrons.

The amount of energy released or absorbed when an electron adds to an isolated neutral atom is called the atom's electron affinity ( $E_{\text {ea }}$ ). By convention, a negative $E_{\text {ea }}$ corresponds to a release of energy and a positive $E_{\text {ea }}$ corresponds to an absorption of energy. Electron affinities are most negative for group 7A elements and most positive for group 2A and 8A elements. As a result, the group 7A elements can act as electron acceptors (oxidizing agents) in chemical reactions.

Main-group metallic elements in groups 1A, 2A, and 3A undergo redox reactions with halogens in group 7A, during which the metal loses one or more electrons to the halogen. The product, a metal halide such as NaCl , is an ionic solid that consists of metal cations and halide anions electrostatically attracted to one another by ionic bonds. The sum of the interaction energies among all ions in a crystal is called the crystal's lattice energy $(U)$.

In general, redox reactions of main-group elements can be described by the octet rule, which states that these elements tend to undergo reactions so as to attain a noble gas electron configuration with filled $s$ and $p$ sublevels in their valence shell. Elements on the left side of the periodic table tend to give up electrons until a noble gas configuration is reached; elements on the right side of the table tend to accept electrons until a noble gas configuration is reached; and the noble gases themselves are essentially unreactive.

Key Words

Born-Haber cycle 213
core electron 205
Coulomb's law 213
electron affinity $\left(E_{\text {ea }}\right), 209$
ionic bond 211
ionic solid 211 ionization energy
( $E_{\mathrm{i}}$ ) 205
lattice energy ( $\boldsymbol{U}$ ) 213
octet rule 230

## Key Concept Summary



## Understanding Key Concepts

Problems 6.1-6.26 appear within the chapter.
6.27 Where on the blank outline of the periodic table do the following elements appear?
(a) Main groups
(b) Halogens
(c) Alkali metals
(d) Noble gases
(e) Alkaline earths
(f) Group 3A elements
(g) Lanthanides

6.28 Which of the following drawings is more likely to represent an ionic compound, and which a covalent compound?

6.29 Circle the approximate part or parts of the periodic table where the following elements appear:
(a) Elements with the smallest values of $E_{i 1}$
(b) Elements with the largest atomic radii
(c) Elements with the most negative values of $E_{\text {ea }}$

6.30 Where on the periodic table would you find the element that has an ion with each of the following electron configurations? Identify each ion.
(a) $3+$ ion: $1 s^{2} 2 s^{2} 2 p^{6}$
(b) $3+$ ion: $[\mathrm{Ar}] 3 d^{3}$
(c) $2+$ ion: $[\mathrm{Kr}] 5 s^{2} 4 d^{10}$
(d) $1+$ ion: $[\mathrm{Kr}] 4 d^{10}$

6.31 Which of the following spheres is likely to represent a metal, and which a nonmetal? Which sphere in the products represents a cation, and which an anion?

6.32 Each of the pictures (a)-(d) represents one of the following substances at $25^{\circ} \mathrm{C}$ : sodium, chlorine, iodine, sodium chloride. Which picture corresponds to which substance?

6.33 Which of the following alkali metal halides has the largest lattice energy, and which has the smallest lattice energy? Explain.

(a)

(b)

(c)
6.34 Three binary compounds are represented on the following drawing-red with red, blue with blue, and green with green. Give a likely formula for each compound, and assign oxidation numbers in each.

6.35 Given the following values for the formation of LiCl from its elements, draw a Born-Haber cycle similar to that shown in Figure 6.8.
$E_{\text {ea }}$ for $\mathrm{Cl}=-348.6 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Li}=+159.4 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 1}$ for $\mathrm{Li}=+520 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{Cl}_{2}=+243 \mathrm{~kJ} / \mathrm{mol}$
Lattice energy for $\mathrm{LiCl}=+853 \mathrm{~kJ} / \mathrm{mol}$

## Additional Problems

## Ions, Ionization Energy, and Electron Affinity

6.36 What are the likely ground-state electron configurations of the following cations?
(a) $\mathrm{La}^{3+}$
(b) $\mathrm{Ag}^{+}$
(c) $\mathrm{Sn}^{2+}$
6.37 What are the likely ground-state electron configurations of the following anions?
(a) $\mathrm{Se}^{2-}$
(b) $\mathrm{N}^{3-}$
6.38 There are two elements in the transition metal series Sc through Zn that have four unpaired electrons in their $2+$ ions. Identify them.
6.39 Identify the element whose $2+$ ion has the ground-state electron configuration $[\mathrm{Ar}] 3 d^{10}$.
6.40 Do ionization energies have a positive sign or a negative sign? Explain.
6.41 Do electron affinities have a positive sign or a negative sign? Explain.
6.42 Which group of elements in the periodic table has the largest $E_{i 1}$, and which group has the smallest? Explain.
6.43 Which element in the periodic table has the smallest ionization energy? Which has the largest?
6.44 (a) Which has the smaller second ionization energy, K or Ca ?
(b) Which has the larger third ionization energy, Ga or Ca ?
6.45 (a) Which has the smaller fourth ionization energy, Sn or Sb ?
(b) Which has the larger sixth ionization energy, Se or Br ?
6.46 Three atoms have the following electron configurations:
(a) $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{3}$
(b) $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6}$
(c) $1 s^{2} 2 s^{2} 2 p^{6} 3 s^{2} 3 p^{6} 4 s^{2}$

Which of the three has the largest $E_{\mathrm{i} 2}$ ? Which has the smallest $E_{\mathrm{i} 7}$ ?
6.47 Write the electron configuration of the atom in the third row of the periodic table that has the smallest $E_{i 4}$.
6.48 Which element in each of the following sets has the smallest first ionization energy, and which has the largest?
(a) $\mathrm{Li}, \mathrm{Ba}, \mathrm{K}$
(b) $\mathrm{B}, \mathrm{Be}, \mathrm{Cl}$
(c) $\mathrm{Ca}, \mathrm{C}, \mathrm{Cl}$
6.49 What elements meet the following descriptions?
(a) Has largest $E_{\mathrm{i} 3}$
(b) Has largest $E_{i 7}$
6.50 What is the relationship between the electron affinity of a monocation such as $\mathrm{Na}^{+}$and the ionization energy of the neutral atom?
6.51 What is the relationship between the ionization energy of a monoanion such as $\mathrm{Cl}^{-}$and the electron affinity of the neutral atom?
6.52 Which has the more negative electron affinity, $\mathrm{Na}^{+}$or Na ? $\mathrm{Na}^{+}$or Cl ?
6.53 Which has the more negative electron affinity, Br or $\mathrm{Br}^{-}$?
6.54 Why is energy usually released when an electron is added to a neutral atom but absorbed when an electron is removed from a neutral atom?
6.55 Why does ionization energy increase regularly across the periodic table from group 1A to group 8A, whereas electron affinity increases irregularly from group 1A to group 7A and then falls dramatically for group 8A?
6.56 Which element in each of the following pairs has the larger (more negative) electron affinity?
(a) F or Fe
(b) Ne or Na
(c) Ba or Br
6.57 According to the data in Figure 6.6, zinc, cadmium, and mercury all have near-zero electron affinities. Explain.

## Lattice Energy and Ionic Bonds

6.58 Order the following compounds according to their expected lattice energies: $\mathrm{LiCl}, \mathrm{KCl}, \mathrm{KBr}, \mathrm{MgCl}_{2}$.
6.59 Order the following compounds according to their expected lattice energies: $\mathrm{AlBr}_{3}, \mathrm{MgBr}_{2}, \mathrm{LiBr}, \mathrm{CaO}$.
6.60 Calculate the energy change (in kilojoules per mole) when lithium atoms lose an electron to bromine atoms to form isolated $\mathrm{Li}^{+}$and $\mathrm{Br}^{-}$ions. (The $E_{\mathrm{i}}$ for Li is 520 $\mathrm{kJ} / \mathrm{mol}$; the $E_{\text {ea }}$ for Br is $-325 \mathrm{~kJ} / \mathrm{mol}$.)
6.61 Cesium has the smallest ionization energy of all elements ( $376 \mathrm{~kJ} / \mathrm{mol}$ ), and chlorine has the most negative electron affinity ( $-349 \mathrm{~kJ} / \mathrm{mol}$ ). Will a cesium atom donate an electron to a chlorine atom to form isolated $\mathrm{Cs}^{+}$and $\mathrm{Cl}^{-}$ions?
6.62 Find the lattice energy of LiBr in Table 6.3, and calculate the energy change (in kilojoules per mole) for the formation of solid LiBr from the elements. (The sublimation energy for Li is $+159.4 \mathrm{~kJ} / \mathrm{mol}$, the bond dissociation energy of $\mathrm{Br}_{2}$ is $+224 \mathrm{~kJ} / \mathrm{mol}$, and the energy necessary to convert $\mathrm{Br}_{2}(l)$ to $\mathrm{Br}_{2}(g)$ is $30.9 \mathrm{~kJ} / \mathrm{mol}$.)
6.63 Look up the lattice energies in Table 6.3, and calculate the energy change (in kilojoules per mole) for the formation of the following substances from their elements:
(a) LiF (The sublimation energy for Li is $+159.4 \mathrm{~kJ} / \mathrm{mol}$, the $E_{\mathrm{i}}$ for Li is $520 \mathrm{~kJ} / \mathrm{mol}$, the $E_{\text {ea }}$ for F is $-328 \mathrm{~kJ} / \mathrm{mol}$, and the bond dissociation energy of $\mathrm{F}_{2}$ is $+158 \mathrm{~kJ} / \mathrm{mol}$.)
(b) $\mathrm{CaF}_{2}$ (The sublimation energy for Ca is $+178.2 \mathrm{~kJ} / \mathrm{mol}, E_{\mathrm{i} 1}=+589.8 \mathrm{~kJ} / \mathrm{mol}$, and $E_{\mathrm{i} 2}=$ $+1145 \mathrm{~kJ} / \mathrm{mol}$.)
6.64 Born-Haber cycles, such as that shown in Figure 6.8, are called cycles because they form closed loops. If any five of the six energy changes in the cycle are known, the value of the sixth can be calculated. Use the following five values to calculate a lattice energy (in kilojoules per mole) for sodium hydride, NaH :
$E_{\text {ea }}$ for $\mathrm{H}=-72.8 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 1}$ for $\mathrm{Na}=+495.8 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Na}=+107.3 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{H}_{2}=+435.9 \mathrm{~kJ} / \mathrm{mol}$
Net energy change for the formation of NaH from its elements $=-60 \mathrm{~kJ} / \mathrm{mol}$
6.65 Calculate a lattice energy for $\mathrm{CaH}_{2}$ (in kilojoules per mole) using the following information:
$E_{\text {ea }}$ for $\mathrm{H}=-72.8 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 1}$ for $\mathrm{Ca}=+589.8 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 2}$ for $\mathrm{Ca}=+1145 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Ca}=+178.2 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{H}_{2}=+435.9 \mathrm{~kJ} / \mathrm{mol}$
Net energy change for the formation of $\mathrm{CaH}_{2}$ from its elements $=-186.2 \mathrm{~kJ} / \mathrm{mol}$
6.66 Calculate the overall energy change (in kilojoules per mole) for the formation of CsF from its elements using the following data:
$E_{\text {ea }}$ for $\mathrm{F}=-328 \mathrm{~kJ} / \mathrm{mol}$
$E_{i 1}$ for $\mathrm{Cs}=+375.7 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 2}$ for $\mathrm{Cs}=+2422 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Cs}=+76.1 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{F}_{2}=+158 \mathrm{~kJ} / \mathrm{mol}$
Lattice energy for $\mathrm{CsF}=+740 \mathrm{~kJ} / \mathrm{mol}$
6.67 The estimated lattice energy for $\mathrm{CsF}_{2}$ is $+2347 \mathrm{~kJ} / \mathrm{mol}$. Use the data given in Problem 6.66 to calculate an overall energy change (in kilojoules per mole) for the formation of $\mathrm{CsF}_{2}$ from its elements. Does the overall reaction absorb energy or release it? In light of your answers to Problem 6.66, which compound is more likely to form in the reaction of cesium with fluorine, CsF or $\mathrm{CsF}_{2}$ ?
6.68 Calculate overall energy changes (in kilojoules per mole) for the formation of CaCl from the elements. The following data are needed:
$E_{\text {ea }}$ for $\mathrm{Cl}=-348.6 \mathrm{~kJ} / \mathrm{mol}$
$E_{i 1}$ for $\mathrm{Ca}=+589.8 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 2}$ for $\mathrm{Ca}=+1145 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Ca}=+178.2 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{Cl}_{2}=+243 \mathrm{~kJ} / \mathrm{mol}$
Lattice energy for $\mathrm{CaCl}_{2}=+2258 \mathrm{~kJ} / \mathrm{mol}$
Lattice energy for $\mathrm{CaCl}=+717 \mathrm{~kJ} / \mathrm{mol}$ (estimated)
6.69 Use the data in Problem 6.68 to calculate an overall energy change for the formation of $\mathrm{CaCl}_{2}$ from the elements. Which is more likely to form, CaCl or $\mathrm{CaCl}_{2}$ ?
6.70 Use the data and the result in Problem 6.64 to draw a Born-Haber cycle for the formation of NaH from its elements.
6.71 Use the data and the result in Problem 6.63a to draw a Born-Haber cycle for the formation of LiF from its elements.

## Main-Group Chemistry

6.72 Which of the elements in groups 7A (F, Cl, Br, I) and 8A ( $\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}, \mathrm{Kr}, \mathrm{Xe}$ ) are gases, which are liquids, and which are solids at room temperature?
6.73 Give at least one important use for each of the following elements:
(a) Lithium
(b) Potassium
(c) Strontium
(d) Helium
6.74 Little is known about the chemistry of astatine (At) from direct observation, but reasonable predictions can be made.
(a) Is astatine likely to be a gas, a liquid, or a solid?
(b) What color is astatine likely to have?
(c) Is astatine likely to react with sodium? If so, what is the formula of the product?
6.75 Look at the properties of the alkali metals summarized in Table 6.4, and predict reasonable values for the melting point, boiling point, density, and atomic radius of francium.
6.76 Tell how each of the following elements is produced commercially:
(a) Sodium
(b) Aluminum
(c) Argon
(d) Bromine
6.77 Why does chemical reactivity increase from top to bottom in group 1A but decrease from top to bottom in group 7A?
6.78 Briefly state the octet rule, and explain why it works.
6.79 Which main-group elements occasionally break the octet rule?
6.80 Write balanced equations for the reaction of potassium with the following substances. If no reaction occurs, write N.R.
(a) $\mathrm{H}_{2}$
(b) $\mathrm{H}_{2} \mathrm{O}$
(c) $\mathrm{NH}_{3}$
(d) $\mathrm{Br}_{2}$
(e) $\mathrm{N}_{2}$
(f) $\mathrm{O}_{2}$
6.81 Write balanced equations for the reaction of calcium with the following substances. If no reaction occurs, write N.R.
(a) $\mathrm{H}_{2}$
(b) $\mathrm{H}_{2} \mathrm{O}$
(c) He
(d) $\mathrm{Br}_{2}$
(e) $\mathrm{O}_{2}$
6.82 Write balanced equations for the reaction of chlorine with the following substances. If no reaction occurs, write N.R.
(a) $\mathrm{H}_{2}$
(b) Ar
(c) $\mathrm{Br}_{2}$
(d) $\mathrm{N}_{2}$
6.83 As a general rule, more reactive halogens can oxidize the anions of less reactive halogens. Predict the products of the following reactions, and identify the oxidizing and reducing agents in each. If no reaction occurs, write N.R.
(a) $2 \mathrm{Cl}^{-}(a q)+\mathrm{F}_{2}(g) \rightarrow$ ?
(b) $2 \mathrm{Br}^{-}(a q)+\mathrm{I}_{2}(s) \rightarrow$ ?
(c) $2 \mathrm{I}^{-}(a q)+\mathrm{Br}_{2}(a q) \rightarrow$ ?
6.84 Aluminum metal can be prepared by reaction of $\mathrm{AlCl}_{3}$ with Na. Write a balanced equation for the reaction, and tell which atoms have been oxidized and which have been reduced.
6.85 The widely used antacid called milk of magnesia is an aqueous suspension of $\mathrm{Mg}(\mathrm{OH})_{2}$. How would you prepare $\mathrm{Mg}(\mathrm{OH})_{2}$ from magnesium metal?
6.86 What is the maximum amount (in grams) of pure iodine that you could obtain from 1.00 kg of the mineral lautarite $\left(\mathrm{CaIO}_{3}\right)$ ?
6.87 Assume that you wanted to prepare a small volume of pure hydrogen by reaction of lithium metal with water. How many grams of lithium would you need to prepare 455 mL of $\mathrm{H}_{2}$ if the density of hydrogen is $0.0893 \mathrm{~g} / \mathrm{L}$ ?
6.88 How many grams of calcium hydride are formed by reaction of 5.65 g of calcium with 3.15 L of $\mathrm{H}_{2}$ if the density of hydrogen is $0.0893 \mathrm{~g} / \mathrm{L}$ and the reaction occurs in $94.3 \%$ yield? Which reactant is limiting?
6.89 How many liters of $\mathrm{N}_{2}$ gas are needed for reaction of 2.87 g of lithium to give lithium nitride if the density of nitrogen is $1.25 \mathrm{~g} / \mathrm{L}$ ?
6.90 Identify the oxidizing agent and the reducing agent in each of the following reactions:
(a) $\mathrm{Mg}(s)+2 \mathrm{H}^{+}(a q) \rightarrow \mathrm{Mg}^{2+}(a q)+\mathrm{H}_{2}(g)$
(b) $\mathrm{Kr}(g)+\mathrm{F}_{2}(g) \rightarrow \mathrm{KrF}_{2}(s)$
(c) $\mathrm{I}_{2}(s)+3 \mathrm{Cl}_{2}(g) \rightarrow 2 \mathrm{ICl}_{3}(l)$
6.91 Identify the oxidizing agent and the reducing agent in each of the following reactions:
(a) $2 \mathrm{XeF}_{2}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \rightarrow$

$$
2 \mathrm{Xe}(g)+4 \mathrm{HF}(a q)+\mathrm{O}_{2}(g)
$$

(b) $\mathrm{NaH}(s)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow$

$$
\mathrm{Na}^{+}(a q)+\mathrm{OH}^{-}(a q)+\mathrm{H}_{2}(g)
$$

(c) $2 \mathrm{TiCl}_{4}(l)+\mathrm{H}_{2}(g) \rightarrow 2 \mathrm{TiCl}_{3}(s)+2 \mathrm{HCl}(g)$

## General Problems

$6.92 \mathrm{Cu}^{+}$has an ionic radius of 77 pm , but $\mathrm{Cu}^{2+}$ has an ionic radius of 73 pm. Explain.
6.93 The following ions all have the same number of electrons: $\mathrm{Ti}^{4+}, \mathrm{Sc}^{3+}, \mathrm{Ca}^{2+}, \mathrm{S}^{2-}$. Order them according to their expected size, and explain your answer.
6.94 Calculate overall energy changes (in kilojoules per mole) for the formation of MgF and $\mathrm{MgF}_{2}$ from their elements. The following data are needed:
$E_{\text {ea }}$ for $F=-328 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 1}$ for $\mathrm{Mg}=+737.7 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 2}$ for $\mathrm{Mg}=+1450.7 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Mg}=+147.7 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{F}_{2}=+158 \mathrm{~kJ} / \mathrm{mol}$
Lattice energy for $\mathrm{MgF}_{2}=+2952 \mathrm{~kJ} / \mathrm{mol}$
Lattice energy for $\mathrm{MgF}=930 \mathrm{~kJ} / \mathrm{mol}$ (estimated)
6.95 In light of your answers to Problem 6.94, which compound is more likely to form in the reaction of magnesium with fluorine, $\mathrm{MgF}_{2}$ or MgF ?
6.96 Give at least one important use of each of the following elements:
(a) Sodium
(b) Magnesium
(c) Fluorine
6.97 Tell how each of the following elements is produced commercially:
(a) Fluorine
(b) Calcium
(c) Chlorine
6.98 Write balanced equations for the reaction of lithium with the following substances. If no reaction occurs, write N.R.
(a) $\mathrm{H}_{2}$
(b) $\mathrm{H}_{2} \mathrm{O}$
(c) $\mathrm{NH}_{3}$
(d) $\mathrm{Br}_{2}$
(e) $\mathrm{N}_{2}$
(f) $\mathrm{O}_{2}$
6.99 Write balanced equations for the reaction of fluorine with the following substances. If no reaction occurs, write N.R.
(a) $\mathrm{H}_{2}$
(b) Na
(c) $\mathrm{Br}_{2}$
(d) NaBr
6.100 Many early chemists noted a diagonal relationship among elements in the periodic table, whereby a given element is sometimes more similar to the element below and to the right than it is to the element directly below. Lithium is more similar to magnesium than to sodium, for example, and boron is more similar to silicon than to aluminum. Use your knowledge about the periodic trends of such properties as atomic radii and $Z_{\text {eff }}$ to explain the existence of diagonal relationships.
6.101 We saw in Section 6.6 that the reaction of solid sodium with gaseous chlorine to yield solid sodium chloride $\left(\mathrm{Na}^{+} \mathrm{Cl}^{-}\right)$is favorable by $411 \mathrm{~kJ} / \mathrm{mol}$. Calculate the energy change for the alternative reaction that yields chlorine sodide $\left(\mathrm{Cl}^{+} \mathrm{Na}^{-}\right)$, and then explain why sodium chloride formation is preferred.

$$
2 \mathrm{Na}(s)+\mathrm{Cl}_{2}(g) \longrightarrow 2 \mathrm{Cl}^{+} \mathrm{Na}^{-}(s)
$$

Assume that the lattice energy for $\mathrm{Cl}^{+} \mathrm{Na}^{-}$is the same as that for $\mathrm{Na}^{+} \mathrm{Cl}^{-}$. The following data are needed in addition to that found in Section 6.6:

$$
E_{\text {ea }} \text { for } \mathrm{Na}=-52.9 \mathrm{~kJ} / \mathrm{mol} \quad E_{\mathrm{i} 1} \text { for } \mathrm{Cl}=+1251 \mathrm{~kJ} / \mathrm{mol}
$$

6.102 Draw a Born-Haber cycle for the reaction of sodium with chlorine to yield chlorine sodide (Problem 6.101).
6.103 One mole of any gas has a volume of 22.4 L at $0^{\circ} \mathrm{C}$ and 1.00 atmosphere pressure. Assume that 0.719 g of an unknown metal M reacted completely with 94.2 mL of $\mathrm{Cl}_{2}$ gas at $0^{\circ} \mathrm{C}$ and 1.00 atmosphere pressure to give a metal halide product. From the data given, several atomic masses for the metal are possible. List several possibilities, and choose the most likely candidate for M .
6.104 Use the following data and data given in Tables 6.2 and 6.3 to calculate the second electron affinity, $E_{\text {ea } 2}$, of oxygen. Is the $\mathrm{O}^{2-}$ ion stable in the gas phase? Why is it stable in solid MgO ?

Heat of sublimation for $\mathrm{Mg}=+147.7 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{O}_{2}=+498.4 \mathrm{~kJ} / \mathrm{mol}$
$E_{\text {ea } 1}$ for $\mathrm{O}=-141.0 \mathrm{~kJ} / \mathrm{mol}$
Net energy change for formation of MgO from its elements $=-601.7 \mathrm{~kJ} / \mathrm{mol}$
6.105 (a) Which element from each set has the largest atomic radius? Explain.
(i) $\mathrm{Ba}, \mathrm{Ti}, \mathrm{Ra}, \mathrm{Li}$
(ii) $\mathrm{F}, \mathrm{Al}, \mathrm{In}, \mathrm{As}$
(b) Which element from each set has the smallest ionization energy? Explain.
(i) $\mathrm{Tl}, \mathrm{Po}, \mathrm{Se}, \mathrm{Ga}$
(ii) $\mathrm{Cs}, \mathrm{Ga}, \mathrm{Bi}, \mathrm{Se}$
6.106 (a) Of the elements $\mathrm{Be}, \mathrm{N}, \mathrm{O}$, and F , which has the most negative electron affinity? Explain.
(b) Of the ions $\mathrm{Se}^{2-}, \mathrm{F}^{-}, \mathrm{O}^{2-}$, and $\mathrm{Rb}^{+}$, which has the largest radius? Explain.
6.107 Given the following information, construct a BornHaber cycle to calculate the lattice energy of $\mathrm{CaC}_{2}(s)$ :

Net energy change for the formation of
$\mathrm{CaC}_{2}(\mathrm{~s})=-60 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Ca}(\mathrm{s})=+178 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 1}$ for $\mathrm{Ca}(g)=+590 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 2}$ for $\mathrm{Ca}(g)=+1145 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{C}(s)=+717 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{C}_{2}(g)=+614 \mathrm{~kJ} / \mathrm{mol}$
$E_{\text {ea1 }}$ for $\mathrm{C}_{2}(\mathrm{~g})=-315 \mathrm{~kJ} / \mathrm{mol}$
$E_{\text {ea2 }}$ for $\mathrm{C}_{2}(\mathrm{~g})=+410 \mathrm{~kJ} / \mathrm{mol}$
6.108 Given the following information, construct a BornHaber cycle to calculate the lattice energy of $\mathrm{CrCl}_{2} \mathrm{I}$ :

Net energy change for the formation of $\mathrm{CrCl}_{2} \mathrm{I}=$ $-420 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $\mathrm{Cl}_{2}=+243 \mathrm{~kJ} / \mathrm{mol}$
Bond dissociation energy for $I_{2}=+151 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{I}_{2}=+62 \mathrm{~kJ} / \mathrm{mol}$
Heat of sublimation for $\mathrm{Cr}=+397 \mathrm{~kJ} / \mathrm{mol}$
$E_{i 1}$ for $\mathrm{Cr}=652 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 2}$ for $\mathrm{Cr}=1588 \mathrm{~kJ} / \mathrm{mol}$
$E_{\mathrm{i} 3}$ for $\mathrm{Cr}=2882 \mathrm{~kJ} / \mathrm{mol}$
$E_{\text {ea }}$ for $\mathrm{Cl}=-349 \mathrm{~kJ} / \mathrm{mol}$
$E_{\text {ea }}$ for $I=-295 \mathrm{~kJ} / \mathrm{mol}$

## Multi-Concept Problems

6.109 Consider the electronic structure of the element bismuth.
(a) The first ionization energy of bismuth is $E_{\mathrm{i} 1}=+703 \mathrm{~kJ} / \mathrm{mol}$. What is the longest possible wavelength of light that could ionize an atom of bismuth?
(b) Write the electron configurations of neutral Bi and the $\mathrm{Bi}^{+}$cation.
(c) What are the $n$ and $l$ quantum numbers of the electron removed when Bi is ionized to $\mathrm{Bi}^{+}$?
(d) Would you expect element 115 to have an ionization energy greater than, equal to, or less than that of bismuth? Explain.
6.110 Iron has three common oxidation states: $\mathrm{Fe}, \mathrm{Fe}^{2+}$, and $\mathrm{Fe}^{3+}$.
(a) Write electron configurations for each of the three.
(b) What are the $n$ and $l$ quantum numbers of the electron removed on going from $\mathrm{Fe}^{2+}$ to $\mathrm{Fe}^{3+}$ ?
(c) The third ionization energy of Fe is $E_{\mathrm{i} 3}=$ $+2952 \mathrm{~kJ} / \mathrm{mol}$. What is the longest wavelength of light that could ionize $\mathrm{Fe}^{2+}(g)$ to $\mathrm{Fe}^{3+}(g)$ ?
(d) The third ionization energy of Ru is less than the third ionization energy of Fe . Explain.
6.111 The ionization energy of an atom can be measured by photoelectron spectroscopy, in which light of wavelength $\lambda$ is directed at an atom, causing an electron to be ejected. The kinetic energy of the ejected electron $\left(E_{\mathrm{K}}\right)$ is measured by determining its velocity, $v$, since $E_{\mathrm{K}}=1 / 2 m v^{2}$. The $E_{\mathrm{i}}$ is then calculated using the relationship that the energy of the incident light equals the sum of $E_{\mathrm{i}}$ plus $E_{\mathrm{K}}$.
(a) What is the ionization energy of rubidium atoms (in kilojoules per mole) if light with $\lambda=58.4 \mathrm{~nm}$ produces electrons with a velocity of $2.450 \times 10^{6} \mathrm{~m} / \mathrm{s}$ ? (The mass of an electron is $9.109 \times 10^{-31} \mathrm{~kg}$.)
(b) What is the ionization energy of potassium (in kilojoules per mole) if light with $\lambda=142 \mathrm{~nm}$ produces electrons with a velocity of $1.240 \times 10^{6} \mathrm{~m} / \mathrm{s}$ ?
6.112 A 1.005 g sample of an unknown alkaline earth metal was allowed to react with a volume of chlorine gas that contains $1.91 \times 10^{22} \mathrm{Cl}_{2}$ molecules. The resulting metal chloride was analyzed for chlorine by dissolving a 0.436 g sample in water and adding an excess of $\mathrm{AgNO}_{3}(a q)$. The analysis yielded 1.126 g of AgCl .
(a) What is the percent Cl in the alkaline earth chloride?
(b) What is the identity of the alkaline earth metal?
(c) Write balanced equations for all chemical reactions.
(d) In the reaction of the alkaline earth metal with chlorine, which reactant is in excess, and how many grams of that reactant remain unreacted?
6.113 Element M is prepared industrially from its oxide by a two-step procedure according to the following (unbalanced) equations:

$$
\begin{align*}
& (1) \mathrm{M}_{2} \mathrm{O}_{3}(s)+\mathrm{C}(s)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{MCl}_{3}(l)+\mathrm{CO}(g)  \tag{1}\\
& (2) \mathrm{MCl}_{3}(l)+\mathrm{H}_{2}(g) \longrightarrow \mathrm{M}(s)+\mathrm{HCl}(g)
\end{align*}
$$

Assume that 0.855 g of $\mathrm{M}_{2} \mathrm{O}_{3}$ is submitted to the reaction sequence. When the HCl produced in step (2) is dissolved in water and titrated with $0.511 \mathrm{M} \mathrm{NaOH}, 144.2 \mathrm{~mL}$ of the NaOH solution is required to neutralize the HCl .
(a) Balance both equations.
(b) What is the atomic mass of element M , and what is its identity?
(c) What mass of M (in grams) is produced in the reaction?
6.114 Assume that 20.0 g of Sr is allowed to react with 25.0 g of $\mathrm{Cl}_{2}$ to give $\mathrm{SrCl}_{2}$.
(a) What is the net energy change in $\mathrm{kJ} / \mathrm{mol}$ for the formation of $\mathrm{SrCl}_{2}$ from its elements? Heat of sublimation for $\mathrm{Sr}=+164.44 \mathrm{~kJ} / \mathrm{mol} ; E_{i 1}$ for $\mathrm{Sr}=$ $+549.5 \mathrm{~kJ} / \mathrm{mol} ; E_{\mathrm{i} 2}$ for $\mathrm{Sr}=+1064.2 \mathrm{~kJ} / \mathrm{mol}$; bond dissociation energy for $\mathrm{Cl}_{2}=+243 \mathrm{~kJ} / \mathrm{mol} ; \mathrm{E}_{\mathrm{ea}}$ for $\mathrm{Cl}=-348.6 \mathrm{~kJ} / \mathrm{mol}$; lattice energy for $\mathrm{SrCl}_{2}=$ $+2,156 \mathrm{~kJ} / \mathrm{mol}$.
(b) Which reactant is limiting, and how many grams of $\mathrm{SrCl}_{2}$ product are formed?
(c) How much energy in kJ is released during the reaction?
6.115 A 0.265 g sample of alkali metal M was burned in air to give a mixture of oxide $\left(\mathrm{M}_{2} \mathrm{O}\right)$ and nitride $\left(\mathrm{M}_{3} \mathrm{~N}\right)$. The reaction product was then dissolved in water to a volume of 250.0 mL , and 50.0 mL of the resultant solution was titrated with 0.100 HCl , requiring 96.8 mL for complete reaction.
(a) What is the identity of the alkali metal?
(b) Write equations for all reactions, including reactions of the oxide and nitride with water.
(c) What mole fraction of the product was the oxide, and what fraction was the nitride?

## eMedia Problems

6.116 After completing the Ion Electron Configuration activity (eChapter 6.1) answer the following questions:
(a) To what type of element (metal or nonmetal) do you add electrons to form ions?
(b) From what type of element do you subtract electrons to form ions?
(c) Which energy level is always involved in ion formation, whether adding or subtracting electrons?
6.117 Use the Interactive Periodic Table (eChapter 5.1) to compare the atomic radius and the ionic radius of the elements in group 2A. How does the ionic radius compare to the atomic radius? Explain this trend.
6.118 Use the Interactive Periodic Table (eChapter 5.1) to compare the atomic radius and the ionic radius of the elements in group 7A. How does the ionic radius compare to the atomic radius? Explain this trend.
6.119 The magnitude of the lattice energy of an ionic compound depends on the charges and sizes of the ions that make up the compound. Use the Coulomb's Law activity (eChapter 6.6) to determine which ionic compound has the larger lattice energy, LiF or SrTe . (Ionic radii in $\AA$ for $\mathrm{Li}^{+}, \mathrm{F}^{-}, \mathrm{Sr}^{2+}$, and $\mathrm{Te}^{2-}$ are $0.68,1.33,1.13$, and 2.21 , respectively. Note that $1 \AA=100 \mathrm{pm}$.)
6.120 Use the Octet Rule activity (eChapter 6.12) to predict the most common ion for each of the elements included in the activity. Explain what is meant by "poorly shielded" and "strongly shielded" in this activity.

## Chapter

## Covalent Bonds and Molecular Structure

## We saw in the last chapter that the bond formed between a metal and a reactive nonmetal typically involves the transfer of elec-

trons. The metal atom loses one or more electrons and becomes a cation, while the reactive nonmetal atom gains one or more electrons and becomes an anion. The oppositely charged ions are held together by the electrostatic attractions that we call ionic bonds.

How, though, do bonds form between atoms of the same or similar elements? How can we describe the

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Shape is crucial, both in chemistry and in architecture.

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| 7.2 | Strengths of Covalent Bonds | 7.11 | Hybridization and $s p^{3}$ Hybrid |
| 7.3 | A Comparison of Ionic and |  | Orbitals |
|  | Covalent Compounds | 7.12 | Other Kinds of Hybrid Orbitals |
| 7.4 | Polar Covalent Bonds: Electronegativity | 7.13 | Molecular Orbital Theory: The Hydrogen Molecule |
| 7.5 | Electron-Dot Structures | 7.14 | Molecular Orbital Theory: Other |
| 7.6 | Electron-Dot Structures of Polyatomic Molecules | 7.15 | Diatomic Molecules Combining Valence Bond Theory |
| 7.7 | Electron-Dot Structures and Resonance | - Int | and Molecular Orbital Theory rlude-Molecular Shape, |
| 7.8 | Formal Charges |  | Handedness, and Drugs |
| 7.9 | Molecular Shapes: The VSEPR Model |  |  |



FIGURE 7.1 A covalent $\mathrm{H}-\mathrm{H}$ bond is the net result of attractive and repulsive electrostatic forces. The nucleuselectron attractions (blue arrows) are greater than the nucleus-nucleus and electronelectron repulsions (red arrows), resulting in a net attractive force that holds the atoms together to form an $\mathrm{H}_{2}$ molecule.

Georgios R. Tsaparlis, "The Chemical Bond as an Atomic Tug-of-War," J. Chem. Educ., Vol. 61, 1984, 677.

FIGURE 7.2 A graph of $>$ potential energy versus internuclear distance for the $\mathrm{H}_{2}$ molecule. If the hydrogen atoms are too far apart, attractions are weak and no bonding occurs. If the atoms are too close, strong repulsions occur. When the atoms are optimally separated, the energy is at a minimum.
bonds in such substances as $\mathrm{H}_{2}, \mathrm{Cl}_{2}, \mathrm{CO}_{2}$, and the literally millions of other nonionic compounds? Simply put, the answer is that the bonds in such compounds are formed by the sharing of electrons between atoms rather than by the transfer of electrons from one atom to another. A bond formed by the sharing of electrons is called a covalent bond and is the most important kind of bond in all of chemistry. We'll explore the nature of covalent bonding in this chapter.

- covalent bond A bond that results from the sharing of electrons between atoms.


## $7.1 \mid$ The Covalent Bond

To see how the formation of a covalent, shared-electron bond between atoms can be described, let's look at the $\mathrm{H}-\mathrm{H}$ bond in the $\mathrm{H}_{2}$ molecule as an example. As two hydrogen atoms come closer together, electrostatic interactions begin to develop between them. The two positively charged nuclei repel each other and the two negatively charged electrons repel each other, but each nucleus attracts both electrons (Figure 7.1). If the attractive forces are stronger than the repulsive forces, a covalent bond is formed, with the two atoms joined together and the two shared electrons occupying the region between the nuclei.


In essence, the shared electrons act as a kind of "glue" to bind the two nuclei together into an $\mathrm{H}_{2}$ molecule. Both nuclei are simultaneously attracted to the same electrons and are therefore held together, much as two tug-of-war teams pulling on the same rope are held together.

As shown in Figure 7.2, the magnitudes of the various attractive and repulsive forces between nuclei and electrons in a covalent bond depend on how close the atoms are. If the hydrogen atoms are too far apart, the attractive forces are small and no bond exists. If the hydrogen atoms are too close together, the repulsive interaction between the nuclei becomes so strong that it pushes the atoms

apart. Thus, there is an optimum distance between nuclei called the bond length where net attractive forces are maximized and the $\mathrm{H}-\mathrm{H}$ molecule is most stable. In the $\mathrm{H}_{2}$ molecule, the bond length is 74 pm . On a graph of energy versus internuclear distance, the bond length corresponds to the minimum-energy, most stable arrangement.

Every covalent bond has its own characteristic length that leads to maximum stability and that is roughly predictable from a knowledge of atomic radii (Section 5.15). For example, because the atomic radius of hydrogen is 37 pm and the atomic radius of chlorine is 99 pm , the $\mathrm{H}-\mathrm{Cl}$ bond length in a hydrogen chloride molecule is approximately $37 \mathrm{pm}+99 \mathrm{pm}=136 \mathrm{pm}$. (The actual value is 127 pm .)

## 7.2 | Strengths of Covalent Bonds

Look again at Figure 7.2, the graph of energy versus internuclear distance for the $\mathrm{H}_{2}$ molecule, and note how the $\mathrm{H}_{2}$ molecule is lower in energy than two separate hydrogen atoms. When pairs of hydrogen atoms bond together, they form lowerenergy $\mathrm{H}_{2}$ molecules and release $436 \mathrm{~kJ} / \mathrm{mol}$. Looked at from the other direction, 436 kJ must be added per mole of $\mathrm{H}_{2}$ molecules to split the molecules apart into hydrogen atoms.


The amount of energy that must be supplied to break a chemical bond in an isolated molecule in the gaseous state-and thus the amount of energy released when the bond forms-is called the bond dissociation energy ( $D$ ). Bond dissociation energies are always positive values because energy must always be supplied to break a bond. Conversely, the amount of energy released on forming a bond is always a negative value.

Every bond in every molecule has its own specific bond dissociation energy. Not surprisingly, though, bonds between the same pairs of atoms usually have similar dissociation energies. For example, carbon-carbon bonds usually have $D$ values of approximately $350-380 \mathrm{~kJ} / \mathrm{mol}$ regardless of the exact structure of the molecule. (Note in the following examples that all the covalent bonds between atoms are indicated by lines, as described in Section 2.8.)




Because similar bonds have similar bond dissociation energies, it's possible to construct a table of average values (Table 7.1) to compare different kinds of bonds. Keep in mind, though, that the actual value in a specific molecule might vary by $\pm 10 \%$ from the average.

The bond dissociation energies listed in Table 7.1 cover a wide range, from a low of $151 \mathrm{~kJ} / \mathrm{mol}$ for the I-I bond to a high of $570 \mathrm{~kJ} / \mathrm{mol}$ for the $\mathrm{H}-\mathrm{F}$ bond. As a rule of thumb, though, most of the bonds commonly encountered in naturally occurring molecules ( $\mathrm{C}-\mathrm{H}, \mathrm{C}-\mathrm{C}, \mathrm{C}-\mathrm{O}$ ) have values in the range $350-400 \mathrm{~kJ} / \mathrm{mol}$.

al
Roger L. DeKock, "The Chemical Bond," J. Chem. Educ., Vol. 64, 1987, 934-941.

Raymond F. Peterson and David F. Treagust, "Grade-12 Students' Misconceptions of Covalent Bonding and Structure," J. Chem. Educ., Vol. 66, 1989, 459-460.


$\square$The units of bond dissociation energy (bond energy) are $\mathrm{kJ} / \mathrm{mol}$. As with ionization energy and electron affinity, bond energies are given for isolated, gaseous-state molecules.


A Sodium chloride, an ionic compound, is a white, crystalline solid. Hydrogen chloride, a molecular compound, is a gas at room temperature.

NaCl 3D model; HCl 3D model

| TABLE 7.1 | Average Bond Dissociation Energies, $D(\mathrm{~kJ} / \mathrm{mol})^{\mathrm{a}}$ |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{H}-\mathrm{H}$ | $436^{\mathrm{a}}$ | $\mathrm{C}-\mathrm{H}$ | 410 | $\mathrm{~N}-\mathrm{H}$ | 390 | $\mathrm{O}-\mathrm{H}$ | 460 | $\mathrm{~F}-\mathrm{F}$ | $159^{\mathrm{a}}$ |
| $\mathrm{H}-\mathrm{C}$ | 410 | $\mathrm{C}-\mathrm{C}$ | 350 | $\mathrm{~N}-\mathrm{C}$ | 300 | $\mathrm{O}-\mathrm{C}$ | 350 | $\mathrm{Cl}-\mathrm{Cl}$ | $243^{\mathrm{a}}$ |
| $\mathrm{H}-\mathrm{F}$ | $570^{\mathrm{a}}$ | $\mathrm{C}-\mathrm{F}$ | 450 | $\mathrm{~N}-\mathrm{F}$ | 270 | $\mathrm{O}-\mathrm{F}$ | 180 | $\mathrm{Br}-\mathrm{Br}$ | $193^{\mathrm{a}}$ |
| $\mathrm{H}-\mathrm{Cl}$ | $432^{\mathrm{a}}$ | $\mathrm{C}-\mathrm{Cl}$ | 330 | $\mathrm{~N}-\mathrm{Cl}$ | 200 | $\mathrm{O}-\mathrm{Cl}$ | 200 | $\mathrm{I}-\mathrm{I}$ | $151^{\mathrm{a}}$ |
| $\mathrm{H}-\mathrm{Br}$ | $366^{\mathrm{a}}$ | $\mathrm{C}-\mathrm{Br}$ | 270 | $\mathrm{~N}-\mathrm{Br}$ | 240 | $\mathrm{O}-\mathrm{Br}$ | 210 | $\mathrm{~S}-\mathrm{F}$ | 310 |
| $\mathrm{H}-\mathrm{I}$ | $298^{\mathrm{a}}$ | $\mathrm{C}-\mathrm{I}$ | 240 | $\mathrm{~N}-\mathrm{I}$ | - | $\mathrm{O}-\mathrm{I}$ | 220 | $\mathrm{~S}-\mathrm{Cl}$ | 250 |
| $\mathrm{H}-\mathrm{N}$ | 390 | $\mathrm{C}-\mathrm{N}$ | 300 | $\mathrm{~N}-\mathrm{N}$ | 240 | $\mathrm{O}-\mathrm{N}$ | 200 | $\mathrm{~S}-\mathrm{Br}$ | 210 |
| $\mathrm{H}-\mathrm{O}$ | 460 | $\mathrm{C}-\mathrm{O}$ | 350 | $\mathrm{~N}-\mathrm{O}$ | 200 | $\mathrm{O}-\mathrm{O}$ | 180 | $\mathrm{~S}-\mathrm{S}$ | 225 |
| $\mathrm{H}-\mathrm{S}$ | 340 | $\mathrm{C}-\mathrm{S}$ | 260 | $\mathrm{~N}-\mathrm{S}$ | - | $\mathrm{O}-\mathrm{S}$ | - |  |  |
| Multiple covalent bonds |  |  |  |  |  |  |  |  |  |
| $\mathrm{C}=\mathrm{C}$ | 611 | $\mathrm{C} \equiv \mathrm{C}$ | 835 | $\mathrm{C}=\mathrm{O}$ | 732 | $\mathrm{O}=\mathrm{O}$ | $498^{\mathrm{a}}$ | $\mathrm{N} \equiv \mathrm{N}$ | $945^{\mathrm{a}}$ |

${ }^{\text {a }}$ Exact value
${ }^{\mathrm{b}}$ We'll discuss multiple covalent bonds in Section 7.5.

### 7.3 A Comparison of Ionic and Covalent Compounds

Look at the comparison between NaCl and HCl , shown in Table 7.2. Sodium chloride, an ionic compound, is a white solid with a melting point of $801^{\circ} \mathrm{C}$ and a boiling point of $1413^{\circ} \mathrm{C}$. Hydrogen chloride, a covalent compound, is a colorless gas with a melting point of $-115^{\circ} \mathrm{C}$ and a boiling point of $-84.9^{\circ} \mathrm{C}$. What accounts for such large differences between the properties of ionic compounds and covalent compounds?
-

| TABLE 7.2 | Some Physical Properties of NaCl and HCl |  |
| :--- | :--- | :--- |
| Property | $\mathbf{N a C l}$ | $\mathbf{H C l}$ |
| Formula mass | 58.44 amu | 36.46 amu |
| Physical appearance | White solid | Colorless gas |
| Type of bond | Ionic | Covalent |
| Melting point | $801^{\circ} \mathrm{C}$ | $-115^{\circ} \mathrm{C}$ |
| Boiling point | $1413^{\circ} \mathrm{C}$ | $-84.9^{\circ} \mathrm{C}$ |

Ionic compounds are high-melting solids because of their ionic bonds. As discussed previously in Section 6.6, a visible sample of sodium chloride consists, not of NaCl molecules, but of a vast three-dimensional network of ions in which each $\mathrm{Na}^{+}$cation is attracted to many surrounding $\mathrm{Cl}^{-}$anions and each $\mathrm{Cl}^{-}$ion is attracted to many surrounding $\mathrm{Na}^{+}$ions. For sodium chloride to melt or boil so that the ions break free of one another, every ionic attraction in the entire crystal must be overcome, a process that requires a large amount of energy.

Covalent compounds, by contrast, are low-melting solids, liquids, or even gases. A sample of a covalent compound, such as hydrogen chloride, consists of discrete HCl molecules. The covalent bond within an individual molecule may be very strong, but the attractive forces between the different molecules are fairly weak. As a result, relatively little energy is required to overcome these forces and cause a covalent compound to melt or boil. We'll look at the nature of intermolecular forces and the boiling process in Chapter 10.

## 7.4 | Polar Covalent Bonds: Electronegativity

We've left the impression up to this point that a given bond is either purely ionic, with electrons completely transferred, or purely covalent, with electrons shared equally. In fact, though, ionic and covalent bonds represent only the two extremes of a continuous spectrum of possibilities. Between these two extremes are the large majority of bonds, in which the bonding electrons are shared unequally between two atoms but are not completely transferred. Such bonds are said to be polar covalent bonds (Figure 7.3). The lowercase Greek letter delta ( $\delta$ ) is used to symbolize the resultant partial charges on the atoms, either partial positive $(\delta+)$ for the atom that has a smaller share of the bonding electrons or partial negative $(\delta-)$ for the atom that has a larger share.


As examples of different points along the bonding spectrum, let's compare three substances, $\mathrm{NaCl}, \mathrm{HCl}$, and $\mathrm{Cl}_{2}$ :

- NaCl The bond in solid sodium chloride is a largely ionic one between $\mathrm{Na}^{+}$ and $\mathrm{Cl}^{-}$. In spite of what we've said previously, though, experiments show that the NaCl bond is only about $80 \%$ ionic and that the electron transferred from Na to Cl still spends some of its time near sodium. A particularly useful way of visualizing this electron transfer is to represent the compound using what is called an electrostatic potential map, which uses color to portray the calculated electron distribution in the molecule. The electron-poor sodium atom is blue, while the electron-rich chlorine is red.

- HCl The bond in a hydrogen chloride molecule is polar covalent. The chlorine atom attracts the bonding electron pair more strongly than hydrogen does, resulting in an unsymmetrical distribution of electrons. Chlorine thus has a partial negative charge (orange in the electrostatic potential map), and hydrogen has a partial positive charge (blue in the electrostatic potential map). Experimentally, the $\mathrm{H}-\mathrm{Cl}$ bond has been found to be about $83 \%$ covalent and 17\% ionic.


The bonding electrons are attracted more strongly by Cl than by H .
< FIGURE 7.3 The bonding continuum from ionic to nonpolar covalent. Polar covalent bonds lie between the two extremes. They are characterized by an unsymmetrical electron distribution in which the bonding electrons are attracted somewhat more strongly by one atom than the other. The symbol $\delta$ (Greek delta) means partial charge, either partial positive $(\delta+$ ) or partial negative ( $\delta-$ ).

James N. Spencer, Richard S.
Moog, and Ronald J. Gillespie, "Demystifying Introductory Chemistry: Part 3. Ionization Energies, Electronegativity, Polar Bonds and Partial Charges," J. Chem. Educ., Vol. 73, 1996, 627-631.


Periodic Trends: Electronegativity movie


William B. Jensen, "Electronegativity from Avogadro to Pauling, Part I: Origins of the Electronegativity Concept," J. Chem. Educ., Vol. 73, 1996, 11-20.

- $\mathrm{Cl}_{2}$ The bond in a chlorine molecule is nonpolar covalent, with the bonding electrons attracted equally to the two identical chlorine atoms. A similar situation exists for all such diatomic molecules that contain a covalent bond between two identical atoms.

$$
\mathrm{Cl}: \mathrm{Cl} \quad \text { A nonpolar covalent bond }
$$



Bond polarity is due to differences in electronegativity (EN), the ability of an atom in a molecule to attract the shared electrons in a covalent bond. As shown graphically in Figure 7.4, metallic elements on the left of the periodic table attract electrons only weakly, whereas the halogens and other reactive nonmetals in the upper right of the table attract electrons strongly. The alkali metals are the least electronegative elements; fluorine, oxygen, nitrogen, and chlorine are the most electronegative. Figure 7.4 also indicates that electronegativity generally decreases down the periodic table within a group.


A FIGURE 7.4 Electronegativity trends in the periodic table. Electronegativity increases from left to right and generally decreases from top to bottom.

Because electronegativity measures the ability of an atom in a molecule to attract shared electrons, it seems logical that it should be related to electron affinity ( $E_{\text {ea, }}$, Section 6.5) and ionization energy ( $E_{\mathrm{i}}$, Section 6.3). Electron affinity, after all, is a measure of the tendency of an isolated atom to gain an electron, and ionization energy is a measure of the tendency of an isolated atom to lose an electron. In fact, one of the ways in which electronegativities were first calculated was by taking the average of the absolute values of $E_{\text {ea }}$ and $E_{\mathrm{i}}$ and then expressing the results on a unitless scale, with fluorine assigned a value of 4.0.

How can we use electronegativity to predict bond polarity? A general but somewhat arbitrary guideline is that bonds between atoms with the same or similar electronegativities are nonpolar covalent, bonds between atoms whose electronegativities differ by more than about 2 units are substantially ionic, and bonds between atoms whose electronegativities differ by less than 2 units are polar covalent. Thus, we can be reasonably sure that a $\mathrm{C}-\mathrm{Cl}$ bond in chloroform, $\mathrm{CHCl}_{3}$, is polar covalent, while an $\mathrm{Na}^{+} \mathrm{Cl}^{-}$bond in sodium chloride is largely ionic.



| Chlorine: | EN $=3.0$ |
| :--- | ---: | :--- | :--- | ---: | :--- |
| Carbon: | EN $=2.5$ |

PROBLEM 7.1 Use the electronegativity values in Figure 7.4 to predict whether the bonds in the following compounds are polar covalent or ionic:
(a) $\mathrm{SiCl}_{4}$
(b) CsBr
(c) $\mathrm{FeBr}_{3}$
(d) $\mathrm{CH}_{4}$

- PROBLEM 7.2 Order the following compounds according to the increasing ionic character of their bonds: $\mathrm{CCl}_{4}, \mathrm{BaCl}_{2}, \mathrm{TiCl}_{3}, \mathrm{Cl}_{2} \mathrm{O}$.
-KEY CONCEPT PROBLEM 7.3 An electrostatic potential map of water is shown below. Which atom, H or O , is positively polarized and which is negatively polarized? Is this polarization consistent with the electronegativity values of O and H given in Figure 7.4?



### 7.5 Electron-Dot Structures

One of the most convenient ways to picture the sharing of electrons between atoms in covalent or polar covalent bonds is to use electron-dot structures, or Lewis structures, named after G. N. Lewis of the University of California at Berkeley. An electron-dot structure represents an atom's valence electrons by dots and indicates by the placement of the dots how the valence electrons are distributed in a molecule. A hydrogen molecule, for example, is written showing a pair of dots between the hydrogen atoms, indicating that the hydrogens share the pair of electrons in a covalent bond:


By sharing two electrons in a covalent bond, each hydrogen effectively has one electron pair and the stable, filled-shell electron configuration of helium. As with ions (Section 6.12), a filled valence shell for each atom in a molecule leads to maximum stability.


Natalie Foote Tiernan,
"Gilbert Newton Lewis and the Amazing Electron Dots," J. Chem. Educ., Vol. 62, 1985, 569-570.

Electron Dot
Structures I activity

Anthony N. Stranges, "Reflections on the Electron Theory of the Chemical Bond: 1900-1925," J. Chem. Educ., Vol. 61, 1984, 185-190.

William B. Jensen, "Abegg, Lewis, Langmuir, and the Octet Rule," J. Chem. Educ., Vol. 61, 1984, 191-200.

Linus Pauling, "G. N. Lewis and the Chemical Bond," J. Chem. Educ., Vol. 61, 1984, 201-203.

D]
S. R. Logan, "The Role of Lewis Structures in Teaching Covalent Bonding," J. Chem. Educ., Vol. 78, 2001, 1457-1458.

$\square$The Lewis structure is a helpful tool for understanding the configuration and chemistry of molecules of main-group elements. In general, Lewis structures cannot be drawn for transitionmetal compounds because of the complex way that partially filled $d$ orbitals influence the configuration and chemistry of these compounds.

Atoms other than hydrogen also form covalent bonds by sharing electron pairs, and the electron-dot structures of the resultant molecules are drawn by assigning the correct number of valence electrons to each atom. Group 3A atoms (such as boron) have three valence electrons, group 4A atoms (such as carbon) have four valence electrons, and so on across the periodic table. The group 7A element fluorine has seven valence electrons, and an electron-dot structure for the $\mathrm{F}_{2}$ molecule shows how a covalent bond can form:


Six of the seven valence electrons in a fluorine atom are already paired in three filled atomic orbitals and thus are not shared in bonding. The seventh fluorine valence electron, however, is unpaired and can be used in forming a covalent bond to another fluorine. Each atom in the resultant $\mathrm{F}_{2}$ molecule thereby achieves a filled valence-shell octet. The three pairs of nonbonding electrons on each fluorine atom are called lone pairs, or nonbonded pairs, and the shared electrons are called a bonding pair.

The tendency of main-group atoms to fill their $s$ and $p$ subshells when they form bonds-the octet rule discussed in Section 6.12-is an important guiding principle that makes it possible to predict the formulas and electron-dot structures of a great many molecules. As a general rule, an atom shares as many of its valence-shell electrons as possible, either until it has no more to share or until it reaches an octet configuration. For second-row elements in particular, the following guidelines apply:

- Group 3 A elements, such as boron, have three valence electrons and can therefore form three electron-pair bonds in neutral molecules such as borane, $\mathrm{BH}_{3}$. The boron atom in the resultant molecule has only three bonding pairs of electrons and cannot reach an electron octet. (The bonding situation in $\mathrm{BH}_{3}$ is actually more complicated than suggested here; we'll deal with it in Section 19.4.)

- Group $4 A$ elements, such as carbon, have four valence electrons and form four bonds, as in methane, $\mathrm{CH}_{4}$. The carbon atom in the resultant molecule has four bonding pairs of electrons.


Methane

- Group $5 A$ elements, such as nitrogen, have five valence electrons and form three bonds, as in ammonia, $\mathrm{NH}_{3}$. The nitrogen atom in the resultant molecule has three bonding pairs of electrons and one lone pair.

- Group 6 A elements, such as oxygen, have six valence electrons and form two bonds, as in water, $\mathrm{H}_{2} \mathrm{O}$. The oxygen atom in the resultant molecule has two bonding pairs of electrons and two lone pairs.

- Group 7 A elements (halogens), such as fluorine, have seven valence electrons and form one bond, as in hydrogen fluoride, HF. The fluorine atom in the resultant molecule has one bonding pair of electrons and three lone pairs.

$$
: \stackrel{\stackrel{\mathrm{F}}{\bullet}}{\bullet}+\mathrm{H} \cdot \longrightarrow \underset{\substack{\mathrm{H} \\ \\ \\ \\ \text { Hydrogen } \\ \text { fluoride }}}{\stackrel{\bullet}{\mathrm{F}}:}
$$

- Group $8 A$ elements (noble gases), such as neon, rarely form covalent bonds because they already have valence-shell octets.

$$
: \ddot{\mathrm{Ne}}: \quad \text { Does not form covalent bonds }
$$

These conclusions are summarized in Table 7.3.

| TABLE 7.3 | Covalent Bonding for Second-Row Elements |  |  |
| :--- | :--- | :--- | :--- |
| Group | Number of <br> Valence Electrons | Number of <br> Bonds | Example |
| 3A | 3 | 3 | $\mathrm{BH}_{3}$ |
| 4 A | 4 | 4 | $\mathrm{CH}_{4}$ |
| 5A | 5 | 3 | $\mathrm{NH}_{3}$ |
| 6A | 6 | 2 | $\mathrm{H}_{2} \mathrm{O}$ |
| 7A | 7 | 1 | HF |
| 8A | 8 | 0 | Ne |

Not all covalent bonds contain just one shared electron pair (a single bond) like those just discussed. In molecules such as $\mathrm{O}_{2}, \mathrm{~N}_{2}$, and many others, the atoms share more than one pair of electrons, leading to the formation of multiple covalent bonds. The oxygen atoms in the $\mathrm{O}_{2}$ molecule, for example, reach valence-shell octets by sharing four electrons (two pairs), giving a double bond. Similarly, the nitrogen atoms in the $\mathrm{N}_{2}$ molecule share six electrons (three pairs), giving a triple bond. In speaking of such molecules, we often use the term bond order to refer to the number of electron pairs shared between atoms. Thus, the fluorine-fluorine bond in the $\mathrm{F}_{2}$ molecule has a bond order of 1 , the oxygen-oxygen bond in the $\mathrm{O}_{2}$ molecule has a bond order of 2 , and the nitrogen-nitrogen bond in the $\mathrm{N}_{2}$ molecule has a bond order of 3. (Although the $\mathrm{O}_{2}$ molecule does have a double bond, the following electron-dot structure is incorrect in other respects, as we'll see in Section 7.14).


Multiple bonds are both shorter and stronger than their corresponding singlebond counterparts because there are more shared electrons holding the atoms together. Compare, for example, the $\mathrm{O}=\mathrm{O}$ double bond in $\mathrm{O}_{2}$ with the $\mathrm{O}-\mathrm{O}$ single

$\square$
These guidelines are invaluable when writing Lewis structures of organic molecules. The number of bonds and nonbonded electron pairs should be noted.

$\sqrt{ }$
Once formed, there is no difference between an ordinary covalent bond and a coordinate covalent bond.

VStudents sometimes inquire about the origin of a positive or negative charge on a molecule. Showing how a charge on an atom occurs ( $\mathrm{H} \rightarrow \mathrm{H}^{+}+\mathrm{e}^{-}$) and how that simple ion can combine with a neutral molecule to form a polyatomic ion may be helpful $\left(\mathrm{H}^{+}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{H}_{3} \mathrm{O}^{+}\right)$.
bond in $\mathrm{H}_{2} \mathrm{O}_{2}$ (hydrogen peroxide), and compare the $\mathrm{N} \equiv \mathrm{N}$ triple bond in $\mathrm{N}_{2}$ with the $\mathrm{N}-\mathrm{N}$ single bond in $\mathrm{N}_{2} \mathrm{H}_{4}$ (hydrazine):

Bond length:
121 pm
Bond strength: $\quad 498 \mathrm{~kJ} / \mathrm{mol}$

148 pm
$213 \mathrm{~kJ} / \mathrm{mol}$
$: N \equiv N:$
110 pm
$945 \mathrm{~kJ} / \mathrm{mol}$

One final point about covalent bonds involves the origin of the bonding electron pair. Although most covalent bonds form when two atoms each contribute one electron, bonds can also form when one atom donates both electrons (a lone pair) to another atom that has a vacant valence orbital. The ammonium ion $\left(\mathrm{NH}_{4}{ }^{+}\right)$, for example, forms when the two lone-pair electrons from the nitrogen atom of ammonia, : $\mathrm{NH}_{3}$, bond to $\mathrm{H}^{+}$. Such bonds are called coordinate covalent bonds.

An ordinary covalent bond-each atom donates one electron

$$
\mathrm{H} \cdot+\cdot \mathrm{H} \longrightarrow \mathrm{H}: \mathrm{H}
$$

A coordinate covalent bond-the nitrogen atom donates both electrons


Note that the nitrogen atom in the ammonium ion $\left(\mathrm{NH}_{4}{ }^{+}\right)$has more than the usual number of bonds-four instead of three-but that it still has an octet of valence electrons. Nitrogen, oxygen, phosphorus, and sulfur form coordinate covalent bonds frequently.

## Worked Example 7.1

Draw an electron-dot structure for phosphine, $\mathrm{PH}_{3}$.

## Strategy

The number of covalent bonds formed by a main-group element depends on the element's group number. Phosphorus, a group 5A element, has five valence electrons and can achieve a valence-shell octet by forming three bonds and leaving one lone pair. Each hydrogen supplies one electron.

## Solution

$$
\stackrel{H}{\mathrm{H}}: \stackrel{\ddot{\mathrm{P}}}{\stackrel{\mathrm{P}}{2}}: \mathrm{H} \quad \text { Phosphine }
$$

- PROBLEM 7.4 Draw electron-dot structures for the following molecules:
(a) $\mathrm{H}_{2} \mathrm{~S}$, a poisonous gas produced by rotten eggs
(b) $\mathrm{CHCl}_{3}$, chloroform

PROBLEM 7.5 Draw an electron-dot structure for the hydronium ion, $\mathrm{H}_{3} \mathrm{O}^{+}$, and show how a coordinate covalent bond is formed by the reaction of $\mathrm{H}_{2} \mathrm{O}$ with $\mathrm{H}^{+}$.

## 7.6 | Electron-Dot Structures of Polyatomic Molecules

## Compounds of Hydrogen and Second-Row Elements: C, N, O

The vast majority of naturally occurring compounds on which life is basedproteins, fats, carbohydrates, and many others-contain only hydrogen and one or more of the second-row elements carbon, nitrogen, and oxygen. Electron-dot structures are relatively easy to draw for such compounds because the octet rule almost always applies and the number of bonds formed by each element is predictable (Table 7.3).

For relatively small molecules that contain only a few second-row atoms in addition to hydrogen, the second-row atoms are bonded to one another in a central core, with hydrogens on the periphery. In ethane $\left(\mathrm{C}_{2} \mathrm{H}_{6}\right)$, for example, two carbon atoms, each of which forms four bonds, combine with six hydrogens, each of which forms one bond. Joining the two carbon atoms and adding the appropriate number of hydrogens to each yields only one possible structure:


For larger molecules that contain numerous second-row atoms, there is usually more than one possible electron-dot structure. In such cases, some additional knowledge about the order of connections between atoms is necessary before a structure can be drawn.

From now on, we'll follow the usual convention of indicating a two-electron covalent bond by a line. Similarly, we'll use two lines between atoms to represent four shared electrons (two pairs) in a double bond, and three lines to represent six shared electrons (three pairs) in a triple bond. Worked Examples 7.2-7.5 and Problems 7.6-7.8 will give you more practice with electron-dot structures.


Gordon H. Purser, "Lewis Structures are Models for Predicting Molecular Structure, Not Electronic Structure" J. Chem. Educ., Vol. 76, 1999, 1013-1017.

## Worked Example 7.2

Draw an electron-dot structure for hydrazine, $\mathrm{N}_{2} \mathrm{H}_{4}$.

## Strategy

Nitrogen, a group 5A element, has five valence electrons and forms three bonds. Join the two nitrogen atoms, and add two hydrogen atoms to each.

## Solution

- 



Hydrazine, $\mathrm{N}_{2} \mathrm{H}_{4}$

## Worked Example 7.3

Draw an electron-dot structure for carbon dioxide, $\mathrm{CO}_{2}$.

## Strategy

Connect the atoms so that carbon forms four bonds and each oxygen forms two bonds.
The only possible structure contains two carbon-oxygen double bonds.

## Solution




Carbon dioxide, $\mathrm{CO}_{2}$

## Worked Example 7.4

Draw an electron-dot structure for the deadly gas hydrogen cyanide, HCN.

## Strategy

First, connect the carbon and nitrogen atoms. The only way the carbon can form four bonds and the nitrogen can form three bonds is if there is a carbon-nitrogen triple bond.

## Solution



## Worked Key Concept Example 7.5

The following structure is a representation of histidine, an amino acid constituent of proteins. Only the connections between atoms are shown; multiple bonds are not indicated. Give the molecular formula of histidine, and complete the structure by showing where the multiple bonds and lone pairs are (red $=\mathrm{O}$, gray $=\mathrm{C}$, blue $=\mathrm{N}$, ivory $=\mathrm{H}$ ).


## Strategy

Count the atoms of each element to find the formula. Then look at each atom in the structure to find what is needed for completion. Each carbon (gray) should have four bonds, each oxygen (red) should have two bonds and two lone pairs, and each nitrogen (blue) should have three bonds and one lone pair.


## Solution

Histidine has the formula $\mathrm{C}_{6} \mathrm{H}_{9} \mathrm{~N}_{3} \mathrm{O}_{2}$.


PROBLEM 7.6 Draw electron-dot structures for the following molecules:
(a) Propane, $\mathrm{C}_{3} \mathrm{H}_{8}$
(b) Hydrogen peroxide, $\mathrm{H}_{2} \mathrm{O}_{2}$
(c) Methylamine, $\mathrm{CH}_{5} \mathrm{~N}$
(d) Ethylene, $\mathrm{C}_{2} \mathrm{H}_{4}$
(e) Acetylene, $\mathrm{C}_{2} \mathrm{H}_{2}$
(f) Phosgene, $\mathrm{Cl}_{2} \mathrm{CO}$

PROBLEM 7.7 There are two molecules with the formula $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$. Draw electrondot structures for both.

- KEY CONCEPT PROBLEM 7.8 The following structure is a representation of cytosine, a constituent of the DNA found in all living cells. Only the connections between atoms are shown; multiple bonds are not indicated. Give the molecular formula of cytosine, and complete the structure by showing where the multiple bonds and lone pairs are (red $=\mathrm{O}$, gray $=\mathrm{C}$, blue $=\mathrm{N}$, ivory $=\mathrm{H}$ ).



0This general method for writing Lewis structures works equally well for the simple molecules discussed in the previous section.

V
Warn students that it is crucial to follow the steps for writing Lewis structures exactly in the order given. Otherwise, an incorrect Lewis structure may result.

Except for hydrogen, terminal atoms always have complete octets.

## Compounds with Elements Below the Second Row

The simple method of drawing electron-dot structures that works well for most compounds of second-row elements sometimes breaks down for compounds that contain elements below the second row of the periodic table. As we saw in Section 6.12, elements in the third row and lower have unfilled $d$ orbitals and are therefore able to expand their valence shell beyond the normal octet of electrons, forming more than the "normal" number of bonds predicted by their group number. In bromine trifluoride, for instance, the bromine atom forms three electron-pair bonds rather than one and has ten electrons in its valence shell rather than eight:


Bromine trifluoride, $\mathrm{BrF}_{3}$


A general method of drawing electron-dot structures that works for any compound is to use the following steps:

Step 1. Find the total number of valence electrons for all atoms in the molecule. Add one additional electron for each negative charge in an anion and subtract one electron for each positive charge in a cation. In $\mathrm{SF}_{4}$, for example, the total is 34 ( 6 from sulfur and 7 from each of 4 fluorines). In $\mathrm{OH}^{-}$, the total is 8 ( 6 from oxygen, 1 from hydrogen, and 1 for the negative charge). In $\mathrm{NH}_{4}{ }^{+}$, the total is 8 ( 5 from nitrogen, 1 from each of 4 hydrogens, minus 1 for the positive charge).


Step 2. Decide what the connections are between atoms, and draw a line to represent each covalent bond. Often, you'll be told the connections; other times you'll have to guess. Remember that hydrogen and the halogens usually form only one bond, elements in the second row usually form the number of bonds given in Table 7.3, and elements in the third row and lower often expand their valence shells and occur as the central atom around which other atoms are grouped. Also, $\mathrm{it}^{\prime}$ s often the case that the central atom is the least electronegative one (except H). If, for example, you were asked to predict the connections in $\mathrm{SF}_{4}$, a good guess would be that each fluorine forms one bond to sulfur, which occurs as the central atom and forms more bonds than are predicted by its group number.


Step 3. Subtract the number of valence electrons used in bonding from the total number calculated in step 1 to find the number that remain. Assign as many of these remaining electrons as necessary to the terminal atoms (other than hydrogen) so that each has an octet. In $\mathrm{SF}_{4}, 8$ of the 34 total valence electrons are used in
covalent bonding, leaving $34-8=26$. Twenty-four of the 26 are assigned to the four terminal fluorine atoms to reach an octet configuration for each:

$8+24=32$ electrons distributed

Step 4. If unassigned electrons remain after step 3, place them on the central atom. In $\mathrm{SF}_{4}, 32$ of the 34 electrons have been assigned, leaving the final 2 to be placed on the central $S$ atom:


34 electrons distributed


Step 5. If no unassigned electrons remain after step 3 but the central atom does not yet have an octet, use one or more lone pairs of electrons from a neighboring atom to form a multiple bond (either double or triple). Oxygen, carbon, nitrogen, and sulfur often form multiple bonds. Worked Example 7.7 shows how to deal with such a case.

## Worked Example 7.6

Draw an electron-dot structure for phosphorus pentachloride, $\mathrm{PCl}_{5}$.

## Strategy

Follow the steps outlined in the text. First, count the total number of valence electrons. Phosphorus has 5, and each chlorine has 7, for a total of 40 . Next, decide on the connections between atoms, and draw a line to indicate each bond. Because chlorine normally forms only one bond, it's likely in the case of $\mathrm{PCl}_{5}$ that all five chlorines are bonded to a central phosphorus atom, which expands its valence shell:


Ten of the 40 valence electrons are necessary for the five $\mathrm{P}-\mathrm{Cl}$ bonds, leaving 30 to be distributed so that each chlorine has an octet. All 30 remaining valence electrons are used in this step.

## SOlUTION



Phosphorus pentachloride, $\mathrm{PCl}_{5}$


Multiple bonds are never introduced into the Lewis structure before step 5 .

## Worked Example 7.7

Draw an electron-dot structure for formaldehyde, $\mathrm{CH}_{2} \mathrm{O}$.

## Strategy

First, count the total number of valence electrons. Carbon has 4, each hydrogen has 1, and the oxygen has 6 , for a total of 12 . Next, decide on the probable connections between atoms, and draw a line to indicate each bond. In the case of formaldehyde, the less electronegative atom (carbon) is the central atom, and both hydrogens and the oxygen are bonded to carbon:


Six of the 12 valence electrons are used for bonds, leaving 6 for assignment to the terminal oxygen atom.


At this point, all the valence electrons are assigned, but the central carbon atom still does not have an octet. We therefore move two of the oxygen electrons from a lone pair into a bonding pair, generating a carbon-oxygen double bond and satisfying the octet rule for both oxygen and carbon.

## Solution



Formaldehyde, $\mathrm{CH}_{2} \mathrm{O}$

© Formaldehyde-based adhesives are used in the manufacture of plywood and particleboard.


Formaldehyde, $\mathrm{CH}_{2} \mathrm{O}$

## Worked Example 7.8

Draw an electron-dot structure for $\mathrm{XeF}_{5}{ }^{+}$.

## Strategy

Count the total number of valence electrons: Xenon has 8 , each fluorine has 7 , and 1 is subtracted to account for the positive charge, giving a total of 42 . Then, decide on the probable connections between atoms, and draw a line for each bond. In the case of $\mathrm{XeF}_{5}{ }^{+}$, it's likely that the five fluorines are bonded to xenon, a fifth-row atom.


With 10 of the 42 valence electrons used in bonds, distribute as many of the remaining 32 electrons as necessary so that each of the terminal fluorine atoms has an octet. Two electrons still remain, so we assign them to xenon to give the final structure, which has a positive charge.

$\square]^{\text {Ju }}$
Juan Quilex Pardo, "Teaching a Model for Writing Lewis Structures," J. Chem. Educ., Vol. 66, 1989, 456-458.

$\square$
James Allen Carroll, "Drawing Lewis Structures Without Anticipating Octets," J. Chem. Educ., Vol. 63, 1986, 28-31.

(1]
Melvin E. Zandler and Erach R. Talaty, "The ' $6 \mathrm{~N}+2$ Rule' for Writing Lewis Octet Structures," J. Chem. Educ., Vol. 61, 1984, 124-127.

## Solution



- PROBLEM 7.9 Carbon monoxide, CO, is a deadly gas produced by incomplete combustion of fuels. Draw an electron-dot structure for CO.
- PROBLEM 7.10 Draw an electron-dot structure for each of the following molecules:
(a) $\mathrm{AlCl}_{3}$
(b) $\mathrm{ICl}_{3}$
(c) $\mathrm{XeOF}_{4}$
(d) HOBr
- PROBLEM 7.11 Draw an electron-dot structure for each of the following ions:
(a) $\mathrm{OH}^{-}$
(b) $\mathrm{H}_{3} \mathrm{~S}^{+}$
(c) $\mathrm{HCO}_{3}^{-}$
(d) $\mathrm{ClO}_{4}^{-}$


## 7.7 | Electron-Dot Structures and Resonance

The steps given in the previous section for drawing electron-dot structures sometimes lead to an interesting problem. Look at ozone, $\mathrm{O}_{3}$, for instance. Step 1 says that there are 18 valence electrons in the molecule, and steps $2-4$ let us draw the following structure:


We find at this point that the central atom does not yet have an octet, and we therefore have to move one of the lone pairs of electrons on a terminal oxygen to become a bonding pair, giving the central oxygen an octet. But do we take a lone pair from the "right-hand" oxygen or the "left-hand" one? Both possibilities lead to acceptable structures:


Which of the two structures for $\mathrm{O}_{3}$ is correct? In fact, neither is correct by itself. Whenever it's possible to write more than one valid electron-dot structure for a molecule, the actual electronic structure is an average of the different possibilities, called a resonance hybrid. Note that the different resonance forms differ only in the placement of the valence-shell electrons. The total number of valence electrons remains the same in both structures, the connections between atoms remain the same, and the relative positions of the atoms remain the same.

Ozone doesn't have one $\mathrm{O}=\mathrm{O}$ double bond and one $\mathrm{O}-\mathrm{O}$ single bond as the individual structures imply; rather, ozone has two equivalent $\mathrm{O}-\mathrm{O}$ bonds that we can think of as having a bond order of 1.5, midway between pure single bonds and pure double bonds. Both bonds have an identical length of 128 pm .

We can't draw a single electron-dot structure that indicates the equivalence of the two $\mathrm{O}^{-} \mathrm{O}$ bonds in $\mathrm{O}_{3}$ because the conventions we use for indicating electron placement aren't good enough. Instead, the idea of resonance is indicated by drawing the two (or more) individual electron-dot structures and using a double-headed resonance arrow to show that both contribute to the resonance

Thomas J. Clark, "Another Procedure for Writing Lewis Structures," J. Chem. Educ., Vol. 61, 1984, 100.
hybrid. A straight, double-headed arrow always indicates resonance; it is never used for any other purpose.

Francis Delvigne, "A Visual Aid for Teaching the Resonance Concept," J. Chem. Educ., Vol. 66, 1989, 461-462.



The fact that single electron-dot structures can't be written for all molecules indicates that such structures are oversimplified and don't always give an accurate representation of the electron distribution in a molecule. There's a more accurate way of describing electron distributions called molecular orbital theory, which we'll look into shortly. This theory is more complex, however, so chemists still make routine use of electron-dot structures.

## Worked Example 7.9

The nitrate ion, $\mathrm{NO}_{3}^{-}$, has three equivalent oxygen atoms, and its electronic structure is a resonance hybrid of three electron-dot structures. Draw them.

## Strategy

Begin as you would for drawing any electron-dot structure. There are 24 valence electrons in the nitrate ion: 5 from nitrogen, 6 from each of 3 oxygens, and 1 for the negative charge. The three equivalent oxygens are all bonded to nitrogen, the less electronegative central atom:


Distributing the remaining 18 valence electrons among the three terminal oxygen atoms completes the octet of each oxygen but leaves nitrogen with only 6 electrons.


To give nitrogen an octet, one of the oxygen atoms must use a lone pair to form an $\mathrm{N}=\mathrm{O}$ double bond. But which one? There are three possibilities, and thus three electron-dot structures for the nitrate ion, which differ only in the placement of bonding and lone-pair electrons. The connections between atoms are the same in all three structures, and the atoms have the same positions in all structures.

## SOlUTION




PROBLEM 7.12 Called "laughing gas," nitrous oxide $\left(\mathrm{N}_{2} \mathrm{O}\right)$ is sometimes used by dentists as an anesthetic. Given the connections $\mathrm{N}-\mathrm{N}-\mathrm{O}$ draw two electron-dot resonance structures for $\mathrm{N}_{2} \mathrm{O}$.

- PROBLEM 7.13 Draw as many electron-dot resonance structures as possible for each of the following molecules or ions, giving all atoms (except H) octets:
(a) $\mathrm{SO}_{2}$
(b) $\mathrm{CO}_{3}{ }^{2-}$
(c) $\mathrm{HCO}_{2}^{-}$
(d) $\mathrm{BF}_{3}$
- KEY CONCEPT PROBLEM 7.14 The following structure shows the connections between atoms for anisole, a compound used in perfumery. Draw two resonance structures for anisole, showing the positions of the multiple bonds in each (red $=\mathrm{O}$, gray $=\mathrm{C}$, ivory $=\mathrm{H}$ ).



## 7.8 | Formal Charges

Closely related to the ideas of electronegativity and polar covalent bonds discussed in Section 7.4 is the concept of formal charges on specific atoms in electron-dot structures. Formal charges result from a kind of electron "bookkeeping" and can be calculated in the following way: Find the number of valence electrons around an atom in a given electron-dot structure, and compare that value with the number of valence electrons in the isolated atom. If the numbers aren't the same, then the atom in the molecule has either gained or lost electrons and thus has a formal charge. If the atom in a molecule has more electrons than the isolated atom, it has a negative formal charge; if it has fewer electrons, it has a positive formal charge.

- FORMAL CHARGE $=\left(\begin{array}{c}\text { Number of } \\ \text { valence electrons } \\ \text { in free atom }\end{array}\right)-\left(\begin{array}{c}\text { Number of } \\ \text { valence electrons } \\ \text { in bonded atom }\end{array}\right)$

In counting the number of valence electrons in a bonded atom, it's necessary to make a distinction between shared, bonding electrons and unshared, nonbonding electrons. For bookkeeping purposes, an atom can be thought of as "owning" all its nonbonding electrons but only half of its bonding electrons, since the bonding electrons are shared with another atom. Thus, we can rewrite the definition of formal charge as

- FORMAL CHARGE $=\left(\begin{array}{c}\text { Number of } \\ \text { valence electrons } \\ \text { in free atom }\end{array}\right)-\frac{1}{2}\left(\begin{array}{c}\text { Number of } \\ \text { bonding } \\ \text { electrons }\end{array}\right)-\left(\begin{array}{c}\text { Number of } \\ \text { nonbonding } \\ \text { electrons }\end{array}\right)$

In the ammonium ion $\left(\mathrm{NH}_{4}^{+}\right)$, for example, each of the four equivalent hydrogen atoms has 2 valence electrons in its covalent bond to nitrogen, and the nitrogen atom has 8 valence electrons, two from each of its four $\mathrm{N}-\mathrm{H}$ bonds:


For bookkeeping purposes, each hydrogen owns half of its two shared bonding electrons, or 1 , while the nitrogen atom owns half of its 8 shared bonding electrons, or 4 . Because an isolated hydrogen atom has 1 electron and the hydrogens in

David G. DeWit, "Using Formal Charges in Teaching Descriptive Inorganic Chemistry," J. Chem. Educ., Vol. 71, 1994, 750-755.
D7. John E. Packer and Sheila D. Woodgate, "Lewis Structures, Formal Charge, and Oxidation Numbers: A More User-Friendly Approach," J. Chem. Educ., Vol. 68, 1991, 456-458.



Acetamide

T
The best resonance structure has (a) formal charges as close to zero as possible and (b) a negative formal charge on the most electronegative atom and a positive formal charge on the least electronegative atom.


Nitrous oxide
the ammonium ion each still own 1 electron, they have neither gained nor lost electrons and thus have no formal charge. An isolated nitrogen atom, however, has 5 valence electrons, while the nitrogen atom in $\mathrm{NH}_{4}^{+}$owns only 4 and thus has a formal charge of +1 . The sum of the formal charges on all the atoms ( +1 in this example) must equal the overall charge on the ion.

$$
\begin{array}{clll} 
& & \text { For hydrogen: } & \text { Isolated hydrogen valence electrons } \\
& \text { Bound hydrogen bonding electrons } & 2 \\
{\left[\begin{array}{l}
\mathrm{H}: \ddot{\mathrm{N}}: \mathrm{H} \\
\ddot{\mathrm{H}}
\end{array}\right]^{+}} & & \text {Bound hydrogen nonbonding electrons } & 0 \\
& & \text { Formal charge }=1-\frac{1}{2}(2)-0=0 & \\
& & & 5 \\
& & \text { For nitrogen: } & \text { Isolated nitrogen valence electrons }
\end{array}
$$

The value of formal charge calculations comes from their application to the resonance structures described in the previous section. It often happens that the resonance structures of a given substance are not identical. One of the structures may be "better" than the others, meaning that it approximates the actual electronic structure of the substance more closely. The resonance hybrid in such cases is thus weighted more strongly toward the more favorable structure.

Take the organic substance called acetamide, for instance, a compound related to proteins. We can write two valid electron-dot structures for acetamide, both of which fulfill the octet rule for the $\mathrm{C}, \mathrm{N}$, and O atoms. One of the two structures has no formal charges, while the other has formal charges on the O and N atoms. (Check for yourself that the formal charges are correct.)


This structure is lower in energy.


This structure is higher in energy.

Which of the two structures gives a more accurate representation of the molecule? Because energy is required to separate + and - charges, the structure without formal charges is probably lower in energy than the structure with formal charges. Thus, the actual electronic structure of acetamide is closer to that of the more favorable electron-dot structure.

As another example, the resonance structure for $\mathrm{N}_{2} \mathrm{O}$ that places the formal negative charge on the more electronegative oxygen atom rather than on the less electronegative nitrogen atom is probably a more accurate representation of the molecule.


## Worked Example 7.10

Calculate the formal charge on each atom in the following electron-dot structure for $\mathrm{SO}_{2}$ :

$$
: \ddot{\mathrm{O}}-\ddot{\mathrm{S}}=\ddot{\mathrm{O}}
$$

## Strategy

Considering each atom separately, find the number of valence electrons on the atom (the periodic group number). Then subtract half the number of bonding electrons and all the nonbonding electrons.

## Solution

| For sulfur: | Isolated sulfur valence electrons | 6 |
| :--- | :--- | :--- |
|  | Bound sulfur bonding electrons | 6 |
|  | Bound sulfur nonbonding electrons | 2 |
|  | Formal charge $=6-\frac{1}{2}(6)-2=+1$ |  |
| For singly bonded oxygen: | Isolated oxygen valence electrons | 6 |
|  | Bound oxygen bonding electrons | 2 |
|  | Bound oxygen nonbonding electrons | 6 |
| For doubly bonded oxygen: | Formal charge $=6-\frac{1}{2}(2)-6=-1$ |  |
|  | Isolated oxygen valence electrons | 6 |
|  | Bound oxygen bonding electrons | 4 |
|  | Bound oxygen nonbonding electrons | 4 |

The sulfur atom of $\mathrm{SO}_{2}$ has a formal charge of +1 and the singly bonded oxygen atom has a formal charge of -1 . We might therefore write the structure for $\mathrm{SO}_{2}$ as

$$
-\ddot{\mathrm{O}}-\stackrel{+}{\stackrel{\mathrm{S}}{2}}=\ddot{\mathrm{O}}
$$

PROBLEM 7.15 Calculate the formal charge on each atom in the three resonance structures for the nitrate ion in Worked Example 7.9.

- PROBLEM 7.16 Calculate the formal charge on each atom in the following electrondot structures:
(a) Cyanate ion: $[\ddot{\mathrm{N}}=\mathrm{C}=\ddot{\mathrm{O}}]^{-}$
(b) Ozone: : $\ddot{\mathrm{O}}-\ddot{\mathrm{O}}=\ddot{\mathrm{O}}$


## 7.9 | Molecular Shapes: The VSEPR Model

Look at the following computer-generated ball-and-stick models of water, ammonia, and methane. Each of these molecules-and every other molecule as wellhas a specific three-dimensional shape. Often, particularly for biologically important molecules, three-dimensional shape plays a crucial part in determining the molecule's chemistry.


James P. Birk and Soraya Abbassian, "Teaching VSEPR: The Plastic Egg Model," J. Chem. Educ., Vol. 73, 1996, 636-637.

Ronald J. Gillespie, James N. Spencer, and Richard S. Moog, "Demystifying Introductory Chemistry: Part 2. Bonding and Molecular Geometry Without Orbitals-The Electron Domain Model," J. Chem. Educ., Vol. 73, 1996, 622-627.


## VSEPR movie

Brian W. Pfennig and Richard L. Frock, "The Use of Molecular Modeling and VSEPR Theory in the Undergraduate Curriculum to Predict the Three-Dimensional Structure of Molecules," J. Chem. Educ., Vol. 76, 1999, 1018-1022.

Ronald J. Gillespie, "Multiple
Bonds and the VSEPR Model," J. Chem. Educ., Vol. 69, 1992, 116-121.

Like so many other molecular properties, shape is determined by the electronic structure of the bonded atoms. The approximate shape of a molecule can often be predicted by using what is called the valence-shell electron-pair repulsion (VSEPR) model. Electrons in bonds and in lone pairs can be thought of as "charge clouds" that repel one another and stay as far apart as possible, thus causing molecules to assume specific shapes. There are only two steps to remember in applying the VSEPR method:

Step 1. Write an electron-dot structure for the molecule, and count the number of electron charge clouds surrounding the atom of interest. A charge cloud is simply a group of electrons, either in a bond or in a lone pair. Thus, the number of charge clouds is the total number of bonds and lone pairs. Multiple bonds count the same as single bonds because it doesn't matter how many electrons occupy each cloud.
Step 2. Predict the arrangement of charge clouds around each atom by assuming that the clouds are oriented in space as far away from one another as possible. How they achieve this orientation depends on their number. Let's look at the possibilities.

Two Charge Clouds When there are only two charge clouds, as occurs on the carbon atoms of $\mathrm{CO}_{2}$ (two double bonds) and HCN (one single bond and one triple bond), the clouds are farthest apart when they point in opposite directions. Thus, $\mathrm{CO}_{2}$ and HCN are linear molecules with bond angles of $180^{\circ}$.
$\mathrm{ACO}_{2}$ molecule
is linear, with a bond
angle of $180^{\circ}$.



An HCN molecule is linear, with a bond angle of $180^{\circ}$.



Three Charge Clouds When there are three charge clouds, as occurs on the carbon atom of formaldehyde (two single bonds and one double bond) and the sulfur atom of $\mathrm{SO}_{2}$ (one single bond, one double bond, and one lone pair), the clouds are farthest apart when they lie in the same plane and point to the corners of an equilateral triangle. Thus, a formaldehyde molecule has a trigonal planar shape, with $\mathrm{H}-\mathrm{C}-\mathrm{H}$ and $\mathrm{H}-\mathrm{C}=\mathrm{O}$ bond angles near $120^{\circ}$. Similarly, an $\mathrm{SO}_{2}$ molecule has a trigonal planar arrangement of its three charge clouds on sulfur, but one point of the triangle is occupied by a lone pair and two points by oxygen atoms. The molecule therefore has a bent rather than linear shape, with an $\mathrm{O}-\mathrm{S}-\mathrm{O}$ bond angle of approximately $120^{\circ}$ rather than $180^{\circ}$.

A formaldehyde molecule is trigonal planar, with bond angles of roughly $120^{\circ}$.


Top view



Side view



Four Charge Clouds When there are four charge clouds, as occurs on the central atoms in $\mathrm{CH}_{4}$ (four single bonds), $\mathrm{NH}_{3}$ (three single bonds and one lone pair), and $\mathrm{H}_{2} \mathrm{O}$ (two single bonds and two lone pairs), the clouds are farthest apart if they extend toward the corners of a regular tetrahedron. As illustrated in Figure 7.5, a regular tetrahedron is a geometric solid whose four identical faces are equilateral triangles. The central atom lies in the center of the tetrahedron, the charge clouds point toward the four corners, and the angle between two lines drawn from the center to any two corners is $109.5^{\circ}$.


Because valence electron octets are so common, particularly for second-row elements, the atoms in a great many molecules have shapes based on the tetrahedron. Methane, for example, has a tetrahedral shape, with $\mathrm{H}-\mathrm{C}-\mathrm{H}$ bond angles of $109.5^{\circ}$. In $\mathrm{NH}_{3}$, the nitrogen atom has a tetrahedral arrangement of its four charge clouds, but one corner of the tetrahedron is occupied by a lone pair, resulting in a trigonal pyramidal shape for the molecule. Similarly, $\mathrm{H}_{2} \mathrm{O}$ has two corners of the tetrahedron occupied by lone pairs and thus has a bent shape.

A methane molecule is tetrahedral, with bond angles of $109.5^{\circ}$.


An ammonia molecule is trigonal pyramidal, with bond angles of $107^{\circ}$.




Note how the three-dimensional shapes of the molecules in the preceding three structures are indicated. Solid lines are assumed to be in the plane of the paper, dashed lines recede behind the plane of the paper away from the viewer, and heavy,


FIGURE 7.5 The tetrahedral geometry of an atom surrounded by four charge clouds. (a) The atom is located in the center of a regular tetrahedron, and (b) the four charge clouds point toward the four corners. (c) The angle between any two bonds is $109.5^{\circ}$.

V
A good way to introduce the tetrahedron is to draw a cube with atoms on alternating corners. Each atom will be on a face diagonal to each other atom, and the symmetry will be more evident. Likewise, an octahedron can be shown as a cube with an atom on each face.

$\checkmark$Molecular geometries are described by the relative positions of the nuclei, not the location of electron clouds. $\mathrm{NH}_{3}$ is trigonal pyramidal, not tetrahedral.

VElectron-dot structures do not imply geometry. It makes no difference whether the two pairs of nonbonded electrons on $\mathrm{H}_{2} \mathrm{O}$ are placed $90^{\circ}$ or $180^{\circ}$ to one another in the electron-dot structure.
wedged lines protrude out of the paper toward the viewer. Note also that the $\mathrm{H}-\mathrm{N}-\mathrm{H}$ bond angles in ammonia $\left(107^{\circ}\right)$ and the $\mathrm{H}-\mathrm{O}-\mathrm{H}$ bond angle in water $\left(104.5^{\circ}\right)$ are less than the ideal $109.5^{\circ}$ tetrahedral value. The angles are diminished somewhat from the tetrahedral value because of the presence of lone pairs. Charge clouds of lonepair electrons spread out more than charge clouds of bonding electrons because they aren't confined to the space between two atoms. As a result, the somewhat enlarged lone-pair charge clouds tend to push in the bond angles in the rest of the molecule.

Five Charge Clouds Five charge clouds, such as are found on the central atoms in $\mathrm{PCl}_{5}, \mathrm{SF}_{4}, \mathrm{ClF}_{3}$, and $\mathrm{I}_{3}^{-}$, are oriented toward the corners of a geometric figure called a trigonal bipyramid. Three clouds lie in a plane and point toward the corners of an equilateral triangle, the fourth cloud points directly up, and the fifth cloud points down:


Trigonal bipyramidal geometry differs from the linear, trigonal planar, and tetrahedral geometries discussed previously because it has two kinds of positions-three equatorial positions (around the "equator" of the bipyramid) and two axial positions (along the "axis" of the bipyramid). The three equatorial positions are at angles of $120^{\circ}$ to one another and at an angle of $90^{\circ}$ to the axial positions. The two axial positions are at angles of $180^{\circ}$ to each other and at an angle of $90^{\circ}$ to the equatorial positions.

Different substances with a trigonal bipyramidal arrangement of charge clouds adopt different shapes, depending on whether the five charge clouds are of bonding or nonbonding electrons. Phosphorus pentachloride, for example, has all five positions around phosphorus occupied by chlorine atoms and thus has a trigonal bipyramidal shape:

A $\mathrm{PCl}_{5}$ molecule is trigonal bipyramidal.



The sulfur atom in $\mathrm{SF}_{4}$ is bonded to four other atoms and has one nonbonding electron lone pair. Because an electron lone pair spreads out and occupies more space than a bonding pair, the nonbonding electrons in $\mathrm{SF}_{4}$ occupy an equatorial position where they are close to ( $90^{\circ}$ away from) only two charge clouds. Were they instead to occupy an axial position, they would be close to three charge clouds. As a result, $\mathrm{SF}_{4}$ has a shape often described as that of a seesaw. The two axial bonds form the board, and the two equatorial bonds form the legs of the seesaw. (You have to tilt your head $90^{\circ}$ to see it.)

An SF 4 molecule is shaped like a seesaw (turn $90^{\circ}$ to see it).


The chlorine atom in $\mathrm{ClF}_{3}$ is bonded to three other atoms and has two nonbonding electron lone pairs. Both lone pairs occupy equatorial positions, resulting in a T shape for the $\mathrm{ClF}_{3}$ molecule. (As with the seesaw, you have to tilt your head $90^{\circ}$ to see the T.)
$\mathrm{A} \mathrm{ClF}_{3}$ molecule is T-shaped (turn $90^{\circ}$ to see it).



Six Charge Clouds Six charge clouds around an atom orient toward the six corners of a regular octahedron, a geometric solid whose eight faces are equilateral triangles. All six positions are equivalent, and the angle between any two adjacent positions is $90^{\circ}$.


As was true in the case of five charge clouds, different shapes are possible for molecules having atoms with six charge clouds, depending on whether the clouds are of bonding or nonbonding electrons. Sulfur hexafluoride, for example, has all six positions around sulfur occupied by fluorine atoms:

An $\mathrm{SF}_{6}$ molecule is octahedral.


The antimony atom in the $\mathrm{SbCl}_{5}{ }^{2-}$ ion also has six charge clouds, but it is bonded to only five atoms and has one nonbonding electron lone pair. As a result, the ion has a square pyramidal shape-a pyramid with a square base:
$\mathrm{An} \mathrm{SbCl}_{5}{ }^{2-}$ ion has a square pyramidal shape.


The xenon atom in $\mathrm{XeF}_{4}$ is bonded to four atoms and has two lone pairs. As you might expect, the lone pairs orient as far away from each other as possible to minimize electronic repulsions, giving the molecule a square planar shape:

An $\mathrm{XeF}_{4}$ molecule has a square planar shape.


All the geometries discussed above for two to six charge clouds around an atom are summarized in Table 7.4.

TABLE 7.4 Molecular Geometry Around Atoms with 2, 3, 4, 5, and 6 Charge Clouds

TABLE 7.4
(Continued)

| Number <br> of Bonds | Number <br> of Lone <br> Pairs | Number <br> of Charge <br> Clouds | Molecular <br> Geometry | Example |
| :--- | :--- | :--- | :--- | :--- |

V
When VSEPR is used to describe the shape of an organic molecule, it is applied to each individual carbon, nitrogen, and oxygen atom.

Shapes of Larger Molecules The geometries around individual atoms in larger molecules can also be predicted from the rules summarized in Table 7.4. For example, each of the two carbon atoms in ethylene $\left(\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}\right)$ has three charge clouds, giving rise to trigonal planar geometry for each carbon. The molecule as a whole is planar, with $\mathrm{H}-\mathrm{C}-\mathrm{C}$ and $\mathrm{H}-\mathrm{C}-\mathrm{H}$ bond angles of approximately $120^{\circ}$.

Each carbon atom in ethylene has trigonal planar geometry. As a result, the entire molecule is planar, with bond angles of $120^{\circ}$.




Side view
Carbon atoms bonded to four other atoms are each at the center of a tetrahedron. As shown below for ethane, $\mathrm{H}_{3} \mathrm{C}-\mathrm{CH}_{3}$, the two tetrahedrons are joined so that the central carbon atom of one is a corner atom of the other.

Each carbon atom in ethane has tetrahedral geometry, with bond angles of $109.5^{\circ}$.




## Worked Example 7.11

Predict the shape of $\mathrm{BrF}_{5}$.

## Strategy

First, draw an electron-dot structure for $\mathrm{BrF}_{5}$ to determine that the central bromine atom has six charge clouds (five bonds and one lone pair). Then predict how the six charge clouds are arranged.


## Solution

Six charge clouds implies an octahedral arrangement; five attached atoms and one lone pair give $\mathrm{BrF}_{5}$ a square pyramidal shape:


- PROBLEM 7.17 Predict the shapes of the following molecules or ions:
(a) $\mathrm{O}_{3}$
(b) $\mathrm{H}_{3} \mathrm{O}^{+}$
(c) $\mathrm{XeF}_{2}$
(d) $\mathrm{PF}_{6}^{-}$
(e) $\mathrm{XeOF}_{4}$
(f) $\mathrm{AlH}_{4}^{-}$
(g) $\mathrm{BF}_{4}^{-}$
(h) $\mathrm{SiCl}_{4}$
(i) $\mathrm{ICl}_{4}^{-}$
(j) $\mathrm{AlCl}_{3}$

PROBLEM 7.18 Acetic acid, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$, is the main organic constituent of vinegar. Draw an electron-dot structure for acetic acid, and show its overall shape. (The two carbons are connected by a single bond, and both oxygens are connected to the same carbon.)
$\curvearrowleft$ KEY CONCEPT PROBLEM 7.19 What is the geometry around the central atom in each of the following molecular models?

(a)

(b)

### 7.10 | Valence Bond Theory

The electron-dot structures described in Sections 7.6 and 7.7 provide a simple way to predict the distribution of valence electrons in a molecule, and the VSEPR model discussed in Section 7.9 provides a simple way to predict molecular shapes. Neither model, however, says anything about the detailed electronic nature of covalent bonds. To describe bonding, a quantum mechanical model called valence bond theory has been developed.

Valence bond theory provides an easily visualized orbital picture of how electron pairs are shared in a covalent bond. In essence, a covalent bond results when two atoms approach each other closely enough so that a singly occupied valence orbital on one atom overlaps a singly occupied valence orbital on the other atom. The now-paired electrons in the overlapping orbitals are attracted to the nuclei of both atoms and thus bond the two atoms together. In the $\mathrm{H}_{2}$ molecule, for instance, the $\mathrm{H}-\mathrm{H}$ bond results from the overlap of two singly occupied hydrogen $1 s$ orbitals:


In the valence bond model, the strength of a covalent bond depends on the amount of orbital overlap: The greater the overlap, the stronger the bond. This, in turn, means that bonds formed by overlap of other than $s$ orbitals have a directionality to them. In the $\mathrm{F}_{2}$ molecule, for instance, each fluorine atom has the electron configuration [He] $2 s^{2} 2 p_{x}{ }^{2} 2 p_{y}{ }^{2} 2 p_{z}{ }^{1}$, so the $\mathrm{F}-\mathrm{F}$ bond results from the overlap of two singly occupied $2 p$ orbitals. The two $p$ orbitals must point directly at each other for optimum overlap to occur, and the F-F bond forms along the orbital axis. Such bonds that result from head-on orbital overlap are called sigma ( $\sigma$ ) bonds.


In HCl , the covalent bond involves overlap of a hydrogen $1 s$ orbital with a chlorine $3 p$ orbital and forms along the $p$-orbital axis:


The key ideas of valence bond theory can be summarized as follows:

## KEY IDEAS OF VALENCE BOND THEORY

- Covalent bonds are formed by overlap of atomic orbitals, each of which contains one electron of opposite spin.
- Each of the bonded atoms maintains its own atomic orbitals, but the electron pair in the overlapping orbitals is shared by both atoms.
- The greater the amount of orbital overlap, the stronger the bond. This leads to a directional character to the bond when other than $s$ orbitals are involved.
(O)

VElectron-dot structures describe a bond as a sharing of a pair of electrons. Valence bond theory explains how electrons become shared by the overlap of atomic orbitals.

$\square$D. W. Emerson, "A Colorful Demonstration to Simulate Orbital Hybridization," J. Chem. Educ., Vol. 65, 1988, 454.

$\square$John Barbaro, "Orbital Bartending," J. Chem. Educ., Vol. 71, 1994, 1012. An analogy for orbital hybridization.

## Methane 3D model



Promotion and Hybridization activity


### 7.11 Hybridization and $s p^{3}$ Hybrid Orbitals

How does valence bond theory describe the electronic structure of a polyatomic molecule, and how does it account for molecular shape? Let's look, for example, at a simple tetrahedral molecule such as methane, $\mathrm{CH}_{4}$. There are several problems to be dealt with.

Carbon has the ground-state electron configuration [He] $2 s^{2} 2 p_{x}{ }^{1} 2 p_{y}{ }^{1}$. It thus has four valence electrons, two of which are paired in a $2 s$ orbital and two of which are unpaired in different $2 p$ orbitals that we'll arbitrarily designate as $2 p_{x}$ and $2 p_{y}$. But how can carbon form four bonds if two of its valence electrons are already paired and only two unpaired electrons are available for sharing? The answer is that an electron must be promoted from the lower-energy $2 s$ orbital to the vacant, higher-energy $2 p$ orbital, giving an excited-state configuration [He] $2 s^{1} 2 p_{x}{ }^{1} 2 p_{y}{ }^{1} 2 p_{z}{ }^{1}$, which has four unpaired electrons.


A second problem is more difficult to resolve: If excited-state carbon uses two kinds of orbitals for bonding, $2 s$ and $2 p$, how can it form four equivalent bonds? Furthermore, if the three $2 p$ orbitals in carbon are at angles of $90^{\circ}$ to one another, and if the $2 s$ orbital has no directionality, how can carbon form bonds with angles of $109.5^{\circ}$ directed to the corners of a regular tetrahedron? The answers to these questions were provided in 1931 by Linus Pauling, who introduced the idea of hybrid orbitals.

Pauling showed that the quantum mechanical wave functions for $s$ and $p$ atomic orbitals derived from the Schrödinger wave equation (Section 5.7) can be mathematically combined to form a new set of equivalent wave functions called hybrid atomic orbitals. When one $s$ orbital combines with three $p$ orbitals, as occurs in an excited-state carbon atom, four equivalent hybrid orbitals, called $s p^{3}$ hybrids, result. (The superscript 3 in the name $s p^{3}$ tells how many $p$ atomic orbitals are combined to construct the hybrid orbitals, not how many electrons occupy each orbital.)


Each of the four equivalent $s p^{3}$ hybrid orbitals has two lobes of different phase like an atomic $p$ orbital, but one of the lobes is larger than the other. The four large lobes are oriented toward the four corners of a tetrahedron (Figure 7.6).

The shared electrons in a covalent bond made with a strongly directed hybrid orbital spend most of their time in the region between the two bonded nuclei. As a result, covalent bonds made with $s p^{3}$ hybrid orbitals are often strong ones. In fact, the energy released on forming the four strong $\mathrm{C}-\mathrm{H}$ bonds in $\mathrm{CH}_{4}$ more than

compensates for the energy required to produce the excited state of carbon. Figure 7.7 shows how the four $\mathrm{C}-\mathrm{H}$ sigma bonds in methane can form by headon overlap of carbon $s p^{3}$ hybrid orbitals with hydrogen $1 s$ orbitals.


Four hydrogen $1 s$ atomic orbitals

A FIGURE 7.6 The formation of four $s p^{3}$ hybrid orbitals by combination of an atomic $s$ orbital with three atomic $p$ orbitals. Each $s p^{3}$ hybrid orbital has two lobes, one of which is larger than the other. The four large lobes are oriented toward the corners of a tetrahedron at angles of $109.5^{\circ}$.
© FIGURE 7.7 The bonding in methane. Each of the four C-H bonds results from headon $(\sigma)$ overlap of a singly occupied carbon $s p^{3}$ hybrid orbital with a singly occupied hydrogen 1 s orbital.

The same kind of $s p^{3}$ hybridization that describes the bonds to carbon in the tetrahedral methane molecule also describes bonds to nitrogen in the trigonal pyramidal ammonia molecule, to oxygen in the bent water molecule, and to all other atoms that VSEPR theory predicts to have a tetrahedral arrangement of four charge clouds.


Methane, $\mathrm{CH}_{4}$


Ammonia, $\mathrm{NH}_{3}$


Water, $\mathrm{H}_{2} \mathrm{O}$

## -

PROBLEM 7.20 Describe the bonding in ethane, $\mathrm{C}_{2} \mathrm{H}_{6}$, and tell what kinds of orbitals on each atom overlap to form the $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{H}$ bonds.

FIGURE 7.8 The formation of $s p^{2}$ hybrid orbitals by combination of one $s$ orbital and two $p$ orbitals. The three hybrids lie in a plane at angles of $120^{\circ}$ to one another. One unhybridized $p$ orbital remains, oriented at a $90^{\circ}$ angle to the plane of the $s p^{2}$ orbitals.

### 7.12 Other Kinds of Hybrid Orbitals

Each of the different geometries shown in Table 7.4-whether based on two, three, four, five, or six charge clouds-can be accounted for by a specific kind of orbital hybridization. Let's look at each.

## $s p^{2}$ Hybridization

Atoms with three charge clouds undergo hybridization by combination of one atomic $s$ orbital with two $p$ orbitals, resulting in three $s p^{2}$ hybrid orbitals. These $s p^{2}$ hybrids lie in a plane and are oriented toward the corners of an equilateral triangle at angles of $120^{\circ}$ to one another. One $p$ orbital remains unchanged and is oriented at a $90^{\circ}$ angle to the plane of the $s p^{2}$ hybrids, as shown in Figure 7.8.


The presence of the unhybridized $p$ orbital on an $s p^{2}$-hybridized atom has some interesting consequences. Look, for example, at ethylene, $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}$, a colorless gas used as starting material for the industrial preparation of polyethylene. Each carbon atom in ethylene has three charge clouds and is $s p^{2}$-hybridized. When two $s p^{2}$-hybridized carbon atoms approach each other with $s p^{2}$ orbitals aligned head-on for $\sigma$ bonding, the unhybridized $p$ orbitals on the carbons also approach each other and form a bond, but in a parallel, sideways manner rather than head-on. Such sideways bonding, in which the shared electrons occupy regions above and below a line connecting the nuclei rather than between the nuclei, is called a pi $(\boldsymbol{\pi})$ bond.


The $\pi$ bond has two regions of orbital overlap-one above and one below the internuclear axis. Both regions are part of the same bond, and the two shared electrons are spread over both regions. Note that the $p$ lobes must be of the same phase for overlap leading to bond formation.

The net result of both $\sigma$ and $\pi$ overlap is the sharing of four electrons and the formation of a carbon-carbon double bond. The two remaining $s p^{2}$ orbitals on each carbon then overlap with hydrogen $1 s$ orbitals to form four $\mathrm{C}-\mathrm{H}$ bonds and complete the $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}$ structure (Figure 7.9).


4 FIGURE 7.9 The structure of ethylene. The carbon-carbon double bond consists of one $\sigma$ bond from the head-on overlap of $s p^{2}$ orbitals and one $\pi$ bond from the sideways overlap of $p$ orbitals. The four $\mathrm{C}-\mathrm{H} \sigma$ bonds result from overlap of carbon $s p^{2}$ orbitals with hydrogen $1 s$ orbitals. The overall shape of the molecule is planar (flat), with $\mathrm{H}-\mathrm{C}-\mathrm{H}$ and $\mathrm{H}-\mathrm{C}-\mathrm{C}$ bond angles of approximately $120^{\circ}$.

PROBLEM 7.21 Describe the hybridization of the carbon atom in formaldehyde, $\mathrm{H}_{2} \mathrm{C}=\mathrm{O}$, and make a rough sketch of the molecule showing the orbitals involved in bonding.

## $s p$ Hybridization

Atoms with two charge clouds undergo hybridization by combination of one atomic $s$ orbital with one $p$ orbital, resulting in two $s p$ hybrid orbitals that are oriented $180^{\circ}$ from each other. Since only one $p$ orbital is involved when an atom undergoes $s p$ hybridization, the other two $p$ orbitals are unchanged and are oriented at $90^{\circ}$ angles to the $s p$ hybrids, as shown in Figure 7.10.


A FIGURE 7.10 The combination of one $s$ and one $p$ orbital gives two $s p$ hybrid orbitals oriented $180^{\circ}$ apart. Two unhybridized $p$ orbitals remain and are oriented at $90^{\circ}$ angles to the $s p$ hybrids.
One of the simplest examples of $s p$ hybridization is found in acetylene, $\mathrm{H}-\mathrm{C} \equiv \mathrm{C}-\mathrm{H}$, a colorless gas used in welding. Both carbon atoms in the acetylene molecule have linear geometry and are $s p$-hybridized. When the two $s p$-hybridized carbon atoms approach each other with their $s p$ orbitals aligned

head-on for $\sigma$ bonding, the unhybridized $p$ orbitals on each carbon are aligned for $\pi$ bonding. Two $p$ orbitals are aligned in an up/down position, and two are aligned in an in/out position. Thus, there are two mutually perpendicular $\pi$ bonds that form in acetylene by sideways overlap of $p$ orbitals, along with one $\sigma$ bond that forms by head-on overlap of the $s p$ orbitals. The net result is the sharing of six electrons and formation of a triple bond (Figure 7.11). In addition, two $\mathrm{C}-\mathrm{H}$ bonds form by overlap of the remaining two $s p$ orbitals with hydrogen $1 s$ orbitals.

© FIGURE 7.11 Formation of a triple bond by two $s p$-hybridized atoms. A $\sigma$ bond forms by head-on overlap of $s p$ orbitals, and two mutually perpendicular $\pi$ bonds form by sideways overlap of $p$ orbitals.

FIGURE 7.12 The five $s p^{3} d$ hybrid orbitals and their trigonal bipyramidal geometry.


- PROBLEM 7.22 Describe the hybridization of the carbon atom in the hydrogen cyanide molecule, $\mathrm{H}-\mathrm{C} \equiv \mathrm{N}$, and make a rough sketch to show the hybrid orbitals it uses for bonding.


## $s p^{3} d$ Hybridization

Atoms with five charge clouds, such as the phosphorus in $\mathrm{PCl}_{5}$, undergo hybridization by combination of five atomic orbitals. Because a given shell has a total of only four $s$ and $p$ orbitals, the need to use five orbitals implies that a $d$ orbital must be involved. Thus, only atoms in the third or lower rows in the periodic table can form the necessary hybrids.

Hybridization of five atomic orbitals occurs by a combination of one $s$ orbital, three $p$ orbitals, and one $d$ orbital, giving five $s p^{3} d$ hybrid orbitals in a trigonal bipyramidal arrangement (Figure 7.12). Three of the hybrid orbitals lie in a plane at angles of $120^{\circ}$, with the remaining two orbitals perpendicular to the plane, one above and one below.


## $s p^{3} d^{2}$ Hybridization

Atoms with six charge clouds, such as the sulfur in $\mathrm{SF}_{6}$, undergo hybridization by combination of six atomic orbitals. This again implies that valence-shell $d$ orbitals are involved and that only atoms in the third or lower rows in the periodic table
can form the necessary hybrids. Hybridization occurs by a combination of one $s$ orbital, three $p$ orbitals, and two $d$ orbitals, resulting in six $s p^{3} d^{2}$ hybrid orbitals with an octahedral arrangement (Figure 7.13). All six orbitals are equivalent, and the angle between any two adjacent orbitals is $90^{\circ}$.


Side view


Top view

A summary of the five most common kinds of hybridization and the geometry that each corresponds to is given in Table 7.5.

| TABLE 7.5 | Hybrid Orbitals and Their Geometry |  |
| :--- | :--- | :--- |
| Number of | Geometry of |  |
| Charge Clouds Charge Clouds Hybridization <br> 2 Linear $s p$ <br> 3 Trigonal planar $s p^{2}$ <br> 4 Tetrahedral $s p^{3}$ <br> 5 Trigonal bipyramidal $s p^{3} d$ <br> 6 Octahedral $s p^{3} d^{2}$ |  |  |

## Worked Example 7.12

Describe the hybridization of the carbon atoms in allene, $\mathrm{H}_{2} \mathrm{C}=\mathrm{C}=\mathrm{CH}_{2}$, and make a rough sketch of the molecule showing its hybrid orbitals.

## Strategy

Draw an electron-dot structure to find the number of charge clouds on each atom.


Then predict the geometry around each atom using VSEPR theory.

## Solution

Because the central carbon atom in allene has two charge clouds (two double bonds), it has a linear geometry and is $s p$-hybridized. Because the two terminal carbon atoms have three charge clouds each (one double bond and two C-H bonds), they have trigonal planar geometry and are $s p^{2}$-hybridized. The central carbon uses its $s p$ orbitals to form two $\sigma$ bonds at $180^{\circ}$ angles and uses its two unhybridized $p$ orbitals to form

4 FIGURE 7.13 The six $s p^{3} d^{2}$ hybrid orbitals and their octahedral geometry.


VHybrid orbital sets have the same geometries as electron cloud sets predicted by VSEPR. Therefore, each VSEPR geometry has a corresponding set of hybrid orbitals used by the central atom.
(The carbon orbitals shown in blue are $s p$ and $s p^{2}$ hybrids; those shown in green are unhybridized $p$ orbitals.)

- PROBLEM 7.23 Describe the hybridization of the central iodine atom in $\mathrm{I}_{3}{ }^{-}$, and make a rough sketch of the ion showing the orbitals involved in bonding.
- PROBLEM 7.24 Describe the hybridization of the sulfur atom in $\mathrm{SF}_{2}, \mathrm{SF}_{4}$, and $\mathrm{SF}_{6}$ molecules.
- KEY CONCEPT PROBLEM 7.25 Identify each of the following sets of hybrid orbitals:

$\square$A. B. Sannigrahi and Tapas Kar, "Molecular Orbital Theory of Bond Order and Valency," J. Chem. Educ., Vol. 65, 1988, 674-676.

Valence bond theory assumes electrons are in atomic orbitals; molecular orbital theory places electrons in orbitals belonging to the entire molecule.

$\pi$ bonds, one to each of the terminal carbons. Each terminal carbon atom uses an $s p^{2}$ orbital for $\sigma$ bonding to carbon, a $p$ orbital for $\pi$ bonding, and its two remaining $s p^{2}$ orbitals for $\mathrm{C}-\mathrm{H}$ bonds.

(a)

(b)

### 7.13 | Molecular Orbital Theory: The Hydrogen Molecule

The valence bond model of covalent bonding is easy to visualize and leads to a satisfactory description for most molecules. It does, however, have some problems. Perhaps the most serious flaw in the valence bond model is that it sometimes leads to an incorrect electronic description. For this reason, another bonding description called molecular orbital (MO) theory is often used. The molecular orbital model is more complex than the valence bond model, particularly for larger molecules, but sometimes gives a more satisfactory accounting of chemical and physical properties.

To introduce some of the basic ideas of molecular orbital theory, let's look again at orbitals. The concept of an orbital derives from the quantum mechanical wave equation, in which the square of the wave function gives the probability of finding an electron within a given region of space. The kinds of orbitals that we've been concerned with up to this point are called atomic orbitals because they are characteristic of individual atoms. Atomic orbitals on the same atom can combine to form hybrids, and atomic orbitals on different atoms can overlap to form covalent bonds, but the orbitals and the electrons in them remain localized on specific atoms.
atomic orbital A wave function whose square gives the probability of finding an electron within a given region of space in an atom.
Molecular orbital theory takes a different approach to bonding by considering the molecule as a whole rather than concentrating on individual atoms. A molecular orbital is to a molecule what an atomic orbital is to an atom.

## - molecular orbital A wave function whose square gives the probability of finding an electron within a given region of space in a molecule.

Like atomic orbitals, molecular orbitals have specific energy levels and specific shapes, and they can be occupied by a maximum of two electrons with opposite spins. The energy and shape of a molecular orbital depend on the size and complexity of the molecule and can thus be fairly complicated, but the fundamental analogy between atomic and molecular orbitals remains.

Let's look at the molecular orbital description of the simple diatomic molecule $\mathrm{H}_{2}$ to see some general features of MO theory. Imagine what might happen when two isolated hydrogen atoms approach each other and begin to interact. The 1 s orbitals begin to blend together, and the electrons spread out over both atoms. Molecular orbital theory says that there are two ways for the orbital interaction to occur-an additive way and a subtractive way. The additive interaction leads to formation of a molecular orbital that is roughly egg-shaped, whereas the subtractive interaction leads to formation of a molecular orbital that contains a node between atoms (Figure 7.14).


The additive combination, denoted $\sigma$, is lower in energy than the two isolated $1 s$ orbitals and is called a bonding molecular orbital because any electrons it contains spend most of their time in the region between the two nuclei, helping to bond the atoms together. The subtractive combination, denoted $\sigma^{*}$ (spoken as "sigma star"), is higher in energy than the two isolated $1 s$ orbitals and is called an antibonding molecular orbital because any electrons it contains can't occupy the central region between the nuclei and can't contribute to bonding. Diagrams of the sort shown in Figure 7.15 are used to show the energy relationships of the various orbitals. The two isolated H atomic orbitals are shown on either side, and the two $\mathrm{H}_{2}$ molecular orbitals are shown in the middle. Each of the starting hydrogen atomic orbitals has one electron, which pair up and occupy the lower-energy bonding MO after covalent bond formation.



FIGURE 7.14 Formation of molecular orbitals in the $\mathrm{H}_{2}$ molecule. The additive combination of two atomic $1 s$ orbitals forms a lower-energy, bonding molecular orbital. The subtractive combination forms a higher-energy, antibonding molecular orbital that has a node between the nuclei.

FIGURE 7.15 A molecular orbital diagram for the $\mathrm{H}_{2}$ molecule. The two electrons are paired in the bonding $\sigma \mathrm{MO}$, and the antibonding $\sigma^{*} \mathrm{MO}$ is vacant.

FIGURE 7.16 MO diagrams for (a) the stable $\mathrm{H}_{2}{ }^{-}$ ion and (b) the unstable $\mathrm{He}_{2}$ molecule.

Similar MO diagrams can be drawn and predictions about stability can be made for related diatomic species such as $\mathrm{H}_{2}^{-}$and $\mathrm{He}_{2}$. For example, we might imagine constructing the $\mathrm{H}_{2}^{-}$ion by bringing together a neutral H • atom with one electron and an $\mathrm{H}^{-}$anion with two electrons. Since the resultant $\mathrm{H}_{2}^{-}$ion has three electrons, two of them will occupy the lower-energy bonding $\sigma \mathrm{MO}$ and one will occupy the higher-energy antibonding $\sigma^{*} \mathrm{MO}$ (Figure 7.16a). Two electrons are lowered in energy while only one electron is raised in energy, so a net gain in stability results. We therefore predict (and find experimentally) that the $\mathrm{H}_{2}^{-}$ion is stable.

(a)


The $\mathrm{He}_{2}$ "molecule"
(b)

What about $\mathrm{He}_{2}$ ? A hypothetical $\mathrm{He}_{2}$ molecule has four electrons, two of which occupy the lower-energy bonding orbital and two of which occupy the higher-energy antibonding orbital, as shown in Figure 7.16b. Since the decrease in energy for the two bonding electrons is counteracted by the increase in energy for the two antibonding electrons, the $\mathrm{He}_{2}$ molecule has no net bonding energy and is not stable.

Bond orders-the number of electron pairs shared between atoms (Section 7.5)— can be calculated from MO diagrams by subtracting the number of antibonding electrons from the number of bonding electrons and dividing by 2 :

$$
\text { Bond order }=\frac{\binom{\text { Number of }}{\text { bonding electrons }}-\binom{\text { Number of }}{\text { antibonding electrons }}}{2}
$$

The $\mathrm{H}_{2}$ molecule, for example, has a bond order of 1 because it has two bonding electrons and no antibonding electrons. Similarly, the $\mathrm{H}_{2}^{-}$ion has a bond order of $1 / 2$, and the hypothetical $\mathrm{He}_{2}$ molecule has a bond order of 0 , which accounts for the instability of $\mathrm{He}_{2}$.

The key ideas of the molecular orbital theory of bonding can be summarized as follows:

## KEY IDEAS OF MOLECULAR ORBITAL THEORY

- Molecular orbitals are to molecules what atomic orbitals are to atoms. A molecular orbital describes a region of space in a molecule where electrons are most likely to be found, and it has a specific size, shape, and energy level.
- Molecular orbitals are formed by combining atomic orbitals on different atoms. The number of molecular orbitals formed is the same as the number of atomic orbitals combined.
- Molecular orbitals that are lower in energy than the starting atomic orbitals are bonding; MOs that are higher in energy than the starting atomic orbitals are antibonding.
- Electrons occupy molecular orbitals beginning with the MO of lowest energy. Only two electrons occupy each orbital, and their spins are paired.
- Bond order can be calculated by subtracting the number of electrons in antibonding MOs from the number in bonding MOs and dividing by 2.

PROBLEM 7.26 Construct an MO diagram for the $\mathrm{He}_{2}^{+}$ion. Is the ion likely to be stable? What is its bond order?

### 7.14 Molecular Orbital Theory: Other Diatomic Molecules

Now that we've looked at bonding in the $\mathrm{H}_{2}$ molecule, let's move up a level in complexity by looking at the bonding in several second-row diatomic molecules$\mathrm{N}_{2}, \mathrm{O}_{2}$, and $\mathrm{F}_{2}$. The valence bond model developed in Section 7.10 predicts that the nitrogen atoms in $\mathrm{N}_{2}$ are triply bonded and have one lone pair each, that the oxygen atoms in $\mathrm{O}_{2}$ are doubly bonded and have two lone pairs each, and that the fluorine atoms in $\mathrm{F}_{2}$ are singly bonded and have three lone pairs each:
Valence bond theory predicts:
$: N \equiv \mathrm{~N}:$

$1 \sigma$ bond and $1 \pi$ bond

$1 \sigma$ bond

Unfortunately, this simple valence bond picture can't be right because it predicts that the electrons in all three molecules are spin-paired. In other words, electron-dot structures indicate that the occupied atomic orbitals in all three molecules contain two electrons each. It's easy to demonstrate experimentally, however, that the $\mathrm{O}_{2}$ molecule has two electrons that are not spin-paired and that these electrons therefore must be in different, singly occupied orbitals.

Experimental evidence for the electronic structure of $\mathrm{O}_{2}$ rests on the observation that substances with unpaired electrons are attracted by magnetic fields and are thus said to be paramagnetic. The more unpaired electrons a substance has, the stronger the paramagnetic attraction. Substances whose electrons are all spinpaired, by contrast, are weakly repelled by magnetic fields and are said to be diamagnetic. Both $\mathrm{N}_{2}$ and $\mathrm{F}_{2}$ are diamagnetic, just as predicted by their electrondot structures, but $\mathrm{O}_{2}$ is paramagnetic. When liquid $\mathrm{O}_{2}$ is poured over the poles of a strong magnet, the $\mathrm{O}_{2}$ sticks to the poles, as shown in Figure 7.17.


FIGURE 7.17 Why does liquid $\mathrm{O}_{2}$ stick to the poles of a magnet?

Why is $\mathrm{O}_{2}$ paramagnetic? Although electron-dot structures and valence bond theory fail in their descriptions, MO theory explains the experimental results nicely. In a molecular orbital description of $\mathrm{N}_{2}, \mathrm{O}_{2}$, and $\mathrm{F}_{2}$, two atoms come together and their valence-shell atomic orbitals interact to form molecular orbitals. Four orbital interactions occur, leading to the formation of four bonding MOs and four antibonding MOs, whose relative energies are shown in Figure 7.18. (Note that the relative energies of the $\sigma_{2 p}$ and $\pi_{2 p}$ orbitals in $\mathrm{N}_{2}$ are different from those in $\mathrm{O}_{2}$ and $\mathrm{F}_{2}$.)

Albert Haim，＂The Relative Energies of Molecular Orbitals for Second－Row Homonuclear Diatomic Molecules；The Effect of s－p Mixing，＂J．Chem．Educ．，Vol．68， 1991，737－738．

FIGURE 7.19 Formation of（a）$\sigma_{2 p}$ and $\sigma^{*}{ }_{2 p}$ MOs by head－on interaction of two $p$ atomic orbitals，and（b）$\pi_{2 p}$ and $\pi^{*}{ }_{2 p}$ MOs by sideways interac－ tion．The bonding MOs result from interaction of lobes with like phase，while antibonding MOs result from interaction of lobes of opposite phase．In each case，the bonding MO concen－ trates electron density between atomic nuclei，whereas the antibonding MO has a node between nuclei． 1991，737－738


When appropriate numbers of electrons are added to occupy the molecular orbitals, the results shown in Figure 7.20 are obtained. Both $\mathrm{N}_{2}$ and $\mathrm{F}_{2}$ have all their electrons spin-paired, but $\mathrm{O}_{2}$ has two unpaired electrons in the degenerate $\pi^{*} 2 p$ orbitals. Both $\mathrm{N}_{2}$ and $\mathrm{F}_{2}$ are therefore diamagnetic, while $\mathrm{O}_{2}$ is paramagnetic.


A FIGURE 7.20 Molecular orbital diagrams for the second-row diatomic molecules (a) $\mathrm{N}_{2}$, (b) $\mathrm{O}_{2}$, and (c) $\mathrm{F}_{2}$. The $\mathrm{O}_{2}$ molecule has two unpaired electrons in its two degenerate $\pi^{*} 2 p$ orbitals and is therefore paramagnetic.

It should be pointed out that MO diagrams like that in Figure 7.20 require experience and (often) mathematical calculation to obtain. MO theory is therefore less easy to visualize and understand on an intuitive level than valence bond theory.

- PROBLEM 7.27 The $\mathrm{B}_{2}$ and $\mathrm{C}_{2}$ molecules have MO diagrams similar to that of $\mathrm{N}_{2}$ in Figure 7.18a. What MOs are occupied in $\mathrm{B}_{2}$ and $\mathrm{C}_{2}$, and what is the bond order in each? Would you expect either of these substances to be paramagnetic?


### 7.15 Combining Valence Bond Theory and Molecular Orbital Theory

Whenever two different theories are used to explain the same concept, the question comes up: Which theory is better? This question isn't easy to answer because it depends on what is meant by "better." Valence bond theory is better because of its simplicity, but MO theory is better because of its accuracy. Best of all, though, is a blend of the two theories that combines the strengths of both.

Valence bond theory has two main problems: (1) For molecules such as $\mathrm{O}_{2}$, valence bond theory makes an incorrect prediction about electronic structure. (2) For molecules such as $\mathrm{O}_{3}$, no single structure is adequate and the concept of resonance involving two or more structures must be added (Section 7.7). The first problem occurs rarely, but the second is much more common. To better deal with resonance, chemists often use a combination of bonding theories in which the $\sigma$ bonds in a given molecule are described by valence bond theory and $\pi$ bonds in the same molecule are described by MO theory.

Take ozone, for instance. Valence bond theory says that ozone is a resonance hybrid of two equivalent structures, both of which have two $\mathrm{O}-\mathrm{O} \sigma$ bonds and one $\mathrm{O}=\mathrm{O} \pi$ bond (Section 7.7). One structure has a lone pair of electrons in the $p$ orbital on the left-hand oxygen atom and a $\pi$ bond to the right-hand oxygen. The other structure has a lone pair of electrons in the $p$ orbital on the right-hand
oxygen and a $\pi$ bond to the left-hand oxygen. The actual structure of $\mathrm{O}_{3}$ is an average of the two resonance forms in which four electrons occupy the entire region encompassed by the overlapping set of three $p$ orbitals. The only difference between the resonance structures is in the placement of $p$ electrons. The atoms themselves are in the same positions in both, and the geometries are the same in both (Figure 7.21).

FIGURE 7.21 The ozone molecule is a hybrid of two resonance forms that differ only in the location of $p$ electrons. The nuclei and the $\sigma$-bond electrons are in the same position in both resonance structures.
-


Valence bond theory thus gives a good description of the $\mathrm{O}-\mathrm{O} \sigma$ bonds but a poor description of the $\pi$ bonding among $p$ atomic orbitals, whose four electrons are spread out, or delocalized, over the molecule. Yet this is exactly what MO theory does best-describe bonds in which electrons are delocalized over a molecule. Thus, a combination of valence bond theory and MO theory is used. The $\sigma$ bonds are best described in valence bond terminology as being localized between pairs of atoms, and the $\pi$ electrons are best described by MO theory as being delocalized over the entire molecule.


- PROBLEM 7.28 Draw two resonance structures for the formate ion, $\mathrm{HCO}_{2}^{-}$, and sketch a $\pi$ molecular orbital showing how the $\pi$ electrons are delocalized over both oxygen atoms.


## Interlude Molecular Shape, Handedness, and Drugs

 handed glove with a glove. not into a left-handed glove.

Why does a right glove fit only on your right hand and not on your left hand? Why do the threads on a lightbulb twist only in one direction so that you have to turn the bulb clockwise to screw it in? The reason has to do with the shapes of the glove and the lightbulb threads and the fact that both have a handedness to them. When the righthanded glove is held up to a mirror, the reflected image looks like a lefthanded glove. (Try it.) When the lightbulb with clockwise threads is reflected in a mirror, the threads in the mirror image twist in a counterclockwise direction.

Molecules too can have shapes that give them a handedness and can thus exist in mirror-image forms, one right-handed and one lefthanded. Take, for example, the main classes of biomolecules found in living organisms: carbohydrates (sugars), proteins, fats, and nucleic acids. These and most other biomolecules are handed, and usually only one of the two possible mirror-image forms occurs naturally in a given organism. The other form can often be made in the laboratory but does not occur naturally.

The biological consequences of molecular shape can be dramatic. Look at the structures of dextromethorphan and levomethorphan, for instance. (The Latin prefixes dextro- and levo- mean "right" and "left," respectively.) Dextromethorphan is a common cough suppressant found in many over-the-counter cold medicines, but its mirror-image, levomethorphan, is a powerful narcotic pain-reliever similar in its effects to morphine. The two substances are chemically identical except for their shapes, yet their biological properties are completely different.


Levomethorphan (a narcotic analgesic)


Dextromethorphan (a cough suppressant)

A The gray spheres in these structures represent carbon atoms, the ivory spheres represent hydrogen, the red spheres represent oxygen, and the blue spheres represent nitrogen.

Two plants both produce carvone, but the mint leaves yield the "left-handed" form, while the caraway seeds yield the "right-handed" form.

As another example of the effects of shape and molecular handedness, look at the substance called carvone. Left-handed carvone occurs in mint plants and has the characteristic odor of spearmint, while right-handed carvone occurs in several herbs and has the odor of caraway seeds. Again, the two structures are the same except for their shapes, yet they have entirely different odors.


Why do different mirror-image forms of molecules have different biological properties? The answer goes back to the question about why a right-handed glove fits only the right hand: A right hand in a right-handed glove is a perfect match because the two shapes are complementary. Putting the right hand into a lefthanded glove produces a mismatch because the two shapes are not complementary. In the same way, handed molecules such as dextromethorphan and carvone have specific shapes that match only complementary-shaped receptor sites in the body. The mirror-image forms of the molecules can't fit into the receptor sites and thus don't elicit the same biological response.

Precise molecular shape is of crucial importance to every living organism. Almost every chemical interaction in living systems is governed by complementarity between handed molecules and their glovelike receptors.

- PROBLEM 7.29 Why is molecular shape so important in biological chemistry?
- KEY CONCEPT PROBLEM 7.30 One of the following two molecules has a handedness to it and can exist in two mirror-image forms; the other does not. Which is which? Why?

(a)

(b)

A covalent bond results from the sharing of electrons between atoms. Every covalent bond has a specific bond length that leads to optimum stability and a specific bond dissociation energy that describes the strength of the bond. Energy is released when a bond is formed, and energy is absorbed when a bond is broken. As a general rule, a main-group atom will share as many of its valence-shell electrons as possible, either until it has no more to share or until it reaches an octet. Atoms in the third and lower rows of the periodic table can expand their valence shells beyond the normal octet by using $d$ orbitals.

An electron-dot structure represents an atom's valence electrons by dots and shows the two electrons in a single bond as a pair of dots shared between atoms or as a single line. In the same way, a double bond is represented as four dots or two lines between atoms, and a triple bond is represented as six dots or three lines between atoms. Occasionally, a molecule can be represented by more than one electron-dot structure. In such cases, no single structure is adequate by itself. The actual electronic structure of the molecule is a resonance hybrid of the different individual structures.

In a bond between dissimilar atoms, such as that in HCl , one atom often attracts the bonding electrons more strongly than the other, giving rise to a polar covalent bond. Bond polarity is due to differences in electronegativity, the ability of an atom in a molecule to attract shared electrons. Electronegativity increases from left to right across a row and generally decreases from top to bottom in a group of the periodic table.

Molecular shape can often be predicted by the valenceshell electron-pair repulsion (VSEPR) model, which treats
the electrons around atoms as charge clouds that repel one another and therefore orient themselves as far away from one another as possible. Atoms with two charge clouds adopt a linear arrangement of charge clouds, atoms with three charge clouds adopt a trigonal planar arrangement, and atoms with four charge clouds adopt a tetrahedral arrangement. Similarly, atoms with five charge clouds are trigonal bipyramidal, and atoms with six charge clouds are octahedral.

According to valence bond theory, covalent bond formation occurs by the overlap of singly occupied atomic orbitals, either head-on along the internuclear axis to form a $\boldsymbol{\sigma}$ bond or sideways above and below the internuclear axis to form a $\pi$ bond. The observed geometry of covalent bonding is described by assuming that $s, p$, and $d$ atomic orbitals combine to generate hybrid orbitals, which are strongly oriented in specific directions: $s p$ hybrid orbitals have linear geometry, $s p^{2}$ hybrid orbitals have trigonal planar geometry, $s p^{3}$ hybrid orbitals have tetrahedral geometry, $s p^{3} d$ hybrid orbitals have trigonal bipyramidal geometry, and $s p^{3} d^{2}$ hybrid orbitals have octahedral geometry.

Molecular orbital theory sometimes gives a more accurate picture of electronic structure than the valence bond model. A molecular orbital is a wave function whose square gives the probability of finding an electron in a given region of space in a molecule. Combination of two atomic orbitals gives two molecular orbitals, a bonding MO that is lower in energy than the starting atomic orbitals and an antibonding MO that is higher in energy than the starting atomic orbitals. Molecular orbital theory is particularly useful for describing delocalized $\pi$ bonding in molecules.

## Key Words

antibonding molecular orbital 279
bond angle 264
bond dissociation energy (D) 245
bond length 245
bond order 251
bonding molecular orbital 279
bonding pair 250
coordinate covalent bond 252
covalent bond 244
diamagnetic 281
double bond 251
electron-dot structure 249
electronegativity (EN) 248
formal charge 261
hybrid atomic orbital 272
lone pair 250
molecular orbital 279
molecular orbital (MO)
theory 278
paramagnetic 281
pi ( $\boldsymbol{\pi}$ ) bond 274
polar covalent bond 247
resonance hybrid 259
sigma ( $\boldsymbol{\sigma}$ ) bond 271
single bond 251
$s p$ hybrid orbital 275
$s p^{2}$ hybrid orbital 274
$s^{3}$ hybrid orbital 272
$s p^{3} d$ hybrid orbital 276
$s p^{3} d^{2}$ hybrid orbital 277
triple bond 251
valence bond theory 271
valence-shell electronpair repulsion (VSEPR) model 264

## Key Concept Summary

- 



## Understanding Key Concepts

Problems 7.1-7.30 appear within the chapter. think is which?

(a) of the following molecular models?

(a)

(c) "hidden" atom in some cases.)

(a)
7.31 Two electrostatic potential maps, one of methyllithium $\left(\mathrm{CH}_{3} \mathrm{Li}\right)$ and one of chloromethane $\left(\mathrm{CH}_{3} \mathrm{Cl}\right)$ are shown. Based on their polarity patterns, which do you

(b)
7.32 What is the geometry around the central atom in each

(b)

(d)
7.33 What is the geometry around the central atom in each of the following molecular models? (There may be a

(c)
(b)

7.34 Three of the following molecular models have a tetrahedral central atom, and one does not. Which is the odd one? (There may be a "hidden" atom in some cases.)

(a)

(b)

(c)

(d)
7.35 Identify each of the following sets of hybrid orbitals:


(c)
7.36 The following ball-and-stick molecular model is a representation of acetaminophen, the active ingredient in such over-the-counter headache remedies as Tylenol (red $=\mathrm{O}$, gray $=\mathrm{C}$, blue $=\mathrm{N}$, ivory $=\mathrm{H}$ ):
(a) What is the molecular formula of acetaminophen?
(b) What is the geometry around each carbon and nitrogen? (The lines between atoms indicate connections only, not whether the bonds are single, double, or triple.)
(c) What is the hybridization of each carbon and nitrogen?

7.37 The following ball-and-stick molecular model is a representation of thalidomide, a drug that causes birth defects when taken by expectant mothers but is valuable for its use against leprosy. The lines indicate only the connections between atoms, not whether the bonds are single, double, or triple (red $=\mathrm{O}$, gray $=\mathrm{C}$, blue $=\mathrm{N}$, ivory $=\mathrm{H}$ ).
(a) What is the molecular formula of thalidomide?
(b) Indicate the positions of the multiple bonds in thalidomide.
(c) What is the geometry around each carbon and each nitrogen?


## Additional Problems

## Electronegativity and Polar Covalent Bonds

7.38 What general trends in electronegativity occur in the periodic table?
7.39 Predict the electronegativity of the undiscovered element with $Z=119$.
7.40 Order the following elements according to increasing electronegativity: $\mathrm{Li}, \mathrm{Br}, \mathrm{Pb}, \mathrm{K}, \mathrm{Mg}, \mathrm{C}$.
7.41 Order the following elements according to decreasing electronegativity: $\mathrm{C}, \mathrm{Ca}, \mathrm{Cs}, \mathrm{Cl}, \mathrm{Cu}$.
7.42 Which of the following substances are largely ionic and which are covalent?
(a) HF
(b) HI
(c) $\mathrm{PdCl}_{2}$
(d) $\mathrm{BBr}_{3}$
(e) NaOH
(f) $\mathrm{CH}_{3} \mathrm{Li}$
7.43 Use the electronegativity data in Figure 7.4 to predict which bond in each of the following pairs is more polar:
(a) $\mathrm{C}-\mathrm{H}$ or $\mathrm{C}-\mathrm{Cl}$
(b) $\mathrm{Si}-\mathrm{Li}$ or $\mathrm{Si}-\mathrm{Cl}$
(c) $\mathrm{N}-\mathrm{Cl}$ or $\mathrm{N}-\mathrm{Mg}$
7.44 Show the direction of polarity for each of the bonds in Problem 7.43 , using the $\delta+/ \delta-$ notation.
7.45 Show the direction of polarity for each of the covalent bonds in Problem 7.42, using the $\delta+/ \delta-$ notation.

## Electron-Dot Structures and Resonance

7.46 What is the octet rule, and why does it apply primarily to main-group elements, not to transition metals?
7.47 Which of the following substances contains an atom that does not follow the octet rule?
(a) $\mathrm{AlCl}_{3}$
(b) $\mathrm{PCl}_{3}$
(c) $\mathrm{PCl}_{5}$
(d) $\mathrm{SiCl}_{4}$
7.48 Draw electron-dot structures for the following molecules or ions:
(a) $\mathrm{CBr}_{4}$
(b) $\mathrm{NCl}_{3}$
(c) $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}$
(d) $\mathrm{BF}_{4}^{-}$
(e) $\mathrm{O}_{2}{ }^{2-}$
(f) $\mathrm{NO}^{+}$
7.49 Draw electron-dot structures for the following molecules, which contain atoms from the third row or lower:
(a) $\mathrm{SbCl}_{3}$
(b) $\mathrm{KrF}_{2}$
(c) $\mathrm{ClO}_{2}$
(d) $\mathrm{PF}_{5}$
(e) $\mathrm{H}_{3} \mathrm{PO}_{4}$
(f) $\mathrm{SeOCl}_{2}$
7.50 Draw as many resonance structures as you can for each of the following molecules or ions:
(a) $\mathrm{HN}_{3}$
(b) $\mathrm{SO}_{3}$
(c) $\mathrm{SCN}^{-}$
7.51 Draw as many resonance structures as you can for the following nitrogen-containing compounds:
(a) $\mathrm{N}_{2} \mathrm{O}$
(b) NO
(c) $\mathrm{NO}_{2}$
(d) $\mathrm{N}_{2} \mathrm{O}_{3}\left(\mathrm{ONNO}_{2}\right)$
7.52 Oxalic acid, $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, is a poisonous substance found in uncooked spinach leaves. If oxalic acid has a $\mathrm{C}-\mathrm{C}$ single bond and no $\mathrm{C}-\mathrm{H}$ bond, draw its electron-dot structure.
7.53 Draw an electron-dot structure for carbon disulfide, $\mathrm{CS}_{2}$. How many double bonds does $\mathrm{CS}_{2}$ have?
7.54 Which of the following pairs of structures represent resonance forms, and which do not?
(a)

(b)

(c)

(d)
 and

7.55 Which of the following pairs of structures represent resonance forms, and which do not?
(a)

(b)

(c)

7.56 Identify the third-row elements, $X$, that form the following ions:
(a)

(b)

7.57 Identify the fourth-row elements, X , that form the following compounds:
(a) $\ddot{\mathrm{O}}=\ddot{\mathrm{X}}-\ddot{\mathrm{O}}$ :
(b) $\quad \stackrel{\ddot{\mathrm{F}}}{\bullet} \quad \stackrel{\ddot{\mathrm{x}}}{ }, \stackrel{\ddot{\mathrm{F}}}{ }$
7.58 Write electron-dot structures for molecules with the following connections:
(a)

(b)

7.59 Write electron-dot structures for molecules with the following connections:
(a)

(b)


## Formal Charges

7.60 Draw an electron-dot structure for carbon monoxide, CO, and assign formal charges to both atoms.
7.61 Assign formal charges to the atoms in the following structures:
(a)

(b)

(c)

7.62 Assign formal charges to the atoms in the following resonance forms of $\mathrm{ClO}_{2}{ }^{-}$:

7.63 Assign formal charges to the atoms in the following resonance forms of $\mathrm{H}_{2} \mathrm{SO}_{3}$ :

7.64 Assign formal charges to the atoms in the following structures. Which of the two do you think is the more important contributor to the resonance hybrid?
(a)

(b)

7.65 Calculate formal charges for the C and O atoms in the following two resonance structures. Which structure do you think is the more important contributor to the resonance hybrid? Explain.


## The VSEPR Model

7.66 What geometric arrangement of charge clouds do you expect for atoms that have the following number of charge clouds?
(a) 3
(b) 5
(c) 2
(d) 6
7.67 What shape do you expect for molecules that meet the following descriptions?
(a) A central atom with two lone pairs and three bonds to other atoms
(b) A central atom with two lone pairs and two bonds to other atoms
(c) A central atom with two lone pairs and four bonds to other atoms
7.68 How many charge clouds are there around the central atom in molecules that have the following geometry?
(a) Tetrahedral
(b) Octahedral
(c) Bent
(d) Linear
(e) Square pyramidal
(f) Trigonal pyramidal
7.69 How many charge clouds are there around the central atom in molecules that have the following geometry?
(a) Seesaw
(b) Square planar
(c) Trigonal bipyramidal
(d) T-shaped
(e) Trigonal planar
(f) Linear
7.70 What shape do you expect for each of the following molecules?
(a) $\mathrm{H}_{2} \mathrm{Se}$
(b) $\mathrm{TiCl}_{4}$
(c) $\mathrm{O}_{3}$
(d) $\mathrm{GaH}_{3}$
7.71 What shape do you expect for each of the following molecules?
(a) $\mathrm{XeO}_{4}$
(b) $\mathrm{SO}_{2} \mathrm{Cl}_{2}$
(c) $\mathrm{OsO}_{4}$
(d) $\mathrm{SeO}_{2}$
7.72 What shape do you expect for each of the following molecules or ions?
(a) $\mathrm{SbF}_{5}$
(b) $\mathrm{IF}_{4}{ }^{+}$
(c) $\mathrm{SeO}_{3}{ }^{2-}$
(d) $\mathrm{CrO}_{4}{ }^{2-}$
7.73 Predict the shape of each of the following ions:
(a) $\mathrm{NO}_{3}{ }^{-}$
(b) $\mathrm{NO}_{2}{ }^{+}$
(c) $\mathrm{NO}_{2}^{-}$
7.74 What shape do you expect for each of the following anions?
(a) $\mathrm{PO}_{4}{ }^{3-}$
(b) $\mathrm{MnO}_{4}^{-}$
(c) $\mathrm{SO}_{4}{ }^{2-}$
(d) $\mathrm{SO}_{3}{ }^{2-}$
(e) $\mathrm{ClO}_{4}^{-}$
(f) $\mathrm{SCN}^{-}$
7.75 What shape do you expect for each of the following cations?
(a) $\mathrm{XeF}_{3}{ }^{+}$
(b) $\mathrm{SF}_{3}{ }^{+}$
(c) $\mathrm{ClF}_{2}{ }^{+}$
(d) $\mathrm{CH}_{3}{ }^{+}$
7.76 What bond angles do you expect for each of the following?
(a) The F-S-F angle in $\mathrm{SF}_{2}$
(b) The $\mathrm{H}-\mathrm{N}-\mathrm{N}$ angle in $\mathrm{N}_{2} \mathrm{H}_{2}$
(c) The $\mathrm{F}-\mathrm{Kr}-\mathrm{F}$ angle in $\mathrm{KrF}_{4}$
(d) The $\mathrm{Cl}-\mathrm{N}-\mathrm{O}$ angle in NOCl
7.77 What bond angles do you expect for each of the following?
(a) The $\mathrm{Cl}-\mathrm{P}-\mathrm{Cl}$ angle in $\mathrm{PCl}_{6}{ }^{-}$
(b) The $\mathrm{Cl}-\mathrm{I}-\mathrm{Cl}$ angle in $\mathrm{ICl}_{2}{ }^{-}$
(c) The $\mathrm{O}-\mathrm{S}-\mathrm{O}$ angle in $\mathrm{SO}_{4}{ }^{2-}$
(d) The $\mathrm{O}-\mathrm{B}-\mathrm{O}$ angle in $\mathrm{BO}_{3}{ }^{3-}$
7.78 Acrylonitrile is used as the starting material for manufacturing acrylic fibers. Predict values for all bond angles in acrylonitrile.


Acrylonitrile
7.79 Predict values for all bond angles in dimethyl sulfoxide, a powerful solvent used in veterinary medicine to treat inflammation.


Dimethyl sulfoxide
7.80 Explain why cyclohexane, a substance that contains a six-membered ring of carbon atoms, is not flat but instead has a puckered, nonplanar shape. Predict the values of the $\mathrm{C}-\mathrm{C}-\mathrm{C}$ bond angles.



Side view
Cyclohexane
7.81 Like cyclohexane (Problem 7.80), benzene also contains a six-membered ring of carbon atoms, but it is flat rather than puckered. Explain, and predict the values of the $\mathrm{C}-\mathrm{C}-\mathrm{C}$ bond angles.


## Hybrid Orbitals and Molecular Orbital Theory

7.82 What is the difference in spatial distribution between electrons in a $\pi$ bond and electrons in a $\sigma$ bond?
7.83 What is the difference in spatial distribution between electrons in a bonding MO and electrons in an antibonding MO?
7.84 What hybridization do you expect for atoms that have the following numbers of charge clouds?
(a) 2
(b) 5
(c) 6
(d) 4
7.85 What spatial arrangement of charge clouds corresponds to each of the following kinds of hybridization?
(a) $s p^{3}$
(b) $s p^{3} d^{2}$
(c) $s p$
7.86 What hybridization do you expect for the central atom in a molecule that has the following geometry?
(a) Tetrahedral
(b) Octahedral
(c) Bent
(d) Linear
(e) Square pyramidal
7.87 What hybridization do you expect for the central atom in a molecule that has the following geometry?
(a) Seesaw
(b) Square planar
(c) Trigonal bipyramidal
(d) T-shaped
(e) Trigonal planar
7.88 What hybridization would you expect for the indicated atom in each of the following?
(a) $\mathrm{H}_{2} \mathrm{C}=\mathrm{O}$
(b) $\mathrm{BH}_{4}^{-}$
(c) $\mathrm{XeOF}_{4}$
(d) $\mathrm{SO}_{3}$
7.89 What hybridization would you expect for the indicated atom in each of the following ions?
(a) $\mathrm{BrO}_{3}{ }^{-}$
(b) $\mathrm{HCO}_{2}^{-}$
(c) $\mathrm{CH}_{3}{ }^{+}$
(d) $\mathrm{CH}_{3}{ }^{-}$
7.90 Urea is excreted as a waste product in animal urine. What is the hybridization of the C and N atoms in urea, and what are the approximate values of the various bond angles?

7.91 The atoms in the amino acid glycine are connected as shown:

(a) Draw an electron-dot structure for glycine.
(b) Predict approximate values for the $\mathrm{H}^{-} \mathrm{C}-\mathrm{H}, \mathrm{O}-\mathrm{C}-\mathrm{O}$, and $\mathrm{H}-\mathrm{N}-\mathrm{H}$ bond angles.
(c) Which hybrid orbitals are used by the C and N atoms?
7.92 Use the MO diagram in Figure 7.18b to describe the bonding in $\mathrm{O}_{2}{ }^{+}, \mathrm{O}_{2}$, and $\mathrm{O}_{2}{ }^{-}$. Which of the three should be stable? What is the bond order of each? Which contain unpaired electrons?
7.93 Use the MO diagram in Figure 7.18a to describe the bonding in $\mathrm{N}_{2}{ }^{+}, \mathrm{N}_{2}$, and $\mathrm{N}_{2}{ }^{-}$. Which of the three should be stable? What is the bond order of each? Which contain unpaired electrons?
7.94 Make a sketch showing the location and geometry of the $p$ orbitals in the allyl cation. Describe the bonding in this cation, using a localized valence bond model for $\sigma$ bonding and a delocalized MO model for $\pi$ bonding.

7.95 Make a sketch showing the location and geometry of the $p$ orbitals in the nitrite ion, $\mathrm{NO}_{2}{ }^{-}$. Describe the bonding in this ion, using a localized valence bond model for $\sigma$ bonding and a delocalized MO model for $\pi$ bonding.

## General Problems

7.96 Vitamin C (ascorbic acid) has the following connections among atoms. Complete the Lewis electron-dot structure for vitamin C, and identify any multiple bonds.

7.97 Tell the hybridization of each carbon atom in ascorbic acid (Problem 7.96).
7.98 The odor of cinnamon oil is due to cinnamaldehyde, $\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}$. What is the hybridization of each carbon atom in cinnamaldehyde? How many $\sigma$ bonds and how many $\pi$ bonds does cinnamaldehyde have?

7.99 Draw three resonance structures for sulfur tetroxide, $\mathrm{SO}_{4}$, whose connections are shown below. (This is a neutral molecule; it is not sulfate ion.) Assign formal charges to the atoms in each structure.


Sulfur tetroxide
7.100 Draw two resonance structures for methyl isocyanate, $\mathrm{CH}_{3} \mathrm{NCO}$, a toxic gas that was responsible for the deaths of at least 3000 people when it was accidentally released into the atmosphere in December 1984 in Bhopal, India. Assign formal charges to the atoms in each resonance structure.
7.101 There are two possible shapes for diimide, $\mathrm{H}-\mathrm{N}=\mathrm{N}-\mathrm{H}$. Draw both, and tell if they are resonance forms.
7.102 Boron trifluoride reacts with dimethyl ether to form a compound with a coordinate covalent bond:

(a) Assign formal charges to the B and O atoms in both the reactants and product.
(b) Describe the geometry and hybridization of the B and O atoms in both reactants and product.
7.103 What is the hybridization of the B and N atoms in borazine, what are the values of the $\mathrm{B}-\mathrm{N}-\mathrm{B}$ and $\mathrm{N}-\mathrm{B}-\mathrm{N}$ bond angles, and what is the overall shape of the molecule?


Borazine
7.104 Benzyne, $\mathrm{C}_{6} \mathrm{H}_{4}$, is a highly energetic and reactive molecule. What hybridization do you expect for the two triply bonded carbon atoms? What are the "theoretical" values for the $\mathrm{C}-\mathrm{C} \equiv \mathrm{C}$ bond angles? Why do you suppose benzyne is so reactive?


Benzyne
7.105 Propose structures for molecules that meet the following descriptions:
(a) Contains a C atom that has two $\pi$ bonds and two $\sigma$ bonds
(b) Contains an N atom that has one $\pi$ bond and two $\sigma$ bonds
(c) Contains an S atom that has a coordinate covalent bond
7.106 Write an electron-dot structure for chloral hydrate, also known in detective novels as "knockout drops."


Chloral hydrate
7.107 Draw a molecular orbital diagram for $\mathrm{Li}_{2}$. What is the bond order? Is the molecule likely to be stable? Explain.
7.108 Calcium carbide, $\mathrm{CaC}_{2}$, reacts with water to produce acetylene, $\mathrm{C}_{2} \mathrm{H}_{2}$, and is sometimes used as a convenient source of that substance. Use the MO diagram in Figure 7.18a to describe the bonding in the carbide anion, $\mathrm{C}_{2}{ }^{2-}$. What is its bond order?
7.109 There are three substances with the formula $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$. Draw electron-dot structures for all, and explain how and why they differ.
7.110 The overall energy change during a chemical reaction can be calculated from a knowledge of bond dissociation energies using the following relationship:
Energy change $=D$ (Bonds broken) $-D$ (Bonds formed) Use the data in Table 7.1 to calculate an energy change for the reaction of methane with chlorine.

$$
\mathrm{CH}_{4}(g)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{CH}_{3} \mathrm{Cl}(g)+\mathrm{HCl}(g)
$$

7.111 The following structure is a computer-drawn representation of aspartame, $\mathrm{C}_{14} \mathrm{H}_{18} \mathrm{~N}_{2} \mathrm{O}_{5}$, known commercially as NutraSweet. Only the connections between atoms are shown; multiple bonds are not indicated. Complete the structure by indicating the positions of the multiple bonds.

7.112 The $\mathrm{N}_{2} \mathrm{O}_{5}$ molecule has six $\mathrm{N}-\mathrm{O} \sigma$ bonds and two $\mathrm{N}-\mathrm{O} \pi$ bonds, but has no $\mathrm{N}-\mathrm{N}$ bonds and no $\mathrm{O}-\mathrm{O}$ bonds. Draw eight resonance structures for $\mathrm{N}_{2} \mathrm{O}_{5}$, and assign formal charges to the atoms in each. Which resonance structures make the more important contributions to the resonance hybrid?
7.113 In the cyanate ion, $\mathrm{OCN}^{-}$, carbon is the central atom.
(a) Draw as many resonance structures as you can for $\mathrm{OCN}^{-}$, and assign formal charges to the atoms in each.
(b) Which resonance structure makes the greatest contribution to the resonance hybrid? Which makes the least contribution? Explain.
(c) Is $\mathrm{OCN}^{-}$linear or bent? Explain.
(d) Which hybrid orbitals are used by the C atom, and how many $\pi$ bonds does the C atom form?
7.114 Aspirin has the following connections among atoms. Complete the electron-dot structure for aspirin, tell how many $\sigma$ bonds and how many $\pi$ bonds the molecule contains, and tell the hybridization of each carbon atom.

7.115 The cation $[\mathrm{H}-\mathrm{C}-\mathrm{N}-\mathrm{Xe}-\mathrm{F}]^{+}$is entirely linear. Draw an electron-dot structure consistent with that geometry, and tell the hybridization of each of the three central atoms C, N, and Xe.
7.116 At high temperatures, sulfur vapor is predominantly in the form of $\mathrm{S}_{2}(g)$ molecules.
(a) Assuming that the molecular orbitals for third-row diatomic molecules are analogous to those for second-row molecules, construct an MO diagram for the valence orbitals of $\mathrm{S}_{2}(g)$.
(b) Is $\mathrm{S}_{2}$ likely to be paramagnetic or diamagnetic?
(c) What is the bond order of $\mathrm{S}_{2}(g)$ ?
(d) When two electrons are added to $\mathrm{S}_{2}$, the disulfide ion $\mathrm{S}_{2}{ }^{2-}$ is formed. Is the bond length in $\mathrm{S}_{2}{ }^{2-}$ likely to be shorter or longer than the bond length in $\mathrm{S}_{2}$ ? Explain.
7.117 Carbon monoxide is produced by incomplete combustion of fossil fuels.
(a) Give the electron configuration for the valence molecular orbitals of CO. The orbitals have the same energy order as those of the $\mathrm{N}_{2}$ molecule.
(b) Do you expect CO to be paramagnetic or diamagnetic?
(c) What is the bond order of CO ? Does this match the bond order predicted by the electron-dot structure?
(d) CO can react with $\mathrm{OH}^{-}$to form the formate ion, $\mathrm{HCO}_{2}{ }^{-}$. Draw an electron-dot structure for the formate ion, and give any resonance structures if appropriate.
7.118 Draw an electron-dot structure for each of the following molecules, and predict the molecular geometry and hybridization of every nonterminal atom.
(a) $\mathrm{F}_{3} \mathrm{~S}-\mathrm{S}-\mathrm{F}$
(b) $\mathrm{CH}_{3}-\mathrm{C} \equiv \mathrm{C}-\mathrm{CO}_{2}{ }^{-}$
7.119 The ion $\mathrm{I}_{5}{ }^{-}$is shaped like a big "V." Draw an electrondot structure consistent with this overall geometry. What is the hybridization of each nonterminal iodine atom in this structure? How does this hybridization give rise to the observed geometry?

## Multi-Concept Problems

7.120 The neutral OH molecule has been implicated in certain ozone-destroying processes that take place in the upper atmosphere.
(a) Draw electron-dot structures for the OH molecule and the $\mathrm{OH}^{-}$ion.
(b) Electron affinity can be defined for molecules just as it is defined for single atoms. Assuming that the electron added to OH is localized in a single atomic orbital on one atom, identify which atom is accepting the electron, and give the $n$ and $l$ quantum numbers of the atomic orbital.
(c) The electron affinity of OH is similar to but slightly more negative than that of O atoms. Explain.
7.121 Suppose that the Pauli exclusion principle were somehow changed to allow three electrons per orbital rather than two.
(a) Instead of an octet, how many outer-shell electrons would be needed for a noble gas electron configuration?
(b) How many electrons would be shared in a covalent bond?
(c) Give the electron configuration, and draw an electron-dot structure for element X with $\mathrm{Z}=12$.
(d) Draw an electron-dot structure for the molecule $X_{2}$.
(e) Assuming that the molecular orbital diagram in Figure 7.20b is valid, tell the bond order for the $X_{2}$ molecule.
7.122 The dichromate ion, $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$, has neither $\mathrm{Cr}-\mathrm{Cr}$ nor $\mathrm{O}-\mathrm{O}$ bonds.
(a) Taking both $4 s$ and $3 d$ electrons into account, draw an electron-dot structure that minimizes the formal charges on the atoms.
(b) How many outer-shell electrons does each Cr atom have in your electron-dot structure? What is the likely geometry around the Cr atoms?
7.123 A compound with the formula $\mathrm{XOCl}_{2}$, reacts violently with water, yielding HCl and the diprotic acid $\mathrm{H}_{2} \mathrm{XO}_{3}$. When 0.350 g of $\mathrm{XOCl}_{2}$ was added to 50.0 mL of water and the resultant solution was titrated, 96.1 mL of 0.1225 M NaOH was required to react with all the acid.
(a) Write a balanced equation for the reaction of $\mathrm{XOCl}_{2}$ with $\mathrm{H}_{2} \mathrm{O}$.
(b) What are the atomic mass and identity of element $X$ ?
(c) Draw an electron-dot structure for $\mathrm{XOCl}_{2}$.
(d) What is the shape of $\mathrm{XOCl}_{2}$ ?
7.124 Just as individual bonds in a molecule are often polar, molecules as a whole are also often polar because of the net sum of individual bond polarities. There are three possible structures for substances with the formula $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$, two of which are polar overall and one of which is not.
(a) Draw the three possible electron-dot structures for $\mathrm{C}_{2} \mathrm{H}_{2} \mathrm{Cl}_{2}$, predict an overall shape for each, and explain how they differ.
(b) Which of the three structures is nonpolar and which two are polar? Explain.
(c) Two of the three structures can be interconverted by a process called cis-trans isomerization, in which rotation around the central carbon-carbon bond takes place when the molecules are irradiated with ultraviolet light. If light with a wavelength of approximately 200 nm is required for isomerization, how much energy in $\mathrm{kJ} / \mathrm{mol}$ is involved?
(d) Sketch the orbitals involved in the central carboncarbon bond, and explain why so much energy is necessary for bond rotation to occur.

## eMedia Problems

7.125 Use the Interactive Periodic Table (eChapter 7.4) to determine the trend in electronegativity as you move across a row in the periodic table. What element would you expect to have the largest electronegativity? What factors contribute to the trends in electronegativity?
7.126 The Polarity activity in eChapter 7.4 displays the resultant dipole when the terminal and/or central atoms in a molecule are changed. Use the activity to determine the conditions under which a molecule will be nonpolar. What conditions lead to the strongest dipole?
7.127 eChapter 7.6 identifies a five-step general method for drawing electron-dot structures. As you work through Electron Dot Structures II in eChapter 7.6, write down the results of each of the five steps in finding the elec-tron-dot structure for each of the molecules.
7.128 While watching the Formal Charges movie in eChapter 7.8, write down the calculations of the formal charges in $\mathrm{HCl}, \mathrm{HCN}, \mathrm{HNC}$, and $\mathrm{NO}_{2}$. Use similar calculations to determine the most stable electron-dot structure for $\mathrm{CO}_{2}$.
7.129 The VSEPR movie (eChapter 7.9) illustrates the arrangements of charge clouds around a central atom.
(a) Which of the arrangements does not have all equal bond angles?
(b) In which of the arrangements are all positions not equivalent with regard to the placement of a single lone pair?
(c) In which (if any) of the arrangements are all positions equivalent with regard to the placement of a single lone pair, but not equivalent with regard to the placement of a second lone pair?
7.130 Work through the Molecular Orbital Theory tutorial in eChapter 7.13, which illustrates the formation of sigma molecular orbitals from $s$ atomic orbitals. $p$ Orbitals will also form sigma orbitals when they overlap head-on. Follow the examples given for the $s$ orbitals and predict how $p$ orbitals will form sigma molecular orbitals.

## Chapter

## Thermochemistry: Chemical Energy

## Why do chemical reactions occur?

As mentioned briefly in the previous chapter,
the answer involves stability. For a reaction to take place spontaneously, the final products of the reaction must be more stable than the starting reactants.
But what is "stability," and what does it mean to say that one substance is more stable than another? The most important factor in determining the stability of a substance is the amount of energy it contains. Highly energetic substances are generally less stable and more reactive, while less energetic substances are

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- Interlude-Energy from Food
generally more stable and less reactive. We'll explore some different forms of energy in this chapter and look at the subject of thermochemistry-the absorption or release of heat energy that accompanies chemical reactions.


### 8.1 Energy

Energy. The word is familiar but is surprisingly hard to define in simple, nontechnical terms. A good working definition is that energy is the capacity to supply heat or do work:

$$
\text { Energy }=\text { Heat }+ \text { Work }
$$

The water falling over a dam, for instance, contains energy that can be used to turn a turbine and generate electricity. A tank of propane gas contains energy that, when released on burning, can heat a house or camper.

Energy can be classified as either kinetic or potential. Kinetic energy ( $E_{\mathrm{K}}$ ) is the energy of motion. The amount of kinetic energy in a moving object with mass $m$ and velocity $v$ is given by the equation

$$
E_{\mathrm{K}}=\frac{1}{2} m v^{2}
$$

The larger the mass of an object and the larger its velocity, the larger the amount of kinetic energy. Thus, water that has fallen over a dam from a great height has a greater velocity and more kinetic energy than the same amount of water that has fallen only a short distance.

Potential energy ( $E_{\mathrm{P}}$ ), by contrast, is stored energy-perhaps stored in an object because of its height or in a molecule because of its chemical bonds. The water sitting in a reservoir behind the dam contains potential energy because of its height above the stream at the bottom of the dam. When the water is allowed to fall, its potential energy is converted into kinetic energy. Propane and other substances used as fuels contain potential energy in their chemical bonds. When these substances undergo reaction with oxygen during burning, some of this potential energy is released as heat.

The units for energy- $\left(\mathrm{kg} \cdot \mathrm{m}^{2}\right) / \mathrm{s}^{2}$-follow from the expression $E_{\mathrm{K}}=1 / 2 \mathrm{mv}{ }^{2}$. If, for instance, your body has a mass of 50.0 kg (about 110 lb ) and you are riding on a bicycle at a speed of $10.0 \mathrm{~m} / \mathrm{s}$ (about $22 \mathrm{mi} / \mathrm{h}$ ), your kinetic energy is $2500\left(\mathrm{~kg} \cdot \mathrm{~m}^{2}\right) / \mathrm{s}^{2}:$

$$
E_{K}=\frac{1}{2} m v^{2}=\frac{1}{2}(50.0 \mathrm{~kg})\left(10.0 \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}=2500 \frac{\mathrm{~kg} \cdot \mathrm{~m}^{2}}{\mathrm{~s}^{2}}=2500 \mathrm{~J}
$$

The SI energy unit $\left(\mathrm{kg} \cdot \mathrm{m}^{2}\right) / \mathrm{s}^{2}$ is given the name joule (J) after the English physicist James Prescott Joule (1818-1889). The joule is a fairly small amount of energy-it takes roughly $100,000 \mathrm{~J}$ to heat a coffee cup full of water from room temperature to boiling-so kilojoules ( $\mathrm{kJ} \mathrm{)} \mathrm{are} \mathrm{more} \mathrm{frequently} \mathrm{used} \mathrm{in} \mathrm{chemistry}$.

The 75 watt incandescent $>$ bulb in this lamp uses energy at the rate of $75 \mathrm{~J} / \mathrm{s}$. Only about $5 \%$ of that energy appears as light, however; the remainder is given off as heat.


In addition to the SI unit joule, some chemists still use the unit calorie (cal, with a lowercase $c$ ). Originally defined as the amount of energy necessary to raise the temperature of 1 g of water by $1^{\circ} \mathrm{C}$ (specifically, from $14.5^{\circ} \mathrm{C}$ to $15.5^{\circ} \mathrm{C}$ ), one calorie is now defined as exactly 4.184 J .

$$
1 \mathrm{cal}=4.184 \mathrm{~J}(\text { exactly })
$$

Nutritionists also use the somewhat confusing unit Calorie (Cal, with a capital C), which is equal to 1000 calories, or 1 kilocalorie (kcal):

$$
1 \mathrm{Cal}=1000 \mathrm{cal}=1 \mathrm{kcal}=4.184 \mathrm{~kJ}
$$

The energy value, or caloric content, of food is measured in Calories. Thus, the statement that a banana contains 70 Calories means that $70 \mathrm{Cal}(70 \mathrm{kcal}$, or 290 kJ ) of energy is released when the banana is used by the body for fuel.

- PROBLEM 8.1 What is the kinetic energy (in kilojoules) of a 2300 lb car moving at $55 \mathrm{mi} / \mathrm{h}$ ?


### 8.2 Energy Changes and Energy Conservation

Let's pursue a bit further the relationship between potential energy and kinetic energy. According to the conservation of energy law, energy can be neither created nor destroyed; it can only be converted from one form into another.
conservation of energy law Energy cannot be created or destroyed; it can only be converted from one form into another.
To take the example of falling water again, the water in a reservoir has potential energy because of its height above the outlet stream but has no kinetic energy because it isn't moving $(v=0)$. As the water starts to fall over the dam, though, its height and potential energy decrease while its velocity and kinetic energy increase. The total of potential energy plus kinetic energy always remains constant (Figure 8.1). When the water reaches the bottom and dashes against the rocks or drives the turbine of a generator, its kinetic energy is converted to other forms of energy-perhaps into heat that raises the temperature of the water or into electrical energy.


A FIGURE 8.1 Conservation of energy. The total amount of energy contained by the water in a reservoir is constant. (a) At the top of the dam, the energy is potential $\left(E_{\mathrm{P}}\right)$. (b)-(c) As the water falls over the dam, its velocity increases and potential energy is converted into kinetic energy $\left(E_{\mathrm{K}}\right)$. (d) At the bottom of the dam, the kinetic energy gained by the water is largely converted into heat and sound as the water dashes against the rocks.

The conversion of kinetic energy into heat when water falls over a dam and strikes the rocks at the bottom illustrates several other important points about energy. One point is that energy has many forms. Thermal energy, for example, seems different from the kinetic energy of falling water, yet it's really quite similar. Thermal energy is simply the kinetic energy of molecular motion, which we measure by finding the temperature of an object. An object has a low temperature and we perceive it as "cold" if its atoms or molecules are moving slowly. Conversely, an object has a high temperature and we perceive it as "hot" if its atoms or molecules are moving rapidly and are colliding forcefully with a thermometer or other measuring device.

Heat, in turn, is the amount of kinetic energy transferred from one object to another as the result of a temperature difference between them. Rapidly moving molecules in the hotter object collide with more slowly moving molecules in the colder object, transferring kinetic energy and causing the slower-moving molecules to speed up.

Chemical energy is another kind of energy that seems different from that of the water in a reservoir, yet again is really quite similar. Chemical energy is a kind of potential energy in which chemical bonds act as the "storage" medium. Just as water releases its potential energy when it falls to a more stable position, chemicals release their potential energy in the form of heat or light when they undergo reactions and form more stable products. We'll explore this topic shortly.

The kinetic energy of water falling through the penstocks of a dam is used to turn huge turbines and generate electricity.


A second point illustrated by the water falling over a dam involves the conservation of energy law. To keep track of all the energy involved, it's necessary to take into account the entire chain of events that ensue from the falling water: the sound of the crashing water, the heating of the rocks at the bottom of the dam, the driving of turbines and electrical generators, the transmission of electrical power, the appliances powered by the electricity, and so on. Carrying the process to its logical extreme, in fact, it's necessary to take the entire universe into account when keeping track of all the energy in the water because the energy lost in one form always shows up elsewhere in another form. So important is the conservation of energy law that it is also known as the first law of thermodynamics.

### 8.3 Internal Energy and State Functions

When keeping track of the energy changes that occur in a chemical reaction, it's helpful to think of the reaction as separate from the world around it. The substances we focus on in an experiment-the starting reactants and the final prod-ucts-are collectively called the system, while everything else-the reaction flask, the room, the building, and so on-is called the surroundings. If the system were somehow isolated from its surroundings so that no energy transfer could occur between the two, then the total internal energy $(E)$ of the system-the sum of all
the kinetic and potential energies for every molecule or ion in the system-would be conserved and remain constant throughout the reaction. In fact, this assertion is just a restatement of the first law of thermodynamics:
first law of thermodynamics (restated) The total internal energy of an isolated system is constant.
In practice, of course, it's not possible to truly isolate a chemical reaction from its surroundings. In any real situation, the chemicals are in physical contact with the walls of the flask or container, and the container itself is in contact with the surrounding air. What's important, however, is not that the system be isolated but that we be able to measure accurately any energy that enters the system from the surroundings or leaves the system and flows to the surroundings (Figure 8.2). That is, we must be able to measure any change in the internal energy of the system, represented by $\Delta E$. The energy change $\Delta E$ represents the difference in internal energy between the final and initial states of the system:


By convention, energy changes are measured from the point of view of the system. Any energy that flows from the system to the surroundings has a negative sign because the system has lost it (that is, $E_{\text {final }}$ is smaller than $E_{\text {initial }}$ ). Any energy that flows to the system from the surroundings has a positive sign because the system has gained it ( $E_{\text {final }}$ is larger than $E_{\text {initial }}$ ). If, for instance, we were to burn 1.00 mol of methane in the presence of 2.00 mol of oxygen, 802 kJ is released as heat and transferred from the system to the surroundings. The system has 802 kJ less energy, so $\Delta E=-802 \mathrm{~kJ}$. This energy flow could be detected and measured by placing the reaction vessel in a water bath and noting the temperature of the bath before and after reaction.

$$
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)+802 \mathrm{~kJ} \text { energy } \quad \Delta E=-802 \mathrm{~kJ}
$$

This experiment tells us that the products of the reaction, $\mathrm{CO}_{2}(g)$ and $2 \mathrm{H}_{2} \mathrm{O}(g)$, have 802 kJ less internal energy than the reactants, $\mathrm{CH}_{4}(g)$ and $2 \mathrm{O}_{2}(g)$, even though we don't know the exact values at the beginning ( $E_{\text {initial }}$ ) and end ( $E_{\text {final }}$ ) of the reaction. Note that the value $\Delta E=-802 \mathrm{~kJ}$ for the reaction refers to the energy released when reactants are converted to products in the molar amounts represented by coefficients in the balanced equation. That is, 802 kJ is released when 1 mol of methane reacts with 2 mol of oxygen.

The internal energy of a system depends on many things: chemical identity, sample size, temperature, pressure, physical state (gas, liquid, or solid), and so forth. What the internal energy does not depend on is the system's past history. It doesn't matter what the system's temperature or physical state was yesterday or an hour ago, and it doesn't matter how the chemicals were made. All that matters is the present condition of the system. Thus, internal energy is said to be

4 FIGURE 8.2 When energy changes are measured in a chemical reaction, the system is the reaction mixture being studied, and the surroundings are the flask, the room, and the rest of the universe. The energy change is the difference between final and initial states $\left(\Delta E=E_{\text {final }}-E_{\text {initial }}\right)$. Any energy that flows from the system to the surroundings has a negative sign because $E_{\text {final }}$ is smaller than $E_{\text {initial }}$, and any energy that flows into the system from the surroundings has a positive sign because $E_{\text {final }}$ is larger than $E_{\text {initial }}$.

vStudents need to relate direction of heat flow with observed temperature change. Demonstrate that for a chemical reaction (system) performed in a beaker (surroundings), if heat energy is released by the system, the beaker absorbs the heat and becomes hotter; if heat energy is absorbed by the system, the beaker contributes the heat and becomes colder.

v
It is important for students to understand that the amount of energy released or gained in a reaction is proportional to the amounts of reactants and products involved in the reaction.

FIGURE 8.3 Since your $>$ position is a state function, the change in your position on going from Castroville, California, to Boston, Massachusetts, is independent of the path you take.
a state function-one whose value depends only on the present state of the system. Pressure, volume, and temperature are other examples of state functions, but work and heat are not.
state function A function or property whose value depends only on the present state (condition) of the system, not on the path used to arrive at that condition.
Let's illustrate the idea of a state function by imagining a trip from the Artichoke Capitol of the World (Castroville, California) to the Hub of the Universe (Boston, Massachusetts). You are the "system," and your position is a state function because how you got to wherever you are is irrelevant. Because your position is a state function, the change in your position when you travel from Castroville to Boston (the two cities are about 2720 miles apart) is independent of the path you take, whether through North Dakota or Louisiana (Figure 8.3).


The cross-country trip shown in Figure 8.3 illustrates an important point about state functions-their reversibility. Imagine that after traveling from Castroville to Boston, you turn around and go back. Because your final position is now identical to your initial position, the value of the change in position is 0 miles. The overall change in a state function is zero when the system returns to its original condition. For a nonstate function, however, the overall change is not zero even if the path returns the system to its original condition. Any work you do in making the trip, for instance, is not recovered when you return to your initial position, and any money or time you spent does not reappear.
PROBLEM 8.2 Which of the following are state functions, and which are not?
(a) The temperature of an ice cube
(b) The volume of an aerosol can
(c) The amount of time required for a 10 mi bike ride

### 8.4 Expansion Work

Just as energy is hard to define in everyday terms and comes in many forms, so too with work. In physics, work $(w)$ is defined as the force $(F)$ that produces the movement of an object times the distance moved (d):

$$
\begin{aligned}
\text { Work } & =\text { Force } \times \text { Distance } \\
w & =F \times d
\end{aligned}
$$

When you run up stairs, for instance, your leg muscles provide a force sufficient to overcome gravity and lift you higher. When you swim, you provide a force sufficient to push water out of the way and pull yourself forward.

The most common type of work encountered in chemical systems is the expansion work (also called pressure-volume, or $P V$ work) done as the result of a volume change in the system. Take the reaction of propane $\left(\mathrm{C}_{3} \mathrm{H}_{8}\right)$ with oxygen, for instance. The balanced equation says that 7 mol of product come from 6 mol of reactant:

$$
\underbrace{\mathrm{C}_{3} \mathrm{H}_{8}(\mathrm{~g})+5 \mathrm{O}_{2}(\mathrm{~g})}_{6 \mathrm{~mol} \text { of gas }} \longrightarrow \underbrace{3 \mathrm{CO}_{2}(\mathrm{~g})+4 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g})}_{7 \mathrm{~mol} \text { of gas }}
$$

If the reaction takes place inside a container outfitted with a movable piston, the greater volume of gas in the product will force the piston outward against the pressure of the atmosphere $(P)$, moving air molecules aside and thereby doing work (Figure 8.4).


A short calculation gives the exact amount of work done during the expansion. We know from physics that force $(F)$ is defined as area times pressure. In Figure 8.4, the force that the expanding gas exerts is the area of the piston $(A)$ times the pressure with which the gas pushes against the piston. This pressure is equal in magnitude but opposite in sign to the external atmospheric pressure $(P)$ that opposes the movement, so it has the value $-P$.

$$
F=-P \times A \quad \text { Where } P \text { is the external atmospheric pressure }
$$

If the piston is moved out a distance $d$, then the amount of work done is equal to force times distance, or, since $F=-P \times A$, pressure times area times distance:

$$
w=F \times d=-P \times A \times d
$$

This equation can be put into a more useful form by noticing that the area of the piston times the distance the piston moves is just the volume change in the system, $\Delta V=A \times d$. Thus, the amount of work done is equal to the pressure the gas exerts against the piston times the volume change (hence the name $P V$ work):


Work done during expansion


A This runner going uphill is doing a lot of work to overcome gravity.

FIGURE 8.4 The expansion in volume that occurs during a reaction forces the piston outward against atmospheric pressure $P$. The amount of work done is equal to the pressure exerted in moving the piston (the opposite of atmospheric pressure, $-P$ ) times the volume change $(\Delta V)$. The volume change is equal to the area of the piston $(A)$ times the distance the piston moves (d). Thus, $w=-P \Delta V$.


0Gases do work when the molecules push against the walls of their container and the volume of the container increases. If there is no volume change, no work is done.

What about the sign of the work done during the expansion? Because the work is done by the system to move air molecules aside as the piston rises, work energy must be leaving the system. Thus, the negative sign of the work in the above equation is consistent with the convention previously established for $\Delta E$ (Section 8.3) whereby we always adopt the point of view of the system. Any energy that flows out of the system has a negative sign because the system has lost it ( $\left.E_{\text {final }}<E_{\text {initial }}\right)$.

If the pressure is given in atmospheres (atm) and the volume change is given in liters, then the amount of work done has the unit liter atmosphere ( $\mathrm{L} \cdot \mathrm{atm}$ ), where $1 \mathrm{~atm}=101 \times 10^{3} \mathrm{~kg} /\left(\mathrm{m} \cdot \mathrm{s}^{2}\right)$. Thus, $1 \mathrm{~L} \cdot \mathrm{~atm}=101 \mathrm{~J}$ :

$$
1 \mathrm{~L} \cdot \mathrm{~atm}=(1 \mathrm{~L})\left(\frac{10^{-3} \mathrm{~m}^{3}}{1 \mathrm{~L}}\right)\left(101 \times 10^{3} \frac{\mathrm{~kg}}{\mathrm{~m} \cdot \mathrm{~s}^{2}}\right)=101 \frac{\mathrm{~kg} \cdot \mathrm{~m}^{2}}{\mathrm{~s}^{2}}=101 \mathrm{~J}
$$

When a reaction takes place with a contraction in volume rather than an expansion, the $\Delta V$ term has a negative sign and the work has a positive sign. This is again consistent with adopting the point of view of the system because the system has now gained work energy ( $E_{\text {final }}>E_{\text {initial }}$ ). An example is the industrial synthesis of ammonia by reaction of hydrogen with nitrogen. Four moles of gaseous reactants yield only 2 mol of gaseous products, so the volume of the system contracts and work is gained by the system.


If there is no volume change, then $\Delta V=0$ and there is no work. Such is the case for the combustion of methane where 3 mol of gaseous reactants give 3 mol of gaseous products: $\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \rightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)$.

## Worked Example 8.1

Calculate the work (in kilojoules) done during a reaction in which the volume expands from 12.0 L to 14.5 L against an external pressure of 5.0 atm .

## Strategy

Expansion work done during a chemical reaction is calculated by the formula $w=-P \Delta V$, where $P$ is the external pressure opposing the change in volume. In this instance, $P=5.0 \mathrm{~atm}$ and $\Delta V=(14.5-12.0) \mathrm{L}=2.5 \mathrm{~L}$. Remember that an expanding system loses work energy and thus has a negative sign.
Solution

$$
\begin{gathered}
w=-(5.0 \mathrm{~atm})(2.5 \mathrm{~L})=-12.5 \mathrm{~L} \cdot \mathrm{~atm} \\
(-12.5 \mathrm{~L} \cdot \mathrm{~atm})\left(101 \frac{\mathrm{~J}}{\mathrm{~L} \cdot \mathrm{~atm}}\right)=-1.3 \times 10^{3} \mathrm{~J}=-1.3 \mathrm{~kJ}
\end{gathered}
$$

PROBLEM 8.3 Calculate the work (in kilojoules) done during a synthesis of ammonia in which the volume contracts from 8.6 L to 4.3 L at a constant external pressure of 44 atm . In which direction does the work energy flow? What is the sign of the energy change?

- KEY CONCEPT PROBLEM 8.4 How much work is done (in kilojoules), and in which direction, as a result of the following reaction?



### 8.5 Energy and Enthalpy

We've seen up to this point that a system can exchange energy with its surroundings either by transferring heat or by doing work. Using the symbol $q$ to represent transferred heat and remembering from the previous section that $w=-P \Delta V$, we can represent the total energy change of a system, $\Delta E$, as

$$
\Delta E=q+w=q-P \Delta V
$$

where $q$ has a positive sign if the system gains heat and a negative sign if the system loses it. Rearranging this equation gives the amount of heat transferred:

$$
q=\Delta E+P \Delta V
$$

Let's look at two ways in which a chemical reaction might be carried out. On the one hand, a reaction might be carried out in a closed container with a constant volume, so that $\Delta V=0$. In such a case, no $P V$ work is done, and the energy change in the system is due entirely to heat transfer, which we write as $q_{v}$ to indicate heat at constant volume:

$$
q_{\mathrm{v}}=\Delta E \quad \text { At constant volume; } \Delta V=0
$$

Alternatively, a reaction might be carried out in an open flask or other apparatus that keeps the pressure constant and allows the volume of the system to change freely. In such a case, $\Delta V \neq 0$ and the energy change in the system might be due to both heat transfer and $P V$ work. We indicate the heat transfer at constant pressure by the symbol $q_{p}$ :

$$
q_{\mathrm{p}}=\Delta E+P \Delta V \quad \text { At constant pressure }
$$

Because reactions carried out at constant pressure are so common in chemistry, the heat change for such a process is given a special symbol, $\Delta H$, called the heat of reaction, or enthalpy change, of the reaction. The enthalpy $(H)$ of a system is the name given to the quantity $E+P V$.

$$
q_{p}=\Delta E+P \Delta V=\Delta H
$$

Note that only the enthalpy change during a reaction is important. As with internal energy, $E$, enthalpy is a state function whose value depends only on the current state of the system, not on the path taken to arrive at that state. Thus, we don't need to know the exact value of the system's enthalpy before and after a reaction. We only need to know the difference between final and initial states:

$$
\Delta H=H_{\text {products }}-H_{\text {reactants }}
$$

$\checkmark$
Relate energy change to physical work: When a person does work, the person's energy diminishes, so when a system does work, $w$ is negative and $\Delta E$ is negative.


vIf the volume of the system does not change, the heat transferred to or from a system is the energy change of that system.


A Many chemical reactions are carried out in open vessels at constant atmospheric pressure.

$\sqrt{ }$If the pressure of the system does not change, the heat transferred to or from a system is the enthalpy change of that system.

V
When reactions are performed in an open container, such as a coffee-cup calorimeter, the pressure ( = atmospheric pressure) does not change and $q_{\mathrm{P}}=\Delta H$; in a closed container, such as a bomb calorimeter, the volume ( = volume of the bomb) does not change and $q_{\mathrm{v}}=\Delta E$. Even in an open container, unless a gas is involved in the reaction, volume changes are usually negligible and $\Delta H \cong \Delta E$.

Heat Transfer activity

$\sqrt{ }$
The states of reactants and products are important in determining an energy change or enthalpy change for a reaction. The energy change will be different for a reaction producing a product as a liquid (with lower energy) versus producing the same product as a gas (with higher energy).

How big a difference is there between $\Delta E$, the heat flow at constant volume, and $\Delta H$, the heat flow at constant pressure? Let's look again at the reaction of propane, $\mathrm{C}_{3} \mathrm{H}_{8}$, with oxygen as an example. When the reaction is carried out at constant volume, no $P V$ work is possible and all the energy is released as heat: $\Delta E=-2045 \mathrm{~kJ}$. When the same reaction is carried out at constant pressure, however, only 2043 kJ of heat is released ( $\Delta H=-2043 \mathrm{~kJ}$ ). The difference, 2 kJ , occurs because at constant pressure, a small amount of expansion work is done against the atmosphere as 6 mol of gaseous reactants are converted into 7 mol of gaseous products.

$$
\begin{array}{ll}
\mathrm{C}_{3} \mathrm{H}_{8}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 3 \mathrm{CO}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(g) & \Delta E=-2045 \mathrm{~kJ} \\
\text { Propane } & \Delta H=-2043 \mathrm{~kJ} \\
& P \Delta V=+2 \mathrm{~kJ}
\end{array}
$$

What is true of the propane-oxygen reaction is also true of most other reactions: The difference between $\Delta H$ and $\Delta E$ is usually small, so the two quantities are nearly equal. Chemists usually measure and speak about $\Delta H$, though, because most reactions are carried out at constant atmospheric pressure in loosely covered vessels.

KEY CONCEPT PROBLEM 8.5 The following reaction has $\Delta E=-186 \mathrm{~kJ} / \mathrm{mol}$.

(a) Is the sign of $P \Delta V$ positive or negative? Explain.
(b) What is the sign and approximate magnitude of $\Delta H$ ? Explain.

### 8.6 The Thermodynamic Standard State

The value of the enthalpy change $\Delta H$ reported for a reaction is the amount of heat released or absorbed when reactants are converted to products at the same temperature and in the molar amounts represented by coefficients in the balanced equation. In the combustion reaction of propane discussed in the previous section, for instance, the reaction of 1 mol of propane gas with 5 mol of oxygen gas to give 3 mol of $\mathrm{CO}_{2}$ gas and 4 mol of water vapor releases 2043 kJ . The actual amount of heat released in a specific reaction, however, depends on the actual amounts of reactants. Thus, reaction of 0.5000 mol of propane with 2.500 mol of $\mathrm{O}_{2}$ releases $0.5000 \times 2043 \mathrm{~kJ}=1022 \mathrm{~kJ}$.

Note that the physical states of reactants and products must be specified as solid $(s)$, liquid $(l)$, gaseous $(g)$, or aqueous $(a q)$ when enthalpy changes are reported. The enthalpy change for the reaction of propane with oxygen is $\Delta H=-2043 \mathrm{~kJ}$ if water is produced as a gas but $\Delta H=-2219 \mathrm{~kJ}$ if water is produced as a liquid.

$$
\begin{array}{ll}
\mathrm{C}_{3} \mathrm{H}_{8}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 3 \mathrm{CO}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(g) & \Delta H=-2043 \mathrm{~kJ} \\
\mathrm{C}_{3} \mathrm{H}_{8}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 3 \mathrm{CO}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(l) & \Delta H=-2219 \mathrm{~kJ}
\end{array}
$$

The difference of 176 kJ between the values of $\Delta H$ for the two reactions arises because the conversion of liquid water to gaseous water requires energy. If liquid water is produced, $\Delta H$ is larger (more negative), but if gaseous water is produced, $\Delta H$ is smaller (less negative) because $44.0 \mathrm{~kJ} / \mathrm{mol}$ is needed for the vaporization.

$$
\begin{array}{rlr}
\mathrm{H}_{2} \mathrm{O}(l) & \longrightarrow \mathrm{H}_{2} \mathrm{O}(g) & \Delta H=44.0 \mathrm{~kJ} \\
\text { or } & 4 \mathrm{H}_{2} \mathrm{O}(l) & \longrightarrow 4 \mathrm{H}_{2} \mathrm{O}(g) \\
& \Delta H & =176 \mathrm{~kJ}
\end{array}
$$

In addition to specifying the physical state of reactants and products when reporting an enthalpy change, it's also necessary to specify the pressure and temperature. To ensure that all measurements are reported in the same way so that different reactions can be compared, a set of conditions called the thermodynamic standard state has been defined.

THERMODYNAMIC STANDARD STATE
Most stable form of a substance at 1 atm pressure* and at a specified temperature, usually $25^{\circ} \mathrm{C} ; 1 \mathrm{M}$ concentration for all substances in solution.

Measurements made under these conditions are indicated by addition of the superscript ${ }^{\circ}$ to the symbol of the quantity reported. Thus, an enthalpy change measured under standard conditions is called a standard enthalpy of reaction and is indicated by the symbol $\Delta H^{\circ}$. The reaction of propane with oxygen, for example, might be written

$$
\mathrm{C}_{3} \mathrm{H}_{8}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 3 \mathrm{CO}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(g) \quad \Delta H^{\circ}=-2043 \mathrm{~kJ}
$$

## Worked Example 8.2

The reaction of nitrogen with hydrogen to make ammonia has $\Delta H^{\circ}=-92.2 \mathrm{~kJ}$ :

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g) \quad \Delta H^{\circ}=-92.2 \mathrm{~kJ}
$$

What is the value of $\Delta E$ (in kilojoules) if the reaction is carried out at a constant pressure of 40.0 atm and the volume change is -1.12 L ?

## Strategy

We are given an enthalpy change, a volume change, and a pressure and asked to find an energy change. Rearrange the equation $\Delta H=\Delta E+P \Delta V$ to the form $\Delta E=$ $\Delta H-P \Delta V$, and then substitute the appropriate values for $\Delta H, P$, and $\Delta V$ :

## Solution

$$
\begin{aligned}
\Delta E & =\Delta H-P \Delta V \\
\text { where } \Delta H & =-92.2 \mathrm{~kJ} \\
P \Delta V & =(40.0 \mathrm{~atm})(-1.12 \mathrm{~L})=-44.8 \mathrm{~L} \cdot \mathrm{~atm} \\
& =(-44.8 \mathrm{~L} \cdot \mathrm{~atm})\left(101 \frac{\mathrm{~J}}{\mathrm{~L} \cdot \mathrm{~atm}}\right)=-4520 \mathrm{~J}=-4.52 \mathrm{~kJ} \\
\Delta E & =(-92.2 \mathrm{~kJ})-(-4.52 \mathrm{~kJ})=-87.7 \mathrm{~kJ}
\end{aligned}
$$

Note that $\Delta E$ is smaller (less negative) than $\Delta H$ for this reaction because the volume change is negative. Because the products have less volume than the reactants, a contraction occurs and a small amount of $P V$ work is gained by the system.

[^10]Standard conditions as defined for thermodynamics ( $P=1 \mathrm{~atm} ; T=298.15 \mathrm{~K}$ ) are different from standard conditions as defined for gas laws ( $P=1 \mathrm{~atm} ; T=273.15 \mathrm{~K}$ ) in Chapter 9.


Changes of State movie

$\nabla$Temperature does not change during a change of state; hence, $\Delta H_{\text {fusion }}$ for water refers to $\mathrm{H}_{2} \mathrm{O}\left(s, 0^{\circ} \mathrm{C}\right) \rightarrow \mathrm{H}_{2} \mathrm{O}\left(l, 0^{\circ} \mathrm{C}\right)$ and $\Delta H_{\text {vap }}$ for water refers to $\mathrm{H}_{2} \mathrm{O}\left(l, 100^{\circ} \mathrm{C}\right) \rightarrow \mathrm{H}_{2} \mathrm{O}\left(\mathrm{g}, 100^{\circ} \mathrm{C}\right)$.


- Dry ice (solid $\mathrm{CO}_{2}$ ) sublimes directly from solid to gas at atmospheric pressure.

PROBLEM 8.6 The reaction between hydrogen and oxygen to yield water vapor has $\Delta H^{\circ}=-484 \mathrm{~kJ}$ :

$$
2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(g) \quad \Delta H^{\circ}=-484 \mathrm{~kJ}
$$

How much $P V$ work is done, and what is the value of $\Delta E$ (in kilojoules) for the reaction of 0.50 mol of $\mathrm{H}_{2}$ with 0.25 mol of $\mathrm{O}_{2}$ at atmospheric pressure if the volume change is -5.6 L ?

PROBLEM 8.7 The explosion of 2.00 mol of solid trinitrotoluene (TNT) with a volume of approximately 274 mL produces gases with a volume of 448 L at room temperature. How much $P V$ work (in kilojoules) is done during the explosion?

$$
2 \mathrm{C}_{7} \mathrm{H}_{5} \mathrm{~N}_{3} \mathrm{O}_{6}(s) \longrightarrow 12 \mathrm{CO}(g)+5 \mathrm{H}_{2}(g)+3 \mathrm{~N}_{2}(g)+2 \mathrm{C}(s)
$$

### 8.7 Enthalpies of Physical and Chemical Change

Almost every change in a system involves either a gain or a loss of enthalpy. The change can be either physical, such as the melting of a solid to a liquid, or chemical, such as the burning of propane. Let's look briefly at examples of both kinds.

## Enthalpies of Physical Change

Imagine what would happen if you started with a block of ice at a low temperature, say $-10^{\circ} \mathrm{C}$, and slowly increased its enthalpy by adding heat. The initial input of heat would cause the temperature of the ice to rise until it reached $0^{\circ} \mathrm{C}$. Additional heat would then cause the ice to melt without raising its temperature as the added energy was expended in overcoming the forces that hold $\mathrm{H}_{2} \mathrm{O}$ molecules rigidly together in the ice crystal. The amount of heat necessary to melt a substance is called the enthalpy of fusion, or heat of fusion ( $\Delta H_{\text {fusion }}$ ), and has a value of $6.01 \mathrm{~kJ} / \mathrm{mol}$ for $\mathrm{H}_{2} \mathrm{O}$.

Once the ice has melted, further input of heat raises the water's temperature until it reaches $100^{\circ} \mathrm{C}$, and additional heat then causes the water to boil. Once again, energy is necessary to overcome the forces holding molecules together in the liquid, so the temperature does not rise again until all the liquid has been converted into vapor. The amount of heat required for evaporation is called the enthalpy of vaporization, or heat of vaporization $\left(\Delta H_{\text {vap }}\right)$, and has a value of $40.7 \mathrm{~kJ} / \mathrm{mol}$ at $100^{\circ} \mathrm{C}$ for $\mathrm{H}_{2} \mathrm{O}$.

Another kind of physical change in addition to melting and boiling is sublimation-the direct conversion of a solid to a vapor without going through a liquid state. Solid $\mathrm{CO}_{2}$ (dry ice), for example, changes directly from solid to vapor at atmospheric pressure without first melting to a liquid. Since enthalpy is a state function, the enthalpy change on going from solid to vapor must be constant regardless of the path taken. Thus, a substance's enthalpy of sublimation, or heat of sublimation $\left(\Delta H_{\text {subl }}\right)$, equals the sum of the heat of fusion and heat of vaporization (Figure 8.5).

FIGURE 8.5 Because enthalpy is a state function, the enthalpy change from solid to vapor does not depend on the path taken between the two states. Therefore, at a constant temperature, $\Delta H_{\text {subl }}=\Delta H_{\text {fusion }}+\Delta H_{\text {vap }}$.


## Enthalpies of Chemical Change

We saw in Section 8.5 that an enthalpy change is often called a heat of reaction because it is a measure of the heat flow into or out of a system at constant pressure. If the products have more enthalpy than the reactants, then heat has flowed into the system from the surroundings and $\Delta H$ has a positive sign. Such reactions are said to be endothermic (endo means "within," so heat flows in). The reaction of 1 mol of barium hydroxide octahydrate* with ammonium chloride, for example, absorbs 80.3 kJ from the surroundings ( $\Delta H^{\circ}=+80.3 \mathrm{~kJ}$ ). The surroundings, having lost heat, become so cold that water freezes around the outside of the container (Figure 8.6).

$$
\begin{aligned}
\mathrm{Ba}(\mathrm{OH})_{2} \cdot 8 \mathrm{H}_{2} \mathrm{O}(s)+ & 2 \mathrm{NH}_{4} \mathrm{Cl}(s) \longrightarrow \\
& \mathrm{BaCl}_{2}(a q)+2 \mathrm{NH}_{3}(a q)+10 \mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H^{\circ}=+80.3 \mathrm{~kJ}
\end{aligned}
$$

If the products have less enthalpy than the reactants, then heat has flowed from the system to the surroundings and $\Delta H$ has a negative sign. Such reactions are said to be exothermic (exo means "out," so heat flows out). The so-called thermite reaction of aluminum with iron(III) oxide, for example, releases so much heat and the surroundings get so hot $\left(\Delta H^{\circ}=-852 \mathrm{~kJ}\right)$ that it is used in construction work and in building railroads to weld iron (Figure 8.7).

$$
2 \mathrm{Al}(s)+\mathrm{Fe}_{2} \mathrm{O}_{3}(s) \longrightarrow 2 \mathrm{Fe}(s)+\mathrm{Al}_{2} \mathrm{O}_{3}(s) \quad \Delta H^{\circ}=-852 \mathrm{~kJ}
$$


© FIGURE 8.7 The thermite reaction of aluminum with iron(III) oxide is so strongly exothermic and releases so much heat to the surroundings that the products become molten.

As noted previously, the value of $\Delta H^{\circ}$ given for an equation assumes that the equation is balanced for the number of moles of reactants and products, that all substances are in their standard states, and that the physical state of each substance is as specified. The actual amount of heat released in a specific reaction depends on the amounts of reactants, as illustrated in Worked Example 8.3.

It should also be emphasized that $\Delta H^{\circ}$ values refer to the reaction going in the direction written. For the reverse reaction, the sign of $\Delta H^{\circ}$ must be changed. Because of the reversibility of state functions (Section 8.3), the enthalpy change for any reaction is equal in magnitude but opposite in sign to that for the reverse reaction. For example, the reaction of iron with aluminum oxide to yield aluminum and iron oxide (the reverse of the thermite reaction) would be endothermic and have $\Delta H^{\circ}=+852 \mathrm{~kJ}$ :

$$
\begin{array}{ll}
2 \mathrm{Fe}(s)+\mathrm{Al}_{2} \mathrm{O}_{3}(s) \longrightarrow 2 \mathrm{Al}(s)+\mathrm{Fe}_{2} \mathrm{O}_{3}(s) & \Delta H^{\circ}=+852 \mathrm{~kJ} \\
2 \mathrm{Al}(s)+\mathrm{Fe}_{2} \mathrm{O}_{3}(s) \longrightarrow 2 \mathrm{Fe}(s)+\mathrm{Al}_{2} \mathrm{O}_{3}(s) & \Delta H^{\circ}=-852 \mathrm{~kJ}
\end{array}
$$

[^11]Bassam Z. Shakhashiri, "Evaporation as an endothermic process," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) 249-251.


A FIGURE 8.6 The reaction of barium hydroxide octahydrate with ammonium chloride is so strongly endothermic and draws so much heat from the surroundings that the temperature falls below $0^{\circ} \mathrm{C}$ and moisture freezes around the container.

v
Endothermic means heat flows into a system and $\Delta H>0$. Exothermic means heat flows out of a system and $\Delta H<0$.


Bassam Z. Shakhashiri, "Endothermic Reactions of Hydrated Barium Hydroxide and Ammonium Salts," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983) pp. 10-12.


A FIGURE 8.8 A calorimeter for measuring the heat flow in a reaction at constant pressure $(\Delta H)$. The reaction takes place inside an insulated vessel outfitted with a loose-fitting top, a thermometer, and a stirrer. Measuring the temperature change that accompanies the reaction makes it possible to calculate $\Delta H$.

## Worked Example 8.3

How much heat (in kilojoules) is evolved when 5.00 g of aluminum reacts with a stoichiometric amount of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ ?

$$
2 \mathrm{Al}(s)+\mathrm{Fe}_{2} \mathrm{O}_{3}(s) \longrightarrow 2 \mathrm{Fe}(s)+\mathrm{Al}_{2} \mathrm{O}_{3}(s) \quad \Delta H^{\circ}=-852 \mathrm{~kJ}
$$

## Strategy

According to the balanced equation, 852 kJ of heat is evolved from the reaction of 2 mol of Al. To find out how much heat is evolved from the reaction of 5.00 g of Al , we have to find out how many moles of aluminum are in 5.00 g .

## Solution

The molar mass of Al is $26.98 \mathrm{~g} / \mathrm{mol}$, so 5.00 g of Al equals 0.185 mol :

$$
5.00 \mathrm{~g} \mathrm{Al} \times \frac{1 \mathrm{~mol} \mathrm{Al}}{26.98 \mathrm{~g} \mathrm{Al}}=0.185 \mathrm{~mol} \mathrm{Al}
$$

Because 2 mol of Al releases 852 kJ of heat, 0.185 mol of Al releases 78.8 kJ of heat:

$$
0.185 \mathrm{~mol} \mathrm{Al} \times \frac{852 \mathrm{~kJ}}{2 \mathrm{~mol} \mathrm{Al}}=78.8 \mathrm{~kJ}
$$

Ballpark Check Since the molar mass of Al is about $27 \mathrm{~g}, 5 \mathrm{~g}$ of aluminum is roughly 0.2 mol , and the heat evolved is about $852 / 2 \mathrm{~kJ} / \mathrm{mol} \times 0.2 \mathrm{~mol}$, or approximately 85 kJ .

PROBLEM 8.8 How much heat (in kilojoules) is evolved or absorbed in each of the following reactions?
(a) Burning of 15.5 g of propane:

$$
\mathrm{C}_{3} \mathrm{H}_{8}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 3 \mathrm{CO}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H^{\circ}=-2219 \mathrm{~kJ}
$$

(b) Reaction of 4.88 g of barium hydroxide octahydrate with ammonium chloride:

$$
\begin{aligned}
& \mathrm{Ba}(\mathrm{OH})_{2} \cdot 8 \mathrm{H}_{2} \mathrm{O}(s)+2 \mathrm{NH}_{4} \mathrm{Cl}(s) \longrightarrow \\
& \quad \mathrm{BaCl}_{2}(a q)+2 \mathrm{NH}_{3}(a q)+10 \mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H^{\circ}=+80.3 \mathrm{~kJ}
\end{aligned}
$$

PROBLEM 8.9 Nitromethane $\left(\mathrm{CH}_{3} \mathrm{NO}_{2}\right)$, sometimes used as a fuel in drag racers, burns according to the following equation:

$$
\begin{aligned}
4 \mathrm{CH}_{3} \mathrm{NO}_{2}(l)+7 \mathrm{O}_{2}(g) \longrightarrow \\
4 \mathrm{CO}_{2}(g)+6 \mathrm{H}_{2} \mathrm{O}(g)+4 \mathrm{NO}_{2}(g) \quad \Delta H^{\circ}=-2441.6 \mathrm{~kJ}
\end{aligned}
$$

How much heat is released by burning 100.0 g of nitromethane?

### 8.8 Calorimetry and Heat Capacity

The amount of heat transferred during a reaction can be measured with a device called a calorimeter, shown schematically in Figure 8.8. At its simplest, a calorimeter is just an insulated vessel with a stirrer, a thermometer, and a loose-fitting lid to keep the contents at atmospheric pressure. The reaction is carried out inside the vessel, and the heat evolved or absorbed is calculated from the temperature change. Because the pressure inside the calorimeter is constant (atmospheric pressure), the temperature measurement makes it possible to calculate the enthalpy change $\Delta H$ during a reaction.

A somewhat more complicated device called a bomb calorimeter is used to measure the heat released during a combustion reaction, or burning of a flammable substance. (More generally, a combustion reaction is any reaction that produces a flame.) The sample is placed in a small cup and sealed under an oxygen atmosphere inside a steel "bomb" that is itself placed in an insulated, water-filled container (Figure 8.9). The reactants are ignited electrically, and the evolved heat is calculated from the temperature change of the surrounding water. Since the reaction takes place at constant volume but not constant pressure, the measurement provides a value for $\Delta E$ rather than $\Delta H$.


How can the temperature change inside a calorimeter be used to calculate $\Delta H$ (or $\Delta E$ ) for a reaction? When a calorimeter and its contents absorb a given amount of heat, the temperature rise that results depends on the calorimeter's heat capacity. Heat capacity $(C)$ is the amount of heat required to raise the temperature of an object or substance a given amount, a relationship that can be expressed by the equation

$$
C=\frac{q}{\Delta T}
$$

where $q$ is the quantity of heat transferred and $\Delta T$ is the temperature change $\left(\Delta T=T_{\text {final }}-T_{\text {initial }}\right)$. The greater the heat capacity, the greater the amount of heat needed to produce a given temperature change. A bathtub full of water, for instance, has a greater heat capacity than a coffee cup full, and it therefore takes far more heat to warm the tubful than the cupful. The exact amount of heat absorbed is equal to the heat capacity times the temperature rise:

$$
q=C \times \Delta T
$$

Heat capacity is an extensive property (Section 1.4), so its value depends on both the size of an object and its composition. To compare different substances, it's useful to define a quantity called specific heat, the amount of heat necessary to raise the temperature of 1 g of a substance by $1^{\circ} \mathrm{C}$. The amount of heat necessary to raise the temperature of a given object, then, is the specific heat times the mass of the object times the rise in temperature:

$$
q=(\text { Specific heat }) \times(\text { Mass of substance }) \times \Delta T
$$

Worked Example 8.5 shows how specific heats are used in calorimetry calculations.
Closely related to specific heat is the molar heat capacity ( $C_{\mathrm{m}}$ ), defined as the amount of heat necessary to raise the temperature of 1 mol of a substance by $1^{\circ} \mathrm{C}$.

John J. Fortman, "Analogical Demonstrations," J. Chem. Educ., Vol. 69, 1992, 323-324.

7i] Charles M. Wynn, Sr., "Heat Flow vs. Cash Flow: A Banking Analogy," J. Chem. Educ., Vol. 74, 1997, 397-398.

< FIGURE 8.9 Diagram of a bomb calorimeter for measuring the heat evolved at constant volume $(\Delta E)$ in a combustion reaction. The reaction is carried out inside a steel bomb, and the heat evolved is transferred to the surrounding water, where the temperature rise is measured.

0Just as density provides a link between mass and volume, heat capacity links heat flow and temperature change, allowing the three variables to be interconverted.

Dad Brother Thomas McCullogh, "A Specific Heat Analogy," J. Chem. Educ., Vol. 57, 1980, 896.

VThe amount of heat transferred and, therefore, the temperature change depend on the amount of substance involved. Specific heat is heat capacity per gram of substance and has units of $\mathrm{J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$; molar heat capacity is heat capacity per mole of substance and has units $\mathrm{J} /\left(\mathrm{mol} \cdot{ }^{\circ} \mathrm{C}\right)$.

Bassam Z. Shakhashiri, "Boiling Water in a Paper Cup: Heat Capacity of Water," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 239-241.

Specific heat and molar heat capacity are intensive properties that depend on the state of the substance.

Doris R. Kimbrough, "Heat Capacity, Body Temperature and Hypothermia," J. Chem. Educ., Vol. 75, 1998, 48-49.

Large masses of water moderate the temperature of the surroundings because of their high heat capacity.

The amount of heat necessary to raise the temperature of a given number of moles of a substance is thus

$$
q=\left(C_{\mathrm{m}}\right) \times(\text { Moles of substance }) \times \Delta T
$$

Values of specific heats and molar heat capacities for some common substances are given in Table 8.1.

| TABLE 8.1 | Specific Heats and Molar Heat Capacities for Some Common <br> Substances at $25^{\circ} \mathrm{C}$ |  |
| :--- | :--- | :--- |
| Substance | Specific Heat <br> $\mathbf{J} /\left(\mathbf{g} \cdot{ }^{\circ} \mathbf{C}\right)$ | Molar Heat Capacity <br> $\mathbf{J} /\left(\mathbf{m o l} \cdot{ }^{\circ} \mathbf{C}\right)$ |
| Air (dry) | 1.01 | 29.1 |
| Aluminum | 0.902 | 24.4 |
| Copper | 0.385 | 24.4 |
| Gold | 0.129 | 25.4 |
| Iron | 0.450 | 25.1 |
| Mercury | 0.140 | 28.0 |
| NaCl | 0.864 | 50.5 |
| Water $(s)^{*}$ | 2.03 | 36.6 |
| Water $(l)$ | 4.179 | 75.3 |

*At $-11^{\circ} \mathrm{C}$
As indicated in Table 8.1, the specific heat of liquid water is considerably higher than that of most other substances, and a large transfer of heat is therefore necessary to either cool or warm a given amount of water. One consequence is that large lakes or other bodies of water tend to moderate the air temperature in surrounding areas. Another consequence is that the human body, which is about $60 \%$ water, is able to maintain a steady internal temperature under changing outside conditions.


## Worked Example 8.4

What is the specific heat of silicon if it takes 192 J to raise the temperature of 45.0 g of Si by $6.0^{\circ} \mathrm{C}$ ?

## Strategy

To find a specific heat of a substance, we need to calculate the amount of energy necessary to raise the temperature of 1 g of the substance by $1^{\circ} \mathrm{C}$.

## Solution

Specific heat of $\mathrm{Si}=\frac{192 \mathrm{~J}}{(45.0 \mathrm{~g})\left(6.0^{\circ} \mathrm{C}\right)}=0.71 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$

## Worked Example 8.5

Aqueous silver ion reacts with aqueous chloride ion to yield a white precipitate of solid silver chloride:

$$
\mathrm{Ag}^{+}(a q)+\mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{AgCl}(s)
$$

When 10.0 mL of $1.00 \mathrm{M} \mathrm{AgNO}_{3}$ solution is added to 10.0 mL of 1.00 M NaCl solution at $25.0^{\circ} \mathrm{C}$ in a calorimeter, a white precipitate of AgCl forms and the temperature of the aqueous mixture increases to $32.6^{\circ} \mathrm{C}$. Assuming that the specific heat of the aqueous mixture is $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$, that the density of the mixture is $1.00 \mathrm{~g} / \mathrm{mL}$, and that the calorimeter itself absorbs a negligible amount of heat, calculate $\Delta H$ (in kilojoules) for the reaction.

## Strategy

Because the temperature rises during the reaction, heat must be liberated and $\Delta H$ must be negative. The amount of heat evolved during the reaction is equal to the amount of heat absorbed by the mixture:

$$
\text { Heat evolved }=(\text { Specific heat }) \times(\text { Mass of mixture }) \times(\text { Temperature change })
$$

Calculating the heat evolved on a per-mole basis then gives the enthalpy change $\Delta H$.

## Solution

$$
\begin{aligned}
& \text { Specific heat }=4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right) \\
& \text { Mass }=(20.0 \mathrm{~mL})\left(1.00 \frac{\mathrm{~g}}{\mathrm{~mL}}\right)=20.0 \mathrm{~g} \\
& \text { Temperature change }=32.6^{\circ} \mathrm{C}-25.0^{\circ} \mathrm{C}=7.6^{\circ} \mathrm{C} \\
& \text { Heat evolved }=\left(4.18 \frac{\mathrm{~J}}{\mathrm{~g} \cdot{ }^{\circ} \mathrm{C}}\right)(20.0 \mathrm{~g})\left(7.6^{\circ} \mathrm{C}\right)=6.4 \times 10^{2} \mathrm{~J}
\end{aligned}
$$

According to the balanced equation, the number of moles of AgCl produced equals the number of moles of $\mathrm{Ag}^{+}$(or $\mathrm{Cl}^{-}$) reacted:

$$
\begin{aligned}
& \text { Moles of } \mathrm{Ag}^{+}=(10.0 \mathrm{~mL})\left(\frac{1.00 \mathrm{~mol} \mathrm{Ag}}{}+\frac{1000 \mathrm{~mL}}{10}\right)=1.00 \times 10^{-2} \mathrm{~mol} \mathrm{Ag}^{+} \\
& \text {Moles of } \mathrm{AgCl}=1.00 \times 10^{-2} \mathrm{~mol} \mathrm{AgCl} \\
& \text { Heat evolved per mole of } \mathrm{AgCl}=\frac{6.4 \times 10^{2} \mathrm{~J}}{1.00 \times 10^{-2} \mathrm{~mol} \mathrm{AgCl}}=64 \mathrm{~kJ} / \mathrm{mol} \mathrm{AgCl}
\end{aligned}
$$

Therefore, $\Delta H=-64 \mathrm{~kJ}$ (Negative because heat is released.)

PROBLEM 8.10 Assuming that Coca Cola has the same specific heat as water [4.18 J/ ( $\left.\left.\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)\right]$, calculate the amount of heat (in kilojoules) transferred when one can (about 350 g ) is cooled from $25^{\circ} \mathrm{C}$ to $3^{\circ} \mathrm{C}$.

PROBLEM 8.11 What is the specific heat of lead if it takes 96 J to raise the temperature of a 75 g block by $10.0^{\circ} \mathrm{C}$ ?


A The reaction of aqueous $\mathrm{Ag}^{+}$with aqueous $\mathrm{Cl}^{-}$to yield solid AgCl is an exothermic process.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "A Chemical Hand Warmer," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 101-102.

Bassam Z. Shakhashiri, "Chemical Cold Pack," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983) pp. 8-9.

Bassam Z. Shakhashiri, "Heat of Neutralization," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983) pp. 15-16.

Students have already employed Hess's law when performing Born-Haber cycle calculations in Chapter 6.

When an equation is reversed, $\Delta H$ must be multiplied by -1 . When an equation is multiplied by a coefficient, $\Delta H$ must be multiplied by the same coefficient.

PROBLEM 8.12 When 25.0 mL of $1.0 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ is added to 50.0 mL of 1.0 M NaOH at $25.0^{\circ} \mathrm{C}$ in a calorimeter, the temperature of the aqueous solution increases to $33.9^{\circ} \mathrm{C}$. Assuming that the specific heat of the solution is $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$, that its density is $1.00 \mathrm{~g} / \mathrm{mL}$, and that the calorimeter itself absorbs a negligible amount of heat, calculate $\Delta H$ (in kilojoules) for the reaction.

$$
\mathrm{H}_{2} \mathrm{SO}_{4}(a q)+2 \mathrm{NaOH}(a q) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{Na}_{2} \mathrm{SO}_{4}(a q)
$$

### 8.9 Hess's Law

Now that we've discussed in general terms the energy changes that occur during chemical reactions, let's look at a specific example in detail. In particular, let's look at the Haber process, the industrial method by which approximately 13 million tons of ammonia are produced each year in the United States, primarily for use as fertilizer. The reaction of hydrogen with nitrogen to make ammonia is exothermic, with $\Delta H^{\circ}=-92.2 \mathrm{~kJ}$.

$$
3 \mathrm{H}_{2}(g)+\mathrm{N}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g) \quad \Delta H^{\circ}=-92.2 \mathrm{~kJ}
$$

If we dig into the details of the reaction, we find that it's not as simple as it looks. In fact, the overall reaction occurs by a series of steps, with hydrazine $\left(\mathrm{N}_{2} \mathrm{H}_{4}\right)$ produced at an intermediate stage:

$$
2 \mathrm{H}_{2}(g)+\mathrm{N}_{2}(g) \longrightarrow \underset{\text { Hydrazine }}{\mathrm{N}_{2} \mathrm{H}_{4}(g) \xrightarrow[\text { Ammonia }]{\mathrm{H}_{2}} 2 \mathrm{NH}_{3}(g)}
$$

The enthalpy change for the conversion of hydrazine to ammonia can be measured as $\Delta H^{\circ}=-187.6 \mathrm{~kJ}$, but if we wanted to measure $\Delta H^{\circ}$ for the formation of hydrazine from hydrogen and nitrogen, we would have difficulty because the reaction doesn't go cleanly. Some of the hydrazine is converted into ammonia while some of the starting nitrogen still remains.

Fortunately, there's a way around the difficulty—a way that makes it possible to measure an energy change indirectly when a direct measurement can't be made. The trick is to realize that because enthalpy is a state function, $\Delta H$ is the same no matter what path is taken between two states. Thus, the sum of the enthalpy changes for the individual steps in a sequence must equal the enthalpy change for the overall reaction, a statement known as Hess's law:

Hess's law The overall enthalpy change for a reaction is equal to the sum of the enthalpy changes for the individual steps in the reaction.
Reactants and products in the individual steps can be added and subtracted like algebraic quantities in determining the overall equation. In the synthesis of ammonia, for example, the sum of the steps 1 and 2 is equal to the overall reaction. Thus, the sum of the enthalpy changes for steps 1 and 2 is equal to the enthalpy change for the overall reaction. With this knowledge, we can calculate the enthalpy change for step 1 . Figure 8.10 shows the situation pictorially.

| Step 1. <br> Step 2. | $2 \mathrm{H}_{2}(g)+\mathrm{N}_{2}(g) \longrightarrow \mathrm{N}_{2}(g)+\mathrm{H}_{4}(g)$ | $\Delta H^{\circ}{ }_{1}=?$ |
| :--- | ---: | :--- |
| Overall <br> reaction | $3 \mathrm{H}_{2}(g)+\mathrm{N}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g)$ | $\Delta H^{\circ}{ }_{2}=-187.6 \mathrm{~kJ}$ |

$$
\text { Since } \quad \begin{aligned}
\Delta H^{\circ}{ }_{1} & +\Delta H^{\circ}{ }_{2}=\Delta H^{\circ} \text { reaction } \\
\text { then } \quad \Delta H_{1}^{\circ} & =\Delta H^{\circ} \text { reaction }-\Delta H^{\circ}{ }_{2} \\
& =(-92.2 \mathrm{~kJ})-(-187.6 \mathrm{~kJ})=+95.4 \mathrm{~kJ}
\end{aligned}
$$



## Worked Example 8.6

Methane, the main constituent of natural gas, burns in oxygen to yield carbon dioxide and water:

$$
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

Use the following information to calculate $\Delta H^{\circ}$ (in kilojoules) for the combustion of methane:

$$
\begin{aligned}
\mathrm{CH}_{4}(g)+\mathrm{O}_{2}(g) & \longrightarrow \mathrm{CH}_{2} \mathrm{O}(g)+\mathrm{H}_{2} \mathrm{O}(g) & \Delta H^{\circ}=-284 \mathrm{~kJ} \\
\mathrm{CH}_{2} \mathrm{O}(g)+\mathrm{O}_{2}(g) & \mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(g) & \Delta H^{\circ}=-518 \mathrm{~kJ} \\
\mathrm{H}_{2} \mathrm{O}(l) & \mathrm{H}_{2} \mathrm{O}(g) & \Delta H^{\circ}=44.0 \mathrm{~kJ}
\end{aligned}
$$

## Strategy

Though it often takes some trial and error, the idea is to combine the individual reactions so that their sum is the desired reaction. The important points to be aware of are that

- All the reactants $\left[\mathrm{CH}_{4}(g)\right.$ and $\left.\mathrm{O}_{2}(g)\right]$ must appear on the left.
- All the products $\left[\mathrm{CO}_{2}(g)\right.$ and $\left.\mathrm{H}_{2} \mathrm{O}(l)\right]$ must appear on the right.
- All intermediate products $\left[\mathrm{CH}_{2} \mathrm{O}(g)\right.$ and $\left.\mathrm{H}_{2} \mathrm{O}(g)\right]$ must occur on both the left and the right so that they cancel.
- A reaction written in the reverse of the direction given $\left[\mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{H}_{2} \mathrm{O}(l)\right]$ must have the sign of its $\Delta H^{\circ}$ changed (Section 8.7).
- A reaction can be multiplied by a coefficient as necessary $\left[\mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{H}_{2} \mathrm{O}(l)\right.$ is multiplied by 2], but $\Delta H^{\circ}$ for the reaction must be multiplied by that same coefficient.


## Solution

| $\mathrm{CH}_{4}(g)+\mathrm{O}_{2}(g)$ | $\longrightarrow \mathrm{CH}_{2} \mathrm{O}(g)+\mathrm{H}_{2} \mathrm{O}(g)$ |
| ---: | :--- |
| $\mathrm{CH}_{2} \mathrm{O}(g)+\mathrm{O}_{2}(g)$ | $\Delta H^{\circ}=-284 \mathrm{~kJ}$ |
| $2\left[\mathrm{CO}_{2} \mathrm{O}(g) \longrightarrow \mathrm{H}_{2} \mathrm{O}(g)\right.$ | $\Delta H^{\circ}=-518 \mathrm{~kJ}$ |
| $\left.\mathrm{H}_{2} \mathrm{O}(l)\right]$ | $2\left[\Delta H^{\circ}=-44.0 \mathrm{~kJ}\right]=-88.0 \mathrm{~kJ}$ |
| $\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)$ | $\Delta H^{\circ}=-890 \mathrm{~kJ}$ |

## Worked Example 8.7

Water gas is the name for the industrially important mixture of CO and $\mathrm{H}_{2}$ prepared by passing steam over hot charcoal at $1000^{\circ} \mathrm{C}$ :

$$
\mathrm{C}(s)+\mathrm{H}_{2} \mathrm{O}(g) \longrightarrow \mathrm{CO}(g)+\mathrm{H}_{2}(g)
$$

4 FIGURE 8.10 A representation of the enthalpy changes for steps in the synthesis of ammonia from nitrogen and hydrogen. If $\Delta H^{\circ}$ values for step 2 and for the overall reaction are known, then $\Delta H^{\circ}$ for step 1 can be calculated. That is, the enthalpy change for the overall reaction equals the sum of the enthalpy changes for the individual steps 1 and 2 , a statement known as Hess's law.


Methylene chloride

The hydrogen is then purified and used as a starting material for preparing ammonia. Use the following information to calculate $\Delta H^{\circ}$ (in kilojoules) for the water-gas reaction:

$$
\begin{aligned}
& \mathrm{C}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g) \\
& 2 \mathrm{CO}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{CO}_{2}(g) \Delta H^{\circ}=-393.5 \mathrm{~kJ} \\
& 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \longrightarrow 266.0 \mathrm{~kJ} \\
& 2 \mathrm{H}_{2} \mathrm{O}(g) \Delta H^{\circ}=-483.6 \mathrm{~kJ}
\end{aligned}
$$

## Strategy

As in Worked Example 8.6, the idea is to find a combination of the individual reactions whose sum is the desired reaction. In this instance, $\mathrm{it}^{\prime}$ 's necessary to reverse the second and third steps and to multiply both by $1 / 2$ to make the overall equation balance. In so doing, the sign of the enthalpy changes for those steps must be changed and also multiplied by $1 / 2$. (Alternatively, we could multiply the first step by 2 and then divide the final result by 2.) Note that $\mathrm{CO}_{2}(g)$ and $\mathrm{O}_{2}(g)$ cancel because they appear on both the right and left sides of reactions.

## Solution

$$
\begin{aligned}
& \mathrm{C}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g}) \longrightarrow \mathrm{CO}_{2}(\mathrm{~g}) \quad \Delta H^{\circ}=-393.5 \mathrm{~kJ} \\
& 1 / 2\left[2 \mathrm{CO}_{2}(\mathrm{~g}) \longrightarrow 2 \mathrm{CO}(g)+\mathrm{O}_{2}(\mathrm{~g})\right] \quad 1 / 2\left[\Delta H^{\circ}=566.0 \mathrm{~kJ}\right]=283.0 \mathrm{~kJ} \\
& 1 / 2\left[2 \mathrm{H}_{2} \mathrm{O}(g) \longrightarrow 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(\mathrm{~g})\right] \quad 1 / 2\left[\Delta H^{\circ}=483.6 \mathrm{~kJ}\right]=241.8 \mathrm{~kJ} \\
& \mathrm{C}(s)+\mathrm{H}_{2} \mathrm{O}(g) \longrightarrow \mathrm{CO}(g)+\mathrm{H}_{2}(g) \quad \Delta H^{\circ}=131.3 \mathrm{~kJ}
\end{aligned}
$$

The water-gas reaction is endothermic by 131.3 kJ .

- PROBLEM 8.13 The industrial degreasing solvent methylene chloride, $\mathrm{CH}_{2} \mathrm{Cl}_{2}$, is prepared from methane by reaction with chlorine:

$$
\mathrm{CH}_{4}(g)+2 \mathrm{Cl}_{2}(g) \longrightarrow \mathrm{CH}_{2} \mathrm{Cl}_{2}(g)+2 \mathrm{HCl}(g)
$$

Use the following data to calculate $\Delta H^{\circ}$ (in kilojoules) for the reaction:

$$
\begin{aligned}
\mathrm{CH}_{4}(g)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{CH}_{3} \mathrm{Cl}(g)+\mathrm{HCl}(g) & \Delta H^{\circ}=-98.3 \mathrm{~kJ} \\
\mathrm{CH}_{3} \mathrm{Cl}(g)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{CH}_{2} \mathrm{Cl}_{2}(g)+\mathrm{HCl}(g) & \Delta H^{\circ}=-104 \mathrm{~kJ}
\end{aligned}
$$

- KEY CONCEPT PROBLEM 8.14 The reaction of A with B to give D proceeds in two steps and can be represented by the following Hess's law diagram.


1) $\mathrm{A}+\mathrm{B} \longrightarrow \mathrm{C} \quad \Delta H^{\circ}=-100 \mathrm{~kJ}$
2) $\mathrm{C}+\mathrm{B} \longrightarrow \mathrm{D} \quad \Delta H^{\circ}=-50 \mathrm{~kJ}$
(a) What is the equation and $\Delta H^{\circ}$ for the net reaction?
(b) Which arrow on the diagram corresponds to which step, and which arrow corresponds to the net reaction?
(c) The diagram shows three energy levels. The energies of which substances are represented by each?

- PROBLEM 8.15 Draw a Hess's law diagram similar to that in Problem 8.14 depicting the energy changes for the reaction in Problem 8.13.


### 8.10 Standard Heats of Formation

Where do the $\Delta H^{\circ}$ values we've been using in previous sections come from? There are so many chemical reactions-several hundred million are known-that it's impossible to measure $\Delta H^{\circ}$ for all of them. A better way is needed.

The most efficient way to manage with the smallest number of experimental measurements is to use what are called standard heats of formation, symbolized $\Delta H^{\circ}{ }_{\mathrm{f}}$.

- standard heat of formation The enthalpy change $\Delta H^{\circ}{ }_{f}$ for the formation of 1 mol of a substance in its standard state from its constituent elements in their standard states.

Note several points about this definition. First, the "reaction" to form a substance from its constituent elements can be (and often is) hypothetical. We can't combine carbon and hydrogen in the laboratory to make methane, for instance, yet the heat of formation for methane is $\Delta H^{\circ}=-74.8 \mathrm{~kJ} / \mathrm{mol}$, which corresponds to the standard enthalpy change for the hypothetical reaction

$$
\mathrm{C}(s)+2 \mathrm{H}_{2}(g) \longrightarrow \mathrm{CH}_{4}(g) \quad \Delta H^{\circ}=-74.8 \mathrm{~kJ}
$$

Second, each substance in the reaction must be in its most stable, standard form at 1 atm pressure and the specified temperature (usually $25^{\circ} \mathrm{C}$ ). Carbon, for example, is most stable as solid graphite rather than diamond under these conditions, and hydrogen is most stable as gaseous $\mathrm{H}_{2}$ molecules rather than H atoms. Table 8.2 gives standard heats of formation for some common substances, and Appendix B gives a more detailed list.



No elements are listed in Table 8.2 because, by definition, the most stable form of any element in its standard state has $\Delta H^{\circ}=0 \mathrm{~kJ}$. (That is, the enthalpy change for formation of an element from itself is zero.) Defining $\Delta H^{\circ}{ }_{\mathrm{f}}$ as zero for all elements thus establishes a kind of thermochemical "sea level," or reference point, from which all enthalpy changes are measured.

How can standard heats of formation be used for thermochemical calculations? The standard enthalpy change for any chemical reaction is found by subtracting the sum of the heats of formation of all reactants from the sum of the heats of formation of all products, with each heat of formation multiplied by the coefficient of that substance in the balanced equation.

$$
\Delta H_{\text {reaction }}^{\circ}=\Delta H_{\mathrm{f}}^{\circ}(\text { Products })-\Delta H_{\mathrm{f}}^{\circ}(\text { Reactants })
$$

## -



A Fermentation of the sugar from grapes yields the ethyl alcohol in wine.

To find $\Delta H^{\circ}$ for the reaction

$\Delta H^{\circ}{ }_{\text {reaction }}=\left[c \Delta H^{\circ}{ }_{\mathrm{f}}(\mathrm{C})+d \Delta H^{\circ}{ }_{\mathrm{f}}(\mathrm{D})+\cdots\right]-\left[a \Delta H^{\circ}{ }_{\mathrm{f}}(\mathrm{A})+b \Delta H^{\circ}{ }_{\mathrm{f}}(\mathrm{B})+\cdots\right]$

For example, let's calculate $\Delta H^{\circ}$ for the fermentation of glucose to make ethyl alcohol (ethanol), the reaction that occurs during the production of alcoholic beverages:

$$
\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s) \longrightarrow 2 \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(l)+2 \mathrm{CO}_{2}(g) \quad \Delta H^{\circ}=?
$$

Using the data in Table 8.2 gives the following answer:

$$
\begin{aligned}
\Delta H^{\circ} & =\left[2 \Delta H_{\mathrm{f}}^{\circ}(\text { Ethanol })+2 \Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{CO}_{2}\right)\right]-\left[\Delta H_{\mathrm{f}}^{\circ}(\text { Glucose })\right] \\
& =(2 \mathrm{~mol})(-277.7 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})-(1 \mathrm{~mol})(-1260 \mathrm{~kJ} / \mathrm{mol}) \\
& =-82 \mathrm{~kJ}
\end{aligned}
$$

The fermentation reaction is exothermic by 82 kJ .
Why does this calculation "work"? It works because it's really just another application of Hess's law. That is, the sum of the individual equations corresponding to the heat of formation for each substance in the reaction equals the enthalpy change for the overall reaction:

| (1) | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s) \longrightarrow 6 \mathrm{C}(\mathrm{s})+6 \mathrm{H}_{2}(g)+3 \mathrm{O}_{2}(g)$ | $-\Delta H^{\circ}{ }_{\mathrm{f}}=+1260 \mathrm{~kJ}$ |
| :---: | :---: | :---: |
| (2) | $2\left[2 \mathrm{C}(\mathrm{s})+3 \mathrm{H}_{2}(g)+1 / 2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(l)\right]$ | $2\left[\Delta H_{\mathrm{f}}^{\circ}=-277.7 \mathrm{~kJ}\right]=-555.4 \mathrm{~kJ}$ |
| (3) | $2\left[\ell(s)+O_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)\right]$ | $2\left[\Delta H_{\mathrm{f}}^{\circ}=-393.5 \mathrm{~kJ}\right]=-787.0 \mathrm{~kJ}$ |
| Net | $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s) \longrightarrow 2 \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(l)+2 \mathrm{CO}_{2}(g)$ | $\Delta H^{\circ}=-82 \mathrm{~kJ}$ |

Note that reaction (1) represents the formation of glucose from its elements written in reverse, so the sign of $\Delta H^{\circ}{ }_{f}$ is reversed. Note also that reactions (2) and (3), which represent the formation of ethyl alcohol and carbon dioxide, respectively, are multiplied by 2 to arrive at the balanced equation.

When we use heats of formation to calculate standard reaction enthalpies, what we're really doing is referencing the enthalpies of both products and reactants to the same point-their constituent elements. By thus referencing product and reactant enthalpies to the same point, they are referenced to one another and the difference between them is the reaction enthalpy (Figure 8.11). Worked Examples 8.8 and 8.9 further illustrate how to use standard heats of formation.

FIGURE 8.11 The standard reaction enthalpy, $\Delta H^{\circ}$, for the generalized reaction $A \rightarrow B$ is the difference between the standard heats of formation of products and reactants. Because the different heats of formation are referenced to the same point (the constituent elements), they are thereby referenced to each other.

## Worked Example 8.8

Calculate $\Delta H^{\circ}$ (in kilojoules) for the synthesis of lime $(\mathrm{CaO})$ from limestone $\left(\mathrm{CaCO}_{3}\right)$, an important step in the manufacture of cement.

$$
\begin{aligned}
\mathrm{CaCO}_{3}(s) \longrightarrow \mathrm{CaO}(s)+\mathrm{CO}_{2}(g) \quad & \Delta H_{\mathrm{f}}^{\circ}\left[\mathrm{CaCO}_{3}(s)\right]=-1206.9 \mathrm{~kJ} / \mathrm{mol} \\
& \Delta H^{\circ}[\mathrm{CaO}(s)]=-635.1 \mathrm{~kJ} / \mathrm{mol} \\
& \Delta H^{\circ}\left[\mathrm{CO}_{2}(g)\right]=-393.5 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

## Strategy

Subtract the heat of formation of the reactant from the sum of the heats of formation of the products.

## Solution

$$
\begin{aligned}
\Delta H^{\circ} & =\left[\Delta H_{\mathrm{f}}^{\circ}(\mathrm{CaO})+\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{CO}_{2}\right)\right]-\left[\Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{CaCO}_{3}\right)\right] \\
& =(1 \mathrm{~mol})(-635.1 \mathrm{~kJ} / \mathrm{mol})+(1 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})-(1 \mathrm{~mol})(-1206.9 \mathrm{~kJ} / \mathrm{mol}) \\
& =178.3 \mathrm{~kJ}
\end{aligned}
$$

The reaction is endothermic by 178.3 kJ .

## Worked Example 8.9

Oxyacetylene welding torches burn acetylene gas, $\mathrm{C}_{2} \mathrm{H}_{2}(g)$. Use the information in Table 8.2 to calculate $\Delta H^{\circ}$ (in kilojoules) for the combustion reaction of acetylene to yield $\mathrm{CO}_{2}(g)$ and $\mathrm{H}_{2} \mathrm{O}(g)$.

## Strategy

Write the balanced equation, look up the appropriate heats of formation for each reactant and product in Table 8.2, and then carry out the calculation, making sure to multiply each $\Delta H^{\circ}$ fy the coefficient given in the balanced equation. Remember also that $\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{O}_{2}\right)=0 \mathrm{~kJ} / \mathrm{mol}$.

## Solution

The balanced equation is

$$
2 \mathrm{C}_{2} \mathrm{H}_{2}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 4 \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)
$$

The necessary heats of formation are

$$
\begin{aligned}
& \Delta H^{\circ}{ }_{\mathrm{f}}\left[\mathrm{C}_{2} \mathrm{H}_{2}(g)\right]=226.7 \mathrm{~kJ} / \mathrm{mol} \quad \Delta H^{\circ}{ }_{\mathrm{f}}\left[\mathrm{H}_{2} \mathrm{O}(g)\right]=-241.8 \mathrm{~kJ} / \mathrm{mol} \\
& \Delta H^{\circ}{ }_{\mathrm{f}}\left[\mathrm{CO}_{2}(g)\right]=-393.5 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

The standard enthalpy change for the reaction is

$$
\begin{aligned}
\Delta H^{\circ} & =\left[4 \Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{CO}_{2}\right)+2 \Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]-\left[2 \Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{C}_{2} \mathrm{H}_{2}\right)\right] \\
& =(4 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(-241.8 \mathrm{~kJ} / \mathrm{mol})-(2 \mathrm{~mol})(226.7 \mathrm{~kJ} / \mathrm{mol}) \\
& =-2511.0 \mathrm{~kJ}
\end{aligned}
$$



A Acetylene burns at a high temperature, making the reaction useful for welding.

PROBLEM 8.16 Use the information in Table 8.2 to calculate $\Delta H^{\circ}$ (in kilojoules) for the reaction of ammonia with $\mathrm{O}_{2}$ to yield nitric oxide (NO) and $\mathrm{H}_{2} \mathrm{O}(g)$, a step in the Ostwald process for the commercial production of nitric acid.

PROBLEM 8.17 Use the information in Table 8.2 to calculate $\Delta H^{\circ}$ (in kilojoules) for the photosynthesis of glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ from $\mathrm{CO}_{2}$ and liquid $\mathrm{H}_{2} \mathrm{O}$, a reaction carried out by all green plants.

Bond dissociation energies are defined for isolated, gaseous-state species. Other factors must be considered when dealing with condensed-state systems.

4 Reactant bonds are broken and product bonds are formed: $\Delta H^{\circ}=D$ (reactant bonds broken) - $D$ (product bonds formed). Students should not confuse this equation with that used for heats of formation: $\Delta H^{\circ}=\Delta H^{\circ}{ }_{\mathrm{f}}($ products $)-$ $\Delta H^{\circ}{ }_{\mathrm{f}}$ (reactants), in which products and reactants appear on the opposite side of the minus sign.

## Bond Dissociation activity

### 8.11 Bond Dissociation Energies

The procedure described in the previous section for determining heats of reaction from heats of formation is extremely useful, but it still presents a major problem. To use the method, it's necessary to know $\Delta H^{\circ}$ for every substance in a reaction. This implies, in turn, that vast numbers of measurements are needed, since there are over 18 million known chemical compounds. In practice, though, only a few thousand $\Delta H^{\circ}{ }_{\mathrm{f}}$ values have been determined.

For those reactions where insufficient $\Delta H^{\circ}{ }_{\mathrm{f}}$ data are available to allow an exact calculation of $\Delta H^{\circ}$, it's often possible to get an approximate answer by using the average bond dissociation energies $(D)$ discussed previously in Section 7.2. Although we didn't identify it as such at the time, a bond dissociation energy is really just a standard enthalpy change, $\Delta H^{\circ}$, for the corresponding bond-breaking reaction.

For the reaction $\mathrm{X}-\mathrm{Y} \longrightarrow \mathrm{X}+\mathrm{Y} \quad \Delta H^{\circ}=D=$ Bond dissociation energy
When we say, for example, that $\mathrm{Cl}_{2}$ has a bond dissociation energy $D=$ $243 \mathrm{~kJ} / \mathrm{mol}$, we mean that the standard enthalpy change for the reaction $\mathrm{Cl}_{2}(g) \rightarrow 2 \mathrm{Cl}(g)$ is $\Delta H^{\circ}=243 \mathrm{~kJ}$. Bond dissociation energies are always positive because energy must always be put into a bond to break it.

Applying Hess's law, we can calculate an approximate enthalpy change for any reaction by subtracting the total energy of bonds in the products from the total energy of bonds in the reactants:

$$
\left.\Delta H^{\circ}=D(\text { Reactant bonds })-D \text { (Product bonds }\right)
$$

In the reaction of $\mathrm{H}_{2}$ with $\mathrm{Cl}_{2}$ to yield HCl , for example, the reactants have one $\mathrm{Cl}-\mathrm{Cl}$ bond and one $\mathrm{H}-\mathrm{H}$ bond, while the product has two $\mathrm{H}-\mathrm{Cl}$ bonds. According to the data in Table 7.1 (page 246), the bond dissociation energy of $\mathrm{Cl}_{2}$ is $243 \mathrm{~kJ} / \mathrm{mol}$, that of $\mathrm{H}_{2}$ is $436 \mathrm{~kJ} / \mathrm{mol}$, and that of HCl is $432 \mathrm{~kJ} / \mathrm{mol}$. We can thus calculate an approximate standard enthalpy change for the reaction.

$$
\begin{aligned}
\Delta H^{\circ} & =D(\text { Reactant bonds })-D(\text { Product bonds }) \\
& =\left(D_{\mathrm{Cl}-\mathrm{Cl}}+D_{\mathrm{H}-\mathrm{H}}\right)-\left(2 D_{\mathrm{H}-\mathrm{Cl}}\right) \\
& =[(1 \mathrm{~mol})(243 \mathrm{~kJ} / \mathrm{mol})+(1 \mathrm{~mol})(436 \mathrm{~kJ} / \mathrm{mol})]-(2 \mathrm{~mol})(432 \mathrm{~kJ} / \mathrm{mol}) \\
& =-185 \mathrm{~kJ}
\end{aligned}
$$

The reaction is exothermic by approximately 185 kJ .

## Worked Example 8.10

Use the data in Table 7.1 to find an approximate $\Delta H^{\circ}$ (in kilojoules) for the industrial synthesis of chloroform by reaction of methane with $\mathrm{Cl}_{2}$.

$$
\mathrm{CH}_{4}(g)+3 \mathrm{Cl}_{2}(g) \longrightarrow \mathrm{CHCl}_{3}(g)+3 \mathrm{HCl}(g)
$$

## Strategy

Identify all the bonds in the reactants and products, and look up the appropriate bond dissociation energies in Table 7.1. Then subtract the total energy of the product bonds from the total energy of the reactant bonds to find the enthalpy change for the reaction.

## Solution

The reactants have four $\mathrm{C}-\mathrm{H}$ bonds and three $\mathrm{Cl}-\mathrm{Cl}$ bonds; the products have one $\mathrm{C}-\mathrm{H}$ bond, three $\mathrm{C}-\mathrm{Cl}$ bonds, and three $\mathrm{H}-\mathrm{Cl}$ bonds. The bond dissociation energies from Table 7.1 are:

$$
\begin{array}{ll}
\mathrm{C}-\mathrm{H} & D=410 \mathrm{~kJ} / \mathrm{mol} \\
\mathrm{C}-\mathrm{Cl} & D=330 \mathrm{~kJ} / \mathrm{mol}
\end{array}
$$

Subtracting the total energy of the product bonds from the total energy of the reactant bonds gives the enthalpy change for the reaction:

$$
\begin{aligned}
\Delta H^{\circ} & =\left[3 D_{\mathrm{Cl}-\mathrm{Cl}}+4 D_{\mathrm{C}-\mathrm{H}}\right]-\left[D_{\mathrm{C}-\mathrm{H}}+3 D_{\mathrm{H}-\mathrm{Cl}}+3 D_{\mathrm{C}-\mathrm{Cl}}\right] \\
& =[(3 \mathrm{~mol})(243 \mathrm{~kJ} / \mathrm{mol})+(4 \mathrm{~mol})(410 \mathrm{~kJ} / \mathrm{mol})]-[(1 \mathrm{~mol})(410 \mathrm{~kJ} / \mathrm{mol})+ \\
& =-327 \mathrm{~kJ}
\end{aligned}
$$

The reaction is exothermic by approximately 330 kJ .

- PROBLEM 8.18 Use the data in Table 7.1 to calculate an approximate $\Delta H^{\circ}$ (in kilojoules) for the industrial synthesis of ethyl alcohol from ethylene: $\mathrm{C}_{2} \mathrm{H}_{4}(g)+$ $\mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(g)$.
- PROBLEM 8.19 Use the data in Table 7.1 to calculate an approximate $\Delta H^{\circ}$ (in kilojoules) for the synthesis of hydrazine from ammonia: $2 \mathrm{NH}_{3}(g)+\mathrm{Cl}_{2}(g) \rightarrow$ $\mathrm{N}_{2} \mathrm{H}_{4}(g)+2 \mathrm{HCl}(g)$.


### 8.12 Fossil Fuels, Fuel Efficiency, and Heats of Combustion

Surely the most familiar of all exothermic reactions is the one that takes place every time we turn up a thermostat, drive a car, or light a match-the burning of a carbon-based fuel by reaction with oxygen to yield $\mathrm{H}_{2} \mathrm{O}, \mathrm{CO}_{2}$, and heat. The amount of energy released on burning a substance is called its heat of combustion, or combustion enthalpy, $\Delta H^{\circ}{ }_{\text {c }}$, which is simply the standard enthalpy change for the reaction of 1 mol of the substance with oxygen. Hydrogen, for instance, has $\Delta H^{\circ}{ }_{\mathrm{C}}=-285.8 \mathrm{~kJ} / \mathrm{mol}$, and methane has $\Delta H^{\circ}{ }_{\mathrm{c}}=-890.3 \mathrm{~kJ} / \mathrm{mol}$. Note that the $\mathrm{H}_{2} \mathrm{O}$ product is liquid rather than vapor.

$$
\begin{aligned}
& \mathrm{H}_{2}(g)+1 / 2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l) \\
& \mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l) \\
& \Delta H^{\circ}{ }_{\mathrm{C}}=-285.8 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

To compare the efficiency of different fuels, it's more useful to calculate combustion enthalpies per gram or per milliliter of substance rather than per mole (Table 8.3). For applications where weight is important, as in rocket engines, hydrogen is ideal because its combustion enthalpy per gram is the highest of any known fuel. For applications where volume is important, as in automobiles, a mixture of hydrocarbons such as those in gasoline is most efficient because hydrocarbon combustion enthalpies per milliliter are relatively high. Octane and toluene are representative examples.

TABLE 8.3 Thermochemical Properties of Some Fuels
Combustion Enthalpy

| Fuel | $\mathbf{k J / m o l}$ | $\mathbf{k J} / \mathbf{g}$ | $\mathbf{k J} / \mathbf{m L}$ |
| :--- | :---: | :---: | :---: |
| Hydrogen, $\mathrm{H}_{2}$ | -285.8 | -141.8 | $-9.9^{*}$ |
| Ethanol, $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ | -1367 | -29.7 | -23.4 |
| Graphite, C | -393.5 | -32.8 | -73.8 |
| Methane, $\mathrm{CH}_{4}$ | -890.3 | -55.5 | $-30.8^{*}$ |
| Methanol, $\mathrm{CH}_{3} \mathrm{OH}$ | -726.4 | -22.7 | -17.9 |
| Octane, $\mathrm{C}_{8} \mathrm{H}_{18}$ | -5470 | -47.9 | -33.6 |
| Toluene, $\mathrm{C}_{7} \mathrm{H}_{8}$ | -3910 | -42.3 | -36.7 |

*Calculated for the compressed liquid at $0^{\circ} \mathrm{C}$


Ethyl alcohol

Donald J. Wink, "The Conversion of Chemical Energy. Part 1. Technological Examples," J. Chem. Educ., Vol. 69, 1992, 108-111.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Making Canned Heat," Chemical Demonstrations, A Sourcebook for Teaches, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 111-112.
7. Gustav P. Dinga, "Hydrogen: The Ultimate Fuel and Energy Carrier," J. Chem. Educ., Vol. 65, 1988, 688-691.

Israel Dostrovsky, "Chemical Fuels from the Sun," Scientific American., Vol. 265, 1991, pp. 102-107.

Harold H. Schobert, "The Geochemistry of Coal. Part II: The Components of Coal," J. Chem. Educ., Vol. 66, 1989, 290-293.


A Much coal lies near the surface of the earth and is obtained by strip mining.

With the exception of hydrogen, all common fuels are organic compounds whose energy is derived ultimately from the sun through the photosynthesis of carbohydrates in green plants. Though the details are complex, the net result of the photosynthesis reaction is the conversion of carbon dioxide and water into glucose, $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}$. Glucose, once formed, is converted into cellulose and starch, which in turn act as structural materials for plants and as food sources for animals. The conversion is highly endothermic and therefore requires a large input of solar energy. It has been estimated that the total annual amount of solar energy absorbed by the earth's vegetation is approximately $10^{19} \mathrm{~kJ}$, an amount sufficient to synthesize $5 \times 10^{14} \mathrm{~kg}$ of glucose per year.

$$
6 \mathrm{CO}_{2}(g)+6 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s)+6 \mathrm{O}_{2}(g) \quad \Delta H^{\circ}=2816 \mathrm{~kJ}
$$

The so-called fossil fuels we use most-coal, natural gas, and petroleum-are thought to be the decayed remains of organisms from previous geologic eras. Both coal and petroleum are enormously complex mixtures of compounds. Coal is primarily of vegetable origin, and many of the compounds it contains are structurally similar to graphite (pure carbon). Petroleum is a viscous liquid mixture of hydrocarbonscompounds of carbon and hydrogen-that are primarily of marine origin.

Coal is burned just as it comes from the mine, but petroleum must be refined before use. Refining begins with distillation-the separation of crude liquid oil into fractions on the basis of their boiling points. So-called straight-run gasoline (bp $30-200^{\circ} \mathrm{C}$ ) consists of compounds with 5-11 carbon atoms per molecule; kerosene (bp $175-300^{\circ} \mathrm{C}$ ) contains compounds in the $\mathrm{C}_{11}-\mathrm{C}_{14}$ range; gas oil (bp 275-400 ${ }^{\circ} \mathrm{C}$ ) contains $\mathrm{C}_{14}-\mathrm{C}_{25}$ substances; and lubricating oils contain whatever remaining compounds will distill. Left over is a tarry residue of asphalt (Figure 8.12).

FIGURE 8.12 The products of petroleum refining. The different fractions are grouped according to the number of carbon atoms their molecules contain.


As the world's petroleum deposits become ever more scarce, other sources of energy will have to be found to replace them. Hydrogen, although it burns cleanly and is relatively nonpolluting, has two drawbacks: low availability and low combustion enthalpy per milliliter. Ethanol and methanol look like good current choices for alternative fuels because both can be produced relatively cheaply and
have reasonable combustion enthalpies. Ethanol can be produced from wood by the breakdown of cellulose to glucose and subsequent fermentation. Methanol is produced directly from natural gas by a two-step process:

$$
\begin{aligned}
\mathrm{CH}_{4}(g)+\mathrm{H}_{2} \mathrm{O}(g) & \longrightarrow \mathrm{CO}(g)+3 \mathrm{H}_{2}(g) \\
\mathrm{CO}(g)+2 \mathrm{H}_{2}(g) & \longrightarrow \mathrm{CH}_{3} \mathrm{OH}(l)
\end{aligned}
$$

- PROBLEM 8.20 Liquid butane ( $\mathrm{C}_{4} \mathrm{H}_{10}$ ), the fuel used in many disposable lighters, has $\Delta H^{\circ}{ }_{\mathrm{f}}=-147.5 \mathrm{~kJ} / \mathrm{mol}$ and a density of $0.579 \mathrm{~g} / \mathrm{mL}$. Write a balanced equation for the combustion of butane, and use Hess's law to calculate the enthalpy of combustion in $\mathrm{kJ} / \mathrm{mol}, \mathrm{kJ} / \mathrm{g}$, and $\mathrm{kJ} / \mathrm{mL}$.


### 8.13 An Introduction to Entropy

We've said on several occasions that chemical and physical processes occur spontaneously only if they go "downhill" energetically so that the final state is more stable and has less energy than the initial state. In other words, energy must be released for a process to occur spontaneously. At the same time, though, we've said that some processes occur perfectly well even though they are endothermic and absorb heat. The reaction of barium hydroxide octahydrate with ammonium chloride shown in Figure 8.6, for example, absorbs 80.3 kJ of heat ( $\Delta H^{\circ}=+80.3 \mathrm{~kJ}$ ) and leaves the surroundings so cold that moisture freezes around the outside of the container.

$$
\begin{array}{r}
\mathrm{Ba}(\mathrm{OH})_{2} \cdot 8 \mathrm{H}_{2} \mathrm{O}(s)+2 \mathrm{NH}_{4} \mathrm{Cl}(s) \longrightarrow \mathrm{BaCl}_{2}(a q)+2 \mathrm{NH}_{3}(a q)+10 \mathrm{H}_{2} \mathrm{O}(l) \\
\Delta H^{\circ}=+80.3 \mathrm{~kJ}
\end{array}
$$

What's going on? How can the spontaneous reaction of barium hydroxide octahydrate with ammonium chloride release energy yet absorb heat? The answer is that, in the context of a chemical reaction, the words "energy" and "heat" don't refer to exactly the same thing. There is another factor in addition to heat that determines whether energy is released and thus determines whether a reaction takes place spontaneously. We'll take only a brief look at this additional factor right now and return for a more in-depth study in Chapter 17.

Before exploring the situation further, it's important to understand what the word spontaneous means in chemistry, for it's not the same as in everyday language. In chemistry, a spontaneous process is one that proceeds on its own without a continuous external influence. The change need not happen quickly, like a spring uncoiling or a rock rolling downhill. It can also happen slowly, like the gradual rusting away of a bridge or abandoned car. A nonspontaneous process, by contrast, takes place only in the presence of a continuous external influence. Energy must be continuously expended to re-coil a spring or to push a rock uphill. When the external influence stops, the process also stops. The reverse of any spontaneous process is always nonspontaneous.

As another example of a process that takes place spontaneously yet absorbs heat, think about what happens when an ice cube melts. At a temperature of $0^{\circ} \mathrm{C}$, ice spontaneously absorbs heat from the surroundings to turn from solid into liquid water without changing temperature.

What do a melting ice cube and the reaction of barium hydroxide octahydrate have in common? The common feature of these and all other spontaneous processes that absorb heat is an increase in the amount of molecular disorder, or randomness, of the system. The eight water molecules rigidly held in the $\mathrm{Ba}(\mathrm{OH})_{2} \cdot 8 \mathrm{H}_{2} \mathrm{O}$ crystal break loose and become free to move about in the aqueous liquid product; similarly, the rigidly held $\mathrm{H}_{2} \mathrm{O}$ molecules in the ice lose their crystalline ordering and move around more freely in liquid water.


John J. Fortman, "Pictorial Analogies III: Heat Flow, Thermodynamics, and Entropy," J. Chem. Educ., Vol. 70, 1993, 102-103.


- Sledding downhill is a spontaneous process that, once started, continues on its own. Hauling the sled back uphill is a nonspontaneous process that requires a continuous input of energy.

FIGURE 8.13 Entropy is a measure of molecular randomness, or disorder. Gases have more randomness and higher entropy than liquids, which in turn have more randomness and higher entropy than solids.

The amount of molecular randomness in a system is called the system's entropy (S). Entropy has the units J/K (joules per kelvin, not kilojoules per kelvin) and is a quantity that can be determined for pure substances, as we'll see in Section 17.5. The larger the value of $S$, the greater the molecular randomness of the particles in the system. Gases, for example, have more randomness and higher entropy than liquids, and liquids have more randomness and higher entropy than solids (Figure 8.13).


A change in entropy is represented as $\Delta S$. When randomness increases, as it does when barium hydroxide octahydrate reacts or ice melts, $\Delta S$ has a positive value. The reaction of $\mathrm{Ba}(\mathrm{OH})_{2} \cdot 8 \mathrm{H}_{2} \mathrm{O}(s)$ with $\mathrm{NH}_{4} \mathrm{Cl}(s)$ has $\Delta S^{\circ}=+428 \mathrm{~J} / \mathrm{K}$, and the melting of ice has $\Delta S^{\circ}=+22.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. When randomness decreases, $\Delta S$ is negative. The freezing of water, for example, has $\Delta S^{\circ}=-22.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. (As with $\Delta H^{\circ}$, the superscript ${ }^{\circ}$ is used in $\Delta S^{\circ}$ to refer to the standard entropy change in a reaction where all products and reactants are in their standard states.)

$$
\Delta S=S_{\text {final }}-S_{\text {initial }}
$$

If $\Delta S$ is positive, the system has become more random ( $S_{\text {final }}>S_{\text {initial }}$ ). If $\Delta S$ is negative, the system has become less random $\left(S_{\text {final }}<S_{\text {initial }}\right)$.

Two factors determine the spontaneity of a chemical or physical change in a system: a release or absorption of heat $(\Delta H)$ and an increase or decrease in molecular randomness $(\Delta S)$. To decide whether a process is spontaneous, both enthalpy and entropy changes must be taken into account:

Favored by decrease in $H$ (negative $\Delta H$ ) Favored by increase in $S$ (positive $\Delta S$ )

Favored by increase in $H$ (positive $\Delta H$ ) Favored by decrease in $S$ (negative $\Delta S$ )

Note that the two factors don't have to operate in the same direction. It's possible for a process to be disfavored by enthalpy (endothermic, positive $\Delta H$ ) yet still be spontaneous, because it is strongly favored by entropy (positive $\Delta S$ ). The melting of ice $\left[\Delta H^{\circ}=+6.01 \mathrm{~kJ} / \mathrm{mol} ; \Delta S^{\circ}=+22.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})\right.$ ] is just such a process, as is the reaction of barium hydroxide octahydrate with ammonium chloride $\left(\Delta H^{\circ}=+80.3 \mathrm{~kJ} ; \Delta S^{\circ}=+428 \mathrm{~J} / \mathrm{K}\right)$. In the latter case, 3 mol of solid reactants produce 10 mol of liquid water, 2 mol of dissolved ammonia, and 3 mol of dissolved ions ( 1 mol of $\mathrm{Ba}^{2+}$ and 2 mol of $\mathrm{Cl}^{-}$), with a consequent large increase in molecular randomness:


Conversely, it's also possible for a process to be favored by enthalpy (exothermic, negative $\Delta H$ ) yet be nonspontaneous, because it is strongly disfavored by entropy (negative $\Delta S$ ). The conversion of liquid water to ice is nonspontaneous above $0^{\circ} \mathrm{C}$, for example, because the process is disfavored by entropy [ $\Delta S^{\circ}=$ $-22.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ ] even though it is favored by enthalpy $\left(\Delta H^{\circ}=-6.01 \mathrm{~kJ} / \mathrm{mol}\right)$.

## Worked Example 8.11

Predict whether $\Delta S^{\circ}$ is likely to be positive or negative for each of the following reactions:
(a) $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}(g)+\mathrm{Br}_{2}(g) \rightarrow \mathrm{CH}_{2} \mathrm{BrCH}_{2} \mathrm{Br}(l)$
(b) $2 \mathrm{C}_{2} \mathrm{H}_{6}(g)+7 \mathrm{O}_{2}(g) \rightarrow 4 \mathrm{CO}_{2}(g)+6 \mathrm{H}_{2} \mathrm{O}(g)$

## Strategy

Look at each reaction and try to decide whether molecular randomness increases or decreases. Reactions that increase the number of gaseous molecules generally have a positive $\Delta S$, while reactions that decrease the number of gaseous molecules have a negative $\Delta S$.

## Solution

(a) The amount of molecular randomness in the system decreases when 2 mol of gaseous reactants combine to give 1 mol of liquid product, so the reaction has a negative $\Delta S^{\circ}$.
(b) The amount of molecular randomness in the system increases when 9 mol of gaseous reactants give 10 mol of gaseous products, so the reaction has a positive $\Delta S^{\circ}$.

- PROBLEM 8.21 Ethane, $\mathrm{C}_{2} \mathrm{H}_{6}$, can be prepared by the reaction of acetylene, $\mathrm{C}_{2} \mathrm{H}_{2}$, with hydrogen:

$$
\mathrm{C}_{2} \mathrm{H}_{2}(g)+2 \mathrm{H}_{2}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{6}(g)
$$

Do you expect $\Delta S^{\circ}$ for the reaction to be positive or negative? Explain.

- KEY CONCEPT PROBLEM 8.22 Is the reaction represented in the following drawing likely to have a positive or a negative value of $\Delta S^{\circ}$ ? Explain.


Formation of Water movie; Formation of Water activity

Gibb's Free Energy activity

FIGURE 8.14 The melting of ice is disfavored by enthalpy $(+\Delta H)$ but favored by entropy $(+\Delta S)$. The freezing of water is favored by enthalpy $(-\Delta H)$ but disfavored by entropy $(-\Delta S)$. Below $0^{\circ} \mathrm{C}$, the enthalpy term $\Delta H$ dominates the entropy term $T \Delta S$ in the Gibbs free-energy equation, so freezing is spontaneous. Above $0^{\circ} \mathrm{C}$, the entropy term dominates the enthalpy term, so melting is spontaneous. At $0^{\circ} \mathrm{C}$, the entropy and enthalpy terms are in balance.

### 8.14 An Introduction to Free Energy

How do we weigh the contributions of changes in both heat $(\Delta H)$ and randomness $(\Delta S)$ to the overall spontaneity of a process? To take both factors into account when deciding the spontaneity of a chemical reaction or other process, we define a quantity called the Gibbs free-energy change $(\Delta G), \Delta G=\Delta H-T \Delta S$.


The value of the free-energy change $\Delta G$ is a general criterion for the spontaneity of a chemical or physical process. If $\Delta G$ has a negative value, the process is spontaneous; if $\Delta G$ has a value of 0 , the process is neither spontaneous nor nonspontaneous but is instead at an equilibrium; and if $\Delta G$ has a positive value, the process is nonspontaneous.
$\Delta G<0 \quad$ Process is spontaneous
$\Delta G=0 \quad$ Process is at equilibrium—neither spontaneous nor nonspontaneous
$\Delta G>0 \quad$ Process is nonspontaneous
The fact that the $T \Delta S$ term in the Gibbs free-energy equation is temperaturedependent implies that some processes might be either spontaneous or nonspontaneous, depending on the temperature. At low temperature, for instance, an unfavorable (positive) $\Delta H$ term might be larger than a favorable (positive) $T \Delta S$ term, but at higher temperature, the $T \Delta S$ term might be larger. Thus, an endothermic process that is nonspontaneous at low temperature can become spontaneous at higher temperature. This, in fact, is exactly what happens in the ice/water transition. At a temperature below $0^{\circ} \mathrm{C}$, melting is nonspontaneous because the unfavorable $\Delta H$ term outweighs the favorable $T \Delta S$ term. At a temperature above $0^{\circ} \mathrm{C}$, however, the melting of ice is spontaneous because the favorable $T \Delta S$ term outweighs the unfavorable $\Delta H$ term (Figure 8.14). Exactly at $0^{\circ} \mathrm{C}$, the two terms are balanced.

$$
\begin{aligned}
& \Delta G^{\circ}=\Delta H^{\circ}-T \Delta S^{\circ} \\
& \text { At }-10^{\circ} \mathrm{C}(263 \mathrm{~K}): \quad \Delta G^{\circ}=6.01 \frac{\mathrm{~kJ}}{\mathrm{~mol}}-(263 \mathrm{~K})\left(0.0220 \frac{\mathrm{~kJ}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)=+0.22 \mathrm{~kJ} / \mathrm{mol} \\
& \text { At } 0^{\circ} \mathrm{C}(273 \mathrm{~K}): \quad \Delta G^{\circ}=6.01 \frac{\mathrm{~kJ}}{\mathrm{~mol}}-(273 \mathrm{~K})\left(0.0220 \frac{\mathrm{~kJ}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)=0.00 \mathrm{~kJ} / \mathrm{mol} \\
& \text { At }+10^{\circ} \mathrm{C}(283 \mathrm{~K}): \quad \Delta G^{\circ}=6.01 \frac{\mathrm{~kJ}}{\mathrm{~mol}}-(283 \mathrm{~K})\left(0.0220 \frac{\mathrm{~kJ}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)=-0.22 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$



Solid water


An example of a chemical reaction in which temperature controls spontaneity is that of carbon with water to yield carbon monoxide and hydrogen. The reaction has an unfavorable $\Delta H$ term (positive) but a favorable $T \Delta S$ term (positive) because randomness increases when a solid and a gas are converted into two gases:

$$
\begin{aligned}
\mathrm{C}(s)+\mathrm{H}_{2} \mathrm{O}(g) \longrightarrow \mathrm{CO}(g)+\mathrm{H}_{2}(g) & \Delta H^{\circ}=+131 \mathrm{~kJ} \quad \text { (Unfavorable) } \\
\Delta S^{\circ}=+134 \mathrm{~J} / \mathrm{K} & \text { (Favorable) }
\end{aligned}
$$

No reaction occurs if carbon and water are mixed at room temperature ( 300 K ) because the unfavorable $\Delta H$ term outweighs the favorable $T \Delta S$ term. At approximately $978 \mathrm{~K}\left(705^{\circ} \mathrm{C}\right)$, however, the reaction becomes spontaneous because the favorable $T \Delta S$ term becomes larger than the unfavorable $\Delta H$ term. Below $978 \mathrm{~K}, \Delta \mathrm{G}$ has a positive value; at $978 \mathrm{~K}, \Delta \mathrm{G}=0$; and above $978 \mathrm{~K}, \Delta \mathrm{G}$ has a negative value (The calculation is not exact because values of $\Delta H$ and $\Delta S$ vary somewhat with temperature.)

$$
\begin{array}{cl}
\Delta G^{\circ}=\Delta H^{\circ}-T \Delta S^{\circ} \\
\text { At } 695^{\circ} \mathrm{C}(968 \mathrm{~K}): \quad \Delta G^{\circ}=131 \mathrm{~kJ}-(968 \mathrm{~K})\left(0.134 \frac{\mathrm{~kJ}}{\mathrm{~K}}\right)=+1 \mathrm{~kJ} \\
\text { At } 705^{\circ} \mathrm{C}(978 \mathrm{~K}): \quad \Delta G^{\circ}=131 \mathrm{~kJ}-(978 \mathrm{~K})\left(0.134 \frac{\mathrm{~kJ}}{\mathrm{~K}}\right)=0 \mathrm{~kJ} \\
\text { At } 715^{\circ} \mathrm{C}(988 \mathrm{~K}): \quad \Delta G^{\circ}=131 \mathrm{~kJ}-(988 \mathrm{~K})\left(0.134 \frac{\mathrm{~kJ}}{\mathrm{~K}}\right)=-1 \mathrm{~kJ}
\end{array}
$$

The reaction of carbon with water is, in fact, the first step of an industrial process used to manufacture methanol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$. As supplies of natural gas and oil are used up, this reaction may become important for the manufacture of synthetic fuels.

A process is at equilibrium when it is balanced between spontaneous and non-spontaneous-that is, when $\Delta G=0$ and it is energetically unfavorable to go either from reactants to products or from products to reactants. Thus, at the equilibrium point, we can set up the equation

$$
\Delta G=\Delta H-T \Delta S=0 \quad \text { (At equilibrium) }
$$

Solving this equation for $T$ gives

$$
T=\frac{\Delta H}{\Delta S}
$$

which makes it possible to calculate the temperature at which a changeover in behavior between spontaneous and nonspontaneous occurs. Using the known values of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for the melting of ice, for instance, we find that the point at which liquid water and solid ice are in equilibrium is

$$
T=\frac{\Delta H^{\circ}}{\Delta S^{\circ}}=\frac{6.01 \mathrm{~kJ}}{0.0220 \frac{\mathrm{~kJ}}{\mathrm{~K}}}=273 \mathrm{~K}=0^{\circ} \mathrm{C}
$$

Not surprisingly, the ice/water equilibrium point is 273 K , or $0^{\circ} \mathrm{C}$, the melting point of ice.

In the same way, the temperature at which the reaction of carbon with water changes between spontaneous and nonspontaneous is 978 K , or $705^{\circ} \mathrm{C}$ :

$$
T=\frac{\Delta H^{\circ}}{\Delta S^{\circ}}=\frac{131 \mathrm{~kJ}}{0.134 \frac{\mathrm{~kJ}}{\mathrm{~K}}}=978 \mathrm{~K}
$$

## Worked Example 8.12

Quicklime $(\mathrm{CaO})$ is produced by heating limestone $\left(\mathrm{CaCO}_{3}\right)$ to drive off $\mathrm{CO}_{2}$ gas. Is the reaction spontaneous under standard conditions at $25^{\circ} \mathrm{C}$ ? Calculate the temperature at which the reaction becomes spontaneous.

$$
\mathrm{CaCO}_{3}(s) \longrightarrow \mathrm{CaO}(s)+\mathrm{CO}_{2}(g) \quad \Delta H^{\circ}=178.3 \mathrm{~kJ} ; \Delta S^{\circ}=160 \mathrm{~J} / \mathrm{K}
$$

## Strategy

The spontaneity of the reaction at a given temperature can be found by determining whether $\Delta G$ is positive or negative at that temperature. The changeover point between spontaneous and nonspontaneous can be found by setting $\Delta G=0$ and solving for $T$.

## Solution

At $25^{\circ} \mathrm{C}$ ( 298 K ), we have

$$
\Delta G=\Delta H-T \Delta S=178.3 \mathrm{~kJ}-(298 \mathrm{~K})\left(0.160 \frac{\mathrm{~kJ}}{\mathrm{~K}}\right)=+130.6 \mathrm{~kJ}
$$

Because $\Delta G$ is positive at this temperature, the reaction is nonspontaneous.
The changeover point between spontaneous and nonspontaneous is:

$$
T=\frac{\Delta H}{\Delta S}=\frac{178.3 \mathrm{~kJ}}{0.160 \frac{\mathrm{~kJ}}{\mathrm{~K}}}=1114 \mathrm{~K}
$$

The reaction becomes spontaneous above $1114 \mathrm{~K}\left(841^{\circ} \mathrm{C}\right)$.

## Worked Key Concept Example 8.13

What are the signs of $\Delta H, \Delta S$, and $\Delta G$ for the following nonspontaneous transformation?


## Strategy

First, decide what kind of process is represented in the drawing. Then decide whether that process increases or decreases the entropy of system and whether it is exothermic or endothermic.

## Solution

The drawing shows ordered particles in a solid subliming to give a gas. Formation of a gas from a solid increases molecular disorder, so $\Delta S$ is positive. Furthermore, because we're told that the process is nonspontaneous, $\Delta G$ is also positive. Because the process is favored by $\Delta S$ (positive) yet still nonspontaneous, $\Delta H$ must be unfavorable (positive). This makes sense, since conversion of a solid to a liquid or gas requires energy and is always endothermic.

PROBLEM 8.23 Which of the following reactions are spontaneous under standard conditions at $25^{\circ} \mathrm{C}$, and which are nonspontaneous?
(a) $\mathrm{AgNO}_{3}(a q)+\mathrm{NaCl}(a q) \rightarrow \mathrm{AgCl}(s)+\mathrm{NaNO}_{3}(a q) ; \Delta G^{\circ}=-55.7 \mathrm{~kJ}$
(b) $2 \mathrm{C}(s)+2 \mathrm{H}_{2}(g) \rightarrow \mathrm{C}_{2} \mathrm{H}_{4}(g) ; \quad \Delta G^{\circ}=68.1 \mathrm{~kJ}$

PROBLEM 8.24 Is the Haber process for the industrial synthesis of ammonia spontaneous or nonspontaneous under standard conditions at $25^{\circ} \mathrm{C}$ ? At what temperature $\left({ }^{\circ} \mathrm{C}\right)$ does the changeover occur?

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g) \quad \Delta H^{\circ}=-92.2 \mathrm{~kJ} ; \Delta S^{\circ}=-199 \mathrm{~J} / \mathrm{K}
$$

- KEY CONCEPT PROBLEM 8.25 The following reaction is exothermic:

(a) Write a balanced equation for the reaction.
(b) What are the signs of $\Delta H$ and $\Delta S$ for the reaction?
(c) Is the reaction likely to be spontaneous at low temperatures only, at high temperatures only, or at all temperatures? Explain.


## Interlude Energy from Food

 550 Calories. Burning the dessert in a calorimeter would release 550 kcal as heat.
ny serious effort to lose weight usually leads to a study of the caloric values of foods. Where do the numbers quoted on food labels come from?
Food is "burned" in the body to yield $\mathrm{H}_{2} \mathrm{O}, \mathrm{CO}_{2}$, and energy, just as natural gas or coal is burned in a furnace to yield the same products. In fact, the "caloric value" of a food is just the heat of reaction, $\Delta H^{\circ}$, for complete combustion of the food (minus a small correction factor). The value is the same whether the food is burned in the body or in a laboratory calorimeter. One gram of protein releases $17 \mathrm{~kJ}(4 \mathrm{kcal}), 1 \mathrm{~g}$ of carbohydrate releases 17 kJ , and 1 g of fat releases 38 kJ . As shown in Table 8.4, which gives the caloric value of some common foods, data are usually given in Calories (note the capital C), where $1 \mathrm{Cal}=1000 \mathrm{cal}=1 \mathrm{kcal}=4.184 \mathrm{~kJ}$.

The numbers quoted in Table 8.4 are not very precise, and different reference sources often give different values. Part of the problem is that the source and variety of the food can cause large differences-an "apple," for instance, may be any one of over a hundred varieties and may come from practically any country on Earth. Perhaps even more important is that many foods-carbohydrates such as bread, in particular-contain a large but variable amount of water, which increases the mass of the food but adds no caloric value.

In a calorimeter, the heat from combustion of a fuel is released quickly and the temperature rises dramatically. Clearly, though, something quite different goes on when food is burned in the body, otherwise we'd burst into flames after a meal. As we've seen, enthalpy is a state function, so the total heat released in going from reactants to products is the same, no matter how many reactions are involved. The body applies this principle by withdrawing energy from food a bit at a time in a long series of interconnected reactions rather than all at once in a single reaction. The carbohydrate in table sugar (sucrose), for instance, is converted to $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ by a series of more than 25 sequential reactions. If the combustion were to occur in a single step, 5640 kJ would be released all at once, but the average for each of 25 steps is only 225 kJ .

$$
\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}(s)+12 \mathrm{O}_{2}(g) \longrightarrow 12 \mathrm{CO}_{2}(g)+11 \mathrm{H}_{2} \mathrm{O}(l) \quad \Delta \mathrm{H}^{\circ}=-5640 \mathrm{~kJ}
$$

Sucrose

Summary

Energy is either kinetic or potential. Kinetic energy $\left(E_{K}\right)$ is the energy of motion; its value depends on both the mass $m$ and velocity $v$ of an object according to the equation $E_{\mathrm{K}}=$ $(1 / 2) m v^{2}$. Potential energy ( $E_{\mathbf{P}}$ ) is the energy stored in an object because of its position or in a chemical substance because of its composition. Heat is the thermal energy transferred between two objects as the result of a temperature difference, whereas temperature is a measure of the kinetic energy of molecular motion.

According to the conservation of energy law, also known as the first law of thermodynamics, energy can be neither created nor destroyed. Thus, the total energy of an isolated system is constant. The total internal energy $(E)$ of a system-the sum of all kinetic and potential energies for each particle in the systemis a state function because its value depends only on the present condition of the system, not on how that condition was reached.

Work ( $w$ ) is defined as the distance moved times the force that produces the motion. In chemistry, most work is expansion work ( $P V$ work) done as the result of a volume change during a reaction when air molecules are pushed aside. The amount of work done by an expanding gas is given by the equation $w=-P \Delta V$, where $P$ is the pressure against which the system must push and $\Delta V$ is the change in volume of the system.

The total internal energy change that takes place during a reaction is the sum of the heat transferred ( $q$ ) and the work done $(-P \Delta V)$. The equation

$$
\Delta E=q+(-P \Delta V) \quad \text { or } \quad q=\Delta E+P \Delta V=\Delta H
$$

where $\Delta H$ is the enthalpy change of the system, is a fundamental equation of thermochemistry. In general, the $P \Delta V$ term is much smaller than the $\Delta E$ term, so that the total internal energy change of a reacting system is approximately equal to $\Delta H$, also called the heat of reaction. Reactions that have a negative $\Delta H$ are exothermic because heat is lost by the system, and reactions that have a positive $\Delta H$ are endothermic because heat is absorbed by the system.

Because enthalpy is a state function, $\Delta H$ is the same no matter what path is taken between reactants and products. Thus, the sum of the enthalpy changes for the individual steps in a reaction is equal to the overall enthalpy change for the entire reaction, a relationship known as Hess's law. Using this law, it is possible to calculate overall enthalpy changes for individual steps that can't be measured directly. Hess's law also makes it possible to calculate the enthalpy change of any reaction if the standard heats of formation $\left(\Delta H^{\circ}{ }_{\mathrm{f}}\right)$ are known for the reactants and products. The standard heat of formation is the enthalpy change for the hypothetical formation of 1 mol of a substance in its standard state from the most stable forms of the constituent elements in their standard states ( 1 atm pressure and a specified temperature, usually $25^{\circ} \mathrm{C}$ ).

In addition to enthalpy, entropy ( $S$ )-a measure of the amount of molecular randomness in a system-is also important in determining whether a given process will occur spontaneously. Together, changes in enthalpy and entropy define a quantity called the Gibbs free-energy change ( $\Delta G$ ) according to the equation $\Delta G=\Delta H-T \Delta S$. If $\Delta G$ is negative, the reaction is spontaneous; if $\Delta G$ is positive, the reaction is nonspontaneous.

## Key Words

chemical energy 300 conservation of energy
law 299
endothermic 309
energy 298
enthalpy (H) 305
enthalpy change $(\Delta H)$
305
entropy (S) 324
exothermic 309
first law of thermodynamics 300
Gibbs free-energy
change $(\Delta G) 326$
heat 300
heat capacity (C) 311
heat of combustion 321
heat of reaction 305
Hess's law 314
internal energy (E) 300
kinetic energy $\left(E_{K}\right) \quad 298$
molar heat capacity ( $C_{\mathrm{m}}$ ) 311
potential energy ( $E_{P}$ )
298
specific heat 311
spontaneous process 323
standard enthalpy of reaction $\left(\boldsymbol{\Delta} \boldsymbol{H}^{\circ}\right) \quad 307$
standard heat of formation ( $\mathbf{\Delta} \boldsymbol{H}^{\mathbf{\circ}} \mathbf{f}$ ) 317
state function 302
sublimation 308
temperature 300
thermochemistry 298
thermodynamic standard state 307
work (w) 302

## Key Concept Summary



## Understanding Key Concepts

Problems 8.1-8.25 appear within the chapter.
8.26 Imagine a reaction that results in a change in both volume and temperature:

(a) Has any work been done? If so, is its sign positive or negative?
(b) Has there been an enthalpy change? If so, what is the sign of $\Delta H$ ? Is the reaction exothermic or endothermic?
8.27 Redraw the following diagram to represent the situation (a) when work has been gained by the system and (b) when work has been lost by the system:

8.28 Acetylene, $\mathrm{C}_{2} \mathrm{H}_{2}$, reacts with $\mathrm{H}_{2}$ in two steps to yield ethane, $\mathrm{CH}_{3} \mathrm{CH}_{3}$ :
(1) $\quad \mathrm{HC} \equiv \mathrm{CH}+\mathrm{H}_{2} \longrightarrow \mathrm{CH}_{2}=\mathrm{CH}_{2} \quad \Delta H^{\circ}=-174.4 \mathrm{~kJ}$
$\begin{array}{ll}\text { (2) } \mathrm{CH}_{2}=\mathrm{CH}_{2}+\mathrm{H}_{2} \longrightarrow \mathrm{CH}_{3} \mathrm{CH}_{3} & \Delta H^{\circ}=-137.0 \mathrm{~kJ} \\ \text { Net } \mathrm{HC} \equiv \mathrm{CH}+2 \mathrm{H}_{2} \longrightarrow \mathrm{CH}_{3} \mathrm{CH}_{3} & \Delta H^{\circ}=-311.4 \mathrm{~kJ}\end{array}$


Which arrow in the Hess's law diagram corresponds to which step, and which arrow corresponds to the net reaction? Where are the reactants located on the diagram, and where are the products located?
8.29 Draw a Hess's law diagram similar to the one in Problem 8.28 for the reaction of ethyl alcohol $\left(\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}\right)$ with oxygen to yield acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$.
(1)

$$
\begin{aligned}
& \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(l)+1 / 2 \mathrm{O}_{2}(g) \longrightarrow \\
& \mathrm{CH}_{3} \mathrm{CHO}(g)+\mathrm{H}_{2} \mathrm{O}(l) \Delta H^{\circ}=-174.2 \mathrm{~kJ} \\
& \mathrm{CH}_{3} \mathrm{CHO}(g)+1 / 2 \mathrm{O}_{2}(g) \longrightarrow \\
& \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(l) \Delta H^{\circ}=-318.4 \mathrm{~kJ}
\end{aligned}
$$

Net $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(l)+\mathrm{O}_{2}(g) \longrightarrow$

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(l)+\mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H^{\circ}=-492.6 \mathrm{~kJ}
$$

8.30 A reaction is carried out in a cylinder fitted with a movable piston, as shown here. The starting volume is $V=5.00 \mathrm{~L}$, and the apparatus is held at constant temperature and pressure. Assuming that $\Delta H=-35.0 \mathrm{~kJ}$ and $\Delta E=-34.8 \mathrm{~kJ}$, redraw the piston to show its position after reaction. Does $V$ increase, decrease, or remain the same?

8.31 The following drawing portrays a reaction of the type
$A \rightarrow B+C$, where the different colored spheres represent different molecular structures. Assume that the reaction has $\Delta H^{\circ}=+55 \mathrm{~kJ}$. Is the reaction likely to be spontaneous at all temperatures, nonspontaneous at all temperatures, or spontaneous at some but nonspontaneous at others? Explain.

8.32 What are the signs of $\Delta H, \Delta S$, and $\Delta G$ for the following spontaneous change? Explain.

8.33 Consider the following spontaneous reaction of $\mathrm{A}_{3}$ molecules:

(a) Write a balanced equation for the reaction.
(b) What are the signs of $\Delta H, \Delta S$, and $\Delta G$ for the reaction? Explain.

## Additional Problems

## Heat, Work, and Energy

8.34 What is the difference between heat and temperature? Between work and energy? Between kinetic energy and potential energy?
8.35 What is internal energy?
8.36 Which has more kinetic energy, a 1400 kg car moving at $115 \mathrm{~km} / \mathrm{h}$ or a $12,000 \mathrm{~kg}$ truck moving at $38 \mathrm{~km} / \mathrm{h}$ ?
8.37 Assume that the kinetic energy of a 1400 kg car moving at $115 \mathrm{~km} / \mathrm{h}$ (Problem 8.36) could be converted entirely into heat. What amount of water could be heated from $20^{\circ} \mathrm{C}$ to $50^{\circ} \mathrm{C}$ by the car's energy?
8.38 Calculate the work done (in joules) by a chemical reaction if the volume increases from 3.2 L to 3.4 L against a constant external pressure of 3.6 atm . What is the sign of the energy change?
8.39 The addition of $\mathrm{H}_{2}$ to $\mathrm{C}=\mathrm{C}$ double bonds is an important reaction used in the preparation of margarine from vegetable oils. If 50.0 mL of $\mathrm{H}_{2}$ and 50.0 mL of ethylene $\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)$ are allowed to react at 1.5 atm , the product ethane $\left(\mathrm{C}_{2} \mathrm{H}_{6}\right)$ has a volume of 50.0 mL . Calculate the amount of $P V$ work done, and tell the direction of the energy flow.

$$
\mathrm{C}_{2} \mathrm{H}_{4}(g)+\mathrm{H}_{2}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{6}(g)
$$

## Energy and Enthalpy

8.40 What is the difference between the internal energy change $\Delta E$ and the enthalpy change $\Delta H$ ? Which of the two is measured at constant pressure, and which at constant volume?
8.41 What is the sign of $\Delta H$ for an exothermic reaction? For an endothermic reaction?
8.42 Under what circumstances are $\Delta E$ and $\Delta H$ essentially equal?
8.43 Which of the following has the highest enthalpy content, and which the lowest at a given temperature: $\mathrm{H}_{2} \mathrm{O}(\mathrm{s}), \mathrm{H}_{2} \mathrm{O}(\mathrm{l})$, or $\mathrm{H}_{2} \mathrm{O}(g)$ ? Explain.
8.44 The enthalpy change for the reaction of 50.0 mL of ethylene with 50.0 mL of $\mathrm{H}_{2}$ at 1.5 atm pressure (Problem $8.39)$ is $\Delta H=-0.31 \mathrm{~kJ}$. What is the value of $\Delta E$ ?
8.45 Assume that a particular reaction evolves 244 kJ of heat and that 35 kJ of $P V$ work is gained by the system. What are the values of $\Delta E$ and $\Delta H$ for the system? For the surroundings?
8.46 Used in welding metals, the reaction of acetylene with oxygen has $\Delta H^{\circ}=-1255.5 \mathrm{~kJ}$ :

$$
\begin{array}{r}
\mathrm{C}_{2} \mathrm{H}_{2}(g)+5 / 2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{H}_{2} \mathrm{O}(g)+2 \mathrm{CO}_{2}(g) \\
\Delta H^{\circ}=-1255.5 \mathrm{~kJ}
\end{array}
$$

How much $P V$ work is done (in kilojoules), and what is the value of $\Delta E$ (in kilojoules) for the reaction of 6.50 g of acetylene at atmospheric pressure if the volume change is -2.80 L ?
8.47 Ethyl chloride $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}\right)$, a substance used as a topical anesthetic, is prepared by reaction of ethylene with hydrogen chloride:

$$
\begin{array}{r}
\mathrm{C}_{2} \mathrm{H}_{4}(g)+\mathrm{HCl}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Cl}(g) \\
\Delta H^{\circ}=-72.3 \mathrm{~kJ}
\end{array}
$$

How much $P V$ work is done (in kilojoules), and what is the value of $\Delta E$ (in kilojoules) if 89.5 g of ethylene and 125 g of HCl are allowed to react at atmospheric pressure and the volume change is -71.5 L ?
8.48 The familiar "ether" used as an anesthetic agent is diethyl ether, $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$. Its heat of vaporization is $+26.5 \mathrm{~kJ} / \mathrm{mol}$ at its boiling point. How much energy (in kilojoules) is required to convert 100 mL of diethyl ether at its boiling point from liquid to vapor if its density is $0.7138 \mathrm{~g} / \mathrm{mL}$ ?
8.49 How much energy (in kilojoules) is required to convert 100 mL of water at its boiling point from liquid to vapor, and how does this compare with the result calculated in Problem 8.48 for diethyl ether? $\left[\Delta H_{\text {vap }}\left(\mathrm{H}_{2} \mathrm{O}\right)=+40.7 \mathrm{~kJ} / \mathrm{mol}\right]$
8.50 Aluminum metal reacts with chlorine with a spectacular display of sparks:

$$
\begin{array}{r}
2 \mathrm{Al}(s)+3 \mathrm{Cl}_{2}(g) \longrightarrow 2 \mathrm{AlCl}_{3}(s) \\
\Delta H^{\circ}=-1408.4 \mathrm{~kJ}
\end{array}
$$

How much heat (in kilojoules) is released on reaction of 5.00 g of Al ?
8.51 How much heat (in kilojoules) is evolved or absorbed in the reaction of 1.00 g of Na with $\mathrm{H}_{2} \mathrm{O}$ ? Is the reaction exothermic or endothermic?

$$
\begin{array}{r}
2 \mathrm{Na}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{NaOH}(a q)+\mathrm{H}_{2}(g) \\
\Delta H^{\circ}=-368.4 \mathrm{~kJ}
\end{array}
$$

8.52 How much heat (in kilojoules) is evolved or absorbed in the reaction of 2.50 g of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ with enough carbon monoxide to produce iron metal? Is the process exothermic or endothermic?

$$
\begin{aligned}
\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \longrightarrow 2 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(g) \\
\Delta H^{\circ}=-24.8 \mathrm{~kJ}
\end{aligned}
$$

8.53 How much heat (in kilojoules) is evolved or absorbed in the reaction of 233.0 g of calcium oxide with enough carbon to produce calcium carbide? Is the process exothermic or endothermic?

$$
\begin{array}{r}
\mathrm{CaO}(s)+3 \mathrm{C}(s) \longrightarrow \mathrm{CaC}_{2}(s)+\mathrm{CO}(g) \\
\Delta H^{\circ}=464.8 \mathrm{~kJ}
\end{array}
$$

## Calorimetry and Heat Capacity

8.54 What is the difference between heat capacity and specific heat?
8.55 Does a measurement carried out in a bomb calorimeter give a value for $\Delta H$ or $\Delta E$ ? Explain.
8.56 Sodium metal is sometimes used as a cooling agent in heat-exchange units because of its relatively high molar heat capacity of $28.2 \mathrm{~J} /\left(\mathrm{mol} \cdot{ }^{\circ} \mathrm{C}\right)$. What is the specific heat of sodium in $\mathrm{J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$ ?
8.57 Titanium metal is used as a structural material in many high-tech applications such as in jet engines. What is the specific heat of titanium in $\mathrm{J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$ if it takes 89.7 J to raise the temperature of a 33.0 g block by $5.20^{\circ} \mathrm{C}$ ? What is the molar heat capacity of titanium in $\mathrm{J} /\left(\mathrm{mol} \cdot{ }^{\circ} \mathrm{C}\right)$ ?
8.58 When 1.045 g of CaO is added to 50.0 mL of water at $25.0^{\circ} \mathrm{C}$ in a calorimeter, the temperature of the water increases to $32.3^{\circ} \mathrm{C}$. Assuming that the specific heat of the solution is $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$ and that the calorimeter itself absorbs a negligible amount of heat, calculate $\Delta H$ (in kilojoules) for the reaction

$$
\mathrm{CaO}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Ca}(\mathrm{OH})_{2}(a q)
$$

8.59 When 0.187 g of benzene, $\mathrm{C}_{6} \mathrm{H}_{6}$, is burned in a bomb calorimeter, the surrounding water bath rises in tem-
perature by $7.48^{\circ} \mathrm{C}$. Assuming that the bath contains 250.0 g of water and that the calorimeter itself absorbs a negligible amount of heat, calculate combustion energies $\Delta E$ for benzene in both kilojoules per gram and kilojoules per mole.
8.60 When a solution containing 8.00 g of NaOH in 50.0 g of water at $25.0^{\circ} \mathrm{C}$ is added to a solution of 8.00 g of HCl in 250.0 g of water at $25.0^{\circ} \mathrm{C}$ in a calorimeter, the temperature of the solution increases to $33.5^{\circ} \mathrm{C}$. Assuming that the specific heat of the solution is $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$ and that the calorimeter absorbs a negligible amount of heat, calculate $\Delta H$ (in kilojoules) for the reaction

$$
\mathrm{NaOH}(a q)+\mathrm{HCl}(a q) \longrightarrow \mathrm{NaCl}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

When the experiment is repeated using a solution of 10.00 g of HCl in 248.0 g of water, the same temperature increase is observed. Explain.
8.61 Instant cold packs used to treat athletic injuries contain solid $\mathrm{NH}_{4} \mathrm{NO}_{3}$ and a pouch of water. When the pack is squeezed, the pouch breaks and the solid dissolves, lowering the temperature because of the endothermic reaction

$$
\begin{array}{r}
\mathrm{NH}_{4} \mathrm{NO}_{3}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{NH}_{4} \mathrm{NO}_{3}(a q) \\
\Delta H=+25.7 \mathrm{~kJ}
\end{array}
$$

What is the final temperature in a squeezed cold pack that contains 50.0 g of $\mathrm{NH}_{4} \mathrm{NO}_{3}$ dissolved in 125 mL of water? Assume a specific heat of $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$ for the solution, an initial temperature of $25.0^{\circ} \mathrm{C}$, and no heat transfer between the cold pack and the environment.

## Hess's Law and Heats of Formation

8.62 How is the standard state of an element defined?
8.63 What is a compound's standard heat of formation?
8.64 What is Hess's law, and why does it "work"?
8.65 Why do elements always have $\Delta H^{\circ}{ }_{f}=0$ ?
8.66 Sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$, the most widely produced chemical in the world, is made by a two-step oxidation of sulfur to sulfur trioxide, $\mathrm{SO}_{3}$, followed by reaction with water. Calculate $\Delta H^{\circ}{ }_{\mathrm{f}}$ for $\mathrm{SO}_{3}$ (in kilojoules per mole), given the following data:

$$
\begin{array}{ll}
\mathrm{S}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{SO}_{2}(g) & \Delta H^{\circ}=-296.8 \mathrm{~kJ} \\
\mathrm{SO}_{2}(g)+1 / 2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{SO}_{3}(g) & \Delta H^{\circ}=-98.9 \mathrm{~kJ}
\end{array}
$$

8.67 Calculate $\Delta H^{\circ}$ (in kilojoules per mole) for benzene, $\mathrm{C}_{6} \mathrm{H}_{6}$, from the following data:

$$
2 \mathrm{C}_{6} \mathrm{H}_{6}(l)+15 \mathrm{O}_{2}(g) \longrightarrow 12 \mathrm{CO}_{2}(g)+6 \mathrm{H}_{2} \mathrm{O}(l)
$$

$$
\Delta H^{\circ}=-6534 \mathrm{~kJ}
$$

$\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{CO}_{2}\right)=-393.5 \mathrm{~kJ} / \mathrm{mol}$
$\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}\right)=-285.8 \mathrm{~kJ} / \mathrm{mol}$
8.68 The standard enthalpy change for the reaction of $\mathrm{SO}_{3}(g)$ with $\mathrm{H}_{2} \mathrm{O}(l)$ to yield $\mathrm{H}_{2} \mathrm{SO}_{4}(a q)$ is $\Delta H^{\circ}=$ -227.8 kJ . Use the information in Problem 8.66 to calculate $\Delta H^{\circ}$ for $\mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{aq})$ (in kilojoules per mole). [For $\mathrm{H}_{2} \mathrm{O}(l), \Delta H^{\circ}{ }_{\mathrm{f}}=-285.8 \mathrm{~kJ} / \mathrm{mol}$.]
8.69 Acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$, whose aqueous solutions are known as vinegar, is prepared by reaction of ethyl alcohol $\left(\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}\right)$ with oxygen:

$$
\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(l)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(l)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Use the following data to calculate $\Delta H^{\circ}$ (in kilojoules) for the reaction:

$$
\begin{aligned}
\Delta H^{\circ}\left(\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}\right) & =-277.7 \mathrm{~kJ} / \mathrm{mol} \\
\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right) & =-484.5 \mathrm{~kJ} / \mathrm{mol} \\
\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}\right) & =-285.8 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

8.70 Styrene $\left(\mathrm{C}_{8} \mathrm{H}_{8}\right)$, the precursor of polystyrene polymers, has a standard heat of combustion of $-4395.2 \mathrm{~kJ} / \mathrm{mol}$. Write a balanced equation for the combustion reaction, and calculate $\Delta H^{\circ}$ for styrene (in kilojoules per mole). $\left[\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{CO}_{2}\right)=-393.5 \mathrm{~kJ} / \mathrm{mol} ; \Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}\right)=\right.$ $-285.8 \mathrm{~kJ} / \mathrm{mol}]$
8.71 Methyl tert-butyl ether (MTBE), $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}$, a gasoline additive used to boost octane ratings, has $\Delta H^{\circ}{ }_{\mathrm{f}}=$ $-313.6 \mathrm{~kJ} / \mathrm{mol}$. Write a balanced equation for its combustion reaction, and calculate its standard heat of combustion in kilojoules.
8.72 Methyl tert-butyl ether (Problem 8.71) is prepared by reaction of methanol $\left(\Delta H^{\circ}{ }_{f}=-238.7 \mathrm{~kJ} / \mathrm{mol}\right)$ with 2-methylpropene, according to the equation


$\Delta H^{\circ}=-57.8 \mathrm{~kJ}$

Methyl tert-butyl ether
Calculate $\Delta H^{\circ}$ (in kilojoules per mole) for 2-methylpropene.
8.73 One possible use for the cooking fat left over after making french fries is to burn it as fuel. Write a balanced equation, and use the following data to calculate the amount of energy released (in kilojoules per milliliter) from the combustion of cooking fat:

$$
\begin{aligned}
& \text { Formula }=\mathrm{C}_{51} \mathrm{H}_{88} \mathrm{O}_{6} \\
& \text { Density }=0.94 \mathrm{~g} / \mathrm{mL} \quad \Delta H_{\mathrm{f}}^{\circ}=-1310 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

## Bond Dissociation Energies

8.74 Use the bond dissociation energies in Table 7.1 to calculate an approximate $\Delta H^{\circ}$ (in kilojoules) for the reaction of ethylene with hydrogen to yield ethane.

$$
\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}(g)+\mathrm{H}_{2}(g) \longrightarrow \mathrm{CH}_{3} \mathrm{CH}_{3}(g)
$$

8.75 Use the bond dissociation energies in Table 7.1 to calculate an approximate $\Delta H^{\circ}$ (in kilojoules) for the industrial synthesis of isopropyl alcohol (rubbing alcohol) by reaction of water with propene, as shown at the top of the next column.

8.76 Calculate an approximate heat of combustion for butane (in kilojoules) by using the bond dissociation energies in Table 7.1. (The strength of the $\mathrm{O}=\mathrm{O}$ bond is $498 \mathrm{~kJ} / \mathrm{mol}$, and that of a $\mathrm{C}=\mathrm{O}$ bond in $\mathrm{CO}_{2}$ is $804 \mathrm{~kJ} / \mathrm{mol}$.)


Butane
8.77 Use the bond dissociation energies in Table 7.1 to calculate an approximate heat of reaction, $\Delta H^{\circ}$ (in kilojoules), for the industrial reaction of ethanol with acetic acid to yield ethyl acetate (used as nail-polish remover) and water.


## Free Energy and Entropy

8.78 What does entropy measure?
8.79 What are the two terms that make up the free-energy change for a reaction, $\Delta G$, and which of the two is usually more important?
8.80 How is it possible for a reaction to be spontaneous yet endothermic?
8.81 Is it possible for a reaction to be nonspontaneous yet exothermic? Explain.
8.82 Tell whether the entropy changes for the following processes are likely to be positive or negative:
(a) The fizzing of a newly opened can of soda
(b) The growth of a plant from seed
8.83 Tell whether the entropy changes, $\Delta S$, for the following processes are likely to be positive or negative:
(a) The conversion of liquid water to water vapor at $100^{\circ} \mathrm{C}$
(b) The freezing of liquid water to ice at $0^{\circ} \mathrm{C}$
(c) The eroding of a mountain by a glacier
8.84 Tell whether the free-energy changes, $\Delta G$, for the process listed in Problem 8.83 are likely to be positive, negative, or zero.
8.85 When a bottle of perfume is opened, odorous molecules mix with air and slowly diffuse throughout the entire room. Is $\Delta G$ for the diffusion process positive, negative, or zero? What about $\Delta H$ and $\Delta S$ for the diffusion?
8.86 One of the steps in the cracking of petroleum into gasoline involves the thermal breakdown of large hydrocarbon molecules into smaller ones. For example, the following reaction might occur:

$$
\mathrm{C}_{11} \mathrm{H}_{24} \longrightarrow \mathrm{C}_{4} \mathrm{H}_{10}+\mathrm{C}_{4} \mathrm{H}_{8}+\mathrm{C}_{3} \mathrm{H}_{6}
$$

Is $\Delta S$ for this reaction likely to be positive or negative? Explain.
8.87 The commercial production of 1,2-dichloroethane, a solvent used in dry cleaning, involves the reaction of ethylene with chlorine:

$$
\mathrm{C}_{2} \mathrm{H}_{4}(g)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Cl}_{2}(l)
$$

Is $\Delta S$ for this reaction likely to be positive or negative? Explain.
8.88 Tell whether reactions with the following values of $\Delta H$ and $\Delta S$ are spontaneous or nonspontaneous and whether they are exothermic or endothermic:
(a) $\Delta H=-48 \mathrm{~kJ} ; \Delta S=+135 \mathrm{~J} / \mathrm{K}$ at 400 K
(b) $\Delta H=-48 \mathrm{~kJ} ; \Delta S=-135 \mathrm{~J} / \mathrm{K}$ at 400 K
(c) $\Delta H=+48 \mathrm{~kJ} ; \Delta S=+135 \mathrm{~J} / \mathrm{K}$ at 400 K
(d) $\Delta H=+48 \mathrm{~kJ} ; \Delta S=-135 \mathrm{~J} / \mathrm{K}$ at 400 K
8.89 Tell whether reactions with the following values of $\Delta H$ and $\Delta S$ are spontaneous or nonspontaneous and whether they are exothermic or endothermic:
(a) $\Delta H=-128 \mathrm{~kJ} ; \Delta S=35 \mathrm{~J} / \mathrm{K}$ at 500 K
(b) $\Delta H=+67 \mathrm{~kJ} ; \Delta S=-140 \mathrm{~J} / \mathrm{K}$ at 250 K
(c) $\Delta H=+75 \mathrm{~kJ} ; \Delta S=95 \mathrm{~J} / \mathrm{K}$ at 800 K
8.90 Suppose that a reaction has $\Delta H=-33 \mathrm{~kJ}$ and $\Delta S=-58 \mathrm{~J} / \mathrm{K}$. At what temperature will it change from spontaneous to nonspontaneous?
8.91 Suppose that a reaction has $\Delta H=+41 \mathrm{~kJ}$ and $\Delta S=-27 \mathrm{~J} / \mathrm{K}$. At what temperature, if any, will it change between spontaneous and nonspontaneous?
8.92 Which of the reactions (a)-(d) in Problem 8.88 are spontaneous at all temperatures, which are nonspontaneous at all temperatures, and which have an equilibrium temperature?
8.93 Vinyl chloride $\left(\mathrm{H}_{2} \mathrm{C}=\mathrm{CHCl}\right)$, the starting material used in the industrial preparation of poly(vinyl chloride), is prepared by a two-step process that begins with the reaction of $\mathrm{Cl}_{2}$ with ethylene to yield 1,2dichloroethane:

$$
\begin{aligned}
& \mathrm{Cl}_{2}(g)+\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}(g) \longrightarrow \mathrm{ClCH}_{2} \mathrm{CH}_{2} \mathrm{Cl}(l) \\
& \Delta H^{\circ}=-217.5 \mathrm{~kJ} / \mathrm{mol} \\
& \Delta S^{\circ}=-233.9 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})
\end{aligned}
$$

(a) Tell whether the reaction is favored by entropy, by enthalpy, by both, or by neither, and then calculate $\Delta G^{\circ}$ at 298 K .
(b) Tell whether the reaction has an equilibrium temperature between spontaneous and nonspontaneous. If yes, calculate the equilibrium temperature.
8.94 Ethyl alcohol has $\Delta H_{\text {fusion }}=5.02 \mathrm{~kJ} / \mathrm{mol}$ and melts at $-114.1^{\circ} \mathrm{C}$. What is the value of $\Delta S_{\text {fusion }}$ for ethyl alcohol?
8.95 Chloroform has $\Delta H_{\text {vaporization }}=29.2 \mathrm{~kJ} / \mathrm{mol}$ and boils at $61.2^{\circ} \mathrm{C}$. What is the value of $\Delta S_{\text {vaporization }}$ for chloroform?

## General Problems

8.96 When 1.50 g of magnesium metal is allowed to react with 200 mL of 6.00 M aqueous HCl , the temperature rises from $25.0^{\circ} \mathrm{C}$ to $42.9^{\circ} \mathrm{C}$. Calculate $\Delta H$ (in kilojoules) for the reaction, assuming that the heat capacity of the calorimeter is $776 \mathrm{~J} /{ }^{\circ} \mathrm{C}$, that the specific heat of the final solution is the same as that of water $\left[\left(4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)\right]\right.$, and that the density of the solution is $1.00 \mathrm{~g} / \mathrm{mL}$.
8.97 Use the data in Appendix B to find standard enthalpies of reaction (in kilojoules) for the following processes:
(a) $\mathrm{C}(s)+\mathrm{CO}_{2}(g) \rightarrow 2 \mathrm{CO}(g)$
(b) $2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g)$
(c) $\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \rightarrow 2 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(g)$
8.98 Find $\Delta H^{\circ}$ (in kilojoules) for the reaction of nitric oxide with oxygen, $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightarrow \mathrm{N}_{2} \mathrm{O}_{4}(g)$, given the following thermochemical data:

$$
\begin{array}{ll}
\mathrm{N}_{2} \mathrm{O}_{4}(g) \longrightarrow 2 \mathrm{NO}_{2}(g) & \Delta H^{\circ}=57.2 \mathrm{~kJ} \\
\mathrm{NO}(g)+1 / 2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{NO}_{2}(g) & \Delta H^{\circ}=-57.0 \mathrm{~kJ}
\end{array}
$$

8.99 The boiling point of a substance is defined as the temperature at which liquid and vapor coexist in equilibrium. Use the heat of vaporization ( $\Delta H_{\text {vap }}=$ $30.91 \mathrm{~kJ} / \mathrm{mol}$ ) and the entropy of vaporization $\left[\Delta S_{\text {vap }}=93.2 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})\right]$ to calculate the boiling point $\left({ }^{\circ} \mathrm{C}\right)$ of liquid bromine.
8.100 What is the melting point of benzene (in kelvins) if $\Delta H_{\text {fusion }}=9.95 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S_{\text {fusion }}=35.7 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ ?
8.101 Metallic mercury is obtained by heating the mineral cinnabar ( HgS ) in air:

$$
\mathrm{HgS}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{Hg}(l)+\mathrm{SO}_{2}(g)
$$

(a) Use the data in Appendix B to calculate $\Delta H^{\circ}$ (in kilojoules) for the reaction.
(b) The entropy change for the reaction is $\Delta S^{\circ}=$ $+36.7 \mathrm{~J} / \mathrm{K}$. Is the reaction spontaneous at $25^{\circ} \mathrm{C}$ ?
(c) Under what conditions, if any, is the reaction nonspontaneous? Explain.
8.102 Use the average bond dissociation energies in Table 7.1 to calculate approximate reaction enthalpies (in kilojoules) for the following processes:
(a) $2 \mathrm{CH}_{4}(g) \rightarrow \mathrm{C}_{2} \mathrm{H}_{6}(g)+\mathrm{H}_{2}(g)$
(b) $\mathrm{C}_{2} \mathrm{H}_{6}(g)+\mathrm{F}_{2}(g) \rightarrow \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{~F}(g)+\mathrm{HF}(g)$
(c) $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightarrow 2 \mathrm{NH}_{3}(g)$
8.103 Methanol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$ is made industrially in two steps from CO and $\mathrm{H}_{2}$. It is so cheap to make that it is being considered for use as a precursor to hydrocarbon fuels such as methane $\left(\mathrm{CH}_{4}\right)$ :

Step 1. $\mathrm{CO}(g)+2 \mathrm{H}_{2}(g) \longrightarrow \mathrm{CH}_{3} \mathrm{OH}(l)$ $\Delta S^{\circ}=-332 \mathrm{~J} / \mathrm{K}$
Step 2. $\mathrm{CH}_{3} \mathrm{OH}(l) \longrightarrow \mathrm{CH}_{4}(g)+1 / 2 \mathrm{O}_{2}(g)$ $\Delta S^{\circ}=162 \mathrm{~J} / \mathrm{K}$
(a) Calculate $\Delta H^{\circ}$ (in kilojoules) for step 1.
(b) Calculate $\Delta G^{\circ}$ (in kilojoules) for step 1.
(c) Is step 1 spontaneous at 298 K ?
(d) Which term is more important, $\Delta H^{\circ}$ or $\Delta S^{\circ}$ ?
(e) In what temperature range is step 1 spontaneous?
(f) Calculate $\Delta H^{\circ}$ for step 2.
(g) Calculate $\Delta G^{\circ}$ for step 2.
(h) Is step 2 spontaneous at 298 K ?
(i) Which term is more important, $\Delta H^{\circ}$ or $\Delta S^{\circ}$ ?
(j) In what temperature range is step 2 spontaneous?
(k) Calculate an overall $\Delta G^{\circ}, \Delta H^{\circ}$, and $\Delta S^{\circ}$ for the formation of $\mathrm{CH}_{4}$ from CO and $\mathrm{H}_{2}$.
(l) Is the overall reaction spontaneous?
(m) If you were designing a production facility, would you plan on carrying out the reactions in separate steps or together? Explain.
8.104 Isooctane, $\mathrm{C}_{8} \mathrm{H}_{18}$, is the component of gasoline from which the term octane rating derives.
(a) Write a balanced equation for the combustion of isooctane with $\mathrm{O}_{2}$ to yield $\mathrm{CO}_{2}(g)$ and $\mathrm{H}_{2} \mathrm{O}(g)$.
(b) The standard molar heat of combustion for isooctane is $-5456.6 \mathrm{~kJ} / \mathrm{mol}$. Calculate $\Delta H^{\circ}{ }_{\mathrm{f}}$ for isooctane.
8.105 We said in Section 8.2 that the potential energy of water at the top of a dam or waterfall is converted into heat when the water dashes against rocks at the bottom. The potential energy of the water at the top is equal to $E_{\mathrm{P}}=m g h$, where $m$ is the mass of the water, $g$ is the acceleration of the falling water due to gravity ( $g=9.81 \mathrm{~m} / \mathrm{s}^{2}$ ), and $h$ is the height of the water. Assuming that all the energy is converted to heat, calculate the temperature rise of the water (in degrees Celsius) after falling over California's Yosemite Falls, a distance of 739 m . The specific heat of water is $4.18 \mathrm{~J} /(\mathrm{g} \cdot \mathrm{K})$.
8.106 For a process to be spontaneous, the total entropy of the system and its surroundings must increase. That is,

$$
\Delta S_{\text {total }}=\Delta S_{\text {system }}+\Delta S_{\text {surr }}>0
$$

(For a spontaneous process)

Furthermore, the entropy change in the surroundings, $\Delta S_{\text {surr }}$, is related to the enthalpy change for the process by the equation $\Delta S_{\text {surr }}=-\Delta H / T$.
(a) Since both $\Delta G$ and $\Delta S_{\text {total }}$ offer criteria for spontaneity, they must be related. Derive a relationship between them.
(b) What is the value of $\Delta S_{\text {surr }}$ for the photosynthesis of glucose from $\mathrm{CO}_{2}$ at 298 K ?

$$
\begin{aligned}
& 6 \mathrm{CO}_{2}(g)+6 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s)+6 \mathrm{O}_{2}(g) \\
& \Delta G^{\circ}=2879 \mathrm{~kJ} / \mathrm{mol} \\
& \Delta S^{\circ}=-210 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})
\end{aligned}
$$

8.107 Set up a Hess's law cycle, and use the following information to calculate $\Delta H^{\circ}$ for aqueous nitric acid, $\mathrm{HNO}_{3}(a q)$. You will need to use fractional coefficients for some equations.

$$
\begin{array}{r}
3 \mathrm{NO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{HNO}_{3}(a q)+\mathrm{NO}(g) \\
\Delta H^{\circ}=-138.4 \mathrm{~kJ} \\
2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{NO}_{2}(g) \\
\Delta H^{\circ}=-114.0 \mathrm{~kJ} \\
4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(l) \\
\Delta H^{\circ}=-1169.6 \mathrm{~kJ}
\end{array}
$$

$\mathrm{NH}_{3}(g) \quad \Delta H^{\circ}{ }_{\mathrm{f}}=-46.1 \mathrm{~kJ} / \mathrm{mol}$
$\mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H_{\mathrm{f}}^{\circ}=-285.8 \mathrm{~kJ} / \mathrm{mol}$
8.108 Hess's law can be used to calculate reaction enthalpies for hypothetical processes that can't be carried out in the laboratory. Set up a Hess's law cycle that will let you calculate $\Delta H^{\circ}$ for the conversion of methane to ethylene:

$$
2 \mathrm{CH}_{4}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{4}(g)+2 \mathrm{H}_{2}(g)
$$

You can use the following information:

$$
\begin{aligned}
& 2 \mathrm{C}_{2} \mathrm{H}_{6}(g)+7 \mathrm{O}_{2}(g) \longrightarrow 4 \mathrm{CO}_{2}(g)+6 \mathrm{H}_{2} \mathrm{O}(l) \\
& \Delta H^{\circ}=-3119.4 \mathrm{~kJ} \\
& \mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l) \\
& \Delta H^{\circ}=-890.3 \mathrm{~kJ} \\
& \mathrm{C}_{2} \mathrm{H}_{4}(g)+\mathrm{H}_{2}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{6}(\mathrm{~g}) \quad \\
& \\
& \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \quad \Delta H^{\circ}=-137.0 \mathrm{~kJ} \\
& \mathrm{f}=-285.8 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

8.109 A 110.0 g piece of molybdenum metal is heated to $100.0^{\circ} \mathrm{C}$ and placed in a calorimeter that contains 150.0 g of water at $24.6^{\circ} \mathrm{C}$. The system reaches equilibrium at a final temperature of $28.0^{\circ} \mathrm{C}$. Calculate the specific heat of molybdenum metal in $\mathrm{J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$. The specific heat of water is $4.184 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$.
8.110 Given 400.0 g of hot tea at $80.0^{\circ} \mathrm{C}$, what mass of ice at $0^{\circ} \mathrm{C}$ must be added to obtain iced tea at $10.0^{\circ} \mathrm{C}$ ? The specific heat of the tea is $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$, and $\Delta H_{\text {fusion }}$ for ice is $+6.01 \mathrm{~kJ} / \mathrm{mol}$.
8.111 Citric acid has three dissociable hydrogens. When 5.00 mL of 0.64 M citric acid and 45.00 mL of 0.77 M NaOH at an initial temperature of $26.0^{\circ} \mathrm{C}$ are mixed, the temperature rises to $27.9^{\circ} \mathrm{C}$ as the citric acid is neutralized. The combined mixture has a mass of 51.6 g and a specific heat of $4.0 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$. Assuming that no heat is transferred to the surroundings, calculate the enthalpy change for the reaction of 1.00 mol of citric acid in kJ . Is the reaction exothermic or endothermic?
8.112 Assume that 100.0 mL of 0.200 M CsOH and 50.0 mL of 0.400 M HCl are mixed in a calorimeter. The solutions start out at $22.50^{\circ} \mathrm{C}$, and the final temperature after reaction is $24.28^{\circ} \mathrm{C}$. The densities of the solutions are all $1.00 \mathrm{~g} / \mathrm{mL}$, and the specific heat of the mixture is $4.2 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$. What is the enthalpy change for the neutralization reaction of 1.00 mol of CsOH in kJ ?
8.113 Imagine that you dissolve 10.0 g of a mixture of $\mathrm{NaNO}_{3}$ and KF in 100.0 g of water and find that the temperature rises by $2.22^{\circ} \mathrm{C}$. Using the following data, calculate the mass of each compound in the original mixture. Assume that the specific heat of the solution is $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$.

$$
\begin{array}{ll}
\mathrm{NaNO}_{3}(s) \longrightarrow \mathrm{NaNO}_{3}(a q) & \Delta H=+20.5 \mathrm{~kJ} / \mathrm{mol} \\
\mathrm{KF}(s) \longrightarrow \mathrm{KF}(a q) & \Delta H=-17.7 \mathrm{~kJ} / \mathrm{mol}
\end{array}
$$

8.114 Consider the reaction $4 \mathrm{CO}(g)+2 \mathrm{NO}_{2}(g) \rightarrow 4 \mathrm{CO}_{2}(g)+$ $\mathrm{N}_{2}(g)$. Using the following information, determine $\Delta H^{\circ}$ for the reaction at $25^{\circ} \mathrm{C}$.

\[

\]

## Multi-Concept Problems

8.115 Consider the reaction $\mathrm{S}_{8}(g) \rightarrow 4 \mathrm{~S}_{2}(g)$, for which $\Delta H=+99 \mathrm{~kJ}$.
(a) The $\mathrm{S}_{8}$ molecule has eight sulfur atoms arranged in a ring. What is the hybridization and geometry around each sulfur atom in $\mathrm{S}_{8}$ ?
(b) The average S-S bond dissociation energy is 225 $\mathrm{kJ} / \mathrm{mol}$. Using the value of $\Delta H$ given above, what is the $\mathrm{S}=\mathrm{S}$ double bond energy in $\mathrm{S}_{2}(g)$ ?
(c) Assuming that the bonding in $\mathrm{S}_{2}$ is similar to the bonding in $\mathrm{O}_{2}$, give a molecular orbital description of the bonding in $\mathrm{S}_{2}$. Is $\mathrm{S}_{2}$ likely to be paramagnetic or diamagnetic?
8.116 Phosgene, $\mathrm{COCl}_{2}(g)$, is a toxic gas used as an agent of warfare in World War I.
(a) Draw an electron-dot structure for phosgene.
(b) Using the table of bond dissociation energies (Table 7.1) and the value $\Delta H^{\circ}{ }_{\mathrm{f}}=716.7 \mathrm{~kJ} / \mathrm{mol}$ for $\mathrm{C}(\mathrm{g})$, estimate $\Delta H^{\circ}{ }_{\mathrm{f}}$ for $\mathrm{COCl}_{2}(\mathrm{~g})$ at $25^{\circ} \mathrm{C}$. Compare your answer to the actual $\Delta H^{\circ}{ }_{\mathrm{f}}$ given in Appendix B, and explain why your calculation is only an estimate.
8.117 Acid spills are often neutralized with sodium carbonate or sodium hydrogen carbonate. For neutralization of acetic acid, the unbalanced equations are
(1)

$$
\begin{gather*}
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(l)+\mathrm{Na}_{2} \mathrm{CO}_{3}(s) \longrightarrow \\
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}(a q)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \\
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(l)+\mathrm{NaHCO}_{3}(s) \longrightarrow  \tag{2}\\
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}(a q)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
\end{gather*}
$$

(a) Balance both reactions.
(b) How many kilograms of each substance is needed to neutralize a 1.000 gallon spill of pure acetic acid (density $=1.049 \mathrm{~g} / \mathrm{mL}$ ) ?
(c) How much heat (in kilojoules) is absorbed or liberated in each reaction? See Appendix B for standard heats of formation; $\Delta H_{\mathrm{f}}^{\circ}=-726.1 \mathrm{~kJ} / \mathrm{mol}$ for $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}(a q)$.
8.118 (a) Write a balanced equation for the reaction of potassium metal with water.
(b) Use the data in Appendix B to calculate $\Delta H^{\circ}$ for the reaction of potassium metal with water.
(c) Assume that a chunk of potassium weighing 7.55 g is dropped into 400.0 g of water at $25.0^{\circ} \mathrm{C}$. What is the final temperature of the water if all the heat released is used to warm the water?
(d) What is the molarity of the KOH solution prepared in part (c), and how many milliliters of $0.554 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ are required to neutralize it?
8.119 Hydrazine, a component of rocket fuel, undergoes combustion to yield $\mathrm{N}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ :

$$
\mathrm{N}_{2} \mathrm{H}_{4}(l)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{N}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

(a) Draw an electron-dot structure for hydrazine, predict the geometry about each nitrogen atom, and tell the hybridization of each nitrogen.
(b) Use the following information to set up a Hess's law cycle, and then calculate $\Delta H^{\circ}$ for the combustion reaction. You will need to use fractional coefficients for some equations.

$$
\begin{gathered}
2 \mathrm{NH}_{3}(g)+3 \mathrm{~N}_{2} \mathrm{O}(g) \longrightarrow 4 \mathrm{~N}_{2}(g)+3 \mathrm{H}_{2} \mathrm{O}(l) \\
\Delta H^{\circ}=-1011.2 \mathrm{~kJ} \\
\mathrm{~N}_{2} \mathrm{O}(g)+3 \mathrm{H}_{2}(g) \longrightarrow \mathrm{N}_{2} \mathrm{H}_{4}(l)+\mathrm{H}_{2} \mathrm{O}(l) \\
\Delta H^{\circ}=-317 \mathrm{~kJ} \\
4 \mathrm{NH}_{3}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{~N}_{2} \mathrm{H}_{4}(l)+2 \mathrm{H}_{2} \mathrm{O}(l) \\
\Delta H^{\circ}=-286 \mathrm{~kJ} \\
\mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H_{\mathrm{f}}^{\circ}=-285.8 \mathrm{~kJ} / \mathrm{mol}
\end{gathered}
$$

(c) How much heat is released on combustion of 100.0 g of hydrazine?
8.120 Reaction of gaseous fluorine with compound $X$ yields a single product Y , whose mass percent composition is $61.7 \% \mathrm{~F}$ and $38.3 \% \mathrm{Cl}$.
(a) What is a probable molecular formula for product Y , and what is a probable formula for X ?
(b) Draw an electron-dot structure for Y , and predict the geometry around the central atom.
(c) Calculate $\Delta H^{\circ}$ for the synthesis of Y using the following information:

$$
\begin{array}{r}
2 \mathrm{ClF}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g}) \longrightarrow \mathrm{Cl}_{2} \mathrm{O}(\mathrm{~g})+\mathrm{OF}_{2}(\mathrm{~g}) \\
\Delta H^{\circ}=+205.6 \mathrm{~kJ} \\
2 \mathrm{ClF}_{3}(\mathrm{l})+2 \mathrm{O}_{2}(\mathrm{~g}) \longrightarrow \mathrm{Cl}_{2} \mathrm{O}(\mathrm{~g})+3 \mathrm{OF}_{2}(\mathrm{~g}) \\
\Delta H^{\circ}=+533.4 \mathrm{~kJ}
\end{array}
$$

$\mathrm{OF}_{2}(\mathrm{~g}) \quad \Delta H^{\circ}{ }_{\mathrm{f}}=+24.7 \mathrm{~kJ} / \mathrm{mol}$
(d) How much heat in kilojoules is released or absorbed in the reaction of 25.0 g of X with a stoichiometric amount of $\mathrm{F}_{2}$, assuming $87.5 \%$ yield for the reaction?

## eMedia Problems

8.121 Using the Enthalpy of Solution activity in eChapter 8.7, add 5.0 g of each solute to 100 g of water.
(a) Determine the temperature change for each solution process.
(b) Calculate the heat ( $q$ ) gained or lost by the water for each process. [Specific heat of water $\left.=4.184 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)\right]$
(c) Calculate the heat $q$ gained or lost by the solute for each process.
(d) Calculate $\Delta H$ for each solution process in $\mathrm{kJ} / \mathrm{mol}$.
8.122 Using the Calorimetry simulation in eChapter 8.8, burn 100 mg of five different compounds in 1000 g of water.
(a) Determine the temperature change of the water for each combustion process.
(b) Calculate the heat gained by the water for each process. [Specific heat of water $=4.184 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$ ]
(c) Calculate the heat gained by the calorimeter for each process.
(d) Calculate $\Delta E$ for each process in $\mathrm{kJ} / \mathrm{mol}$.
(e) Why does this activity allow you to calculate $\Delta E$ and not $\Delta H$ ?
8.123 Of the four reactions in the Formation of Water activity (eChapter 8.14),
(a) Why is $\Delta G$ negative for all the reactions?
(b) Which have positive $\Delta S$ ?
(c) For which is $\Delta G$ temperature dependent? Why?
(d) For which can temperature dependence not be determined from the information available? Why?
8.124 Watch the Airbags movie (eChapter 8.13) and determine the signs of $\Delta H, \Delta S$, and $\Delta G$ for the decomposition of sodium azide. Could the decomposition of sodium azide be used to inflate airbags if the reaction were endothermic? Explain.
8.125 Use the Gibbs Free Energy activity (eChapter 8.14), to determine the signs of each of the thermodynamic properties at $0 \mathrm{~K}, 298 \mathrm{~K}$, and 1500 K .
(a) Which reactions have signs that are not temperature dependent?
(b) Which reactions are endothermic? Which are exothermic?
(c) Which are spontaneous at all temperatures? What are the signs of $\Delta H$ and $\Delta S$ ?
(d) Which are only spontaneous at low temperatures? What are the signs of $\Delta H$ and $\Delta S$ ?
(e) Which are only spontaneous at high temperatures? What are the signs of $\Delta H$ and $\Delta S$ ?

## Chapter

## Gases:

## Their Properties and Behavior

## A quick look around tells you that matter takes different

forms. Most of the things around you are solids, substances whose constituent atoms, molecules, or ions are held rigidly together in a definite way, giving the solid a definite volume and shape. Other substances are liquids,
 whose constituent atoms or molecules are held together less strongly, giving the liquid a definite volume but a changeable and indefinite shape. Still other

## CONTENTS

Without the invisible blanket of air surrounding us, Steven Fossett's voyage around the world in the balloon Spirit of Freedom would not have been possible.

### 9.1 Gases and Gas Pressure

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Joseph S. Schmuckler, "Gases and Their Behavior," J. Chem. Educ., Vol. 57, 1980, 85.
substances are gases, whose constituent atoms or molecules have little attraction for one another and are therefore free to move about in whatever volume is available.

Though gases are few in number-only about a hundred substances are gases at room temperature-their study was enormously important in the historical development of chemical theories. We'll look briefly at this historical development in the present chapter, and we'll see how the behavior of gases can be described.

### 9.1 Gases and Gas Pressure

We live surrounded by a blanket of air-the mixture of gases that make up the earth's atmosphere. As shown in Table 9.1, nitrogen and oxygen account for more than $99 \%$ by volume of dry air. The remaining $1 \%$ is largely argon, with trace amounts of several other substances also present. Carbon dioxide, about which there is so much current concern because of the so-called greenhouse effect, is present in air only to the extent of about $0.037 \%$, or 370 parts per million ( ppm ). Though small, this value has risen in the past 150 years from an estimated 290 ppm in 1850, as the burning of fossil fuels and the deforestation of tropical rain forests have increased.

| TABLE 9.1 | Composition of Dry Air at Sea Level |  |
| :--- | :--- | :--- |
| Constituent | \%Volume | \% Mass |
| $\mathrm{N}_{2}$ | 78.08 | 75.52 |
| $\mathrm{O}_{2}$ | 20.95 | 23.14 |
| Ar | 0.93 | 1.29 |
| $\mathrm{CO}_{2}$ | 0.037 | 0.05 |
| Ne | $1.82 \times 10^{-3}$ | $1.27 \times 10^{-3}$ |
| He | $5.24 \times 10^{-4}$ | $7.24 \times 10^{-5}$ |
| $\mathrm{CH}_{4}$ | $1.7 \times 10^{-4}$ | $9.4 \times 10^{-5}$ |
| Kr | $1.14 \times 10^{-4}$ | $3.3 \times 10^{-4}$ |

Air is typical of gases in many respects, and its behavior illustrates several important points about gases. For instance, gas mixtures are always homogeneous. Unlike liquids, which often fail to mix with one another and which may separate into distinct layers-oil and water, for example-gases always mix thoroughly. Furthermore, gases are compressible. When pressure is applied, the volume of a gas contracts proportionately. Solids and liquids, however, are nearly incompressible, and even the application of great pressure changes their volume only slightly.

Homogeneous mixing and compressibility both result from the fact that the molecules in gases are far apart (Figure 9.1). Mixing occurs because individual gas molecules have little interaction with their neighbors and the chemical identities of those neighbors are therefore irrelevant. In solids and liquids, by contrast, molecules are packed closely together, where they are affected by various attractive and repulsive forces that can inhibit their mixing. Compressibility is possible in gases because less than $0.1 \%$ of the volume of a typical gas is taken up by the molecules themselves under normal circumstances; the remaining $99.9 \%$ is empty space. By contrast, approximately $70 \%$ of a solid's or liquid's volume is taken up by the molecules.

One of the most obvious characteristics of gases is that they exert a measurable pressure on the walls of their container (Figure 9.1b). We're all familiar with pumping

up a tire or inflating a balloon and feeling the hardness that results from the pressure inside. In scientific terms, pressure $(P)$ is defined as a force $F$ exerted per unit area $A$. Force, in turn, is defined as mass ( $m$ ) times acceleration (a), which, on Earth, is usually the acceleration due to gravity, $a=9.81 \mathrm{~m} / \mathrm{s}^{2}$.

$$
\operatorname{Pressure}(P)=\frac{F}{A}=\frac{m \times a}{A}
$$

The SI unit for force is the newton (N), where $1 \mathrm{~N}=1(\mathrm{~kg} \cdot \mathrm{~m}) / \mathrm{s}^{2}$, and the SI unit for pressure is the pascal ( $\mathbf{P a}$ ), where $1 \mathrm{~Pa}=1 \mathrm{~N} / \mathrm{m}^{2}=1 \mathrm{~kg} /\left(\mathrm{m} \cdot \mathrm{s}^{2}\right)$. Expressed in more familiar units, a pascal is actually a very small amount-the pressure exerted by a mass of 10.2 mg resting on an area of $1.00 \mathrm{~cm}^{2}$ :

$$
P=\frac{m \times a}{A}=\frac{(10.2 \mathrm{mg})\left(\frac{1 \mathrm{~kg}}{10^{6} \mathrm{mg}}\right)\left(9.81 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right)}{\left(1.00 \mathrm{~cm}^{2}\right)\left(\frac{1 \mathrm{~m}^{2}}{10^{4} \mathrm{~cm}^{2}}\right)}=\frac{1.00 \times 10^{-4} \frac{\mathrm{~kg} \cdot \mathrm{~m}}{\mathrm{~s}^{2}}}{1.00 \times 10^{-4} \mathrm{~m}^{2}}=1.00 \mathrm{~Pa}
$$

In rough terms, a penny sitting on the tip of your finger exerts a pressure of about 250 Pa.

Just as the air in a tire and a penny on your fingertip exert pressure, the mass of the atmosphere pressing down on the earth's surface exerts what we call atmospheric pressure. In fact, a $1.00 \mathrm{~m}^{2}$ column of air extending from the earth's surface through the upper atmosphere has a mass of about $10,300 \mathrm{~kg}$, producing an atmospheric pressure of approximately $101,000 \mathrm{~Pa}$, or 101 kPa (Figure 9.2).

$$
P=\frac{m \times a}{A}=\frac{10,300 \mathrm{~kg} \times 9.81 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}}{1.00 \mathrm{~m}^{2}}=101,000 \mathrm{~Pa}=101 \mathrm{kPa}
$$

As is frequently the case with SI units, which must serve many scientific disciplines, the pascal is an inconvenient size for most chemical measurements. Thus, the alternative pressure units millimeter of mercury ( $\mathbf{m m ~ H g}$ ) and atmosphere (atm) are more frequently used.

The millimeter of mercury, also called a torr after the seventeenth-century Italian scientist Evangelista Torricelli (1608-1647), is based on atmospheric pressure

4 FIGURE 9.1 (a) A gas is a large collection of particles moving at random throughout a volume that is primarily empty space. (b) Collisions of randomly moving particles with the walls of the container exert a force per unit area that we perceive as gas pressure.
-

$\triangle$ Forcing more air into the tire increases the pressure and makes the tire feel "hard."


A FIGURE 9.2 A column of air $1.00 \mathrm{~m}^{2}$ in cross-sectional area extending from the earth's surface through the upper atmosphere has a mass of about $10,300 \mathrm{~kg}$, producing an atmospheric pressure of approximately $101,000 \mathrm{~Pa}$.


FIGURE 9.4 Open-end manometers for measuring pressure in a gas-filled bulb. In (a), the pressure in the bulb is lower than atmospheric, so the mercury level is higher in the arm open to the bulb; in (b), the pressure in the bulb is higher than atmospheric, so the mercury level is higher in the arm open to the atmosphere.

[^12]measurements using a mercury barometer. As shown in Figure 9.3, a barometer consists simply of a long, thin tube that is sealed at one end, filled with mercury, and then inverted into a dish of mercury. Some mercury runs from the tube into the dish until the downward pressure of the mercury in the column is exactly balanced by the outside atmospheric pressure, which presses on the mercury in the dish and pushes it up the column. The height of the mercury column varies slightly from day to day depending on the altitude and weather conditions, but standard atmospheric pressure at sea level is defined to be exactly 760 mm Hg .

FIGURE 9.3 A mercury barometer is used to measure atmospheric pressure by determining the height of a mercury column supported in a sealed glass tube. The downward pressure of the mercury in the column is exactly balanced by the outside atmospheric pressure that presses down on the mercury in the dish and pushes it up the column.


Knowing the density of mercury ( $1.35951 \times 10^{4} \mathrm{~kg} / \mathrm{m}^{3}$ at $0^{\circ} \mathrm{C}$ ) and the acceleration due to gravity $\left(9.80665 \mathrm{~m} / \mathrm{s}^{2}\right)$, it's possible to calculate the pressure exerted by the column of mercury $760 \mathrm{~mm}(0.760 \mathrm{~m})$ in height. Thus, 1 standard atmosphere of pressure ( 1 atm ), or 760 mm Hg , is equal to $101,325 \mathrm{~Pa}$ :

$$
\begin{gathered}
P=(0.760 \mathrm{~m})\left(1.35951 \times 10^{4} \frac{\mathrm{~kg}}{\mathrm{~m}^{3}}\right)\left(9.80665 \frac{\mathrm{~m}}{\mathrm{~s}^{2}}\right)=101,325 \mathrm{~Pa} \\
\mathbf{1} \mathbf{~ a t m}=760 \mathbf{~ m m ~ H g}=\mathbf{1 0 1 , 3 2 5} \mathbf{P a}
\end{gathered}
$$

Gas pressure inside a container is often measured using an open-end manometer, a simple instrument similar in principle to the mercury barometer. As shown in Figure 9.4, an open-end manometer consists of a U-tube filled with mercury, with one end connected to a gas-filled container and the other end open to the

atmosphere. The difference between the pressure of the gas and the pressure of the atmosphere is equal to the difference between the heights of the mercury levels in the two arms of the U-tube. If the gas pressure inside the container is less than atmospheric, the mercury level is higher in the arm connected to the container (Figure 9.4a). If the gas pressure inside the container is greater than atmospheric, the mercury level is higher in the arm open to the atmosphere (Figure 9.4b).

## Worked Example 9.1

Typical atmospheric pressure on top of Mt. Everest $(29,035 \mathrm{ft})$ is 265 mm Hg . Convert this value to pascals and to atmospheres.

## Strategy

Use the conversion factors $1 \mathrm{~atm} / 760 \mathrm{~mm} \mathrm{Hg}$ and $101,325 \mathrm{~Pa} / 760 \mathrm{~mm} \mathrm{Hg}$ to carry out the necessary calculations.

## Solution

$$
\begin{aligned}
& 265 \mathrm{~mm} \mathrm{Hg} \times \frac{101,325 \mathrm{~Pa}}{760 \mathrm{~mm} \mathrm{Hg}}=3.53 \times 10^{4} \mathrm{~Pa} \\
& 265 \mathrm{~mm} \mathrm{Hg} \times \frac{1 \mathrm{~atm}}{760 \mathrm{~mm} \mathrm{Hg}}=0.349 \mathrm{~atm}
\end{aligned}
$$

Ballpark Check One atmosphere equals 760 mm Hg pressure. Since 265 mm Hg is about $1 / 3$ of 760 mm Hg , the air pressure on Mt. Everest is about $1 / 3$ of standard atmospheric pressure-approximately $30,000 \mathrm{~Pa}$, or 0.3 atm .

## Worked Example 9.2

Assume that you are using an open-end manometer (Figure 9.4) filled with mineral oil rather than mercury. What is the gas pressure in the bulb (in millimeters of mercury) if the level of mineral oil in the arm connected to the bulb is 237 mm higher than the level in the arm connected to the atmosphere and atmospheric pressure is 746 mm Hg ? The density of mercury is $13.6 \mathrm{~g} / \mathrm{mL}$, and the density of mineral oil is $0.822 \mathrm{~g} / \mathrm{mL}$.

## Strategy

The gas pressure in the bulb equals the difference between the outside pressure and the manometer reading. The manometer reading indicates that the pressure of the gas in the bulb is less than atmospheric because the liquid level is higher on the side connected to the sample. Because mercury is more dense than mineral oil by a factor of $13.6 / 0.822$, or 16.5 , a given pressure will hold a column of mercury only $1 / 16.5$ times the height of a column of mineral oil.

## Solution

$$
\begin{gathered}
P_{\text {manometer }}=237 \mathrm{~mm} \text { mineral oil } \times \frac{0.822 \mathrm{~mm} \mathrm{Hg}}{13.6 \mathrm{~mm} \text { mineral oil }}=14.3 \mathrm{~mm} \mathrm{Hg} \\
P_{\text {bulb }}=P_{\text {outside }}-P_{\text {manometer }}=746 \mathrm{~mm} \mathrm{Hg}-14.3 \mathrm{~mm} \mathrm{Hg}=732 \mathrm{~mm} \mathrm{Hg}
\end{gathered}
$$

PROBLEM 9.1 Pressures are often given in the unit pounds per square inch (psi). How many pounds per square inch correspond to 1.00 atm ? To 1.00 mm Hg ?

PROBLEM 9.2 If the density of water is $1.00 \mathrm{~g} / \mathrm{mL}$ and the density of mercury is $13.6 \mathrm{~g} / \mathrm{mL}$, how high a column of water (in meters) can be supported by standard atmospheric pressure?


A Atmospheric pressure decreases as altitude increases. On the top of Mt. Everest, typical atmospheric pressure is 265 mm Hg.
\& Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Boiling at Reduced Pressure," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 24-25.

B Bassam Z. Shakhashiri,
"Boyle's Law," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp. 14-19.

Gas Laws activity

Bassam Z. Shakhashiri, "Effect of Pressure on the Size of a Balloon," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp. 12-13.


Bassam Z. Shakhashiri,
"Boyle's Law and the Mass of a Textbook," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp. 20-23.

[^13]- PROBLEM 9.3 What is the pressure (in atmospheres) in a container of gas connected to a mercury-filled, open-end manometer if the level in the arm connected to the container is 24.7 cm higher than in the arm open to the atmosphere and atmospheric pressure is 0.975 atm ?
$\curvearrowleft$ KEY CONCEPT PROBLEM 9.4 What is the pressure of the gas inside the following apparatus (in mm Hg ) if the outside pressure is 750 mm Hg ?



### 9.2 The Gas Laws

Unlike solids and liquids, different gases show remarkably similar physical behavior regardless of their chemical makeup. Helium and fluorine, for example, are vastly different in their chemical properties yet are almost identical in much of their physical behavior. Numerous observations made in the late 1600s showed that the physical properties of any gas can be defined by four variables: pressure $(P)$, temperature ( $T$ ), volume ( $V$ ), and amount, or number of moles ( $n$ ). The specific relationships among these four variables are called the gas laws, and a gas whose behavior follows the laws exactly is called an ideal gas.

## Boyle's Law: The Relationship Between Volume and Pressure

Imagine that you have a sample of gas inside a cylinder with a movable piston at one end (Figure 9.5). What would happen if you were to decrease the volume of the gas by pushing the piston partway down? Experience tells you that you would feel a resistance to pushing the piston because the pressure of the gas in the cylinder would increase. According to Boyle's law, the volume of a fixed amount of gas at a constant temperature varies inversely with its pressure. If the gas pressure is halved, the gas volume doubles; if the pressure is doubled, the volume is halved.

FIGURE 9.5 Boyle's law. At constant $n$ and $T$, the volume of an ideal gas decreases proportionately as its pressure increases. If the pressure is doubled, the volume is halved. If the pressure is halved, the volume is doubled.


Boyle's law The volume of an ideal gas varies inversely with pressure. That is, $P$ times $V$ is constant when $n$ and $T$ are kept constant. (The symbol $\propto$ means "is proportional to," and $k$ denotes a constant.)

$$
V \propto 1 / P \quad \text { or } \quad P V=k \text { at constant } n \text { and } T
$$

The validity of Boyle's law can be demonstrated by making a simple series of pressure-volume measurements on a gas sample (Table 9.2) and plotting them as in Figure 9.6. When $V$ is plotted versus $P$, as in Figure 9.6a, the result is a curve in the form of a hyperbola. When $V$ is plotted versus $1 / P$, as in Figure 9.6b, the result is a straight line. Such graphical behavior is characteristic of mathematical equations of the form $y=m x+b$. In this case, $y=V, m=$ the slope of the line (the constant $k$ in the present instance), $x=1 / P$, and $b=$ the $y$-intercept (a constant; 0 in the present instance). (See Appendix A. 3 for a review of linear equations.)

$$
\begin{aligned}
& V=k\left(\frac{1}{P}\right)+0 \quad(\text { or } P V=k) \\
& \uparrow \uparrow \uparrow \\
& y=m x+b
\end{aligned}
$$



A FIGURE 9.6 Boyle's law. (a) A plot of $V$ versus $P$ for a gas sample is a hyperbola, but (b) a plot of $V$ versus $1 / P$ is a straight line. Such a straight-line graph is characteristic of equations having the form $y=m x+b$.

## Charles' Law: The Relationship Between Volume and Temperature

Imagine that you again have a gas sample inside a cylinder with a movable piston at one end (Figure 9.7). What would happen if you were to raise the temperature of the sample while letting the piston move freely to keep the pressure constant? Common sense tells you that the piston would move up because the volume of the gas in the cylinder would expand. According to Charles' law, the volume of a fixed amount of an ideal gas at a constant pressure varies directly with its absolute temperature. If the gas temperature in kelvins is doubled, the volume is doubled; if the gas temperature is halved, the volume is halved.

[^14]

## N. Szczepanski, "A Simple

 Demonstration of Charles' Law," J. Chem. Educ. 71, 1994, 433. Bassam Z. Shakhashiri, "Thermal Expansion of Gases," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp. 24-27.Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Charles' Law: The Relationship Between Volume and Temperature of a Gas," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), p. 23.


John T. Petty, "Charles' Law of Gases: A Simple Demonstration," J. Chem. Educ. 72, 1995, 257.

Figure 9.8 and Table 9.3

TABLE 9.3 TemperatureVolume
Measurements on a Gas
Sample at Constant $n, P$

| Temperature <br> (K) | Volume <br> (L) |
| :--- | :--- |
| 123 | 0.45 |
| 173 | 0.63 |
| 223 | 0.82 |
| 273 | 1.00 |
| 323 | 1.18 |
| 373 | 1.37 |

R. P. Graham, "Guy-Lussac: Chemist Extraordinary," J. Chem. Educ. 58, 1981, 789.

Harold Goldwhite, "GuyLussac after 200 Years," J. Chem. Educ. 55, 1978, 366-368.

FIGURE 9.7 Charles' law. At constant $n$ and $P$, the volume of an ideal gas increases proportionately as its absolute temperature increases. If the absolute temperature is doubled, the volume is doubled. If the absolute temperature is halved, the volume is halved.


The validity of Charles' law can be demonstrated by making a series of temperature-volume measurements on a gas sample, giving the results listed in Table 9.3. Like Boyle's law, Charles' law also takes the mathematical form $y=m x+b$, where $y=V, m=$ the slope of the line (the constant $k$ in the present instance), $x=T$, and $b=$ the $y$-intercept ( 0 in the present instance). A plot of $V$ versus $T$ is therefore a straight line whose slope is the constant $k$ (Figure 9.8).

$$
\begin{aligned}
& V=k T+0 \\
& \uparrow \uparrow \uparrow \begin{array}{l}
\uparrow \\
y=m x+b
\end{array} \quad\left(\text { or } \frac{V}{T}=k\right) .
\end{aligned}
$$


(a)

(b)

A FIGURE 9.8 Charles' law. A plot of $V$ versus $T$ for a gas sample is a straight line that can be extrapolated to absolute zero.

The plots of volume versus temperature shown in Figure 9.8 demonstrate an interesting point. When temperature is plotted on the Celsius scale, as in Figure 9.8a, the straight line can be extrapolated to $V=0$ at $T=-273^{\circ} \mathrm{C}$. Because matter can't have a negative volume, this extrapolation suggests that $-273^{\circ} \mathrm{C}$ must be the lowest possible temperature, or absolute zero on the Kelvin scale. In fact, the approximate value of absolute zero was first determined using this simple method.

## Avogadro's Law: The Relationship Between Volume and Amount

Imagine that you have two more gas samples inside cylinders with movable pistons (Figure 9.9). One cylinder contains 1 mol of a gas and the other cylinder contains 2 mol of the gas at the same temperature and pressure as the first. Common sense says that the gas in the second cylinder will have twice the volume of the gas in the first cylinder because there is twice as much of it. According to Avogadro's law, the volume of an ideal gas at a fixed pressure and temperature depends on its molar amount. If the amount of the gas is halved, the gas volume is halved; if the amount is doubled, the volume is doubled.

© FIGURE 9.9 Avogadro＇s law．At constant $T$ and $P$ ，the volume of an ideal gas increases proportionately as its molar amount increases．If the molar amount is doubled，the volume is doubled．If the molar amount is halved，the volume is halved．

Avogadro＇s law The volume of an ideal gas varies directly with its molar amount．That is，$V$ divided by $n$ is constant when $T$ and $P$ are held constant．

$$
V \propto n \quad \text { or } \quad V / n=k \text { at constant } T \text { and } P
$$

Put another way，Avogadro＇s law also says that equal volumes of different gases at the same temperature and pressure contain the same molar amounts．A 1 L container of oxygen contains the same number of moles as a 1 L container of helium，fluorine，argon，or any other gas at the same $T$ and $P$ ．Experiments show that 1 mol of an ideal gas occupies a volume（the standard molar volume）of 22.414 L at $0^{\circ} \mathrm{C}$ and 1.0000 atm pressure．For comparison，the standard molar vol－ ume is almost exactly the same as the volume of three basketballs．

## Worked Key Concept Example 9.3

Show the approximate level of the movable piston in drawings（a）and（b）after the indicated changes have been made to the initial gas sample．

（initial）
$T=250 \mathrm{~K}$
$n=0.140 \mathrm{~mol}$
$P=1.0 \mathrm{~atm}$

（a）
$T=375 \mathrm{~K}$
$n=0.140 \mathrm{~mol}$
$P=1.0 \mathrm{~atm}$

（b）
$T=250 \mathrm{~K}$
$n=0.070 \mathrm{~mol}$
$P=0.50 \mathrm{~atm}$

## Strategy

Identify which of the variables $P, n$ ，and $T$ have changed，and calculate the effect of each change on the volume according to the appropriate gas law．

## Solution

（a）The temperature $T$ has increased by a factor of $375 / 250=1.5$ ，while the molar amount $n$ and the pressure $P$ are unchanged．According to Charles＇law，the volume will increase by a factor of 1.5 ．
（b）The temperature $T$ is unchanged，while both the molar amount $n$ and the pres－ sure $P$ are halved．According to Avogadro＇s law，halving the molar amount will

Students tend to remember the standard molar volume while forgetting that this value holds true only under stan－ dard conditions．One mole of an ideal gas occupies 22．4 L only at 1.00 atm and 273.15 K ．
halve the volume, and according to Boyle's law, halving the pressure will double the volume. The two changes cancel, so the volume is unchanged.


(a)
$T=375 \mathrm{~K}$
$n=0.140 \mathrm{~mol}$
$P=1.0 \mathrm{~atm}$

(b)
$T=250 \mathrm{~K}$
$n=0.070 \mathrm{~mol}$
$P=0.50 \mathrm{~atm}$

- KEY CONCEPT PROBLEM 9.5 Show the approximate level of the movable piston in drawings (a) and (b) after the indicated changes have been made to the initial gas sample.



### 9.3 The Ideal Gas Law

All three of the gas laws discussed in the previous section can be combined into a single statement called the ideal gas law, which describes how the volume of a gas is affected by changes in pressure, temperature, and amount. When the values of any three of the variables $P, V, T$, and $n$ are known, the value of the fourth can be calculated using the ideal gas law. The constant $R$ in the equation is called the gas constant and has the same value for all gases.

$$
\text { IDEAL GAS LAW } \quad V=\frac{n R T}{P} \quad \text { or } \quad P V=n R T
$$

The ideal gas law can be rearranged in different ways to take the form of Boyle's law, Charles' law, or Avogadro's law.

$$
\begin{array}{llrl}
\text { Boyle's law: } & P V & =n R T=k & \\
\text { Charles' law: } & \frac{V}{T} & =\frac{n R}{P}=k & \\
\text { (When } n \text { and } T \text { are constant) } \\
\text { Avogadro's law: } P \text { are constant) } & \frac{V}{n} & =\frac{R T}{P}=k & \\
\text { (When } T \text { and } P \text { are constant) }
\end{array}
$$

The value of the gas constant $R$ can be calculated from a knowledge of the standard molar volume of a gas. Since 1 mol of a gas occupies a volume of
22.414 L at $0^{\circ} \mathrm{C}(273.15 \mathrm{~K})$ and 1 atm pressure, the gas constant $R$ is equal to $0.082058(\mathrm{~L} \cdot \mathrm{~atm}) /(\mathrm{K} \cdot \mathrm{mol})$, or $8.3145 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ in SI units:

$$
\begin{aligned}
R & =\frac{P \cdot V}{n \cdot T}=\frac{(1 \mathrm{~atm})(22.414 \mathrm{~L})}{(1 \mathrm{~mol})(273.15 \mathrm{~K})}=0.082058 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}} \\
& =8.3145 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol}) \quad(\text { When } P \text { is in pascals and } V \text { is in cubic meters })
\end{aligned}
$$

The specific conditions used in the calculation- 1 atm pressure and $0^{\circ} \mathrm{C}$ (273.15 K) —are said to represent standard temperature and pressure, abbreviated STP. These standard conditions are generally used when reporting measurements on gases. Note that the standard temperature for gas measurements $\left(0^{\circ} \mathrm{C}\right.$, or 273.15 K ) is different from that usually assumed for thermodynamic measurements $\left(25^{\circ} \mathrm{C}\right.$, or 298.15 K ; Section 8.6$)$. Note also that the standard pressure for gas measurements, still listed here and in most other books as 1 atm ( $101,325 \mathrm{~Pa}$ ), has been redefined to be 1 bar $(100,000 \mathrm{~Pa})$. Thus, the new standard pressure is 0.986923 atm , making the standard molar volume 22.711 L rather than 22.414 L .

Standard temperature and pressure (STP) for gases $T=0^{\circ} \mathrm{C} \quad P=1 \mathrm{~atm}$
The name ideal gas law implies that there must be some gases whose behavior is nonideal. In fact, there is no such thing as an ideal gas that obeys the equation perfectly under all circumstances; all real gases deviate slightly from the behavior predicted by the law. As Table 9.4 shows, for example, the actual molar volume of a real gas often differs slightly from the 22.414 L ideal value. Under most conditions, though, the deviations from ideal behavior are so slight as to make little difference. We'll discuss circumstances in Section 9.8 where the deviations are greater.

TABLE 9.4 Molar Volumes of Some Real Gases at STP


## Worked Example 9.4

How many moles of air are in the lungs of an average adult with a lung capacity of 3.8 L? Assume that the person is at 1.00 atm pressure and has a normal body temperature of $37^{\circ} \mathrm{C}$.

## Strategy

This problem asks for a value of $n$ when $V, P$, and $T$ are given. Rearrange the ideal gas law to the form $n=P V / R T$, convert the temperature from degrees Celsius to Kelvin, and substitute the given values of $P, V$, and $T$ into the equation.
Solution

$$
n=\frac{P V}{R T}=\frac{(1.00 \mathrm{~atm})(3.8 \mathrm{~L})}{\left(0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)(310 \mathrm{~K})}=0.15 \mathrm{~mol}
$$

The lungs of an average adult hold 0.15 mol of air.
$\checkmark$ BALLPARK CHECK A lung volume of 4 L is about $1 / 6$ of 22.4 L , the standard molar volume of an ideal gas. Thus, the lungs have a capacity of about $1 / 6 \mathrm{~mol}$, or 0.17 mol .

© How many moles of methane are in these tanks?

## Worked Example 9.5

In a typical automobile engine, the mixture of gasoline and air in a cylinder is compressed from 1.0 atm to 9.5 atm . If the uncompressed volume of the cylinder is 410 mL , what is the volume (in milliliters) when the mixture is fully compressed?

## Strategy

This is a Boyle's law problem because only $P$ and $V$ are changing, while $n$ and $T$ remain fixed. We can therefore set up the following equation and solve for $V_{\text {final }}$ -

$$
(P V)_{\mathrm{initial}}=(P V)_{\mathrm{final}}=n R T
$$

## Solution

$$
V_{\text {final }}=\frac{(P V)_{\text {initial }}}{P_{\text {final }}}=\frac{(1.0 \mathrm{~atm})(410 \mathrm{~mL})}{9.5 \mathrm{~atm}}=43 \mathrm{~mL}
$$

$\checkmark$ BALLPARK CHECK Because the pressure in the cylinder increases about 10-fold, the volume must decrease about 10 -fold according to Boyle's law, from approximately 400 mL to 40 mL .

PROBLEM 9.6 How many moles of methane gas, $\mathrm{CH}_{4}$, are in a storage tank with a volume of $1.000 \times 10^{5} \mathrm{~L}$ at STP? How many grams?

- PROBLEM 9.7 An aerosol spray can with a volume of 350 mL contains 3.2 g of propane gas $\left(\mathrm{C}_{3} \mathrm{H}_{8}\right)$ as propellant. What is the pressure (in atmospheres) of gas in the can at $20^{\circ} \mathrm{C}$ ?

PROBLEM 9.8 A helium gas cylinder of the sort used to fill balloons has a volume of 43.8 L and a pressure of $1.51 \times 10^{4} \mathrm{kPa}$ at $25.0^{\circ} \mathrm{C}$. How many moles of helium are in the tank?

- PROBLEM 9.9 What final temperature $\left({ }^{\circ} \mathrm{C}\right)$ is required for the pressure inside an automobile tire to increase from 2.15 atm at $0^{\circ} \mathrm{C}$ to 2.37 atm , assuming the volume remains constant?

KEY CONCEPT PROBLEM 9.10 Show the approximate level of the movable piston in drawings (a), (b), and (c) after the indicated changes have been made to the gas.


## 9.4 | Stoichiometric Relationships with Gases

Many chemical reactions, including some of the most important processes in the chemical industry, involve gases. Thirteen million tons of ammonia, for example, are manufactured each year in the United States by the reaction of hydrogen with nitrogen according to the equation $3 \mathrm{H}_{2}+\mathrm{N}_{2} \rightarrow 2 \mathrm{NH}_{3}$. Thus, it's necessary to be able to calculate amounts of gaseous reactants just as it's necessary to calculate amounts of solids, liquids, and solutions (Sections 3.4-3.9).

Most gas calculations are just applications of the ideal gas law in which three of the variables $P, V, T$, and $n$ are known, and the fourth variable must be calculated. For example, the reaction used in the deployment of automobile air bags is the high-temperature decomposition of sodium azide, $\mathrm{NaN}_{3}$, to produce $\mathrm{N}_{2}$ gas. (The sodium is then removed by a subsequent reaction.) How many liters of $\mathrm{N}_{2}$ at 1.15 atm and $30^{\circ} \mathrm{C}$ are produced by decomposition of 145 g of $\mathrm{NaN}_{3}$ ?

$$
2 \mathrm{NaN}_{3}(s) \longrightarrow 2 \mathrm{Na}(s)+3 \mathrm{~N}_{2}(g)
$$

Values for $P$ and $T$ are given, the value of $n$ can be calculated, and the ideal gas law will then let us find $V$. To find $n$, the number of moles of $\mathrm{N}_{2}$ gas produced, we first need to find how many moles of $\mathrm{NaN}_{3}$ are in 145 g :

$$
\begin{aligned}
& \text { Molar mass of } \mathrm{NaN}_{3}=65.0 \mathrm{~g} / \mathrm{mol} \\
& \text { Moles of } \mathrm{NaN}_{3}=145 \mathrm{~g} \mathrm{NaN}_{3} \times \frac{1 \mathrm{~mol} \mathrm{NaN}_{3}}{65.0 \mathrm{~g} \mathrm{NaN}_{3}}=2.23 \mathrm{~mol} \mathrm{NaN}_{3}
\end{aligned}
$$

Next, find how many moles of $\mathrm{N}_{2}$ are produced in the decomposition reaction. According to the balanced equation, 2 mol of $\mathrm{NaN}_{3}$ yields 3 mol of $\mathrm{N}_{2}$, so 2.23 mol of $\mathrm{NaN}_{3}$ yields 3.35 mol of $\mathrm{N}_{2}$ :

$$
\text { Moles of } \mathrm{N}_{2}=2.23 \mathrm{~mol} \mathrm{NaN}_{3} \times \frac{3 \mathrm{~mol} \mathrm{~N}_{2}}{2 \mathrm{~mol} \mathrm{NaN}_{3}}=3.35 \mathrm{~mol} \mathrm{~N}_{2}
$$

Finally, use the ideal gas law to calculate the volume of $\mathrm{N}_{2}$. Remember to use the Kelvin temperature ( 303 K ) rather than the Celsius temperature $\left(30^{\circ} \mathrm{C}\right)$ in the calculation:

$$
V=\frac{n R T}{P}=\frac{3.35 \mathrm{~mol} \times 0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}} \times 303 \mathrm{~K}}{1.15 \mathrm{~atm}}=72.4 \mathrm{~L}
$$

Worked Example 9.6 illustrates another gas stoichiometry calculation.
Still other applications of the ideal gas law make it possible to calculate such properties as density and molar mass. Densities are calculated by weighing a known volume of a gas at a known temperature and pressure, as shown in Figure 9.10. Using the ideal gas law to find the volume at STP and then dividing the measured mass by the volume gives the density at STP. Worked Example 9.7 gives a sample calculation.

Molar masses, and therefore molecular masses, can also be calculated using the ideal gas law. Imagine, for instance, that an unknown gas bubbling up in a swamp is collected, placed in a sample bulb, and found to have a density of $0.714 \mathrm{~g} / \mathrm{L}$ at STP. What is the molecular mass of the gas?

Let's assume that we have 1.00 L of sample, which has a mass of 0.714 g . Since the density is measured at STP, we know $T, P$, and $V$, and we need to find $n$, the molar amount of gas that has a mass of 0.714 g :

$$
n=\frac{P V}{R T}=\frac{(1.00 \mathrm{~atm})(1.00 \mathrm{~L})}{\left(0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)(273 \mathrm{~K})}=0.0446 \mathrm{~mol}
$$

Dividing the mass of the sample by the number of moles then gives the molar mass:

$$
\text { Molar mass }=\frac{0.714 \mathrm{~g}}{0.0446 \mathrm{~mol}}=16.0 \mathrm{~g} / \mathrm{mol}
$$

Thus, the molar mass of the unknown gas (actually methane, $\mathrm{CH}_{4}$ ) is $16.0 \mathrm{~g} / \mathrm{mol}$, and the molecular mass is 16.0 amu .


A Automobile air bags are inflated with $\mathrm{N}_{2}$ gas produced by decomposition of sodium azide.

77. Andreas Madlung, "The Chemistry Behind the Air Bag," J. Chem. Educ. 73, 1996, 347-348.

0 William L. Bell, "Chemistry of Air Bags," J. Chem. Educ. 67, 1990, 61.


A FIGURE 9.10 Determining the density of an unknown gas. A bulb of known volume is evacuated, weighed when empty, filled with gas at a known pressure and temperature, and weighed again. Dividing the mass by the volume gives the density.

Bassam Z. Shakhashiri, "Determination of the Molecular Mass of a Volatile Liquid," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983) pp. 51-54. A boilingwater bath is used to heat a volatile liquid until it is vaporized, completely filling an Erlenmeyer flask covered by aluminum foil with a pinhole orifice. From atmospheric pressure, bath temperature, volume of the flask, and mass of recondensed vapor, the molar mass of the volatile liquid is determined.

Lee R. Summerlin, and James L.
Ealy, Jr., "Determining the Molecular Weight of a Gas," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), pp. 19-20. The molar mass of butane is determined by the vapor density method.

Density of Gases activity

It's often true in chemistry, particularly in gas-law calculations, that a problem can be solved in more than one way. As an alternative method for calculating the molar mass of the unknown swamp gas, you might recognize that 1 mol of an ideal gas has a volume of 22.4 L at STP. Since 1 L of the unknown gas has a mass of $0.714 \mathrm{~g}, 22.4 \mathrm{~L}$ of the gas ( 1 mol ) has a mass of 16.0 g :

$$
\text { Molar mass }=\left(0.714 \frac{\mathrm{~g}}{\mathrm{~L}}\right)\left(22.4 \frac{\mathrm{~L}}{\mathrm{~mol}}\right)=16.0 \mathrm{~g} / \mathrm{mol}
$$

Worked Example 9.8 illustrates another calculation of the molar mass of an unknown gas.

## Worked Example 9.6

A typical high-pressure tire on a racing bicycle might have a volume of 365 mL and a pressure of 7.80 atm at $25^{\circ} \mathrm{C}$. Suppose the rider filled the tire with helium to minimize weight. What is the mass of the helium in the tire?

## Strategy

We are given $V, P$, and $T$, and we need to use the ideal gas law to calculate $n$, the number of moles of helium in the tire. With $n$ known, we then do a mole-to-mass conversion.

## SOlUTION

$$
\begin{aligned}
& \quad n=\frac{P V}{R T}=\frac{(7.80 \mathrm{~atm})(0.365 \mathrm{~L})}{\left(0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)(298 \mathrm{~K})}=0.116 \mathrm{~mol} \\
& \text { Grams of helium }=0.116 \mathrm{~mol} \mathrm{He} \times \frac{4.00 \mathrm{~g} \mathrm{He}}{1 \mathrm{~mol} \mathrm{He}}=0.464 \mathrm{~g}
\end{aligned}
$$

## Worked Example 9.7

What is the density (in grams per liter) of ammonia at STP if the gas in a 1.000 L bulb weighs 0.672 g at $25^{\circ} \mathrm{C}$ and 733.4 mm Hg pressure?

## Strategy

The density of any substance is mass divided by volume. For the ammonia sample, the mass is 0.672 g but the volume of the gas is given under nonstandard conditions and must first be converted to STP. Because the amount of sample $n$ is constant, we can set the quantity $P V / R T$ measured under nonstandard conditions equal to $P V / R T$ at STP and then solve for $V$ at STP.

## SOlUTION

$$
\begin{gathered}
n=\left(\frac{P V}{R T}\right)_{\text {measured }}=\left(\frac{P V}{R T}\right)_{\mathrm{STP}} \text { or } V_{\mathrm{STP}}=\left(\frac{P V}{R T}\right)_{\text {measured }} \times\left(\frac{R T}{P}\right)_{\mathrm{STP}} \\
V_{\mathrm{STP}}=\left(\frac{733.4 \mathrm{~mm} \mathrm{Hg} \times 1.000 \mathrm{~L}}{298 \mathrm{~K}}\right)\left(\frac{273 \mathrm{~K}}{760 \mathrm{~mm} \mathrm{Hg}}\right)=0.884 \mathrm{~L}
\end{gathered}
$$

The amount of gas in the 1.000 L bulb under the measured nonstandard conditions would have a volume of only 0.884 L at STP. Dividing the given mass by this volume gives the density of ammonia at STP:

$$
\text { Density }=\frac{\text { Mass }}{\text { Volume }}=\frac{0.672 \mathrm{~g}}{0.884 \mathrm{~L}}=0.760 \mathrm{~g} / \mathrm{L}
$$

To identify the contents of an unlabeled cylinder of gas, a sample was collected and found to have a density of $5.380 \mathrm{~g} / \mathrm{L}$ at $15^{\circ} \mathrm{C}$ and 736 mm Hg pressure. What is the molar mass of the gas?

## Strategy

Let's assume we have a 1.000 L sample of the gas, which weighs 5.380 g . We know the temperature, volume, and pressure of the gas and can therefore use the ideal gas law to find $n$, the number of moles in the sample. Dividing the mass by the number of moles then gives the molar mass.

## Solution

$$
\begin{gathered}
P V=n R T \text { or } n=\frac{P V}{R T} \\
n=\frac{\left(736 \mathrm{~mm} \mathrm{Hg} \times \frac{1 \mathrm{~atm}}{760 \mathrm{~mm} \mathrm{Hg}}\right)(1.000 \mathrm{~L})}{\left(0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)(288 \mathrm{~K})}=0.0410 \mathrm{~mol} \\
\frac{5.380 \mathrm{~g}}{0.410 \mathrm{~mol}}=131 \mathrm{~g} / \mathrm{mol}
\end{gathered}
$$

The gas is probably xenon (atomic mass $=131.3 \mathrm{amu})$.

- PROBLEM 9.11 Carbonate-bearing rocks like limestone $\left(\mathrm{CaCO}_{3}\right)$ react with dilute acids such as HCl to produce carbon dioxide, according to the equation

$$
\mathrm{CaCO}_{3}(s)+2 \mathrm{HCl}(a q) \longrightarrow \mathrm{CaCl}_{2}(a q)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
$$

How many grams of $\mathrm{CO}_{2}$ are formed by complete reaction of 33.7 g of limestone? What is the volume (in liters) of this $\mathrm{CO}_{2}$ at STP?

- PROBLEM 9.12 Propane gas $\left(\mathrm{C}_{3} \mathrm{H}_{8}\right)$ is used as a fuel in rural areas. How many liters of $\mathrm{CO}_{2}$ are formed at STP by the complete combustion of the propane in a container with a volume of 15.0 L and a pressure of 4.5 atm at $25^{\circ} \mathrm{C}$ ? The unbalanced equation is

$$
\mathrm{C}_{3} \mathrm{H}_{8}(g)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
$$

PROBLEM 9.13 A foul-smelling gas produced by the reaction of HCl with $\mathrm{Na}_{2} \mathrm{~S}$ was collected, and a 1.00 L sample was found to have a mass of 1.52 g at STP. What is the molecular mass of the gas? What is its likely formula and name?

### 9.5 Partial Pressure and Dalton's Law

Just as the gas laws apply to all pure gases, regardless of chemical identity, they also apply to mixtures of gases, such as air. The pressure, volume, temperature, and amount of a gas mixture are all related by the ideal gas law.

What is responsible for the pressure in a gas mixture? Because the pressure of a pure gas at constant temperature and volume is proportional to its amount ( $P=n R T / V)$, the pressure contribution from each individual gas in a mixture is also proportional to its amount in the mixture. In other words, the total pressure exerted by a mixture of gases in a container at constant $V$ and $T$ equals the sum of the pressures of each individual gas in the container, a statement known as Dalton's law of partial pressures.

Dalton's law of
partial pressures
$P_{\text {total }}=P_{1}+P_{2}+P_{3}+\ldots$ At constant $V$ and $T$, where $P_{1}, P_{2}, \ldots$ refer to the pressures each individual gas would have if it were alone.

$\triangle$ Carbonate-bearing rocks like limestone $\left(\mathrm{CaCO}_{3}\right)$ react with dilute acids such as HCl to produce bubbles of carbon dioxide.

The individual pressures of the various gases in the mixture, $P_{1}, P_{2}$, and so forth, are called partial pressures and refer to the pressure each individual gas would exert if it were alone in the container. That is,

$$
P_{1}=n_{1}\left(\frac{R T}{V}\right) \quad P_{2}=n_{2}\left(\frac{R T}{V}\right) \quad P_{3}=n_{3}\left(\frac{R T}{V}\right) \quad \ldots \text { and so forth }
$$

But because all the gases in the mixture have the same temperature and volume, we can rewrite Dalton's law to indicate that the total pressure depends only on the total molar amount of gas present and not on the chemical identities of the individual gases:

$$
P_{\text {total }}=\left(n_{1}+n_{2}+n_{3}+\cdots\right)\left(\frac{R T}{V}\right)
$$

The concentration of any individual component in a gas mixture is usually expressed as a mole fraction ( $\boldsymbol{X}$ ), which is defined simply as the number of moles of the component divided by the total number of moles in the mixture:

$$
- \text { mole fraction }(X)=\frac{\text { Moles of component }}{\text { Total moles in mixture }}
$$

The mole fraction of component 1 , for example, is

$$
X_{1}=\frac{n_{1}}{n_{1}+n_{2}+n_{3}+\cdots}=\frac{n_{1}}{n_{\text {total }}}
$$

But because $n=P V / R T$, we can also write

$$
X_{1}=\frac{P_{1}\left(\frac{V}{R T}\right)}{P_{\text {total }}\left(\frac{V}{R T}\right)}=\frac{P_{1}}{P_{\text {total }}}
$$

which can be rearranged to solve for $P_{1}$, the partial pressure of component 1 :

$$
P_{1}=X_{1} \cdot P_{\text {total }}
$$

This equation says that the partial pressure exerted by each component in a gas mixture is equal to the mole fraction of that component times the total pressure. In air, for example, the mole fractions of $\mathrm{N}_{2}, \mathrm{O}_{2}, \mathrm{Ar}$, and $\mathrm{CO}_{2}$ are $0.7808,0.2095,0.0093$, and 0.000 37, respectively (Table 9.1), and the total pressure of the air is the sum of the individual partial pressures:

$$
P_{\mathrm{air}}=P_{\mathrm{N}_{2}}+P_{\mathrm{O}_{2}}+P_{\mathrm{Ar}}+P_{\mathrm{CO}_{2}}+\ldots
$$

Thus, at a total air pressure of $1 \mathrm{~atm}(760 \mathrm{~mm} \mathrm{Hg})$, the partial pressures of the individual components are

$$
\begin{aligned}
& P_{\mathrm{N}_{2}}=0.7808 \mathrm{~atm} \mathrm{~N}_{2}=593.4 \mathrm{~mm} \mathrm{Hg} \\
& P_{\mathrm{O}_{2}}=0.2095 \mathrm{~atm} \mathrm{O} \mathrm{O}_{2}=159.2 \mathrm{~mm} \mathrm{Hg} \\
& P_{\mathrm{Ar}}=0.0093 \mathrm{~atm} \mathrm{Ar}=7.1 \mathrm{~mm} \mathrm{Hg} \\
& P_{\mathrm{CO}_{2}}=0.00037 \mathrm{~atm} \mathrm{CO} 2=0.3 \mathrm{~mm} \mathrm{Hg} \\
& P_{\text {air }}=1.0000 \mathrm{~atm} \text { air }=760.0 \mathrm{~mm} \mathrm{Hg}
\end{aligned}
$$

There are numerous practical applications of Dalton's law, ranging from the use of anesthetic agents in hospital operating rooms, where partial pressures of both oxygen and anesthetic in the patient's lungs must be constantly monitored, to the composition of diving gases used for underwater exploration. Worked Example 9.9 gives an illustration.

## Worked Example 9.9

At an underwater depth of 250 ft , the pressure is 8.38 atm . What should the mole percent of oxygen in the diving gas be for the partial pressure of oxygen in the gas to be 0.21 atm , the same as it is in air at 1.0 atm ?

## Strategy

The partial pressure of a gas in a mixture is equal to the mole fraction of the gas times the total pressure. Rearranging this equation lets us solve for mole fraction of $\mathrm{O}_{2}$.

## Solution

$$
\begin{aligned}
& \text { Since } P_{\mathrm{O}_{2}}=X_{\mathrm{O}_{2}} \cdot P_{\text {total }} \text { then } X_{\mathrm{O}_{2}}=\frac{P_{\mathrm{O}_{2}}}{P_{\text {total }}} \\
& X_{\mathrm{O}_{2}}=\frac{0.21 \mathrm{~atm}}{8.38 \mathrm{~atm}}=0.025 \\
& \text { Percent } \mathrm{O}_{2}=0.025 \times 100 \%=2.5 \% \mathrm{O}_{2}
\end{aligned}
$$

The diving gas should contain $2.5 \% \mathrm{O}_{2}$ for the partial pressure of $\mathrm{O}_{2}$ to be the same at 8.38 atm as it is in air at 1.0 atm .

PROBLEM 9.14 What is the mole fraction of each component in a mixture of 12.45 g of $\mathrm{H}_{2}, 60.67 \mathrm{~g}$ of $\mathrm{N}_{2}$, and 2.38 g of $\mathrm{NH}_{3}$ ?

- PROBLEM 9.15 What is the total pressure (in atmospheres) and what is the partial pressure of each component if the gas mixture in Problem 9.14 is in a 10.00 L steel container at $90^{\circ} \mathrm{C}$ ?
- PROBLEM 9.16 On a humid day in summer, the mole fraction of gaseous $\mathrm{H}_{2} \mathrm{O}$ (water vapor) in the air at $25^{\circ} \mathrm{C}$ can be as high as 0.0287 . Assuming a total pressure of 0.977 atm , what is the partial pressure (in atmospheres) of $\mathrm{H}_{2} \mathrm{O}$ in the air?
- KEY CONCEPT PROBLEM 9.17 What is the partial pressure of each gas—red, yellow, and green-if the total pressure inside the following container is 600 mm Hg ?



### 9.6 The Kinetic-Molecular Theory of Gases

Thus far, we've concentrated on describing the behavior of gases rather than on understanding the reasons for that behavior. Actually, the reasons are straightforward and were explained more than a century ago using a model called the kinetic-molecular theory. The kinetic-molecular theory is based on the following assumptions:

1. A gas consists of tiny particles, either atoms or molecules, moving about at random.
2. The volume of the particles themselves is negligible compared with the total volume of the gas; most of the volume of a gas is empty space.
3. The gas particles act independently of one another; there are no attractive or repulsive forces between particles.


A The partial pressure of oxygen in the scuba tanks must be the same underwater as in air at atmospheric pressure.


Kinetic Energies in a Gas movie

Kinetic-Molecular Theory of Gases activity

FIGURE 9.11 (a) Decreasing the volume of the gas at constant $n$ and $T$ increases the frequency of collisions with the container walls and therefore increases the pressure (Boyle's law). (b) Increasing the temperature (kinetic energy) at constant $n$ and $P$ increases the volume of the gas (Charles' law). (c) Increasing the amount of gas at constant $T$ and $P$ increases the volume (Avogadro's law). (d) Changing the identity of some gas molecules at constant $T$ and $V$ has no effect on the pressure (Dalton's law).
4. Collisions of the gas particles, either with other particles or with the walls of a container, are elastic; that is, the total kinetic energy of the gas particles is constant at constant $T$.
5. The average kinetic energy of the gas particles is proportional to the Kelvin temperature of the sample.
Beginning with these assumptions, it's possible not only to understand the behavior of gases but also to derive quantitatively the ideal gas law (though we'll not do so here). For example, let's look at how the individual gas laws follow from the five postulates of kinetic-molecular theory:

- Boyle's law $(P \propto 1 / V)$ : Gas pressure is a measure of the number and forcefulness of collisions between gas particles and the walls of their container. The smaller the volume at constant $n$ and $T$, the more crowded together the particles are and the greater the frequency of collisions. Thus, pressure increases as volume decreases (Figure 9.11a).
- Charles' law $(V \propto T)$ : Temperature is a measure of the average kinetic energy of the gas particles. The higher the temperature at constant $n$ and $P$, the faster the gas particles move and the more room they need to move around in to avoid increasing their collisions with the walls of the container. Thus, volume increases as temperature increases (Figure 9.11b).
- Avogadro's law $(V \propto n)$ : The more particles there are in a gas sample, the more volume the particles need at constant $P$ and $T$ to avoid increasing their collisions with the walls of the container. Thus, volume increases as amount increases (Figure 9.11c).
- Dalton's law $\left(P_{\text {total }}=P_{1}+P_{2}+\ldots\right)$ : The chemical identity of the particles in a gas is irrelevant. Total pressure of a fixed volume of gas depends only on the temperature $T$ and the total number of moles of gas $n$. The pressure exerted by a specific kind of particle thus depends on the mole fraction of that kind of particle in the mixture (Figure 9.11d).


One of the more important conclusions from kinetic-molecular theory comes from assumption 5-the relationship between temperature and $E_{\mathrm{K}}$, the kinetic energy of molecular motion. It can be shown that the total kinetic energy of a mole of gas particles equals $3 R T / 2$ and that the average kinetic energy per particle is thus $3 R T / 2 N_{\mathrm{A}}$, where $N_{\mathrm{A}}$ is Avogadro's number. Knowing this relationship makes it possible to calculate the average speed $u$ of a gas particle. To take a helium atom at room temperature ( 298 K ), for example, we can write

$$
E_{\mathrm{K}}=\frac{3 R T}{2 N_{\mathrm{A}}}=\frac{1}{2} m u^{2}
$$

which can be rearranged to give

$$
\begin{aligned}
u^{2} & =\frac{3 R T}{m N_{\mathrm{A}}} \\
\text { or } \quad u & =\sqrt{\frac{3 R T}{m N_{\mathrm{A}}}}=\sqrt{\frac{3 R T}{M}} \quad \text { where } M \text { is the molar mass }
\end{aligned}
$$

Substituting appropriate values for $R[8.314 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})]$ and for $M$, the molar mass of helium $\left(4.00 \times 10^{-3} \mathrm{~kg} / \mathrm{mol}\right)$, we have

$$
\begin{aligned}
u & =\sqrt{\frac{3 \times 8.314 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}} \times 298 \mathrm{~K}}{4.00 \times 10^{-3} \frac{\mathrm{~kg}}{\mathrm{~mol}}}}=\sqrt{1.86 \times 10^{6} \frac{\mathrm{~J}}{\mathrm{~kg}}} \\
& =\sqrt{1.86 \times 10^{6} \frac{\mathrm{~kg} \cdot \mathrm{~m}^{2}}{\mathrm{~s}^{2}}} \mathrm{~kg}
\end{aligned}=1.36 \times 10^{3} \mathrm{~m} / \mathrm{s} .
$$

Thus, the average speed of a helium atom at room temperature is more than $1.3 \mathrm{~km} / \mathrm{s}$, or about $3000 \mathrm{mi} / \mathrm{h}$ ! Average speeds of some other molecules at $25^{\circ} \mathrm{C}$ are given in Table 9.5. The heavier the molecule, the slower the average speed.

TABLE 9.5 $\quad$ Average Speeds ( $\mathrm{m} / \mathrm{s}$ ) of Some Molecules at $25^{\circ} \mathrm{C}$


Just because the average speed of helium atoms at 298 K is $1.36 \mathrm{~km} / \mathrm{s}$ doesn't mean that all helium atoms are moving at that speed or that a given atom will travel from Maine to California in one hour. As shown in Figure 9.12, there is a broad distribution of speeds among particles in a gas, a distribution that flattens out and moves higher as the temperature increases. Furthermore, an individual gas particle is likely to travel only a very short distance before it collides with another particle and bounces off in a different direction. Thus, the actual path followed by a gas particle is a random zigzag.

Reggie L. Hudson, "Toy Flying Saucers and Molecular Speeds," J. Chem. Educ. 59, 1982, 1025-1026.

FIGURE 9.12 The distribution of speeds for helium atoms at different temperatures.

Diffusion of Bromine Vapor movie

FIGURE 9.13 (a) Diffusion is the mixing of gas molecules by random motion under conditions where molecular collisions occur. (b) Effusion is the escape of a gas through a pinhole without molecular collisions.


For helium at room temperature and 1 atm pressure, the average distance between collisions (the mean free path) is only about $2 \times 10^{-7} \mathrm{~m}$, or 1000 atomic diameters, and there are approximately $10^{10}$ collisions per second. For a larger $\mathrm{O}_{2}$ molecule, the mean free path is about $6 \times 10^{-8} \mathrm{~m}$.

- PROBLEM 9.18 Calculate the average speed of a nitrogen molecule (in meters per second) on a hot day in summer $\left(T=37^{\circ} \mathrm{C}\right)$ and on a cold day in winter ( $T=-25^{\circ} \mathrm{C}$ ).
- PROBLEM 9.19 At what temperature does the average speed of an oxygen molecule equal that of an airplane moving at 580 mph ?


### 9.7 Graham's Law: Diffusion and Effusion of Gases

The constant motion and high velocities of gas particles lead to some important practical consequences. One such consequence is that gases mix rapidly when they come in contact. Take the stopper off a bottle of perfume, for instance, and the odor will spread rapidly through the room as perfume molecules mix with the molecules in the air. This mixing of different gases by random molecular motion with frequent collisions is called diffusion. A similar process in which gas molecules escape without collisions through a tiny hole into a vacuum is called effusion (Figure 9.13).

(a)

(b)

According to Graham's law, formulated in the mid-1800s by the Scottish chemist Thomas Graham (1805-1869), the rate of effusion of a gas is inversely proportional to the square root of its mass. In other words, the lighter the molecule, the more rapidly it effuses.

Graham's law The rate of effusion of a gas is inversely proportional to the square root of its mass, $m$.

$$
\text { Rate } \propto \frac{1}{\sqrt{m}}
$$

In comparing two gases at the same temperature and pressure, we can set up an equation showing that the ratio of the effusion rates of the two gases is inversely proportional to the ratio of the square roots of their masses:

$$
\frac{\text { Rate }_{1}}{\text { Rate }_{2}}=\frac{\sqrt{m_{2}}}{\sqrt{m_{1}}}=\sqrt{\frac{m_{2}}{m_{1}}}
$$

The inverse relationship between the rate of effusion and the square root of the mass follows directly from the connection between temperature and kinetic energy described in the previous section. Because temperature is a measure of average kinetic energy and is independent of the gas's chemical identity, different gases at the same temperature have the same average kinetic energy:

$$
\begin{aligned}
\text { Since } & \frac{1}{2} m u^{2} & =\frac{3 R T}{2 N_{\mathrm{A}}} \text { for any gas } \\
\text { then } & \left(\frac{1}{2} m u^{2}\right)_{\text {gas } 1} & =\left(\frac{1}{2} m u^{2}\right)_{\text {gas } 2} \text { at the same } T
\end{aligned}
$$

Canceling the factor of $1 / 2$ from both sides and rearranging, we find that the average speeds of the molecules in two gases vary as the inverse ratio of the square roots of their masses:

$$
\begin{array}{llrl} 
& \text { Since } & \left(\frac{1}{2} m u^{2}\right)_{\text {gas } 1} & =\left(\frac{1}{2} m u^{2}\right)_{\text {gas } 2} \\
\text { then } & \left(m u^{2}\right)_{\text {gas } 1} & =\left(m u^{2}\right)_{\text {gas } 2} \text { and } \frac{\left(u_{\text {gas } 1}\right)^{2}}{\left(u_{\text {gas } 2}\right)^{2}}=\frac{m_{2}}{m_{1}} \\
\text { so } & \frac{u_{\text {gas } 1}}{u_{\text {gas } 2}} & =\frac{\sqrt{m_{2}}}{\sqrt{m_{1}}}=\sqrt{\frac{m_{2}}{m_{1}}}
\end{array}
$$

If, as seems reasonable, the rate of effusion of a gas is proportional to the average speed of the gas molecules, then Graham's law results.

One of the most important practical consequences of Graham's law is that mixtures of gases can be separated into their pure components by taking advantage of the different rates of diffusion of the components. (Diffusion is more complex than effusion because of the molecular collisions that occur, but Graham's law usually works as a good approximation.) For example, naturally occurring uranium is a mixture of isotopes, primarily ${ }^{235} \mathrm{U}(0.72 \%)$ and ${ }^{238} \mathrm{U}(99.28 \%)$. In uranium enrichment plants that purify the fissionable uranium- 235 used for fuel in nuclear reactors, elemental uranium is converted into volatile uranium hexafluoride, $\mathrm{bp} 56^{\circ} \mathrm{C}$, and $\mathrm{UF}_{6}$ gas is allowed to diffuse from one chamber to another through a permeable membrane. The ${ }^{235} \mathrm{UF}_{6}$ and ${ }^{238} \mathrm{UF}_{6}$ molecules diffuse through the membrane at slightly different rates according to the square root of the ratio of their masses:

$$
\begin{aligned}
& \text { For }{ }^{235} \mathrm{UF}_{6}, m=349.03 \mathrm{amu} \\
& \text { For }{ }^{238} \mathrm{UF}_{6}, m=352.04 \mathrm{amu} \\
& \text { so } \frac{\text { Rate of }{ }^{235} \mathrm{UF}_{6} \text { diffusion }}{\text { Rate of }{ }^{238} \mathrm{UF}_{6} \text { diffusion }}=\sqrt{\frac{352.04 \mathrm{amu}}{349.03 \mathrm{amu}}}=1.0043
\end{aligned}
$$

Bassam Z. Shakhashiri, "Ratio of Diffusion Coefficients: The Ammonium Chloride Ring," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983) pp. 59-62. Ammonia vapor and hydrogen chloride gas are simultaneously introduced into opposite ends of dry glass tubing. A white ring of solid ammonium chloride forms inside the tube closer to the end at which the hydrogen chloride was introduced, showing an inverse relationship between the rate of diffusion and the molar mass of each reactant. No distinction is made between diffusion and effusion, and Graham's law is erroneously used in explaining the data.


Lee R. Summerlin, and James L. Ealy, Jr., "Diffusion of Gases," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), pp. 14-15.

Ammonia and hydrogen chloride diffusion rates are determined.

Dianne N. Epp, "Overhead Projection of Graham's Law of Gaseous Diffusion," J. Chem. Educ. 67, 1990, 1061.

B Bassam Z. Shakhashiri, "Relative Velocity of Sound Propagation: Musical Molecular Weights," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp. 88-89.


A The uranium- 235 used as a fuel in nuclear reactors is obtained by gas diffusion of $\mathrm{UF}_{6}$ in these cylinders.

0Students sometimes think that some substances are ideal gases while other substances are nonideal. All gases are ideal under certain conditions and nonideal under others.

The $\mathrm{UF}_{6}$ gas that passes through the membrane is thus very slightly enriched in the lighter, faster-moving isotope. After repeating the process many thousands of times, a separation of isotopes can be achieved. Approximately $85 \%$ of the Western world's nuclear fuel supply—some 5000 tons per year-is produced by this gas diffusion method.

## Worked Example 9.10

Assume that you have a sample of hydrogen gas containing $\mathrm{H}_{2}, \mathrm{HD}$, and $\mathrm{D}_{2}$ that you want to separate into pure components ( $\mathrm{H}={ }^{1} \mathrm{H}$ and $\mathrm{D}={ }^{2} \mathrm{H}$ ). What are the relative rates of diffusion of the three molecules according to Graham's law?

## Strategy

First, find the masses of the three molecules: for $\mathrm{H}_{2}, m=2.0 \mathrm{amu}$; for HD , $m=3.0 \mathrm{amu}$; for $\mathrm{D}_{2}, m=4.0 \mathrm{amu}$. Then apply Graham's law to different pairs of gas molecules.

## Solution

Since $D_{2}$ is the heaviest of the three molecules, it will diffuse most slowly, and we'll call its relative rate 1.00. We can then compare HD and $\mathrm{H}_{2}$ with $\mathrm{D}_{2}$ :

Comparing HD with $\mathrm{D}_{2}$, we have

$$
\frac{\text { Rate of HD diffusion }}{\text { Rate of } \mathrm{D}_{2} \text { diffusion }}=\sqrt{\frac{\text { Mass of } \mathrm{D}_{2}}{\text { Mass of } \mathrm{HD}}}=\sqrt{\frac{4.0 \mathrm{amu}}{3.0 \mathrm{amu}}}=1.15
$$

Comparing $\mathrm{H}_{2}$ with $\mathrm{D}_{2}$, we have

$$
\frac{\text { Rate of } \mathrm{H}_{2} \text { diffusion }}{\text { Rate of } \mathrm{D}_{2} \text { diffusion }}=\sqrt{\frac{\text { Mass of } \mathrm{D}_{2}}{\text { Mass of } \mathrm{H}_{2}}}=\sqrt{\frac{4.0 \mathrm{amu}}{2.0 \mathrm{amu}}}=1.41
$$

Thus, the relative rates of diffusion are $\mathrm{H}_{2}(1.41)>\mathrm{HD}(1.15)>\mathrm{D}_{2}(1.00)$.

- PROBLEM 9.20 Which gas in each of the following pairs diffuses more rapidly, and what are the relative rates of diffusion?
(a) Kr and $\mathrm{O}_{2}$
(b) $\mathrm{N}_{2}$ and acetylene $\left(\mathrm{C}_{2} \mathrm{H}_{2}\right)$
- PROBLEM 9.21 What are the relative rates of diffusion of the three naturally occurring isotopes of neon, ${ }^{20} \mathrm{Ne},{ }^{21} \mathrm{Ne}$, and ${ }^{22} \mathrm{Ne}$ ?


### 9.8 The Behavior of Real Gases

Before ending this discussion of gases, it's worthwhile expanding on a point made earlier: The behavior of a real gas is often a bit different from that of an ideal gas. For instance, kinetic-molecular theory assumes that the volume of the gas particles themselves is negligible compared with the total gas volume. The assumption is valid at STP, where the volume taken up by molecules of a typical gas is only about $0.05 \%$ of the total volume, but the assumption is not valid at 500 atm and $0^{\circ} \mathrm{C}$, where the volume of the molecules is about $20 \%$ of the total volume (Figure 9.14). As a result, the volume of a real gas at high pressure is larger than predicted by the ideal gas law.

A second problem with real gases is the assumption that there are no attractive forces between particles. At lower pressures, this assumption is a good one because the gas particles are so far apart. At higher pressures, however, the particles

(a)

(b)

FIGURE 9.14 The volume taken up by the gas particles themselves is less important at lower pressure (a) than at higher pressure (b). As a result, the volume of a real gas at high pressure is somewhat larger than the ideal value.
are much closer together and the attractive forces between them become more important. In general, intermolecular attractions become significant at a distance of about 10 molecular diameters and increase rapidly as the distance diminishes (Figure 9.15). The result is to draw the molecules together slightly, decreasing the volume at a given pressure (or decreasing the pressure for a given volume).

© FIGURE 9.15 Molecules attract one another at distances up to about 10 molecular diameters. The result is a decrease in the actual volume of most real gases when compared with ideal gases at pressures up to 300 atm .

Note that the effect of molecular volume (to increase $V$ ) is opposite that of intermolecular attractions (to decrease $V$ ). The two factors therefore tend to cancel at intermediate pressures, but the effect of molecular volume dominates above about 350 atm .

Both problems can be dealt with mathematically by a modification of the ideal gas law called the van der Waals equation, which uses two correction factors, $a$ and $b$. The increase in $V$ caused by the effect of molecular volume is corrected by subtracting an amount $n b$ from the observed volume. For reasons we won't go into, the decrease in $V$ (or, equivalently, the decrease in $P$ ) caused by the effect of intermolecular attractions is best corrected by adding an amount $a n^{2} / V^{2}$ to the pressure.


PROBLEM 9.22 Assume that you have 0.500 mol of $\mathrm{N}_{2}$ in a volume of 0.600 L at 300 K . Calculate the pressure in atmospheres using both the ideal gas law and the van der Waals equation. For $\mathrm{N}_{2}, a=1.35\left(\mathrm{~L}^{2} \cdot \mathrm{~atm}\right) / \mathrm{mol}^{2}$, and $b=0.0387 \mathrm{~L} / \mathrm{mol}$.

### 9.9 The Earth's Atmosphere

The mantle of gases surrounding the earth is far from the uniform mixture you might expect. Although atmospheric pressure decreases in a regular way at higher altitudes (Figure 9.16a), the profile of temperature versus altitude is much more complex (Figure 9.16b). Four regions of the atmosphere have been defined based on this temperature curve. The temperature in the troposphere, the region nearest



A FIGURE 9.16 Variations of (a) atmospheric pressure and (b) average temperature with altitude. Four regions of the earth's atmosphere are defined based on the temperature variations.


- The photochemical smog over many cities is the end result of pollution from automobile exhausts.
the earth's surface, decreases regularly up to about 12 km altitude, where it reaches a minimum value, and then increases in the stratosphere, up to about 50 km . Above the stratosphere, in the mesosphere, ( $50-85 \mathrm{~km}$ ), the temperature again decreases but then again increases in the thermosphere. To give you a feeling for these altitudes, passenger jets normally fly near the top of the troposphere at altitudes of 10 to 12 km , and the world altitude record for aircraft is 37.65 km roughly in the middle of the stratosphere.


## Chemistry of the Troposphere

Not surprisingly, it's the layer nearest the earth's surface-the troposphere-that is the most easily disturbed by human activities and has the greatest effect on the earth's surface conditions. Among those effects, air pollution, acid rain, and the greenhouse effect are particularly important.

The earth and its atmosphere as seen from space.


Air Pollution Air pollution has appeared in the last two centuries as an unwanted by-product of our industrialized societies. Its causes are relatively straightforward; its control is difficult. The main causes of air pollution are the release of unburned hydrocarbon molecules and the production of nitric oxide, NO , during combustion of petroleum products in older industrial plants and the more than 500 million automobile engines presently in use worldwide. The NO is further oxidized by reaction with air to yield nitrogen dioxide, $\mathrm{NO}_{2}$, which splits into NO plus free oxygen atoms in the presence of sunlight (symbolized by $h \nu$ ). Reaction of the oxygen atoms with $\mathrm{O}_{2}$ molecules then yields ozone, $\mathrm{O}_{3}$, a highly reactive substance that can further combine with unburned hydrocarbons in the air. The end
result is the production of so-called photochemical smog, the hazy, brownish layer lying over many cities.

$$
\begin{aligned}
\mathrm{NO}_{2}(g)+h \nu & \longrightarrow \mathrm{NO}(g)+\mathrm{O}(g) \\
\mathrm{O}(g)+\mathrm{O}_{2}(g) & \longrightarrow \mathrm{O}_{3}(g)
\end{aligned}
$$

Acid Rain Acid rain, a second major environmental problem, results primarily from the production of sulfur dioxide, $\mathrm{SO}_{2}$, that accompanies the burning of sulfur-containing coal in power-generating plants. Sulfur dioxide is slowly converted to $\mathrm{SO}_{3}$ by reaction with oxygen in air, and $\mathrm{SO}_{3}$ dissolves in rainwater to yield dilute sulfuric acid, $\mathrm{H}_{2} \mathrm{SO}_{4}$.

$$
\begin{aligned}
\mathrm{S}(\text { in coal })+\mathrm{O}_{2}(\mathrm{~g}) & \longrightarrow \mathrm{SO}_{2}(g) \\
2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) & \longrightarrow 2 \mathrm{SO}_{3}(g) \\
\mathrm{SO}_{3}(g)+\mathrm{H}_{2} \mathrm{O}(l) & \longrightarrow \mathrm{H}_{2} \mathrm{SO}_{4}(a q)
\end{aligned}
$$

Among the many dramatic effects of acid rain are the extinction of fish from acidic lakes throughout parts of the northeastern United States, Canada, and Scandinavia, the damage to forests throughout much of central and eastern Europe, and the deterioration everywhere of marble buildings and statuary. Marble is a form of calcium carbonate, $\mathrm{CaCO}_{3}$, and, like all metal carbonates, reacts with acid to produce $\mathrm{CO}_{2}$. The result is a slow eating away of the stone.

$$
\mathrm{CaCO}_{3}(s)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \longrightarrow \mathrm{CaSO}_{4}(a q)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CO}_{2}(g)
$$

Greenhouse Effect The third major atmospheric problem, the so-called greenhouse effect and the global warming that could result, is less well documented and not as well understood as either air pollution or acid rain. The basis of concern about the greenhouse problem is the fear that human activities over the past century have disturbed the earth's delicate thermal balance. One component of that balance is the radiant energy the earth's surface receives from the sun, a certain amount of which is radiated back into space as infrared energy. Although much of this radiation passes out through the atmosphere, some is absorbed by atmospheric gases, particularly water vapor, carbon dioxide, and methane. This absorbed radiation warms the atmosphere and acts to maintain a relatively stable temperature at the earth's surface. Should increasing amounts of radiation be absorbed, increased atmospheric heating could result and global temperatures could rise.

Careful measurements show that concentrations of atmospheric carbon dioxide have been rising in the last 150 years, largely because of the increased use of fossil fuels, from an estimated 290 parts per million (ppm) in 1850 to a current level of 370 ppm (Figure 9.17). Thus, there is concern among many atmospheric


## FIGURE 9.17

Concentrations of atmospheric $\mathrm{CO}_{2}$ have increased dramatically in the last 150 years as a result of increased fossil fuel use. Atmospheric scientists worry that global atmospheric warming may occur as a result.


A The details on this marble statue have been eaten away over the years by acid rain.


Carbon Dioxide Behaves as an Acid in Water movie
scientists that increased absorption of infrared radiation and widespread global warming might follow. The worries stem from the predictions of sophisticated computer models, which predict a potential warming of as much as $3^{\circ} \mathrm{C}$ by the year 2050, an amount that would result in an increased melting of polar ice caps and a resultant rise in ocean levels.

## Chemistry of the Upper Atmosphere

Relatively little of the atmosphere's mass is located above the troposphere, but the chemistry that occurs there is nonetheless crucial to maintaining life on earth. Particularly important is what takes place in the ozone layer, an atmospheric band stretching from about $20-40 \mathrm{~km}$ above the earth's surface. Ozone $\left(\mathrm{O}_{3}\right)$ is a severe pollutant at low altitudes but is critically important in the upper atmosphere because it absorbs intense ultraviolet radiation from the sun. Even though it is present in very small amounts in the stratosphere, ozone acts as a shield to prevent high-energy solar radiation from reaching the earth's surface, where it can cause such problems as eye cataracts and skin cancer.

Around 1976, a disturbing decrease in the amount of ozone present over the South Pole began showing up (Figure 9.18), and more recently a similar phenomenon has been found over the North Pole. Ozone levels drop to below $50 \%$ of normal in the polar spring before returning to near normal in the autumn.

FIGURE 9.18 A falsecolor satellite image of the ozone hole over Antarctica on September 26, 2002. The lowest ozone concentrations are represented by the black and violet regions, where ozone levels are up to $50 \%$ lower than normal.

The principal cause of ozone depletion is the presence in the stratosphere of chlorofluorocarbons ( CFCs ), such as $\mathrm{CF}_{2} \mathrm{Cl}_{2}$ and $\mathrm{CFCl}_{3}$. Because they are inexpensive and stable, yet not toxic, flammable, or corrosive, CFCs are ideal as propellants in aerosol cans, as refrigerants, as solvents, and as fire-extinguishing agents. In addition, they are used for blowing bubbles into foamed plastic insulation. Unfortunately, the stability that makes CFCs so useful also causes them to persist in the environment. Molecules released at ground level slowly find their way into the stratosphere, where they undergo a complex series of reactions that ultimately result in ozone destruction.

There are several different mechanisms of ozone destruction that predominate under different stratospheric conditions. All are multistep processes that begin when ultraviolet light ( $h \nu$ ) strikes a CFC molecule, breaking a carbon-chlorine bond and generating a chlorine atom:

$$
\mathrm{CFCl}_{3}+h \nu \longrightarrow \mathrm{CFCl}_{2}+\mathrm{Cl}
$$

The resultant chlorine atom reacts with ozone to yield $\mathrm{O}_{2}$ and ClO , and two ClO molecules then give $\mathrm{Cl}_{2} \mathrm{O}_{2}$. Further reaction occurs when $\mathrm{Cl}_{2} \mathrm{O}_{2}$ is struck by more ultraviolet light to generate $\mathrm{O}_{2}$ and two more chlorine atoms.

$$
\begin{array}{ll}
\text { (1) } & 2\left[\mathrm{Cl}+\mathrm{O}_{3} \longrightarrow \mathrm{O}_{2}+\mathrm{ClO}\right] \\
\text { (2) } & 2 \mathrm{ClO} \longrightarrow \mathrm{Cl}_{2} \mathrm{O}_{2} \\
\text { (3) } & \mathrm{Cl}_{2} \mathrm{O}_{2}+h \nu \longrightarrow 2 \mathrm{Cl}+\mathrm{O}_{2} \\
\text { Net: } & 2 \mathrm{O}_{3}+h \nu \longrightarrow 3 \mathrm{O}_{2}
\end{array}
$$

Look at the overall result of the above reaction sequence. Chlorine atoms are used up in the first step but are regenerated in the third step, so they don't appear in the net equation. Thus, the net sequence is a never-ending chain reaction, in which the generation of just a few chlorine atoms from a few CFC molecules leads to the destruction of a great many ozone molecules.

Recognition of the problem led the U.S. government in 1980 to ban the use of CFCs for aerosol propellants and, more recently, for refrigerants. Worldwide action to reduce CFC use began in September 1987, and an international ban on the industrial production and release of CFCs took effect in 1996. The ban has not been wholly successful, however, because of a substantial black market that has developed, particularly in Russia and China where up to $\$ 300$ million per year of illegal CFCs are manufactured. Even with these stringent efforts, amounts of CFCs in the stratosphere will continue to rise through the early 2000s and will not return to acceptable levels until the middle of the century.

- PROBLEM 9.23 The ozone layer is about 20 km thick, has an average total pressure of $10 \mathrm{~mm} \mathrm{Hg}\left(1.3 \times 10^{-2} \mathrm{~atm}\right)$, and has an average temperature of 230 K . The partial pressure of ozone in the layer is only about $1.2 \times 10^{-6} \mathrm{~mm} \mathrm{Hg}$ $\left(1.6 \times 10^{-9} \mathrm{~atm}\right)$. How many meters thick would the layer be if all the ozone contained in it were compressed into a thin layer of pure $\mathrm{O}_{3}$ at STP?


## Interlude <br> Inhaled Anesthetics

William Morton's demonstration in 1846 of ether-induced anesthesia during dental surgery ranks as one of the most important medical breakthroughs of all time. Before that date, all surgery had been carried out with the patient conscious. Use of chloroform as an anesthetic quickly followed Morton's work, made popular by Queen Victoria of England, who in 1853 gave birth to a child while anesthetized by chloroform.

Literally hundreds of substances in addition to ether and chloroform have subsequently been shown to act as inhaled anesthetics. Halothane, enflurane, isoflurane, and methoxyflurane are at present the most commonly used agents in hospital operating rooms. All four are potent at relatively low doses, are nontoxic, and are nonflammable, an important safety feature.



Halothane



Isoflurane





Methoxyflurane

Despite their importance, surprisingly little is known about how inhaled anesthetics work in the body. Even the definition of anesthesia as a behavioral state is imprecise, and the nature of the changes in brain function leading to anesthesia are unknown. Remarkably, the potency of different inhaled anesthetics correlates well with their solubility in olive oil: the more soluble in olive oil, the more potent as an anesthetic. This unusual observation has led many scientists to believe that anesthetics act by dissolving in the fatty membranes surrounding nerve cells. The resultant changes in the fluidity and shape of the membranes apparently decrease the ability of sodium ions to pass into the nerve cells, thereby blocking the firing of nerve impulses.

Depth of anesthesia is determined by the concentration of anesthetic agent that reaches the brain. Brain concentration, in turn, depends on the solubility and transport of the anesthetic agent in the bloodstream and on its partial pressure in inhaled air. Anesthetic potency is usually expressed as a minimum alveolar concentration (MAC), defined as the percent concentration of anesthetic in inhaled air that results in anesthesia in $50 \%$ of patients. As shown in Table 9.6, nitrous oxide, $\mathrm{N}_{2} \mathrm{O}$, is the least potent of the common anesthetics. Fewer than $50 \%$ of patients are immobilized by breathing an 80:20 mix of nitrous oxide and oxygen. Methoxyflurane is the most potent agent; a partial pressure of only 1.2 mm Hg is sufficient to anesthetize $50 \%$ of patients, and a partial pressure of 1.4 mm Hg will anesthetize $95 \%$.

| TABLE 9.6 | Relative Potency of Inhaled Anesthetics |  |
| :--- | :---: | :---: |
| Anesthetic | MAC (\%) | MAC <br> (partial pressure, mm Hg) |
| Nitrous oxide | - | $>760$ |
| Enflurane | 1.7 | 13 |
| Isoflurane | 1.4 | 11 |
| Halothane | 0.75 | 5.7 |
| Methoxyflurane | 0.16 | 1.2 |

PROBLEM 9.24 For ether, a partial pressure of 15 mm Hg results in anesthesia in $50 \%$ of patients. What is the MAC for ether?

PROBLEM 9.25 Chloroform has an MAC of 0.77\%.
(a) What partial pressure of chloroform is required to anesthetize $50 \%$ of patients?
(b) What mass of chloroform in 10.0 L of air at STP will produce the appropriate MAC?

## Summary

A gas is a collection of atoms or molecules moving independently through a volume that is largely empty space. Collisions of the randomly moving particles with the walls of their container exert a force per unit area that we perceive as pressure. The SI unit for pressure is the pascal, but the atmosphere and the millimeter of mercury are more commonly used. The physical condition of any gas is defined by four variables: pressure ( $P$ ), temperature ( $T$ ), volume ( $V$ ), and molar amount ( $n$ ). The specific relationships among these variable are called the gas laws:

| Boyle's law: | The volume of a gas varies <br> inversely with its pressure. <br> That is, $V \propto 1 / P$ or $P V=k$ at |
| :--- | :--- |
| constant $n, T$. |  |

The three individual gas laws can be combined into a single ideal gas law, $P V=n R T$. If any three of the four variables $P, V, T$ and $n$ are known, the fourth can be calculated. The constant $R$ in the equation is called the gas constant and has the same value for all gases. At standard temperature and pressure (STP; 1 atm and $0^{\circ} \mathrm{C}$ ), the standard molar volume of an ideal gas is 22.414 L .

The gas laws apply to mixtures of gases as well as to pure gases. According to Dalton's law of partial pressures, the total pressure exerted by a mixture of gases in a container is equal to the sum of the pressures each individual gas would exert alone.

The behavior of gases can be accounted for using a model called the kinetic-molecular theory, a group of five postulates:

1. A gas consists of tiny particles moving at random.
2. The volume of the gas particles is negligible compared with the total volume.
3. There are no forces between particles, either attractive or repulsive.
4. Collisions of gas particles are elastic.
5. The average kinetic energy of gas particles is proportional to their absolute temperature.

The connection between temperature and kinetic energy obtained from the kinetic-molecular theory makes it possible to calculate the average speed of a gas particle at any temperature. An important practical consequence of this relationship is Graham's law, which states that the rate of a gas's effusion, or spontaneous passage through a pinhole in a membrane, depends inversely on the square root of the gas's mass.

Real gases differ in their behavior from that predicted by the ideal gas law, particularly at high pressure, where gas particles are forced close together and intermolecular attractions become significant.

## Key Words

atmosphere (atm) 343
Avogadro's law 348
Boyle's law 346
Charles' law 348
Dalton's law of partial
pressures 355
diffusion 360
effusion 360
gas constant (R) 350
gas laws 346
Graham's law 360
ideal gas 346
ideal gas law 350
kinetic-molecular theory 357
manometer 344

## millimeter of mercury

 (mm Hg) 343mole fraction (X) 356
newton (N) 343
pascal (Pa) 343
pressure (P) 343
standard molar volume 349

## standard temperature and pressure (STP) 351 <br> van der Waals equation 363

## Key Concept Summary



## Understanding Key Concepts

Problems 9.1-9.25 appear within the chapter.
9.26 Assume that you have a sample of gas in a cylinder with a movable piston, as shown in the following drawing:


Redraw the apparatus to show what the sample will look like after (a) the temperature is increased from 300 K to 450 K at constant pressure, (b) the pressure is increased from 1 atm to 2 atm at constant temperature, and (c) the temperature is decreased from 300 K to 200 K and the pressure is decreased from 3 atm to 2 atm .
9.27 Assume that you have a sample of gas at 350 K in a sealed container, as represented in (a). Which of the drawings (b)-(d) represents the gas after the temperature is lowered from 350 K to 150 K ?

(a)

(b)

(c)

(d)
9.28 Assume that you have a mixture of He (atomic mass $=4 \mathrm{amu}$ ) and Xe (atomic mass $=131 \mathrm{amu}$ ) at 300 K . Which of the drawings best represents the mixture (blue $=\mathrm{He}$; green $=\mathrm{Xe}$ )?

9.29 Three bulbs, two of which contain different gases and one of which is empty, are connected as shown in the following drawing:


Redraw the apparatus to represent the gases after the stopcocks are opened and the system is allowed to come to equilibrium.
9.30 The apparatus shown is called a closed-end manometer because the arm not connected to the gas sample is closed to the atmosphere and is under vacuum. Explain how you can read the gas pressure in the bulb.

9.31 Redraw the following open-end manometer to show what it would look like when stopcock $A$ is opened.

9.32 Effusion of a 1:1 mixture of two gases through a small pinhole produces the results shown below.
(a) Which gas molecules-yellow or blue-have a higher average speed?
(b) If the yellow molecules have a molecular mass of 25 amu , what is the molecular mass of the blue molecules?

9.33 A glass tube has one end in a dish of mercury and the other end closed by a stopcock. The distance from the surface of the mercury to the bottom of the stopcock is 800 mm . The apparatus is at $25^{\circ} \mathrm{C}$, and the mercury level in the tube is the same as that in the dish.

(a) Show on drawing (1) what the approximate level of mercury in the tube will be when the temperature of the entire apparatus is lowered from $+25^{\circ} \mathrm{C}$ to $-25^{\circ} \mathrm{C}$.
(b) Show on drawing (2) what the approximate level of mercury in the tube will be when a vacuum pump is connected to the top of the tube, the stopcock is opened, the tube is evacuated, the stopcock is closed, and the pump is removed.
(c) Show on drawing (3) what the approximate level of mercury in the tube will be when the stopcock in drawing (2) is opened.

## Additional Problems

## Gases and Gas Pressure

9.34 What is temperature a measure of?
9.35 Why are gases so much more compressible than solids or liquids?
9.36 Atmospheric pressure at the top of Pikes Peak in Colorado is approximately 480 mm Hg . Convert this value to atmospheres and to pascals.
9.37 Carry out the following conversions:
(a) 352 torr to kPa
(b) 0.255 atm to mm Hg
(c) 0.0382 mm Hg to Pa
9.38 What is the pressure (in millimeters of mercury) inside a container of gas connected to a mercury-filled open-end manometer of the sort shown in Figure 9.4 when the level in the arm connected to the container is 17.6 cm
lower than the level in the arm open to the atmosphere, and the atmospheric pressure reading outside the apparatus is 754.3 mm Hg ?
9.39 What is the pressure (in atmospheres) inside a container of gas connected to a mercury-filled open-end manometer when the level in the arm connected to the container is 28.3 cm higher than the level in the arm open to the atmosphere, and the atmospheric pressure reading outside the apparatus is 1.021 atm ?
9.40 Assume that you have an open-end manometer filled with ethyl alcohol (density $=0.7893 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$ ) rather than mercury (density $=13.546 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$ ). What is the pressure (in pascals) if the level in the arm open to the atmosphere is 55.1 cm higher than the level in the arm connected to the gas sample and the atmospheric pressure reading is 752.3 mm Hg ?
9.41 Assume that you have an open-end manometer filled with chloroform (density $=1.4832 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$ ) rather than mercury (density $=13.546 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$ ). What is the difference in height between the liquid in the two arms if the pressure in the arm connected to the gas sample is 0.788 atm and the atmospheric pressure reading is 0.849 atm ? In which arm is the chloroform level higher?
9.42 Calculate the average molecular mass of air from the data given in Table 9.1.
9.43 What is the average molecular mass of a diving-gas mixture that contains $2.0 \%$ by volume $\mathrm{O}_{2}$ and $98.0 \%$ by volume He ?

## The Gas Laws

9.44 Assume that you have a cylinder with a movable piston. What would happen to the gas pressure inside the cylinder if you were to do the following?
(a) Triple the Kelvin temperature while holding the volume constant
(b) Reduce the amount of gas by $1 / 3$ while holding the temperature and volume constant
(c) Decrease the volume by $45 \%$ at constant $T$
(d) Halve the Kelvin temperature, and triple the volume
9.45 Assume that you have a cylinder with a movable piston. What would happen to the gas volume of the cylinder if you were to do the following?
(a) Halve the Kelvin temperature while holding the pressure constant
(b) Increase the amount of gas by $1 / 4$ while holding the temperature and pressure constant
(c) Decrease the pressure by $75 \%$ at constant $T$
(d) Double the Kelvin temperature, and double the pressure
9.46 Which sample contains the most molecules: 1.00 L of $\mathrm{O}_{2}$ at STP, 1.00 L of air at STP, or $1.00 \mathrm{~L} \mathrm{of}_{2}$ at STP?
9.47 Which sample contains more molecules: 2.50 L of air at $50^{\circ} \mathrm{C}$ and 750 mm Hg pressure or 2.16 L of $\mathrm{CO}_{2}$ at $-10^{\circ} \mathrm{C}$ and 765 mm Hg pressure?
9.48 Oxygen gas is commonly sold in 49.0 L steel containers at a pressure of 150 atm . What volume (in liters) would the gas occupy at a pressure of 1.02 atm if its temperature remained unchanged? If its temperature was raised from $20.0^{\circ} \mathrm{C}$ to $35.0^{\circ} \mathrm{C}$ at constant $P=150 \mathrm{~atm}$ ?
9.49 A compressed air tank carried by scuba divers has a volume of 8.0 L and a pressure of 140 atm at $20^{\circ} \mathrm{C}$. What is the volume of air in the tank (in liters) at STP?
9.50 If 15.0 g of $\mathrm{CO}_{2}$ gas has a volume of 0.30 L at 300 K , what is its pressure in millimeters of mercury?
9.51 If 20.0 g of $\mathrm{N}_{2}$ gas has a volume of 0.40 L and a pressure of 6.0 atm , what is its Kelvin temperature?
9.52 The matter in interstellar space consists almost entirely of hydrogen atoms at a temperature of 100 K and a density of approximately 1 atom $/ \mathrm{cm}^{3}$. What is the gas pressure in millimeters of mercury?
9.53 Methane gas, $\mathrm{CH}_{4}$, is sold in a 43.8 L cylinder containing 5.54 kg . What is the pressure inside the cylinder (in kilopascals) at $20^{\circ} \mathrm{C}$ ?
9.54 Many laboratory gases are sold in steel cylinders with a volume of 43.8 L . What mass (in grams) of argon is inside a cylinder whose pressure is $17,180 \mathrm{kPa}$ at $20^{\circ} \mathrm{C}$ ?
9.55 A small cylinder of helium gas used for filling balloons has a volume of 2.30 L and a pressure of $13,800 \mathrm{kPa}$ at $25^{\circ} \mathrm{C}$. How many balloons can you fill if each one has a volume of 1.5 L and a pressure of 1.25 atm at $25^{\circ} \mathrm{C}$ ?

## Gas Stoichiometry

9.56 Which sample contains more molecules, 15.0 L of steam (gaseous $\mathrm{H}_{2} \mathrm{O}$ ) at $123.0^{\circ} \mathrm{C}$ and 0.93 atm pressure or a 10.5 g ice cube at $-5.0^{\circ} \mathrm{C}$ ?
9.57 Which sample contains more molecules, 3.14 L of Ar at $85.0^{\circ} \mathrm{C}$ and 1111 mm Hg pressure or $11.07 \mathrm{~g} \mathrm{of} \mathrm{Cl}_{2}$ ?
9.58 Imagine that you have two identical flasks, one containing hydrogen at STP and the other containing oxygen at STP. How can you tell which is which without opening them?
9.59 Imagine that you have two identical flasks, one containing chlorine gas and the other containing argon. How can you tell which is which without opening them?
9.60 What is the total mass (in grams) of oxygen in a room measuring 4.0 m by 5.0 m by 2.5 m ? Assume that the gas is at STP and that air contains $20.95 \%$ oxygen by volume.
9.61 The average oxygen content of arterial blood is approximately 0.25 g of $\mathrm{O}_{2}$ per liter. Assuming a body temperature of $37^{\circ} \mathrm{C}$, how many moles of oxygen are transported by each liter of arterial blood? How many milliliters?
9.62 One mole of any gas has a volume of 22.414 L at STP. What are the densities of the following gases (in grams per liter) at STP?
(a) $\mathrm{CH}_{4}$
(b) $\mathrm{CO}_{2}$
(c) $\mathrm{O}_{2}$
(d) $\mathrm{UF}_{6}$
9.63 What is the density (in grams per liter) of a gas mixture that contains $27.0 \% \mathrm{~F}_{2}$ and $73.0 \%$ He by volume at 714 mm Hg and $27.5^{\circ} \mathrm{C}$ ?
9.64 An unknown gas is placed in a 1.500 L bulb at a pressure of 356 mm Hg and a temperature of $22.5^{\circ} \mathrm{C}$, and is found to weigh 0.9847 g . What is the molecular mass of the gas?
9.65 What are the molecular masses of the gases with the following densities:
(a) $1.342 \mathrm{~g} / \mathrm{L}$ at STP
(b) $1.053 \mathrm{~g} / \mathrm{L}$ at $25^{\circ} \mathrm{C}$ and 752 mm Hg
9.66 Pure oxygen gas was first prepared by heating mercury(II) oxide, HgO :

$$
2 \mathrm{HgO}(s) \longrightarrow 2 \mathrm{Hg}(l)+\mathrm{O}_{2}(g)
$$

What volume (in liters) of oxygen at STP is released by heating 10.57 g of HgO ?
9.67 How many grams of HgO would you need to heat if you wanted to prepare 0.0155 mol of $\mathrm{O}_{2}$ according to the equation in Problem 9.66?
9.68 Hydrogen gas can be prepared by reaction of zinc metal with aqueous HCl :

$$
\mathrm{Zn}(s)+2 \mathrm{HCl}(a q) \longrightarrow \mathrm{ZnCl}_{2}(a q)+\mathrm{H}_{2}(g)
$$

(a) How many liters of $\mathrm{H}_{2}$ would be formed at 742 mm Hg and $15^{\circ} \mathrm{C}$ if 25.5 g of zinc was allowed to react?
(b) How many grams of zinc would you start with if you wanted to prepare 5.00 L of $\mathrm{H}_{2}$ at 350 mm Hg and $30.0^{\circ} \mathrm{C}$ ?
9.69 Ammonium nitrate can decompose explosively when heated according to the equation

$$
2 \mathrm{NH}_{4} \mathrm{NO}_{3}(s) \longrightarrow 2 \mathrm{~N}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(g)+\mathrm{O}_{2}(g)
$$

How many liters of gas would be formed at $450^{\circ} \mathrm{C}$ and 1.00 atm pressure by explosion of 450 g of $\mathrm{NH}_{4} \mathrm{NO}_{3}$ ?
9.70 The reaction of sodium peroxide $\left(\mathrm{Na}_{2} \mathrm{O}_{2}\right)$ with $\mathrm{CO}_{2}$ is used in space vehicles to remove $\mathrm{CO}_{2}$ from the air and generate $\mathrm{O}_{2}$ for breathing:

$$
2 \mathrm{Na}_{2} \mathrm{O}_{2}(s)+2 \mathrm{CO}_{2}(g) \longrightarrow 2 \mathrm{Na}_{2} \mathrm{CO}_{3}(s)+\mathrm{O}_{2}(g)
$$

(a) Assuming that air is breathed at an average rate of $4.50 \mathrm{~L} / \mathrm{min}\left(25^{\circ} \mathrm{C} ; 735 \mathrm{~mm} \mathrm{Hg}\right)$ and that the concentration of $\mathrm{CO}_{2}$ in expelled air is $3.4 \%$ by volume, how many grams of $\mathrm{CO}_{2}$ are produced in 24 h ?
(b) How many days would a 3.65 kg supply of $\mathrm{Na}_{2} \mathrm{O}_{2}$ last?
9.71 Titanium(III) chloride, a substance used in catalysts for preparing polyethylene, is made by high-temperature reaction of $\mathrm{TiCl}_{4}$ vapor with $\mathrm{H}_{2}$ :

$$
2 \mathrm{TiCl}_{4}(g)+\mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{TiCl}_{3}(s)+2 \mathrm{HCl}(g)
$$

(a) How many grams of $\mathrm{TiCl}_{4}$ are needed for complete reaction with 155 L of $\mathrm{H}_{2}$ at $435^{\circ} \mathrm{C}$ and 795 mm Hg pressure?
(b) How many liters of HCl gas at STP will result from the reaction described in part (a)?

## Dalton's Law and Mole Fraction

9.72 Use the information in Table 9.1 to calculate the partial pressure (in atmospheres) of each gas in dry air at STP.
9.73 Natural gas is a mixture of many substances, primarily $\mathrm{CH}_{4}, \mathrm{C}_{2} \mathrm{H}_{6}, \mathrm{C}_{3} \mathrm{H}_{8}$, and $\mathrm{C}_{4} \mathrm{H}_{10}$. Assuming that the total pressure of the gases is 1.48 atm and that their mole ratio is $94: 4.0: 1.5: 0.50$, calculate the partial pressure (in atmospheres) of each gas.
9.74 A special gas mixture used in bacterial growth chambers contains $1.00 \%$ by weight $\mathrm{CO}_{2}$ and $99.0 \% \mathrm{O}_{2}$. What is the partial pressure (in atmospheres) of each gas at a total pressure of 0.977 atm ?
9.75 A gas mixture for use in some lasers contains $5.00 \%$ by weight $\mathrm{HCl}, 1.00 \% \mathrm{H}_{2}$, and $94 \% \mathrm{Ne}$. The mixture is sold in cylinders that have a volume of 49.0 L and a pressure of $13,800 \mathrm{kPa}$ at $21.0^{\circ} \mathrm{C}$. What is the partial pressure (in kilopascals) of each gas in the mixture?
9.76 What is the mole fraction of each gas in the mixture described in Problem 9.75?
9.77 A mixture of Ar and $\mathrm{N}_{2}$ gases has a density of $1.413 \mathrm{~g} / \mathrm{L}$ at STP. What is the mole fraction of each gas?
9.78 Magnesium metal reacts with aqueous HCl to yield $\mathrm{H}_{2}$ gas:

$$
\mathrm{Mg}(s)+2 \mathrm{HCl}(a q) \longrightarrow \mathrm{MgCl}_{2}(a q)+\mathrm{H}_{2}(g)
$$

The gas that forms is found to have a volume of 3.557 L at $25^{\circ} \mathrm{C}$ and a pressure of 747 mm Hg . Assuming that the gas is saturated with water vapor at a partial pressure of 23.8 mm Hg , what is the partial pressure (in millimeters of mercury) of the $\mathrm{H}_{2}$ ? How many grams of magnesium metal were used in the reaction?
9.79 Chlorine gas was first prepared in 1774 by the oxidation of NaCl with $\mathrm{MnO}_{2}$ :
$2 \mathrm{NaCl}(s)+2 \mathrm{H}_{2} \mathrm{SO}_{4}(l)+\mathrm{MnO}_{2}(s) \longrightarrow$

$$
\mathrm{Na}_{2} \mathrm{SO}_{4}(s)+\mathrm{MnSO}_{4}(s)+2 \mathrm{H}_{2} \mathrm{O}(g)+\mathrm{Cl}_{2}(g)
$$

Assume that the gas produced is saturated with water vapor at a partial pressure of 28.7 mm Hg and that it has a volume of 0.597 L at $27^{\circ} \mathrm{C}$ and 755 mm Hg pressure.
(a) What is the mole fraction of $\mathrm{Cl}_{2}$ in the gas?
(b) How many grams of NaCl were used in the experiment, assuming complete reaction?

## Kinetic-Molecular Theory and Graham's Law

9.80 What are the basic assumptions of the kinetic-molecular theory?
9.81 What is the difference between effusion and diffusion?
9.82 What is the difference between heat and temperature?
9.83 Why does a helium-filled balloon lose pressure faster than an air-filled balloon?
9.84 The average temperature at an altitude of 20 km is 220 K . What is the average speed (in meters per second) of an $\mathrm{N}_{2}$ molecule at this altitude?
9.85 At what temperature ( ${ }^{\circ} \mathrm{C}$ ) will xenon atoms have the same average speed that $\mathrm{Br}_{2}$ molecules have at $20^{\circ} \mathrm{C}$ ?
9.86 Which has a higher average speed, $\mathrm{H}_{2}$ at 150 K or He at $375^{\circ} \mathrm{C}$ ?
9.87 Which has a higher average speed, a Ferrari at 145 mph or a $\mathrm{UF}_{6}$ molecule at $25^{\circ} \mathrm{C}$ ?
9.88 An unknown gas is found to diffuse through a porous membrane 2.92 times more slowly than $\mathrm{H}_{2}$. What is the molecular mass of the gas?
9.89 What is the molecular mass of a gas that diffuses through a porous membrane 1.86 times faster than Xe ? What might the gas be?
9.90 Rank the following gases in order of their speed of diffusion through a membrane, and calculate the ratio of their diffusion rates: $\mathrm{HCl}, \mathrm{F}_{2}, \mathrm{Ar}$
9.91 Which will diffuse through a membrane more rapidly, CO or $\mathrm{N}_{2}$ ? Assume that the samples contain only the most abundant isotopes of each element, ${ }^{12} \mathrm{C},{ }^{16} \mathrm{O}$, and ${ }^{14} \mathrm{~N}$.
9.92 A big-league fastball travels at about $45 \mathrm{~m} / \mathrm{s}$. At what temperature $\left({ }^{\circ} \mathrm{C}\right)$ do helium atoms have this same average speed?
9.93 Traffic on the German autobahns reaches speeds of up to $230 \mathrm{~km} / \mathrm{h}$. At what temperature $\left({ }^{\circ} \mathrm{C}\right)$ do oxygen molecules have this same average speed?

## General Problems

9.94 Chlorine occurs as a mixture of two isotopes, ${ }^{35} \mathrm{Cl}$ and ${ }^{37} \mathrm{Cl}$. What is the ratio of the diffusion rates of the three species $\left({ }^{35} \mathrm{Cl}\right)_{2},{ }^{35} \mathrm{Cl}{ }^{37} \mathrm{Cl}$, and $\left({ }^{37} \mathrm{Cl}\right)_{2}$ ?
9.95 What would the atmospheric pressure be (in millimeters of mercury) if our atmosphere were composed of pure $\mathrm{CO}_{2}$ gas?
9.96 The surface temperature of Venus is about 1050 K , and the pressure is about 75 Earth atmospheres. Assuming that these conditions represent a Venusian "STP," what is the standard molar volume (in liters) of a gas on Venus?
9.97 When you look directly up at the sky, you are actually looking through a very tall, transparent column of air that extends from the surface of the earth thousands of kilometers into space. If the air in this column were liquefied, how tall would it be? The density of liquid air is $0.89 \mathrm{~g} / \mathrm{mL}$.
9.98 Assume that you take a flask, evacuate it to remove all the air, and find its mass to be 478.1 g . You then fill the flask with argon to a pressure of 2.15 atm and reweigh it. What would the balance read (in grams) if the flask has a volume of 7.35 L and the temperature is $20.0^{\circ} \mathrm{C}$ ?
9.99 The apparatus shown consists of three bulbs connected by stopcocks. What is the pressure inside the system when the stopcocks are opened? Assume that the lines connecting the bulbs have zero volume and that the temperature remains constant.

9.100 The apparatus shown consists of three temperaturejacketed 1.000 L bulbs connected by stopcocks. Bulb A contains a mixture of $\mathrm{H}_{2} \mathrm{O}(g), \mathrm{CO}_{2}(g)$, and $\mathrm{N}_{2}(g)$ at $25^{\circ} \mathrm{C}$ and a total pressure of 564 mm Hg . Bulb B is empty and is held at a temperature of $-70^{\circ} \mathrm{C}$. Bulb C is also empty and is held at a temperature of $-190^{\circ} \mathrm{C}$. The stopcocks are closed, and the volume of the lines connecting the bulbs is zero. $\mathrm{CO}_{2}$ sublimes at $-78^{\circ} \mathrm{C}$, and $\mathrm{N}_{2}$ boils at $-196^{\circ} \mathrm{C}$.

(a) The stopcock between A and B is opened, and the system is allowed to come to equilibrium. The pressure in A and B is now 219 mm Hg . What do bulbs $A$ and $B$ contain?
(b) How many moles of $\mathrm{H}_{2} \mathrm{O}$ are in the system?
(c) Both stopcocks are opened, and the system is again allowed to come to equilibrium. The pressure throughout the system is 33.5 mm Hg . What do bulbs $\mathrm{A}, \mathrm{B}$, and C contain?
(d) How many moles of $\mathrm{N}_{2}$ are in the system?
(e) How many moles of $\mathrm{CO}_{2}$ are in the system?
9.101 Assume that you have 1.00 g of nitroglycerin in a 500.0 mL steel container at $20.0^{\circ} \mathrm{C}$ and 1.00 atm pressure. An explosion occurs, raising the temperature of the container and its contents to $425^{\circ} \mathrm{C}$. The balanced equation is

$$
\begin{aligned}
& 4 \mathrm{C}_{3} \mathrm{H}_{5} \mathrm{~N}_{3} \mathrm{O}_{9}(l) \longrightarrow \\
& 12 \mathrm{CO}_{2}(g)
\end{aligned}+10 \mathrm{H}_{2} \mathrm{O}(g)+6 \mathrm{~N}_{2}(g)+\mathrm{O}_{2}(g)
$$

(a) How many moles of nitroglycerin and how many moles of gas (air) were in the container originally?
(b) How many moles of gas are in the container after the explosion?
(c) What is the pressure (in atmospheres) inside the container after the explosion according to the ideal gas law?
9.102 Use both the ideal gas law and the van der Waals equation to calculate the pressure (in atmospheres) of 45.0 g of $\mathrm{NH}_{3}$ gas in a 1.000 L container at $0^{\circ} \mathrm{C}, 50^{\circ} \mathrm{C}$, and $100^{\circ} \mathrm{C}$. For $\mathrm{NH}_{3}, a=4.17\left(\mathrm{~L}^{2} \cdot \mathrm{~atm}\right) / \mathrm{mol}^{2}$ and $b=0.0371 \mathrm{~L} / \mathrm{mol}$.
9.103 When solid mercury $(\mathrm{I})$ carbonate, $\mathrm{Hg}_{2} \mathrm{CO}_{3}$, is added to nitric acid, $\mathrm{HNO}_{3}$, a reaction occurs to give mercury(II) nitrate, $\mathrm{Hg}\left(\mathrm{NO}_{3}\right)_{2}$, water, and two gases A and B :

$$
\begin{aligned}
& \mathrm{Hg}_{2} \mathrm{CO}_{3}(s)+ \mathrm{HNO}_{3}(a q) \longrightarrow \\
& \mathrm{Hg}\left(\mathrm{NO}_{3}\right)_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{A}(g)+\mathrm{B}(g)
\end{aligned}
$$

(a) When the gases are placed in a 500.0 mL bulb at $20^{\circ} \mathrm{C}$, the pressure is 258 mm Hg . How many moles of gas are present?
(b) When the gas mixture is passed over $\mathrm{CaO}(s)$, gas A reacts, forming $\mathrm{CaCO}_{3}(s)$ :

$$
\mathrm{CaO}(s)+\mathrm{A}(g)+\mathrm{B}(g) \longrightarrow \mathrm{CaCO}_{3}(s)+\mathrm{B}(g)
$$

The remaining gas B is collected in a 250.0 mL container at $20^{\circ} \mathrm{C}$ and found to have a pressure of 344 mm Hg. How many moles of B are present?
(c) The mass of gas B collected in part (b) was found to be 0.218 g . What is the density of $B$ (in grams per liter)?
(d) What is the molecular mass of $B$, and what is its formula?
(e) Write a balanced equation for the reaction of mercury(I) carbonate with nitric acid.
9.104 Dry ice (solid $\mathrm{CO}_{2}$ ) has occasionally been used as an "explosive" in mining. A hole is drilled, dry ice and a small amount of gunpowder are placed in the hole, a fuse is added, and the hole is plugged. When lit, the exploding gunpowder rapidly vaporizes the dry ice, building up an immense pressure. Assume that 500.0 g of dry ice is placed in a cavity with a volume of 0.800 L and the ignited gunpowder heats the $\mathrm{CO}_{2}$ to 700 K . What is the final pressure inside the hole?
9.105 Consider the combustion reaction of 0.148 g of a hydrocarbon having formula $\mathrm{C}_{n} \mathrm{H}_{2 n+2}$ with an excess of $\mathrm{O}_{2}$ in a 400.0 mL steel container. Before reaction, the gaseous mixture had a temperature of $25.0^{\circ} \mathrm{C}$ and a pressure of 2.000 atm . After complete combustion and loss of considerable heat, the mixture of products and excess $\mathrm{O}_{2}$ had a temperature of $125.0^{\circ} \mathrm{C}$ and a pressure of 2.983 atm .
(a) What is the formula and molar mass of the hydrocarbon?
(b) What are the partial pressures (in atmospheres) of the reactants?
(c) What are the partial pressures (in atmospheres) of the products and the excess $\mathrm{O}_{2}$ ?
9.106 Natural gas is a mixture of hydrocarbons, primarily methane $\left(\mathrm{CH}_{4}\right)$ and ethane $\left(\mathrm{C}_{2} \mathrm{H}_{6}\right)$. A typical mixture might have $X_{\text {methane }}=0.915$ and $X_{\text {ethane }}=0.085$. Let's assume that we have a 15.50 g sample of natural gas in a volume of 15.00 L at a temperature of $20.00^{\circ} \mathrm{C}$.
(a) How many total moles of gas are in the sample?
(b) What is the pressure of the sample (in atmospheres)?
(c) What is the partial pressure of each component in the sample (in atmospheres)?
(d) When the sample is burned in an excess of oxygen, how much heat (in kilojoules) is liberated?
9.107 A mixture of $\mathrm{CS}_{2}(g)$ and excess $\mathrm{O}_{2}(g)$ is placed in a 10.0 L reaction vessel at $100.0^{\circ} \mathrm{C}$ and a pressure of 3.00 atm . A spark causes the $\mathrm{CS}_{2}$ to ignite, burning it completely, according to the equation:

$$
\mathrm{CS}_{2}(g)+3 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{SO}_{2}(g)
$$

After reaction, the temperature returns to $100.0^{\circ} \mathrm{C}$, and the mixture of product gases $\left(\mathrm{CO}_{2}, \mathrm{SO}_{2}\right.$, and unreacted $\mathrm{O}_{2}$ ) is found to have a pressure of 2.40 atm . What is the partial pressure of each gas in the product mixture?
9.108 Gaseous compound $Q$ contains only xenon and oxygen. When 0.100 g of Q is placed in a 50.0 mL steel vessel at $0^{\circ} \mathrm{C}$, the pressure is 0.229 atm .
(a) What is the molar mass of Q , and what is a likely formula?
(b) When the vessel and its contents are warmed to $100^{\circ} \mathrm{C}, \mathrm{Q}$ decomposes into its constituent elements, giving a final pressure inside the container of 0.941 atm . What are the partial pressures of xenon and oxygen in the container?
9.109 When 10.0 g of a mixture of $\mathrm{Ca}\left(\mathrm{ClO}_{3}\right)_{2}$ and $\mathrm{Ca}(\mathrm{ClO})_{2}$ is heated to $700^{\circ} \mathrm{C}$ in a 10.0 L vessel, both compounds decompose, forming $\mathrm{O}_{2}(g)$ and $\mathrm{CaCl}_{2}(s)$. The final pressure inside the vessel is 1.00 atm .
(a) Write balanced equations for the decomposition reactions.
(b) What is the mass of each compound in the original mixture?
9.110 A 5.00 L vessel contains 25.0 g of $\mathrm{PCl}_{3}$ and 3.00 g of $\mathrm{O}_{2}$ at $15^{\circ} \mathrm{C}$. The vessel is heated to $200.0^{\circ} \mathrm{C}$, and the contents react to give $\mathrm{POCl}_{3}$. What is the final pressure in the vessel, assuming that the reaction goes to completion and that all reactants and products are in the gas phase?
9.111 When 2.00 mol of $\mathrm{NOCl}(\mathrm{g})$ was heated to $225^{\circ} \mathrm{C}$ in a 400.0 L steel reaction vessel, the NOCl partially decomposed according to the equation $2 \mathrm{NOCl}(g) \rightarrow$ $2 \mathrm{NO}(g)+\mathrm{Cl}_{2}(g)$. The pressure in the vessel after reaction is 0.246 atm.
(a) What is the partial pressure of each gas in the vessel after reaction?
(b) What percent of the NOCl decomposed?
9.112 Ozone $\left(\mathrm{O}_{3}\right)$ can be prepared in the laboratory by passing an electrical discharge through oxygen gas: $3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{O}_{3}(\mathrm{~g})$. Assume that an evacuated steel vessel with a volume of 10.00 L is filled with 32.00 atm of $\mathrm{O}_{2}$ at $25^{\circ} \mathrm{C}$ and an electric discharge is passed through the vessel, causing some of the oxygen to be converted into ozone. As a result, the pressure inside the vessel drops to 30.64 atm at $25.0^{\circ} \mathrm{C}$. What is the final mass percent of ozone in the vessel?
9.113 A steel container with a volume of 500.0 mL is evacuated, and 25.0 g of $\mathrm{CaCO}_{3}$ is added. The container and contents are then heated to 1500 K , causing the $\mathrm{CaCO}_{3}$ to decompose completely, according to the equation: $\mathrm{CaCO}_{3}(\mathrm{~s}) \rightarrow \mathrm{CaO}(\mathrm{s})+\mathrm{CO}_{2}(g)$
(a) Using the ideal gas law and ignoring the volume of any solids remaining in the container, calculate the pressure inside the container at 1500 K .
(b) Now make a more accurate calculation of the pressure inside the container. Take into account the volume of solid CaO (density $=3.34 \mathrm{~g} / \mathrm{mL}$ ) in the container, and use the van der Waals equation to calculate the pressure. The van der Waals constants for $\mathrm{CO}_{2}(g)$ are: $a=3.59\left(\mathrm{~L}^{2} \cdot \mathrm{~atm}\right) / \mathrm{mol}^{2}$, and $b=0.0427 \mathrm{~L} / \mathrm{mol}$.

## Multi-Concept Problems

9.114 An empty 4.00 L steel vessel is filled with 1.00 atm of $\mathrm{CH}_{4}(g)$ and 4.00 atm of $\mathrm{O}_{2}(g)$ at $300^{\circ} \mathrm{C}$. A spark causes the $\mathrm{CH}_{4}$ to burn completely, according to the equation:

$$
\begin{array}{r}
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \\
\Delta H^{\circ}=-802 \mathrm{~kJ}
\end{array}
$$

(a) What mass of $\mathrm{CO}_{2}(g)$ is produced in the reaction?
(b) What is the final temperature inside the vessel after combustion, assuming that the steel vessel has a mass of 14.500 kg , the mixture of gases has an average molar heat capacity of $21 \mathrm{~J} /\left(\mathrm{mol} \cdot{ }^{\circ} \mathrm{C}\right)$, and the heat capacity of steel is $0.449 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$ ?
(c) What is the partial pressure of $\mathrm{CO}_{2}(g)$ in the vessel after combustion?
9.115 When a gaseous compound X containing only $\mathrm{C}, \mathrm{H}$, and O is burned in $\mathrm{O}_{2}, 1$ volume of the unknown gas reacts with 3 volumes of $\mathrm{O}_{2}$ to give 2 volumes of $\mathrm{CO}_{2}$ and 3 volumes of gaseous $\mathrm{H}_{2} \mathrm{O}$. Assume all volumes are measured at the same temperature and pressure.
(a) Calculate a formula for the unknown gas, and write a balanced equation for the combustion reaction.
(b) Is the formula you calculated an empirical formula or a molecular formula? Explain.
(c) Draw two different possible electron-dot structures for the compound X .
(d) Combustion of 5.000 g of X releases 144.2 kJ heat. Look up $\Delta H^{\circ}$ falues for $\mathrm{CO}_{2}(g)$ and $\mathrm{H}_{2} \mathrm{O}(g)$ in Appendix B, and calculate $\Delta H^{\circ}{ }_{\mathrm{f}}$ for compound X .
9.116 Isooctane, $\mathrm{C}_{8} \mathrm{H}_{18}$, is the component of gasoline from which the term octane rating derives.
(a) Write a balanced equation for the combustion of isooctane to yield $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$.
(b) Assuming that gasoline is $100 \%$ isooctane, that isooctane burns to produce only $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$, and that the density of isooctane is $0.792 \mathrm{~g} / \mathrm{mL}$, what mass of $\mathrm{CO}_{2}$ (in kilograms) is produced each year by the annual U.S. gasoline consumption of $4.6 \times 10^{10} \mathrm{~L}$ ?
(c) What is the volume (in liters) of this $\mathrm{CO}_{2}$ at STP?
(d) How many moles of air are necessary for the combustion of 1 mol of isooctane, assuming that air is $21.0 \% \mathrm{O}_{2}$ by volume? What is the volume (in liters) of this air at STP?
9.117 The Rankine temperature scale used in engineering is to the Fahrenheit scale as the Kelvin scale is to the Celsius scale. That is, 1 Rankine degree is the same size as 1 Fahrenheit degree, and $0^{\circ} \mathrm{R}=$ absolute zero.
(a) What temperature corresponds to the freezing point of water on the Rankine scale?
(b) What is the value of the gas constant $R$ on the Rankine scale in $(\mathrm{L} \cdot \mathrm{atm}) /\left({ }^{\circ} \mathrm{R} \cdot \mathrm{mol}\right)$ ?
(c) Use the van der Waals equation to determine the pressure inside a 400.0 mL vessel that contains 2.50 mol of $\mathrm{CH}_{4}$ at a temperature of $525^{\circ} \mathrm{R}$. For $\mathrm{CH}_{4}$, $a=2.253\left(\mathrm{~L}^{2} \cdot \mathrm{~atm}\right) / \mathrm{mol}^{2} ; b=0.04278 \mathrm{~L} / \mathrm{mol}$.
9.118 Chemical explosions are characterized by the instantaneous release of large quantities of hot gases, which set up a shock wave of enormous pressure (up to 700,000 atm ) and velocity (up to $20,000 \mathrm{mi} / \mathrm{h}$ ). For example, explosion of nitroglycerin $\left(\mathrm{C}_{3} \mathrm{H}_{5} \mathrm{~N}_{3} \mathrm{O}_{9}\right)$ releases four gases, A, B, C, and D:

$$
n \mathrm{C}_{3} \mathrm{H}_{5} \mathrm{~N}_{3} \mathrm{O}_{9}(l) \longrightarrow \vec{a} \mathrm{~A}(g)+b \mathrm{~B}(g)+c \mathrm{C}(g)+d \mathrm{D}(g)
$$

Assume that the explosion of $1 \mathrm{~mol}(227 \mathrm{~g})$ of nitroglycerin releases gases with a temperature of $1950^{\circ} \mathrm{C}$ and a volume of 1323 L at 1.00 atm pressure.
(a) How many moles of hot gas are released by the explosion of 0.00400 mol of nitroglycerin?
(b) When the products released by explosion of 0.00400 mol of nitroglycerin were placed in a 500.0 mL flask and the flask was cooled to $-10^{\circ} \mathrm{C}$, product A solidified, and the pressure inside the flask was 623 mm Hg . How many moles of A were present, and what is its likely identity?
(c) When gases $\mathrm{B}, \mathrm{C}$, and D were passed through a tube of powdered $\mathrm{Li}_{2} \mathrm{O}$, gas B reacted to form $\mathrm{Li}_{2} \mathrm{CO}_{3}$. The remaining gases, C and D , were collected in another 500.0 mL flask and found to have a pressure of 260 mm Hg at $25^{\circ} \mathrm{C}$. How many moles of $B$ were present, and what is its likely identity?
(d) When gases C and D were passed through a hot tube of powdered copper, gas $C$ reacted to form CuO . The remaining gas, D , was collected in a third 500.0 mL flask and found to have a mass of 0.168 g and a pressure of 223 mm Hg at $25^{\circ} \mathrm{C}$. How many moles each of C and D were present, and what are their likely identities?
(e) Write a balanced equation for the explosion of nitroglycerin.
9.119 Combustion analysis of 0.1500 g of methyl tert-butyl ether, an octane booster used in gasoline, gave 0.3744 g of $\mathrm{CO}_{2}$ and 0.1838 g of $\mathrm{H}_{2} \mathrm{O}$. When a flask having a volume of 1.00 L was evacuated and then filled with methyl tertbutyl ether vapor at a pressure of 100.0 kPa and a temperature of $54.8^{\circ} \mathrm{C}$, the mass of the flask increased by 3.233 g .
(a) What is the empirical formula of methyl tert-butyl ether?
(b) What is the molecular mass and molecular formula of methyl tert-butyl ether?
(c) Write a balanced equation for the combustion reaction.
(d) The enthalpy of combustion for methyl tert-butyl ether is $\Delta H^{\circ}{ }_{\text {combustion }}=-3368.7 \mathrm{~kJ} / \mathrm{mol}$. What is its standard enthalpy of formation, $\Delta H^{\circ}{ }_{\mathrm{f}}$ ?

## eMedia Problems

9.120 The Gas Laws activity (eChapter 9.2) allows you to view how the volume of a gas changes when pressure, temperature, and amount of gas are changed. What happens to the volume when the pressure is doubled? What law does this illustrate? What happens when the amount of gas is doubled? What law does this represent?
9.121 The Density of Gases activity (eChapter 9.4) allows you to compare the densities of various gases at different temperatures and pressures. How does the density change when the pressure is increased? Why does pressure affect density this way?
9.122 Use the Partial Pressure activity in eChapter 9.5 to answer the following questions:
(a) What is the total pressure when 1.0 mol of any gas is added to the container?
(b) How does the number of He molecules change when 1.0 mol of $\mathrm{N}_{2}$ is added?
(c) How does the partial pressure of He change when 1.0 mol of $\mathrm{N}_{2}$ is added? Explain.
(d) How is the total pressure related to the partial pressures of the gases in the mixture?
9.123 Run the Diffusion and Effusion activity (eChapter 9.7). Assume that the time represented is 1 minute, and determine the rate of effusion for each of the gases. What is the mass ratio of the two gases?
9.124 The relative speeds of helium and neon atoms are illustrated in the Kinetic Energies in a Gas movie (eChapter 9.6). Given that the average kinetic energies of all gases are equal at a given temperature, determine how much faster helium atoms move (on average) than neon atoms. How does this particular aspect of kinetic-molecular theory ( $E_{\mathrm{K}} \propto$ to absolute temperature) explain Charles' observation that pressure increases with increasing temperature at constant volume?

## Chapter

## Liquids, Solids, and Phase Changes

## The kinetic-molecular theory developed in the previous chapter accounts for the properties of gases by assuming that gas particles act independently

 of one another. Because the attractive forces between them are so weak, the particles in gases are free to move about at random and occupy whatever space is available. The same is not true in liquids and solids, however. Liquids and solids are distinguished from gases by the presence of strong attractive forces between particles. In liquids, these attractive forces are strong enough to hold the particles in close contact whileThis thermometer works on the principle that the liquids in the different glass bulbs have slightly different densities, causing them to rise or sink as the density of the fluid in the column varies with temperature.

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■ Interlude—Liquid Crystals

FIGURE 10.1 A molecular comparison of gases, liquids, and solids. (a) In gases, the particles feel little attraction for one another and are free to move about randomly. (b) In liquids, the particles are held close together by attractive forces but are free to move over one another. (c) In solids, the particles are rigidly held in an ordered arrangement.

VA bond is polar if the atoms joined have different electronegativities. A molecule is polar if the bond polarities are not symmetrically arranged, which results in an uneven distribution of charges about the molecule and a net dipole moment.
still letting them slip and slide over one another. In solids, the forces are so strong that they hold the particles rigidly in place and prevent their movement (Figure 10.1).


In this chapter, we'll examine the nature of the forces responsible for the properties of liquids and solids, paying particular attention to the ordering of particles in solids and to the different kinds of solids that result. In addition, we'll look at what happens during transitions between solid, liquid, and gaseous states and at the effects of temperature and pressure on these transitions.

## 10.1 | Polar Covalent Bonds and Dipole Moments

Before looking at the forces between molecules, it's first necessary to develop the ideas of bond dipoles and dipole moments. We saw in Section 7.4 that polar covalent bonds form between atoms of different electronegativity. Chlorine is more electronegative than carbon, for example, and the chlorine atom in chloromethane $\left(\mathrm{CH}_{3} \mathrm{Cl}\right)$ thus attracts the electrons in the $\mathrm{C}-\mathrm{Cl}$ bond toward itself. The $\mathrm{C}-\mathrm{Cl}$ bond is therefore polarized so that the chlorine atom is slightly electron-rich $(\delta-)$ and the carbon atom is slightly electron-poor $(\delta+)$.

Because the polar $\mathrm{C}-\mathrm{Cl}$ bond in chloromethane has two polar ends-a positive end and a negative end-we describe it as being a bond dipole, and we often represent the dipole using an arrow with a cross at one end $(\leftrightarrow)$ to indicate the direction of electron displacement. The point of the arrow represents the negative end of the dipole ( $\delta-$ ), and the crossed end (which looks like a plus sign) represents the positive end $(\delta+)$. This polarity is clearly visible in an electrostatic potential map (Section 7.4), which shows the electron-rich chlorine atom as red and the electron-poor remainder of the molecule as blue-green.

The measure of net molecular polarity is a quantity called the dipole moment, $\boldsymbol{\mu}($ Greek mu$)$, which is defined as the magnitude of the charge $Q$ at either end of the molecular dipole times the distance $r$ between the charges: $\mu=Q \times r$. Dipole moments are expressed in debyes ( D ), where $1 \mathrm{D}=3.336 \times 10^{-30}$ coulomb meters $(\mathrm{C} \cdot \mathrm{m})$ in SI units. To calibrate your thinking, the charge on an electron is $1.60 \times 10^{-19} \mathrm{C}$. Thus, if one proton and one electron were separated by $100 \mathrm{pm}(\mathrm{a}$ bit less than the length of a typical covalent bond), then the dipole moment would be $1.60 \times 10^{-29} \mathrm{C} \cdot \mathrm{m}$, or 4.80 D :

$$
\begin{aligned}
& \mu=Q \times r \\
& \mu=\left(1.60 \times 10^{-19} \mathrm{C}\right)\left(100 \times 10^{-12} \mathrm{~m}\right)\left(\frac{1 \mathrm{D}}{3.336 \times 10^{-30} \mathrm{C} \cdot \mathrm{~m}}\right)=4.80 \mathrm{D}
\end{aligned}
$$

It's relatively easy to measure dipole moments experimentally, and values for some common substances are given in Table 10.1. Once the dipole moment is known, it's then possible to get an idea of the amount of charge separation in a molecule. In chloromethane, for example, the experimentally measured dipole moment is $\mu=1.87 \mathrm{D}$. If we assume that the contributions of the nonpolar $\mathrm{C}-\mathrm{H}$ bonds are small, then most of the chloromethane dipole moment is due to the $\mathrm{C}-\mathrm{Cl}$ bond. Since the $\mathrm{C}-\mathrm{Cl}$ bond distance is 178 pm , we can calculate that the dipole moment of chloromethane would be $1.78 \times 4.80 \mathrm{D}=8.54 \mathrm{D}$ if the $\mathrm{C}-\mathrm{Cl}$ bond were ionic (that is, if a full negative charge on chlorine were separated from a full positive charge on carbon by a distance of 178 pm ). But because the measured dipole moment of chloromethane is only 1.87 D , we can conclude that the $\mathrm{C}-\mathrm{Cl}$ bond is only about $(1.87 / 8.54)(100 \%)=22 \%$ ionic. Thus, the chlorine atom in chloromethane has an excess of about 0.2 electron, and the carbon atom has a deficiency of about 0.2 electron.

Not surprisingly, the largest dipole moment listed in Table 10.1 belongs to the ionic compound NaCl . Water and ammonia also have substantial dipole moments because both oxygen and nitrogen are electronegative relative to hydrogen and because both O and N have lone pairs of electrons that make substantial contributions to net molecular polarity:
R. J. Tykodi, "Identifying Polar and Nonpolar Molecules," J. Chem. Educ., Vol. 66, 1989, 1007-1011.

7h Thomas H. Bindel and Timothy C. Smiley, "The Ropes: A Molecular Polarity Activity," J. Chem. Educ., Vol. 71, 1994, 945.


| TABLE 10.1 | Dipole <br> Moments of |
| :--- | :--- |
| Some Common Compounds |  |$|$| Dipole |
| :--- |
| Moment (D) |

*Measured in the gas phase


Ammonia ( $\mu=1.47 \mathrm{D}$ )
In contrast with water and ammonia, carbon dioxide and tetrachloromethane $\left(\mathrm{CCl}_{4}\right)$ have zero dipole moments. Molecules of both substances contain individual polar covalent bonds, but because of the symmetry of their structures, the individual bond polarities exactly cancel.


Water ( $\mu=1.85 \mathrm{D}$ )


DT Carlos Furio and Ma. Luisa 1] Calatayud, "Difficulties with the Geometry and Polarity of Molecules: Beyond Misconceptions," J. Chem. Educ., Vol. 73, 1996, 36-41.



Tetrachloromethane $(\mu=0)$

Molecular Polarity activity

## Worked Example 10.1

The dipole moment of HCl is 1.03 D , and the distance between atoms is 127 pm . What is the percent ionic character of the HCl bond?

## Strategy

If HCl were $100 \%$ ionic, a negative charge $\left(\mathrm{Cl}^{-}\right)$would be separated from a positive charge $\left(\mathrm{H}^{+}\right)$by 127 pm . Calculate the expected dipole moment, and compare that calculated value to the actual value.

## Solution

The calculated dipole moment is:

$$
\begin{aligned}
& \mu=Q \times r \\
& \mu=\left(1.60 \times 10^{-19} \mathrm{C}\right)\left(127 \times 10^{-12} \mathrm{~m}\right)\left(\frac{1 \mathrm{D}}{3.336 \times 10^{-30} \mathrm{C} \cdot \mathrm{~m}}\right)=6.09 \mathrm{D}
\end{aligned}
$$

The observed dipole moment of $\mathrm{HCl}(1.03 \mathrm{D})$ implies that the $\mathrm{H}-\mathrm{Cl}$ bond is only about $17 \%$ ionic:

$$
\frac{1.03 \mathrm{D}}{6.09 \mathrm{D}} \times 100 \%=16.9 \%
$$

## Worked Example 10.2

Would you expect vinyl chloride $\left(\mathrm{H}_{2} \mathrm{C}=\mathrm{CHCl}\right)$, the starting material used for preparation of poly(vinyl chloride) polymer, to have a dipole moment? If so, indicate the direction.

## Strategy

First, use the VSEPR model described in Section 7.9 to predict the molecular shape of vinyl chloride. Then, assign polarities to the individual bonds according to the differences in electronegativity of the bonded atoms (Figure 7.4), and make a reasonable guess about the overall polarity that would result by summing the individual contributions.

## Solution

Because both carbon atoms have three charge clouds, each has trigonal planar geometry, and the molecule as a whole is planar:


Only the $\mathrm{C}-\mathrm{Cl}$ bond has a substantial polarity, giving the molecule a net polarity:



- PROBLEM 10.1 The dipole moment of HF is $\mu=1.82 \mathrm{D}$, and the bond length is 92 pm . Calculate the percent ionic character of the H-F bond. Is HF more ionic or less ionic than HCl (Worked Example 10.1)?
- PROBLEM 10.2 Tell which of the following compounds is likely to have a dipole moment, and show the direction of each.
(a) $\mathrm{SF}_{6}$
(b) $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}$
(c) $\mathrm{CHCl}_{3}$
(d) $\mathrm{CH}_{2} \mathrm{Cl}_{2}$
- KEY CONCEPT PROBLEM 10.3 The dipole moment of methanol is $\mu=1.70 \mathrm{D}$. Use arrows to indicate the direction in which electrons are displaced.

-KEY CONCEPT PROBLEM 10.4 Methylamine, $\mathrm{CH}_{3} \mathrm{NH}_{2}$, is responsible for the odor of rotting fish. Look at the following electrostatic potential map of methylamine, and explain the observed polarity.



### 10.2 Intermolecular Forces

Now that we know a bit about molecular polarities, let's see how they give rise to some of the forces that occur between molecules. The existence of such forces is easy to show. Take $\mathrm{H}_{2} \mathrm{O}$, for example. An individual $\mathrm{H}_{2} \mathrm{O}$ molecule consists of two hydrogen atoms and one oxygen atom joined together in a specific way by the intramolecular forces that we call covalent bonds. But a visible sample of $\mathrm{H}_{2} \mathrm{O}$ exists either as solid ice, liquid water, or gaseous steam, depending on its temperature. Thus, there must also be some intermolecular forces between molecules that hold the molecules together at certain temperatures (Figure 10.2). (Strictly speaking, the term intermolecular refers only to molecular substances, but we'll use it generally to refer to interactions among all kinds of particles, including molecules, ions, and atoms.)

Intermolecular forces as a whole are usually called van der Waals forces after the Dutch scientist Johannes van der Waals (1837-1923). These forces are of several different types, including dipole-dipole forces, London dispersion forces, and hydrogen bonds. In addition, ion-dipole forces operate between ions and molecules. All these intermolecular forces are electrical in origin and result from the mutual attraction of unlike charges or the mutual repulsion of like charges. If the particles are ions, then full charges are present and the ion-ion attractions are so strong (energies on the order of $500-1000 \mathrm{~kJ} / \mathrm{mol}$ ) that they give rise to what we call ionic bonds (Section 6.6). If the particles are neutral, then only partial charges are present at best, but even so, the attractive forces can be substantial.

VIntramolecular forces are the relatively strong bonding forces that hold atoms together in the molecular unit. Intermolecular forces are the relatively weak forces that hold one molecular unit to other molecular units.

Robert R. Perkins, "Put the Body to Rest," J. Chem. Educ., Vol. 72, 1995, 151-152. An analogical demonstration of molecular polarity and chemical and physical changes involving intramolecular and intermolecular forces.

FIGURE 10.2 (a) The atoms in an individual $\mathrm{N}_{2}$ molecule are held together by the strong intramolecular force we call a covalent bond. Different $\mathrm{N}_{2}$ molecules are weakly attracted to one another at low temperature by intermolecular forces, causing nitrogen to become liquid. (b) At higher temperatures, intermolecular forces are no longer able to keep molecules close together, so nitrogen becomes a gas.

Ponnadural Ramasami, "Students as Solids, Liquids, and Gases," J. Chem. Educ., Vol. 76, 1999, 485.

FIGURE 10.3 Polar $>$ molecules orient toward ions so that (a) the positive end of the dipole is near an anion and (b) the negative end of the dipole is near a cation.


## Ion-Dipole Forces

We saw in the previous section that a molecule has a net polarity and an overall dipole moment if the sum of its individual bond dipoles is nonzero. One side of the molecule has a net excess of electrons and a partial negative charge ( $\delta-$ ), while the other side has a net deficiency of electrons and a partial positive charge $(\delta+)$. An ion-dipole force is the result of electrical interactions between an ion and the partial charges on a polar molecule (Figure 10.3).

(a)

(b)

As you might expect, the favored orientation of a polar molecule in the presence of ions is one where the positive end of the dipole is near an anion and the negative end of the dipole is near a cation. The magnitude of the interaction energy $E$ depends on the charge on the ion $z$, on the strength of the dipole as measured by its dipole moment $\mu$, and on the inverse square of the distance $r$ from the ion to the dipole: $E=z \mu / r^{2}$. Ion-dipole forces are particularly important in aqueous solutions of ionic substances such as NaCl , in which polar water molecules surround the ions. We'll explore this point in more detail in the next chapter.

## Dipole-Dipole Forces

Neutral but polar molecules experience dipole-dipole forces as the result of electrical interactions among dipoles on neighboring molecules. The forces can be either attractive or repulsive, depending on the orientation of the molecules
(Figure 10.4), and the net force in a large collection of molecules results from many individual interactions of both types. The forces are generally weak, with energies on the order of $3-4 \mathrm{~kJ} / \mathrm{mol}$, and are significant only when molecules are in close contact.


Not surprisingly, the strength of a given dipole-dipole interaction depends on the sizes of the dipole moments involved. The more polar the substance, the greater the strength of its dipole-dipole interactions. Butane, for instance, is a nonpolar molecule with a molecular mass of 58 amu and a boiling point of $-0.5^{\circ} \mathrm{C}$, while acetone has the same molecular mass yet boils $57^{\circ} \mathrm{C}$ higher because it is polar.


Mol mass $=58 \mathrm{amu}$ $\mathrm{bp}=-0.5^{\circ} \mathrm{C}$
$\triangle$ FIGURE 10.4 (a) Polar molecules attract one another when they orient with unlike charges close together, but (b) repel one another when they orient with like charges together.


| TABLE 10.2 | Comparison of Molecular Masses, Dipole Moments, and Boiling Points |  |  |
| :--- | :--- | :--- | :--- |
| Substance | Mol Mass (amu) | Dipole Moment (D) | bp (K) |
| $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | 44.10 | 0.1 | 231 |
| $\mathrm{CH}_{3} \mathrm{OCH}_{3}$ | 46.07 | 1.3 | 248 |
| $\mathrm{CH}_{3} \mathrm{Cl}$ | 50.49 | 1.9 | 249 |
| $\mathrm{CH}_{3} \mathrm{CN}$ | 41.05 | 3.9 | 355 |

Doris R. Kimbrough and Ronald DeLorenzo, "Solving the Mystery of Fading Fingerprints with London Dispersion Forces," J. Chem. Educ., Vol. 75, 1998, 1300-1301.
C. Jayne Wilcox, "London Dispersion Forces and the Wave," J. Chem. Educ., Vol. 75, 1998, 1300-1301.

FIGURE 10.5 (a) Averaged over time, the electron distribution in a $\mathrm{Br}_{2}$ molecule is symmetrical. (b) At any given instant, however, the electron distribution may be unsymmetrical, resulting in a temporary dipole in that molecule and inducing a complementary attractive dipole in neighboring molecules.


| TABLE $\mathbf{1 0 . 3}$ | Melting <br> Points and <br> Boiling Points of the Halogens |
| :--- | ---: |
| Halogen | $\mathbf{m p}(\mathbf{( K )}$ |
| bp (K) |  |
| $\mathrm{F}_{2}$ | 53.5 |
| $\mathrm{Cl}_{2}$ | 172.2 |
| $\mathrm{Br}_{2}$ | 265.9 |
| $\mathrm{I}_{2}$ | 386.7 |

## London Dispersion Forces

The causes of intermolecular forces among charged and polar particles are easy to understand, but it's less obvious how such forces arise among nonpolar molecules or the individual atoms of a noble gas. Benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)$, for example, has zero dipole moment and therefore experiences no dipole-dipole forces. Nevertheless, there must be some intermolecular forces present among benzene molecules because the substance is a liquid rather than a gas at room temperature, with a melting point of $5.5^{\circ} \mathrm{C}$ and a boiling point of $80.1^{\circ} \mathrm{C}$.


Benzene
$\mu=0$
$\mathrm{mp}=5.5^{\circ} \mathrm{C}$
$\mathrm{bp}=80.1^{\circ} \mathrm{C}$


All atoms and molecules experience London dispersion forces, which result from the motion of electrons. Take even a simple nonpolar molecule like $\mathrm{Br}_{2}$, for instance. Averaged over time, the distribution of electrons throughout the molecule is symmetrical, but at any given instant there may be more electrons at one end of the molecule than at the other, giving the molecule a short-lived dipole. This instantaneous dipole on one molecule can affect the electron distributions in neighboring molecules and induce temporary dipoles in those neighbors (Figure 10.5b). As a result, weak attractive forces develop and $\mathrm{Br}_{2}$ is a liquid at room temperature rather than a gas.


London forces are generally small, with energies in the range $1-10 \mathrm{~kJ} / \mathrm{mol}$, and their exact magnitude depends on the ease with which a molecule's electron cloud can be distorted by a nearby electric field, a property referred to as polarizability. A smaller molecule or lighter atom is less polarizable and has smaller dispersion forces because it has only a few, tightly held electrons. A larger molecule or heavier atom, however, is more polarizable and has larger dispersion forces because it has many electrons, some of which are less tightly held and are farther from the nucleus. Among the halogens, for instance, the $F_{2}$ molecule is small and less polarizable, while $\mathrm{I}_{2}$ is larger and more polarizable. As a result, $\mathrm{F}_{2}$ has smaller dispersion forces and is a gas at room temperature, while $\mathrm{I}_{2}$ has larger dispersion forces and is a solid (Table 10.3).

Shape is also important in determining the magnitude of the dispersion forces affecting a molecule. More spread-out shapes, which maximize molecular surface area, allow greater contact between molecules and give rise to higher dispersion forces than do more compact shapes, which minimize molecular contact. Pentane, for example, boils at 309.4 K , whereas 2,2-dimethylpropane boils at 282.7 K . Both substances have the same molecular formula, $\mathrm{C}_{5} \mathrm{H}_{12}$, but pentane is longer
and somewhat spread out, whereas 2,2-dimethylpropane is more spherical and compact (Figure 10.6).


(a) Pentane ( $\mathrm{bp}=309.4 \mathrm{~K}$ )


(b) 2,2-Dimethylpropane (bp $=282.7 \mathrm{~K})$

## Hydrogen Bonds

In many ways, hydrogen bonds are responsible for life on Earth. They cause water to be a liquid rather than a gas at ordinary temperatures, and they are the primary intermolecular force that holds huge biomolecules in the shapes needed to play their essential roles in biochemistry. Deoxyribonucleic acid (DNA), for instance, contains two long molecular strands coiled around each other and held together by hydrogen bonds.


A hydrogen bond is an attractive interaction between a hydrogen atom bonded to a very electronegative atom ( $\mathrm{O}, \mathrm{N}$, or F ) and an unshared electron pair on another electronegative atom. For example, hydrogen bonds occur in both water and ammonia:




FIGURE 10.6 (a) Longer, less compact molecules like pentane feel stronger dispersion forces and have consequently higher boiling points than (b) more compact molecules like 2,2-dimethylpropane.

## -

)John W. Hill, "A People-and Velcro Model for Hydrogen Bonding," J. Chem. Educ., Vol. 67, 1990, 223.

Hydrogen bonds arise because $\mathrm{O}-\mathrm{H}, \mathrm{N}-\mathrm{H}$, and $\mathrm{F}-\mathrm{H}$ bonds are highly polar, with a partial positive charge on the hydrogen and a partial negative charge on the electronegative atom. In addition, the hydrogen atom has no core electrons to shield its nucleus, and it has a small size, so it can be approached closely by other molecules. As a result, the dipole-dipole attraction between the hydrogen and an unshared electron pair on a nearby atom is unusually strong, giving rise to a hydrogen bond. Water, in particular, is able to form a vast three-dimensional network of hydrogen bonds because each $\mathrm{H}_{2} \mathrm{O}$ molecule has two hydrogens and two electron pairs (Figure 10.7).


- FIGURE 10.7 Liquid water contains a vast threedimensional network of hydrogen bonds resulting from the attraction between positively polarized hydrogens and electron pairs on negatively polarized oxygens. Each oxygen can form two hydrogen bonds, represented by dotted lines.

Hydrogen bonds can be quite strong, with energies up to $40 \mathrm{~kJ} / \mathrm{mol}$. To see one effect of hydrogen bonding, look at Table 10.4, which plots the boiling points of the covalent binary hydrides for the group 4A-7A elements. As you might expect, the boiling points generally increase with molecular mass down a group of the periodic table as a result of increased London dispersion forces-for example, $\mathrm{CH}_{4}<\mathrm{SiH}_{4}<\mathrm{GeH}_{4}<\mathrm{SnH}_{4}$. Three substances, however, are clearly anomalous: $\mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{O}$, and HF. All three have higher boiling points than might be expected, because of the hydrogen bonds they contain.

TABLE 10.4 Boiling Points of the Covalent Binary Hydrides of Groups 4A, 5A, 6A, and 7A

*The boiling points generally increase with increasing molecular mass down a group of the periodic table, but the hydrides of nitrogen $\left(\mathrm{NH}_{3}\right)$, oxygen $\left(\mathrm{H}_{2} \mathrm{O}\right)$, and fluorine (HF) have abnormally high boiling points because these molecules form hydrogen bonds.

A comparison of the various kinds of intermolecular forces discussed in this section is shown in Table 10.5.

TABLE 10.5 A Comparison of Intermolecular Forces

| Force | Strength | Characteristics |
| :--- | :--- | :--- |
| Ion-dipole | Moderate $(10-50 \mathrm{~kJ} / \mathrm{mol})$ | Occurs between ions and polar <br> solvents |
| Dipole-dipole | Weak $(3-4 \mathrm{~kJ} / \mathrm{mol})$ | Occurs between polar <br> molecules |
| London dispersion | Weak $(1-10 \mathrm{~kJ} / \mathrm{mol})$ | Occurs between all molecules; <br> strength depends on size, <br> polarizability |
| Hydrogen bond | Moderate $(10-40 \mathrm{~kJ} / \mathrm{mol})$ | Occurs between molecules <br> with O-H,N-H, and F-H <br> bonds |
|  |  | bon |

## Worked Example 10.3

Identify the likely kinds of intermolecular forces in the following substances:
(a) HCl
(b) $\mathrm{CH}_{3} \mathrm{CH}_{3}$
(c) $\mathrm{CH}_{3} \mathrm{NH}_{2}$
(d) Kr

## Strategy

Look at the structure of each substance, and decide what intermolecular forces are present. All molecules have dispersion forces; polar molecules have dipole-dipole forces; and molecules with $\mathrm{O}-\mathrm{H}, \mathrm{N}-\mathrm{H}$, or $\mathrm{F}-\mathrm{H}$ bonds have hydrogen bonds.

## Solution

(a) HCl is a polar molecule but can't form hydrogen bonds. It has dipole-dipole forces and dispersion forces.
(b) $\mathrm{CH}_{3} \mathrm{CH}_{3}$ is a nonpolar molecule and has only dispersion forces.
(c) $\mathrm{CH}_{3} \mathrm{NH}_{2}$ is a polar molecule that can form hydrogen bonds. In addition, it has dipole-dipole forces and dispersion forces.
(d) Kr is nonpolar and has only dispersion forces.

- PROBLEM 10.5 Of the substances $\mathrm{Ar}, \mathrm{Cl}_{2}, \mathrm{CCl}_{4}$, and $\mathrm{HNO}_{3}$, which has:
(a) The largest dipole-dipole forces?
(b) The largest hydrogen-bond forces?
(c) The smallest dispersion forces?

PROBLEM 10.6 Consider the kinds of intermolecular forces present in the following compounds, and rank the substances in likely order of increasing boiling point: $\mathrm{H}_{2} \mathrm{~S}(34 \mathrm{amu}), \mathrm{CH}_{3} \mathrm{OH}(32 \mathrm{amu}), \mathrm{C}_{2} \mathrm{H}_{6}(30 \mathrm{amu}), \mathrm{Ar}(40 \mathrm{amu})$.

## 10.3 | Some Properties of Liquids

Many familiar and observable properties of liquids can be explained by the intermolecular forces just discussed. We all know, for instance, that some liquids, such as water or gasoline, flow easily when poured, whereas others, such as motor oil or maple syrup, flow sluggishly.

The measure of a liquid's resistance to flow is called its viscosity. Not surprisingly, viscosity is related to the ease with which individual molecules move around in the liquid and thus to the intermolecular forces present. Substances with small nonpolar molecules, such as pentane and benzene, experience only weak intermolecular forces and have relatively low viscosities, whereas more

William M. Hemmerlin and Kenton Abel, "Viscosity Races," J. Chem. Educ., Vol. 68, 1991, 417.

Andrew J. Rosenthal, "Demonstration of Surface Tension," J. Chem. Educ., Vol. 78, 2001, 332-333.

Todd P. Silverstein, "Polarity, Miscibility, and Surface Tension of Liquids," J. Chem. Educ., Vol. 70, 1993, 253.

Lee R. Summerlin and James L. Ealy, Jr., "Surface Tension of Water: The Magic Touch," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), p. 45.

Bassam Z. Shakhashiri, "At the
Water's Edge: Surface Spreading and Surface Tension," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 301-304.


- Less viscous liquids like water flow freely when poured, while more viscous liquids like motor oil flow sluggishly.

- Surface tension allows a water strider to walk on a pond without penetrating the surface.

(1)Todd P. Silverstein, "Why Do Alcoholic Beverages Have Legs?" J. Chem. Educ., Vol. 75, 1998, 723-724.

Changes of State movie
polar substances, such as glycerol $\left[\mathrm{C}_{3} \mathrm{H}_{5}(\mathrm{OH})_{3}\right]$, experience stronger intermolecular forces and so have higher viscosities.

Another familiar property of liquids is surface tension, the resistance of a liquid to spread out and increase its surface area. Surface tension is caused by the difference in intermolecular forces experienced by molecules at the surface of a liquid and those experienced by molecules in the interior. Molecules at the surface feel attractive forces on only one side and are thus drawn in toward the liquid, while molecules in the interior are surrounded and are drawn equally in all directions (Figure 10.8). The ability of a water strider to walk on water and the beading up of water on a newly waxed car are both due to surface tension.


A FIGURE 10.8 Surface tension, which causes these drops of liquid mercury to form beads, is due to the different forces experienced by molecules in the interior of a liquid and those on the surface. Molecules on the surface feel attractive forces on only one side and are thus drawn in toward the liquid.

Surface tension, like viscosity, is generally higher in liquids that have stronger intermolecular forces. Both properties are also temperature-dependent because molecules at higher temperatures have more kinetic energy to counteract the attractive forces holding them together. Data for some common substances are given in Table 10.6. Note that mercury has a particularly large surface tension, causing droplets to form beads (Figure 10.8) and giving the top of the mercury column in a barometer a particularly rounded appearance.

TABLE 10.6 Viscosities and Surface Tensions of Some Common Substances at $20^{\circ} \mathrm{C}$

| Name | Formula | Viscosity <br> $\left(\mathbf{N} \cdot \mathbf{s} / \mathbf{m}^{\mathbf{2}}\right)$ | Surface Tension <br> $\left(\mathbf{J} / \mathbf{m}^{\mathbf{2}}\right)$ |
| :--- | :--- | :--- | :--- |
| Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | $2.4 \times 10^{-4}$ | $1.61 \times 10^{-2}$ |
| Benzene | $\mathrm{C}_{6} \mathrm{H}_{6}$ | $6.5 \times 10^{-4}$ | $2.89 \times 10^{-2}$ |
| Water | $\mathrm{H}_{2} \mathrm{O}$ | $1.00 \times 10^{-3}$ | $7.29 \times 10^{-2}$ |
| Ethanol | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ | $1.20 \times 10^{-3}$ | $2.23 \times 10^{-2}$ |
| Mercury | Hg | $1.55 \times 10^{-3}$ | $4.6 \times 10^{-1}$ |
| Glycerol | $\mathrm{C}_{3} \mathrm{H}_{5}(\mathrm{OH})_{3}$ | 1.49 | $6.34 \times 10^{-2}$ |

## 10.4 | Phase Changes

Solid ice melts to liquid water; liquid water freezes to solid ice or evaporates to gaseous steam; gaseous steam condenses to liquid water. Such processes, in which the physical form but not the chemical identity of a substance changes, are called phase changes, or changes of state. Matter in any one state, or phase, can change into either of the other two. Solids can even change directly into gases, as occurs when dry ice (solid $\left.\mathrm{CO}_{2}\right)$ sublimes. The names of the various phase changes are:

| Fusion (melting) | solid $\rightarrow$ liquid |
| :--- | :--- |
| Freezing | liquid $\rightarrow$ solid |
| Vaporization | liquid $\rightarrow$ gas |
| Condensation | gas $\rightarrow$ liquid |
| Sublimation | solid $\rightarrow$ gas |
| Deposition | gas $\rightarrow$ solid |

Like all naturally occurring processes, every phase change has associated with it a free-energy change, $\Delta G$. This free-energy change $\Delta G$ is made up of two contributions, an enthalpy part $(\Delta H)$ and a temperature-dependent entropy part $(T \Delta S)$, according to the equation $\Delta G=\Delta H-T \Delta S$ that we saw in Section 8.14. The enthalpy part is the heat flow associated with making or breaking the intermolecular attractions that hold liquids and solids together, while the entropy part is associated with the change in disorder or randomness between the various phases. Gases are more random and have more entropy than liquids, which in turn are more random and have more entropy than solids.

The melting of a solid to a liquid, the sublimation of a solid to a gas, and the vaporization of a liquid to a gas all involve a change from a less random phase to a more random one, and all absorb heat energy to overcome the intermolecular forces holding particles together. Thus, both $\Delta S$ and $\Delta H$ are positive for these phase changes. By contrast, the freezing of a liquid to a solid, the deposition of a gas to a solid, and the condensation of a gas to a liquid all involve a change from a more random phase to a less random one, and all release heat energy as intermolecular attractions increase to hold particles more tightly together. Thus, both $\Delta S$ and $\Delta H$ have negative values for these phase changes. The situations are summarized in Figure 10.9.


Let's look at the transitions of solid ice to liquid water and liquid water to vapor to see some examples of energy relationships during phase changes. For the melting, or fusion, of ice to water, $\Delta H=+6.01 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S=+22.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$; for the vaporization of water to steam, $\Delta H=+40.67 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S=+109 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. Both $\Delta H$ and $\Delta S$ are larger for the liquid $\rightarrow$ vapor change than for the solid $\rightarrow$ liquid change because many more intermolecular attractions need to be overcome and much more randomness is gained in the change of liquid to vapor. This highly endothermic conversion of liquid water to gaseous water vapor is used by many organisms as a cooling mechanism. When our bodies perspire on a warm day, evaporation of the perspiration absorbs heat and leaves the skin feeling cooler.

$\sqrt{ }$A phase change usually refers to what occurs when a solid, liquid, or gas is converted to one of the other two states. Sometimes more than one solid state exists for a substance, such as the metallic and nonmetallic forms of solid tin, and a phase change can occur between the two.

- FIGURE 10.9 Changes from a less random phase to a more random one have positive values of $\Delta H$ and $\Delta S$. Changes from a more random phase to a less random one have negative values of $\Delta H$ and $\Delta S$.


A Evaporation of perspiration carries away heat and cools the body after exertion.


A Why do citrus growers spray their trees with water on cold nights?

On a heating curve for a pure substance the temperature remains constant during a phase change. Within a given state, temperature rises with a slope that depends on the heat capacity of the substance in that state.


FIGURE 10.10 A heating curve for $\mathrm{H}_{2} \mathrm{O}$, showing the temperature changes and phase transitions that occur when heat is added. The plateau at $0^{\circ} \mathrm{C}$ represents the melting of solid ice, and the plateau at $100^{\circ} \mathrm{C}$ represents the boiling of liquid water.

For phase changes in the opposite direction, the numbers have the same absolute values but opposite signs. That is, $\Delta H=-6.01 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S=-22.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for the freezing of liquid water to ice, and $\Delta H=-40.67 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S=-109$ $\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})$ for the condensation of water vapor to liquid water. Citrus growers take advantage of the exothermic freezing of water when they spray their trees with water on cold nights to prevent frost damage. As water freezes on the leaves, it releases enough heat to protect the tree.

Knowing the values of $\Delta H$ and $\Delta S$ for a phase transition makes it possible to calculate the temperature at which the change occurs. Recall from Section 8.14 that $\Delta G$ is negative for a spontaneous process, positive for a nonspontaneous process, and zero for a process at equilibrium. Thus, by setting $\Delta G=0$ and solving for $T$ in the free-energy equation, we can calculate the temperature at which two phases are in equilibrium. For the solid $\rightarrow$ liquid phase change in water, for instance, we have

$$
\begin{aligned}
\Delta G & =\Delta H-T \Delta S=0 \quad \text { at equilibrium } \\
\text { or } \quad T & =\Delta H / \Delta S
\end{aligned}
$$

where $\Delta H=+6.01 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S=+22.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$

$$
\text { so } \quad T=\frac{6.01 \frac{\mathrm{~kJ}}{\mathrm{~mol}}}{0.0220 \frac{\mathrm{~kJ}}{\mathrm{~K} \cdot \mathrm{~mol}}}=273 \mathrm{~K}
$$

In other words, ice turns into liquid water, and liquid water turns into ice, at 273 K , or $0^{\circ} \mathrm{C}$, at 1 atm pressure-hardly a surprise. (In practice, the calculation is done in the opposite direction. That is, the temperature at which a phase change occurs is measured and then used to calculate $\Delta S$ for the process: $\Delta S=\Delta H / T$.)

The results of continuously adding heat to a substance can be displayed on a heating curve like that shown in Figure 10.10 for $\mathrm{H}_{2} \mathrm{O}$. Beginning with solid $\mathrm{H}_{2} \mathrm{O}$ at an arbitrary temperature, say $-25.0^{\circ} \mathrm{C}$, addition of heat raises the ice's temperature until it reaches $0^{\circ} \mathrm{C}$. Since the molar heat capacity of ice (Section 8.8 ) is $36.57 \mathrm{~J} /\left(\mathrm{mol} \cdot{ }^{\circ} \mathrm{C}\right)$, and since we need to raise the temperature $25.0^{\circ} \mathrm{C}, 914 \mathrm{~J} / \mathrm{mol}$ is required:

Energy to heat ice from $-25^{\circ} \mathrm{C}$ to $0^{\circ} \mathrm{C}=\left(36.57 \frac{\mathrm{~J}}{\mathrm{~mol} \cdot{ }^{\circ} \mathrm{C}}\right)\left(25.0^{\circ} \mathrm{C}\right)=914 \mathrm{~J} / \mathrm{mol}$


Once the temperature of the ice reaches $0^{\circ} \mathrm{C}$, addition of further heat goes into disrupting hydrogen bonds and other intermolecular forces rather than into increasing the temperature, as indicated by the plateau at $0^{\circ} \mathrm{C}$ on the heating curve in Figure 10.10. At this temperature-the melting point-solid and liquid coexist in equilibrium as molecules break free from their positions in the ice crystals and enter the liquid phase. Not until the solid turns completely to liquid does heat again cause the temperature to rise. The amount of energy required to overcome enough intermolecular forces to convert a solid into a liquid is the enthalpy of fusion, or heat of fusion, $\Delta H_{\text {fusion }}$. For ice, $\Delta H_{\text {fusion }}=+6.01 \mathrm{~kJ} / \mathrm{mol}$.

Continued addition of heat to liquid water raises the temperature until it reaches $100^{\circ} \mathrm{C}$. We can calculate from the molar heat capacity of liquid water [75.4 $\mathrm{J} /\left(\mathrm{mol} \cdot{ }^{\circ} \mathrm{C}\right)$ ] that $7.54 \mathrm{~kJ} / \mathrm{mol}$ is required:
Energy to heat water from $0^{\circ} \mathrm{C}$ to $100^{\circ} \mathrm{C}=\left(75.4 \frac{\mathrm{~J}}{\mathrm{~mol} \cdot{ }^{\circ} \mathrm{C}}\right)\left(100^{\circ} \mathrm{C}\right)=7.54 \times 10^{3} \mathrm{~J} / \mathrm{mol}$
Once the temperature of the water reaches $100^{\circ} \mathrm{C}$, addition of further heat again goes into overcoming intermolecular forces rather than into increasing the temperature, as indicated by the second plateau at $100^{\circ} \mathrm{C}$ on the heating curve. At this temperature-the boiling point-liquid and vapor coexist in equilibrium as molecules break free from the surface of the liquid and enter the gas phase. The amount of energy necessary to convert a liquid into a gas is called the enthalpy of vaporization, or heat of vaporization, $\Delta \boldsymbol{H}_{\text {vap }}$. For water, $\Delta H_{\text {vap }}=+40.67 \mathrm{~kJ} / \mathrm{mol}$. Only after the liquid has been completely vaporized does the temperature again rise.

Notice that the largest part ( $40.67 \mathrm{~kJ} / \mathrm{mol}$ ) of the $56.05 \mathrm{~kJ} / \mathrm{mol}$ required to convert solid ice at $-25^{\circ} \mathrm{C}$ to gaseous steam at $125^{\circ} \mathrm{C}$ is used for vaporization. The heat of vaporization for water is large because all the hydrogen bonds must be broken before molecules can escape from the liquid. Table 10.7 gives further data on both heat of fusion and heat of vaporization for some common compounds. Note that what is true for water is also true for other compounds: The heat of vaporization of a compound is always larger than its heat of fusion because almost all intermolecular forces must be overcome before vaporization can occur, but relatively fewer intermolecular forces must be overcome for a solid to change to a liquid.

| TABLE 10.7 | Heats of Fusion and Heats of Vaporization <br> for Some Common Compounds |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Name | Formula | $\boldsymbol{\Delta} \boldsymbol{H}_{\text {fusion }}$ <br> $\mathbf{( k J J / m o l )}$ | $\boldsymbol{\Delta} \boldsymbol{H}_{\text {vap }}$ <br> $\mathbf{( k J / m o l )}$ |
| Ammonia | $\mathrm{NH}_{3}$ | 5.97 | 23.4 |
| Benzene | $\mathrm{C}_{6} \mathrm{H}_{6}$ | 9.95 | 30.8 |
| Ethanol | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ | 5.02 | 38.6 |
| Helium | He | 0.02 | 0.10 |
| Mercury | Hg | 2.33 | 56.9 |
| Water | $\mathrm{H}_{2} \mathrm{O}$ | 6.01 | 40.67 |

## Worked Example 10.4

The boiling point of water is $100^{\circ} \mathrm{C}$, and the enthalpy change for the conversion of water to steam is $\Delta H_{\text {vap }}=40.67 \mathrm{~kJ} / \mathrm{mol}$. What is the entropy change for vaporization, $\Delta S_{\text {vap }}$, in $\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})$ ?

## Strategy

At the temperature where a phase change occurs, the two phases coexist in equilibrium and $\Delta G$, the free-energy difference between the phases, is zero: $\Delta \mathrm{G}=$ $\Delta H-T \Delta S=0$. Rearranging this equation gives $\Delta S=\Delta H / T$, where both $\Delta H$ and $T$ are known. Remember that $T$ must be expressed in kelvins.


- Because bromine is colored, it's possible to see its reddish vapor above the liquid.


## Solution

$$
\Delta S_{\text {vap }}=\frac{\Delta H_{\text {vap }}}{T}=\frac{40.67 \frac{\mathrm{~kJ}}{\mathrm{~mol}}}{373.15 \mathrm{~K}}=0.1090 \mathrm{~kJ} /(\mathrm{K} \cdot \mathrm{~mol})=109.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})
$$

As you might expect, there is a large positive entropy change, corresponding to a large increase in randomness, on converting water from a liquid to a gas.

- PROBLEM 10.7 Which of the following processes would you expect to have a positive value of $\Delta S$, and which a negative value?
(a) Sublimation of dry ice
(b) Formation of dew on a cold morning
(c) Mixing of cigarette smoke with air in a closed room
- PROBLEM 10.8 Chloroform has $\Delta H_{\text {vap }}=29.2 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S_{\text {vap }}=87.5$ $\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})$. What is the boiling point of chloroform in kelvins?


## 10.5 | Evaporation, Vapor Pressure, and Boiling Point

The conversion of a liquid to a vapor takes place in a visible way when the liquid boils, but it takes place under other conditions as well. Let's imagine the two experiments illustrated in Figure 10.11. In experiment (a), we place a liquid in an open container; in experiment (b), we place the liquid in a closed container connected to a mercury manometer (Section 9.1). After a certain amount of time has passed, the liquid in the first container has evaporated, while the liquid in the second container remains but the pressure has risen. At equilibrium and at a constant temperature, the pressure has a constant value called the vapor pressure of the liquid.


A FIGURE 10.11 Liquids after sitting for a length of time in (a) an open container and (b) a closed container. The liquid in the open container has evaporated, but the liquid in the closed container has brought about a rise in pressure.

Evaporation and vapor pressure are both explained on a molecular level by the kinetic-molecular theory developed in Section 9.6 to account for the behavior of gases. The molecules in a liquid are in constant motion, but at a variety of speeds depending on the amount of kinetic energy they have. In considering a large sample, molecular kinetic energies follow a distribution curve like that
shown in Figure 10.12. The exact shape of the curve depends on the temperature. The higher the temperature and the lower the boiling point of the substance, the greater the fraction of molecules in the sample that have sufficient kinetic energy to break free from the surface of the liquid and escape into the vapor.


Molecules that enter the vapor phase in an open container can escape the liquid and drift away until the liquid evaporates entirely, but molecules in a closed container are trapped. As more and more molecules pass from the liquid to the vapor, chances increase that random motion will cause some of them to return occasionally to the liquid. Ultimately, the number of molecules returning to the liquid and the number escaping become equal, at which point a dynamic equilibrium exists. Although individual molecules are constantly passing back and forth from one phase to the other, the total numbers of molecules in both liquid and vapor phases remain constant.

The numerical value of a liquid's vapor pressure depends on the magnitude of the intermolecular forces present and on the temperature. The smaller the intermolecular forces, the higher the vapor pressure because loosely held molecules escape more easily. The higher the temperature, the higher the vapor pressure because a larger fraction of molecules have sufficient kinetic energy to escape.

## The Clausius-Clapeyron Equation

As indicated by the plots in Figure 10.13a, the vapor pressure of a liquid rises with temperature in a nonlinear way. A linear relationship is found, however, when the logarithm of the vapor pressure, $\ln P_{\text {vap, }}$, is plotted against the inverse of the Kelvin temperature, $1 / T$. Table 10.8 gives the appropriate data for water, and Figure 10.13b shows the plot. As noted in Section 9.2, a linear graph is characteristic of mathematical equations of the form $y=m x+b$. In the present instance, $y=\ln P_{\text {vap }}, x=1 / T$, $m$ is the slope of the line ( $-\Delta H_{\text {vap }} / R$ ), and $b$ is the $y$-intercept (a constant, $C$ ). Thus, the data fit an expression known as the Clausius-Clapeyron equation:

Clausius-Clapeyron equation

$$
\begin{aligned}
\ln P_{\text {vap }} & =\left(-\frac{\Delta H_{\text {vap }}}{R}\right) \frac{1}{T}+C \\
\uparrow & \uparrow \uparrow \uparrow \\
y & =m \quad x+b
\end{aligned}
$$

where $\Delta H_{\text {vap }}$ is the heat of vaporization of the liquid, $R$ is the gas constant (Section 9.3), and $C$ is a constant characteristic of each specific substance.


Vapor Pressure vs. Temperature activity

FIGURE 10.12 The distribution of molecular kinetic energies in a liquid. Only the faster-moving molecules have sufficient kinetic energy to escape from the liquid and enter the vapor. The higher the temperature, the larger the number of molecules that have enough energy to escape.
J. A. Sears and C. J. Grieve, "A Vapor Pressure Demonstration," J. Chem. Educ., Vol. 67, 1990, 427. Hexane is introduced into a sealed Erlenmeyer flask containing hot water and fitted with a delivery tube. The hexane is vaporized by the hot water, forcing water from the flask into a graduated cylinder. As the flask cools, water is drawn back into the flask, showing that the vapor pressure of the hexane decreases with a decrease in temperature.


TABLE 10.8 Vapor Pressure of Water at Various Temperatures

| Temp <br> (K) | $\boldsymbol{P}_{\mathbf{v a p}}$ <br> $(\mathbf{m m} \mathbf{H g})$ | $\mathbf{l n} \boldsymbol{P}_{\mathbf{v a p}}$ | $\mathbf{1 / T}$ | Temp <br> (K) | $\boldsymbol{P}_{\mathbf{v a p}}$ <br> $\mathbf{( m m} \mathbf{H g})$ | $\mathbf{l n} \boldsymbol{P}_{\text {vap }}$ | $\mathbf{1 / T}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 273 | 4.58 | 1.522 | 0.00366 | 333 | 149.4 | 5.007 | 0.00300 |
| 283 | 9.21 | 2.220 | 0.00353 | 343 | 233.7 | 5.454 | 0.00292 |
| 293 | 17.5 | 2.862 | 0.00341 | 353 | 355.1 | 5.872 | 0.00283 |
| 303 | 31.8 | 3.459 | 0.00330 | 363 | 525.9 | 6.265 | 0.00275 |
| 313 | 55.3 | 4.013 | 0.00319 | 373 | 760.0 | 6.633 | 0.00268 |
| 323 | 92.5 | 4.527 | 0.00310 | 378 | 906.0 | 6.809 | 0.00265 |

FIGURE 10.13
(a) The vapor pressures of water, ethanol, and diethyl ether show a nonlinear rise when plotted as a function of temperature. (b) A plot of $\ln P_{\text {vap }}$ versus 1/T (Kelvin) for water, prepared from the data in Table 10.8, shows a linear relationship.


Lee R. Summerlin and James L. Ealy, Jr., "The Effect of Pressure on Boiling Point," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), p. 21.

© What is the vapor pressure of the liquid at its boiling point?

The Clausius-Clapeyron equation makes it possible to calculate the heat of vaporization of a liquid by measuring its vapor pressure at several temperatures and then plotting the results to obtain the slope of the line. Alternatively, once the heat of vaporization and the vapor pressure at one temperature are known, the vapor pressure of the liquid at any other temperature can be calculated, as shown in Worked Example 10.5.

When the vapor pressure of a liquid rises to the point where it becomes equal to the external pressure, the liquid changes completely into vapor and the liquid boils. On a molecular level, you might picture boiling in the following way: Imagine that a few molecules in the interior of the liquid momentarily break free from their neighbors and form a microscopic bubble. If the external pressure from the atmosphere is greater than the vapor pressure inside the bubble, the bubble is immediately crushed. At the temperature where the external pressure and the vapor pressure in the bubble are the same, however, the bubble is not crushed. Instead, it rises through the denser liquid, grows larger as more molecules join it, and appears as part of the vigorous action we associate with boiling.

The temperature at which boiling occurs when the external pressure is exactly 1 atm is called the normal boiling point of the liquid. On the plots in Figure 10.13a, the normal boiling points of the three liquids are reached when the curves cross the dashed line representing 760 mm Hg -for ether, $34.6^{\circ} \mathrm{C}$ (307.8 K); for ethanol, $78.3^{\circ} \mathrm{C}$ ( 351.5 K ); and for water, $100.0^{\circ} \mathrm{C}$ ( 373.15 K ).

If the external pressure is less than 1 atm , then the vapor pressure necessary for boiling is reached earlier than 1 atm and the liquid boils at a lower than normal temperature. On top of Mt. Everest, for example, where the atmospheric pressure is only about 260 mm Hg , water boils at approximately $71^{\circ} \mathrm{C}$. Conversely, if the external pressure on a liquid is greater than 1 atm , the vapor pressure necessary for boiling is reached later and the liquid boils at a greater than normal temperature. Pressure cookers take advantage of this effect by causing water to boil at a higher temperature, thereby allowing food to cook more rapidly.

## Worked Example 10.5

The vapor pressure of ethanol at $34.7^{\circ} \mathrm{C}$ is 100.0 mm Hg , and the heat of vaporization of ethanol is $38.6 \mathrm{~kJ} / \mathrm{mol}$. What is the vapor pressure of ethanol (in millimeters of mercury) at $65.0^{\circ} \mathrm{C}$ ?

## Strategy

There are several ways to do this problem. One way is to use the vapor pressure at $T=307.9 \mathrm{~K}\left(34.7^{\circ} \mathrm{C}\right)$ to find a value for $C$ in the Clausius-Clapeyron equation. You could then use that value to solve for $\ln P_{\text {vap }}$ at $T=338.2 \mathrm{~K}\left(65.0^{\circ} \mathrm{C}\right)$.

Alternatively, because $C$ is a constant, its value is the same at any two pressures and temperatures. That is:

$$
C=\ln P_{1}+\frac{\Delta H_{\mathrm{vap}}}{R T_{1}}=\ln P_{2}+\frac{\Delta H_{\mathrm{vap}}}{R T_{2}}
$$

This equation can be rearranged to solve for the desired quantity, $\ln P_{2}$ :

$$
\ln P_{2}=\ln P_{1}+\left(\frac{\Delta H_{\mathrm{vap}}}{R}\right)\left(\frac{1}{T_{1}}-\frac{1}{T_{2}}\right)
$$

where $P_{1}=100.0 \mathrm{~mm} \mathrm{Hg}$ and $\ln P_{1}=4.6052, \Delta H_{\text {vap }}=38.6 \mathrm{~kJ} / \mathrm{mol}, R=8.3145$ $\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol}), T_{2}=338.2 \mathrm{~K}\left(65.0^{\circ} \mathrm{C}\right)$, and $T_{1}=307.9 \mathrm{~K}\left(34.7^{\circ} \mathrm{C}\right)$.

## Solution

$$
\begin{aligned}
& \ln P_{2}=4.6052+\left(\frac{38,600 \frac{\mathrm{~J}}{\mathrm{~mol}}}{8.3145 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}}\right)\left(\frac{1}{307.9 \mathrm{~K}}-\frac{1}{338.2 \mathrm{~K}}\right) \\
& \ln P_{2}=4.6052+1.3509=5.9561 \\
& P_{2}=\operatorname{antiln}(5.9561)=386.1 \mathrm{~mm} \mathrm{Hg}
\end{aligned}
$$

Antilogarithms are reviewed in Appendix A.2.

## Worked Example 10.6

Ether has $P_{\text {vap }}=400 \mathrm{~mm} \mathrm{Hg}$ at $17.9^{\circ} \mathrm{C}$ and a normal boiling point of $34.6^{\circ} \mathrm{C}$. What is the heat of vaporization, $\Delta H_{\text {vap }}$, for ether in kilojoules per mole?

## Strategy

The heat of vaporization, $\Delta H_{\text {vap }}$, of a liquid can be obtained either graphically from the slope of a plot of $\ln P_{\text {vap }}$ versus $1 / T$, or algebraically from the Clausius-Clapeyron equation. As derived in Worked Example 10.5,

$$
\ln P_{2}=\ln P_{1}+\left(\frac{\Delta H_{\mathrm{vap}}}{R}\right)\left(\frac{1}{T_{1}}-\frac{1}{T_{2}}\right)
$$

which can be solved for $\Delta H_{\text {vap }}$ :

$$
\Delta H_{\mathrm{vap}}=\frac{\left(\ln P_{2}-\ln P_{1}\right)(R)}{\left(\frac{1}{T_{1}}-\frac{1}{T_{2}}\right)}
$$

where $P_{1}=400 \mathrm{~mm} \mathrm{Hg}$ and $\ln P_{1}=5.991, P_{2}=760 \mathrm{~mm} \mathrm{Hg}$ at the normal boiling point and $\ln P_{2}=6.633, R=8.3145 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol}), T_{1}=291.1 \mathrm{~K}\left(17.9^{\circ} \mathrm{C}\right)$, and $T_{2}=$ $307.8 \mathrm{~K}\left(34.6^{\circ} \mathrm{C}\right)$.

## Solution

$$
\Delta H_{\text {vap }}=\frac{(6.633-5.991)\left(8.3145 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)}{\frac{1}{291.1 \mathrm{~K}}-\frac{1}{307.8 \mathrm{~K}}}=28,600 \mathrm{~J} / \mathrm{mol}=28.6 \mathrm{~kJ} / \mathrm{mol}
$$

- PROBLEM 10.9 The normal boiling point of benzene is $80.1^{\circ} \mathrm{C}$, and the heat of vaporization is $\Delta H_{\text {vap }}=30.8 \mathrm{~kJ} / \mathrm{mol}$. What is the boiling point of benzene (in ${ }^{\circ} \mathrm{C}$ ) on top of Mt. Everest, where $P=260 \mathrm{~mm} \mathrm{Hg}$ ?
- PROBLEM 10.10 Bromine has $P_{\text {vap }}=400 \mathrm{~mm}$ at $41.0^{\circ} \mathrm{C}$ and a normal boiling point of 331.9 K . What is the heat of vaporization, $\Delta H_{\text {vap, }}$, of bromine in kilojoules per mole?


## 10.6 | Kinds of Solids

It's obvious from a brief look around that most substances are solids rather than liquids or gases. It's also obvious that there are many different kinds of solids. Some solids, such as iron and aluminum, are hard and metallic; others, such as sugar and table salt, are crystalline and easily broken; and still others, such as rubber and many plastics, are soft and amorphous.

The most fundamental distinction between kinds of solids is that some are crystalline and others are amorphous. Crystalline solids are those whose atoms, ions, or molecules have an ordered arrangement extending over a long range. This order on the atomic level is also seen on the visible level because crystalline solids usually have flat faces and distinct angles (Figure 10.14a). Amorphous solids, by contrast, are those whose constituent particles are randomly arranged and have no ordered long-range structure (Figure 10.14b). Rubber is an example.


Crystalline solids can be further categorized as ionic, molecular, covalent network, or metallic. Ionic solids are those like sodium chloride, whose constituent particles are ions. A crystal of sodium chloride is composed of alternating $\mathrm{Na}^{+}$ and $\mathrm{Cl}^{-}$ions ordered in a regular three-dimensional arrangement and held together by ionic bonds, as discussed in Section 6.6. Molecular solids are those like sucrose or ice, whose constituent particles are molecules held together by the intermolecular forces discussed in Section 10.2. A crystal of ice, for example, is composed of $\mathrm{H}_{2} \mathrm{O}$ molecules held together in a regular way by hydrogen bonding (Figure 10.15a). Covalent network solids are those like quartz (Figure 10.15b) or diamond, whose atoms are linked together by covalent bonds into a giant threedimensional array. In effect, a covalent network solid is one very large molecule.


Metallic solids, such as silver or iron, also consist of large arrays of atoms, but their crystals have metallic properties such as electrical conductivity. We'll discuss metals in Chapter 21.

A summary of the different types of crystalline solids and their characteristics is given in Table 10.9.

TABLE 10.9 Types of Crystalline Solids and Their Characteristics

| Type of Solid | Intermolecular <br> Forces | Properties | Examples |
| :--- | :--- | :--- | :--- |
| Ionic | Ion-ion forces | Brittle, hard, <br> high-melting <br> Soft, low-melting, <br> nonconducting | $\mathrm{NaCl}^{2}, \mathrm{KBr}$, <br> $\mathrm{MgCl}_{2}$ <br> $\mathrm{H}_{2} \mathrm{O}, \mathrm{Br}_{2}$, <br> $\mathrm{CO}_{2}, \mathrm{CH}_{4}$ |
| Molecular | Dispersion forces, <br> dipole-dipole <br> forces, hydrogen <br> bonds | Hard, high-melting | C (diamond, <br> graphite), <br> $\mathrm{SiO}_{2}$ |
| Covalent network | Covalent bonds | $\mathrm{Na}, \mathrm{Zn}, \mathrm{Cu}, \mathrm{Fe}$ |  |

## 10.7 | Probing the Structure of Solids: X-Ray Crystallography

According to a fundamental principle of optics, the wavelength of light used to observe an object must be smaller than the object itself. Since atoms have diame-
ters of around $2 \times 10^{-10} \mathrm{~m}$ and the visible light detected by our eyes has waveobserve an object must be smaller than the object itself. Since atoms have diame-
ters of around $2 \times 10^{-10} \mathrm{~m}$ and the visible light detected by our eyes has wavelengths of $4-7 \times 10^{-7} \mathrm{~m}$, it is impossible to see atoms using even the finest optical microscope. To "see" atoms, we must use "light" with a wavelength of approximately $10^{-10} \mathrm{~m}$, which is in the X-ray region of the electromagnetic spectrum (Section 5.2).

A FIGURE 10.15 Crystal structures of (a) ice, a molecular solid, and (b) quartz, a covalent network solid. Ice consists of individual $\mathrm{H}_{2} \mathrm{O}$ molecules held together in a regular manner by hydrogen bonds. Quartz ( $\mathrm{SiO}_{2}$ ) is essentially one very large molecule whose Si and O atoms are linked by covalent bonds. Each silicon atom has tetrahedral geometry and is bonded to four oxygens; each oxygen has approximately linear geometry and is bonded to two silicons. The shorthand representation on the right shows how $\mathrm{SiO}_{4}$ tetrahedra join at their corners to share oxygen atoms.

FIGURE 10.16 An X-ray diffraction experiment. A beam of $X$ rays is passed through a crystal and allowed to strike a photographic film. The rays are diffracted by atoms in the crystal, giving rise to a regular pattern of spots on the film.

FIGURE 10.17 Interference of electromagnetic waves. (a) Constructive interference occurs if the waves are in-phase and produces a wave with increased intensity. (b) Destructive interference occurs if the waves are out-of-phase and results in cancellation.

The origins of X-ray crystallography go back to the work of Max von Laue in 1912. On passing $X$ rays through a crystal of sodium chloride and letting them strike a photographic plate, Laue noticed that a pattern of spots was produced on the plate, indicating that the $X$ rays were being diffracted by the atoms in the crystal. A typical diffraction pattern is shown in Figure 10.16.


Diffraction of electromagnetic radiation occurs when a beam is scattered by an object containing regularly spaced lines (such as those in a diffraction grating) or points (such as the atoms in a crystal). This scattering can happen only if the spacing between the lines or points is comparable to the wavelength of the radiation. As shown schematically in Figure 10.17, diffraction is due to interference between two waves passing through the same region of space at the same time. If the waves are in-phase, peak to peak and trough to trough, the interference is constructive and the combined wave is increased in intensity. If the waves are out-of-phase, however, the interference is destructive and the wave is canceled. Constructive interference gives rise to the intense spots observed on Laue's photographic plate, while destructive interference causes the surrounding light areas.


How does the diffraction of $X$ rays by atoms in a crystal give rise to the observed pattern of spots on a photographic plate? According to an explanation advanced in 1913 by the English physicist William H. Bragg and his 22-year-old son William L. Bragg, the $X$ rays are diffracted by different layers of atoms in the crystal, leading to constructive interference in some instances but destructive interference in others.

To understand the Bragg analysis, imagine that incoming $X$ rays with wavelength $\lambda$ strike a crystal face at an angle $\theta$ and then bounce off at the same angle, just as light bounces off a mirror (Figure 10.18). Those rays that strike an atom in the top layer are reflected at the same angle $\theta$, and those rays that strike an atom in the second layer are also reflected at the angle $\theta$. But because the second layer of atoms is farther from the X -ray source, the distance that the $X$ rays have to travel to reach the second layer is farther than the distance they have to travel to reach the first layer by an amount indicated as $B C$ in Figure 10.18. Using trigonometry, you can show that the extra distance $B C$ is equal to the distance between atomic layers $d(=A C)$ times the sine of the angle $\theta$ :

$$
\sin \theta=\frac{B C}{d} \quad \text { so } \quad B C=d \sin \theta
$$



Of course, the extra distance $B C=C B^{\prime}$ must also be traveled again by the reflected rays as they exit the crystal, making the total extra distance traveled equal to $2 d \sin \theta$.

$$
B C+C B^{\prime}=2 d \sin \theta
$$

The key to the Bragg analysis is the realization that the different rays striking the two layers of atoms are in-phase initially but can be in-phase after reflection only if the extra distance $B C+C B^{\prime}$ is equal to a whole number of wavelengths $n \lambda$, where $n$ is an integer $(1,2,3, \ldots)$. If the extra distance is not a whole number of wavelengths, then the reflected rays will be out-of-phase and will cancel. Setting the extra distance $2 d \sin \theta=n \lambda$ and rearranging to solve for $d$ gives the Bragg equation:

$$
B C+C B^{\prime}=2 d \sin \theta=n \lambda
$$

- BRAGG EQUATION $d=\frac{n \lambda}{2 \sin \theta}$

Of the variables in the Bragg equation, the value of the wavelength $\lambda$ is known, the value of $\sin \theta$ can be measured, and the value of $n$ is a small integer, usually assumed to be 1 . Thus, the distance $d$ between layers of atoms in a crystal can be calculated. For their work, the Braggs shared the 1915 Nobel Prize in physics; the younger Bragg was 25 at the time.

Computer-controlled X-ray diffractometers are now available that automatically rotate a crystal and measure the diffraction from all angles. Analysis of the X-ray diffraction pattern then makes it possible to measure the interatomic distance between any two atoms in a crystal. For molecular substances, this knowledge of interatomic distances indicates which atoms are close enough to form a bond. X-ray analysis thus provides a means for determining the structures of molecules (Figure 10.19).

## re

FIGURE 10.18 Diffraction of $X$ rays of wavelength $\lambda$ from atoms in the top two layers of a crystal. Rays striking atoms in the second layer travel a distance equal to $B C+C B^{\prime}$ farther than rays striking atoms in the first layer. If this distance is a whole number of wavelengths, the reflected rays are in-phase and interfere constructively. Knowing the angle $\theta$ then makes it possible to calculate the distance $d$ between the layers.

$\square$The variable $n$ in the Bragg equation is the order of diffraction. After a rainfall, double or triple rainbows are sometimes observed with each successive rainbow fainter than the previous one. Tthe most intense spectrum is due to a first-order diffraction. The fainter spectra are due to higher orders of diffraction.

FIGURE 10.19 A computer-generated structure of adenosine triphosphate (ATP), the biological molecule that has been called "the energy currency of the living cell," as determined by X-ray crystallography.

Keenan E. Dungey, George Lisensky, and S. Michael Condren, "Kixium Monolayers: A Simple Alternative to the Bubble Raft Model for Close-Packed Spheres," J. Chem. Educ., Vol. 76, 1999, 618-619.

Daryl L. Ostercamp, "Close Packing of Identical Spheres," J. Chem. Educ., Vol. 69, 1992, 162.

FIGURE 10.20 (a) In simple cubic packing, all the layers are identical and all atoms are lined up in stacks and rows. Each sphere is touched by six neighbors, four in the same layer, one directly above, and one directly below. (b) In bodycentered cubic packing, the spheres in layer $a$ are separated slightly and the spheres in layer $b$ are offset so that they fit into the depressions between atoms in layer $a$. The third layer is a repeat of the first. Each sphere is touched by eight neighbors, four in the layer below and four in the layer above.


### 10.8 Unit Cells and the Packing of Spheres in Crystalline Solids

How do particles-whether atoms, ions, or molecules-pack together in crystals? Let's look at metals, which are the simplest examples of crystal packing because the individual atoms can be treated as spheres. Not surprisingly, metal atoms (and other kinds of particles as well) generally pack together in crystals so that they can be as close as possible and maximize intermolecular attractions.

If you were to take a large number of uniformly sized marbles and arrange them in a box in some orderly way, there are four possibilities you might come up with. One way to arrange the marbles is in orderly rows and stacks, with the spheres in one layer sitting directly on top of those in the previous layer so that all layers are identical (Figure 10.20a). Called simple cubic packing, each sphere is touched by six neighbors-four in its own layer, one above, and one below-and is thus said to have a coordination number of 6 . Only $52 \%$ of the available volume is occupied by the spheres in simple cubic packing, making inefficient use of space and minimizing attractive forces. Of all the metals in the periodic table, only polonium crystallizes in this way.


Alternatively, space could be used more efficiently if, instead of stacking the spheres directly on top of one another, you slightly separate the spheres in a given layer and offset alternating layers in an $a-b-a-b$ arrangement so that the spheres in the $b$ layers fit into the depressions between spheres in the $a$ layers, and vice versa
(Figure 10.20b). Called body-centered cubic packing, each sphere has a coordination number of 8-four neighbors above and four below-and space is used quite efficiently: $68 \%$ of the available volume is occupied. Iron, sodium, and 14 other metals crystallize in this way.

The remaining two packing arrangements of spheres are both said to be closestpacked. The hexagonal closest-packed arrangement (Figure 10.21a) has two alternating layers, $a-b-a-b$. Each layer has a hexagonal arrangement of touching spheres, which are offset so that spheres in a $b$ layer fit into the small triangular depressions between spheres in an $a$ layer. Zinc, magnesium, and 19 other metals crystallize in this way.


The cubic closest-packed arrangement (Figure 10.21b) has three alternating layers, $a-b-c-a-b-c$. The $a-b$ layers are identical to those in the hexagonal closestpacked arrangement, but the third layer is offset from both $a$ and $b$ layers. Silver, copper, and 16 other metals crystallize with this arrangement.

In both kinds of closest-packed arrangements, each sphere has a coordination number of 12 -six neighbors in the same layer, three above, and three below-and $74 \%$ of the available volume is filled. The next time you're in a grocery store, look to see how the oranges are stacked in their display box. Chances are good they'll have a closest-packed arrangement.

## Unit Cells

Having now taken a bulk view of how spheres can pack in a crystal, let's also take a close-up view. Just as a large wall might be made up of many identical bricks

vStudents tend to consider the center atom of a bodycentered cubic cell as different from the corner atoms. All atoms in the unit cell are identical. The unit cell can be reconfigured so that the atom originally in the center is positioned on a corner and vice versa.

FIGURE 10.21 (a) In hexagonal closest-packing, there are two alternating hexagonal layers, $a$ and $b$, offset from each other so that the spheres in one layer sit in the small triangular depressions of neighboring layers. (b) In cubic closest-packing, there are three alternating hexagonal layers, $a$, $b$, and $c$, offset from one another so that the spheres in one layer sit in the small triangular depressions of neighboring layers. In both kinds of closest-packing, each sphere is touched by 12 neighbors, 6 in the same layer, 3 in the layer above, and 3 in the layer below.


Close Packing movie; Close Packing activity


A What kind of packing arrangement do these oranges have?


- Just as this wall is made of many bricks stacked together in a regular way, a crystal is made of many small repeating units called unit cells.


## Sodium 3D model

$\sqrt{ }$
Primative cubic is also known as simple cubic.

VAtoms that belong to more than one unit cell are classified as corner, edge, or face atoms, which contribute, respectively, $1 / 8,1 / 4,1 / 2$ atom per unit cell.

vVisualizing threedimensional unit cells is difficult for many students. It is helpful to introduce the unit cell using a two-dimensional analog, such as a square array and a closest packed array of pennies laid flat on a table. The number of pennies per unit cell, the coordination number of each penny, and the percent empty space can be determined.

Frank Galasso, "The Importance of Understanding Structure," J. Chem. Educ., Vol. 70, 1993, 287-290. A discussion of the relationship between unit cells and the structure of solids.

stacked together in a repeating pattern, a crystal is made up of many small repeat units called unit cells stacked together in three dimensions.

Fourteen different unit-cell geometries occur in crystalline solids. All are par-allelepipeds-six-sided geometric solids whose faces are parallelograms. We'll be concerned here only with those unit cells that have cubic symmetry; that is, cells whose edges are equal in length and whose angles are $90^{\circ}$.

There are three kinds of cubic unit cells: primitive-cubic, body-centered cubic, and face-centered cubic. As shown in Figure 10.22a, a primitive-cubic unit cell for a metal has an atom at each of its eight corners, where it is shared with seven neighboring cubes that come together at the same point. As a result, only $1 / 8$ of each corner atom "belongs to" a given cubic unit. This primitive-cubic unit cell, with all atoms arranged in orderly rows and stacks, is the repeat unit found in simple cubic packing.


A FIGURE 10.22 Geometries of (a) primitive-cubic and (b) body-centered cubic unit cells in both a skeletal view (top) and a space-filling view (bottom). Part (c) shows how eight primitive-cubic unit cells stack together to share a common corner.

A body-centered cubic unit cell has eight corner atoms plus an additional atom in the center of the cube (Figure 10.22b). This body-centered cubic unit cell, with two repeating offset layers and with the spheres in a given layer slightly separated, is the repeat unit found in body-centered cubic packing.

A face-centered cubic unit cell has eight corner atoms plus an additional atom on each of its six faces, where it is shared with one other neighboring cube (Figure 10.23). Thus, $1 / 2$ of each face atom belongs to a given unit cell. This face-centered cubic unit cell is the repeat unit found in cubic closest-packing, as can be seen by looking down the body diagonal of a unit cell (Figure 10.23b). The faces of the unit-cell cube are at $54.7^{\circ}$ angles to the layers of the atoms.

A summary of stacking patterns, coordination numbers, amount of space used, and unit cells for the four kinds of packing of spheres is given in Table 10.10. Hexagonal closest-packing is the only one of the four that has a noncubic unit cell.

(a)

(b)

FIGURE 10.23 (a) Geometry of a face-centered cubic unit cell, and (b) a view down a body diagonal showing how this unit cell is found in cubic closest-packing. The faces are tilted at $54.7^{\circ}$ angles to the three repeating atomic layers.

TABLE 10.10 Summary of the Four Kinds of Packing for Spheres

| Structure | Stacking <br> Pattern | Coordination <br> Number | Space <br> Used (\%) | Unit <br> Cell |
| :--- | :--- | :--- | :--- | :--- |
| Simple cubic | $a-a-a-a-$ | 6 | 52 | Primitive cubic |
| Body-centered cubic | $a-b-a-b-$ | 8 | 68 | Body-centered cubic |
| Hexagonal closest-packed | $a-b-a-b-$ | 12 | 74 | (Noncubic) |
| Cubic closest-packed | $a-b-c-a-b-c-$ | 12 | 74 | Face-centered cubic |

## Worked Example 10.7

How many atoms are in one primitive-cubic unit cell of a metal?

## Strategy and Solution

As shown in Figure 10.22a, there is an atom at each of the eight corners of the primitive-cubic unit cell. When unit cells are stacked together, each corner atom is shared by eight cubes, so that only $1 / 8$ of each atom "belongs" to a given unit cell. Thus there is $1 / 8 \times 8=1$ atom per unit cell.

## Worked Example 10.8

Silver metal crystallizes in a cubic closest-packed arrangement with the edge of the unit cell having a length $d=407 \mathrm{pm}$. What is the radius (in picometers) of a silver atom?

## Strategy and Solution

Cubic closest-packing uses a face-centered cubic unit cell. Looking at any one face of the cube head-on shows that the face atoms touch the corner atoms along the diagonal

VWhen determining the density of a metal, students sometimes use the volume of the atoms instead of the volume of the entire unit cell. The density of a substance includes the empty space between atoms.
of the face but that corner atoms do not touch one another along the edges. Each diagonal is therefore equal to four atomic radii, $4 r$ :


Because the diagonal and two edges of the cube form a right triangle, we can use the Pythagorean theorem to set the sum of the squares of the two edges equal to the square of the diagonal, $d^{2}+d^{2}=(4 r)^{2}$, and then solve for $r$, the radius of one atom:

$$
\begin{gathered}
d^{2}+d^{2}=(4 r)^{2} \\
2 d^{2}=16 r^{2} \text { and } r^{2}=\frac{d^{2}}{8} \\
\text { thus } r=\sqrt{\frac{d^{2}}{8}}=\sqrt{\frac{(407 \mathrm{pm})^{2}}{8}}=144 \mathrm{pm}
\end{gathered}
$$

The radius of a silver atom is 144 pm .

## Worked Example 10.9

Nickel has a face-centered cubic unit cell with a length of 352.4 pm along an edge. What is the density of nickel in $\mathrm{g} / \mathrm{cm}^{3}$ ?

## Strategy

Density is mass divided by volume. The mass of a single unit cell can be calculated by counting the number of atoms in the cell and multiplying by the mass of a single atom. The volume of a single cubic unit cell with edge $d$ is $d^{3}=\left(3.524 \times 10^{-8} \mathrm{~cm}\right)^{3}=$ $4.376 \times 10^{-23} \mathrm{~cm}^{3}$.

## Solution

Each of the eight corner atoms in a face-centered cubic unit cell is shared by eight unit cells, so that only $1 / 8 \times 8=1$ atom belongs to a single cell. In addition, each of the six face atoms is shared by two unit cells, so that $1 / 2 \times 6=3$ atoms belong to a single cell. Thus, a single cell has 1 corner atom and 3 face atoms, for a total of 4 , and each atom has a mass equal to the molar mass of nickel ( $58.69 \mathrm{~g} / \mathrm{mol}$ ) divided by Avogadro's number $\left(6.022 \times 10^{23}\right.$ atoms $\left./ \mathrm{mol}\right)$. We can now calculate the density:

$$
\text { Density }=\frac{\text { Mass }}{\text { Volume }}=\frac{(4 \text { atoms })\left(\frac{58.69 \frac{\mathrm{~g}}{\mathrm{~mol}}}{6.022 \times 10^{23} \frac{\mathrm{atoms}}{\mathrm{~mol}}}\right)}{4.376 \times 10^{-23} \mathrm{~cm}^{3}}=8.909 \mathrm{~g} / \mathrm{cm}^{3}
$$

The calculated density of nickel is $8.909 \mathrm{~g} / \mathrm{cm}^{3}$. (The measured value is $8.90 \mathrm{~g} / \mathrm{cm}^{3}$.)

## Worked Key Concept Example 10.10

Imagine a tiled floor in the following pattern. Identify the smallest repeating rectangular unit, analogous to a two-dimensional unit cell.


## Strategy

Using trial and error, the idea is to draw two perpendicular sets of parallel lines that define a repeating rectangular unit. There may be more than one possibility.

## SOlUTION



- PROBLEM 10.11 How many atoms are in the following?
(a) One body-centered cubic unit cell of a metal
(b) One face-centered cubic unit cell of a metal
- PROBLEM 10.12 Polonium metal crystallizes in a simple cubic arrangement, with the edge of a unit cell having a length $d=334 \mathrm{pm}$. What is the radius (in picometers) of a polonium atom?
- PROBLEM 10.13 What is the density of polonium (Problem 10.12) in $\mathrm{g} / \mathrm{cm}^{3}$ ?
- KEY CONCEPT PROBLEM 10.14 Imagine a tiled floor in the following pattern. Identify the smallest repeating unit, analogous to a two-dimensional unit cell.



### 10.9 Structures of Some Ionic Solids

Simple ionic solids such as NaCl and KBr are like metals in that the individual ions are spheres that pack together in a regular way. They differ from metals, however, in that the spheres are not all the same size-anions are generally larger than cations (Section 6.2). As a result, ionic solids adopt a variety of different unit cells, depending on the size and charge of the ions. $\mathrm{NaCl}, \mathrm{KCl}$, and a number of other

## -



Cesium Chloride 3D model

FIGURE 10.24 The unit cell of NaCl in both (a) a skeletal view and (b) a space-filling view in which one face of the unit cell is viewed head-on. The larger chloride anions adopt a face-centered cubic unit cell, with the smaller sodium cations fitting into the holes between adjacent anions.

$\square$The ratio of cations to anions in a unit cell must be consistent with the empirical formula of the ionic compound, as predicted in Chapter 6 .

James P. Birk, "A Model to Illustrate the Brittleness of Ionic and Metallic Crystals," J. Chem. Educ., Vol. 62, 1985, 667.

FIGURE 10.25 Unit cells of (a) CuCl and (b) $\mathrm{BaCl}_{2}$. Both are based on a face-centered cubic arrangement of one ion, with the other ion tetrahedrally surrounded in holes. In CuCl , only alternating holes are filled, while in $\mathrm{BaCl}_{2}$, all holes are filled.
salts have a face-centered cubic unit cell in which the larger $\mathrm{Cl}^{-}$anions occupy corners and faces, while the smaller $\mathrm{Na}^{+}$cations fit into the holes between adjacent anions (Figure 10.24).


It's necessary, of course, that the unit cell of an ionic substance be electrically neutral, with equal numbers of positive and negative charges. In the NaCl unit cell, for instance, there are four $\mathrm{Cl}^{-}$anions $(1 / 8 \times 8=1$ corner atom, plus $1 / 2 \times 6=3$ face atoms) and also four $\mathrm{Na}^{+}$cations $(1 / 4 \times 12=3$ edge atoms, plus 1 center atom). (Remember that each corner atom in a cubic unit cell is shared by eight cells, each face atom is shared by two cells, and each edge atom is shared by four cells.)

Two other common ionic unit cells are shown in Figure 10.25. Copper(I) chloride has a face-centered cubic arrangement of the larger $\mathrm{Cl}^{-}$anions, with the

(a)

smaller $\mathrm{Cu}^{+}$cations in holes so that each is surrounded by a tetrahedron of four anions. Barium chloride, by contrast, has a face-centered cubic arrangement of the smaller $\mathrm{Ba}^{2+}$ cations, with the larger $\mathrm{Cl}^{-}$anions surrounded tetrahedrally. As required for charge neutrality, there are twice as many $\mathrm{Cl}^{-}$anions as $\mathrm{Ba}^{2+}$ cations.

- PROBLEM 10.15 Count the numbers of + and - charges in the CuCl and $\mathrm{BaCl}_{2}$ unit cells (Figure 10.25), and show that both cells are electrically neutral.

KEY CONCEPT PROBLEM 10.16 Rhenium oxide crystallizes in the following cubic unit cell:

(a) How many rhenium atoms and how many oxygen atoms are in each unit cell?
(b) What is the formula of rhenium oxide?
(c) What is the oxidation state of rhenium?
(d) What is the geometry around each oxygen atom?
(e) What is the geometry around each rhenium atom?

### 10.10 Structures of Some Covalent Network Solids

## Carbon

Carbon exists in more than 40 known structural forms, or allotropes, several of which are crystalline but most of which are amorphous. Graphite, the most common allotrope of carbon and the most stable under normal conditions, is a crystalline covalent network solid that consists of two-dimensional sheets of fused six-membered rings (Figure 10.26a). Each carbon atom is $s p^{2}$-hybridized and is connected to three other carbons. The diamond form of elemental carbon is a covalent network solid in which each carbon atom is $s p^{3}$-hybridized and is bonded with tetrahedral geometry to four other carbons (Figure 10.26b).

In addition to graphite and diamond, a third crystalline allotrope of carbon called fullerene was discovered in 1985 as a constituent of soot. Fullerene consists of spherical $\mathrm{C}_{60}$ molecules with the extraordinary shape of a soccer ball. The $\mathrm{C}_{60}$ ball has 12 pentagonal and 20 hexagonal faces, with each atom $s p^{2}$-hybridized and bonded to three other atoms (Figure 10.27a). Closely related to both graphite and fullerene are a group of carbon allotropes called nanotubes (Figure 10.27b). Carbon nanotubes are tubular structures made of repeating six-membered carbon rings, as if a sheet of graphite were rolled up. Typically, the tubes have a diameter of about $2-30 \mathrm{~nm}$ and a length of up to 1 mm .

The different structures of the carbon allotropes lead to widely different properties. Because of its three-dimensional network of strong single bonds that tie all atoms in a crystal together, diamond is the hardest known substance. In addition to its use in jewelry, diamond is widely used industrially for the tips of saw blades


FIGURE 10.26 Two crystalline allotropes of carbon: (a) Graphite is a covalent network solid consisting of twodimensional sheets of six-membered rings. The atoms in each sheet are offset slightly from the atoms in the neighboring sheets. (b) Diamond is a vast, three-dimensional array of $s p^{3}$-hybridized carbon atoms, each of which is bonded with tetrahedral geometry to four other carbons.

FIGURE 10.27 -
(a) Fullerene, $\mathrm{C}_{60}$, is a molecular solid whose molecules have the shape of a soccer ball. The ball has 12 pentagonal and 20 hexagonal faces, and each carbon atom is $s p^{2}$-hybridized. (b) Carbon nanotubes consist of sheets of graphite rolled into tubes of $2-30 \mathrm{~nm}$ diameter.
and drilling bits. It is an electrical insulator and has a melting point of over $3550^{\circ} \mathrm{C}$. Clear, colorless, and highly crystalline, diamonds are very rare and are found in only a few places in the world, primarily in South Africa.

Graphite is the black, slippery substance used as the "lead" in pencils, as an electrode material in batteries, and as a lubricant in locks. All these properties result from its sheetlike structure. Air and water molecules can adsorb onto the flat faces of the sheets, allowing the sheets to slide over one another and giving graphite its greasy feeling and lubricating properties. Graphite is more stable than diamond at normal pressures but can be converted into diamond at very high pressure. Some industrial diamonds are now made from graphite by applying $150,000 \mathrm{~atm}$ pressure at high temperature.


Fullerene, black and shiny like graphite, is the subject of active current research because of its interesting electronic properties. When allowed to react with rubidium metal, a superconducting material called rubidium fulleride, $\mathrm{Rb}_{3} \mathrm{C}_{60}$, is formed. (We'll discuss superconductors in more detail in Section 21.6.) Carbon nanotubes are being studied for use as fibers in the structural composites used to make golf clubs, bicycle frames, boats, and airplanes. On a mass basis, nanotubes are up to ten times as strong as steel.

(a)

(b)

## Silica

Just as living organisms are based on carbon compounds, most rocks and minerals are based on silicon compounds. Quartz and much sand, for instance, are nearly pure silica, $\mathrm{SiO}_{2}$; silicon and oxygen together make up nearly $75 \%$ of the mass of the earth's crust. Considering that silicon and carbon are both in group 4A of the periodic table, you might expect $\mathrm{SiO}_{2}$ to be similar in its properties to $\mathrm{CO}_{2}$. In fact, though, $\mathrm{CO}_{2}$ is a molecular substance and a gas at room temperature, whereas $\mathrm{SiO}_{2}$ (Figure $10.15 b$ ) is a covalent network solid with a melting point over $1600^{\circ} \mathrm{C}$.

The dramatic difference in properties between $\mathrm{CO}_{2}$ and $\mathrm{SiO}_{2}$ is due primarily to the difference in electronic structure between carbon and silicon. The $\pi$ part of a carbon-oxygen double bond is formed by sideways overlap of a carbon $2 p$ orbital with an oxygen $2 p$ orbital (Section 7.12). If a similar silicon-oxygen double bond were to form, it would require overlap of an oxygen $2 p$ orbital and a silicon $3 p$ orbital. But because the $\mathrm{Si}-\mathrm{O}$ bond distance is longer than the $\mathrm{C}-\mathrm{O}$ distance and a $3 p$ orbital is larger than a $2 p$ orbital, overlap between the two is not as favorable. As a result, silicon forms four single bonds to four oxygens in a covalent network structure rather than two double bonds to two oxygens in a molecular structure.

Heating silica above about $1600^{\circ} \mathrm{C}$ breaks many of its $\mathrm{Si}-\mathrm{O}$ bonds and turns it from a crystalline solid into a viscous liquid. When this fluid is cooled, some of the $\mathrm{Si}-\mathrm{O}$ bonds re-form in a random arrangement, and a noncrystalline, amorphous solid called quartz glass is formed. If additives are mixed in before cooling, a wide variety of glasses can be prepared. Common window glass, for instance, is prepared by adding $\mathrm{CaCO}_{3}$ and $\mathrm{Na}_{2} \mathrm{CO}_{3}$. Addition of various transition metal ions results in the preparation of colored glasses, and addition of $\mathrm{B}_{2} \mathrm{O}_{3}$ produces a high-melting borosilicate glass that is sold under the trade name Pyrex. Borosilicate glass is particularly useful for cooking utensils and laboratory glassware because it expands very little when heated and is thus unlikely to crack.


A The sand in these dunes is nearly pure $\mathrm{SiO}_{2}$.


A Colored glasses contain transition metal ions; borosilicate glass is used in cooking utensils because of its resistance to thermal shock.

### 10.11 Phase Diagrams

Now that we've looked at the three phases of matter individually, let's take an overall view. As noted previously, any one phase of matter can change spontaneously into either of the other two, depending on the temperature and pressure. A particularly convenient way to picture the pressure and temperature dependency of a pure substance in a closed system without air present is to use what is called a phase diagram. As illustrated for water in Figure 10.28, a typical phase diagram shows which phase is stable at different combinations of pressure and temperature. When a boundary line between phases is crossed by changing either the temperature or the pressure, a phase change occurs.


FIGURE 10.28 A phase diagram for $\mathrm{H}_{2} \mathrm{O}$, showing a negative slope for the solid/liquid boundary. Various features of the diagram are discussed in the text. Note that the pressure and temperature axes are not drawn to scale.

$\square$Nicholas K. Kildahl, "Journey Around a Phase Diagram," J. Chem. Educ., Vol. 71, 1994, 1052-1054.


A At the triple point, solid exists in the boiling liquid. That is, solid, liquid, and gas coexist in equilibrium.


The simplest way to understand a phase diagram is to begin at the origin in the lower left corner of Figure 10.28 and travel up and right along the boundary line between solid on the left and gas on the right. Points on this line represent pressure/temperature combinations at which the two phases are in equilibrium in a closed system and a phase transition (sublimation) between solid ice and gaseous water vapor occurs. At some point along the solid/gas line, an intersection is reached where two lines diverge to form the bounds of the liquid region. The solid/liquid boundary for $\mathrm{H}_{2} \mathrm{O}$ goes up and slightly left, while the liquid/gas boundary continues curving up and to the right. Called the triple point, this three-way intersection represents a unique combination of pressure and temperature at which all three phases coexist in equilibrium. For water, the triple-point temperature $T_{\mathrm{t}}$ is $0.0098^{\circ} \mathrm{C}$, and the triple-point pressure $P_{\mathrm{t}}$ is $6.0 \times 10^{-3} \mathrm{~atm}$.

Continuing up and slightly left from the triple point, the solid/liquid boundary line represents the melting point of solid ice (or the freezing point of liquid water) at various pressures. When the pressure is 1 atm , the melting point (called the normal melting point) is exactly $0^{\circ} \mathrm{C}$. There is a slight negative slope to the line, indicating that the melting point of ice decreases as pressure increases. Water is unusual in this respect, because most substances have a positive slope to their solid/liquid line, indicating that their melting points increase with pressure. We'll say more about this behavior shortly.

Continuing up and right from the triple point, the liquid/gas boundary line represents those pressure/temperature combinations at which liquid and gas coexist and water boils (or steam condenses). In fact, the part of the curve up to 1 atm pressure is simply the vapor pressure curve we saw previously in Figure 10.13a. When the pressure is 1 atm , water is at its normal boiling point of $100^{\circ} \mathrm{C}$. Continuing along the liquid/gas boundary line, we suddenly reach the critical point, where the line abruptly ends. The critical temperature $T_{\mathrm{c}}$ is the temperature beyond which a gas cannot be liquefied, no matter how great the pressure; the critical pressure $P_{c}$ is the pressure beyond which a liquid cannot be vaporized, no matter how high the temperature. For water, $T_{\mathrm{c}}=374.4^{\circ} \mathrm{C}$ and $P_{\mathrm{c}}=217.7 \mathrm{~atm}$.

We're all used to seeing solid/liquid and liquid/gas phase transitions, but behavior at the critical point lies so far outside our normal experiences that it's hard to imagine. A gas at the critical point is under such high pressure and its molecules are so close together, that it becomes indistinguishable from a liquid. A
liquid at the critical point is at such a high temperature and its molecules so relatively far apart, that it becomes indistinguishable from a gas. The two phases simply blend into each other to form a supercritical fluid that is neither true liquid nor true gas. No distinct physical phase change occurs on going beyond the critical point. Rather, a whitish, pearly sheen momentarily appears, and the visible boundary between liquid and gas suddenly vanishes. Frankly, you have to see it to believe it.

The phase diagram of $\mathrm{CO}_{2}$ shown in Figure 10.29 has many of the same features as that of water but differs in several interesting respects. First, the triple point is at $P_{\mathrm{t}}=5.11 \mathrm{~atm}$, meaning that $\mathrm{CO}_{2}$ can't be a liquid below this pressure, no matter what the temperature. At 1 atm pressure, $\mathrm{CO}_{2}$ is a solid below $-78.5^{\circ} \mathrm{C}$ but a gas above this temperature. Second, the slope of the solid/liquid boundary is positive, meaning that the solid phase is favored as the pressure rises and that the melting point of solid $\mathrm{CO}_{2}$ therefore increases with pressure.


The effect of pressure on the slope of the solid/liquid boundary line-negative for $\mathrm{H}_{2} \mathrm{O}$ but positive for $\mathrm{CO}_{2}$ and most other substances-depends on the relative densities of the solid and liquid phases. For $\mathrm{CO}_{2}$ and most other substances, the solid phase is denser than the liquid because particles are packed closer together in the solid. Increasing the pressure pushes the molecules even closer together, thereby favoring the solid phase even more and giving the solid/liquid boundary line a positive slope. Water, however, becomes less dense when it freezes to a solid, because large empty spaces are left between molecules due to the ordered threedimensional network of hydrogen bonds in ice (Figure 10.15a). As a result, increasing the pressure favors the liquid phase, giving the solid/liquid boundary a negative slope.

Figure 10.30 shows a simple demonstration of the effect of pressure on melting point. If a thin wire with heavy weights at each end is draped over a block of ice near $0^{\circ} \mathrm{C}$, the wire rapidly cuts through the block because the increased pressure lowers the melting point of the ice under the wire, causing the ice to liquefy. If the same experiment is tried with a block of dry ice (solid $\mathrm{CO}_{2}$ ), however, nothing happens. The dry ice is unaffected because increased pressure makes melting more difficult rather than less difficult.

4 FIGURE 10.29 A phase diagram for $\mathrm{CO}_{2}$, showing a positive slope for the solid/ liquid boundary. The pressure and temperature axes are not to scale.

Stephen J. Hawkes, "There is No Perceptible Inflection at the Triple Point," J. Chem. Educ., Vol. 76, 1999, 226.

Stephen J. Hawkes, "A Simple Experiment for the Demonstration of the Phase Diagram of Carbon Dioxide," J. Chem. Educ., Vol. 73, 1996, 837-838.

© FIGURE 10.30 Why does the weighted wire cut through this block of ice?

## Worked Example 10.11

Freeze-dried foods are prepared by freezing the food and removing water by subliming the ice at low pressure. Look at the phase diagram of water in Figure 10.28, and tell the maximum pressure (in mm Hg ) at which ice and water vapor are in equilibrium.

## Strategy

Ice and water vapor are in equilibrium only below the triple-point pressure, $P_{\mathrm{t}}=6.0 \times 10^{-3} \mathrm{~atm}$, which needs to be converted to millimeters of mercury.

## SOLUTION

$$
6.0 \times 10^{-3} \mathrm{~atm} \times \frac{760 \mathrm{~mm} \mathrm{Hg}}{1 \mathrm{~atm}}=4.6 \mathrm{~mm} \mathrm{Hg}
$$

PROBLEM 10.17 Look at the phase diagram of $\mathrm{CO}_{2}$ in Figure 10.29, and tell the minimum pressure (in atmospheres) at which liquid $\mathrm{CO}_{2}$ can exist.

- PROBLEM 10.18 Look at the phase diagram of $\mathrm{CO}_{2}$ in Figure 10.29, and describe what happens to a $\mathrm{CO}_{2}$ sample when the following changes are made:
(a) The temperature is increased from $-100^{\circ} \mathrm{C}$ to $0^{\circ} \mathrm{C}$ at a constant pressure of 2 atm .
(b) The pressure is reduced from 72 atm to 5.0 atm at a constant temperature of $30^{\circ} \mathrm{C}$.
(c) The pressure is first increased from 3.5 atm to 76 atm at $-10^{\circ} \mathrm{C}$, and the temperature is then increased from $-10^{\circ} \mathrm{C}$ to $45^{\circ} \mathrm{C}$.

KEY CONCEPT PROBLEM 10.19 Gallium metal has the following phase diagram (the pressure axis is not to scale). In the region shown, gallium has two different solid phases.
(a) Where on the diagram are the solid, liquid, and vapor regions?
(b) How many triple points does gallium have? Circle each on the diagram.
(c) At 1 atm pressure, which phase is more dense, solid or liquid? Explain.


## Interlude Liquid Crystals


-
 he world is rarely as orderly as textbooks make it appear. In this chapter, for instance, we've made it seem that the distinction between liquids and solids is clear-cut and that the phase transition between them is always sharply defined. The truth, though, is more complex. At certain temperatures, many substances (about $0.5 \%$ of known compounds) exist in a phase that is neither fully liquid nor fully solid. The molecules in these liquid crystals can move around, as in viscous liquids, but have a restricted range of motion, as in solids.

The molecules in most liquid crystals have a rigid, rodlike shape with a length four to eight times greater than their diameter. When packed together, the molecules tend to orient with their long axes roughly parallel, like logs in a stack of firewood. Individual molecules can migrate through the fluid and can spin around their long axis, but they can't rotate end over end. Several different liquid crystalline phases exist, depending on the amount of ordering. Two of the most common are the nematic phase, in which the ends of the molecules are randomly arranged, and the smectic phase, in which the molecules are arranged in layers.


The widespread use of liquid crystals for displays in digital watches, pocket calculators, and computer screens hinges on the fact that the orientation of liquidcrystal molecules is extremely sensitive to the presence of small electric fields and to the nature of nearby surfaces. As shown schematically in Figure 10.31, a typical liquid-crystal display (LCD) contains a thin layer of nematic liquid-crystal molecules sandwiched between two glass sheets that have been rubbed in different directions with a thin nylon brush and then layered with tiny transparent electrode strips made of indium/tin oxide. The outside of each glass sheet is coated

FIGURE 10.31 A liquidcrystal display (LCD), whose operation is explained in the text.
with a polarizer oriented parallel to the rubbing direction, and one of the sheets is further coated with a reflecting mirror. Because the molecules in the liquid crystal align parallel to the direction of rubbing, and because the two glass sheets are rubbed at $90^{\circ}$ angles to each other, the molecules undergo a gradual $90^{\circ}$ twist in orientation between the two surfaces.


An LCD works in the following way: A beam of ordinary light consists of electromagnetic waves vibrating in various planes perpendicular to the direction of travel. When light passes through a polarizer, such as the lenses of Polaroid sunglasses, only those waves vibrating in a single plane pass through, resulting in a beam of planepolarized light. The light then passes through a layer of liquid crystal that twists the plane of polarization by $90^{\circ}$, thereby allowing the beam to pass through the second polarizer, strike the mirror, and reflect back to be seen as a white background.

To form an LCD image, a voltage is applied to an appropriate pattern of tiny electrodes, causing the molecules in the liquid crystal to reorient parallel to the electric field. As a result, the molecules are no longer able to twist the plane of the polarized light, and the light can no longer pass through the second polarizer to reflect off the mirror. The areas under the electrodes are therefore seen as dark.

- PROBLEM 10.20 How does a liquid crystal differ from a typical solid crystal, such as that of sodium chloride?
- PROBLEM 10.21 What structural feature do liquid-crystal molecules share?

The presence of polar covalent bonds in a molecule can cause the molecule as a whole to have a net polarity, a property measured by the dipole moment.

Intermolecular forces, known collectively as van der Waals forces, are the attractions responsible for holding particles together in the liquid and solid phases. There are several kinds of intermolecular forces, all of which arise from electrical attractions: Dipole-dipole forces occur between two polar molecules. London dispersion forces are characteristic of all molecules and result from the presence of temporary dipole moments caused by momentarily unsymmetrical electron distributions. A hydrogen bond is the attraction between a positively polarized hydrogen atom bonded to $\mathrm{O}, \mathrm{N}$, or F and a lone pair of electrons on an $\mathrm{O}, \mathrm{N}$, or F atom of another molecule. In addition, ion-dipole forces occur between an ion and a polar molecule.

Matter in any one phase-solid, liquid, or gas-can undergo a phase change to any of the other two phases. Like all naturally occurring processes, a phase change has associated with it a free-energy change, $\Delta G=\Delta H-T \Delta S$. The enthalpy component, $\Delta H$, is a measure of the change in intermolecular forces; the entropy component, $\Delta S$, is a measure of the change in molecular randomness accompanying the phase transition. The enthalpy change for the solid-liquid transition is called the heat of fusion, and the enthalpy change for the liquid-vapor transition is the heat of vaporization.

The effects of temperature and pressure on phase changes can be displayed on phase diagrams. A typical phase diagram has three regions-solid, liquid, and gas-separated by three boundary lines: solid/gas, solid/liquid, and liquid/gas. The boundary lines represent pressure/temperature combinations
at which two phases are in equilibrium and phase changes occur. At exactly 1 atm pressure, the temperature at the solid/liquid boundary corresponds to the normal melting point of the substance, and the temperature at the liquid/gas boundary corresponds to the normal boiling point. The three lines meet at the triple point, a unique combination of temperature and pressure at which all three phases coexist in equilibrium. The liquid/gas line runs from the triple point to the critical point, a pressure/temperature combination beyond which liquid and gas phases become a supercritical fluid that is neither liquid nor gas.

Solids can be characterized as amorphous if their particles are randomly arranged or crystalline if their particles are ordered. Crystalline solids can be further characterized as ionic solids if their particles are ions, molecular solids if their particles are molecules, covalent network solids if they consist of a covalently bonded array of atoms without discrete molecules, or metallic solids if their particles are metal atoms.

The regular three-dimensional network of particles in a crystal is made up of small repeating units called unit cells. There are 14 kinds of unit cells, three of which have cubic symmetry. Simple cubic packing uses a primitive-cubic unit cell, with an atom at each corner of the cube. Body-centered cubic packing uses a body-centered cubic unit cell, with an atom at the center and at each corner of the cube. Cubic closestpacking uses a face-centered cubic unit cell, with an atom at the center of each face and at each corner of the cube. A fourth kind of packing, called hexagonal closest-packing, uses a noncubic unit cell.
allotrope 411
amorphous solid 400
body-centered cubic
packing 405
body-centered cubic unit cell 406
Bragg equation 403
Clausius-Clapeyron equation 398
coordination number 404
covalent network solid 400
critical point 414
crystalline solid 400
cubic closest-packing 405
diffraction 402
dipole 382
dipole moment ( $\boldsymbol{\mu}$ ) 383
dipole-dipole force 386
face-centered cubic unit cell 406
heat of fusion ( $\Delta H_{\text {fusion }}$ ) 395
heat of vaporization
( $\Delta H_{\text {vap }}$ ) 395
hexagonal closestpacking 405
hydrogen bond 389

## intermolecular force

 385ion-dipole force 386
ionic solid 400
London dispersion force 388
metallic solid 401
molecular solid 400
normal boiling point 398
normal melting point 414
phase 392
phase change 392
phase diagram 413

## primitive-cubic unit cell 406

simple cubic packing 404
supercritical fluid 415
surface tension 392
triple point 414
unit cell 406
van der Waals forces 385
vapor pressure 396
viscosity 391

## Key Concept Summary



## Understanding Key Concepts

Problems 10.1-10.21 appear within the chapter.
10.22 Ethyl acetate, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$, is commonly used as a solvent and nail-polish remover. Look at the following electrostatic potential map of ethyl acetate, and explain the observed polarity.

10.23 Identify each of the following kinds of packing.

(a)

(b)

(c)

(d)
10.24 Zinc sulfide, or sphalerite, crystallizes in the following cubic unit cell:

(a) What kind of packing do the sulfide ions adopt?
(b) How many $\mathrm{S}^{2-}$ ions and how many $\mathrm{Zn}^{2+}$ ions are in the unit cell?
10.25 Perovskite, a mineral containing calcium, oxygen, and titanium, crystallizes in the following cubic unit cell:

(a) What is the formula of perovskite?
(b) What is the oxidation number of titanium in perovskite?
10.26 The phase diagram of a substance is shown below.


(a) Approximately what is the normal boiling point, and what is the normal melting point of the substance?
(b) What is the physical state of the substance under the following conditions?
(i) $T=150 \mathrm{~K}, P=0.5 \mathrm{~atm}$
(ii) $T=325 \mathrm{~K}, P=0.9 \mathrm{~atm}$
(iii) $T=450 \mathrm{~K}, P=265 \mathrm{~atm}$
10.27 Boron nitride, BN , is a covalent network solid with a structure similar to that of graphite. Sketch a small portion of the boron nitride structure.
10.28 Imagine a tiled floor made of square and octagonal tiles in the following pattern. Identify the smallest repeating unit, analogous to a unit cell.

10.29 The following phase diagram of elemental carbon has three different solid phases in the region shown.
(O)

(a) Show where the solid, liquid, and vapor regions are on the diagram.
(b) How many triple points does carbon have? Circle each on the diagram.
(c) Graphite is the most stable solid phase under normal conditions. Identify the graphite phase on the diagram.
(d) On heating graphite to 2500 K at a pressure of $100,000 \mathrm{~atm}$, it can be converted into diamond. Identify the diamond phase on the graph.
(e) Which phase is more dense, graphite or diamond? Explain.

## Additional Problems

## Dipole Moments and Intermolecular Forces

10.30 Why do some molecules have dipole moments while others do not?
10.31 What is the difference between London dispersion forces and dipole-dipole forces?
10.32 What are the most important kinds of intermolecular forces present in each of the following substances?
(a) Chloroform, $\mathrm{CHCl}_{3}$
(b) Oxygen, $\mathrm{O}_{2}$
(c) Polyethylene, $\mathrm{C}_{n} \mathrm{H}_{2 n+2}$
(d) Methanol, $\mathrm{CH}_{3} \mathrm{OH}$
10.33 Of the substances $\mathrm{Xe}, \mathrm{CH}_{3} \mathrm{Cl}, \mathrm{HF}$, which has:
(a) The smallest dipole-dipole forces?
(b) The largest hydrogen bond forces?
(c) The largest dispersion forces?
10.34 Methanol $\left(\mathrm{CH}_{3} \mathrm{OH} ; \mathrm{bp}=65^{\circ} \mathrm{C}\right)$ boils nearly $230^{\circ}$ higher than methane $\left(\mathrm{CH}_{4} ; \mathrm{bp}=-164^{\circ} \mathrm{C}\right)$, but 1-decanol $\left(\mathrm{C}_{10} \mathrm{H}_{21} \mathrm{OH} ; \mathrm{bp}=229^{\circ} \mathrm{C}\right)$ boils only $55^{\circ}$ higher than decane ( $\left.\mathrm{C}_{10} \mathrm{H}_{22} ; \mathrm{bp}=174^{\circ} \mathrm{C}\right)$. Explain.
10.35 Which substance in each of the following pairs would you expect to have larger dispersion forces?
(a) Ethane, $\mathrm{C}_{2} \mathrm{H}_{6}$, or octane, $\mathrm{C}_{8} \mathrm{H}_{18}$
(b) HCl or HI
(c) $\mathrm{H}_{2} \mathrm{O}$ or $\mathrm{H}_{2} \mathrm{Se}$
10.36 Which of the following substances would you expect to have a nonzero dipole moment? Explain, and show the direction of each.
(a) $\mathrm{Cl}_{2} \mathrm{O}$
(b) $\mathrm{XeF}_{4}$
(c) Chloroethane, $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{Cl}$
(d) $\mathrm{BF}_{3}$
10.37 Which of the following substances would you expect to have a nonzero dipole moment? Explain, and show the direction of each.
(a) $\mathrm{NF}_{3}$
(b) $\mathrm{CH}_{3} \mathrm{NH}_{2}$
(c) $\mathrm{XeF}_{2}$
(d) $\mathrm{PCl}_{5}$
10.38 Why is the dipole moment of $\mathrm{SO}_{2} 1.63 \mathrm{D}$, but that of $\mathrm{CO}_{2}$ is zero?
10.39 Draw three-dimensional structures of $\mathrm{PCl}_{3}$ and $\mathrm{PCl}_{5}$, and then explain why one of the molecules has a dipole moment and one does not.
10.40 Draw a picture that shows how hydrogen bonding takes place between two ammonia molecules.
10.41 1,3-Propanediol, $\mathrm{HOCH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{OH}$, can form intramolecular hydrogen bonds as well as intermolecular hydrogen bonds. Draw a structure of 1,3-propanediol that shows an intramolecular hydrogen bond.

## Vapor Pressure and Phase Changes

10.42 Why is $\Delta H_{\text {vap }}$ usually larger than $\Delta H_{\text {fusion }}$ ?
10.43 Why is the heat of sublimation, $\Delta H_{\text {subl }}$, equal to the sum of $\Delta H_{\text {vap }}$ and $\Delta H_{\text {fusion }}$ at the same temperature?
10.44 Mercury has $\mathrm{mp}=-38.9^{\circ} \mathrm{C}$ and $\mathrm{bp}=356.6^{\circ} \mathrm{C}$. What, if any, phase changes take place under the following conditions at 1.0 atm pressure?
(a) The temperature of a sample is raised from $-30^{\circ} \mathrm{C}$ to $365^{\circ} \mathrm{C}$.
(b) The temperature of a sample is lowered from 291 K to 238 K .
(c) The temperature of a sample is lowered from 638 K to 231 K .
10.45 Iodine has $\mathrm{mp}=113.5^{\circ} \mathrm{C}$ and $\mathrm{bp}=184.4^{\circ} \mathrm{C}$. What, if any, phase changes take place under the following conditions at 1.0 atm pressure?
(a) The temperature of a solid sample is held at $113.5^{\circ} \mathrm{C}$ while heat is added.
(b) The temperature of a sample is lowered from 452 K to 389 K .
10.46 Water at room temperature is placed in a flask connected by rubber tubing to a vacuum pump, and the pump is turned on. After several minutes, the volume of the water has decreased and what remains has turned to ice. Explain.
10.47 Ether at room temperature is placed in a flask connected by a rubber tube to a vacuum pump, the pump is turned on, and the ether begins boiling. Explain.
10.48 How much energy (in kilojoules) is needed to heat 5.00 g of ice from $-10.0^{\circ} \mathrm{C}$ to $30.0^{\circ} \mathrm{C}$ ? The heat of fusion of water is $6.01 \mathrm{~kJ} / \mathrm{mol}$, and the molar heat capacity is $36.6 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for ice and $75.3 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for liquid water.
10.49 How much energy (in kilojoules) is released when 15.3 g of steam at $115.0^{\circ} \mathrm{C}$ is condensed to give liquid water at $75.0^{\circ} \mathrm{C}$ ? The heat of vaporization of liquid water is 40.67 $\mathrm{kJ} / \mathrm{mol}$, and the molar heat capacity is $75.3 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for the liquid and $33.6 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for the vapor.
10.50 How much energy (in kilojoules) is released when 7.55 g of water at $33.5^{\circ} \mathrm{C}$ is cooled to $-10.0^{\circ} \mathrm{C}$ ? (See Problem 10.48 for the necessary data.)
10.51 How much energy (in kilojoules) is released when 25.0 g of ethanol vapor at $93.0^{\circ} \mathrm{C}$ is cooled to $-10.0^{\circ} \mathrm{C}$ ? Ethanol has $\mathrm{mp}=-114.5^{\circ} \mathrm{C}, \mathrm{bp}=78.4^{\circ} \mathrm{C}, \Delta H_{\text {vap }}=$ $38.56 \mathrm{~kJ} / \mathrm{mol}$, and $\Delta H_{\text {fusion }}=4.60 \mathrm{~kJ} / \mathrm{mol}$. The molar heat capacity is $113 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for the liquid and $65.7 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for the vapor.
10.52 Draw a molar heating curve for ethanol, $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$, similar to that shown for water in Figure 10.10. Begin with solid ethanol at its melting point, and raise the temperature to $100^{\circ} \mathrm{C}$. The necessary data are given in Problem 10.51.
10.53 Draw a molar heating curve for sodium similar to that shown for water in Figure 10.10. Begin with solid sodium at its melting point, and raise the temperature to $1000^{\circ} \mathrm{C}$. The necessary data are $\mathrm{mp}=97.8^{\circ} \mathrm{C}, \mathrm{bp}=883^{\circ} \mathrm{C}$, $\Delta H_{\text {vap }}=89.6 \mathrm{~kJ} / \mathrm{mol}$, and $\Delta H_{\text {fusion }}=2.64 \mathrm{~kJ} / \mathrm{mol}$. Assume that the molar heat capacity is $28.2 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for both liquid and vapor phases and does not change with temperature.
10.54 Naphthalene, better known as "mothballs," has $\mathrm{bp}=218^{\circ} \mathrm{C}$ and $\Delta H_{\text {vap }}=43.3 \mathrm{~kJ} / \mathrm{mol}$. What is the entropy of vaporization, $\Delta S_{\text {vap }}$ [in $\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})$ ] for naphthalene?
10.55 What is the entropy of fusion, $\Delta S_{\text {fusion }}[\mathrm{in} \mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})]$ for sodium? The necessary data are given in Problem 10.53.
10.56 Carbon disulfide, $\mathrm{CS}_{2}$, has $P_{\text {vap }}=100 \mathrm{~mm}$ at $-5.1^{\circ} \mathrm{C}$ and a normal boiling point of $46.5^{\circ} \mathrm{C}$. What is $\Delta H_{\text {vap }}$ for carbon disulfide in $\mathrm{kJ} / \mathrm{mol}$ ?
10.57 The vapor pressure of $\mathrm{SiCl}_{4}$ is 100 mm Hg at $5.4^{\circ} \mathrm{C}$, and the normal boiling point is $56.8^{\circ} \mathrm{C}$. What is $\Delta H_{\text {vap }}$ for $\mathrm{SiCl}_{4}$ in $\mathrm{kJ} / \mathrm{mol}$ ?
10.58 What is the vapor pressure of $\mathrm{CS}_{2}($ in mm Hg$)$ at $20.0^{\circ} \mathrm{C}$ ? (See Problem 10.56.)
10.59 What is the vapor pressure of $\mathrm{SiCl}_{4}$ (in mm Hg ) at $30.0^{\circ} \mathrm{C}$ ? (See Problem 10.57.)
10.60 Dichloromethane, $\mathrm{CH}_{2} \mathrm{Cl}_{2}$, is an organic solvent used for removing caffeine from coffee beans. The following table gives the vapor pressure of dichloromethane at various temperatures. Fill in the rest of the table, and use the data to plot curves of $P_{\text {vap }}$ versus $T$ and $\ln P_{\text {vap }}$ versus $1 / T$.

| Temp (K) | $\boldsymbol{P}_{\text {vap }}(\mathbf{m m} \mathbf{H g})$ | $\ln \boldsymbol{P}_{\text {vap }}$ | $\mathbf{1 / T}$ |
| :--- | :---: | :--- | :--- |
| 263 | 80.1 | $?$ | $?$ |
| 273 | 133.6 | $?$ | $?$ |
| 283 | 213.3 | $?$ | $?$ |
| 293 | 329.6 | $?$ | $?$ |
| 303 | 495.4 | $?$ | $?$ |
| 313 | 724.4 | $?$ | $?$ |

10.61 The following table gives the vapor pressure of mercury at various temperatures. Fill in the rest of the table, and use the data to plot curves of $P_{\text {vap }}$ versus $T$ and $\ln P_{\text {vap }}$ versus $1 / T$.

| Temp (K) | $\boldsymbol{P}_{\mathbf{v a p}}(\mathbf{m m} \mathbf{H g})$ | $\ln \left(\boldsymbol{P}_{\mathbf{v a p}}\right)$ | $\mathbf{1} / \boldsymbol{T}$ |
| :--- | :---: | :--- | :--- |
| 500 | 39.3 | $?$ | $?$ |
| 520 | 68.5 | $?$ | $?$ |
| 540 | 114.4 | $?$ | $?$ |
| 560 | 191.6 | $?$ | $?$ |
| 580 | 286.4 | $?$ | $?$ |
| 600 | 432.3 | $?$ | $?$ |

10.62 Use the plot you made in Problem 10.60 to find a value (in $\mathrm{kJ} / \mathrm{mol}$ ) for $\Delta H_{\text {vap }}$ for dichloromethane.
10.63 Use the plot you made in Problem 10.61 to find a value (in $\mathrm{kJ} / \mathrm{mol}$ ) for $\Delta H_{\text {vap }}$ for mercury. The normal boiling point of mercury is 630 K .
10.64 Choose any two temperatures and corresponding vapor pressures in the table given in Problem 10.60, and use those values to calculate $\Delta H_{\text {vap }}$ for dichloromethane (in $\mathrm{kJ} / \mathrm{mol}$ ). How does the value you calculated compare to the value you read from your plot in Problem 10.62?
10.65 Choose any two temperatures and corresponding vapor pressures in the table given in Problem 10.61, and use those values to calculate $\Delta H_{\text {vap }}$ for mercury (in $\mathrm{kJ} / \mathrm{mol}$ ). How does the value you calculated compare to the value you read from your plot in Problem 10.63?

## Structures of Solids

10.66 List the four main classes of crystalline solids, and give a specific example of each.
10.67 What kinds of particles are present in each of the four main classes of crystalline solids?
10.68 What is a unit cell?
10.69 Which of the four kinds of packing used by metals makes the most efficient use of space, and which makes the least efficient use?
10.70 Copper crystallizes in a face-centered cubic unit cell with an edge length of 362 pm . What is the radius of a copper atom (in picometers)? What is the density of copper in $\mathrm{g} / \mathrm{cm}^{3}$ ?
10.71 Lead crystallizes in a face-centered cubic unit cell with an edge length of 495 pm . What is the radius of a lead atom (in picometers)? What is the density of lead in $\mathrm{g} / \mathrm{cm}^{3}$ ?
10.72 Aluminum has a density of $2.699 \mathrm{~g} / \mathrm{cm}^{3}$ and crystallizes with a face-centered cubic unit cell. What is the edge length of a unit cell (in picometers)?
10.73 Tungsten crystallizes in a body-centered cubic unit cell with an edge length of 317 pm . What is the length (in picometers) of a unit-cell diagonal that passes through the center atom?
10.74 In light of your answer to Problem 10.73, what is the radius (in picometers) of a tungsten atom?
10.75 Sodium has a density of $0.971 \mathrm{~g} / \mathrm{cm}^{3}$ and crystallizes with a body-centered cubic unit cell. What is the radius of a sodium atom, and what is the edge length of the cell (both in picometers)?
10.76 Titanium metal has a density of $4.54 \mathrm{~g} / \mathrm{cm}^{3}$ and an atomic radius of 144.8 pm . In what cubic unit cell does titanium crystallize?
10.77 Calcium metal has a density of $1.55 \mathrm{~g} / \mathrm{cm}^{3}$ and crystallizes in a cubic unit cell with an edge length of 558.2 pm .
(a) How many Ca atoms are in one unit cell?
(b) In which of the three cubic unit cells does calcium crystallize?
10.78 Sodium hydride, NaH , crystallizes in a face-centered cubic unit cell similar to that of NaCl (Figure 10.24). How many $\mathrm{Na}^{+}$ions touch each $\mathrm{H}^{-}$ion, and how many $\mathrm{H}^{-}$ions touch each $\mathrm{Na}^{+}$ion?
10.79 Cesium chloride crystallizes in a cubic unit cell with $\mathrm{Cl}^{-}$ions at the corners and a $\mathrm{Cs}^{+}$ion in the center. Count the numbers of + and - charges, and show that the unit cell is electrically neutral.
10.80 If the edge length of an NaH unit cell is 488 pm , what is the length (in picometers) of an $\mathrm{Na}-\mathrm{H}$ bond? (See Problem 10.78.)
10.81 The edge length of a CsCl unit cell (Problem 10.79) is 412.3 pm . What is the length (in picometers) of the $\mathrm{Cs}-\mathrm{Cl}$ bond? If the ionic radius of a $\mathrm{Cl}^{-}$ion is 181 pm , what is the ionic radius (in picometers) of a $\mathrm{Cs}^{+}$ion?

## Phase Diagrams

10.82 Look at the phase diagram of $\mathrm{CO}_{2}$ in Figure 10.29, and tell what phases are present under the following conditions:
(a) $T=-60^{\circ} \mathrm{C}, P=0.75 \mathrm{~atm}$
(b) $T=-35^{\circ} \mathrm{C}, P=18.6 \mathrm{~atm}$
(c) $T=-80^{\circ} \mathrm{C}, P=5.42 \mathrm{~atm}$
10.83 Look at the phase diagram of $\mathrm{H}_{2} \mathrm{O}$ in Figure 10.28, and tell what happens to an $\mathrm{H}_{2} \mathrm{O}$ sample when the following changes are made:
(a) The temperature is reduced from $48^{\circ} \mathrm{C}$ to $-4.4^{\circ} \mathrm{C}$ at a constant pressure of 6.5 atm .
(b) The pressure is increased from 85 atm to 226 atm at a constant temperature of $380^{\circ} \mathrm{C}$.
10.84 Bromine has $T_{\mathrm{t}}=-7.3^{\circ} \mathrm{C}, P_{\mathrm{t}}=44 \mathrm{~mm} \mathrm{Hg}, T_{\mathrm{c}}=315^{\circ} \mathrm{C}$, and $P_{\mathrm{c}}=102 \mathrm{~atm}$. The density of the liquid is $3.1 \mathrm{~g} / \mathrm{cm}^{3}$, and the density of the solid is $3.4 \mathrm{~g} / \mathrm{cm}^{3}$. Sketch a phase diagram for bromine, and label all points of interest.
10.85 Oxygen has $T_{\mathrm{t}}=54.3 \mathrm{~K}, P_{\mathrm{t}}=1.14 \mathrm{~mm} \mathrm{Hg}, T_{\mathrm{c}}=154.6 \mathrm{~K}$, and $P_{\mathrm{C}}=49.77 \mathrm{~atm}$. The density of the liquid is $1.14 \mathrm{~g} / \mathrm{cm}^{3}$, and the density of the solid is $1.33 \mathrm{~g} / \mathrm{cm}^{3}$. Sketch a phase diagram for oxygen, and label all points of interest.
10.86 Refer to the bromine phase diagram you sketched in Problem 10.84, and tell what phases are present under the following conditions:
(a) $T=-10^{\circ} \mathrm{C}, P=0.0075 \mathrm{~atm}$
(b) $T=25^{\circ} \mathrm{C}, P=16 \mathrm{~atm}$
10.87 Refer to the oxygen phase diagram you sketched in Problem 10.85, and tell what phases are present under the following conditions:
(a) $T=-210^{\circ} \mathrm{C}, P=1.5 \mathrm{~atm}$
(b) $T=-100^{\circ} \mathrm{C}, P=66 \mathrm{~atm}$
10.88 Does solid oxygen (Problem 10.85) melt when pressure is applied, as water does? Explain.
10.89 Assume that you have samples of the following three gases at $25^{\circ} \mathrm{C}$. Which of the three can be liquefied by applying pressure, and which cannot? Explain.
Ammonia: $T_{\mathrm{c}}=132.5^{\circ} \mathrm{C}$ and $P_{\mathrm{c}}=112.5 \mathrm{~atm}$
Methane: $T_{\mathrm{c}}=-82.1^{\circ} \mathrm{C}$ and $P_{\mathrm{c}}=45.8 \mathrm{~atm}$
Sulfur dioxide: $T_{\mathrm{c}}=157.8^{\circ} \mathrm{C}$ and $P_{\mathrm{c}}=77.7 \mathrm{~atm}$
10.90 Benzene has a melting point of $5.53^{\circ} \mathrm{C}$ and a boiling point of $80.09^{\circ} \mathrm{C}$ at atmospheric pressure. Its density is $0.8787 \mathrm{~g} / \mathrm{cm}^{3}$ when liquid and $0.899 \mathrm{~g} / \mathrm{cm}^{3}$ when solid; it has $T_{\mathrm{C}}=289.01^{\circ} \mathrm{C}, P_{\mathrm{c}}=48.34 \mathrm{~atm}, T_{\mathrm{t}}=5.52^{\circ} \mathrm{C}$, and $P_{\mathrm{t}}=0.0473 \mathrm{~atm}$. Starting from a point at 200 K and 66.5 atm, trace the following path on a phase diagram:
(a) First, increase $T$ to 585 K while keeping $P$ constant.
(b) Next, decrease $P$ to 38.5 atm while keeping $T$ constant.
(c) Then, decrease $T$ to 278.66 K while keeping $P$ constant.
(d) Finally, decrease $P$ to 0.0025 atm while keeping $T$ constant.
What is your starting phase, and what is your final phase?
10.91 Refer to the oxygen phase diagram you drew in Problem 10.85, and trace the following path starting from a point at 0.0011 atm and $-225^{\circ} \mathrm{C}$ :
(a) First, increase $P$ to 35 atm while keeping $T$ constant.
(b) Next, increase $T$ to $-150^{\circ} \mathrm{C}$ while keeping $P$ constant.
(c) Then, decrease $P$ to 1.0 atm while keeping $T$ constant.
(d) Finally, decrease $T$ to $-215^{\circ} \mathrm{C}$ while keeping $P$ constant.
What is your starting phase, and what is your final phase?
10.92 How many phase transitions did you pass through in Problem 10.90, and what are they?
10.93 What phase transitions did you pass through in Problem 10.91?

## General Problems

10.94 Fluorine is more electronegative than chlorine (Figure 7.4), yet fluoromethane ( $\mathrm{CH}_{3} \mathrm{~F} ; \mu=1.85 \mathrm{D}$ ) has a smaller dipole moment than chloromethane ( $\mathrm{CH}_{3} \mathrm{Cl} ; \mu=1.87 \mathrm{D}$ ). Explain.
10.95 What is the atomic radius (in picometers) of an argon atom if solid argon has a density of $1.623 \mathrm{~g} / \mathrm{cm}^{3}$ and crystallizes at low temperature in a face-centered cubic unit cell?
10.96 Mercury has $\mathrm{mp}=-38.9^{\circ} \mathrm{C}$, a molar heat capacity of $27.9 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for the liquid and $28.2 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for the solid, and $\Delta H_{\text {fusion }}=2.33 \mathrm{~kJ} / \mathrm{mol}$. Assuming that the heat capacities don't change with temperature, how much energy (in kilojoules) is needed to heat 7.50 g of Hg from a temperature of $-50.0^{\circ} \mathrm{C}$ to $+50.0^{\circ} \mathrm{C}$ ?
10.97 Silicon carbide, SiC , is a covalent network solid with a structure similar to that of diamond. Sketch a small portion of the SiC structure.
10.98 In Denver, the "Mile-High City," water boils at $95^{\circ} \mathrm{C}$. What is atmospheric pressure (in atmospheres) in Denver? $\Delta H_{\text {vap }}$ for $\mathrm{H}_{2} \mathrm{O}$ is $40.67 \mathrm{~kJ} / \mathrm{mol}$.
10.99 Acetic acid, the principal nonaqueous constituent of vinegar, exists as a dimer in the liquid phase, with two acetic acid molecules joined together by two hydrogen bonds. Sketch the structure you would expect this dimer to have.


Acetic acid
10.100 Magnesium metal has $\Delta H_{\text {fusion }}=9.037 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S_{\text {fusion }}=9.79 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. What is the melting point (in ${ }^{\circ} \mathrm{C}$ ) of magnesium?
10.101 Titanium tetrachloride, $\mathrm{TiCl}_{4}$, has a melting point of $-23.2^{\circ} \mathrm{C}$ and has $\Delta H_{\text {fusion }}=9.37 \mathrm{~kJ} / \mathrm{mol}$. What is the entropy of fusion, $\Delta S_{\text {fusion }}[\mathrm{in} \mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})]$, for $\mathrm{TiCl}_{4}$ ?
10.102 Dichlorodifluoromethane, $\mathrm{CCl}_{2} \mathrm{~F}_{2}$, one of the chlorofluorocarbon refrigerants responsible for destroying part of the earth's ozone layer, has $P_{\text {vap }}=40.0 \mathrm{~mm} \mathrm{Hg}$ at $-81.6^{\circ} \mathrm{C}$ and $P_{\text {vap }}=400 \mathrm{~mm} \mathrm{Hg}$ at $-43.9^{\circ} \mathrm{C}$. What is the normal boiling point of $\mathrm{CCl}_{2} \mathrm{~F}_{2}\left(\right.$ in $\left.{ }^{\circ} \mathrm{C}\right)$ ?
10.103 The chlorofluorocarbon refrigerant trichlorofluoromethane, $\mathrm{CCl}_{3} \mathrm{~F}$, has $P_{\text {vap }}=100.0 \mathrm{~mm} \mathrm{Hg}$ at $-23^{\circ} \mathrm{C}$ and $\Delta H_{\text {vap }}=24.77 \mathrm{~kJ} / \mathrm{mol}$.
(a) What is the normal boiling point of trichlorofluoromethane (in ${ }^{\circ} \mathrm{C}$ )?
(b) What is $\Delta S_{\text {vap }}$ for trichlorofluoromethane?
10.104 Nitrous oxide, $\mathrm{N}_{2} \mathrm{O}$, occasionally used as an anesthetic by dentists under the name "laughing gas," has $P_{\text {vap }}=100 \mathrm{~mm} \mathrm{Hg}$ at $-110.3^{\circ} \mathrm{C}$ and a normal boiling point of $-88.5^{\circ} \mathrm{C}$. What is the heat of vaporization of nitrous oxide (in $\mathrm{kJ} / \mathrm{mol}$ )?
10.105 Acetone, a common laboratory solvent, has $\Delta H_{\text {vap }}=29.1 \mathrm{~kJ} / \mathrm{mol}$ and a normal boiling point of $56.2^{\circ} \mathrm{C}$. At what temperature (in ${ }^{\circ} \mathrm{C}$ ) does acetone have $P_{\text {vap }}=105 \mathrm{~mm} \mathrm{Hg}$ ?
10.106 Use the following data to sketch a phase diagram for krypton: $T_{\mathrm{t}}=-169^{\circ} \mathrm{C}, P_{\mathrm{t}}=133 \mathrm{~mm} \mathrm{Hg}, T_{\mathrm{c}}=-63^{\circ} \mathrm{C}$, $P_{\mathrm{c}}=54 \mathrm{~atm}, \mathrm{mp}=-156.6^{\circ} \mathrm{C}, \mathrm{bp}=-152.3^{\circ} \mathrm{C}$. The density of solid krypton is $2.8 \mathrm{~g} / \mathrm{cm}^{3}$, and the density of the liquid is $2.4 \mathrm{~g} / \mathrm{cm}^{3}$. Can a sample of gaseous krypton at room temperature be liquefied by raising the pressure?
10.107 What is the physical phase of krypton (Problem 10.106) under the following conditions:
(a) $P=5.3 \mathrm{~atm}, T=-153^{\circ} \mathrm{C}$
(b) $P=65 \mathrm{~atm}, T=250 \mathrm{~K}$
10.108 Calculate the percent volume occupied by the spheres in a body-centered cubic unit cell.
10.109 Iron crystallizes in a body-centered cubic unit cell with an edge length of 287 pm . What is the radius of an iron atom (in picometers)?
10.110 Iron metal has a density of $7.86 \mathrm{~g} / \mathrm{cm}^{3}$ and a molar mass of 55.85 g . Use this information together with the data in Problem 10.109 to calculate a value for Avogadro's number.
10.111 Silver metal crystallizes in a face-centered cubic unit cell with an edge length of 408 pm . The molar mass of silver is $107.9 \mathrm{~g} / \mathrm{mol}$, and its density is $10.50 \mathrm{~g} / \mathrm{cm}^{3}$. Use these data to calculate a value for Avogadro's number.
10.112 A drawing of the NaCl unit cell is shown in Figure 10.24.
(a) What is the edge length (in picometers) of the NaCl unit cell? The ionic radius of $\mathrm{Na}^{+}$is 97 pm , and the ionic radius of $\mathrm{Cl}^{-}$is 181 pm .
(b) What is the density of NaCl in $\mathrm{g} / \mathrm{cm}^{3}$ ?
10.113 Niobium oxide crystallizes in the following cubic unit cell:

(a) How many niobium atoms and how many oxygen atoms are in each unit cell?
(b) What is the formula of niobium oxide?
(c) What is the oxidation state of niobium?
10.114 For each of the following substances, identify the intermolecular force or forces that predominate. Using your knowledge of the relative strengths of the various forces, rank the substances in order of their normal boiling points.

$$
\mathrm{Al}_{2} \mathrm{O}_{3}, \mathrm{~F}_{2}, \mathrm{H}_{2} \mathrm{O}, \mathrm{Br}_{2}, \mathrm{ICl}, \mathrm{NaCl}
$$

10.115 One form of silver telluride $\left(\mathrm{Ag}_{2} \mathrm{Te}\right)$ crystallizes with a cubic unit cell and a density of $7.70 \mathrm{~g} / \mathrm{cm}^{3}$. X-ray crystallography shows that the edge of the cubic unit cell has a length of 529 pm . How many Ag atoms are in the unit cell?
10.116 Substance $X$ has a vapor pressure of 100 mm Hg at its triple point $\left(48^{\circ} \mathrm{C}\right)$. When 1 mol of $X$ is heated at 1 atm pressure with a constant rate of heat input, the following heating curve is obtained:

(a) Sketch the phase diagram for $X$, including labels for different phases, triple point, melting point, and boiling point.
(b) For each of the following, choose which phase of $X$ (solid, liquid, or gas) fits the description:
(i) Is the most dense at $50^{\circ} \mathrm{C}$
(ii) Is the least dense at $50^{\circ} \mathrm{C}$
(iii) Has the greatest specific heat
(iv) Predominates at $80^{\circ} \mathrm{C}$ and 1 atm
(v) Can have a vapor pressure of 20 mm Hg

## Multi-Concept Problems

10.117 Look up thermodynamic data for ethanol $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right)$ in Appendix B, estimate the normal boiling point of ethanol, and calculate the vapor pressure of ethanol at $25^{\circ} \mathrm{C}$.
10.118 The mineral magnetite is an iron oxide ore that has a density of $5.20 \mathrm{~g} / \mathrm{cm}^{3}$. At high temperature, magnetite reacts with carbon monoxide to yield iron metal and carbon dioxide. When 2.660 g of magnetite is allowed to react with sufficient carbon monoxide, the $\mathrm{CO}_{2}$ product is found to have a volume of 1.136 L at 298 K and 751 mm Hg pressure.
(a) What mass of iron (in grams) is formed in the reaction?
(b) What is the formula of magnetite?
(c) Magnetite has a somewhat complicated cubic unit cell with an edge length of 839 pm . How many Fe and O atoms are present in each unit cell?
10.119 A group 3A metal has a density of $2.70 \mathrm{~g} / \mathrm{cm}^{3}$ and a cubic unit cell with an edge length of 404 pm . Reaction of a $1.07 \mathrm{~cm}^{3}$ chunk of the metal with an excess of hydrochloric acid gives a colorless gas that occupies 4.00 L at $23.0^{\circ} \mathrm{C}$ and a pressure of 740 mm Hg .
(a) Identify the metal.
(b) Is the unit cell primitive, body-centered, or facecentered?
(c) What is the atomic radius of the metal atom in picometers?
10.120 A cube-shaped crystal of an alkali metal, 1.62 mm on an edge, was vaporized in a 500.0 mL evacuated flask. The pressure of the resulting vapor was 12.5 mm at $802^{\circ} \mathrm{C}$. The structure of the solid metal is known to be body-centered cubic.
(a) What is the atomic radius of the metal atom in picometers?
(b) Use the data in Figure 5.19 to identify the alkali metal.
(c) What are the densities of the solid and the vapor (in $\mathrm{g} / \mathrm{cm}^{3}$ )?
10.121 Assume that 1.588 g of an alkali metal undergoes complete reaction with the amount of gaseous halogen contained in a 0.500 L flask at 298 K and 755 mm Hg pressure. In the reaction, 22.83 kJ is released ( $\Delta H=-22.83 \mathrm{~kJ}$ ). The product, a binary ionic compound, crystallizes in a unit cell with anions in a facecentered cubic arrangement and with cations centered along each edge between anions. In addition, there is a cation in the center of the cube.
(a) What is the identity of the alkali metal?
(b) The edge length of the unit cell is 535 pm . Find the radius of the alkali metal cation from the data in Figure 6.1, and then calculate the radius of the halide anion. Identify the anion from the data in Figure 6.2.
(c) Sketch a space-filling, head-on view of the unit cell, labeling the ions. Are the anions in contact with one another?
(d) What is the density of the compound in $\mathrm{g} / \mathrm{cm}^{3}$ ?
(e) What is the standard heat of formation for the compound?

## eMedia Problems

10.122 The Molecular Polarity activity (eChapter 10.1) allows you to experiment with various polyatomic molecules. Use geometry to explain how a molecule such as $\mathrm{BF}_{3}$ can contain individual bond dipoles and yet have a zero dipole moment overall.
10.123 The Heating Curves activity in eChapter 10.4 identifies four processes that take place as ice is heated from $-25^{\circ} \mathrm{C}$ to over $100^{\circ} \mathrm{C}$. List the four processes, and explain what is happening to the temperature and what the added heat is doing during each process.
10.124 The interactive Vapor Pressure vs. Temperature activity (eChapter 10.5) compares the number of molecules having a given kinetic energy at two different temperatures.
(a) How does the energy required for evaporation change as the temperature is changed?
(b) How does the number of molecules having a kinetic energy equal to or greater than this energy change when temperature is increased?
(c) How does this observation explain the increased rate of evaporation and increased vapor pressure at higher temperatures?
10.125 Using the Equilibrium Vapor Pressure activity (eChapter 10.5), compare the vapor pressures of methanol, ethanol, acetic acid, water, and benzene.
(a) Arrange the compounds in order of decreasing equilibrium vapor pressure at $100^{\circ} \mathrm{C}$ and at $50^{\circ} \mathrm{C}$.
(b) If one compound has a higher equilibrium vapor pressure than another at a particular temperature, will it necessarily have a higher equilibrium vapor pressure at all temperatures? If not, give an example of two compounds whose vapor pressure curves cross, and the temperature at which their vapor pressures are roughly equal.
10.126 Stop the motion of each of the models in eChapter 10.6 and sketch the structure of each of the types of solids. Identify significant differences between the structures, and explain the differences in properties.

## Chapter

## Solutions and Their Properties

## Thus far, we've been concerned primarily with pure substances, both elements and compounds.

If you look around, though, it's clear that most of the substances you see in day-to-day life are mixtures. Air is a gaseous mixture of (primarily) oxygen and nitrogen, blood is a liquid mixture of many different components, and rocks are solid mixtures of different minerals.

We saw in Section 2.7 that a mixture is any intimate combination of two or more pure substances and that

## CONTENTS

- Pearls are a type of colloid, a mixture of large particles consisting primarily of calcium carbonate.


### 11.1 Solutions

11.2 Energy Changes and the Solution
Process
11.3 Units of Concentration
11.4 Some Factors Affecting Solubility
11.5 Physical Behavior of Solutions: Colligative Properties
11.6 Vapor-Pressure Lowering of Solutions: Raoult's Law

11.7 Boiling-Point Elevation and
Freezing-Point Depression of
Solutions
11.8 Osmosis and Osmotic Pressure
11.9 Some Uses of Colligative Properties
11.10 Fractional Distillation of Liquid Mixtures

- Interlude—Dialysis


These sterling silver candlesticks are a solid/solid solution of $92.5 \%$ silver and 7.5\% copper.

[^15]mixtures are classified as either heterogeneous or homogeneous, depending on their appearance. Heterogeneous mixtures are those in which the mixing of components is visually nonuniform and which therefore have regions of different composition. Homogeneous mixtures are those in which the mixing is uniform, at least to the naked eye, and which therefore have the same composition throughout. We'll explore the properties of some homogeneous mixtures in this chapter, with particular emphasis on the mixtures we call solutions.

## 11.1 | Solutions

Homogeneous mixtures can be classified according to the size of their constituent particles as either solutions or colloids. Solutions, the most important class of homogeneous mixtures, contain particles with diameters in the range $0.1-2 \mathrm{~nm}$ the size of a typical ion or small molecule. They are transparent, although they may be colored, and they do not separate on standing. Colloids, such as milk and fog, contain particles with diameters in the range $2-500 \mathrm{~nm}$. Although they are often murky or opaque to light, they do not separate on standing. Mixtures called suspensions also exist, having even larger particles than colloids. These are not truly homogeneous, however, because their particles separate on standing and are visible with a low-power microscope. Blood, paint, and aerosol sprays, are examples.

We usually think of a solution as a solid dissolved in a liquid or as a mixture of liquids, but there are many other kinds of solutions as well. In fact, any one state of matter can form a solution with any other state, and seven different kinds of solutions are possible (Table 11.1). Even solutions of one solid with another and solutions of a gas in a solid are well known. Metal alloys, such as stainless steel ( $4-30 \%$ chromium in iron) and brass ( $10-40 \%$ zinc in copper) are solid/solid solutions, and hydrogen in palladium is a gas/solid solution. Metallic palladium, in fact, is able to absorb up to 935 times its own volume of $\mathrm{H}_{2}$ gas.

TABLE 11.1 Some Different Kinds of Solutions

| Kind of Solution | Example |
| :--- | :--- |
| Gas in gas | Air $\left(\mathrm{O}_{2}, \mathrm{~N}_{2}, \mathrm{Ar}\right.$, and other gases $)$ |
| Gas in liquid | Carbonated water $\left(\mathrm{CO}_{2}\right.$ in water $)$ |
| Gas in solid | $\mathrm{H}_{2}$ in palladium metal |
| Liquid in liquid | Gasoline (mixture of hydrocarbons) |
| Liquid in solid | Dental amalgam (mercury in silver) |
| Solid in liquid | Seawater $(\mathrm{NaCl}$ and other salts in water) |
| Solid in solid | Metal alloys, such as sterling silver $(92.5 \% \mathrm{Ag}, 7.5 \% \mathrm{Cu})$ |

For solutions in which a gas or solid is dissolved in a liquid, the dissolved substance is called the solute and the liquid is called the solvent. When one liquid is dissolved in another, the minor component is usually considered the solute and the major component is the solvent. Thus, ethyl alcohol is the solute and water the solvent in a mixture of $10 \%$ ethyl alcohol and $90 \%$ water, but water is the solute and ethyl alcohol the solvent in a mixture of $90 \%$ ethyl alcohol and $10 \%$ water.

## 11.2 | Energy Changes and the Solution Process

With the exception of gas/gas mixtures, such as air, the different kinds of solutions listed in Table 11.1 involve condensed phases, either liquid or solid. Thus, all the intermolecular forces described in Chapter 10 to explain the properties of pure
liquids and solids are also important for explaining the properties of solutions. The situation is more complex for solutions than for pure substances, though, because there are three types of interactions among particles that have to be taken into account: solvent-solvent interactions, solvent-solute interactions, and solute-solute interactions.

A good rule of thumb, often summarized in the phrase "like dissolves like," is that solutions will form when the three types of interactions are similar in kind and in magnitude. Thus, ionic solids like NaCl dissolve in polar solvents like water because the strong ion-dipole attractions between $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions and polar $\mathrm{H}_{2} \mathrm{O}$ molecules are similar in magnitude to the strong dipole-dipole attractions between water molecules and to the strong ion-ion attractions between $\mathrm{Na}^{+}$ and $\mathrm{Cl}^{-}$ions. In the same way, nonpolar organic substances like cholesterol, $\mathrm{C}_{27} \mathrm{H}_{46} \mathrm{O}$, dissolve in nonpolar organic solvents like benzene, $\mathrm{C}_{6} \mathrm{H}_{6}$, because of the similar London dispersion forces present among both kinds of molecules. Oil, however, does not dissolve in water because the two liquids have different kinds of intermolecular forces.


The dissolution of a solid in a liquid can be visualized as shown in Figure 11.1 for NaCl . When solid NaCl is placed in water, those ions that are less tightly held because of their position at a corner or an edge of the crystal are exposed to water molecules, which collide with them until an ion happens to break free. More water molecules then cluster around the ion, stabilizing it by means of ion-dipole attractions. A new edge or corner is thereby exposed on the crystal, and the process continues until the entire crystal has dissolved. The ions in solution are said to be


© Why don't oil and water mix?


Wilbur Bergquist, "Do 'Likes Dissolve Likes'? An Illustration of Polar and Nonpolar Solvents," J. Chem. Educ., Vol. 69, 1992, 158. Iodine is shown to dissolve in ethyl alcohol and an alcohol/water mixture, but not in water alone. The relationship between solubility and the molecular polarities of solvent and solute are noted.

4 FIGURE 11.1 Dissolution of NaCl crystals in water. Water molecules surround an accessible edge or corner ion in a crystal and collide with it until the ion breaks free. Additional water molecules then surround the ion and stabilize it by means of ion-dipole attractions.

$\square$
Hydration involves iondipole forces, discussed in Chapter 10. Because opposite charges attract, water molecules differ in their orientation around an anion and around a cation.

Walter H. Corkern and Linda L. Munchausen, "Solubility of Alcohols," J. Chem. Educ., Vol. 69, 1992, 928. An overhead projector demonstration.

Katia Pravia and David F. Maynard, "Why Don't Oil and Water Mix?" J. Chem. Educ., Vol. 73, 1996, 497. An overhead projector demonstration.

FIGURE 11.2 Entropies of solution are usually positive because molecular randomness usually increases when (a) a solid dissolves in a liquid or (b) one liquid dissolves in another.

Todd P. Silverstein, "Polarity, Miscibility, and Surface Tension," J. Chem. Educ., Vol. 70, 1993, 253.

Barry K. Thornton, "An Analogy to Illustrate Miscibility of Liquids," J. Chem. Educ., Vol. 71, 1994, 156.

Michael J. Sanger and Steven M. Badger III, "Using Computer-Based Visualization Strategies to Improve Students' Understanding of Molecular Polarity and Miscibility," J. Chem. Educ., Vol. 78, 2001, 1412-1416.
solvated-more specifically, hydrated, when water is the solvent-meaning that they are surrounded and stabilized by an ordered shell of solvent molecules.

Like all chemical and physical processes, the dissolution of a solute in a solvent has associated with it a free-energy change, $\Delta G$ (Section 8.14). If $\Delta G$ is negative, the process is spontaneous and the substance dissolves; if $\Delta G$ is positive, the process is nonspontaneous and the substance does not dissolve. The free-energy change has two terms: $\Delta G=\Delta H-T \Delta S$. The enthalpy term $\Delta H$ measures the heat flow into or out of the system during dissolution, and the temperaturedependent entropy term $T \Delta S$ measures the change in the amount of molecular disorder or randomness in the system. The enthalpy change is called the enthalpy of solution, or heat of solution $\left(\Delta H_{\text {soln }}\right)$, and the entropy change is called the entropy of solution ( $\Delta S_{\text {soln }}$ ).

What values might we expect for $\Delta H_{\text {soln }}$ and $\Delta S_{\text {soln }}$ ? Let's take the entropy change first. Entropies of solution are usually positive because molecular randomness usually increases during dissolution: $+43.4 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ for NaCl in water, for example. When a solid dissolves in a liquid, randomness increases on going from a well-ordered crystal to a less-ordered state in which solvated ions or molecules are able to move freely in solution. When one liquid dissolves in another, randomness increases as the different molecules intermingle (Figure 11.2). Table 11.2 lists values of $\Delta S_{\text {soln }}$ for some common ionic substances.


TABLE 11.2 Some Enthalpies and Entropies of Solution in Water at $25^{\circ} \mathrm{C}$

| Substance | $\Delta \boldsymbol{H}_{\text {soln }}(\mathbf{k J} / \mathbf{m o l})$ | $\Delta \boldsymbol{S}_{\text {soln }}[\mathbf{J} /(\mathbf{K} \cdot \mathbf{m o l})]$ |
| :--- | :---: | :--- |
| LiCl | -37.0 | 10.5 |
| NaCl | 3.9 | 43.4 |
| KCl | 17.2 | 75.0 |
| LiBr | -48.8 | 21.5 |
| NaBr | -0.6 | 54.6 |
| KBr | 19.9 | 89.0 |
| KOH | -57.6 | 12.9 |

Values for enthalpies of solution, $\Delta H_{\text {soln }}$, are difficult to predict (Table 11.2). Some solids dissolve exothermically and have a negative $\Delta H_{\text {soln }}(-37.0 \mathrm{~kJ} / \mathrm{mol}$ for LiCl in water), but others dissolve endothermically and have a positive $\Delta H_{\text {soln }}$ $(+17.2 \mathrm{~kJ} / \mathrm{mol}$ for KCl in water). Athletes take advantage of both situations when they use instant hot packs or cold packs to treat injuries. Both kinds of instant packs consist of a pouch of water and a dry chemical, either $\mathrm{CaCl}_{2}$ or $\mathrm{MgSO}_{4}$ for hot packs, and $\mathrm{NH}_{4} \mathrm{NO}_{3}$ for cold packs. When the pack is squeezed, the pouch breaks and the solid dissolves, either raising or lowering the temperature (Figure 11.3).

| Hot packs: | $\mathrm{CaCl}_{2}(s)$ | $\Delta H_{\text {soln }}=-81.3 \mathrm{~kJ} / \mathrm{mol}$ |
| :--- | :--- | :--- |
|  | $\mathrm{MgSO}_{4}(s)$ | $\Delta H_{\text {soln }}=-91.2 \mathrm{~kJ} / \mathrm{mol}$ |
| Cold packs: | $\mathrm{NH}_{4} \mathrm{NO}_{3}(s)$ | $\Delta H_{\text {soln }}=+25.7 \mathrm{~kJ} / \mathrm{mol}$ |



The value of the heat of solution for a substance results from an interplay of the three kinds of interactions mentioned earlier:

- Solvent-solvent interactions: Energy is required (positive $\Delta H$ ) to overcome intermolecular forces between solvent molecules because the molecules must be separated and pushed apart to make room for solute particles.
- Solute-solute interactions: Energy is required (positive $\Delta H$ ) to overcome intermolecular forces holding solute particles together in a crystal. For an ionic solid, this is the lattice energy (Section 6.6). Substances with higher lattice energies therefore tend to be less soluble than substances with lower lattice energies.
- Solvent-solute interactions: Energy is released (negative $\Delta H$ ) when solvent molecules cluster around solute particles and solvate them. For ionic substances in water, the amount of hydration energy released is generally greater for smaller cations than for larger ones because water molecules can approach the positive nuclei of smaller ions more closely and thus bind more tightly. In addition, hydration energy generally increases as the charge on the ion increases.

The first two kinds of interactions are endothermic, requiring an input of energy to spread apart solvent molecules and to break apart crystals. Only the third interaction is exothermic, as attractive intermolecular forces develop between solvent and solute particles. The sum of the three interactions determines whether $\Delta H_{\text {soln }}$ is endothermic or exothermic. For some substances, the one exothermic interaction is sufficiently large to outweigh the two endothermic interactions, but for other substances, the opposite is true (Figure 11.4).

4 FIGURE 11.3 (a) Dissolution of $\mathrm{CaCl}_{2}$ in water is exothermic, causing the temperature of the water to rise from its initial value of $25^{\circ} \mathrm{C}$. (b) Dissolution of $\mathrm{NH}_{4} \mathrm{NO}_{3}$ is endothermic, causing the temperature of the water to fall from its initial value.

VThe strength of an ion-dipole interaction increases and the hydration energy becomes more negative as the charge-toradius ratio of the ion increases.

FIGURE 11.4 The value of $\Delta H_{\text {soln }}$ is the sum of three terms: solvent-solvent, solutesolute, and solvent-solute. It can be either (a) negative or (b) positive.

(a) Negative $\Delta H_{\text {soln }}$

(b) Positive $\Delta H_{\text {soln }}$

## Worked Example 11.1

Pentane $\left(\mathrm{C}_{5} \mathrm{H}_{12}\right)$ and 1-butanol $\left(\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{OH}\right)$ are organic liquids with similar molecular masses, but their solubility properties differ substantially. Which of the two would you expect to be more soluble in water? Explain.

## Strategy

Look at the structures and decide on the kinds of intermolecular forces present between molecules. The substance with intermolecular forces similar to those in water will be more soluble in water.

## Solution

Pentane is a nonpolar molecule and is unlikely to have strong intermolecular interactions with polar water molecules. 1-Butanol, however, has an -OH group just as water does, and is therefore a polar molecule that can form hydrogen bonds with water. 1-Butanol is more soluble in water.


- PROBLEM 11.1 Arrange the following compounds in order of their expected increasing solubility in water: $\mathrm{Br}_{2}, \mathrm{KBr}$, toluene $\left(\mathrm{C}_{7} \mathrm{H}_{8}\right.$, a constituent of gasoline).
- PROBLEM 11.2 Which would you expect to have the larger (more negative) hydration energy?
(a) $\mathrm{Na}^{+}$or $\mathrm{Cs}^{+}$
(b) $\mathrm{K}^{+}$or $\mathrm{Ba}^{2+}$


### 11.3 Units of Concentration

In daily life, it's often sufficient to describe a solution as either dilute or concentrated. In scientific work, though, it's usually necessary to know the exact concentration of a solution-that is, to know the exact amount of solute dissolved in a given amount of solvent. There are many ways of expressing concentration, each of which has its own advantages and disadvantages. We'll look briefly at four of the most common methods: molarity, mole fraction, mass percent, and molality.

## Molarity (M)

The most common way of expressing concentration in a chemistry laboratory is to use molarity. As discussed previously in Section 3.7, a solution's molarity is given by the number of moles of solute per liter of solution (mol/L, abbreviated M). If,
for example, you dissolve $0.500 \mathrm{~mol}(20.0 \mathrm{~g})$ of NaOH in enough water to give 1.000 L of solution, then the solution has a concentration of 0.500 M .

$$
\text { Molarity }(\mathbf{M})=\frac{\text { Moles of solute }}{\text { Liters of solution }}
$$

The advantages of using molarity are twofold: (1) Stoichiometry calculations are simplified because numbers of moles are used rather than mass, and (2) amounts of solution (and therefore of solute) are measured by volume rather than by mass. As a result, titrations are particularly easy (Section 3.10).

The disadvantages of using molarity are also twofold: (1) The exact concentration depends on the temperature because the volume of a solution expands or contracts as the temperature changes, and (2) the exact amount of solvent in a given volume can't be determined unless the density of the solution is known. (Remember from Section 3.7 that solutions of a given molarity are prepared by dissolving a solute in a small amount of solvent and then diluting with solvent to the desired volume. The solution is not made by dissolving the solute in the desired volume of solvent.)

## Mole Fraction (X)

As discussed in Section 9.5, the mole fraction (X) of any component in a solution is given by the number of moles of the component divided by the total number of moles making up the solution (including solvent):

$$
\text { Mole fraction }(X)=\frac{\text { Moles of component }}{\text { Total moles making up the solution }}
$$

For example, a solution prepared by dissolving $1.00 \mathrm{~mol}(32.0 \mathrm{~g})$ of methyl alcohol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$ in $5.00 \mathrm{~mol}(90.0 \mathrm{~g})$ of water has a methyl alcohol concentration $X=1.00 \mathrm{~mol} /(1.00 \mathrm{~mol}+5.00 \mathrm{~mol})=0.167$. Note that mole fractions are dimensionless because the units cancel.

Mole fractions are independent of temperature and are particularly useful for calculations involving gas mixtures. Except in special situations, mole fractions are not often used for liquid solutions because other methods are generally more convenient.

## Mass Percent (mass \%)

As the name suggests, the mass percent of any component in a solution is the mass of that component divided by the total mass of the solution times $100 \%$ :

$$
\text { Mass percent }=\frac{\text { Mass of component }}{\text { Total mass of solution }} \times 100 \%
$$

For example, a solution prepared by dissolving 10.0 g of glucose in 100.0 g of water has a glucose concentration of 9.09 mass $\%$ :

$$
\text { Mass } \% \text { glucose }=\frac{10.0 \mathrm{~g}}{10.0 \mathrm{~g}+100.0 \mathrm{~g}} \times 100 \%=9.09 \text { mass } \%
$$

Closely related to mass percent, and particularly useful for very dilute solutions, are the concentration units parts per million ( $p p m$ ) and parts per billion ( $p p b$ ):

$$
\begin{aligned}
& \text { Parts per million }(\mathrm{ppm})=\frac{\text { Mass of component }}{\text { Total mass of solution }} \times 10^{6} \\
& \text { Parts per billion }(\mathrm{ppb})=\frac{\text { Mass of component }}{\text { Total mass of solution }} \times 10^{9}
\end{aligned}
$$

vMolarity contains a volume term in the denominator. As temperature increases, volume increases and molarity decreases. Mole fraction, mass percent, and molality contain no volume terms and are independent of temperature.

$\square$
Alvin D. White, "An Alternative Introduction to Mole Fraction," J. Chem. Educ., Vol. 59, 1982, 153.

Donald DeLorenzo, "Mole Fraction Analogies," J. Chem. Educ., Vol. 57, 1980, 733.

$\square$Clifton E. Meloan, Mindy L. Meloan, and John M. Meloan "Candy Sprinkles to Illustrate One Part per Million," J. Chem. Educ., Vol. 71, 1994, 658.

0In environmental applications parts per million is often taken to mean milligrams of solute per liter of aqueous solution, which seems to contradict the use of ppm as a tem-perature-independent unit. However, the mass of solute is negligible relative to the mass of water, so 1 L of water $\approx 1 \mathrm{~kg}$ of water $\approx 1 \mathrm{~kg}$ of solution.


- Dissolving a quarter teaspoon of table sugar in this swimming pool would give a concentration of about 1 ppb .

A concentration of 1 ppm for a substance means that each kilogram of solution contains 1 mg of the solute. For dilute aqueous solutions near room temperature, where 1 kg has a volume of $1 \mathrm{~L}, 1 \mathrm{ppm}$ also means that each liter of solution contains 1 mg of solute. In the same way, a concentration of 1 ppb means that each liter of an aqueous solution contains 0.001 mg of solute. Values in ppm and ppb are frequently used for expressing the concentrations of trace amounts of impurities in air or water. Thus, you might express the maximum allowable concentration of lead in drinking water as 50 ppb , or about 1 g per 20,000 L.

The advantage of using mass percent (or ppm) for expressing concentration is that the values are independent of temperature because masses don't change when substances are heated or cooled. The disadvantage of using mass percent is that it is generally more difficult when working with liquid solutions to measure amounts by mass rather than by volume. Furthermore, the density of a solution must be known before a concentration in mass percent can be converted into molarity. Worked Example 11.3 shows how to make the conversion.

## Worked Example 11.2

Assume that you have a 5.75 mass \% solution of LiCl in water. What mass of solution (in grams) contains 1.60 g of LiCl ?

## Strategy

Describing a concentration as 5.75 mass $\%$ means that 100.0 g of solution contains 5.75 g of LiCl , a relationship that can be used as a conversion factor.

## Solution

$$
\text { Mass of Soln }=1.60 \mathrm{~g} \mathrm{LiCl} \times \frac{100 \mathrm{~g} \text { soln }}{5.75 \mathrm{~g} \mathrm{LiCl}}=27.8 \mathrm{~g} \text { soln }
$$

## Worked Example 11.3

The density of a 25.0 mass \% solution of sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$ in water is $1.1783 \mathrm{~g} / \mathrm{mL}$ at $25.0^{\circ} \mathrm{C}$. What is the molarity of the solution?

## Strategy

Describing a solution as 25.0 mass \% sulfuric acid in water means that 100.0 g of solution contains 25.0 g of $\mathrm{H}_{2} \mathrm{SO}_{4}$ and 75.0 g of water. Since we want to calculate the concentration in molarity, we first need to find the number of moles of sulfuric acid dissolved in a specific mass of solution. We next use density as a conversion factor to find the volume of that solution and then calculate molarity by dividing the number of moles by the volume.

## Solution

First, convert the 25.0 g of $\mathrm{H}_{2} \mathrm{SO}_{4}$ into moles:

$$
\frac{\text { Moles } \mathrm{H}_{2} \mathrm{SO}_{4}}{100.0 \mathrm{~g} \text { solution }}=\frac{25.0 \mathrm{~g} \mathrm{H}_{2} \mathrm{SO}_{4}}{100.0 \mathrm{~g} \text { solution }} \times \frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}{98.1 \mathrm{~g} \mathrm{H}_{2} \mathrm{SO}_{4}}=\frac{0.255 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}{100.0 \mathrm{~g} \text { solution }}
$$

Next, find the volume of 100.0 g of solution, using density as the conversion factor:

$$
\text { Volume }=100.0 \mathrm{~g} \text { soln } \times \frac{1 \mathrm{~mL}}{1.1783 \mathrm{~g} \mathrm{soln}}=84.87 \mathrm{~mL}=0.08487 \mathrm{~L}
$$

Then, calculate the molarity of the solution:

$$
\text { Molarity }=\frac{\text { Moles } \mathrm{H}_{2} \mathrm{SO}_{4}}{\text { Liters of solution }}=\frac{0.255 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}{0.08487 \mathrm{~L}}=3.00 \mathrm{M}
$$

The molarity of the 25.0 mass $\%$ sulfuric acid solution is 3.00 M .

PROBLEM 11.3 What is the mass percent concentration of a saline solution prepared by dissolving 1.00 mol of NaCl in 1.00 L of water?

- PROBLEM 11.4 The legal limit for human exposure to carbon monoxide in the workplace is 35 ppm . Assuming that the density of air is $1.3 \mathrm{~g} / \mathrm{L}$, how many grams of carbon monoxide are in 1.0 L of air at the maximum allowable concentration?
- PROBLEM 11.5 Assuming that seawater is an aqueous solution of NaCl , what is its molarity? The density of seawater is $1.025 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$, and the NaCl concentration is 3.50 mass \%.


## Molality ( $m$ )

The molality of a solution is defined as the number of moles of solute per kilogram of solvent ( $\mathrm{mol} / \mathrm{kg}$ ):

$$
\text { Molality }(m)=\frac{\text { Moles of solute }}{\text { Mass of solvent }(\mathrm{kg})}
$$

To prepare a 1.000 m solution of KBr in water, for example, you would dissolve 1.000 mol of $\mathrm{KBr}(119.0 \mathrm{~g})$ in $1.000 \mathrm{~kg}(1000 \mathrm{~mL})$ of water. You can't say for sure what the final volume of the solution will be, although it will probably be a bit larger than 1000 mL . Although the names sound similar, note the differences between molarity and molality. Molarity is the number of moles of solute per volume (liter) of solution, whereas molality is the number of moles of solute per mass (kilogram) of solvent.

The main advantage of using molality is that it is temperature-independent because masses don't change when substances are heated or cooled. Thus, it is well suited for calculating certain properties of solutions that we'll discuss later in this chapter. The disadvantages of using molality are that amounts of solution must be measured by mass rather than by volume and that the density of the solution must be known to convert molality into molarity (see Worked Example 11.5).

A summary of the four methods of expressing concentration, together with a comparison of their relative advantages and disadvantages, is given in Table 11.3.

$\sigma$
Students tend to be careless in their use of units. Stress that concentration units refer to solute, solvent, or solution, and that it is helpful to include these terms as part of the unit. For example, molality ( $\mathrm{mol} / \mathrm{kg}$ ) means mol solute/kg solvent.

TABLE 11.3 A Comparison of Various Concentration Units

| Name | Units | Advantages | Disadvantages |
| :--- | :--- | :--- | :--- |
| Molarity (M) | mol solute | Useful in stoichiometry; <br> measure by volume | Temperature-dependent; must know <br> density to find solvent mass |
| Mole fraction $(X)$ | None | Temperature-independent; <br> useful in special applications | Measure by mass; must know <br> density to convert to molarity |
| Mass \% | $\%$ | Temperature-independent; <br> useful for small amounts | Measure by mass; must know <br> density to convert to molarity |
| Molality $(m)$ | mol solute | Temperature-independent; <br> useful in special applications | Measure by mass; must know <br> density to convert to molarity |

## Worked Example 11.4

What is the molality of a solution made by dissolving 1.45 g of table sugar (sucrose, $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$ ) in 30.0 mL of water? The molar mass of sucrose is $342.3 \mathrm{~g} / \mathrm{mol}$.

## Strategy

Molality is the number of moles of solute per kilogram of solvent. Thus, we need to find how many moles are in 1.45 g of sucrose and how many kilograms are in 30.0 mL of water.

## Solution

The number of moles of sucrose is

$$
1.45 \mathrm{~g} \text { sucrose } \times \frac{1 \mathrm{~mol} \text { sucrose }}{342.3 \mathrm{~g} \text { sucrose }}=4.24 \times 10^{-3} \mathrm{~mol} \text { sucrose }
$$

Since the density of water is $1.00 \mathrm{~g} / \mathrm{mL}, 30.0 \mathrm{~mL}$ of water has a mass of 30.0 g , or 0.0300 kg . Thus, the molality of the solution is

$$
\text { Molality }=\frac{4.24 \times 10^{-3} \mathrm{~mol}}{0.0300 \mathrm{~kg}}=0.141 \mathrm{~m}
$$

## Worked Example 11.5

Ethylene glycol, $\mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{OH})_{2}$, is a colorless liquid used as automobile antifreeze. If the density at $20^{\circ} \mathrm{C}$ of a 4.028 m solution of ethylene glycol in water is $1.0241 \mathrm{~g} / \mathrm{mL}$, what is the molarity of the solution? The molar mass of ethylene glycol is $62.07 \mathrm{~g} / \mathrm{mol}$.

## Strategy

A 4.028 m solution of ethylene glycol in water contains 4.028 mol of ethylene glycol per kilogram of water. To find the solution's molarity, we need to find the number of moles of solute per volume (liter) of solution. The volume, in turn, can be found from the mass of the solution by using density as a conversion factor.

## Solution

The mass of the solution is the sum of the masses of solute and solvent. Assuming that 1.000 kg of solvent is used to dissolve 4.028 mol of ethylene glycol, the mass of the ethylene glycol is

$$
\text { Mass of ethylene glycol }=4.028 \mathrm{~mol} \times 62.07 \frac{\mathrm{~g}}{\mathrm{~mol}}=250.0 \mathrm{~g}
$$

Dissolving this 250.0 g of ethylene glycol in 1.000 kg (or 1000 g ) of water gives the total mass of the solution:

$$
\text { Mass of solution }=250.0 \mathrm{~g}+1000 \mathrm{~g}=1250 \mathrm{~g}
$$

The volume of the solution is obtained from its mass by using density as a conversion factor:

$$
\text { Volume of solution }=1250 \mathrm{~g} \times \frac{1 \mathrm{~mL}}{1.0241 \mathrm{~g}}=1221 \mathrm{~mL}=1.221 \mathrm{~L}
$$

The molarity of the solution is the number of moles of solute divided by the volume of solution:

$$
\text { Molarity of solution }=\frac{4.028 \mathrm{~mol}}{1.221 \mathrm{~L}}=3.299 \mathrm{M}
$$

## Worked Example 11.6

A 0.750 M solution of $\mathrm{H}_{2} \mathrm{SO}_{4}$ in water has a density of $1.046 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$. What is the concentration of this solution in (a) mole fraction, (b) mass percent, and (c) molality? The molar mass of $\mathrm{H}_{2} \mathrm{SO}_{4}$ is $98.1 \mathrm{~g} / \mathrm{mol}$.

## Strategy and Solution

(a) Let's pick an arbitrary amount of the solution that will make the calculations easy, say 1.00 L . Since the concentration of the solution is $0.750 \mathrm{~mol} / \mathrm{L}$ and the density is $1.046 \mathrm{~g} / \mathrm{mL}$ (or $1.046 \mathrm{~kg} / \mathrm{L}$ ), 1.00 L of the solution contains $0.750 \mathrm{~mol}\left(73.6 \mathrm{~g}\right.$ ) of $\mathrm{H}_{2} \mathrm{SO}_{4}$ and has a mass of 1.046 kg :

$$
\begin{aligned}
& \text { Moles of } \mathrm{H}_{2} \mathrm{SO}_{4} \text { in } 1.00 \mathrm{~L} \text { soln }=0.750 \frac{\mathrm{~mol}}{\mathrm{~L}} \times 1.00 \mathrm{~L}=0.750 \mathrm{~mol} \\
& \text { Mass of } \mathrm{H}_{2} \mathrm{SO}_{4} \text { in } 1.00 \mathrm{~L} \text { soln }=0.750 \mathrm{~mol} \times 98.1 \frac{\mathrm{~g}}{\mathrm{~mol}}=73.6 \mathrm{~g} \\
& \text { Mass of } 1.00 \mathrm{~L} \text { soln }=1.00 \mathrm{~L} \times 1.046 \frac{\mathrm{~kg}}{\mathrm{~L}}=1.046 \mathrm{~kg}
\end{aligned}
$$

Subtracting the mass of $\mathrm{H}_{2} \mathrm{SO}_{4}$ from the total mass of the solution gives 0.972 kg of water, or 54.0 mol in 1.00 L of solution:

$$
\begin{aligned}
& \text { Mass of } \mathrm{H}_{2} \mathrm{O} \text { in } 1.00 \mathrm{~L} \text { soln }=(1.046 \mathrm{~kg})-(0.0736 \mathrm{~kg})=0.972 \mathrm{~kg} \mathrm{H}_{2} \mathrm{O} \\
& \text { Moles of } \mathrm{H}_{2} \mathrm{O} \text { in 1.00 } \mathrm{L} \text { of soln }=972 \mathrm{~g} \times \frac{1 \mathrm{~mol}}{18.0 \mathrm{~g}}=54.0 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}
\end{aligned}
$$

Thus, the mole fraction of $\mathrm{H}_{2} \mathrm{SO}_{4}$ is

$$
X_{\mathrm{H}_{2} \mathrm{SO}_{4}}=\frac{0.750 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}{0.750 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}+54.0 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}=0.0137
$$

(b) The mass percent concentration can be determined from the calculations in part (a):

$$
\text { Mass } \% \text { of } \mathrm{H}_{2} \mathrm{SO}_{4}=\frac{0.0736 \mathrm{~kg} \mathrm{H}_{2} \mathrm{SO}_{4}}{1.046 \mathrm{~kg} \text { total }} \times 100 \%=7.04 \%
$$

(c) The molality of the solution can also be determined from the calculations in part (a). Since 0.972 kg of water has 0.750 mol of $\mathrm{H}_{2} \mathrm{SO}_{4}$ dissolved in it, 1.00 kg of water would have 0.772 mol of $\mathrm{H}_{2} \mathrm{SO}_{4}$ dissolved in it:

$$
1.00 \mathrm{~kg} \mathrm{H}_{2} \mathrm{O} \times \frac{0.750 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}}{0.972 \mathrm{~kg} \mathrm{H}_{2} \mathrm{O}}=0.772 \mathrm{~mol} \mathrm{H}_{2} \mathrm{SO}_{4}
$$

Thus, the molality of the sulfuric acid solution is 0.772 m .

PROBLEM 11.6 What is the molality of a solution prepared by dissolving 0.385 g of cholesterol, $\mathrm{C}_{27} \mathrm{H}_{46} \mathrm{O}$, in 40.0 g of chloroform, $\mathrm{CHCl}_{3}$ ? What is the mole fraction of cholesterol in the solution?

PROBLEM 11.7 What mass (in grams) of a 0.500 m solution of sodium acetate, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}$, in water would you use to obtain 0.150 mol of sodium acetate?

- PROBLEM 11.8 The density at $20^{\circ} \mathrm{C}$ of a 0.258 m solution of glucose in water is $1.0173 \mathrm{~g} / \mathrm{mL}$, and the molar mass of glucose is 180.2 g . What is the molarity of the solution?
- PROBLEM 11.9 The density at $20^{\circ} \mathrm{C}$ of a 0.500 M solution of acetic acid in water is $1.0042 \mathrm{~g} / \mathrm{mL}$. What is the concentration of this solution in molality? The molar mass of acetic acid, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$, is 60.05 g .

PROBLEM 11.10 Assuming that seawater is a 3.50 mass \% aqueous solution of NaCl , what is the molality of seawater?

3Lee R. Summerlin, Christie. L Borgford, and Julie. B. Ealy, "Supersaturation," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 121-122. Excess solute suddenly precipitates from a supersaturated solution of sodium acetate trihydrate in this demonstration.

Jamil Ahmad, "Crystallization from a Supersaturated Solution of Sodium Acetate," J. Chem. Educ., Vol. 77, 2000, 1446.

FIGURE 11.5 A supersaturated solution of sodium acetate in water. When a tiny seed crystal is added, larger crystals begin to grow and precipitate from the solution until equilibrium is reached.

$\nabla$Solubility of solids in liquids is usually given in units of grams of solute per 100 mL of solvent. Because solubility changes with temperature, the temperature is also specified (usually $20^{\circ} \mathrm{C} \approx$ room temperature).

## 11.4 | Some Factors Affecting Solubility

If you take solid NaCl and add it to water, dissolution occurs rapidly at first but then slows down as more and more NaCl is added. Eventually the dissolution stops because a dynamic equilibrium is reached where the number of $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions leaving a crystal to go into solution is equal to the number of ions returning from the solution to the crystal. At this point, the solution is said to be saturated in that solute.

$$
\text { Solute }+ \text { Solvent } \underset{\text { Crystallize }}{\stackrel{\text { Dissolve }}{\rightleftharpoons}} \text { Solution }
$$

Note that this definition requires a saturated solution to be at equilibrium with undissolved solid. Substances that are more soluble at high temperature than at low temperature can sometimes form what are called supersaturated solutions, which contain a greater-than-equilibrium amount of solute. For example, when a saturated solution of sodium acetate is prepared at high temperature and then cooled slowly, a supersaturated solution results, as shown in Figure 11.5. Such a solution is unstable, however, and precipitation occurs when a tiny seed crystal of sodium acetate is added to initiate crystallization.


## Effect of Temperature on Solubility

The amount of solute per unit of solvent needed to form a saturated solution is called the solute's solubility. Like melting point and boiling point, the solubility of a substance in a given solvent is a physical property characteristic of that substance. Different substances can have greatly different solubilities, as shown in

Figure 11.6. Sodium chloride, for instance, has a solubility of $36.0 \mathrm{~g} / 100 \mathrm{~mL}$ of water at $20^{\circ} \mathrm{C}$, and sodium nitrate has a solubility of $87.6 \mathrm{~g} / 100 \mathrm{~mL}$ of water at $20^{\circ} \mathrm{C}$. Sometimes, particularly when two liquids are involved, the solvent and solute are miscible, meaning that they are mutually soluble in all proportions. A solution of ethyl alcohol and water is an example.


Solubilities are temperature-dependent, and the temperature at which a specific measurement is made must be reported. As Figure 11.6 shows, there is no obvious correlation between structure and solubility or between solubility and temperature. The solubilities of most molecular and ionic solids increase with increasing temperature, although the solubilities of some $(\mathrm{NaCl})$ are almost unchanged, and the solubilities of others $\left[\mathrm{Ce}_{2}\left(\mathrm{SO}_{4}\right)_{3}\right]$ decrease.

The effect of temperature on the solubility of gases is more predictable than its effect on the solubility of solids. Most gases (helium is the only common exception) become less soluble in water as the temperature increases (Figure 11.7). One consequence of this decreased solubility is that carbonated drinks bubble continuously as they warm up to room temperature after being refrigerated. Soon, they lose so much dissolved $\mathrm{CO}_{2}$ that they become "flat." A much more important consequence is the damage to aquatic life that can result from the decrease in concentration of

« FIGURE 11.6 Solubilities of some common solids in water as a function of temperature. Most substances become more soluble as temperature rises, although the exact relationship is often complex and nonlinear.
C. A. Snyder and D. C. Snyder, "Simple Soda Bottle Solubility and Equilibria," J. Chem. Educ., Vol. 69, 1992, 573. Bromocresol green indicator, added to a glass bottle of seltzer water, changes color from yellow to green to blue as carbon dioxide concentration is decreased. Observations are related to temperature and pressure effects on gas solubility, and LeChâtelier's principle is applied to the equilibria involved.

James H. Cragin, "Soft Drink Bubbles," J. Chem. Educ., Vol. 60, 1983, 71.

FIGURE 11.7 Solubilities of some gases in water as a function of temperature. Most gases become less soluble in water as the temperature rises. The concentration units are millimoles per liter ( $\mathrm{mmol} / \mathrm{L}$ ) at a gas pressure of 1 atm .


- Divers who ascend too quickly can develop the bends, a condition caused by the formation of nitrogen bubbles in the blood. Treatment involves placement in this high-pressure tank called a hyperbaric chamber, and a slow, controlled change to atmospheric pressure.

Bassam Z. Shakhashiri, "Effect of Temperature and Pressure on the Solubility of Gases in Liquids," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 280-282.

Doris R. Kimbrough,
"Henry's Law and Noisy Knuckles," J. Chem. Educ., Vol. 76, 1999, 1509-1510.

FIGURE 11.8 A molecular view of Henry's law. (a) At a given pressure, an equilibrium exists in which equal numbers of gas particles enter and leave the solution. (b) When pressure is increased by pushing on the piston, more gas particles are temporarily forced into solution than are able to leave, so solubility increases until a new equilibrium is reached (c).
dissolved oxygen in lakes and rivers when hot water is discharged from industrial plants, an effect known as thermal pollution.

## Effect of Pressure on Solubility

Pressure has practically no effect on the solubility of liquids and solids but has a profound effect on the solubility of gases. According to Henry's law, the solubility of a gas in a liquid at a given temperature is directly proportional to the partial pressure of the gas over the solution:

## Henry's law Solubility $=k \cdot P$

The constant $k$ in this expression is characteristic of a specific gas, and $P$ is the partial pressure of the gas over the solution. Doubling the partial pressure doubles the solubility, tripling the partial pressure triples the solubility, and so forth. Henry'slaw constants are usually given in units of $\mathrm{mol} /(\mathrm{L} \cdot \mathrm{atm})$, and measurements are reported at $25^{\circ} \mathrm{C}$. Note that at a gas partial pressure $P$ of 1 atm the Henry's-law constant $k$ is numerically equal to the solubility of the gas in moles per liter.

Perhaps the most common example of Henry's-law behavior occurs when you open a can of soda or other carbonated drink. Bubbles of gas immediately come fizzing out of solution because the pressure of $\mathrm{CO}_{2}$ in the can drops and $\mathrm{CO}_{2}$ suddenly becomes less soluble. A more serious example of Henry's-law behavior occurs when a deep-sea diver surfaces too quickly and develops a painful and life-threatening condition called the "bends." Bends occur because large amounts of nitrogen dissolve in the blood at high underwater pressures. When the diver ascends and pressure decreases too rapidly, bubbles of nitrogen form in the blood, blocking capillaries and inhibiting blood flow. The condition can be prevented by using an oxygen/helium mixture for breathing rather than air (oxygen/nitrogen), because helium has a much lower solubility in blood than nitrogen.

On a molecular level, the increase in gas solubility with increasing pressure occurs because of a change in the position of the equilibrium between dissolved and undissolved gas. At a given pressure, an equilibrium is established in which equal numbers of gas particles enter and leave the solution (Figure 11.8a). When the pressure is increased, however, more particles are forced into solution than leave it, so gas solubility increases until a new equilibrium is established (Figure $11.8 \mathrm{~b}-\mathrm{c}$ ).


## Worked Example 11.7

The Henry's-law constant of methyl bromide $\left(\mathrm{CH}_{3} \mathrm{Br}\right)$, a gas used as a soil fumigating agent, is $k=0.159 \mathrm{~mol} /(\mathrm{L} \cdot \mathrm{atm})$ at $25^{\circ} \mathrm{C}$. What is the solubility (in mol/L) of methyl bromide in water at $25^{\circ} \mathrm{C}$ and a partial pressure of 125 mm Hg ?

## Strategy

According to Henry's law, the solubility of a gas in water equals $k \cdot P$.

## Solution

$$
\begin{aligned}
& k=0.159 \mathrm{~mol} /(\mathrm{L} \cdot \mathrm{~atm}) \\
& P=125 \mathrm{~mm} \mathrm{Hg} \times \frac{1 \mathrm{~atm}}{760 \mathrm{~mm} \mathrm{Hg}}=0.164 \mathrm{~atm} \\
& \text { Solubility }=k \cdot P=0.159 \frac{\mathrm{~mol}}{\mathrm{~L} \cdot \mathrm{~atm}} \times 0.164 \mathrm{~atm}=0.0261 \mathrm{M}
\end{aligned}
$$

The solubility of methyl bromide in water at a partial pressure of 125 mm Hg is 0.0261 M .

- PROBLEM 11.11 The solubility of $\mathrm{CO}_{2}$ in water is $3.2 \times 10^{-2} \mathrm{M}$ at $25^{\circ} \mathrm{C}$ and 1 atm pressure. What is the Henry's-law constant for $\mathrm{CO}_{2}$ in $\mathrm{mol} /(\mathrm{L} \cdot \mathrm{atm})$ ?
- PROBLEM 11.12 The partial pressure of $\mathrm{CO}_{2}$ in air is approximately $4.0 \times 10^{-4}$ atm. Use the Henry's-law constant you calculated in Problem 11.11 to find the concentration of $\mathrm{CO}_{2}$ in:
(a) A can of soda under a $\mathrm{CO}_{2}$ pressure of 2.5 atm at $25^{\circ} \mathrm{C}$
(b) A can of soda open to the atmosphere at $25^{\circ} \mathrm{C}$


### 11.5 Physical Behavior of Solutions: Colligative Properties

The behavior of solutions is qualitatively similar to that of pure solvents but is quantitatively different. Pure water boils at $100.0^{\circ} \mathrm{C}$ and freezes at $0.0^{\circ} \mathrm{C}$, for example, but a 1.00 m (molal) solution of NaCl in water boils at $101.0^{\circ} \mathrm{C}$ and freezes at $-3.7^{\circ} \mathrm{C}$.

The elevation of boiling point and the lowering of freezing point that are observed on comparing a pure solvent with a solution are examples of colligative properties-properties that depend on the amount of a dissolved solute but not on its chemical identity. The word colligative means "bound together in a collection" and is used because a "collection" of solute particles is responsible for the observed effects. Other colligative properties are a decrease in vapor pressure of a solution compared with the pure solvent and osmosis, the migration of solvent and other small molecules through a semipermeable membrane.

In comparing the properties of a pure solvent with those of a solution...
Colligative
properties $\left\{\begin{array}{l}\text { Vapor pressure of solution is lower. } \\ \text { Boiling point of solution is higher. } \\ \text { Freezing point of solution is lower. } \\ \text { Osmosis, the migration of solvent molecules } \\ \text { through a semipermeable membrane, occurs } \\ \text { when solvent and solution are separated by } \\ \text { the membrane. }\end{array}\right.$

We'll look at each of the four colligative properties in more detail in Sections 11.6-11.8.

### 11.6 Vapor-Pressure Lowering of Solutions: Raoult's Law

Recall from Section 10.5 that a liquid in a closed container is in equilibrium with its vapor and that the amount of pressure exerted by the vapor is called the vapor pressure. When you compare the vapor pressure of a pure solvent with that of a solution at the same temperature, however, you find that the two values are different. If the solute is nonvolatile and has no appreciable vapor pressure of its own, as occurs when a solid is dissolved, then the vapor pressure of the solution is always lower than that of the pure solvent. If the solute is volatile and has a significant vapor pressure of its own, as often occurs in a mixture of two liquids, then the vapor pressure of the mixture is intermediate between the vapor pressures of the two pure liquids.

## Solutions with a Nonvolatile Solute

It's easy to demonstrate with manometers that a solution of a nonvolatile solute has a lower vapor pressure than the pure solvent (Figure 11.9). Alternatively, you can show the same effect by comparing the evaporation rate of pure solvent with the evaporation rate of a solution. A solution always evaporates more slowly than a pure solvent does, because its vapor pressure is lower and its molecules therefore escape less readily.

(a)

(b)
© FIGURE 11.9 The equilibrium vapor pressure of a solution with (a) a nonvolatile solute is always lower than that of (b) the pure solvent by an amount that depends on the mole fraction of the solvent.


According to Raoult's law, the vapor pressure of a solution containing a nonvolatile solute is equal to the vapor pressure of the pure solvent times the mole fraction of the solvent. That is,

$$
\mapsto \text { RaOULT'S LAW } \quad P_{\text {soln }}=P_{\text {solv }} \times X_{\text {solv }}
$$

where $P_{\text {soln }}$ is the vapor pressure of the solution, $P_{\text {solv }}$ is the vapor pressure of pure solvent at the same temperature, and $X_{\text {solv }}$ is the mole fraction of the solvent in the solution.

Take a solution of 1.00 mol of glucose in 15.0 mol of water at $25^{\circ} \mathrm{C}$, for instance. The vapor pressure of pure water at $25^{\circ} \mathrm{C}$ is 23.76 mm Hg , and the mole fraction of water in the solution is $15.0 \mathrm{~mol} /(1.0 \mathrm{~mol}+15.0 \mathrm{~mol})=0.938$. Thus, Raoult's law predicts a vapor pressure for the solution of $23.76 \mathrm{~mm} \mathrm{Hg} \times 0.938=22.3 \mathrm{~mm} \mathrm{Hg}$, which corresponds to a vapor-pressure lowering, $\Delta P_{\text {soln }}$, of 1.5 mm Hg :

Alternatively, the amount of vapor-pressure lowering can be calculated by multiplying the mole fraction of the solute times the vapor pressure of the pure solvent. That is,

$$
\begin{aligned}
\Delta P_{\text {soln }}=P_{\text {solv }} \times X_{\text {solute }} & =23.76 \mathrm{~mm} \mathrm{Hg} \times \frac{1.00 \mathrm{~mol}}{1.00 \mathrm{~mol}+15.0 \mathrm{~mol}} \\
& =1.5 \mathrm{~mm} \mathrm{Hg}
\end{aligned}
$$

If an ionic substance such as NaCl is the solute, we have to calculate mole fractions based on the total concentration of solute particles (ions) rather than NaCl formula units. A solution of 1.00 mol NaCl in 15.0 mol water at $25^{\circ} \mathrm{C}$, for example, contains 2.00 mol of dissolved particles (assuming complete dissociation), resulting in a mole fraction for water of 0.882 and a solution vapor pressure of 21.0 mm Hg .

$$
\begin{aligned}
& X_{\text {water }}=\frac{15.0 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}{1.00 \mathrm{~mol} \mathrm{Na}^{+}+1.00 \mathrm{~mol} \mathrm{Cl}^{-}+15.0 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}=0.882 \\
& P_{\text {soln }}=P_{\text {solv }} \times X_{\text {solv }}=23.76 \mathrm{~mm} \mathrm{Hg} \times 0.882=21.0 \mathrm{~mm} \mathrm{Hg}
\end{aligned}
$$

Note that because the mole fraction of water is smaller in the NaCl solution than in the glucose solution, the vapor pressure of the NaCl solution is lower: 21.0 mm Hg for NaCl versus 22.3 mm Hg for glucose at $25^{\circ} \mathrm{C}$.

Just as the ideal gas law discussed in Section 9.3 applies only to "ideal" gases, Raoult's law applies only to ideal solutions. Raoult's law approximates the behavior of most real solutions, but significant deviations from ideality occur as the solute concentration increases. The law works best when solute concentrations are low and when solute and solvent particles have similar intermolecular forces.

If the intermolecular forces between solute particles and solvent molecules are weaker than the forces between solvent molecules alone, then the solvent molecules are less tightly held in the solution and the vapor pressure is higher than Raoult's law predicts. Conversely, if the intermolecular forces between solute and solvent molecules are stronger than the forces between solvent molecules alone, then the solvent molecules are more tightly held in the solution and the vapor pressure is lower than predicted. Solutions of ionic substances, in particular, often have a vapor pressure significantly lower than predicted, because the ion-dipole forces between dissolved ions and polar water molecules are so strong.

A further complication is that ionic substances rarely dissociate completely, so a solution of an ionic compound usually contains fewer particles than the formula of the compound would suggest. The actual extent of dissociation can be expressed as a van't Hoff factor (i):

- van't Hoff factor $\quad i=\frac{\text { moles of particles in solution }}{\text { moles of solute dissolved }}$

To take a solution of NaCl as an example, the experimentally determined van't Hoff factor for 0.05 m NaCl is 1.9 , meaning that each mole of NaCl gives only 1.9 mol of particles rather than the 2.0 mol expected for complete dissociation. Of the 1.9 mol of particles, 0.1 mol is undissociated $\mathrm{NaCl}, 0.9 \mathrm{~mol}$ is $\mathrm{Cl}^{-}$, and 0.9 mol is $\mathrm{Na}^{+}$. Thus, NaCl is only $(0.9 / 1.0) \times 100 \%=90 \%$ dissociated, and the amount of vapor pressure lowering is less than expected.

What accounts for the lowering of the vapor pressure when a nonvolatile solute is dissolved in a solvent? As we've noted on numerous prior occasions, a physical process such as the vaporization of a liquid to a gas is accompanied by a free-energy change, $\Delta G_{\text {vap }}=\Delta H_{\text {vap }}-T \Delta S_{\text {vap }}$. The more negative the value of $\Delta G_{\text {vap }}$, the more favored the vaporization process. Thus, if we want to compare the ease of vaporization of a pure solvent with that of the solvent in a solution, we have to compare the signs and relative magnitudes of the $\Delta H_{\text {vap }}$ and $\Delta S_{\text {vap }}$ terms in the two cases.

FIGURE 11.10 The lower vapor pressure of a solution relative to that of a pure solvent is due to the difference in their entropies of vaporization, $\Delta S_{\text {vap. }}$. Because the entropy of the solvent in a solution is higher to begin with, $\Delta S_{\text {vap }}$ is smaller for the solution than for the pure solvent. As a result, vaporization of the solvent from the solution is less favored (less negative $\Delta G_{\text {vap }}$ ), and the vapor pressure of the solution is lower.

The vaporization of a liquid to a gas is disfavored by enthalpy (positive $\Delta H_{\text {vap }}$ ) because energy is required to overcome intermolecular attractions in the liquid. At the same time, however, vaporization is favored by entropy (positive $\Delta S_{\text {vap }}$ ) because molecular randomness increases when molecules go from a semi-ordered liquid state to a disordered gaseous state.

The heats of vaporization for a pure solvent and a solvent in a solution are similar because similar intermolecular forces must be overcome in both cases for solvent molecules to escape from the liquid. The entropies of vaporization for a pure solvent and a solvent in a solution are not similar, however. Because a solvent in a solution has more molecular disorder and higher entropy than a pure solvent does, the entropy change on going from liquid to vapor is smaller for the solvent in a solution than for the pure solvent. Subtracting a smaller $T \Delta S_{\text {vap }}$ from $\Delta H_{\text {vap }}$ thus results in a larger (more positive) $\Delta G_{\text {vap }}$ for the solution. As a result, vaporization is less favored for the solution, and the vapor pressure of the solution at equilibrium is lower (Figure 11.10).


## Worked Example 11.8

What is the vapor pressure (in mm Hg ) of a solution made by dissolving 18.3 g of NaCl in 500.0 g of $\mathrm{H}_{2} \mathrm{O}$ at $70^{\circ} \mathrm{C}$, assuming (a) complete dissociation and (b) a van't Hoff factor of 1.9? The vapor pressure of pure water at $70^{\circ} \mathrm{C}$ is 233.7 mm Hg .

## Strategy

According to Raoult's law, the vapor pressure of the solution equals the vapor pressure of pure solvent times the mole fraction of the solvent in the solution. Thus, we have to find the numbers of moles of solvent and solute and then calculate the mole fraction of solvent.

## Solution

(a) First, use molar mass to calculate the number of moles of NaCl and $\mathrm{H}_{2} \mathrm{O}$.

$$
\begin{aligned}
& \text { Moles of } \mathrm{NaCl}=18.3 \mathrm{~g} \mathrm{NaCl} \times \frac{1 \mathrm{~mol} \mathrm{NaCl}}{58.44 \mathrm{~g} \mathrm{NaCl}}=0.313 \mathrm{~mol} \mathrm{NaCl} \\
& \text { Moles of } \mathrm{H}_{2} \mathrm{O}=500.0 \mathrm{~g} \mathrm{H}_{2} \mathrm{O} \times \frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}{18.02 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}}=27.75 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}
\end{aligned}
$$

Next, calculate the mole fraction of water in the solution. Assuming that NaCl dissociates completely into two particles when dissolved in water, the solution contains 0.626 mol of dissolved particles: $0.313 \mathrm{~mol} \mathrm{Na}^{+}$ions and $0.313 \mathrm{~mol} \mathrm{Cl}^{-}$ions. Thus, the mole fraction of water is

$$
\text { Mole fraction of } \mathrm{H}_{2} \mathrm{O}=\frac{27.75 \mathrm{~mol}}{0.626 \mathrm{~mol}+27.75 \mathrm{~mol}}=0.9779
$$

From Raoult's law, the vapor pressure of the solution is

$$
P_{\text {soln }}=P_{\text {solv }} \times X_{\text {solv }}=233.7 \mathrm{~mm} \mathrm{Hg} \times 0.9779=228.5 \mathrm{~mm} \mathrm{Hg}
$$

(b) A van't Hoff factor of 1.9 means that the NaCl dissociates incompletely and gives only 1.9 particles per formula unit rather than 2 . Thus, the solution contains $1.9 \times 0.313 \mathrm{~mol}=0.59 \mathrm{~mol}$ of dissolved particles and the mole fraction of water is

$$
\text { Mole fraction of } \mathrm{H}_{2} \mathrm{O}=\frac{27.75 \mathrm{~mol}}{0.59 \mathrm{~mol}+27.75 \mathrm{~mol}}=0.9792
$$

From Raoult's law, the vapor pressure of the solution is

$$
P_{\text {soln }}=P_{\text {solv }} \times X_{\text {solv }}=233.7 \mathrm{~mm} \mathrm{Hg} \times 0.9792=228.8 \mathrm{~mm} \mathrm{Hg}
$$

## Worked Example 11.9

How many grams of sucrose must be added to 320 g of water to lower the vapor pressure by 1.5 mm Hg at $25^{\circ} \mathrm{C}$ ? The vapor pressure of water at $25^{\circ} \mathrm{C}$ is 23.8 mm Hg , and the molar mass of sucrose is $342.3 \mathrm{~g} / \mathrm{mol}$.

## Strategy

According to Raoult's law, $P_{\text {soln }}=P_{\text {solv }} \times X_{\text {solv }}$, which can be rearranged to the form $X_{\text {solv }}=P_{\text {soln }} / P_{\text {solv }}$. This equation can then be solved to find the number of moles of sucrose, and hence the number of grams.

## Solution

First, calculate the vapor pressure of the solution, $P_{\text {soln }}$, by subtracting the amount of vapor-pressure lowering from the vapor pressure of the pure solvent, $P_{\text {solv }}$ :

$$
P_{\text {soln }}=23.8 \mathrm{~mm} \mathrm{Hg}-1.5 \mathrm{~mm} \mathrm{Hg}=22.3 \mathrm{~mm} \mathrm{Hg}
$$

Now calculate the mole fraction of water, $X_{\text {solv }}$.

$$
\begin{array}{ll}
\text { Since } & P_{\text {soln }}=P_{\text {solv }} \times X_{\text {solv }} \\
\text { then } & X_{\text {solv }}=\frac{P_{\text {soln }}}{P_{\text {solv }}}=\frac{22.3 \mathrm{~mm} \mathrm{Hg}}{23.8 \mathrm{~mm} \mathrm{Hg}}=0.937
\end{array}
$$

This mole fraction of water is the number of moles of water divided by the total number of moles of sucrose plus water:

$$
X_{\text {solv }}=\frac{\text { Moles of water }}{\text { Total moles }}
$$

Since the number of moles of water is

$$
\text { Moles of water }=320 \mathrm{~g} \times \frac{1 \mathrm{~mol}}{18.0 \mathrm{~g}}=17.8 \mathrm{~mol}
$$

then the total number of moles of sucrose plus water is

$$
\text { Total moles }=\frac{\text { Moles of water }}{X_{\text {solv }}}=\frac{17.8 \mathrm{~mol}}{0.937}=19.0 \mathrm{~mol}
$$

Subtracting the number of moles of water from the total number of moles gives the number of moles of sucrose needed:

$$
\text { Moles of sucrose }=19.0 \mathrm{~mol}-17.8 \mathrm{~mol}=1.2 \mathrm{~mol}
$$

Converting moles into grams then gives the mass of sucrose needed:

$$
\text { Grams of sucrose }=1.2 \mathrm{~mol} \times 342.3 \frac{\mathrm{~g}}{\mathrm{~mol}}=4.1 \times 10^{2} \mathrm{~g}
$$



For a solution of a nonvolatile solid in a liquid, the vapor pressure of a solution is always lower than the vapor pressure of the pure solvent. For a solution of two volatile liquids, the vapor pressure is lower than the vapor pressure of the more volatile liquid and higher than the vapor pressure of the less volatile liquid.

PROBLEM 11.13 What is the vapor pressure (in mm Hg ) of a solution prepared by dissolving 5.00 g of benzoic acid $\left(\mathrm{C}_{7} \mathrm{H}_{6} \mathrm{O}_{2}\right)$ in 100.00 g of ethyl alcohol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}\right)$ at $35^{\circ} \mathrm{C}$ ? The vapor pressure of pure ethyl alcohol at $35^{\circ} \mathrm{C}$ is 100.5 mm Hg .

PROBLEM 11.14 How many grams of NaBr must be added to 250 g of water to lower the vapor pressure by 1.30 mm Hg at $40^{\circ} \mathrm{C}$ assuming complete dissociation? The vapor pressure of water at $40^{\circ} \mathrm{C}$ is 55.3 mm Hg .

- KEY CONCEPT PROBLEM 11.15 The following diagram shows a close-up view of part of the vapor-pressure curve for a pure solvent and a solution of a nonvolatile solute. Which curve represents the pure solvent, and which the solution?



## Solutions with a Volatile Solute

As you might expect from Dalton's law (Section 9.5), the overall vapor pressure $P_{\text {total }}$ of a mixture of two volatile liquids A and B is the sum of the vapor-pressure contributions of the individual components, $P_{\mathrm{A}}$ and $P_{\mathrm{B}}$ :

$$
P_{\text {total }}=P_{\mathrm{A}}+P_{\mathrm{B}}
$$

The individual vapor pressures $P_{\mathrm{A}}$ and $P_{\mathrm{B}}$ are calculated by Raoult's law. That is, the vapor pressure of $A$ is equal to the mole fraction of $A\left(X_{A}\right)$ times the vapor pressure of pure $\mathrm{A}\left(P_{\mathrm{A}}^{\circ}\right)$, and the vapor pressure of B is equal to the mole fraction of $\mathrm{B}\left(X_{\mathrm{B}}\right)$ times the vapor pressure of pure $\mathrm{B}\left(P^{\circ}{ }_{\mathrm{B}}\right)$. Thus, the total vapor pressure of the solution is

$$
P_{\text {total }}=P_{\mathrm{A}}+P_{\mathrm{B}}=\left(P_{\mathrm{A}}^{\circ} \cdot X_{\mathrm{A}}\right)+\left(P_{\mathrm{B}}^{\circ} \cdot X_{\mathrm{B}}\right)
$$

Take a mixture of the two similar organic liquids benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}, \mathrm{bp}=80.1^{\circ} \mathrm{C}\right)$ and toluene $\left(\mathrm{C}_{7} \mathrm{H}_{8}, \mathrm{bp}=110.6^{\circ} \mathrm{C}\right)$, for example. Pure benzene has a vapor pressure $P^{\circ}=96.0 \mathrm{~mm} \mathrm{Hg}$ at $25^{\circ} \mathrm{C}$, and pure toluene has $P^{\circ}=30.3 \mathrm{~mm} \mathrm{Hg}$ at the same temperature. In a 1:1 molar mixture of the two, where the mole fraction of each is $X=0.500$, the vapor pressure of the solution is 63.2 mm Hg :


$P_{\text {total }}=\left(P_{\text {benzene }}^{\circ}\right)\left(X_{\text {benzene }}\right)+\left(P_{\text {toluene }}^{\circ}\right)\left(X_{\text {toluene }}\right)$
$=(96.0 \mathrm{~mm} \mathrm{Hg} \times 0.500)+(30.3 \mathrm{~mm} \mathrm{Hg} \times 0.500)$
$=48.0 \mathrm{~mm} \mathrm{Hg}+15.2 \mathrm{~mm} \mathrm{Hg}=63.2 \mathrm{~mm} \mathrm{Hg}$
Note that the vapor pressure of the mixture is intermediate between the vapor pressures of the two pure liquids (Figure 11.11).


As with nonvolatile solutes, Raoult's law for a mixture of volatile liquids applies only to ideal solutions. Most real solutions show behavior that deviates slightly from the ideal in either a positive or negative way, depending on the kinds and strengths of intermolecular forces present in the solution.

## Worked Key Concept Example 11.10

The following diagram shows a close-up view of part of the vapor-pressure curves for two pure liquids and a mixture of the two. Which curves represent pure liquids, and which represents the mixture?


## Strategy and Solution

The vapor pressure of a mixture of two volatile liquids is always intermediate between the vapor pressures of the two pure liquids. Thus, the top (red) and bottom (blue) curves represent pure liquids, and the middle curve (green) represents the mixture.

## PROBLEM 11.16

(a) What is the vapor pressure (in mm Hg ) of a solution prepared by dissolving 25.0 g of ethyl alcohol $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right)$ in 100.0 g of water at $25^{\circ} \mathrm{C}$ ? The vapor pressure of pure water is 23.8 mm Hg , and the vapor pressure of ethyl alcohol is 61.2 mm Hg at $25^{\circ} \mathrm{C}$.
(b) What is the vapor pressure of the solution if 25.0 g of water is dissolved in 100.0 g of ethyl alcohol at $25^{\circ} \mathrm{C}$ ?

FIGURE 11.11 The vapor pressure of a solution of the two volatile liquids benzene and toluene at $25^{\circ} \mathrm{C}$ is the sum of the two individual contributions, each calculated by Raoult's law.


FIGURE 11.12 Phase diagrams for a pure solvent (red line) and a solution of a nonvolatile solute (green line). Because the vapor pressure of the solution is lower than that of the pure solvent at a given temperature, the temperature at which the vapor pressure reaches atmospheric pressure is higher for the solution than for the solvent. Thus, the boiling point of the solution is higher by an amount $\Delta T_{\mathrm{b}}$. Furthermore, because the liquid/vapor phase transition line is lower for the solution than for the solvent, the triplepoint temperature $T_{\mathrm{t}}$ is lower and the solid/liquid phase transition line is shifted to a lower temperature. As a result, the freezing point of the solution is lower than that of the pure solvent by an amount $\Delta T_{\mathrm{f}}$.

KEY CONCEPT PROBLEM 11.17 The following phase diagram shows part of the vapor-pressure curves for a pure liquid (green curve) and a solution of the first liquid with a second volatile liquid (red curve).

(a) Is the boiling point of the second liquid higher or lower than that of the first liquid?
(b) Draw on the diagram the approximate position of the vapor-pressure curve for the second liquid.

## 11.7 $\mid$ Boiling-Point Elevation and Freezing-Point Depression of Solutions

We saw in Section 10.5 that the vapor pressure of a liquid rises with increasing temperature and that the liquid boils when its vapor pressure equals atmospheric pressure. Because a solution of a nonvolatile solute has a lower vapor pressure than a pure solvent has at a given temperature, the solution must be heated to a higher temperature to cause it to boil. Furthermore, the lower vapor pressure of the solution means that the liquid/vapor phase transition line on a phase diagram is always lower for the solution than for the pure solvent. As a result, the triplepoint temperature $T_{\mathrm{t}}$ is lower for the solution, the solid/liquid phase transition line is shifted to a lower temperature for the solution, and the solution must be cooled to a lower temperature to freeze. Figure 11.12 shows the situation.


The boiling-point elevation of a solution relative to that of a pure solvent depends on the concentration of dissolved particles, just as vapor-pressure lowering does. Thus, a 1.00 m solution of glucose in water boils at $100.51^{\circ} \mathrm{C}$ at 1 atm pressure $\left(0.51^{\circ} \mathrm{C}\right.$ above normal), but a 1.00 m solution of NaCl in water boils at
$101.02^{\circ} \mathrm{C}\left(1.02^{\circ} \mathrm{C}\right.$ above normal) because there are twice as many particles (ions) dissolved in the NaCl solution as there are in the glucose solution.

The change in boiling point $\Delta T_{\mathrm{b}}$ for a solution is

$$
\Delta T_{\mathrm{b}}=K_{\mathrm{b}} \cdot m
$$

where $m$ is the molal (not molar) concentration of solute particles and $K_{\mathrm{b}}$ is the molal boiling-point-elevation constant characteristic of each liquid. The concentration must be expressed in molality-number of moles of solute particles per kilogram of solvent-rather than molarity so that the solute concentration is independent of temperature. Molal boiling-point-elevation constants are given in Table 11.4 for some common substances.

> TABLE $11.4 \quad \begin{aligned} & \text { Molal Boiling-Point-Elevation Constants }\left(K_{\mathrm{b}}\right) \text { and } \\ & \text { Molal Freezing-Point-Depression Constants }\left(K_{\mathrm{f}}\right)\end{aligned}$ for Some Common Substances

| Substance | $\mathbf{K}_{\mathbf{b}}$ <br> $\left[\left({ }^{\circ} \mathbf{C} \cdot \mathbf{k g}\right) / \mathbf{m o l}\right]$ | $\mathbf{K}_{\mathbf{f}}$ <br> $\left[\left({ }^{\circ} \mathbf{C} \cdot \mathbf{k g}\right) / \mathbf{m o l}\right]$ |
| :--- | :--- | :---: |
| Benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)$ | 2.53 | 5.12 |
| Camphor $\left(\mathrm{C}_{10} \mathrm{H}_{16} \mathrm{O}\right)$ | 5.95 | 37.7 |
| Chloroform $\left(\mathrm{CHCl}_{3}\right)$ | 3.63 | 4.70 |
| Diethyl ether $\left(\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}\right)$ | 2.02 | 1.79 |
| Ethyl alcohol $\left(\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}\right)$ | 1.22 | 1.99 |
| Water $\left(\mathrm{H}_{2} \mathrm{O}\right)$ | 0.51 | 1.86 |

The freezing-point depression of a solution relative to that of a pure solvent depends on the concentration of solute particles, just as boiling-point elevation does. For example, a 1.00 m solution of glucose in water freezes at $-1.86^{\circ} \mathrm{C}$, and a 1.00 m solution of NaCl in water freezes at $-3.72^{\circ} \mathrm{C}$. The change in freezing point $\Delta T_{\mathrm{f}}$ for a solution is

$$
\Delta T_{\mathrm{f}}=K_{\mathrm{f}} \bullet m
$$

where $m$ is the molal concentration of solute particles and $K_{f}$ is the molal freezing-point-depression constant characteristic of each solvent. Some molal freezing-point-depression constants are also given in Table 11.4.

As with vapor-pressure lowering (Section 11.6), the actual amount of boilingpoint elevation and freezing-point depression observed for solutions of ionic substances depends on the amount of dissociation, as given by a van't Hoff factor. The formulas for both boiling-point elevation and freezing-point depression can be modified to take dissociation into account:

$$
\begin{array}{ll}
\Delta T_{\mathrm{b}}=K_{\mathrm{b}} \cdot m \cdot i & \text { where } m \text { is the molal concentration of formula units } \\
\Delta T_{\mathrm{f}}=K_{\mathrm{f}} \cdot m \cdot i & \text { and } i \text { is the van't Hoff factor }
\end{array}
$$

The fundamental cause of boiling-point elevation and freezing-point depression in solutions is the same as the cause of vapor-pressure lowering (Section 11.6): the entropy difference between the pure solvent and the solvent in a solution. Let's take boiling-point elevations first. We know that liquid and vapor phases are in equilibrium at the boiling point ( $T_{\mathrm{b}}$ ) and that the free-energy difference between the two phases ( $\Delta G_{\text {vap }}$ ) is therefore zero (Section 8.14).

$$
\begin{array}{ll}
\text { Since } & \Delta G_{\text {vap }}=\Delta H_{\text {vap }}-T_{b} \Delta S_{\text {vap }}=0 \\
\text { then } & \Delta H_{\text {vap }}=T_{\mathrm{b}} \Delta S_{\text {vap }} \quad \text { and } \quad T_{\mathrm{b}}=\frac{\Delta H_{\text {vap }}}{\Delta S_{\text {vap }}}
\end{array}
$$

FIGURE 11.13 The higher boiling point of a solution relative to that of a pure solvent is due to a difference in their entropies of vaporization, $\Delta S_{\text {vap. }}$. Because the solvent in a solution has a higher entropy to begin with, $\Delta S_{\text {vap }}$ is smaller for the solution than for the pure solvent. As a result, the boiling point of the solution $T_{\mathrm{b}}$ is higher than that of the pure solvent.

Sarah F. McDuffie and Catherine E. Matthews, "Antifreeze Solutions: The Colligative Properties of Antifreeze," The Science Teacher, Vol. 63, 1996, 41-43.

Donald DeLorenzo, "FreezeProof Bugs," J. Chem. Educ., Vol. 58, 1981, 788.

FIGURE 11.14 The lower freezing point of a solution relative to that of a pure solvent is due to a difference in their entropies of fusion, $\Delta S_{\text {fusion }}$. Because the solvent in a solution has a higher entropy level to begin with, $\Delta S_{\text {fusion }}$ is larger for the solution than for the pure solvent. As a result, the freezing point of the solution $T_{f}$ is lower than that of the pure solvent.

In comparing the heats of vaporization $\left(\Delta H_{\text {vap }}\right)$ for a pure solvent and for a solvent in a solution, we find that the two values are similar because similar intermolecular forces holding the solvent molecules must be overcome in both cases. In comparing the entropies of vaporization, however, the two values are not similar. Because the solvent in a solution has more molecular randomness than a pure solvent has, the entropy change between solution and vapor is smaller than the entropy change between pure solvent and vapor. But if $\Delta S_{\text {vap }}$ is smaller for the solution, then $T_{\mathrm{b}}$ must be correspondingly larger. In other words, the boiling point of the solution $\left(T_{\mathrm{b}}\right)$ is higher than that of the pure solvent (Figure 11.13).
-



A similar explanation accounts for freezing-point depression. We know that liquid and solid phases are in equilibrium at the freezing point, so the free-energy difference between the phases $\left(\Delta G_{\text {fusion }}\right)$ is zero.

$$
\begin{array}{ll}
\text { Since } & \Delta G_{\text {fusion }}=\Delta H_{\text {fusion }}-T_{\mathrm{f}} \Delta S_{\text {fusion }}=0 \\
\text { then } & \Delta H_{\text {fusion }}=T_{\mathrm{f}} \Delta S_{\text {fusion }} \quad \text { and } \quad T_{\mathrm{f}}=\frac{\Delta H_{\text {fusion }}}{\Delta S_{\text {fusion }}}
\end{array}
$$

In comparing the solvent in a solution with a pure solvent, the heats of fusion ( $\left.\Delta H_{\text {fusion }}\right)$ are similar because similar intermolecular forces between solvent molecules are involved. The entropies of fusion ( $\Delta S_{\text {fusion }}$ ), however, are not similar. Because the solvent in a solution has more molecular randomness than a pure solvent has, the entropy change between the solvent in the solution and the solid is larger than the entropy change between pure solvent and the solid. With $\Delta S_{\text {fusion }}$ larger for the solution, $T_{\mathrm{f}}$ must be correspondingly smaller, meaning that the freezing point of the solution $\left(T_{\mathrm{f}}\right)$ is lower than that of the pure solvent (Figure 11.14).


## Worked Example 11.11

What is the molality of an aqueous glucose solution if the boiling point of the solution at 1 atm pressure is $101.27^{\circ} \mathrm{C}$ ? The molal boiling-point-elevation constant for water is given in Table 11.4.

## Strategy

Rearrange the equation for molal boiling-point elevation to solve for $m$ :

$$
\Delta T_{\mathrm{b}}=K_{\mathrm{b}} \cdot m \quad \text { so } \quad m=\frac{\Delta T_{\mathrm{b}}}{K_{\mathrm{b}}}
$$

where $K_{\mathrm{b}}=0.51\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$ and $\Delta T_{\mathrm{b}}=101.27^{\circ} \mathrm{C}-100.00^{\circ} \mathrm{C}=1.27^{\circ} \mathrm{C}$.

## Solution

$$
m=\frac{1.27^{\circ} \mathrm{C}}{0.51 \frac{{ }^{\circ} \mathrm{C} \cdot \mathrm{~kg}}{\mathrm{~mol}}}=2.5 \frac{\mathrm{~mol}}{\mathrm{~kg}}=2.5 \mathrm{~m}
$$

The molality of the solution is 2.5 m .

PROBLEM 11.18 What is the normal boiling point (in ${ }^{\circ} \mathrm{C}$ ) of a solution prepared by dissolving 1.50 g of aspirin (acetylsalicylic acid, $\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}_{4}$ ) in 75.00 g of chloroform $\left(\mathrm{CHCl}_{3}\right)$ ? The normal boiling point of chloroform is $61.7^{\circ} \mathrm{C}$, and $K_{\mathrm{b}}$ for chloroform is given in Table 11.4.

PROBLEM 11.19 What is the freezing point (in ${ }^{\circ} \mathrm{C}$ ) of a solution prepared by dissolving 7.40 g of $\mathrm{MgCl}_{2}$ in 110 g of water? The value of $K_{\mathrm{f}}$ for water is given in Table 11.4, and the van't Hoff factor for $\mathrm{MgCl}_{2}$ is $i=2.7$.

PROBLEM 11.20 Assuming complete dissociation, what is the molality of an aqueous solution of KBr whose freezing point is $-2.95^{\circ} \mathrm{C}$ ? The molal freezing-pointdepression constant of water is given in Table 11.4.

- PROBLEM 11.21 When 9.12 g of HCl was dissolved in 190 g of water, the freezing point of the solution was $-4.65^{\circ} \mathrm{C}$. What is value of the van't Hoff factor for HCl ?
- KEY CONCEPT PROBLEM 11.22 The following phase diagram shows a closeup view of the liquid/vapor phase transition boundaries for pure chloroform and a solution of a nonvolatile solute in chloroform.
(a) What is the approximate boiling point of pure chloroform?
(b) What is the approximate molal concentration of the nonvolatile solute? (See Table 11.4 to find $K_{\mathrm{b}}$ for chloroform.)



## $11.8 \mid$ Osmosis and Osmotic Pressure

Certain materials, including those that make up the membranes around living cells, are semipermeable. That is, they allow water or other small molecules to pass through, but they block the passage of large solute molecules or ions. When a solution and a pure solvent (or two solutions of different concentration) are separated by the right kind of semipermeable membrane, solvent molecules pass



A A cucumber (top) shrivels into a pickle (bottom) when immersed in salt water, because osmotic pressure drives water from the cucumber's cells.
through the membrane in a process called osmosis. Although the passage of solvent through the membrane takes place in both directions, passage from the pure solvent side to the solution side is more favored and occurs faster. As a result, the amount of liquid on the pure solvent side decreases, the amount of liquid on the solution side increases, and the concentration of the solution decreases.

Osmosis can be demonstrated with the experimental setup shown in Figure 11.15, in which a solution in the bulb is separated by a semipermeable membrane from pure solvent in the beaker. Solvent passes through the membrane from the beaker to the bulb, causing the liquid level in the attached tube to rise. The increased weight of liquid in the tube creates an increased pressure that pushes solvent back through the membrane until the rates of forward and reverse passage become equal and the liquid level stops rising. The amount of pressure necessary to achieve this equilibrium is called the osmotic pressure, $\Pi$ (Greek capital pi), of the solution. Osmotic pressures can be extremely high, even for relatively dilute solutions. The osmotic pressure of a 0.15 M NaCl solution at $25^{\circ} \mathrm{C}$, for example, is 7.3 atm , a value that will support a difference in water level of approximately 250 ft !


- FIGURE 11.15 The phenomenon of osmosis. A solution inside the bulb is separated from pure solvent in the beaker by a semipermeable membrane. Net passage of solvent from the beaker through the membrane occurs, and the liquid in the tube rises until an equilibrium is reached. At equilibrium, the osmotic pressure exerted by the column of liquid in the tube is sufficient to prevent further net passage of solvent.

The amount of osmotic pressure between solution and pure solvent depends on the concentration of solute particles in the solution according to the equation

$$
\Pi=\mathrm{M} R T
$$

where M is the molar concentration of solute particles, $R$ is the gas constant [0.082 $06(\mathrm{~L} \cdot \mathrm{~atm}) /(\mathrm{K} \cdot \mathrm{mol})]$, and $T$ is the temperature in kelvins. For example, a 1.00 M solution of glucose in water at 300 K has an osmotic pressure of 24.6 atm :

$$
\Pi=\mathrm{M} R T=1.00 \frac{\mathrm{~mol}}{\mathrm{~L}} \times 0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}} \times 300 \mathrm{~K}=24.6 \mathrm{~atm}
$$

Note that the solute concentration is given in molarity when calculating osmotic pressure rather than in molality. Because osmotic-pressure measurements are made at the specific temperature given in the equation $\Pi=M R T$, it's not necessary to express concentration in a temperature-independent unit such as molality.

Osmosis, like all colligative properties, results from an increase in entropy as pure solvent passes through the membrane and mixes with the solution. Perhaps the simplest explanation of osmosis is seen by looking at the molecular level (Figure 11.15). Solvent molecules on the solvent side of the membrane, because of their somewhat greater concentration, approach the membrane a bit more frequently than molecules on the solution side, thereby passing through more often.

## Worked Example 11.12

The total concentration of dissolved particles inside red blood cells is approximately 0.30 M , and the membrane surrounding the cells is semipermeable. What would the osmotic pressure (in atmospheres) inside the cells become if the cells were removed from blood plasma and placed in pure water at 298 K ?

## Strategy

If red blood cells were removed from the body and placed in pure water, water would pass through the cell membrane, causing an increase in pressure inside the cells. The amount of this pressure would be

$$
\Pi=\mathrm{M} R T
$$

where $\mathrm{M}=0.30 \mathrm{~mol} / \mathrm{L}, R=0.08206(\mathrm{~L} \cdot \mathrm{~atm}) /(\mathrm{K} \cdot \mathrm{mol}), T=298 \mathrm{~K}$.

## Solution

$$
\Pi=0.30 \frac{\mathrm{~mol}}{\mathrm{~L}} \times 0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}} \times 298 \mathrm{~K}=7.3 \mathrm{~atm}
$$

The buildup of internal pressure would cause the blood cells to burst.

## Worked Example 11.13

A solution of an unknown substance in water at 293 K gives rise to an osmotic pressure of 5.66 atm . What is the molarity of the solution?

## Strategy

We are given values for $\Pi$ and $T$, and we need to solve for $M$ in the equation $\Pi=M R T$. Rearranging this equation, we get

$$
M=\frac{\Pi}{R T}
$$

where $\Pi=5.66 \mathrm{~atm}, R=0.08206(\mathrm{~L} \cdot \mathrm{~atm}) /(\mathrm{K} \cdot \mathrm{mol})$, and $T=293 \mathrm{~K}$.

## Solution

$$
\mathrm{M}=\frac{5.66 \mathrm{~atm}}{0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}} \times 293 \mathrm{~K}}=0.235 \mathrm{M}
$$


© Osmotic pressure is responsible for the rise of sap in tall trees.

Joseph G. Morse and Ed Vitz, "A Simple Demonstration Model of Osmosis," J. Chem. Educ., Vol. 76, 1999, 64-65.

Bassam Z. Shakhashiri,
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Lee R. Summerlin, Christie. L. Borgford, and Julie. B. Ealy, "Osmosis and the Egg Membrane," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 136-137.


A Fresh water is obtained from seawater by desalination using reverse osmosis.

Gerald Parkinson, Charlene Crabb, and Takeshi Kamiya, "Seawater Gets Fresh," Chem. Eng., Vol. 106(3), 1999, 32-35. Desalination by reverse osmosis.

- PROBLEM 11.23 What osmotic pressure (in atmospheres) would you expect for a solution of $0.125 \mathrm{M} \mathrm{CaCl}_{2}$ that is separated from pure water by a semipermeable membrane at 310 K ? Assume $100 \%$ dissociation for $\mathrm{CaCl}_{2}$.
- PROBLEM 11.24 A solution of an unknown substance in water at 300 K gives rise to an osmotic pressure of 3.85 atm . What is the molarity of the solution?


## 11.9 | Some Uses of Colligative Properties

We use colligative properties in many ways, both in the chemical laboratory and in day-to-day life. Motorists in winter, for instance, take advantage of freezingpoint lowering when they drive on streets where the snow has been melted by a sprinkling of salt. The antifreeze added to automobile radiators and the de-icer solution sprayed on airplane wings also work by lowering the freezing point of water. That same automobile antifreeze keeps radiator water from boiling over in summer by raising its boiling point.

One of the more interesting uses of colligative properties is the desalination of seawater by reverse osmosis. When pure water and seawater are separated by a membrane, the passage of water molecules from the pure side to the solution side is faster than passage in the reverse direction. As osmotic pressure builds up, though, the rates of forward and reverse water passage eventually become equal at an osmotic pressure of about 30 atm at $25^{\circ} \mathrm{C}$. If a pressure even greater than 30 atm is now applied to the solution side, the reverse passage of water becomes favored. As a result, pure water can be obtained from seawater (Figure 11.16).


A FIGURE 11.16 A schematic for the desalination of seawater by reverse osmosis. By applying a pressure on the seawater that is greater than osmotic pressure, water is forced through the osmotic membrane from the seawater side to the pure water side.

The most important use of colligative properties in the laboratory is for determining the molecular mass of an unknown substance. Any of the four colligative properties we've discussed can be used, but the most accurate values are obtained from osmotic-pressure measurements because the magnitude of the osmosis effect is so great. For example, a solution of 0.0200 M glucose in water at 300 K will give an osmotic-pressure reading of 374.2 mm Hg , a value that can easily be read to four significant figures. The same solution, however, will lower the freezing point by only $0.04^{\circ} \mathrm{C}$, a value that can be read to only one significant figure. Worked Example 11.14 shows how osmotic pressure can be used to find molecular mass.

A solution prepared by dissolving 20.0 mg of insulin in water and diluting to a volume of 5.00 mL gives an osmotic pressure of 12.5 mm Hg at 300 K . What is the molecular mass of insulin?

## Strategy

To determine molecular mass, we need to know the number of moles of insulin represented by the 20.0 mg sample. We can do this by first rearranging the equation for osmotic pressure to find the molar concentration of the insulin solution and then multiplying by the volume of the solution to obtain the number of moles of insulin.

## Solution

$$
\begin{aligned}
& \text { Since } \quad \Pi=\mathrm{MRT}, \quad \text { then } \quad \mathrm{M}=\frac{\Pi}{R T} \\
& \mathrm{M}=\frac{12.5 \mathrm{~mm} \mathrm{Hg} \times \frac{1 \mathrm{~atm}}{760 \mathrm{~mm} \mathrm{Hg}}}{0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}} \times 300 \mathrm{~K}}=6.68 \times 10^{-4} \mathrm{M}
\end{aligned}
$$

Since the volume of the solution is 5.00 mL , the number of moles of insulin is

$$
\text { Moles insulin }=6.68 \times 10^{-4} \frac{\mathrm{~mol}}{\mathrm{~L}} \times \frac{1 \mathrm{~L}}{1000 \mathrm{~mL}} \times 5.00 \mathrm{~mL}=3.34 \times 10^{-6} \mathrm{~mol}
$$

Knowing both the mass and the number of moles of insulin, we can calculate the molar mass and hence the molecular mass:

$$
\text { Molar mass }=\frac{\text { mass of insulin }}{\text { moles of insulin }}=\frac{0.0200 \mathrm{~g} \text { insulin }}{3.34 \times 10^{-6} \mathrm{~mol} \mathrm{insulin}}=5990 \mathrm{~g} / \mathrm{mol}
$$

The molecular mass of insulin is 5990 amu .
PROBLEM 11.25 A solution of 0.250 g of naphthalene (mothballs) in 35.00 g of camphor lowers the freezing point by $2.10^{\circ} \mathrm{C}$. What is the molar mass of naphthalene? The freezing-point-depression constant for camphor is $37.7\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.

- PROBLEM 11.26 What is the molar mass of sucrose (table sugar) if a solution prepared by dissolving 0.822 g of sucrose in 300.0 mL of water has an osmotic pressure of 149 mm Hg at 298 K ?


### 11.10 | Fractional Distillation of Liquid Mixtures

Perhaps the most commercially important of all applications of colligative properties is in the refining of petroleum to make gasoline. Petroleum refineries appear as a vast maze of pipes, tanks, and towers. The pipes, though, are just for transferring the petroleum or its products, and the tanks are just for storage. It's in the towers that the separation of crude petroleum into usable fractions takes place. As we saw in Section 8.12, petroleum is a complex mixture of hydrocarbon molecules that are refined by distillation into different fractions: straight-run gasoline (bp $30-200^{\circ} \mathrm{C}$ ), kerosene (bp $175-300^{\circ} \mathrm{C}$ ), and gas oil (bp $275-400^{\circ} \mathrm{C}$ ).

Called fractional distillation, this separation of petroleum into fractions occurs when a mixture of volatile liquids is boiled and the vapors are condensed. Because the vapor is enriched in the component with the higher vapor pressure according to Raoult's law (Section 11.6), the condensed vapors are also enriched in


A Distillation of petroleum into fractions according to boiling point is carried out in the large towers of this refinery.
that component, and a partial purification can be effected. If the boil/condense cycle is repeated a large number of times, complete purification of the more volatile liquid component can be achieved.

Let's look at the separation by fractional distillation of a 1:1 molar mixture of benzene and toluene. If we begin by heating the mixture, boiling occurs when the sum of the vapor pressures equals atmospheric pressure-that is, when $X \cdot P^{\circ}{ }_{\text {benzene }}+X \cdot P^{\circ}{ }_{\text {toluene }}=760 \mathrm{~mm} \mathrm{Hg}$. Reading from the vapor-pressure curves in Figure 11.17 (or calculating values with the Clausius-Clapeyron equation as discussed in Section 10.5), we find that boiling occurs at $365.3 \mathrm{~K}\left(92.2^{\circ} \mathrm{C}\right)$, where $P_{\text {benzene }}^{\circ}=1084 \mathrm{~mm} \mathrm{Hg}$ and $P_{\text {toluene }}^{\circ}=436 \mathrm{~mm} \mathrm{Hg}$ :

$$
\begin{aligned}
P_{\text {mixt }} & =X \cdot P^{\circ}{ }_{\text {benzene }}+X \cdot P_{\text {toluene }}^{\circ} \\
& =(0.5000)(1084 \mathrm{~mm} \mathrm{Hg})+(0.5000)(436 \mathrm{~mm} \mathrm{Hg}) \\
& =542 \mathrm{~mm} \mathrm{Hg}+218 \mathrm{~mm} \mathrm{Hg} \\
& =760 \mathrm{~mm} \mathrm{Hg}
\end{aligned}
$$



- FIGURE 11.17 Vapor-pressure curves for pure benzene (blue), pure toluene (red), and a 1:1 mixture of the two (green). The mixture boils at $92.2^{\circ} \mathrm{C}(365.3 \mathrm{~K})$ at atmospheric pressure.

Although the starting liquid mixture of benzene and toluene has a 1:1 molar composition, the composition of the vapor is not 1:1. Of the 760 mm Hg total vapor pressure for the boiling mixture, $542 / 760=71.3 \%$ is due to benzene and $218 / 760=28.7 \%$ is due to toluene. If we now condense the vapor, the liquid we get has this same 71.3:28.7 composition. On boiling this new liquid mixture, the composition of the vapor now becomes $86.4 \%$ benzene and $13.6 \%$ toluene. A third condense/boil cycle brings the composition of the vapor to $94.4 \%$ benzene $/ 5.6 \%$ toluene, and so on through further cycles until the desired level of purity is reached.

Fractional distillation can be represented on a liquid/vapor phase diagram by plotting temperature versus composition, as shown in Figure 11.18. The lower region of the diagram represents the liquid phase, and the upper region represents the vapor phase. Between the two is a thin equilibrium region where liquid and vapor coexist.

To understand how the diagram works, let's imagine starting with the $50: 50$ benzene/toluene mixture and heating it to its boiling point $\left(92.2^{\circ} \mathrm{C}\right.$ on the diagram). The lower curve represents the liquid composition ( $50: 50$ ), but the upper curve represents the vapor composition (approximately 71:29 at $92.2^{\circ} \mathrm{C}$ ). The two points are connected by a short horizontal line called a tie line to indicate that the


- FIGURE 11.18 A phase diagram of temperature versus composition (mole fraction) for a mixture of benzene and toluene. Liquid composition is given by the lower curve, and vapor composition is given by the top curve. The thin region between curves represents an equilibrium between phases. Liquid and vapor compositions at a given temperature are connected by a horizontal tie line, as explained in the text.
temperature is the same at both points. Condensing the 71:29 vapor mixture by lowering the temperature gives a 71:29 liquid mixture that, when heated to its boiling point $\left(86.6^{\circ} \mathrm{C}\right)$, has an $86: 14$ vapor composition, as represented by another tie line. In essence, fractional distillation is simply a walk across successive tie lines in whatever number of steps is necessary to reach the desired purity.

In practice, the successive boil/condense cycles occur naturally in the distillation column, and there is no need to isolate liquid mixtures at intermediate stages of purification. Fractional distillation is therefore relatively simple to carry out and is routinely used on a daily basis in chemical plants and laboratories throughout the world (Figure 11.19).


4 FIGURE 11.19 A simple fractional distillation column used in a chemistry laboratory. The vapors from a boiling mixture of liquids rise inside the column, where they condense on contact with the cool column walls, drip back, and are reboiled by contact with more hot vapor. Numerous boil/condense cycles occur before vapors finally pass out the top of the column, reach the water-cooled condenser, and drip into the receiver.

KEY CONCEPT PROBLEM 11.27 The following graph is a phase diagram of temperature versus composition for mixtures of the two liquids chloroform and dichloromethane.

(a) Label the regions on the diagram corresponding to liquid and vapor.
(b) Assume that you begin with a mixture of $60 \%$ chloroform and $40 \%$ dichloromethane. At what approximate temperature will the mixture begin to boil? Mark as point $a$ on the diagram the liquid composition at the boiling point, and mark as point $b$ the vapor composition at the boiling point.
(c) Assume that the vapor at point $b$ condenses and is reboiled. Mark as point $c$ on the diagram the liquid composition of the condensed vapor and as point $d$ on the diagram the vapor composition of the reboiled material.
(d) What will the approximate composition of the liquid be after carrying out two cycles of boiling and condensing?

## Interlude

## Dialysis



- Hemodialysis on this artificial kidney blood of patients whose Hemodianses the blooned.
machine clean malfunctioned.
kidneys have
- PROBLEM 11.28 What is the difference between a dialysis membrane and the typical semipermeable membrane used for osmosis?


## Summary

Solutions are homogeneous mixtures that contain particles the size of a typical ion or small molecule. Any one state of matter can mix with any other state, leading to seven possible kinds of solutions. For solutions in which a gas or solid is dissolved in a liquid, the dissolved substance is called the solute and the liquid is called the solvent.

The dissolution of a solute in a solvent has associated with it a free-energy change, $\Delta G=\Delta H-T \Delta S$. The enthalpy change is the heat of solution ( $\Delta H_{\text {soln }}$ ), and the entropy change is the entropy of solution ( $\Delta S_{\text {soln }}$ ). Heats of solution can be either positive or negative, depending on the relative strengths of solvent-solvent, solute-solute, and solventsolute intermolecular forces. Entropies of solution are usually positive because disorder increases when a pure solute dissolves in a pure solvent.

The concentration of a solution can be expressed in many ways, including molarity (moles of solute per liter of solution), mole fraction (moles of solute per mole of solution), mass percent (mass of solute per mass of solution times $100 \%$ ), and molality (moles of solute per kilogram of solvent). When equilibrium is reached and no further solute dissolves in a given amount of solvent, a solution is said to be saturated. The concentration at this point represents the
solubility of the solute. Solubilities are usually temperaturedependent, although often not in a simple way. Gas solubilities usually decrease with increasing temperature, but the solubilities of solids can either increase or decrease. The solubilities of gases also depend on pressure. According to Henry's law, the solubility of a gas in a liquid at a given temperature is proportional to the partial pressure of the gas over the solution.

In comparison with a pure solvent, a solution has a lower vapor pressure at a given temperature, a lower freezing point, and a higher boiling point. In addition, a solution that is separated from solvent by a semipermeable membrane gives rise to the phenomenon of osmosis. All four of these properties of solutions depend only on the concentration of dissolved solute rather than on the chemical identity of the solute and are therefore called colligative properties. The fundamental cause of all colligative properties is the same: the higher entropy of the solvent in a solution relative to that of the pure solvent.

Colligative properties have many practical uses, including the melting of snow by salt, the desalination of seawater by reverse osmosis, the separation and purification of volatile liquids by fractional distillation, and the determination of molecular mass by osmotic pressure measurement.

## Key Words

colligative property 443
colloid 430
entropy of solution $\left(\Delta S_{\text {soln }}\right) 432$
fractional distillation 457
heat of solution ( $\Delta H_{\text {soln }}$ ) 432
Henry's law 442
mass percent (mass \%) 435
miscible 441
molal boiling-pointelevation constant ( $K_{\mathrm{b}}$ ) 451
molal freezing-pointdepression constant ( $K_{\mathrm{f}}$ ) 451
molality (m) 437
molarity (M) 435
mole fraction (X) 435
osmosis 454

## osmotic pressure (П)

 454 parts per billion (ppb) 435parts per million (ppm) 435
Raoult's law 444
reverse osmosis 456
saturated 440
solubility 440
solute 430
solution 430
solvent 430
supersaturated 440
van't Hoff factor (i) 445


## Understanding Key Concepts

Problems 11.1-11.28 appear within the chapter.
11.29 The following phase diagram shows part of the liquid/vapor phase-transition boundaries for pure ether and a solution of a nonvolatile solute in ether.

(a) What is the approximate normal boiling point of pure ether?
(b) What is the approximate molal concentration of the solute? [ $K_{\mathrm{b}}$ for ether is $2.02\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.]
11.30 Rank the situations represented by the following drawings according to increasing entropy.

(c)
11.31 The following diagram shows a close-up view of part of the vapor-pressure curves for a solvent (red curve) and a solution of the solvent with a second liquid (green curve). Is the second liquid more volatile or less volatile than the solvent?

11.32 Assume that two liquids are separated by a semipermeable membrane. Make a drawing that shows the situa-
 tion after equilibrium is reached.

11.33 Assume that you are distilling a 1:1 molar mixture of chloroform $\left(\mathrm{CHCl}_{3} ; \mathrm{bp}=61.7^{\circ} \mathrm{C}\right)$ and tetrachloromethane $\left(\mathrm{CCl}_{4} ; \mathrm{bp}=76.5^{\circ} \mathrm{C}\right)$. After the mixture has been heated to its boiling point and vapor has reached the top of the column, predict the approximate temperatures at the three points indicated.

11.34 Two beakers, one with pure water (blue) and the other with a solution of NaCl in water (green), are placed in a closed container as represented by drawing (a). Which of the drawings (b)-(d) represents what the beakers will look like after a substantial amount of time has passed?

(a)

(c)

(b)

(d)

## Additional Problems

## Solutions and Energy Changes

11.36 If a single 5 g block of NaCl is placed in water, it dissolves slowly, but if 5 g of powdered NaCl is placed in water, it dissolves rapidly. Explain.
11.37 Give an example of each of the following kinds of solutions:
(a) A gas in a liquid
(b) A solid in a solid
(c) A liquid in a solid
11.38 Explain the solubility rule of thumb "like dissolves like" in terms of the intermolecular forces that occur in solutions.
11.39 $\mathrm{Br}_{2}$ is much more soluble in tetrachloromethane, $\mathrm{CCl}_{4}$, than in water. Explain.
11.40 Why do ionic substances with higher lattice energies tend to be less soluble in water than substances with lower lattice energies?
11.41 Which would you expect to have the larger hydration energy, $\mathrm{SO}_{4}{ }^{2-}$ or $\mathrm{ClO}_{4}{ }^{-}$? Explain.
11.35 A phase diagram of temperature versus composition for a mixture of the two volatile liquids octane ( $\mathrm{bp}=69^{\circ} \mathrm{C}$ ) and decane ( $\mathrm{bp}=126^{\circ} \mathrm{C}$ ) is shown. Assume that you begin with a mixture containing 0.60 mol of decane and 0.40 mol of octane.

(a) What region on the diagram corresponds to vapor, and what region corresponds to liquid?
(b) At what approximate temperature will the mixture begin to boil? Mark as point $a$ on the diagram the liquid composition at the boiling point, and mark as point $b$ the vapor composition at the boiling point.
(c) Assume that the vapor at point $b$ condenses and is reboiled. Mark as point $c$ on the diagram the liquid composition of the condensed vapor and as point $d$ on the diagram the vapor composition of the reboiled material.

## Units of Concentration

11.46 What is the difference between molarity and molality?
11.47 What is the difference between a saturated and a supersaturated solution?
11.48 How would you prepare each of the following solutions?
(a) A 0.150 M solution of glucose in water
(b) A 1.135 m solution of KBr in water
(c) A solution of methyl alcohol and water in which $\mathrm{X}_{\mathrm{CH}_{3} \mathrm{OH}}=0.15$ and $\mathrm{X}_{\mathrm{H}_{2} \mathrm{O}}=0.85$
11.49 How would you prepare each of the following solutions?
(a) 100 mL of a 155 ppm solution of urea, $\mathrm{CH}_{4} \mathrm{~N}_{2} \mathrm{O}$, in water
(b) 100 mL of an aqueous solution whose $\mathrm{K}^{+}$concentration is 0.075 M
11.50 How would you prepare 165 mL of a 0.0268 M solution of benzoic acid $\left(\mathrm{C}_{7} \mathrm{H}_{6} \mathrm{O}_{2}\right)$ in chloroform $\left(\mathrm{CHCl}_{3}\right)$ ?
11.51 How would you prepare 165 mL of a 0.0268 m solution of benzoic acid $\left(\mathrm{C}_{7} \mathrm{H}_{6} \mathrm{O}_{2}\right)$ in chloroform $\left(\mathrm{CHCl}_{3}\right)$ ?
11.52 Which of the following solutions is more concentrated?
(a) 0.500 M KCl or 0.500 mass $\% \mathrm{KCl}$ in water
(b) 1.75 M glucose or 1.75 m glucose in water
11.53 Which of the following solutions has the higher molarity?
(a) 10 ppm KI in water or $10,000 \mathrm{ppb} \mathrm{KBr}$ in water
(b) 0.25 mass $\% \mathrm{KCl}$ in water or 0.25 mass $\%$ citric acid $\left(\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{7}\right)$ in water
11.54 What is the mass percent concentration of the following solutions?
(a) Dissolve 0.655 mol of citric acid, $\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{7}$, in 1.00 kg of water.
(b) Dissolve 0.135 mg of KBr in 5.00 mL of water.
(c) Dissolve 5.50 g of aspirin, $\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}_{4}$, in 145 g of dichloromethane, $\mathrm{CH}_{2} \mathrm{Cl}_{2}$.
11.55 What is the molality of each solution prepared in Problem 11.54?
11.56 The so-called ozone layer in the earth's stratosphere has an average total pressure of $10 \mathrm{~mm} \mathrm{Hg}\left(1.3 \times 10^{-2} \mathrm{~atm}\right)$. The partial pressure of ozone in the layer is about $1.2 \times 10^{-6} \mathrm{~mm} \mathrm{Hg}\left(1.6 \times 10^{-9} \mathrm{~atm}\right)$. What is the concentration of ozone (in parts per million), assuming that the average molar mass of air is $29 \mathrm{~g} / \mathrm{mol}$ ?
11.57 Persons are medically considered to have lead poisoning if they have a concentration of greater than 10 micrograms of lead per deciliter of blood. What is this concentration in parts per billion?
11.58 What is the concentration of each of the following solutions?
(a) The molality of a solution prepared by dissolving 25.0 g of $\mathrm{H}_{2} \mathrm{SO}_{4}$ in 1.30 L of water
(b) The mole fraction of each component of a solution prepared by dissolving 2.25 g of nicotine, $\mathrm{C}_{10} \mathrm{H}_{14} \mathrm{~N}_{2}$, in 80.0 g of $\mathrm{CH}_{2} \mathrm{Cl}_{2}$
11.59 Household bleach is a 5.0 mass $\%$ aqueous solution of sodium hypochlorite, NaOCl . What is the molality of the bleach? What is the mole fraction of NaOCl in the bleach?
11.60 The density of a 16.0 mass \% solution of sulfuric acid in water is $1.1094 \mathrm{~g} / \mathrm{mL}$ at $25.0^{\circ} \mathrm{C}$. What is the molarity of the solution?
11.61 Ethylene glycol, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}$, is the principal constituent of automobile antifreeze. If the density of a 40.0 mass $\%$ solution of ethylene glycol in water is $1.0514 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$, what is the molarity?
11.62 What is the molality of the 40.0 mass \% ethylene glycol solution used for automobile antifreeze (Problem 11.61)?
11.63 What is the molality of the 16.0 mass \% solution of sulfuric acid in Problem 11.60?
11.64 Nalorphine ( $\mathrm{C}_{19} \mathrm{H}_{21} \mathrm{NO}_{3}$ ), a relative of morphine, is used to combat withdrawal symptoms in narcotics users. How many grams of a $1.3 \times 10^{-3} \mathrm{~m}$ aqueous solution of nalorphine are needed to obtain a dose of 1.5 mg ?
11.65 How many grams of water should you add to 32.5 g of sucrose, $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$, to get a 0.850 m solution?
11.66 A 0.944 M solution of glucose, $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}$, in water has a density of $1.0624 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$. What is the concentration of this solution in the following units?
(a) Mole fraction
(b) Mass percent
(c) Molality
11.67 Lactose, $\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}$, is a naturally occurring sugar found in mammalian milk. A 0.335 M solution of lactose in water has a density of $1.0432 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$. What is the concentration of this solution in the following units?
(a) Mole fraction
(b) Mass percent
(c) Molality

## Solubility and Henry's Law

11.68 Vinyl chloride $\left(\mathrm{H}_{2} \mathrm{C}=\mathrm{CHCl}\right)$, the starting material from which PVC polymer is made, has a Henry's-law constant of $0.091 \mathrm{~mol} /(\mathrm{L} \cdot \mathrm{atm})$ at $25^{\circ} \mathrm{C}$. What is the solubility of vinyl chloride in water (in $\mathrm{mol} / \mathrm{L}$ ) at $25^{\circ} \mathrm{C}$ and a partial pressure of 0.75 atm ?
11.69 Hydrogen sulfide, $\mathrm{H}_{2} \mathrm{~S}$, is a toxic gas responsible for the odor of rotten eggs. The solubility of $\mathrm{H}_{2} \mathrm{~S}(g)$ in water at STP is 0.195 M . What is the Henry's-law constant of $\mathrm{H}_{2} \mathrm{~S}$ at $0^{\circ} \mathrm{C}$ ? What is the solubility of $\mathrm{H}_{2} \mathrm{~S}$ in water at $0^{\circ} \mathrm{C}$ and a partial pressure of 25.5 mm Hg ?
11.70 Fish generally need an $\mathrm{O}_{2}$ concentration in water of at least $4 \mathrm{mg} / \mathrm{L}$ for survival. What partial pressure of oxygen above the water (in atmospheres at $0^{\circ} \mathrm{C}$ ) is needed to obtain this concentration? The solubility of $\mathrm{O}_{2}$ in water at $0^{\circ} \mathrm{C}$ and 1 atm partial pressure is $2.21 \times 10^{-3} \mathrm{~mol} / \mathrm{L}$.
11.71 At an altitude of $10,000 \mathrm{ft}$, the partial pressure of oxygen in the lungs is about 68 mm Hg . What is the concentration (in $\mathrm{mg} / \mathrm{L}$ ) of dissolved $\mathrm{O}_{2}$ in blood (or water) at this partial pressure and a normal body temperature of $37^{\circ} \mathrm{C}$ ? The solubility of $\mathrm{O}_{2}$ in water at $37^{\circ} \mathrm{C}$ and 1 atm partial pressure is $1.93 \times 10^{-3} \mathrm{~mol} / \mathrm{L}$.
11.72 Look at the solubility graph in Figure 11.7, and estimate an approximate Henry's-law constant for xenon at STP.
11.73 Ammonia, $\mathrm{NH}_{3}$, is one of the few gases that does not obey Henry's law. Suggest a reason.

## Colligative Properties

11.74 What factor is responsible for all colligative properties?
11.75 What is osmotic pressure?
11.76 When 1 mol of NaCl is added to 1 L of water, the boiling point increases. When 1 mol of methyl alcohol is added to 1 L of water, the boiling point decreases. Explain.
11.77 When 100 mL of $9 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ at $0^{\circ} \mathrm{C}$ is added to 100 mL of liquid water at $0^{\circ} \mathrm{C}$, the temperature rises to $12^{\circ} \mathrm{C}$. When 100 mL of $9 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ at $0^{\circ} \mathrm{C}$ is added to 100 g of solid ice at $0^{\circ} \mathrm{C}$, the temperature falls to $-12^{\circ} \mathrm{C}$. Explain the difference in behavior.
11.78 Draw a phase diagram showing how the phase boundaries differ for a pure solvent compared with a solution.
11.79 A solution concentration must be expressed in molality when considering boiling-point elevation or freezingpoint depression but can be expressed in molarity when considering osmotic pressure. Why?
11.80 What is the vapor pressure (in mm Hg ) of the following solutions, each of which contains a nonvolatile solute? The vapor pressure of water at $45.0^{\circ} \mathrm{C}$ is 71.93 mm Hg .
(a) A solution of 10.0 g of urea, $\mathrm{CH}_{4} \mathrm{~N}_{2} \mathrm{O}$, in 150.0 g of water at $45.0^{\circ} \mathrm{C}$
(b) A solution of 10.0 g of LiCl in 150.0 g of water at $45.0^{\circ} \mathrm{C}$, assuming complete dissociation
11.81 What is the vapor pressure (in mm Hg ) of a solution of 16.0 g of glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ in 80.0 g of methanol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$ at $27^{\circ} \mathrm{C}$ ? The vapor pressure of pure methanol at $27^{\circ} \mathrm{C}$ is 140 mm Hg .
11.82 What is the boiling point (in ${ }^{\circ} \mathrm{C}$ ) of each of the solutions in Problem 11.80? For water, $K_{\mathrm{b}}=0.51\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.
11.83 What is the freezing point (in ${ }^{\circ} \mathrm{C}$ ) of each of the solutions in Problem 11.80? For water, $K_{\mathrm{f}}=1.86\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.
11.84 A 1.0 m solution of $\mathrm{K}_{2} \mathrm{SO}_{4}$ in water has a freezing point of $-4.3^{\circ} \mathrm{C}$. What is the value of the van't Hoff factor $i$ for $\mathrm{K}_{2} \mathrm{SO}_{4}$ ?
11.85 The van't Hoff factor for KCl is $i=1.85$. What is the boiling point of a 0.75 m solution of KCl in water? For water, $K_{\mathrm{b}}=0.51\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.
11.86 Acetone, $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}$, and ethyl acetate, $\mathrm{C}_{4} \mathrm{H}_{8} \mathrm{O}_{2}$, are organic liquids often used as solvents. At $30^{\circ} \mathrm{C}$, the vapor pressure of acetone is 285 mm Hg and the vapor pressure of ethyl acetate is 118 mm Hg . What is the vapor pressure (in mm Hg ) at $30^{\circ} \mathrm{C}$ of a solution prepared by dissolving 25.0 g of acetone in 25.0 g of ethyl acetate?
11.87 The industrial solvents chloroform, $\mathrm{CHCl}_{3}$, and dichloromethane, $\mathrm{CH}_{2} \mathrm{Cl}_{2}$, are prepared commercially by reaction of methane with chlorine, followed by fractional distillation of the product mixture. At $25^{\circ} \mathrm{C}$, the vapor pressure of $\mathrm{CHCl}_{3}$ is 205 mm Hg and the vapor pressure of $\mathrm{CH}_{2} \mathrm{Cl}_{2}$ is 415 mm Hg . What is the vapor pressure (in mm Hg ) at $25^{\circ} \mathrm{C}$ of a mixture of 15.0 g of $\mathrm{CHCl}_{3}$ and 37.5 g of $\mathrm{CH}_{2} \mathrm{Cl}_{2}$ ?
11.88 What is the mole fraction of each component in the liquid mixture in Problem 11.86, and what is the mole fraction of each component in the vapor at $30^{\circ} \mathrm{C}$ ?
11.89 What is the mole fraction of each component in the liquid mixture in Problem 11.87, and what is the mole fraction of each component in the vapor at $25^{\circ} \mathrm{C}$ ?
11.90 A solution prepared by dissolving 5.00 g of aspirin, $\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}_{4}$, in 215 g of chloroform has a normal boiling point that is elevated by $\Delta T=0.47^{\circ} \mathrm{C}$ over that of pure chloroform. What is the value of the molal boiling-point-elevation constant for chloroform?
11.91 A solution prepared by dissolving 3.00 g of ascorbic acid (vitamin C, $\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{6}$ ) in 50.0 g of acetic acid has a freezing point that is depressed by $\Delta T=1.33^{\circ} \mathrm{C}$ below that of pure acetic acid. What is the value of the molal freezing-point-depression constant for acetic acid?
11.92 A solution of citric acid, $\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{7}$, in 50.0 g of acetic acid has a boiling point elevation of $\Delta T=1.76^{\circ} \mathrm{C}$. What is the molality of the solution if the molal boiling-pointelevation constant for acetic acid is $K_{\mathrm{b}}=$ $3.07\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.
11.93 What is the normal boiling point (in ${ }^{\circ} \mathrm{C}$ ) of ethyl alcohol if a solution prepared by dissolving 26.0 g of glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ in 285 g of ethyl alcohol has a boiling point of $79.1^{\circ} \mathrm{C}$ ? See Table 11.4 to find $K_{\mathrm{b}}$ for ethyl alcohol.
11.94 What osmotic pressure (in atmospheres) would you expect for each of the following solutions?
(a) 5.00 g of NaCl in 350.0 mL of aqueous solution at $50^{\circ} \mathrm{C}$
(b) 6.33 g of sodium acetate, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}$, in 55.0 mL of aqueous solution at $10^{\circ} \mathrm{C}$
11.95 What osmotic pressure (in mm Hg ) would you expect for an aqueous solution of 11.5 mg of insulin $($ mol. mass $=5990 \mathrm{amu})$ in 6.60 mL of solution at 298 K ? What would the height of the water column be (in meters)? The density of mercury is $13.534 \mathrm{~g} / \mathrm{mL}$ at 298 K .
11.96 A solution of an unknown molecular substance in water at 300 K gives rise to an osmotic pressure of 4.85 atm. What is the molarity of the solution?
11.97 Human blood gives rise to an osmotic pressure of approximately 7.7 atm at body temperature, $37.0^{\circ} \mathrm{C}$. What must the molarity of an intravenous glucose solution be to have the same osmotic pressure as blood?

## Uses of Colligative Properties

11.98 Which of the four colligative properties is most often used for molecular mass determination, and why?
11.99 If cost per gram were not a concern, which of the following substances would be the most efficient per unit mass for melting snow from sidewalks and roads: glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right), \mathrm{LiCl}, \mathrm{NaCl}, \mathrm{CaCl}_{2}$ ? Explain.
11.100 Cellobiose is a sugar obtained by degradation of cellulose. If 200.0 mL of aqueous solution containing 1.500 g of cellobiose at $25.0^{\circ} \mathrm{C}$ gives rise to an osmotic pressure of 407.2 mm Hg , what is the molecular mass of cellobiose?
11.101 Met-enkephalin is one of the so-called endorphins, a class of naturally occurring morphinelike chemicals in the brain. What is the molecular mass of metenkephalin if 20.0 mL of an aqueous solution containing 15.0 mg met-enkephalin at 298 K supports a column of water 32.9 cm high? The density of mercury at 298 K is $13.534 \mathrm{~g} / \mathrm{mL}$.
11.102 The freezing point of a solution prepared by dissolving 1.00 mol of hydrogen fluoride, HF , in 500 g water is $-3.8^{\circ} \mathrm{C}$, but the freezing point of a solution prepared by dissolving 1.00 mol of hydrogen chloride, HCl , in 500 g of water is $-7.4^{\circ} \mathrm{C}$. Explain.
11.103 The boiling point of a solution prepared by dissolving 71 g of $\mathrm{Na}_{2} \mathrm{SO}_{4}$ in 1.00 kg of water is $100.8^{\circ} \mathrm{C}$. Explain.
11.104 Elemental analysis of $\beta$-carotene, a dietary source of vitamin A, shows that it contains $10.51 \% \mathrm{H}$ and $89.49 \%$ C. Dissolving 0.0250 g of $\beta$-carotene in 1.50 g of camphor gives a freezing-point depression of $1.17^{\circ} \mathrm{C}$. What are the molecular mass and formula of $\beta$-carotene? $\left[K_{\mathrm{f}}\right.$ for camphor is $37.7\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.]
11.105 Lysine, one of the amino acid building blocks found in proteins, contains $49.29 \% \mathrm{C}, 9.65 \% \mathrm{H}, 19.16 \% \mathrm{~N}$, and $21.89 \%$ O by elemental analysis. A solution prepared by dissolving 30.0 mg of lysine in 1.200 g of the organic solvent biphenyl, gives a freezing-point depression of $1.37^{\circ} \mathrm{C}$. What are the molecular mass and formula of lysine? [ $K_{\mathrm{f}}$ for biphenyl is $8.00\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}$.]

## General Problems

11.106 When salt is spread on snow-covered roads at $-2^{\circ} \mathrm{C}$, the snow melts. When salt is spread on snow-covered roads at $-30^{\circ} \mathrm{C}$, nothing happens. Explain.
11.107 How many grams of KBr dissolved in 125 g of water is needed to raise the boiling point of water to $103.2^{\circ} \mathrm{C}$ ?
11.108 How many grams of ethylene glycol (automobile antifreeze, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}_{2}$ ) dissolved in 3.55 kg of water is needed to lower the freezing point of water in an automobile radiator to $-22.0^{\circ} \mathrm{C}$ ?
11.109 When 1 mL of toluene is added to 100 mL of benzene (bp $80.1^{\circ} \mathrm{C}$ ), the boiling point of the benzene solution rises, but when 1 mL of benzene is added to 100 mL of toluene (bp $110.6^{\circ} \mathrm{C}$ ), the boiling point of the toluene solution falls. Explain.
11.110 When solid $\mathrm{CaCl}_{2}$ is added to liquid water, the temperature rises. When solid $\mathrm{CaCl}_{2}$ is added to ice at $0^{\circ} \mathrm{C}$, the temperature falls. Explain.
11.111 Silver chloride has a solubility of $0.007 \mathrm{mg} / \mathrm{mL}$ in water at $5^{\circ} \mathrm{C}$. What is the osmotic pressure (in atmospheres) of a saturated solution of AgCl ?
11.112 How many grams of naphthalene, $\mathrm{C}_{10} \mathrm{H}_{8}$ (commonly used as household mothballs), should be added to 150.0 g of benzene to depress its freezing point by $0.35^{\circ} \mathrm{C}$ ? See Table 11.4 to find $K_{\mathrm{f}}$ for benzene.
11.113 Bromine is sometimes used as a solution in tetrachloromethane, $\mathrm{CCl}_{4}$. What is the vapor pressure (in mm Hg ) of a solution of 1.50 g of $\mathrm{Br}_{2}$ in 145.0 g of $\mathrm{CCl}_{4}$ at 300 K ? The vapor pressure of pure bromine at 300 K is 30.5 kPa , and the vapor pressure of $\mathrm{CCl}_{4}$ is 16.5 kPa .
11.114 Assuming that seawater is a 3.5 mass $\%$ solution of NaCl and that its density is $1.00 \mathrm{~g} / \mathrm{mL}$, calculate both its boiling point and its freezing point in ${ }^{\circ} \mathrm{C}$.
11.115 There's actually much more in seawater than just dissolved NaCl . Major ions present include $19,000 \mathrm{ppm}$ $\mathrm{Cl}^{-}, 10,500 \mathrm{ppm} \mathrm{Na}+, 2650 \mathrm{ppm} \mathrm{SO}{ }_{4}{ }^{2-}, 1350 \mathrm{ppm}$
$\mathrm{Mg}^{2+}, 400 \mathrm{ppm} \mathrm{Ca}{ }^{2+}, 380 \mathrm{ppm} \mathrm{K}{ }^{+}, 140 \mathrm{ppm} \mathrm{HCO} 3{ }^{-}$, and $65 \mathrm{ppm} \mathrm{Br}^{-}$.
(a) What is the total molality of all ions present in seawater?
(b) Assuming molality and molarity to be equal, what amount of osmotic pressure (in atmospheres) would seawater give rise to at 300 K ?
11.116 Rubbing alcohol is a 90 mass \% solution of isopropyl alcohol, $\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}$, in water.
(a) How many grams of rubbing alcohol contains 10.5 g of isopropyl alcohol?
(b) How many moles of isopropyl alcohol are in 50.0 g of rubbing alcohol?
11.117 Although inconvenient, it's possible to use osmotic pressure to measure temperature. What is the temperature (in kelvins) if a solution prepared by dissolving 17.5 mg of glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$ in 50.0 mL of aqueous solution gives rise to an osmotic pressure of 37.8 mm Hg ?
11.118 The steroid hormone estradiol contains only C, H, and O; combustion analysis of a 3.47 mg sample yields 10.10 mg CO 2 and $2.76 \mathrm{mg} \mathrm{H} \mathrm{H}_{2} \mathrm{O}$. On dissolving 7.55 mg of estradiol in 0.500 g of camphor, the melting point of camphor is depressed by $2.10^{\circ} \mathrm{C}$. What is the molecular mass of estradiol, and what is a probable formula? [For camphor, $\left.K_{\mathrm{f}}=37.7\left({ }^{\circ} \mathrm{C} \cdot \mathrm{kg}\right) / \mathrm{mol}.\right]$
11.119 Many acids are partially dissociated into ions in aqueous solution. Trichloroacetic acid $\left(\mathrm{CCl}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$, for instance, is partially dissociated in water according to the equation
$\mathrm{CCl}_{3} \mathrm{CO}_{2} \mathrm{H}(a q) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{CCl}_{3} \mathrm{CO}_{2}^{-}(a q)$
What is the percentage of molecules dissociated if the freezing point of a 1.00 m solution of trichloroacetic acid in water is $-2.53^{\circ} \mathrm{C}$ ?
11.120 Addition of 50.00 mL of $2.238 \mathrm{~m} \mathrm{H}_{2} \mathrm{SO}_{4}$ (solution density $=1.1243 \mathrm{~g} / \mathrm{mL}$ ) to 50.00 mL of $2.238 \mathrm{M} \mathrm{BaCl}_{2}$ gives a white precipitate.
(a) What is the mass of the precipitate in grams?
(b) If you filter the mixture and add more $\mathrm{H}_{2} \mathrm{SO}_{4}$ solution to the filtrate, would you obtain more precipitate? Explain.
11.121 A solid mixture of $\mathrm{KCl}, \mathrm{KNO}_{3}$, and $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$ is 20.92 mass $\%$ chlorine, and a 1.000 g sample of the mixture in 500.0 mL of aqueous solution at $25^{\circ} \mathrm{C}$ has an osmotic pressure of 744.7 mm Hg . What are the mass percents of $\mathrm{KCl}, \mathrm{KNO}_{3}$, and $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$ in the mixture?
11.122 A solution of LiCl in a mixture of water and methanol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$ has a vapor pressure of 39.4 mm Hg at $17^{\circ} \mathrm{C}$ and 68.2 mm Hg at $27^{\circ} \mathrm{C}$. The vapor pressure of pure water is 14.5 mm Hg at $17^{\circ} \mathrm{C}$ and 26.8 mm Hg at $27^{\circ} \mathrm{C}$, and the vapor pressure of pure methanol is 82.5 mm Hg at $17^{\circ} \mathrm{C}$ and 140.3 mm Hg at $27^{\circ} \mathrm{C}$. What is the composition of the solution (in mass percent)?
11.123 An aqueous solution of KI has a freezing point of $-1.95^{\circ} \mathrm{C}$ and an osmotic pressure of 25.0 atm at $25.0^{\circ} \mathrm{C}$. Assuming that the KI completely dissociates in water, what is the density of the solution?
11.124 An aqueous solution of a certain organic compound has a density of $1.063 \mathrm{~g} / \mathrm{mL}$, an osmotic pressure of 12.16 atm at $25.0^{\circ} \mathrm{C}$, and a freezing point of $-1.03^{\circ} \mathrm{C}$. The compound is known not to dissociate in water. What is the molar mass of the compound?
11.125 At $60^{\circ} \mathrm{C}$, compound X has a vapor pressure of 96 mm Hg , benzene $\left(\mathrm{C}_{6} \mathrm{H}_{6}\right)$ has a vapor pressure of 395 mm Hg , and a 50:50 mixture by mass of benzene and X has a vapor pressure of 299 mm Hg . What is the molar mass of X ?
11.126 An aqueous solution containing 100.0 g of NaCl and 100.0 g of $\mathrm{CaCl}_{2}$ has a volume of 1.00 L and a density of $1.15 \mathrm{~g} / \mathrm{mL}$. The vapor pressure of pure water at $25^{\circ} \mathrm{C}$ is 23.8 mm Hg , and you can assume complete dissociation for both solutes.
(a) What is the boiling point of the solution?
(b) What is the vapor pressure of the solution at $25^{\circ} \mathrm{C}$ ?
11.127 Iodic acid, $\mathrm{HIO}_{3}$, is a weak acid that undergoes only partial dissociation in water. If a 1.00 M solution of $\mathrm{HIO}_{3}$ has a density of $1.07 \mathrm{~g} / \mathrm{mL}$ and a freezing point of $-2.78^{\circ} \mathrm{C}$, what percent of the $\mathrm{HIO}_{3}$ is dissociated?
11.128 A 1.24 M solution of KI has a density of $1.15 \mathrm{~g} / \mathrm{cm}^{3}$.
(a) What is the molality of the solution?
(b) What is the freezing point of the solution assuming complete dissociation of KI?
(c) The actual freezing point of the solution is $-4.46^{\circ} \mathrm{C}$. What percent of the KI is dissociated?
11.129 Desert countries like Saudi Arabia have built reverse osmosis plants to produce fresh water from seawater. Assume that seawater has the composition 0.470 M NaCl and $0.068 \mathrm{M} \mathrm{MgCl}_{2}$ and that both compounds are completely dissociated.
(a) What is the osmotic pressure of seawater at $25^{\circ} \mathrm{C}$ ?
(b) If the reverse osmosis equipment can exert a maximum pressure of 100.0 atm at $25.0^{\circ} \mathrm{C}$, what is the maximum volume of fresh water that can be obtained from 1.00 L of seawater?
11.130 A solution prepared by dissolving 100.0 g of a mixture of sugar $\left(\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}\right)$ and table salt $(\mathrm{NaCl})$ in 500.0 g of water has a freezing point of $-2.25^{\circ} \mathrm{C}$. What is the mass of each individual solute? Assume that NaCl is completely dissociated.

## Multi-Concept Problems

11.131 Treatment of 1.385 g of an unknown metal M with an excess of aqueous HCl evolved a gas that was found to have a volume of 382.6 mL at $20.0^{\circ} \mathrm{C}$ and 755 mm Hg pressure. Heating the reaction mixture to evaporate the water and remaining HCl then gave a white crystalline compound, $\mathrm{MCl}_{x}$. After dissolving the compound in 25.0 g of water, the melting point of the resulting solution was $-3.53^{\circ} \mathrm{C}$.
(a) How many moles of $\mathrm{H}_{2}$ gas are evolved?
(b) What mass of $\mathrm{MCl}_{x}$ is formed?
(c) What is the molality of particles (ions) in the solution of $\mathrm{MCl}_{x}$ ?
(d) How many moles of ions are in solution?
(e) What are the formula and molecular mass of $\mathrm{MCl}_{x}$ ?
(f) What is the identity of the metal M?
11.132 A compound that contains only C and H was burned in excess $\mathrm{O}_{2}$ to give $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$. When 0.270 g of the compound was burned, the amount of $\mathrm{CO}_{2}$ formed reacted completely with 20.0 mL of 2.00 M NaOH solution according to the equation

$$
2 \mathrm{OH}^{-}(a q)+\mathrm{CO}_{2}(g) \longrightarrow \mathrm{CO}_{3}^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

When 0.270 g of the compound was dissolved in 50.0 g of camphor, the resulting solution had a freezing point of $177.9^{\circ} \mathrm{C}$. (Pure camphor freezes at $179.8^{\circ} \mathrm{C}$ and has $K_{\mathrm{f}}=37.7^{\circ} \mathrm{C} / \mathrm{m}$.)
(a) What is the empirical formula of the compound?
(b) What is the molecular mass of the compound?
(c) What is the molecular formula of the compound?
11.133 Combustion analysis of a 36.72 mg sample of the male hormone testosterone gave 106.43 mg CO 2 and 32.100 $\mathrm{mg} \mathrm{H}_{2} \mathrm{O}$ as the only combustion products. When 5.00 mg of testosterone was dissolved in 15.0 mL of a suitable solvent at $25^{\circ} \mathrm{C}$, an osmotic pressure of 21.5 mm Hg was measured. What is the molecular formula of testosterone?
11.134 When 8.900 g of a mixture of an alkali metal chloride $(\mathrm{XCl})$ and an alkaline earth chloride $\left(\mathrm{YCl}_{2}\right)$ was dissolved in 150.0 g of water, the freezing point of the resultant solution was $-4.42^{\circ} \mathrm{C}$. Addition of an excess of aqueous $\mathrm{AgNO}_{3}$ to the solution yielded a white precipitate with a mass of 27.575 g . How much of each metal chloride was present in the original mixture, and what are the identities of the two metals X and Y ?

## eMedia Problems

11.135 Of the five solutes in the Enthalpy of Solution activity (eChapter 11.2), two form solutions with solute-solvent interactions that are greater than the solute-solute and solvent-solvent interactions. Identify the two solutes. How can you tell?
11.136 Looking at the Expressions of Concentration activity in eChapter 11.3, identify the units of concentration that are determined directly from the mass of solute, and explain how they differ. Identify the units that are determined directly from the moles of solute, and explain how they differ.
11.137 Use the Henry's Law activity in eChapter 11.4 to answer the following questions:
(a) How is the concentration of vapor above the solution affected by the increase in pressure?
(b) How does the system compensate for this change?
(c) How does increasing pressure affect the solubility of a gas in solution?
11.138 The Boiling-Point Elevation and Freezing-Point Depression activity (eChapter 11.7) illustrates how the boiling point and freezing point of water are affected by the addition of different solutes.
(a) Explain why $\mathrm{NH}_{4} \mathrm{NO}_{3}$ causes a smaller change than either NaCl or KOH , even though both $\Delta T$ equations are independent of solute and all three solutes contain the same number of ions per mole.
(b) What characteristic of ethylene glycol makes it a much more efficient antifreeze than water.
11.139 Write down all of the calculations required to determine the identity of the metal chloride in the Determination of Molar Mass activity (eChapter 11.9). Use similar calculations to identify the alkaline earth metal chloride that gives a solution with osmotic pressure of 1.32 atm upon addition of 100.0 mg to water under the same conditions of volume and temperature.

## Chapter

## Chemical Kinetics

## CONTENTS

Monarchos drives to the finish to win the 2001 Kentucky Derby. His speed is defined as the change in location per unit time (meters per second, $\mathrm{m} / \mathrm{s}$ ).
Similarly, the speed, or rate, of a chemical reaction is defined as a change in concentration per unit time (molar per second, $\mathrm{M} / \mathrm{s}$ ).
12.1 Reaction Rates
12.2 Rate Laws and Reaction Order
12.3 Experimental Determination of a Rate Law
12.4 Integrated Rate Law for a FirstOrder Reaction
12.5 Half-Life of a First-Order Reaction
12.6 Second-Order Reactions
12.7 Zeroth-Order Reactions
12.8 Reaction Mechanisms

### 12.9 Rate Laws and Reaction Mechanisms

12.10 Reaction Rates and Temperature: The Arrhenius Equation
12.11 Using the Arrhenius Equation
12.12 Catalysis
12.13 Homogeneous and Heterogeneous Catalysts

- Interlude-Explosives


A Liquid ammonia is used as a fertilizer.

ת Bassam Z. Shakhashiri, "Color Variations of the Landolt Reaction," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 4 (The University of Wisconsin Press, Madison, 1992), pp. 26-28. Three pairs of colorless solutions are mixed. After 10 seconds the three mixtures turn red, yellow, and blue, respectively. Each clock reaction is the reduction of iodate by bisulfite. The observed colors are related to the amount of triiodide produced, which depends on the relative amounts of iodate and bisulfite reacted, and whether or not starch is present.
concerned with reaction rates and the sequence of steps by which reactions occur is called chemical kinetics.

Chemical kinetics is a subject of crucial environmental and economic importance. In the upper atmosphere, for example, maintenance or depletion of the ozone layer, which protects us from the sun's harmful ultraviolet radiation, depends on the relative rates of reactions that produce and destroy $\mathrm{O}_{3}$ molecules. In the chemical industry, the profitability of the process for the synthesis of ammonia, which is used as a fertilizer, depends on the rate at which gaseous $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ can be converted to $\mathrm{NH}_{3}$.

In this chapter, we'll describe reaction rates and examine how they are affected by variables such as concentrations and temperature. We'll also see how chemists use rate data to propose a mechanism, or pathway, by which a reaction takes place. By understanding reaction mechanisms, we can control known reactions and predict new ones.

## $12.1 \mid$ Reaction Rates

The rates of chemical reactions differ greatly. Some reactions, such as the combination of sodium and bromine, occur instantly. Other reactions, such as the rusting of iron, are imperceptibly slow. To describe the rate of a reaction quantitatively, we must specify how fast the concentration of a reactant or a product changes per unit time.

$$
\text { Rate }=\frac{\text { Concentration change }}{\text { Time change }}
$$


© Which of these reactions is faster? (a) The reaction between sodium and bromine, or (b) the rusting of iron.

One reaction that has been studied in detail is the thermal decomposition of gaseous dinitrogen pentoxide, $\mathrm{N}_{2} \mathrm{O}_{5}$, to give the brown gas nitrogen dioxide and molecular oxygen:

$$
\underset{\substack{\text { Colorless }}}{2 \mathrm{~N}_{2} \mathrm{O}_{5}(g) \longrightarrow} \underset{\text { Brown }}{4 \mathrm{NO}_{2}(g)}+\underset{\text { Colorless }}{\mathrm{O}_{2}(g)}
$$

Changes in concentration as a function of time can be determined by measuring the increase in pressure as 2 gas molecules are converted to 5 gas molecules. Alternatively, concentration changes can be monitored by measuring the intensity of the brown color due to $\mathrm{NO}_{2}$. Reactant and product concentrations as a function of time at $55^{\circ} \mathrm{C}$ are listed in Table 12.1. Note that the concentrations of $\mathrm{NO}_{2}$ and $\mathrm{O}_{2}$ increase as the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ decreases.

| TABLE 12.1 | Concentrations as a Function of Time at $55^{\circ} \mathrm{C}$ for the Reaction $2 \mathrm{~N}_{2} \mathrm{O}_{5}(g) \longrightarrow 4 \mathrm{NO}_{2}(g)+\mathrm{O}_{2}(g)$ |  |  |
| :---: | :---: | :---: | :---: |
|  | Concentration (M) |  |  |
| Time (s) | $\mathrm{N}_{2} \mathrm{O}_{5}$ | $\mathrm{NO}_{2}$ | $\mathrm{O}_{2}$ |
| 0 | 0.0200 | 0 | 0 |
| 100 | 0.0169 | 0.0063 | 0.0016 |
| 200 | 0.0142 | 0.0115 | 0.0029 |
| 300 | 0.0120 | 0.0160 | 0.0040 |
| 400 | 0.0101 | 0.0197 | 0.0049 |
| 500 | 0.0086 | 0.0229 | 0.0057 |
| 600 | 0.0072 | 0.0256 | 0.0064 |
| 700 | 0.0061 | 0.0278 | 0.0070 |

The reaction rate can be defined either as the increase in the concentration of a product per unit time or as the decrease in the concentration of a reactant per unit time. Let's look first at product formation. In the decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$, the rate of formation of $\mathrm{O}_{2}$ is given by the equation
Rate of formation of $\mathrm{O}_{2}=\frac{\Delta\left[\mathrm{O}_{2}\right]}{\Delta t}=\frac{\text { Conc of } \mathrm{O}_{2} \text { at time } t_{2}-\text { Conc of } \mathrm{O}_{2} \text { at time } t_{1}}{t_{2}-t_{1}}$ where the square brackets surrounding $\mathrm{O}_{2}$ denote its molar concentration; $\Delta\left[\mathrm{O}_{2}\right]$ is the change in the molar concentration of $\mathrm{O}_{2} ; \Delta t$ is the change in the time; and $\Delta\left[\mathrm{O}_{2}\right] / \Delta t$ is the change in the molar concentration of $\mathrm{O}_{2}$ during the interval from time $t_{1}$ to $t_{2}$. During the time period 300 to 400 s , for example, the average rate of formation of $\mathrm{O}_{2}$ is $9 \times 10^{-6} \mathrm{M} / \mathrm{s}$ :

$$
\text { Rate of formation of } \mathrm{O}_{2}=\frac{\Delta\left[\mathrm{O}_{2}\right]}{\Delta t}=\frac{0.0049 \mathrm{M}-0.0040 \mathrm{M}}{400 \mathrm{~s}-300 \mathrm{~s}}=9 \times 10^{-6} \mathrm{M} / \mathrm{s}
$$

The units of reaction rate are molar per second, $\mathrm{M} / \mathrm{s}$, or, equivalently, moles per liter second, $\mathrm{mol} /(\mathrm{L} \cdot \mathrm{s})$. We define reaction rate in terms of concentration (moles per liter) rather than amount (moles) because we want the rate to be independent of the scale of the reaction. When twice as much $0.0200 \mathrm{M} \mathrm{N}_{2} \mathrm{O}_{5}$ decomposes in a vessel of twice the volume, twice the number of moles of $\mathrm{O}_{2}$ form per second, but the number of moles of $\mathrm{O}_{2}$ per liter that form per second is unchanged.

Plotting the data of Table 12.1 to give the three curves that appear in Figure 12.1 gives additional insight into the concept of reaction rate. Looking at the time period 300 to 400 s on the $\mathrm{O}_{2}$ curve, $\Delta\left[\mathrm{O}_{2}\right]$ and $\Delta t$ are represented, respectively, by the vertical and horizontal sides of a right triangle. The slope of the third side, the hypotenuse of the triangle, is $\Delta\left[\mathrm{O}_{2}\right] / \Delta t$, the average rate of $\mathrm{O}_{2}$ formation during that time period. The steeper the slope of the hypotenuse, the faster the rate. Look, for example, at the triangle defined by $\Delta\left[\mathrm{NO}_{2}\right]$ and $\Delta t$. The average rate of formation of $\mathrm{NO}_{2}$ during the time period 300 to 400 s is $3.7 \times 10^{-5} \mathrm{M} / \mathrm{s}$, which is four times the rate of formation of $\mathrm{O}_{2}$, in accord with the 4:1 ratio of the coefficients of $\mathrm{NO}_{2}$ and $\mathrm{O}_{2}$ in the chemical equation for decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$.
Rate of formation of $\mathrm{NO}_{2}=\frac{\Delta\left[\mathrm{NO}_{2}\right]}{\Delta t}=\frac{0.0197 \mathrm{M}-0.0160 \mathrm{M}}{400 \mathrm{~s}-300 \mathrm{~s}}=3.7 \times 10^{-5} \mathrm{M} / \mathrm{s}$
As $\mathrm{O}_{2}$ and $\mathrm{NO}_{2}$ form, $\mathrm{N}_{2} \mathrm{O}_{5}$ disappears. Consequently, $\Delta\left[\mathrm{N}_{2} \mathrm{O}_{5}\right] / \Delta t$ is negative, in accord with the negative slope of the hypotenuse of the triangle defined by $\Delta\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]$ and $\Delta t$ in Figure 12.1. Because reaction rate is defined as a positive quantity,

Lee R. Summerlin and James L.
Ealy, "The Starch-Iodine Clock Reaction," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), pp. 107-108.

Bassam Z. Shakhashiri,
"Hydrogen Peroxide Iodine Clock: Oxidation of Potassium Iodide by Hydrogen Peroxide," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 4 (The University of Wisconsin Press, Madison, 1992), pp. 37-43.

Xavier Creary and Karen M. Morris, "A New Twist on the Iodine Clock Reaction: Determining the Order of a Reaction," J. Chem. Educ., Vol. 76, 1999, 530-531.



A FIGURE 12.1 Concentrations measured as a function of time when gaseous $\mathrm{N}_{2} \mathrm{O}_{5}$ at an initial concentration of 0.0200 M decomposes to gaseous $\mathrm{NO}_{2}$ and $\mathrm{O}_{2}$ at $55^{\circ} \mathrm{C}$. Note that the concentrations of $\mathrm{O}_{2}$ and $\mathrm{NO}_{2}$ increase as the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ decreases. The slope of the hypotenuse of each triangle gives the average rate of change of the product or reactant concentration during the indicated time interval. The rate of formation of $\mathrm{O}_{2}$ is one-fourth the rate of formation of $\mathrm{NO}_{2}$ and one-half the rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$.
we must always introduce a minus sign when calculating the rate of disappearance of a reactant. During the time period 300 to 400 s , for example, the average rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ is $1.9 \times 10^{-5} \mathrm{M} / \mathrm{s}$ :

$$
\text { Rate of decomposition of } \begin{aligned}
\mathrm{N}_{2} \mathrm{O}_{5} & =\frac{-\Delta\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]}{\Delta t}=\frac{-(0.0101 \mathrm{M}-0.0120 \mathrm{M})}{400 \mathrm{~s}-300 \mathrm{~s}} \\
& =1.9 \times 10^{-5} \mathrm{M} / \mathrm{s}
\end{aligned}
$$

When quoting a reaction rate, it's important to specify the reactant or product on which the rate is based because the rates of product formation and reactant consumption may differ, depending on the coefficients in the balanced equation. For the decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}, 4 \mathrm{~mol}$ of $\mathrm{NO}_{2}$ form and 2 mol of $\mathrm{N}_{2} \mathrm{O}_{5}$ disappear for each mole of $\mathrm{O}_{2}$ that forms. Therefore, the rate of formation of $\mathrm{O}_{2}$ is one-fourth the rate of formation of $\mathrm{NO}_{2}$ and one-half the rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ :

$$
\begin{aligned}
& \left.\begin{array}{c}
\begin{array}{c}
\text { Rate of formation } \\
\text { of } \mathrm{O}_{2}
\end{array}
\end{array}\right)=\frac{1}{4}\binom{\text { Rate of formation }}{\text { of } \mathrm{NO}_{2}}=\frac{1}{2}\binom{\text { Rate of decomposition }}{\text { of } \mathrm{N}_{2} \mathrm{O}_{5}} \\
& \text { or } \quad \frac{\Delta\left[\mathrm{O}_{2}\right]}{\Delta \mathrm{t}}=\frac{1}{4}\left(\frac{\Delta\left[\mathrm{NO}_{2}\right]}{\Delta \mathrm{t}}\right)=-\frac{1}{2}\left(\frac{\Delta\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]}{\Delta \mathrm{t}}\right)
\end{aligned}
$$

To avoid the ambiguity of more than one rate, chemists have defined a general rate of reaction equal to the rate of consumption of a reactant or formation of a product divided by its coefficient in the balanced chemical equation. Thus, for the reaction

$$
2 \mathrm{~N}_{2} \mathrm{O}_{5}(\mathrm{~g}) \longrightarrow 4 \mathrm{NO}_{2}(g)+\mathrm{O}_{2}(g)
$$

the general rate of reaction has a single value given by the equation

$$
\text { General rate of reaction }=-\frac{1}{2}\left(\frac{\Delta\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]}{\Delta t}\right)=\frac{1}{4}\left(\frac{\Delta\left[\mathrm{NO}_{2}\right]}{\Delta t}\right)=\frac{\Delta\left[\mathrm{O}_{2}\right]}{\Delta t}
$$

In this book, however, we will usually quote reaction rates in terms of the rate of consumption or formation of a specific substance, and will be careful to specify the substance on which the rate is based.

It's also important to specify the time when quoting a rate because the rate changes as the reaction proceeds. For example, the average rate of formation of $\mathrm{NO}_{2}$ is $3.7 \times 10^{-5} \mathrm{M} / \mathrm{s}$ during the time period 300 to 400 s , but it is only $2.2 \times 10^{-5} \mathrm{M} / \mathrm{s}$ during the period 600 to 700 s . Ordinarily, reaction rates decrease as the reaction mixture runs out of reactants, as indicated by the decreasing slopes of the curves in Figure 12.1 as time passes.

Often, chemists want to know the rate of a reaction at a specific time $t$ rather than the rate averaged over a time interval $\Delta t$. For example, what is the rate of formation of $\mathrm{NO}_{2}$ at time $t=350$ s? If we make our measurements at shorter and shorter time intervals, the triangle defined by $\Delta\left[\mathrm{NO}_{2}\right]$ and $\Delta t$ will shrink to a point, and the slope of the hypotenuse of the triangle will approach the slope of the tangent to the curve, as shown in Figure 12.2. The slope of the tangent to a con-centration-versus-time curve at a time $t$ is called the instantaneous rate at that particular time. The instantaneous rate at the beginning of a reaction $(t=0)$ is called the initial rate.

© FIGURE 12.2 Concentration of $\mathrm{NO}_{2}$ versus time when $\mathrm{N}_{2} \mathrm{O}_{5}$ decomposes at $55^{\circ} \mathrm{C}$. The average rate of formation of $\mathrm{NO}_{2}$ during a time interval $\Delta t$ equals the slope of the hypotenuse of the triangle defined by $\Delta\left[\mathrm{NO}_{2}\right]$ and $\Delta t$. As the time interval about the time $t=350$ s gets smaller, the triangle shrinks to a point, and the slope of the hypotenuse approaches the slope of the tangent to the curve at time $t$. The slope of the tangent at time $t$ is defined as the instantaneous rate at that particular time. The initial rate is the slope of the tangent to the curve at $t=0$.

## Worked Example 12.1

Ethanol $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right)$, the active ingredient in alcoholic beverages and an octane booster in gasoline, is produced by fermentation of glucose. The balanced equation is

$$
\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(a q) \longrightarrow 2 \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(a q)+2 \mathrm{CO}_{2}(g)
$$

(a) How is the rate of formation of ethanol related to the rate of consumption of glucose?
(b) Write this relationship in terms of $\Delta\left[\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right] / \Delta t$ and $\Delta\left[\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right] / \Delta t$.

## Strategy

To find the relative rates, look at the coefficients in the balanced chemical equation.

## Solution

(a) According to the balanced equation, 2 mol of ethanol are produced for each mole of glucose that reacts. Therefore, the rate of formation of ethanol is twice the rate of consumption of glucose.
(b) Since the rate of formation of ethanol is $\Delta\left[\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right] / \Delta t$ and the rate of consumption of glucose is $-\Delta\left[\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right] / \Delta t$ (note the minus sign), we can write

$$
\frac{\Delta\left[\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}\right]}{\Delta t}=-2 \frac{\Delta\left[\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right]}{\Delta t}
$$

- PROBLEM 12.1 The oxidation of iodide ion by arsenic acid, $\mathrm{H}_{3} \mathrm{AsO}_{4}$, is described by the balanced equation

$$
3 \mathrm{I}^{-}(a q)+\mathrm{H}_{3} \mathrm{AsO}_{4}(a q)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{I}_{3}^{-}(a q)+\mathrm{H}_{3} \mathrm{AsO}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

(a) If $-\Delta\left[\mathrm{I}^{-}\right] / \Delta t=4.8 \times 10^{-4} \mathrm{M} / \mathrm{s}$, what is the value of $\Delta\left[\mathrm{I}_{3}{ }^{-}\right] / \Delta t$ during the same time interval?
(b) What is the average rate of consumption of $\mathrm{H}^{+}$during that time interval?

- PROBLEM 12.2 Use the data in Table 12.1 to calculate the average rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ and the average rate of formation of $\mathrm{O}_{2}$ during the time interval 200-300 s.


## 12.2 | Rate Laws and Reaction Order

We noted in Section 12.1 that the rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ depends on its concentration, slowing down as the $\mathrm{N}_{2} \mathrm{O}_{5}$ concentration decreases. Ordinarily, the rate of a chemical reaction depends on the concentrations of at least some of the reactants.

Let's consider the general reaction

$$
a \mathrm{~A}+b \mathrm{~B} \longrightarrow \text { Products }
$$

where A and B are the reactants, and $a$ and $b$ are stoichiometric coefficients in the balanced chemical equation. The dependence of the reaction rate on the concentration of each reactant is given by an equation called the rate law.

The rate law is usually written in the form

$$
\text { Rate }=-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}]^{m}[\mathrm{~B}]^{n}
$$

where $k$ is a proportionality constant called the rate constant. We have arbitrarily expressed the rate as the rate of disappearance of $\mathrm{A}(-\Delta[\mathrm{A}] / \Delta t)$, but we could equally well have written it as the rate of disappearance of any reactant (say,
$-\Delta[\mathrm{B}] / \Delta t$ ) or as the rate of appearance of any product. The exponents $m$ and $n$ in the rate law indicate how sensitive the rate is to changes in [A] and [B], and they are usually unrelated to the coefficients $a$ and $b$ in the balanced equation. For the simple reactions discussed in this book, the exponents are usually small positive integers. For more complex reactions, however, the exponents can be negative, zero, or even fractions.

An exponent of 1 means that the rate depends linearly on the concentration of the corresponding reactant. For example, if $m=1$ and [A] is doubled, the rate doubles. If $m=2$ and [A] is doubled, $[A]^{2}$ quadruples and the rate increases by a factor of 4 . Figure 12.3 shows how the rate changes depend on the value of the exponent. When $m$ is zero, the rate is independent of the concentration of A because any number raised to the zeroth power is unity $\left([A]^{0}=1\right)$. When $m$ is negative, the rate decreases as [A] increases. For example, if $m=-1$ and [A] is doubled, $[\mathrm{A}]^{-1}$ is halved and the rate decreases by a factor of 2 .


A FIGURE 12.3 Change in reaction rate when the concentration of a reactant $A$ is doubled for different values of the exponent $m$ in the rate law, rate $=k[\mathrm{~A}]^{m}[\mathrm{~B}]^{n}$. Note that the rate change increases as $m$ increases.

The values of the exponents $m$ and $n$ determine the reaction order with respect to A and B, respectively. The sum of the exponents $(m+n)$ defines the overall reaction order. Thus, if the rate law is

$$
\text { Rate }=k[\mathrm{~A}]^{2}[\mathrm{~B}] \quad m=2 ; n=1 ; \text { and } m+n=3
$$

we say that the reaction is second order in A, first order in B, and third order overall.
The values of the exponents in a rate law must be determined by experiment; they cannot be deduced from the stoichiometry of the reaction. As Table 12.2 shows, there is no


Tionello Pobliani and Mario N. Berberan-Santos, "Inflation Rates, Car Devaluation, and Chemical Kinetics," J. Chem. Educ., Vol. 73, 1996, 950-952.

TABLE 12.2 Balanced Chemical Equations and Experimentally Determined Rate Laws for Some Reactions

| Reaction | Rate Law |
| :--- | :--- |
| $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CBr}(a q)+\mathrm{H}_{2} \mathrm{O}(a q) \longrightarrow\left(\mathrm{CH}_{3}\right)_{3} \mathrm{COH}(a q)+\mathrm{H}^{+}(a q)+\mathrm{Br}^{-}(a q)$ | Rate $=k\left[\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CBr}\right]$ |
| $\mathrm{HCO}_{2} \mathrm{H}(a q)+\mathrm{Br}_{2}(a q) \longrightarrow 2 \mathrm{H}^{+}(a q)+2 \mathrm{Br}^{-}(a q)+\mathrm{CO}_{2}(g)$ | Rate $=k\left[\mathrm{Br}_{2}\right]$ |
| $\mathrm{BrO}_{3}^{-}(a q)+5 \mathrm{Br}^{-}(a q)+6 \mathrm{H}^{+}(a q) \longrightarrow 3 \mathrm{Br}_{2}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)$ | Rate $=k\left[\mathrm{BrO}_{3}^{-}\right]\left[\mathrm{Br}^{-}\right]\left[\mathrm{H}^{+}\right]^{2}$ |
| $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \longrightarrow 2 \mathrm{HI}(g)$ | Rate $=k\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]$ |
| $\mathrm{CH}_{3} \mathrm{CHO}(g) \longrightarrow \mathrm{CH}_{4}(g)+\mathrm{CO}(g)$ | Rate $=k\left[\mathrm{CH}_{3} \mathrm{CHO}\right]^{3 / 2}$ |

general relationship between the stoichiometric coefficients in the balanced chemical equation and the exponents in the rate law. In the first reaction in Table 12.2, for example, the coefficients of $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CBr}$ and $\mathrm{H}_{2} \mathrm{O}$ in the balanced equation are both 1, but the exponents in the rate law are 1 for $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CBr}$ and 0 for $\mathrm{H}_{2} \mathrm{O}$ : Rate $=k\left[\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CBr}\right]^{1}\left[\mathrm{H}_{2} \mathrm{O}\right]^{0}=k\left[\left(\mathrm{CH}_{3}\right)_{3} \mathrm{CBr}\right]$. In Section 12.9, we'll see that the exponents in a rate law depend on the reaction mechanism.

## Worked Example 12.2

Look at the second reaction in Table 12.2, shown in progress in Figure 12.4. What is the order of the reaction with respect to each of the reactants, and what is the overall reaction order?

## Strategy

To find the reaction order with respect to each reactant, look at the exponents in the rate law, not the coefficients in the balanced chemical equation, and then sum the exponents to obtain the overall reaction order.

## Solution

The rate law for the second reaction in Table 12.2 is

$$
\text { Rate }=k\left[\mathrm{Br}_{2}\right]
$$

Because $\mathrm{HCO}_{2} \mathrm{H}$ (formic acid) does not appear in the rate law, the rate is independent of the concentration of $\mathrm{HCO}_{2} \mathrm{H}$, and the reaction is zeroth order in $\mathrm{HCO}_{2} \mathrm{H}$. Because the exponent on $\left[\mathrm{Br}_{2}\right]$ (understood) is 1 , the reaction is first order in $\mathrm{Br}_{2}$. The reaction is first order overall because the sum of the exponents is 1 .


- FIGURE 12.4 The reaction of formic acid $\left(\mathrm{HCO}_{2} \mathrm{H}\right)$ and bromine ( $\mathrm{Br}_{2}$ ). As time passes (left to right), the red color of bromine disappears because $\mathrm{Br}_{2}$ is reduced to the colorless $\mathrm{Br}^{-}$ion. The concentration of $\mathrm{Br}_{2}$ as a function of time, and thus the reaction rate, can be determined by measuring the intensity of the color.

- PROBLEM 12.3 Consider the last three reactions in Table 12.2. What is the order of each reaction in the various reactants, and what is the overall reaction order for each?


## 12.3 | Experimental Determination of a Rate Law

One method of determining the values of the exponents in a rate law is to carry out a series of experiments in which the initial rate of a reaction is measured as a function of different sets of initial concentrations. Consider, for example, the air oxidation of nitric oxide, one of the reactions that contributes to the formation of acid rain:

$$
2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{NO}_{2}(g)
$$

Some initial rate data are collected in Table 12.3.
Note that pairs of experiments are designed to investigate the effect on the initial rate of a change in the initial concentration of a single reactant. In the first two experiments, for example, the concentration of NO is doubled from 0.015 M to 0.030 M while the concentration of $\mathrm{O}_{2}$ is held constant. The initial rate increases by a factor of 4 , from $0.048 \mathrm{M} / \mathrm{s}$ to $0.192 \mathrm{M} / \mathrm{s}$, indicating that the rate depends on the concentration of NO squared, $[\mathrm{NO}]^{2}$. When $[\mathrm{NO}]$ is held constant and $\left[\mathrm{O}_{2}\right]$ is

| Experiment | Initial [NO] | Initial [0 $\left.\mathbf{O}_{\mathbf{2}}\right]$ | Initial Rate of Formation of $\mathbf{N O}_{\mathbf{2}}$ <br> $(\mathbf{M} / \mathbf{s})$ |
| :--- | :--- | :--- | :--- |
| 1 | 0.015 | 0.015 | 0.048 |
| 2 | 0.030 | 0.015 | 0.192 |
| 3 | 0.015 | 0.030 | 0.096 |
| 4 | 0.030 | 0.030 | 0.384 |

doubled (experiments 1 and 3), the initial rate doubles from $0.048 \mathrm{M} / \mathrm{s}$ to 0.096 $\mathrm{M} / \mathrm{s}$, indicating that the rate depends on the concentration of $\mathrm{O}_{2}$ to the first power, $\left[\mathrm{O}_{2}\right]^{1}$. Therefore, the rate law for formation of $\mathrm{NO}_{2}$ is

$$
\text { Rate }=\frac{\Delta\left[\mathrm{NO}_{2}\right]}{\Delta t}=k\left[\mathrm{NO}^{2}\left[\mathrm{O}_{2}\right]\right.
$$

In accord with this rate law, which is second order in NO, first order in $\mathrm{O}_{2}$, and third order overall, the initial rate increases by a factor of 8 when the concentrations of both NO and $\mathrm{O}_{2}$ are doubled (experiments 1 and 4).

The preceding method uses initial rates rather than rates at a later stage of the reaction because chemical reactions are reversible and we want to avoid complications from the reverse reaction: reactants $\leftarrow$ products. As the product concentrations build up, the rate of the reverse reaction increases. If the reverse rate becomes comparable to the forward rate, the measured rate will depend on the concentrations of both reactants and products. At the beginning of the reaction, however, the product concentrations are zero, and therefore the products can't affect the measured rate. When we measure an initial rate, we are measuring the rate of only the forward reaction, so only reactants (and catalysts; see Section 12.12) can appear in the rate law.

One aspect of determining a rate law is to establish the reaction order. Another is to evaluate the numerical value of the rate constant $k$. Each reaction has its own characteristic value of the rate constant, which depends on temperature but does not depend on concentrations. To evaluate $k$ for the formation of $\mathrm{NO}_{2}$, for instance, we can use the data from any one of the experiments in Table 12.3. Solving the rate law for $k$ and substituting the initial rate and concentrations from the first experiment, we obtain

$$
k=\frac{\text { Rate }}{\left[\mathrm{NO}_{2}\right]^{2}\left[\mathrm{O}_{2}\right]}=\frac{0.048 \frac{\mathrm{M}}{\mathrm{~s}}}{(0.015 \mathrm{M})^{2}(0.015 \mathrm{M})}=1.4 \times 10^{4} /\left(\mathrm{M}^{2} \cdot \mathrm{~s}\right)
$$

Try repeating the calculation for experiments $2-4$, and show that you get the same value of $k$. Note that the units of $k$ in this example are $1 /\left(\mathrm{M}^{2} \cdot \mathrm{~s}\right)$, read as "one over molar squared second." Because rates have units of $M / s$, the units of $k$ depend on the number of concentration terms in the rate law and on the values of the exponents. Units for some common cases are given below:

| Rate Law | Overall Reaction Order | Units for $\boldsymbol{k}$ |
| :--- | :--- | :--- |
| Rate $=k$ | Zeroth order | $\mathrm{M} / \mathrm{s} \mathrm{or} \mathrm{M} \mathrm{s} \mathrm{s}^{-1}$ |
| Rate $=k[\mathrm{~A}]$ | First order | $1 / \mathrm{sor} \mathrm{s}^{-1}$ |
| Rate $=k[\mathrm{~A}][\mathrm{B}]$ | Second order | $1 /(\mathrm{M} \cdot \mathrm{s})$ or $\mathrm{M}^{-1} \mathrm{~s}^{-1}$ |
| Rate $=k[\mathrm{~A}][\mathrm{B}]^{2}$ | Third order | $1 /\left(\mathrm{M}^{2} \cdot \mathrm{~s}\right)$ or $\mathrm{M}^{-2} \mathrm{~s}^{-1}$ |

Be careful not to confuse the rate of a reaction and the rate constant. The rate depends on concentrations, whereas the rate constant does not (it is a constant).

The rate always has units of $\mathrm{M} / \mathrm{s}$, whereas the units of the rate constant depend on the overall reaction order.

Worked Example 12.3 gives another instance of how a rate law can be determined from initial rates.

## Worked Example 12.3

Initial rate data for the decomposition of gaseous $\mathrm{N}_{2} \mathrm{O}_{5}$ at $55^{\circ} \mathrm{C}$ are as follows:

| Experiment | Initial $\left[\mathbf{N}_{\mathbf{2}} \mathbf{O}_{\mathbf{5}}\right]$ | Initial Rate of Decomposition <br> of $\mathbf{N}_{\mathbf{2}} \mathbf{O}_{\mathbf{5}} \mathbf{( M / s )}$ |
| :--- | :--- | :--- |
| 1 | 0.020 | $3.4 \times 10^{-5}$ |
| 2 | 0.050 | $8.5 \times 10^{-5}$ |

(a) What is the rate law?
(b) What is the value of the rate constant?

## Strategy

(a) The rate law for the decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ can be written as

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]}{\Delta t}=k\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]^{m}
$$

where $m$ is both the order of the reaction in $\mathrm{N}_{2} \mathrm{O}_{5}$ and the overall reaction order. To find the value of the exponent $m$, compare the change in the initial concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ for experiments 1 and 2 with the change in the initial rate.
(b) To find the value of the rate constant $k$, solve the rate law for $k$ and then substitute in the data from either experiment.

## Solution

(a) Comparing experiments 1 and 2 shows that an increase in the initial concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ by a factor of 2.5 increases the initial rate by a factor of 2.5 :

$$
\frac{\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]_{2}}{\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]_{1}}=\frac{0.050 \mathrm{M}}{0.020 \mathrm{M}}=2.5 \quad \frac{(\text { Rate })_{2}}{(\text { Rate })_{1}}=\frac{8.5 \times 10^{-5} \mathrm{M} / \mathrm{s}}{3.4 \times 10^{-5} \mathrm{M} / \mathrm{s}}=2.5
$$

The rate depends linearly on the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$, and therefore the rate law is

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]}{\Delta t}=k\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]
$$

The reaction is first order in $\mathrm{N}_{2} \mathrm{O}_{5}$. If the rate had increased by a factor of $(2.5)^{2}=6.25$, the reaction would have been second order in $\mathrm{N}_{2} \mathrm{O}_{5}$. If the rate had increased by a factor of $(2.5)^{3}=15.6$, the reaction would have been third order in $\mathrm{N}_{2} \mathrm{O}_{5}$; and so on.

A more formal way to approach this problem is to write the rate law for each experiment:

$$
(\text { Rate })_{1}=k\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]_{1}=k(0.020 \mathrm{M})^{m} \quad(\text { Rate })_{2}=k\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]_{2}=k(0.050 \mathrm{M})^{m}
$$

If we then divide the second equation by the first, we obtain

$$
\frac{(\text { Rate })_{2}}{(\text { Rate })_{1}}=\frac{k(0.050 \mathrm{M})^{m}}{k(0.020 \mathrm{M})^{m}}=(2.5)^{m}
$$

Comparing this ratio to the ratio of the experimental rates,

$$
\frac{(\text { Rate })_{2}}{(\text { Rate })_{1}}=\frac{8.5 \times 10^{-5} \mathrm{M} / \mathrm{s}}{3.4 \times 10^{-5} \mathrm{M} / \mathrm{s}}=2.5
$$

shows that the exponent $m$ must have a value of 1 . Therefore, the rate law is

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]}{\Delta t}=k\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]
$$

(b) Solving the rate law for $k$ and substituting in the data from the first experiment gives

$$
k=\frac{\text { Rate }}{\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]}=\frac{3.4 \times 10^{-5} \frac{\mathrm{M}}{\mathrm{~s}}}{0.020 \mathrm{M}}=1.7 \times 10^{-3} \mathrm{~s}^{-1}
$$

The units of $k, 1 / \mathrm{s}^{\text {or } \mathrm{s}^{-1}}$, are given by the ratio of the units for the rate and the concentration. These are the expected units for a first-order reaction.

## Worked Example 12.4

What is the rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ at $55^{\circ} \mathrm{C}$ when its concentration is 0.030 M ? (See Worked Example 12.3.)

## Strategy

Calculate the rate by substituting the rate constant found in Worked Example 12.3 $\left(1.7 \times 10^{-3} \mathrm{~s}^{-1}\right)$ and the given concentration $(0.030 \mathrm{M})$ into the rate law.

## Solution

Rate $=-\frac{\Delta\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]}{\Delta t}=k\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]=\left(\frac{1.7 \times 10^{-3}}{\mathrm{~s}}\right)(0.030 \mathrm{M})=5.1 \times 10^{-5} \mathrm{M} / \mathrm{s}$
$\checkmark$ Ballpark Check Because the reaction is first order in $\mathrm{N}_{2} \mathrm{O}_{5}$ and the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ is $3 / 2$ times that in experiment 1 of Worked Example 12.3, the decomposition rate will increase by a factor of $3 / 2$ from $3.4 \times 10^{-5} \mathrm{M} / \mathrm{s}$ to about $5 \times 10^{-5} \mathrm{M} / \mathrm{s}$, which agrees with the detailed solution.

PROBLEM 12.4 The oxidation of iodide ion by hydrogen peroxide in an acidic solution is described by the balanced equation:

$$
\mathrm{H}_{2} \mathrm{O}_{2}(a q)+3 \mathrm{I}^{-}(a q)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{I}_{3}^{-}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

The rate of formation of the red-colored triiodide ion, $\Delta\left[I_{3}{ }^{-}\right] / \Delta t$, can be determined by measuring the rate of appearance of the color (Figure 12.5). Following are initial rate data at $25^{\circ} \mathrm{C}$ :

| Experiment | Initial $\left[\mathbf{H}_{\mathbf{2}} \mathbf{O}_{\mathbf{2}}\right]$ | Initial $\left[\mathbf{I}^{-}\right]$ | Initial Rate of Formation <br> of $\mathbf{I}_{\mathbf{3}}{ }^{-}(\mathbf{M} / \mathbf{s})$ |
| :--- | :--- | :--- | :--- |
| 1 | 0.100 | 0.100 | $1.15 \times 10^{-4}$ |
| 2 | 0.100 | 0.200 | $2.30 \times 10^{-4}$ |
| 3 | 0.200 | 0.100 | $2.30 \times 10^{-4}$ |
| 4 | 0.200 | 0.200 | $4.60 \times 10^{-4}$ |

(a) What is the rate law for formation of $\mathrm{I}_{3}{ }^{-}$?
(b) What is the value of the rate constant?
(c) What is the rate of formation of $\mathrm{I}_{3}{ }^{-}$when the concentrations are $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]=$ 0.300 M and $\left[\mathrm{I}^{-}\right]=0.400 \mathrm{M}$ ?

- FIGURE 12.5 A sequence of photographs showing the progress of the reaction of hydrogen peroxide $\left(\mathrm{H}_{2} \mathrm{O}_{2}\right)$ and iodide ion ( $\mathrm{I}^{-}$). As time passes (left to right), the red color due to triiodide ion $\left(\mathrm{I}_{3}{ }^{-}\right)$ increases in intensity.

- PROBLEM 12.5 What are the units of the rate constant for each of the reactions in Table 12.2?
- KEY CONCEPT PROBLEM 12.6 The relative rates of the reaction $\mathrm{A}+\mathrm{B} \rightarrow$ products in vessels (a)-(d) are 1:1:4:4. Red spheres represent A molecules, and blue spheres represent B molecules.

(a) What is the order of the reaction in $A$ and $B$, and what is the overall reaction order?
(b) Write the rate law.


## 12.4 | Integrated Rate Law for a First-Order Reaction

Thus far we've focused on the rate law, an equation that tells how a reaction rate depends on reactant concentrations. We're also interested, however, in how reactant and product concentrations vary with time. For example, it's important to know the rate at which the atmospheric ozone layer is being destroyed by air pollutants, but we also want to know what the ozone concentration will be 50 years from now and how long it will take for the concentration to be reduced by a given amount, say, $10 \%$.

Because the kinetics of the pollution-induced decomposition of ozone is a very complicated problem, let's consider instead a simple, general first-order reaction

$$
\mathrm{A} \longrightarrow \text { Products }
$$

A first-order reaction is one whose rate depends on the concentration of a single reactant raised to the first power.

$$
\text { Rate }=-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}]
$$

An example is the decomposition of hydrogen peroxide in basic solution, which we'll discuss in Worked Example 12.5 at the end of this section:

$$
2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g)
$$

Using calculus, it's possible to convert the rate law to another form, called the integrated rate law:

$$
\ln \frac{[\mathrm{A}]_{t}}{[\mathrm{~A}]_{0}}=-k t
$$

In this equation, $\ln$ denotes the natural logarithm, $[\mathrm{A}]_{0}$ designates the concentration of A at some initial time, arbitrarily considered to be $t=0$, and $[\mathrm{A}]_{t}$ is the concentration of A at any time $t$ thereafter. (See Appendix A. 2 for a review of logarithms.) The ratio $[\mathrm{A}]_{t} /[\mathrm{A}]_{0}$ is the fraction of A that remains at time $t$. Thus, the integrated rate law is a concentration-time equation that makes it possible to calculate the concentration of A at any time $t$ or the fraction of A that remains at any time $t$. The integrated rate law can also be used to calculate the time required for the initial concentration of A to drop to any particular value or to any particular fraction of its initial concentration (Figure 12.6a). Worked Example 12.5 shows how to use the integrated rate law.

Since $\ln \left([\mathrm{A}]_{t} /[\mathrm{A}]_{0}\right)=\ln [\mathrm{A}]_{t}-\ln [\mathrm{A}]_{0}$, we can rewrite the integrated rate law as

$$
\ln [\mathrm{A}]_{t}=-k t+\ln [\mathrm{A}]_{0}
$$

This equation is of the form $y=m x+b$, which says that $\ln [A]_{t}$ is a linear function of time:


If we graph $\ln [A]$ versus time, we obtain a straight line having a slope $m=-k$ and an intercept $b=\ln [A]_{0}$ (Figure 12.6 b ). The value of the rate constant is simply equal to minus the slope of the straight line:

$$
k=-(\text { Slope })
$$



This graphical method of determining a rate constant, illustrated in Worked Example 12.6, is an alternative to the method of initial rates used in Worked Example 12.3. It should be emphasized, however, that a plot of $\ln [A]$ versus time will give a straight line only if the reaction is first order in A. Indeed, a good way of testing whether a reaction is first order is to examine the appearance of such a plot.

## Worked Example 12.5

The decomposition of hydrogen peroxide in dilute sodium hydroxide solution is described by the equation

$$
2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g)
$$

The reaction is first order in $\mathrm{H}_{2} \mathrm{O}_{2}$, the rate constant for consumption of $\mathrm{H}_{2} \mathrm{O}_{2}$ at $20^{\circ} \mathrm{C}$ is $1.8 \times 10^{-5} \mathrm{~s}^{-1}$, and the initial concentration of $\mathrm{H}_{2} \mathrm{O}_{2}$ is 0.30 M .
(a) What is the concentration of $\mathrm{H}_{2} \mathrm{O}_{2}$ after 4.00 h ?
(b) How long will it take for the $\mathrm{H}_{2} \mathrm{O}_{2}$ concentration to drop to 0.12 M ?
(c) How long will it take for $90 \%$ of the $\mathrm{H}_{2} \mathrm{O}_{2}$ to decompose?

## Strategy

Since this reaction has a first-order rate law, $-\Delta\left[\mathrm{H}_{2} \mathrm{O}_{2}\right] / \Delta t=k\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]$, we can use the corresponding concentration-time equation for a first-order reaction:

$$
\ln \frac{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{t}}{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{0}}=-k t
$$

In each part, we substitute the known quantities into this equation and solve for the unknown.

FIGURE 12.6 Plots of (a) reactant concentration versus time and (b) natural logarithm of reactant concentration versus time for a first-order reaction. A first-order reaction exhibits an exponential decay of the reactant concentration (a) and a linear decay of the logarithm of the reactant concentration (b). The slope of the plot of $\ln [\mathrm{A}]$ versus time gives the rate constant.

## Solution

(a) Because $k$ has units of $\mathrm{s}^{-1}$, we must first convert the time from hours to seconds:

$$
t=(4.00 \mathrm{~h})\left(\frac{60 \mathrm{~min}}{\mathrm{~h}}\right)\left(\frac{60 \mathrm{~s}}{\mathrm{~min}}\right)=14,400 \mathrm{~s}
$$

Then, substitute the values of $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{0}, k$, and $t$ into the concentration-time equation:

$$
\ln \frac{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{t}}{0.30 \mathrm{M}}=-\left(1.8 \times 10^{-5} \mathrm{~s}^{-1}\right)\left(1.44 \times 10^{4} \mathrm{~s}\right)=-0.259
$$

Taking the antilogarithm (antiln) of both sides gives

$$
\begin{aligned}
& \frac{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{t}}{0.30 \mathrm{M}}=e^{-0.259}=0.772 \\
& {\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{t}=(0.772)(0.30 \mathrm{M})=0.23 \mathrm{M}}
\end{aligned}
$$

(b) First, solve the concentration-time equation for the time:

$$
t=-\frac{1}{k} \ln \frac{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{t}}{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{0}}
$$

Then evaluate the time by substituting the concentrations and the value of $k$ :

$$
t=-\left(\frac{1}{1.8 \times 10^{-5} \mathrm{~s}^{-1}}\right) \ln \frac{0.12 \mathrm{M}}{0.30 \mathrm{M}}=-\left(\frac{1}{1.8 \times 10^{-5} \mathrm{~s}^{-1}}\right)(-0.916)=5.1 \times 10^{4} \mathrm{~s}
$$

Thus, the $\mathrm{H}_{2} \mathrm{O}_{2}$ concentration reaches 0.12 M at a time of $5.1 \times 10^{4} \mathrm{~s}(14 \mathrm{~h})$.
(c) When $90 \%$ of the $\mathrm{H}_{2} \mathrm{O}_{2}$ has decomposed, $10 \%$ remains. Therefore,

$$
\frac{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{t}}{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{0}}=\frac{(0.10)(0.30 \mathrm{M})}{0.30 \mathrm{M}}=0.10
$$

The time required for $90 \%$ decomposition is
$t=-\left(\frac{1}{1.8 \times 10^{-5} \mathrm{~s}^{-1}}\right) \ln 0.10=-\left(\frac{1}{1.8 \times 10^{-5} \mathrm{~s}^{-1}}\right)(-2.30)=1.3 \times 10^{5} \mathrm{~s}$
$\checkmark$ BALLPARK CHECK The concentration of $\mathrm{H}_{2} \mathrm{O}_{2}(0.23 \mathrm{M})$ after 4.00 h is less than the initial concentration $(0.30 \mathrm{M})$. A longer period of time $(14 \mathrm{~h})$ is required for the concentration to drop to 0.12 M , and a still more time ( 36 h ) is needed for the concentration to fall to 0.030 M ( $10 \%$ of the original concentration). These results look reasonable. A plot of $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]$ versus time would exhibit an exponential decay of the $\mathrm{H}_{2} \mathrm{O}_{2}$ concentration, as expected for a first-order reaction.

## Worked Example 12.6

Experimental concentration-versus-time data for the decomposition of gaseous $\mathrm{N}_{2} \mathrm{O}_{5}$ at $55^{\circ} \mathrm{C}$ are listed in Table 12.1 and are plotted in Figure 12.1. Use those data to confirm that the decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ is a first-order reaction. What is the value of the rate constant for consumption of $\mathrm{N}_{2} \mathrm{O}_{5}$ ?

## Strategy

To confirm that the reaction is first order, check to see if a plot of $\ln \left[\mathrm{N}_{2} \mathrm{O}_{5}\right]$ versus time gives a straight line. The rate constant for a first-order reaction equals minus the slope of the straight line.

## Solution

Values of $\ln \left[\mathrm{N}_{2} \mathrm{O}_{5}\right]$ are listed in the following table and are plotted versus time in the graph:


Because the data points lie on a straight line, the reaction is first order in $\mathrm{N}_{2} \mathrm{O}_{5}$. The slope of the line can be determined from the coordinates of any two widely separated points on the line, and the rate constant $k$ can be calculated from the slope:

$$
\begin{aligned}
\text { Slope } & =\frac{\Delta y}{\Delta x}=\frac{(-5.02)-(-4.17)}{650 \mathrm{~s}-150 \mathrm{~s}}=\frac{-0.85}{500 \mathrm{~s}}=-1.7 \times 10^{-3} \mathrm{~s}^{-1} \\
k & =-(\text { Slope })=1.7 \times 10^{-3} \mathrm{~s}^{-1}
\end{aligned}
$$

Note that the slope is negative, $k$ is positive, and the value of $k$ agrees with the value obtained earlier in Worked Example 12.3 by the method of initial rates.

- PROBLEM 12.7 In acidic aqueous solution, the complex ion $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}^{2+}$ undergoes a slow reaction in which the bromide ion is replaced by a water molecule:

$$
\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}^{2+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)^{3+}(a q)+\mathrm{Br}^{-}(a q)
$$

The reaction is first order in $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}^{2+}$, the rate constant at $25^{\circ} \mathrm{C}$ is $6.3 \times 10^{-6} \mathrm{~s}^{-1}$, and the initial concentration of $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}^{2+}$ is 0.100 M .
(a) What is its molarity after a reaction time of 10.0 h ?
(b) How many hours are required for $75 \%$ of the $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}^{2+}$ to react?

- PROBLEM 12.8 At high temperatures, cyclopropane is converted to propene, the material from which polypropylene plastics are made:


Given the following concentration data, test whether the reaction is first order and calculate the value of the rate constant.

| Time (min) | 0 | 5.0 | 10.0 | 15.0 | 20.0 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| [Cyclopropane] | 0.098 | 0.080 | 0.066 | 0.054 | 0.044 |

## 12.5 | Half-Life of a First-Order Reaction

The half-life of a reaction, symbolized by $t_{1 / 2}$, is the time required for the reactant concentration to drop to one-half of its initial value. Consider the first-order reaction

$$
\mathrm{A} \longrightarrow \text { Products }
$$


$\triangle$ The purple complex ion $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}^{2+}$ (left) reacts with water in acidic solution, yielding the pinkish-orange complex ion $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)^{3+}$ (right).

First-Order Process movie

## Rates of Reaction activity

To relate the reaction's half-life to the rate constant, let's begin with the integrated rate law:

$$
\ln \frac{[\mathrm{A}]_{t}}{[\mathrm{~A}]_{0}}=-k t
$$

When $t=t_{1 / 2}$, the fraction of A that remains, $[\mathrm{A}]_{t} /[\mathrm{A}]_{0}$, is $1 / 2$. Therefore,

$$
\begin{aligned}
\ln \frac{1}{2} & =-k t_{1 / 2} \\
\text { so } \quad t_{1 / 2} & =\frac{-\ln \frac{1}{2}}{k}=\frac{\ln 2}{k} \\
\text { or } \quad t_{1 / 2} & =\frac{0.693}{k}
\end{aligned}
$$

Thus, the half-life of a first-order reaction is readily calculated from the rate constant, and vice versa.

The half-life of a first-order reaction is a constant because it depends only on the rate constant and not on the reactant concentration. This point is worth noting because reactions that are not first order have half-lives that do depend on concentration; that is, the amount of time in one half-life changes as the reactant concentration changes for a non-first-order reaction.

The constancy of the half-life for a first-order reaction is illustrated in Figure 12.7. Each successive half-life is an equal period of time in which the reactant concentration decreases by a factor of 2 . We'll see in Chapter 22 that half-lives are widely used in describing radioactive decay rates.


A FIGURE 12.7 Concentration of a reactant A as a function of time for a first-order reaction. The concentration falls from its initial value, $[\mathrm{A}]_{0}$, to $[\mathrm{A}]_{0} / 2$ after one half-life, to $[\mathrm{A}]_{0} / 4$ after a second half-life, to $[\mathrm{A}]_{0} / 8$ after a third half-life, and so on. For a first-order reaction, each half-life represents an equal amount of time.

## Worked Example 12.7

(a) Estimate the half-life for the decomposition of gaseous $\mathrm{N}_{2} \mathrm{O}_{5}$ at $55^{\circ} \mathrm{C}$ from the concentration-versus-time plot in Figure 12.1.
(b) Calculate the half-life from the rate constant $\left(1.7 \times 10^{-3} \mathrm{~s}^{-1}\right)$.
(c) If the initial concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ is 0.020 M , what is the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ after five half-lives?
(d) How long will it take for the $\mathrm{N}_{2} \mathrm{O}_{5}$ concentration to fall to $12.5 \%$ of its initial value?

## Strategy

Because the decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ is a first-order reaction (Worked Example 12.6), we can determine its half-life either from the time required for $\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]$ to drop to onehalf of its initial value or from the equation $t_{1 / 2}=0.693 / k$. To find $\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]$ after $n$ halflives, multiply its initial concentration by $(1 / 2)^{n}$ since $\left[\mathrm{N}_{2} \mathrm{O}_{5}\right.$ ] drops by a factor of 2 during each successive half-life.

## Solution

(a) Figure 12.1 shows that the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ falls from 0.020 M to 0.010 M during a time period of approximately 400 s . At $800 \mathrm{~s},\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]$ has decreased by another factor of 2 , to 0.0050 M . Therefore, $t_{1 / 2} \approx 400 \mathrm{~s}$.
(b) Based on the value of the rate constant,

$$
t_{1 / 2}=\frac{0.693}{k}=\frac{0.693}{1.7 \times 10^{-3} \mathrm{~s}^{-1}}=4.1 \times 10^{2} \mathrm{~s}(6.8 \mathrm{~min})
$$

(c) At $5 t_{1 / 2},\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]$ will be $(1 / 2)^{5}=1 / 32$ of its initial value. Therefore,

$$
\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]=\frac{0.020 \mathrm{M}}{32}=0.00062 \mathrm{M}
$$

(d) Since $12.5 \%$ of the initial concentration corresponds to $1 / 8$ or $(1 / 2)^{3}$ of the initial concentration, the time required is three half-lives:

$$
t=3 t_{1 / 2}=3\left(4.1 \times 10^{2} \mathrm{~s}\right)=1.2 \times 10^{3} \mathrm{~s}(20 \mathrm{~min})
$$

PROBLEM 12.9 Consider the first-order decomposition of $\mathrm{H}_{2} \mathrm{O}_{2}$ in Worked Example 12.5.
(a) What is the half-life (in hours) of the reaction at $20^{\circ} \mathrm{C}$ ?
(b) What is the molarity of $\mathrm{H}_{2} \mathrm{O}_{2}$ after four half-lives if the initial concentration of $\mathrm{H}_{2} \mathrm{O}_{2}$ is 0.30 M ?
(c) How many hours will it take for the concentration to drop to $25 \%$ of its initial value?

KEY CONCEPT PROBLEM 12.10 Consider the first-order reaction $A \rightarrow B$ in which A molecules (red spheres) are converted to B molecules (blue spheres).
(a) Given the following pictures at $t=0 \mathrm{~min}$ and $t=10 \mathrm{~min}$, what is the half-life of the reaction?
(b) Draw a picture that shows the number of A and B molecules present at $t=15 \mathrm{~min}$.


Integrated Rate Law, Second-Order Reaction activity

## 12.6 | Second-Order Reactions

A second-order reaction is one whose rate depends on the concentration of a single reactant raised to the second power or on the concentrations of two different reactants, each raised to the first power. For the simpler type, $\mathrm{A} \rightarrow$ products, the rate law is

$$
\text { Rate }=-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}]^{2}
$$

An example is the thermal decomposition of nitrogen dioxide to yield NO and $\mathrm{O}_{2}$ :

$$
2 \mathrm{NO}_{2}(g) \longrightarrow 2 \mathrm{NO}(g)+\mathrm{O}_{2}(g)
$$

Using calculus, it's possible to convert the rate law to the integrated rate law

$$
\frac{1}{[\mathrm{~A}]_{t}}=k t+\frac{1}{[\mathrm{~A}]_{0}}
$$

This integrated rate law then allows us to calculate the concentration of A at any time $t$ if the initial concentration $[\mathrm{A}]_{0}$ is known.

Since the integrated rate law has the form $y=m x+b$, a graph of $1 /[A]$ versus time is a straight line if the reaction is second order:


The slope of the straight line is the rate constant $k$, and the intercept is $1 /[\mathrm{A}]_{0}$. Thus, by plotting $1 /[\mathrm{A}]$ versus time, we can test whether the reaction is second order and can determine the value of the rate constant (see Worked Example 12.8).

We can obtain an expression for the half-life of a second-order reaction by substituting $[\mathrm{A}]_{t}=[\mathrm{A}]_{0} / 2$ and $t=t_{1 / 2}$ into the integrated rate law:


A FIGURE 12.8 Concentration of a reactant A as a function of time for a second-order reaction. Note that each half-life is twice as long as the preceding one because $t_{1 / 2}=1 / k[\mathrm{~A}]_{0}$ and the concentration of A at the beginning of each successive half-life is smaller by a factor of 2 .

$$
\begin{aligned}
& \quad \frac{1}{\left(\frac{[\mathrm{~A}]_{0}}{2}\right)}=k t_{1 / 2}+\frac{1}{[\mathrm{~A}]_{0}} \\
& \text { so } \quad t_{1 / 2}=\frac{1}{k}\left(\frac{2}{[\mathrm{~A}]_{0}}-\frac{1}{[\mathrm{~A}]_{0}}\right) \\
& \text { or } \quad t_{1 / 2}=\frac{1}{k[\mathrm{~A}]_{0}}
\end{aligned}
$$

In contrast with a first-order reaction, the time required for the concentration of A to drop to one-half of its initial value in a second-order reaction depends on both the rate constant and the initial concentration. Thus, the value of $t_{1 / 2}$ increases as the reaction proceeds because the value of $[\mathrm{A}]_{0}$ at the beginning of each successive half-life is smaller by a factor of 2 . Consequently, each half-life for a second-order reaction is twice as long as the preceding one (Figure 12.8).

Table 12.4 summarizes some important differences between first-order and second-order reactions of the type $\mathrm{A} \rightarrow$ products.

TABLE 12.4 Characteristics of First- and Second-Order Reactions of the Type

## $\mathrm{A} \longrightarrow$ Products

## First-Order <br> Second-Order

Rate law $-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}] \quad-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}]^{2}$

Concentration-time equation
$\ln [\mathrm{A}]_{t}=-k t+\ln [\mathrm{A}]_{0} \quad \frac{1}{[\mathrm{~A}]_{t}}=k t+\frac{1}{[\mathrm{~A}]_{0}}$
Linear graph
Graphical determination of $k$
Half-life
$\ln [\mathrm{A}]$ versus $t \quad \frac{1}{[\mathrm{~A}]}$ versus $t$
$k=-$ (Slope $) \quad k=$ Slope
$t_{1 / 2}=\frac{0.693}{k}$
(constant)
$t_{1 / 2}=\frac{1}{k[\mathrm{~A}]_{0}}$
(not constant)

## Worked Example 12.8

At elevated temperatures, nitrogen dioxide decomposes to nitric oxide and molecular oxygen:

$$
2 \mathrm{NO}_{2}(g) \longrightarrow 2 \mathrm{NO}(g)+\mathrm{O}_{2}(g)
$$

Concentration-time data for consumption of $\mathrm{NO}_{2}$ at $300^{\circ} \mathrm{C}$ are as follows:

| Time (s) | $\mathbf{[ N \mathbf { N O } _ { \mathbf { 2 } } ]}$ | Time (s) | [NO $\mathbf{2}]$ |
| :---: | :--- | :--- | :--- |
| 0 | $8.00 \times 10^{-3}$ | 200 | $4.29 \times 10^{-3}$ |
| 50 | $6.58 \times 10^{-3}$ | 300 | $3.48 \times 10^{-3}$ |
| 100 | $5.59 \times 10^{-3}$ | 400 | $2.93 \times 10^{-3}$ |
| 150 | $4.85 \times 10^{-3}$ | 500 | $2.53 \times 10^{-3}$ |

(a) Is the reaction first order or second order?
(b) What is the value of the rate constant?
(c) What is the concentration of $\mathrm{NO}_{2}$ at $t=20.0 \mathrm{~min}$ ?
(d) What is the half-life of the reaction when the initial concentration of $\mathrm{NO}_{2}$ is $6.00 \times 10^{-3} \mathrm{M}$ ?
(e) What is $t_{1 / 2}$ when $\left[\mathrm{NO}_{2}\right]_{0}$ is $3.00 \times 10^{-3} \mathrm{M}$ ?

## Strategy

To determine whether the reaction is first order or second order, calculate values of $\ln \left[\mathrm{NO}_{2}\right]$ and $1 /\left[\mathrm{NO}_{2}\right]$, and then graph these values versus time. The rate constant can be obtained from the slope of the straight-line plot, and concentrations and half-lives can be calculated from the appropriate equation in Table 12.4.

## Solution

(a) The plot of $\ln \left[\mathrm{NO}_{2}\right]$ versus time is curved, but the plot of $1 /\left[\mathrm{NO}_{2}\right]$ versus time is a straight line. The reaction is therefore second order in $\mathrm{NO}_{2}$.

| Time (s) | $\mathbf{[ \mathbf { N O } _ { \mathbf { 2 } } ]}$ | $\mathbf{l n}\left[\mathbf{N O}_{\mathbf{2}}\right]$ | $\mathbf{1} /\left[\mathbf{N O}_{\mathbf{2}}\right]$ |
| :---: | :--- | :--- | :--- |
| 0 | $8.00 \times 10^{-3}$ | -4.828 | 125 |
| 50 | $6.58 \times 10^{-3}$ | -5.024 | 152 |
| 100 | $5.59 \times 10^{-3}$ | -5.187 | 179 |
| 150 | $4.85 \times 10^{-3}$ | -5.329 | 206 |
| 200 | $4.29 \times 10^{-3}$ | -5.451 | 233 |
| 300 | $3.48 \times 10^{-3}$ | -5.661 | 287 |
| 400 | $2.93 \times 10^{-3}$ | -5.833 | 341 |
| 500 | $2.53 \times 10^{-3}$ | -5.980 | 395 |



(b) The rate constant equals the slope of the straight line in the plot of $1 /\left[\mathrm{NO}_{2}\right]$ versus time, which we can estimate from the coordinates of two widely separated points on the line:

$$
k=\text { Slope }=\frac{\Delta y}{\Delta x}=\frac{340 \mathrm{M}^{-1}-150 \mathrm{M}^{-1}}{400 \mathrm{~s}-50 \mathrm{~s}}=\frac{190 \mathrm{M}^{-1}}{350 \mathrm{~s}}=0.54 /(\mathrm{M} \cdot \mathrm{~s})
$$

(c) The concentration of $\mathrm{NO}_{2}$ at $t=20.0 \mathrm{~min}\left(1.20 \times 10^{3} \mathrm{~s}\right)$ can be calculated using the integrated rate law:

$$
\frac{1}{\left[\mathrm{NO}_{2}\right]_{t}}=k t+\frac{1}{\left[\mathrm{NO}_{2}\right]_{0}}
$$

Substituting the values of $k, t$, and $\left[\mathrm{NO}_{2}\right]_{0}$ gives

$$
\begin{aligned}
\frac{1}{\left[\mathrm{NO}_{2}\right]_{t}} & =\left(\frac{0.54}{\mathrm{M} \cdot \mathrm{~s}}\right)\left(1.20 \times 10^{3} \mathrm{~s}\right)+\frac{1}{8.00 \times 10^{-3} \mathrm{M}} \\
& =\frac{648}{\mathrm{M}}+\frac{125}{\mathrm{M}}=\frac{773}{\mathrm{M}} \\
{\left[\mathrm{NO}_{2}\right]_{t} } & =1.3 \times 10^{-3} \mathrm{M}
\end{aligned}
$$

(d) The half-life of a second-order reaction can be calculated from the rate constant and the initial concentration of $\mathrm{NO}_{2}\left(6.00 \times 10^{-3} \mathrm{M}\right)$ :

$$
t_{1 / 2}=\frac{1}{k\left[\mathrm{NO}_{2}\right]_{0}}=\frac{1}{\left(\frac{0.54}{\mathrm{M} \cdot \mathrm{~s}}\right)\left(6.00 \times 10^{-3} \mathrm{M}\right)}=3.1 \times 10^{2} \mathrm{~s}
$$

(e) When $\left[\mathrm{NO}_{2}\right]_{0}$ is $3.00 \times 10^{-3} \mathrm{M}, t_{1 / 2}=6.2 \times 10^{2} \mathrm{~s}$ (twice as long as when $\left[\mathrm{NO}_{2}\right]_{0}$ is $6.00 \times 10^{-3} \mathrm{M}$ because $\left[\mathrm{NO}_{2}\right]_{0}$ is now smaller by a factor of 2 ).

- PROBLEM 12.11 Hydrogen iodide gas decomposes at $410^{\circ} \mathrm{C}$ :

$$
2 \mathrm{HI}(g) \longrightarrow \mathrm{H}_{2}(g)+\mathrm{I}_{2}(g)
$$

The following data describe this decomposition.

| Time (min) | 0 | 20 | 40 | 60 | 80 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| [HI] | 0.500 | 0.382 | 0.310 | 0.260 | 0.224 |

(a) Is the reaction first order or second order?
(b) What is the value of the rate constant for consumption of HI ?
(c) At what time (in minutes) does the HI concentration reach 0.100 M ?
(d) How many minutes does it take for the HI concentration to drop from 0.400 M to 0.200 M ?

## 12.7 | Zeroth-Order Reactions

A zeroth-order reaction of the type $\mathrm{A} \rightarrow$ products is one that has the rate law

$$
\text { Rate }=-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}]^{0}=k(1)=k
$$

Throughout the course of the reaction, the rate remains constant $(=k)$, independent of the concentration of the reactant. The integrated rate law is

$$
[\mathrm{A}]=-k t+[\mathrm{A}]_{0}
$$

This is another equation of the form $y=m x+b$, so a graph of [A] versus time is a straight line with a slope $=-k$ (Figure 12.9). Note that both the rate constant $k$ and the rate of a zeroth-order reaction have a constant value equal to minus the slope of the [A] versus time plot.

Zeroth-order reactions are relatively uncommon, but they can occur under special circumstances. Take, for example, the decomposition of gaseous ammonia on a hot platinum surface:

$$
2 \mathrm{NH}_{3}(g) \xrightarrow[\text { Pt catalyst }]{1130 \mathrm{~K}} \mathrm{~N}_{2}(g)+3 \mathrm{H}_{2}(g)
$$

The platinum surface is completely covered by an attached layer of $\mathrm{NH}_{3}$ molecules, but the number of $\mathrm{NH}_{3}$ molecules that can fit on the surface is limited by geometrical constraints, and is very small compared with the total number of $\mathrm{NH}_{3}$ molecules. Most of the $\mathrm{NH}_{3}$ is in the gas phase above the surface. As $\mathrm{NH}_{3}$ molecules on the surface decompose, they are replaced by molecules from the gas phase, so the number of $\mathrm{NH}_{3}$ molecules on the surface remains constant. Because only the $\mathrm{NH}_{3}$ molecules on the surface react under these conditions, the reaction rate is independent of the total concentration of $\mathrm{NH}_{3}$ :

$$
\text { Rate }=-\Delta\left[\mathrm{NH}_{3}\right] / \Delta t=k\left[\mathrm{NH}_{3}\right]^{0}=k
$$

## Francisco J. Arnaiz, "Mice in

 the Box for Zero-Order Kinetics," J. Chem. Educ., Vol. 76, 1999, 1458.

## FIGURE 12.9

Concentration of a reactant A as a function of time for a zeroth-order reaction.

John J. Fortman, "Pictorial
Analogies XIII: Kinetics and Mechanisms," J. Chem. Educ., Vol. 71, 1994, 848-849.

$\square$Arthur M. Last, "Doing the Dishes: An Analogy for Use in Teaching Reaction Kinetics," J. Chem. Educ., Vol. 62, 1985, 1015-1016.

## 12.8| Reaction Mechanisms

Thus far, our discussion of chemical kinetics has centered on reaction rates. We've seen that the rate of a reaction usually depends on both reactant concentrations and the value of the rate constant. An equally important issue in chemical kinetics is the reaction mechanism, the sequence of molecular events, or reaction steps, that defines the pathway from reactants to products. Chemists want to know the sequence in which the various reaction steps take place so they can better control known reactions and predict new ones.
$\begin{array}{ll}- \text { Reaction Mechanism } & \begin{array}{l}\text { The sequence of reaction steps that defines the path- } \\ \text { way from reactants to products. }\end{array}\end{array}$
A single step in a reaction mechanism is called an elementary reaction or elementary step. To clarify the crucial distinction between an elementary reaction and an overall reaction, let's consider the gas-phase reaction of nitrogen dioxide and carbon monoxide to give nitric oxide and carbon dioxide:

$$
\mathrm{NO}_{2}(g)+\mathrm{CO}(g) \longrightarrow \mathrm{NO}(g)+\mathrm{CO}_{2}(g) \quad \text { Overall reaction }
$$

Experimental evidence suggests that this reaction takes place by a two-step mechanism:

Step 1. $\mathrm{NO}_{2}(g)+\mathrm{NO}_{2}(g) \longrightarrow \mathrm{NO}(g)+\mathrm{NO}_{3}(g) \quad$ Elementary reaction
Step 2. $\mathrm{NO}_{3}(g)+\mathrm{CO}(g) \longrightarrow \mathrm{NO}_{2}(g)+\mathrm{CO}_{2}(g) \quad$ Elementary reaction
In the first elementary step, two $\mathrm{NO}_{2}$ molecules collide with enough energy to break one $\mathrm{N}-\mathrm{O}$ bond and form another, resulting in the transfer of an oxygen atom from one $\mathrm{NO}_{2}$ molecule to the other. In the second step, the $\mathrm{NO}_{3}$ molecule formed in the first step collides with a CO molecule, and the transfer of an oxygen atom from $\mathrm{NO}_{3}$ to CO yields an $\mathrm{NO}_{2}$ molecule and a $\mathrm{CO}_{2}$ molecule (Figure 12.10).


- FIGURE 12.10 Elementary steps in the reaction of $\mathrm{NO}_{2}$ with CO .

The chemical equation for an elementary reaction is a description of an individual molecular event that involves breaking and/or making chemical bonds. By contrast, the balanced equation for an overall reaction describes only the stoichiometry of the overall process, but provides no information about how the reaction occurs. The equation for the reaction of $\mathrm{NO}_{2}$ with CO , for example, does not tell us that the reaction occurs by direct transfer of an oxygen atom from an $\mathrm{NO}_{2}$ molecule to a CO molecule.

Elementary reaction-describes an individual molecular event.
Overall reaction-describes reaction stoichiometry.

The elementary steps in a proposed reaction mechanism must sum to give the overall reaction. When we sum the elementary steps in the reaction of $\mathrm{NO}_{2}$ with CO and then cancel the molecules that appear on both sides of the resulting equation, we obtain the overall reaction:

Step 1.

$$
\begin{array}{lr}
\text { Step 1. } & \mathrm{NO}_{2}(g)+\mathrm{NO}_{2}(g) \longrightarrow \mathrm{NO}(g)+\mathrm{NO}_{3}(g) \\
\text { Step 2. } & \mathrm{NO}_{3}(g)+\mathrm{CO}(g) \longrightarrow \mathrm{NO}_{2}(g)+\mathrm{CO}_{2}(g)
\end{array}
$$

Elementary reaction
Elementary reaction
$\mathrm{NO}_{2}(g)+\mathrm{NO}_{2}(g)+\mathrm{NO}_{3}(g)+\mathrm{CO}(g) \longrightarrow \mathrm{NO}(g)+\mathrm{NO}_{3}(g)+\mathrm{NO}_{2}(g)+\mathrm{CO}_{2}(g)$
$\mathrm{NO}_{2}(g)+\mathrm{CO}(g) \longrightarrow \mathrm{NO}(g)+\mathrm{CO}_{2}(g)$
Overall reaction

A species that is formed in one step of a reaction mechanism and consumed in a subsequent step, such as $\mathrm{NO}_{3}$ in our example, is called a reaction intermediate. Reaction intermediates do not appear in the net equation for the overall reaction, and it's only by looking at the elementary steps that their presence is noticed.

Elementary reactions are classified on the basis of their molecularity, the number of molecules (or atoms) on the reactant side of the chemical equation for the elementary reaction. A unimolecular reaction is an elementary reaction that involves a single reactant molecule-for example, the unimolecular decomposition of ozone in the upper atmosphere:

$$
\mathrm{O}_{3}{ }^{*}(\mathrm{~g}) \longrightarrow \mathrm{O}_{2}(\mathrm{~g})+\mathrm{O}(\mathrm{~g})
$$



The asterisk on $\mathrm{O}_{3}$ indicates that the ozone molecule is in an energetically excited state because it has previously absorbed ultraviolet light from the sun. The absorbed energy causes one of the two $\mathrm{O}-\mathrm{O}$ bonds to break, with the loss of an oxygen atom.

A bimolecular reaction is an elementary reaction that results from an energetic collision between two reactant molecules. An example taken from the chemistry of the upper atmosphere is the reaction of an ozone molecule with an oxygen atom to yield two $\mathrm{O}_{2}$ molecules:


Both unimolecular and bimolecular reactions are common, but termolecular reactions, which involve three atoms or molecules, are rare. As any pool player knows, three-body collisions are much less probable than two-body collisions. There are some reactions, however, that require a three-body collision, notably the combination of two atoms to form a diatomic molecule. For example, oxygen atoms in the upper atmosphere combine as a result of collisions involving some third molecule M:



A The beautiful northern lights, or aurora borealis, are often observed in the Northern Hemisphere at high latitudes. The light is partly produced by excited O atoms in the upper atmosphere.


In the atmosphere, M is most likely $\mathrm{N}_{2}$, but in principle it could be any atom or molecule. The role of $M$ is to carry away the energy that is released when the $\mathrm{O}-\mathrm{O}$ bond is formed. If $M$ were not involved in the collision, the two oxygen atoms would simply bounce off each other, and no reaction would occur.

## Worked Example 12.9

The following two-step mechanism has been proposed for the gas-phase decomposition of nitrous oxide $\left(\mathrm{N}_{2} \mathrm{O}\right)$ :

(a) Write the chemical equation for the overall reaction.
(b) Identify any reaction intermediates.
(c) What is the molecularity of each of the elementary reactions?
(d) What is the molecularity of the overall reaction?

## Strategy

To find the overall reaction, sum the elementary steps. To identify intermediates and molecularity, look at the individual steps.

## Solution

(a) The overall reaction is the sum of the two elementary steps:

| Step 1. | $\mathrm{N}_{2} \mathrm{O}(g) \longrightarrow \mathrm{N}_{2}(g)+\mathrm{O}(g)$ | Elementary reaction |
| ---: | :---: | ---: |
| Step 2. $\mathrm{N}_{2} \mathrm{O}(g)+\mathrm{O}(g) \longrightarrow \mathrm{N}_{2}(g)+\mathrm{O}_{2}(g)$ | Elementary reaction |  |
| $2 \mathrm{~N}_{2} \mathrm{O}(g)+\mathrm{O}(g) \longrightarrow 2 \mathrm{~N}_{2}(g)+\mathrm{O}(g)+\mathrm{O}_{2}(g)$ |  |  |
| $2 \mathrm{~N}_{2} \mathrm{O}(g) \longrightarrow 2 \mathrm{~N}_{2}(g)+\mathrm{O}_{2}(g)$ | Overall reaction |  |

(b) The oxygen atom is a reaction intermediate because it is formed in the first elementary step and consumed in the second step.
(c) The first elementary reaction is unimolecular because it involves a single reactant molecule. The second elementary step is bimolecular because it involves two reactant molecules.
(d) It's inappropriate to use the word molecularity in connection with the overall reaction because the overall reaction does not describe an individual molecular event. Only an elementary reaction can have a molecularity.

- KEY CONCEPT PROBLEM 12.12 A suggested mechanism for the reaction of nitrogen dioxide and molecular fluorine is

$$
\text { Step 1. } \quad \mathrm{NO}_{2}(g)+\mathrm{F}_{2}(g) \longrightarrow \mathrm{NO}_{2} \mathrm{~F}(g)+\mathrm{F}(g)
$$



(a) Give the chemical equation for the overall reaction, and identify any reaction intermediates.
(b) What is the molecularity of each of the elementary reactions?

## 12.9 | Rate Laws and Reaction Mechanisms

Recall from Section 12.2 that the rate law for an overall chemical reaction must be determined experimentally. It can't be deduced from the stoichiometric coefficients in the balanced equation for the overall reaction. By contrast, the rate law for an elementary reaction follows directly from its molecularity because an elementary reaction is an individual molecular event. The concentration of each reactant in an elementary reaction appears in the rate law, with an exponent equal to its coefficient in the chemical equation for the elementary reaction.

Consider, for example, the unimolecular decomposition of ozone:

$$
\mathrm{O}_{3}(g) \longrightarrow \mathrm{O}_{2}(g)+\mathrm{O}(g)
$$

The number of moles of $\mathrm{O}_{3}$ per liter that decompose per unit time is directly proportional to the molar concentration of $\mathrm{O}_{3}$ :

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{O}_{3}\right]}{\Delta t}=k\left[\mathrm{O}_{3}\right]
$$

The rate of a unimolecular reaction is always first order in the concentration of the reactant molecule.

For a bimolecular elementary reaction of the type $A+B \rightarrow$ products, the reaction rate depends on the frequency of collisions between $A$ and $B$ molecules. The frequency of AB collisions involving any particular A molecule is proportional to the molar concentration of $B$, while the total frequency of $A B$ collisions involving all A molecules is proportional to the molar concentration of A times the molar concentration of B (Figure 12.11). Therefore, the reaction obeys the second-order rate law

$$
\text { Rate }=-\frac{\Delta[\mathrm{A}]}{\Delta t}=-\frac{\Delta[\mathrm{B}]}{\Delta t}=k[\mathrm{~A}][\mathrm{B}]
$$

By a similar line of reasoning, a bimolecular reaction of the type

$$
\mathrm{A}+\mathrm{A} \longrightarrow \text { Products }
$$

has the second-order rate law:

$$
\text { Rate }=-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}][\mathrm{A}]=k[\mathrm{~A}]^{2}
$$

Rate laws for elementary reactions are summarized in Table 12.5. Note that the overall reaction order for an elementary reaction always equals its molecularity.

The experimentally observed rate law for an overall reaction depends on the reaction mechanism-that is, on the sequence of elementary steps and their relative rates. If the overall reaction occurs in a single elementary step, the experimental
7. David W. Ball, "Another Auto Analogy: Rate-Determining Steps," J. Chem. Educ., Vol. 64, 1987, 486-487.


Bassam Z. Shakhashiri,
"Hydrolysis of 2-chloro-2methylpropane," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 4 (The University of Wisconsin Press, Madison, 1992), pp. 56-64. The time required for the color change in this reaction is shown to increase with increasing sodium hydroxide concentration, decrease with increasing 2 -chloro-2-methylpropane concentration, and increase as the ratio of water/acetone increases. These observations are related to the mechanism of 2-chloro-2-methylpropane hydrolysis.


- FIGURE 12.11 The effect of concentration on the frequency of collisions between A molecules (blue) and B molecules (red). (a) The frequency of AB collisions involving any one A molecule is proportional to the concentration of B molecules. (b) Doubling the concentration of A molecules (from 1 to 2 per unit volume) doubles the total frequency of AB collisions. (c) Doubling the concentration of B molecules doubles the frequency of AB collisions involving any one A molecule. (d) Doubling the concentration of A molecules and doubling the concentration of $B$ molecules quadruples the total frequency of $A B$ collisions. Thus, the total frequency of $A B$ collisions is proportional to the concentration of $A$ molecules times the concentration of $B$ molecules.

TABLE 12.5 Rate Laws for Elementary Reactions

| Elementary Reaction | Molecularity | Rate Law |
| :--- | :--- | :--- |
| $\mathrm{A} \longrightarrow$ Products | Unimolecular | Rate $=k[\mathrm{~A}]$ |
| $\mathrm{A}+\mathrm{A} \longrightarrow$ Products | Bimolecular | Rate $=k[\mathrm{~A}]^{2}$ |
| $\mathrm{~A}+\mathrm{B} \longrightarrow$ Products | Bimolecular | Rate $=k[\mathrm{~A}][\mathrm{B}]$ |
| $\mathrm{A}+\mathrm{A}+\mathrm{B} \longrightarrow$ Products | Termolecular | Rate $=k[\mathrm{~A}]^{2}[\mathrm{~B}]$ |
| $\mathrm{A}+\mathrm{B}+\mathrm{C} \longrightarrow$ Products | Termolecular | Rate $=k[\mathrm{~A}][\mathrm{B}][\mathrm{C}]$ |

rate law is the same as the rate law for the elementary reaction. An example is the conversion of bromomethane to methanol in basic solution:

$$
\mathrm{CH}_{3} \mathrm{Br}(a q)+\mathrm{OH}^{-}(a q) \longrightarrow \mathrm{Br}^{-}(a q)+\mathrm{CH}_{3} \mathrm{OH}(a q)
$$



This reaction occurs in a single bimolecular step in which a new $\mathrm{C}-\mathrm{O}$ bond forms at the same time as the $\mathrm{C}-\mathrm{Br}$ bond breaks. The experimental rate law is

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{CH}_{3} \mathrm{Br}\right]}{\Delta t}=k\left[\mathrm{CH}_{3} \mathrm{Br}\right]\left[\mathrm{OH}^{-}\right]
$$

When an overall reaction occurs in two or more elementary steps, one of the steps is often much slower than the others. The slowest step in a reaction mechanism is called the rate-determining step because that step acts as a bottleneck, limiting the rate at which reactants can be converted to products. A chemical reaction is somewhat like the cafeteria line in a dining hall in this respect. The rate at which the line moves is determined not by the faster steps, perhaps picking up a salad or a beverage, but by the slowest step, perhaps waiting for a well-done hamburger. The overall reaction can occur no faster than the speed of the ratedetermining step.

In the reaction of nitrogen dioxide with carbon monoxide, for example, the first step in the mechanism is slower and rate-determining, whereas the second step occurs more rapidly:

$$
\begin{array}{cl}
\mathrm{NO}_{2}(g)+\mathrm{NO}_{2}(g) \xrightarrow{k_{1}} \mathrm{NO}(g)+\mathrm{NO}_{3}(g) & \text { Slower, rate-determining } \\
\mathrm{NO}_{3}(g)+\mathrm{CO}(g) \xrightarrow{k_{2}} \mathrm{NO}_{2}(g)+\mathrm{CO}_{2}(g) & \text { Faster } \\
\hline \mathrm{NO}_{2}(g)+\mathrm{CO}(g) \longrightarrow \mathrm{NO}(g)+\mathrm{CO}_{2}(g) & \text { Overall reaction }
\end{array}
$$

The constants $k_{1}$ and $k_{2}$, written above the arrows in the preceding equations, are the rate constants for the elementary reactions. The rate of the overall reaction is determined by the rate of the first, slower step. In the second step, the unstable intermediate $\left(\mathrm{NO}_{3}\right)$ reacts as soon as it is formed in the first step.

Because the rate law for an overall reaction depends on the reaction mechanism, it provides important clues to the mechanism. A plausible mechanism must meet two criteria: (1) The elementary steps must sum up to give the overall reaction, and (2) the mechanism must be consistent with the observed rate law for the overall reaction.

The procedure that chemists use in establishing a reaction mechanism goes something like this: First, the rate law is determined by experiment. Then, a series of elementary steps is devised, and the rate law predicted by the proposed mechanism is worked out. If the observed and predicted rate laws don't agree, the mechanism must be discarded and another one must be devised. If the observed and predicted rate laws do agree, the proposed mechanism is a plausible (though not necessarily correct) pathway for the reaction. Figure 12.12 summarizes the procedure.


A FIGURE 12.12 Flowchart illustrating the logic used in studies of reaction mechanisms.


A Which is more likely to slow down this line: picking up a beverage or waiting for a hamburger?

In the reaction of $\mathrm{NO}_{2}$ with CO , for example, the experimental rate law is

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{NO}_{2}\right]}{\Delta t}=k\left[\mathrm{NO}_{2}\right]^{2}
$$

The rate law predicted by the proposed mechanism is that for the rate-determining step, where $k_{1}$ is the rate constant for that step. Note that the predicted rate law follows directly from the molecularity of the rate-determining step:

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{NO}_{2}\right]}{\Delta t}=k_{1}\left[\mathrm{NO}_{2}\right]^{2}
$$

Because the observed and predicted rate laws have the same form (second-order dependence on $\left[\mathrm{NO}_{2}\right]$ ), the proposed mechanism is consistent with the experimental rate law. The observed rate constant $k$ is the same as $k_{1}$, the rate constant for the first elementary step.

The case for a particular mechanism is strengthened considerably if a reaction intermediate can be isolated or if an unstable intermediate (such as $\mathrm{NO}_{3}$ ) can be detected spectroscopically. It's easy to disprove a mechanism, but it's never possible to finally "prove" a mechanism because there may be an alternative reaction pathway-not yet imagined-that also fits the experimental facts. The best that we can do to establish a mechanism is to accumulate a convincing body of experimental evidence that supports it. Proving a reaction mechanism is more like proving a case in a law court than proving a theorem in mathematics.

## Worked Example 12.10

The following reaction has a second-order rate law:

$$
\mathrm{H}_{2}(g)+2 \mathrm{ICl}(g) \longrightarrow \mathrm{I}_{2}(g)+2 \mathrm{HCl}(g) \quad \text { Rate }=k\left[\mathrm{H}_{2}\right][\mathrm{ICl}]
$$

Devise a possible reaction mechanism.

## Strategy

The reaction doesn't occur in a single elementary step because, if it did, the rate law would be third order: Rate $=k\left[\mathrm{H}_{2}\right][\mathrm{ICl}]^{2}$. The observed rate law will be obtained if the rate-determining step involves the bimolecular reaction of $\mathrm{H}_{2}$ and ICl.

## Solution

A plausible sequence of elementary steps is

$$
\begin{array}{cl}
\mathrm{H}_{2}(g)+\mathrm{ICl}(g) \xrightarrow{k_{1}} \mathrm{HI}(g)+\mathrm{HCl}(g) & \text { Slower, rate-determining } \\
\mathrm{HI}(g)+\mathrm{ICl}(g) \xrightarrow{k_{2}} \mathrm{I}_{2}(g)+\mathrm{HCl}(g) & \text { Faster } \\
\hline \mathrm{H}_{2}(g)+2 \mathrm{ICl}(g) \longrightarrow \mathrm{I}_{2}(g)+2 \mathrm{HCl}(g) & \text { Overall reaction }
\end{array}
$$

The rate law predicted by this mechanism, Rate $=k_{1}\left[\mathrm{H}_{2}\right][\mathrm{ICl}]$, agrees with the observed rate law.

- PROBLEM 12.13 Write the rate law for each of the following elementary reactions:
(a) $\mathrm{O}_{3}(g)+\mathrm{O}(g) \rightarrow 2 \mathrm{O}_{2}(g)$
(b) $\mathrm{Br}(g)+\mathrm{Br}(g)+\operatorname{Ar}(g) \rightarrow \mathrm{Br}_{2}(g)+\operatorname{Ar}(g)$
(c) $\mathrm{Co}(\mathrm{CN})_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)^{2-}(a q) \rightarrow \mathrm{Co}(\mathrm{CN})_{5}{ }^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)$
- PROBLEM 12.14 The following reaction has a first-order rate law:

$$
\begin{aligned}
& \mathrm{Co}(\mathrm{CN})_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)^{2-}(a q)+\mathrm{I}^{-}(a q) \longrightarrow \mathrm{Co}(\mathrm{CN})_{5} \mathrm{I}^{3-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\
& \text { Rate }=k\left[\mathrm{Co}(\mathrm{CN})_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)^{2-}\right]
\end{aligned}
$$

Suggest a possible reaction mechanism, and show that your mechanism agrees with the observed rate law.

### 12.10 Reaction Rates and Temperature: The Arrhenius Equation

Everyday experience tells us that the rates of chemical reactions increase with increasing temperature. Familiar fuels such as gas, oil, and coal are relatively inert at room temperature, but burn rapidly at elevated temperatures. Many foods last almost indefinitely when stored in a freezer, but spoil quickly at room temperature. Metallic magnesium is inert in cold water, but reacts with hot water (Figure 12.13). As a rule of thumb, reaction rates tend to double when the temperature is increased by $10^{\circ} \mathrm{C}$.

To understand why reaction rates depend on temperature, we need a picture of how reactions take place. According to the collision theory model, a bimolecular reaction occurs when two properly oriented reactant molecules come together in a sufficiently energetic collision. To be specific, let's consider one of the simplest possible reactions, the reaction of an atom $A$ with a diatomic molecule $B C$ to give a diatomic molecule $A B$ and an atom $C$ :

$$
\mathrm{A}+\mathrm{BC} \longrightarrow \mathrm{AB}+\mathrm{C}
$$

An example from atmospheric chemistry is the reaction of an oxygen atom with an HCl molecule to give an OH molecule and a chlorine atom:

$$
\mathrm{O}(g)+\mathrm{HCl}(g) \longrightarrow \mathrm{OH}(g)+\mathrm{Cl}(g)
$$

If the reaction occurs in a single step, the electron distribution about the three nuclei must change in the course of the collision such that a new bond, A-B, develops at the same time the old bond, $\mathrm{B}-\mathrm{C}$, breaks. Between the reactant and product stages, the nuclei pass through a configuration in which all three atoms are weakly linked together. We can picture the progress of the reaction as


If $A$ and $B C$ have filled shells of electrons (no unpaired electrons or vacant, lowenergy orbitals), they will repel each other. To achieve the configuration A---B---C, then, the atoms require energy to overcome this repulsion. The energy comes from the kinetic energy of the colliding particles and is converted to potential energy in A---B---C. In fact, A---B---C has more potential energy than either the reactants or the products. Thus, there is a potential energy barrier that must be surmounted before reactants can be converted to products, as depicted graphically on the potential energy profile in Figure 12.14.

The height of the barrier is called the activation energy, $E_{a}$, and the configuration of atoms at the maximum in the potential energy profile is called the transition state, or the activated complex. Since energy is conserved in the collision, all the energy needed to climb the potential energy hill must come from the kinetic energy of the colliding molecules. If the collision energy is less than $E_{a}$, the reactant molecules can't surmount the barrier and they simply bounce apart. If the


A FIGURE 12.13 Magnesium is inert in cold water (left) but reacts with hot water (right). Evidence of reaction is the pink color of phenolphthalein, which indicates formation of an alkaline solution, and the bubbles of gas. The reaction is $\mathrm{Mg}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \rightarrow$ $\mathrm{Mg}^{2+}(a q)+2 \mathrm{OH}^{-}(a q)+\mathrm{H}_{2}(g)$ nius Law and Storage of Food," J. Chem. Educ., Vol. 76, 1999, 504-505.

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IlLee A. Krug, "The Collision Theory and an American Tradition," J. Chem. Educ., Vol. 64, 1987, 1000.

B Bassam Z. Shakhashiri, "Lightsticks," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983), pp. 146-152. Cyalume ${ }^{\circledR}$ lightsticks are used to demonstrate the effect of temperature on reaction rates.

Bassam Z. Shakhashiri, Lloyd G. Williams, Glen E. Dirreen, and Ann Francis, "Cool-Light Chemiluminescence," J. Chem. Educ., Vol. 58, 1981, 70-72. Cyalume ${ }^{\circledR}$ lightstick chemiluminescence reactions.


A FIGURE 12.14 Potential energy profile for the reaction $A+B C \rightarrow A B+C$, showing the energy barrier between the reactants and products. As the reaction progresses, kinetic energy of the reactants is first converted into potential energy of the transition state and is then transformed into kinetic energy of the products. At each point along the profile, the total energy is conserved. The profile is drawn for an exothermic reaction, so $\Delta E$, the energy of reaction, is negative.
collision energy is at least as great as $E_{\mathrm{a}}$, however, the reactants can climb over the barrier and be converted to products.

Experimental evidence for the notion of an activation energy barrier comes from a comparison of collision rates and reaction rates. Collision rates in gases can be calculated from kinetic-molecular theory (Section 9.6). For a gas at room temperature ( 298 K ) and 1 atm pressure, each molecule undergoes approximately $10^{9}$ collisions per second, or 1 collision every $10^{-9}$ s. Thus, if every collision resulted in reaction, every gas-phase reaction would be complete in about $10^{-9} \mathrm{~s}$. By contrast, observed reactions often have half-lives of minutes or hours, so it's clear that only a tiny fraction of the collisions lead to reaction.

Very few collisions are productive because very few occur with a collision energy as large as the activation energy. The fraction of collisions with an energy equal to or greater than the activation energy $E_{\mathrm{a}}$ is represented in Figure 12.15 at two different temperatures by the areas under the curves to the right of $E_{\mathrm{a}}$. When $E_{\mathrm{a}}$ is large compared with $R T$, this fraction $f$ is approximated by the equation

$$
f=e^{-E_{a} / R T}
$$

where $R$ is the gas constant $[8.314 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})]$ and $T$ is the absolute temperature in kelvins. Note that $f$ is a very small number. For example, for a reaction having an activation energy of $75 \mathrm{~kJ} / \mathrm{mol}$, the value of $f$ at 298 K is $7 \times 10^{-14}$ :

$$
f=\exp \left[\frac{-75,000 \frac{\mathrm{~J}}{\mathrm{~mol}}}{\left(8.314 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)(298 \mathrm{~K})}\right]=e^{-30.3}=7 \times 10^{-14}
$$

Thus, only 7 collisions in 100 trillion are sufficiently energetic to convert reactants to products.


A FIGURE 12.15 Plots of the fraction of collisions with a particular energy at two different temperatures. For each plot, the total area under the curve is unity, and the area to the right of $E_{\mathrm{a}}$ is the fraction $f$ of the collisions with an energy greater than or equal to $E_{\mathrm{a}}$. The fraction of collisions that are sufficiently energetic to result in reaction increases exponentially with increasing temperature.

As the temperature increases, the distribution of collision energies broadens and shifts to higher energies (Figure 12.15), resulting in a rapid increase in the fraction of collisions that lead to products. At 308 K , for example, the calculated value of $f$ for the reaction with $E_{\mathrm{a}}=75 \mathrm{~kJ} / \mathrm{mol}$ is $2 \times 10^{-13}$. Thus, a temperature increase of just $3 \%$, from 298 K to 308 K , increases the value of $f$ by a factor of 3 . Collision theory therefore accounts nicely for the exponential dependence of reaction rates on reciprocal temperature. As $T$ increases ( $1 / T$ decreases), $f=e^{-E_{\mathrm{a}} / R T}$ increases exponentially. Collision theory also explains why reaction rates are so much lower than collision rates. (Collision rates also increase with increasing temperature, but only by a small amount-less than $2 \%$ on going from 298 K to 308 K .)

The fraction of collisions that lead to products is further reduced by an orientation requirement. Even if the reactants collide with sufficient energy, they won't react unless the orientation of the reaction partners is correct for formation of the transition state. For example, a collision of $A$ with the $C$ end of the molecule BC can't result in formation of AB :


The reactant molecules would simply collide and then separate without reaction:


The fraction of collisions having proper orientation for conversion of reactants to products is called the steric factor, $p$. For the reaction, $A+B C \rightarrow A B+C$, the value of $p$ is expected to be about 0.5 because $A$ has a nearly $1: 1$ probability of
colliding with each of the $B$ and $C$ ends of $B C$. (This assumes that $B$ and $C$ have similar sizes and electronic properties.) For reactions of complex molecules, $p$ is a fraction considerably less than 0.5.

Now let's see how the two parameters $p$ and $f$ enter into the rate law. Since bimolecular collisions between any two molecules-say, A and B-occur at a rate that is proportional to their concentrations, we can write

$$
\text { Collision rate }=\mathrm{Z}[\mathrm{~A}][\mathrm{B}]
$$

where Z is a constant related to the collision frequency and has units of a secondorder rate constant, $1 /(\mathrm{M} \cdot \mathrm{s})$ or $\mathrm{M}^{-1} \mathrm{~s}^{-1}$. The reaction rate is lower than the collision rate by a factor $p \times f$ because only a fraction of the colliding molecules have the correct orientation and the minimum energy needed for reaction:

$$
\text { Reaction rate }=p \times f \times \text { Collision rate }=p f Z[\mathrm{~A}][\mathrm{B}]
$$

Since the rate law is

$$
\text { Reaction rate }=k[\mathrm{~A}][\mathrm{B}]
$$

the rate constant predicted by collision theory is $k=p f Z$, or $k=p Z e^{-E_{\mathrm{a}} / R T}$.

Arrhenius Equation activity


This expression is usually written in a form called the Arrhenius equation, named after Svante Arrhenius, the Swedish chemist who proposed it in 1889 on the basis of experimental studies of reaction rates:

$$
\text { ARrhenius equation: } k=A e^{-E_{\mathrm{a}} / R T}
$$

The parameter $A(=p Z)$ is called the frequency factor (or pre-exponential factor). In accord with the minus sign in the exponent, the rate constant decreases as $E_{\mathrm{a}}$ increases and increases as $T$ increases.

- KEY CONCEPT PROBLEM 12.15 The potential energy profile for the one-step reaction $A B+C D \rightarrow A C+B D$ is shown below. The energies are in $\mathrm{kJ} / \mathrm{mol}$ relative to an arbitrary zero of energy.

(a) What is the value of the activation energy for this reaction?
(b) Is the reaction exothermic or endothermic?
(c) Suggest a plausible structure for the transition state.


### 12.11 Using the Arrhenius Equation

As we saw in Section 12.10, the activation energy $E_{a}$ is one of the most important factors affecting the rate of a chemical reaction. Its value can be determined using the Arrhenius equation if values of the rate constant are known at different temperatures. Taking the natural logarithm of both sides of the Arrhenius equation, we obtain the logarithmic form

$$
\ln k=\ln A-\frac{E_{\mathrm{a}}}{R T}
$$

This equation can be rearranged into the form $y=m x+b$, so a graph of $\ln k$ versus $1 / T$ (called an Arrhenius plot) gives a straight line with slope $m=-E_{\mathrm{a}} / R$ and intercept $b=\ln A$ :


The experimental value of the activation energy can be determined from the slope of the straight line, as shown in Worked Example 12.11.

$$
E_{\mathrm{a}}=-R(\text { Slope })
$$

Still another form of the Arrhenius equation can be derived that allows us to estimate the activation energy from rate constants at just two temperatures. At temperature $T_{1}$,

$$
\ln k_{1}=\left(\frac{-E_{\mathrm{a}}}{R}\right)\left(\frac{1}{T_{1}}\right)+\ln A
$$

and at temperature $T_{2}$,

$$
\ln k_{2}=\left(\frac{-E_{\mathrm{a}}}{R}\right)\left(\frac{1}{T_{2}}\right)+\ln A
$$

Subtracting the first equation from the second, and remembering that $\left(\ln k_{2}-\ln k_{1}\right)=\ln \left(k_{2} / k_{1}\right)$, we obtain

$$
\ln \left(\frac{k_{2}}{k_{1}}\right)=\left(\frac{-E_{\mathrm{a}}}{R}\right)\left(\frac{1}{T_{2}}-\frac{1}{T_{1}}\right)
$$

This equation can be used to calculate $E_{\mathrm{a}}$ from rate constants $k_{1}$ and $k_{2}$ at temperatures $T_{1}$ and $T_{2}$. By the same token, if we know $E_{\mathrm{a}}$ and the rate constant $k_{1}$ at one temperature $T_{1}$, we can calculate the rate constant $k_{2}$ at another temperature $T_{2}$. Worked Example 12.11 shows how this is done.

## Worked Example 12.11

Rate constants for the gas-phase decomposition of hydrogen iodide, $2 \mathrm{HI}(g) \rightarrow$ $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g)$, are listed in the following table:

| Temperature <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{k}$ <br> $\left(\mathbf{M}^{\mathbf{- 1}} \mathbf{s}^{\mathbf{- 1}}\right)$ | Temperature <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{k}$ <br> $\left(\mathbf{M}^{\mathbf{- 1}} \mathbf{s}^{-\mathbf{1}} \mathbf{)}\right.$ |
| :--- | :--- | :--- | :--- |
| 283 | $3.52 \times 10^{-7}$ | 427 | $1.16 \times 10^{-3}$ |
| 356 | $3.02 \times 10^{-5}$ | 508 | $3.95 \times 10^{-2}$ |
| 393 | $2.19 \times 10^{-4}$ |  |  |

(a) Find the activation energy (in $\mathrm{kJ} / \mathrm{mol}$ ) using all five data points.
(b) Calculate $E_{\mathrm{a}}$ from the rate constants at $283^{\circ} \mathrm{C}$ and $508^{\circ} \mathrm{C}$.
(c) Given the rate constant at $283^{\circ} \mathrm{C}$ and the value of $E_{\mathrm{a}}$ obtained in part (b), what is the rate constant at $293^{\circ} \mathrm{C}$ ?

## Strategy

(a) The activation energy $E_{\mathrm{a}}$ can be determined from the slope of a linear plot of $\ln k$ versus $1 / T$.
(b) To calculate $E_{\mathrm{a}}$ from values of the rate constant at two temperatures, use the equation

$$
\ln \left(\frac{k_{2}}{k_{1}}\right)=\left(\frac{-E_{\mathrm{a}}}{R}\right)\left(\frac{1}{T_{2}}-\frac{1}{T_{1}}\right)
$$

(c) Use the same equation and the known values of $E_{\mathrm{a}}$ and $k_{1}$ at $T_{1}$ to calculate $k_{2}$ at $T_{2}$.

## Solution

(a) Since the temperature in the Arrhenius equation is expressed in kelvins, we must first convert the Celsius temperatures to absolute temperatures, then calculate values of $1 / T$ and $\ln k$, and plot $\ln k$ versus $1 / T$. The results are shown in the following table and graph:

| $\boldsymbol{t}$ <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{T}$ <br> $\mathbf{( K )}$ | $\boldsymbol{k}$ <br> $\left(\mathbf{M}^{\mathbf{1}} \mathbf{s}^{-\mathbf{1}}\right)$ | $\mathbf{1 / T}$ <br> $\mathbf{( 1 / K )}$ | $\mathbf{l n} \boldsymbol{k}$ |
| :--- | :--- | :--- | :--- | ---: |
| 283 | 556 | $3.52 \times 10^{-7}$ | 0.00180 | -14.860 |
| 356 | 629 | $3.02 \times 10^{-5}$ | 0.00159 | -10.408 |
| 393 | 666 | $2.19 \times 10^{-4}$ | 0.00150 | -8.426 |
| 427 | 700 | $1.16 \times 10^{-3}$ | 0.00143 | -6.759 |
| 508 | 781 | $3.95 \times 10^{-2}$ | 0.00128 | -3.231 |



The slope of the straight-line plot can be determined from the coordinates of two widely separated points:
Slope $=\frac{\Delta y}{\Delta x}=\frac{(-14.0)-(-3.9)}{\left(0.00175 \mathrm{~K}^{-1}\right)-\left(0.00130 \mathrm{~K}^{-1}\right)}=\frac{-10.1}{0.00045 \mathrm{~K}^{-1}}=-2.24 \times 10^{4} \mathrm{~K}$
Finally, calculate the activation energy from the slope:

$$
\begin{aligned}
E_{\mathrm{a}} & =-R(\text { Slope })=-\left(8.314 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)\left(-2.24 \times 10^{4} \mathrm{~K}\right) \\
& =1.9 \times 10^{5} \mathrm{~J} / \mathrm{mol}=190 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

Note that the slope of the Arrhenius plot is negative and the activation energy is positive. The greater the activation energy for a particular reaction, the steeper the slope of the $\ln k$ versus $1 / T$ plot and the greater the increase in the rate constant for a given increase in temperature.
(b) Substituting the values of $k_{1}=3.52 \times 10^{-7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ at $T_{1}=556 \mathrm{~K}\left(283^{\circ} \mathrm{C}\right)$ and $k_{2}=3.95 \times 10^{-2} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ at $T_{2}=781 \mathrm{~K}\left(508^{\circ} \mathrm{C}\right)$ into the equation

$$
\ln \left(\frac{k_{2}}{k_{1}}\right)=\left(\frac{-E_{\mathrm{a}}}{R}\right)\left(\frac{1}{T_{2}}-\frac{1}{T_{1}}\right)
$$

gives

$$
\ln \left(\frac{3.95 \times 10^{-2} \mathrm{M}^{-1} \mathrm{~s}^{-1}}{3.52 \times 10^{-7} \mathrm{M}^{-1} \mathrm{~s}^{-1}}\right)=\left(\frac{-E_{\mathrm{a}}}{8.314 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}}\right)\left(\frac{1}{781 \mathrm{~K}}-\frac{1}{556 \mathrm{~K}}\right)
$$

and simplifying this equation gives

$$
\begin{aligned}
11.628 & =\left(\frac{-E_{\mathrm{a}}}{8.314 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}}\right)\left(\frac{-5.18 \times 10^{-4}}{\mathrm{~K}}\right) \\
E_{\mathrm{a}} & =1.87 \times 10^{5} \mathrm{~J} / \mathrm{mol}=187 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

(c) Use the same equation as in part (b), but now the known values are $k_{1}=3.52 \times 10^{-7} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ at $T_{1}=556 \mathrm{~K}\left(283^{\circ} \mathrm{C}\right)$ and $E_{\mathrm{a}}=1.87 \times 10^{5} \mathrm{~J} / \mathrm{mol}$, and $k_{2}$ at $T_{2}=566 \mathrm{~K}\left(293^{\circ} \mathrm{C}\right)$ is the unknown:

$$
\ln \left(\frac{k_{2}}{3.52 \times 10^{-7} \mathrm{M}^{-1} \mathrm{~s}^{-1}}\right)=\left(\frac{-1.87 \times 10^{5} \frac{\mathrm{~J}}{\mathrm{~mol}}}{8.314 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}}\right)\left(\frac{1}{566 \mathrm{~K}}-\frac{1}{556 \mathrm{~K}}\right)=0.715
$$

Taking the antiln of both sides gives

$$
\begin{aligned}
\frac{k_{2}}{3.52 \times 10^{-7} \mathrm{M}^{-1} \mathrm{~s}^{-1}} & =e^{0.715}=2.04 \\
k_{2} & =7.18 \times 10^{-7} \mathrm{M}^{-1} \mathrm{~s}^{-1}
\end{aligned}
$$

In this temperature range, a rise in temperature of 10 K doubles the rate constant.

- PROBLEM 12.16 Rate constants for the decomposition of gaseous dinitrogen pentoxide are $3.7 \times 10^{-5} \mathrm{~s}^{-1}$ at $25^{\circ} \mathrm{C}$ and $1.7 \times 10^{-3} \mathrm{~s}^{-1}$ at $55^{\circ} \mathrm{C}$.

$$
2 \mathrm{~N}_{2} \mathrm{O}_{5}(g) \longrightarrow 4 \mathrm{NO}_{2}(g)+\mathrm{O}_{2}(g)
$$

(a) What is the activation energy for this reaction in $\mathrm{kJ} / \mathrm{mol}$ ?
(b) What is the rate constant at $35^{\circ} \mathrm{C}$ ?

### 12.12 Catalysis

Reaction rates are affected not only by reactant concentrations and temperature but also by the presence of catalysts. A catalyst is a substance that increases the rate of a reaction without being consumed in the reaction. An example is manganese dioxide, a black powder that speeds up the thermal decomposition of potassium chlorate:

$$
2 \mathrm{KClO}_{3}(s) \xrightarrow[\text { Heat }]{\mathrm{MnO}_{2} \text { catalyst }} 2 \mathrm{KCl}(s)+3 \mathrm{O}_{2}(g)
$$

In the absence of a catalyst, $\mathrm{KClO}_{3}$ decomposes very slowly, even when heated, but when a small amount of $\mathrm{MnO}_{2}$ is mixed with the $\mathrm{KClO}_{3}$ before heating, rapid evolution of oxygen ensues. The $\mathrm{MnO}_{2}$ can be recovered unchanged after the reaction is complete.


A $\mathrm{MnO}_{2}$ catalyzes the thermal decomposition of $\mathrm{KClO}_{3}$ to KCl and $\mathrm{O}_{2}$ gas.

(a)

(b)
© FIGURE 12.16 The rate of decomposition of aqueous hydrogen peroxide can be monitored qualitatively by collecting the evolved oxygen gas in a balloon. (a) In the absence of a catalyst, little $\mathrm{O}_{2}$ is produced. (b) After addition of aqueous sodium iodide, the balloon rapidly inflates with $\mathrm{O}_{2}$.

Doris Kolb, "Catalysis," J. Chem. Educ., Vol. 56, 1979, 743-747.

Albert Haim, "Catalysis: New Reaction Pathways, Not Just a Lowering of the Activation Energy," J. Chem. Educ., Vol. 66, 1989, 935-937.

Catalysts are of enormous importance, both in the chemical industry and in living organisms. Nearly all industrial processes for the manufacture of essential chemicals use catalysts to favor formation of specific products and to lower reaction temperatures, thus reducing energy costs. In environmental chemistry, catalysts such as nitric oxide play a role in the formation of air pollutants, while other catalysts, such as platinum in automobile catalytic converters, are potent weapons in the battle to control air pollution.

In living organisms, chemical reactions are catalyzed by large molecules called enzymes, which facilitate specific reactions of crucial biological importance (see Section 24.6). For example, nitrogenase, an enzyme present in bacteria on the root nodules of leguminous plants such as peas and beans, catalyzes the conversion of atmospheric nitrogen to ammonia. The ammonia serves as a nitrogen fertilizer for plant growth. In the human body, the enzyme carbonic anhydrase catalyzes the reaction of carbon dioxide with water:

$$
\mathrm{CO}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{HCO}_{3}^{-}(a q)
$$

The forward reaction occurs when the blood takes up $\mathrm{CO}_{2}$ in the tissues, and the reverse reaction occurs when the blood releases $\mathrm{CO}_{2}$ in the lungs. Remarkably, carbonic anhydrase increases the rate of these reactions by a factor of about $10^{6}$.

How does a catalyst work? A catalyst accelerates the rate of a reaction by making available a new and more efficient mechanism for conversion of reactants to products. Let's consider the decomposition of hydrogen peroxide in a basic, aqueous solution:

$$
2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g)
$$

Although unstable with respect to water and oxygen, hydrogen peroxide decomposes only very slowly at room temperature because the reaction has a high activation energy ( $76 \mathrm{~kJ} / \mathrm{mol}$ ). In the presence of iodide ion, however, the reaction is appreciably faster (Figure 12.16) because it can proceed by a different, lowerenergy pathway:

Step 1. $\mathrm{H}_{2} \mathrm{O}_{2}(a q)+\mathrm{I}^{-}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{IO}^{-}(a q)$
Slower, rate-determining
Step 2. $\mathrm{H}_{2} \mathrm{O}_{2}(a q)+\mathrm{IO}^{-}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g)+\mathrm{I}^{-}(a q)$ Faster

$$
2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g) \quad \text { Overall reaction }
$$

The $\mathrm{H}_{2} \mathrm{O}_{2}$ first oxidizes the catalyst $\left(\mathrm{I}^{-}\right)$to hypoiodite ion $\left(\mathrm{IO}^{-}\right)$and then reduces the intermediate $\mathrm{IO}^{-}$back to $\mathrm{I}^{-}$. The catalyst does not appear in the overall reaction because it is consumed in step 1 and regenerated in step 2 . The catalyst is, however, intimately involved in the reaction because $\mathrm{I}^{-}$appears in the observed rate law:

$$
\text { Rate }=-\frac{\Delta\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]}{\Delta t}=k\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]\left[\mathrm{I}^{-}\right]
$$

The rate law is consistent with the reaction of $\mathrm{H}_{2} \mathrm{O}_{2}$ and $\mathrm{I}^{-}$as the rate-determining step. In general, a catalyst is consumed in one step of a reaction and is regenerated in a subsequent step, whereas an intermediate is formed in one step and is consumed in a subsequent step.

The catalyzed pathway for a reaction might have a faster rate than the uncatalyzed pathway either because of a larger frequency factor $A$ or a smaller activation energy $E_{\mathrm{a}}$ in the Arrhenius equation. Usually, however, catalysts function by making available a reaction pathway with a lower activation energy (Figure 12.17). In the decomposition of hydrogen peroxide, for example, catalysis by $\mathrm{I}^{-}$ lowers $E_{\mathrm{a}}$ for the overall reaction by $19 \mathrm{~kJ} / \mathrm{mol}$.

Because the reaction occurs in two steps, the energy profile in Figure 12.17 exhibits two maxima (two transition states), with a minimum in between that represents the energy of the intermediate species present after the first step. The first maximum is higher than the second because the first step is rate-determining, and

the activation energy for the overall reaction is $E_{\mathrm{a}}$ for the first step. Maxima for both steps, though, are lower than $E_{\mathrm{a}}$ for the uncatalyzed pathway. Note that a catalyst does not affect the energies of the reactants and products. They are the same for the catalyzed pathway and the uncatalyzed pathway.

## Worked Key Concept Example 12.12

The relative rates of the reaction $A+B \rightarrow A B$ in vessels (1)-(4) are 1:2:1:2. Red spheres represent A molecules, blue spheres represent $B$ molecules, and yellow spheres represent molecules of a third substance C.


(2)

(3)

(4)
(a) What is the order of the reaction in $\mathrm{A}, \mathrm{B}$, and C ?
(b) Write the rate law.
(c) Write a mechanism that agrees with the rate law.
(d) Why doesn't C appear in the equation for the overall reaction?

## Strategy and Solution

(a) Count the number of molecules of each type in vessels (1)-(4), and compare the relative rates with the relative number of molecules. The concentration of A molecules in vessel (2) is twice that in vessel (1) while the concentrations of B and C remain constant. Because the reaction rate in vessel (2) is twice that in vessel (1), the rate is proportional to [A], and so the reaction is first order in A . When $[\mathrm{B}]$ is doubled [compare vessels (1) and (3)], the rate is unchanged, so the reaction is zero order in B. When [C] is doubled [compare vessels (1) and (4)], the rate doubles, so the reaction is first order in C.
(b) The rate law can be written as rate $=k[\mathrm{~A}]^{m}[\mathrm{~B}]^{n}[\mathrm{C}]^{p}$, where the exponents $m, n$, and $p$ specify the reaction orders in $\mathrm{A}, \mathrm{B}$, and C , respectively. Since the reaction is first order in A and C , and zero order in B , the rate law is rate $=k[\mathrm{~A}][\mathrm{C}]$.
© FIGURE 12.17 Typical potential energy profiles for a reaction whose activation energy is lowered by the presence of a catalyst: (a) the catalyzed pathway; (b) the uncatalyzed pathway. The shape of the barrier for the catalyzed pathway describes the decomposition of $\mathrm{H}_{2} \mathrm{O}_{2}$ : The first of the two maxima is higher because the first step is rate-determining.

(c) The rate law tells us that A and C collide in the rate-determining step because the rate law for the overall reaction is the rate law for the rate-determining step. Subsequent steps in the mechanism are faster than the rate-determining step, and the various steps must sum up to give the overall reaction. Therefore, a plausible mechanism is

$$
\begin{aligned}
\mathrm{A}+\mathrm{C} \longrightarrow \mathrm{AC} & \begin{array}{l}
\text { Slower, rate-determining } \\
\mathrm{AC}+\mathrm{B} \longrightarrow \mathrm{AB}+\mathrm{C}
\end{array} \\
\hline \mathrm{~A}+\mathrm{B} \longrightarrow \mathrm{AB} & \text { Overall reaction }
\end{aligned}
$$

(d) C doesn't appear in the overall reaction because it is consumed in the first step and regenerated in the second step. C is therefore a catalyst. AC is an intermediate because it is formed in the first step and consumed in the second step.

- KEY CONCEPT PROBLEM 12.17 The relative rates of the reaction $2 \mathrm{~A}+\mathrm{C}_{2} \rightarrow$ 2 AC in vessels (1)-(4) are 1:1:2:3. Red spheres represent A molecules, blue spheres represent $B$ molecules, and connected yellow spheres represent $C_{2}$ molecules.

$\}$A. Sae, "Hydrogen Peroxide Demo Curing the Brown-Bottle-with-Cap Syndrome," J. Chem. Educ., Vol. 71, 1994, 433. Hydrogen peroxide solutions from three different consumer products are decomposed catalytically with iodide, producing oxygen gas and water in the presence of bubble bath. The rate of oxygen production is proportional to the amount of bubbling observed. Observations are related to the reaction mechanism.

Lee R. Summerlin and James L. Ealy, "Catalytic Decomposition of Hydrogen Peroxide: Foam Production," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), pp. 101-102. Oxygen gas is catalytically produced in the presence of detergent resulting in the formation of a large quantity of foam.


(2)

(3)

(4)
(a) What is the order of the reaction in $\mathrm{A}, \mathrm{B}$, and $\mathrm{C}_{2}$ ?
(b) Write the rate law.
(c) Write a mechanism that agrees with the rate law.
(d) Identify all catalysts and intermediates in your mechanism.

### 12.13 Homogeneous and Heterogeneous Catalysts

Catalysts are commonly classified as either homogeneous or heterogeneous. A homogeneous catalyst is one that exists in the same phase as the reactants. For example, iodide ion is a homogeneous catalyst for the decomposition of aqueous hydrogen peroxide because both $\mathrm{I}^{-}$and $\mathrm{H}_{2} \mathrm{O}_{2}$ are present in the same aqueous solution phase.

In the atmosphere, nitric oxide is a gas-phase homogeneous catalyst for the conversion of molecular oxygen to ozone, a process described by the following series of reactions:

$$
\begin{aligned}
& 1 / 2 \mathrm{O}_{2}(g)+\mathrm{NO}(g) \longrightarrow \mathrm{NO}_{2}(g) \\
& \mathrm{NO}_{2}(g) \xrightarrow{\text { Sunlight }} \mathrm{NO}(g)+\mathrm{O}(g) \\
& \mathrm{O}(g)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{O}_{3}(g) \\
& 3 / 2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{O}_{3}(g)
\end{aligned}
$$

Nitric oxide first reacts with atmospheric $\mathrm{O}_{2}$ to give nitrogen dioxide, a poisonous brown gas. Subsequently, $\mathrm{NO}_{2}$ absorbs sunlight and dissociates to give an oxygen atom, which then reacts with $\mathrm{O}_{2}$ to form ozone. As usual, the catalyst $(\mathrm{NO})$ and the intermediates $\left(\mathrm{NO}_{2}\right.$ and O$)$ do not appear in the chemical equation for the overall reaction.

A heterogeneous catalyst is one that exists in a different phase from that of the reactants. Ordinarily, the catalyst is a solid, and the reactants are either gases or liquids. In the Fischer-Tropsch process for manufacturing synthetic gasoline, for example, tiny particles of a metal such as iron or cobalt coated on alumina $\left(\mathrm{Al}_{2} \mathrm{O}_{3}\right)$ catalyze the conversion of gaseous carbon monoxide and hydrogen to hydrocarbons such as octane $\left(\mathrm{C}_{8} \mathrm{H}_{18}\right)$ :

$$
8 \mathrm{CO}(g)+17 \mathrm{H}_{2}(g) \xrightarrow[\text { catalyst }]{\mathrm{Co} / \mathrm{Al}_{2} \mathrm{O}_{3}} \mathrm{C}_{8} \mathrm{H}_{18}(l)+8 \mathrm{H}_{2} \mathrm{O}(l)
$$

The mechanism of heterogeneous catalysis is often complex and not well understood. Important steps, however, involve (1) attachment of reactants to the surface of the catalyst, a process called adsorption, (2) conversion of reactants to products on the surface, and (3) desorption of products from the surface. The adsorption step is thought to involve chemical bonding of reactants to the highly reactive metal atoms on the surface with accompanying breaking, or at least weakening, of bonds in the reactants.

To illustrate, consider the catalytic hydrogenation of compounds with $\mathrm{C}=\mathrm{C}$ double bonds, a reaction used in the food industry to convert unsaturated vegetable oils to solid fats. The simplest reaction of this type is the hydrogenation of ethylene, which is catalyzed by finely divided metals such as Ni, Pd, or Pt:


As shown in Figure 12.18, the function of the metal surface is to adsorb the reactants and facilitate the rate-determining step, breaking the strong $\mathrm{H}-\mathrm{H}$ bond in the $\mathrm{H}_{2}$ molecule. Because the $\mathrm{H}-\mathrm{H}$ bond breaking is accompanied by simultaneous formation of bonds from the separating H atoms to the surface metal atoms, the activation energy for the process is lowered. The H atoms then move about on the surface until they encounter the C atoms of the adsorbed $\mathrm{C}_{2} \mathrm{H}_{4}$ molecule. Subsequent stepwise formation of two new $\mathrm{C}-\mathrm{H}$ bonds gives $\mathrm{C}_{2} \mathrm{H}_{6}$, which is finally desorbed from the surface.


A FIGURE 12.18 Proposed mechanism for the catalytic hydrogenation of ethylene $\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)$ on a metal surface. (a) $\mathrm{H}_{2}$ and $\mathrm{C}_{2} \mathrm{H}_{4}$ are adsorbed on the metal surface. (b) The $\mathrm{H}-\mathrm{H}$ bond breaks as $\mathrm{H}-$ metal bonds form, and the H atoms move about on the surface. (c) One H atom forms a bond to a C atom of the adsorbed $\mathrm{C}_{2} \mathrm{H}_{4}$ to give a metal-bonded $\mathrm{C}_{2} \mathrm{H}_{5}$ group. (d) A second H atom bonds to the $\mathrm{C}_{2} \mathrm{H}_{5}$ group, and the resulting $\mathrm{C}_{2} \mathrm{H}_{6}$ molecule is desorbed from the surface.

Christine L Copper and
Edward Koubeck, "An Experiment To Demonstrate How a Catalyst Affects the Rate of a Reaction," J. Chem. Educ., Vol. 76, 1999, 1714-1715. Describes a chemistry experiment that allows students to calculate rates of reaction, orders of reaction, and activation energies.


Most of the catalysts used in industrial chemical processes are heterogeneous, in part because such catalysts can be easily separated from the reaction products. Table 12.6 lists some commercial processes that employ heterogeneous catalysts.

| Reaction | Catalyst | Commercial Process | End Product: <br> Commercial Uses |
| :---: | :---: | :---: | :---: |
| $2 \mathrm{SO}_{2}+\mathrm{O}_{2} \longrightarrow 2 \mathrm{SO}_{3}$ | Pt or $\mathrm{V}_{2} \mathrm{O}_{5}$ | Intermediate step in the contact process for synthesis of sulfuric acid | $\mathrm{H}_{2} \mathrm{SO}_{4}$ : Manufacture of fertilizers, chemicals; oil refining |
| $4 \mathrm{NH}_{3}+5 \mathrm{O}_{2} \longrightarrow 4 \mathrm{NO}+6 \mathrm{H}_{2} \mathrm{O}$ | Pt and Rh | First step in the Ostwald process for synthesis of nitric acid | $\mathrm{HNO}_{3}$ : Manufacture of explosives, fertilizers, plastics, dyes, lacquers |
| $\mathrm{N}_{2}+3 \mathrm{H}_{2} \longrightarrow 2 \mathrm{NH}_{3}$ | $\mathrm{Fe}, \mathrm{K}_{2} \mathrm{O}$, and $\mathrm{Al}_{2} \mathrm{O}_{3}$ | Haber process for synthesis of ammonia | $\mathrm{NH}_{3}$ : Manufacture of fertilizers, nitric acid |
| $\mathrm{H}_{2} \mathrm{O}+\mathrm{CH}_{4} \longrightarrow \mathrm{CO}+3 \mathrm{H}_{2}$ | Ni | Steam-hydrocarbon re-forming process for synthesis of hydrogen | $\mathrm{H}_{2}$ : Manufacture of ammonia, methanol |
| $\mathrm{CO}+\mathrm{H}_{2} \mathrm{O} \longrightarrow \mathrm{CO}_{2}+\mathrm{H}_{2}$ | ZnO and CuO | Water-gas shift reaction to improve yield in the synthesis of $\mathrm{H}_{2}$ | $\mathrm{H}_{2}$ : Manufacture of ammonia, methanol |
| $\mathrm{CO}+2 \mathrm{H}_{2} \longrightarrow \mathrm{CH}_{3} \mathrm{OH}$ | ZnO and $\mathrm{Cr}_{2} \mathrm{O}_{3}$ | Industrial synthesis of methanol | $\mathrm{CH}_{3} \mathrm{OH}$ : Manufacture of plastics, adhesives, gasoline additives; industrial solvent |
|  | Ni, Pd, or Pt | Catalytic hydrogenation of compounds with $\mathrm{C}=\mathrm{C}$ bonds, as in conversion of unsaturated vegetable oils to solid fats | Food products: margarine, shortening |

Another important application of heterogeneous catalysts is in automobile catalytic converters. Despite much work on engine design and fuel composition, automotive exhaust emissions contain air pollutants such as unburned hydrocarbons $\left(\mathrm{C}_{x} \mathrm{H}_{y}\right)$, carbon monoxide, and nitric oxide. Carbon monoxide results from incomplete combustion of hydrocarbon fuels, and nitric oxide is produced when atmospheric nitrogen and oxygen combine at the high temperatures present in an
automobile engine. Catalytic converters help convert the offending pollutants to carbon dioxide, water, nitrogen, and oxygen (Figure 12.19):

$$
\begin{aligned}
\mathrm{C}_{x} \mathrm{H}_{y}(g)+(x+y / 4) \mathrm{O}_{2}(g) & \longrightarrow x \mathrm{CO}_{2}(g)+(y / 2) \mathrm{H}_{2} \mathrm{O}(g) \\
2 \mathrm{CO}(g)+\mathrm{O}_{2}(g) & \longrightarrow 2 \mathrm{CO}_{2}(g) \\
2 \mathrm{NO}(g) & \longrightarrow \mathrm{N}_{2}(g)+\mathrm{O}_{2}(g)
\end{aligned}
$$



A FIGURE 12.19 The gases exhausted from an automobile engine pass through a catalytic converter where air pollutants such as unburned hydrocarbons $\left(\mathrm{C}_{x} \mathrm{H}_{y}\right), \mathrm{CO}$, and NO are converted to $\mathrm{CO}_{2}, \mathrm{H}_{2} \mathrm{O}, \mathrm{N}_{2}$, and $\mathrm{O}_{2}$. The photo shows a cutaway view of a catalytic converter. The beads are impregnated with the heterogeneous catalyst.

Typical catalysts for these reactions are the so-called noble metals Pt and Pd , and transition metal oxides $\mathrm{V}_{2} \mathrm{O}_{5}, \mathrm{Cr}_{2} \mathrm{O}_{3}$, and CuO . Because the surface of the catalyst is rendered ineffective ("poisoned") by adsorption of lead, automobiles with catalytic converters must use unleaded gasoline.

Sir John Meurig Thomas, "Solid Acid Catalysts," Scientific American., April 1992, 112-118.

Th Cynthia M. Friend, "Catalysis on Surfaces," Scientific American., April 1993, 74-79.

Mitch Jacoby, "Getting Auto Exhausts to Pristine," Chem. Eng. News, January 25, 1999, 36-44.

Robert J. Farrauto, Ronald M. Heck, and Barry K. Speronello, "Environmental Catalysts," Chem. Eng. News, September 7, 1992, 34-44.

## Interlude Explosives

Some chemical reactions are slow and some are fast, but explosions are in a class by themselves. Chemical explosions are characterized by the nearly instantaneous release of large quantities of hot gases such as $\mathrm{N}_{2}, \mathrm{CO}_{2}$, and $\mathrm{H}_{2} \mathrm{O}$. The rapidly expanding gases set up a shock wave of enormous pressure-up to $700,000 \mathrm{~atm}$-that propagates through the surroundings at speeds of up to $9000 \mathrm{~m} / \mathrm{s}(20,000 \mathrm{mi} / \mathrm{h})$, causing the physical destruction we've all seen in movies and television newscasts.

Explosives are generally categorized as either primary or secondary, depending on their sensitivity to shock. Primary explosives are the most sensitive to heat and shock. They are generally used in detonators, blasting caps, and military fuses to initiate the explosion of the less-sensitive secondary explosives. Mercury(II) fulminate, $\mathrm{Hg}(\mathrm{ONC})_{2}$, was the first initiator to be used commercially, but it has been largely replaced by lead(II) azide, $\mathrm{Pb}\left(\mathrm{N}_{3}\right)_{2}$, which is more stable when stored under hot conditions.

Secondary explosives, or high explosives, are generally less sensitive to heat and shock than primary explosives and are therefore safer to manufacture, transport, and handle. Most secondary explosives will simply burn rather than explode when ignited in air, and most can be detonated only by the nearby explosion of a primary initiator. Among the most common secondary explosives are nitroglycerin, trinitro-

The high-pressure shock wave caused by
a che a chemical explosuiding.
demolish this buil
toluene (TNT), pentaerythritol tetranitrate (PETN), and RDX.



Nitroglycerin




As suggested by these structures, most explosives are rich in oxygen and nitrogen, and most contain nitro groups, $-\mathrm{NO}_{2}$. Because the chemical bonds in nitro groups are relatively weak (about $200 \mathrm{~kJ} / \mathrm{mol}$ ), and because the explosion products $\left(\mathrm{CO}_{2}, \mathrm{~N}_{2}, \mathrm{H}_{2} \mathrm{O}\right.$, and others) are extremely stable, a great deal of energy is released within a few microseconds during an explosion. One mole ( 227 g ) of nitroglycerin, for example, releases 1427 kJ when it explodes. The actual mix of reaction products is complex, but the reaction can be approximated by the balanced equation

$$
4 \mathrm{C}_{3} \mathrm{H}_{5} \mathrm{~N}_{3} \mathrm{O}_{9}(l) \longrightarrow 12 \mathrm{CO}_{2}(g)+10 \mathrm{H}_{2} \mathrm{O}(g)+6 \mathrm{~N}_{2}(g)+\mathrm{O}_{2}(g)
$$

Thus, 29 mol of gaseous products with a volume of 650 L at STP (Section 9.3) are produced from just 4 mol of liquid nitroglycerin.

The first commercially important high explosive was nitroglycerin, prepared in 1847 by reaction of glycerin with nitric acid in the presence of sulfuric acid:


This reaction is extremely hazardous to carry out. In fact, it wasn't until 1865 that the Swedish chemist and industrialist Alfred Nobel succeeded in finding a relatively safe method of producing nitroglycerin and of incorporating it into a reliable commercial blasting product known as dynamite. (Nobel's discovery resulted in a large personal fortune, which he used to establish the Nobel Prizes.) Modern industrial dynamite used for quarrying stone and blasting roadbeds is a mixture of ammonium nitrate and nitroglycerin absorbed onto diatomaceous earth.

Military explosives are generally used as fillings for bombs or shells and must therefore have a very low sensitivity to impact shock on firing. In addition, they must have good stability for long-term storage under adverse conditions, and they should have a low mass-to-energy ratio. TNT and RDX are the most commonly used military high explosives. PETN and RDX are also often compounded with waxes or synthetic polymers to make so-called plastic explosives.

PROBLEM 12.18 The explosive decomposition of nitroglycerin is highly exothermic. Explain.

PROBLEM 12.19 Would you expect a higher activation energy for the decomposition of a primary or a secondary explosive? Explain.

PROBLEM 12.20 The reaction that occurs on detonation of pentaerythritol tetranitrate (PETN) can be approximated by the equation

$$
\mathrm{C}_{5} \mathrm{H}_{8} \mathrm{~N}_{4} \mathrm{O}_{12}(s) \longrightarrow 4 \mathrm{CO}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(g)+2 \mathrm{~N}_{2}(g)+\mathrm{C}(s)
$$

Use the standard heats of formation given in Appendix $B$ to calculate the standard heat of reaction in kilojoules. For PETN, $\Delta H^{\circ}{ }_{\mathrm{f}}=537 \mathrm{~kJ} / \mathrm{mol}$. (For a review of $\Delta H^{\circ}{ }_{\mathrm{f}}$, see Section 8.10.)

- PROBLEM 12.21 How many liters of gas are produced from the decomposition of 1.54 kg of PETN according to the equation in Problem 12.20? Assume that the gas has a temperature of $800^{\circ} \mathrm{C}$ and a pressure of 0.975 atm .

Chemical kinetics is the area of chemistry concerned with reaction rates. A reaction rate is defined as the increase in the concentration of a product, or the decrease in the concentration of a reactant, per unit time. It can be expressed as the average rate during a given time interval, the instantaneous rate at a particular time, or the initial rate at the beginning of the reaction.

Reaction rates depend on reactant concentrations, temperature, and the presence of catalysts. The concentration dependence is given by the rate law, rate $=k[\mathrm{~A}]^{m}[\mathrm{~B}]^{n}$, where $k$ is the rate constant, $m$ and $n$ specify the reaction order with respect to reactants A and B , and $m+n$ is the overall reaction order. The values of $m$ and $n$ must be determined by experiment; they can't be deduced from the stoichiometry of the overall reaction.

The integrated rate law is a concentration-time equation that makes it possible to calculate concentrations at any time $t$ or the time required for an initial concentration to reach any particular value. For a first-order reaction, the integrated rate law is $\ln [\mathrm{A}]_{t}=-k t+\ln [\mathrm{A}]_{0}$. A graph of $\ln [\mathrm{A}]$ versus time is a straight line with a slope equal to $-k$. For a second-order reaction, the integrated rate law is $1 /[\mathrm{A}]_{t}=k t+1 /[\mathrm{A}]_{0}$. A graph of $1 /[A]$ versus time is linear with a slope equal to $k$. For a zerothorder reaction, the integrated rate law is $[\mathrm{A}]=-k t+[\mathrm{A}]_{0}$, and a graph of $[\mathrm{A}]$ versus time is linear with a slope equal to $-k$. The half-life ( $t_{1 / 2}$ ) of a reaction is the time required for the reactant concentration to drop to one-half its initial value.

A reaction mechanism is the sequence of elementary reactions, or elementary steps, that defines the pathway from reactants to products. Elementary reactions are classified as unimolecular, bimolecular, or termolecular, depending on whether one, two, or three reactant molecules are
involved. The rate law for an elementary reaction follows directly from its molecularity: rate $=k[\mathrm{~A}]$ for a unimolecular reaction, and rate $=k[\mathrm{~A}]^{2}$ or rate $=k[\mathrm{~A}][\mathrm{B}]$ for a bimolecular reaction. The observed rate law for an overall reaction depends on the sequence of elementary steps and their relative rates. The slowest step in a reaction mechanism is called the rate-determining step. A chemical species that is formed in one elementary step and consumed in a subsequent step is called a reaction intermediate. An acceptable mechanism must meet two criteria: (1) The elementary steps must sum to give the overall reaction, and (2) the mechanism must be consistent with the observed rate law.

The temperature dependence of rate constants is described by the Arrhenius equation, $k=A e^{-E_{a} / R T}$, where $A$ is the frequency factor and $E_{\mathrm{a}}$ is the activation energy. The value of $E_{\mathrm{a}}$ can be determined from the slope of a linear plot of $\ln k$ versus $1 / T$, and it can be interpreted as the height of the potential energy barrier between reactants and products. The configuration of atoms at the top of the barrier is called the transition state. According to collision theory, the rate constant is given by $k=p Z e^{-E_{\mathrm{a}} / R T}$, where $p$ is a steric factor (the fraction of collisions in which the molecules have the proper orientation for reaction), $Z$ is a constant related to the collision frequency, and $e^{-E_{a} / R T}$ is the fraction of collisions with energy equal to or greater than $E_{a}$.

A catalyst is a substance that increases the rate of a reaction without being consumed in the reaction. It functions by making available an alternative reaction pathway that has a lower activation energy. A homogeneous catalyst is present in the same phase as the reactants, whereas a heterogeneous catalyst is present in a different phase.

## Key Words

activation energy, $\boldsymbol{E}_{\mathbf{a}} 499$
Arrhenius equation 502
bimolecular reaction 493
catalyst 505
chemical kinetics 472
collision theory 499
elementary reaction 492
elementary step 492
first-order reaction 482
frequency factor 502
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initial rate 475
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rate law 476
reaction intermediate 493
reaction mechanism 492
reaction order 477
reaction rate 473
second-order reaction 488
steric factor, $\boldsymbol{p} 501$
termolecular reaction 493
transition state 499 unimolecular reaction 493
zeroth-order reaction 491


## Understanding Key Concepts

Problems 12.1-12.21 appear within the chapter.
12.22 The following reaction is first order in A (red spheres) and first order in B (blue spheres):
A $+\mathrm{B} \longrightarrow$ Products

Rate $=k[\mathrm{~A}][\mathrm{B}]$
(1)

(2)

(3)

(4)
(a) What are the relative rates of this reaction in vessels (1)-(4)? Each vessel has the same volume.
(b) What are the relative values of the rate constant $k$ for cases (1)-(4)?
12.23 Consider the first-order decomposition of A molecules (red spheres) in three vessels of equal volume.

(1)

(2)

(3)
(a) What are the relative rates of decomposition in vessels (1)-(3)?
(b) What are the relative half-lives of the reactions in vessels (1)-(3)?
(c) How will the rates and half-lives be affected if the volume of each vessel is decreased by a factor of 2 ?
12.24 Consider the first-order reaction $A \rightarrow B$ in which $A$ molecules (red spheres) are converted to B molecules (blue spheres).
(a) Given the following pictures at $t=0 \mathrm{~min}$ and $t=1 \mathrm{~min}$, draw pictures that show the number of A and B molecules present at $t=2 \mathrm{~min}$ and $t=3 \mathrm{~min}$.
(b) What is the half-life of the reaction?

12.25 The following pictures represent the progress of the reaction $A \rightarrow B$ in which A molecules (red spheres) are converted to $B$ molecules (blue spheres).

$t=0 \mathrm{~min}$

$t=1$ min

$t=2$ min
(a) What is the order of the reaction?
(b) Draw a picture that shows the number of A and B molecules present at $t=3 \mathrm{~min}$.
(c) Suppose that each sphere represents $6.0 \times 10^{21}$ molecules and that the volume of the container is 1.0 L . What is the rate constant for the reaction in the usual units?
12.26 The following pictures represent the progress of a reaction in which two A molecules combine to give a more complex molecule $\mathrm{A}_{2}, 2 \mathrm{~A} \rightarrow \mathrm{~A}_{2}$.

(a) Is the reaction first order or second order in A ?
(b) What is the rate law?
(c) Draw an appropriate picture in the last box, and specify the time.
12.27 What is the molecularity of each of the following elementary reactions?

12.28 Consider a reaction that occurs by the following mechanism:
-

$$
\begin{aligned}
& \mathrm{A}+\mathrm{BC} \longrightarrow \mathrm{AC}+\mathrm{B} \\
& \mathrm{AC}+\mathrm{D} \longrightarrow \mathrm{~A}+\mathrm{CD}
\end{aligned}
$$

The potential energy profile for this reaction is shown below:

(a) What is the equation for the overall reaction?
(b) Write structural formulas for all species present at reaction stages $1-5$. Identify each species as a reactant, product, catalyst, intermediate, or transition state.
(c) Which of the two steps in the mechanism is the rate-determining step? Write the rate law for the overall reaction.
(d) Is the reaction endothermic or exothermic? Add labels to the diagram that show the values of the energy of reaction $\Delta E$ and the activation energy $E_{\mathrm{a}}$ for the overall reaction.
12.29 Draw a plausible transition state for the bimolecular reaction of nitric oxide with ozone. Use dashed lines to indicate the atoms that are weakly linked together in the transition state.

$$
\mathrm{NO}(g)+\mathrm{O}_{3}(g) \longrightarrow \mathrm{NO}_{2}(g)+\mathrm{O}_{2}(g)
$$



## Additional Problems

## Reaction Rates

12.30 What are the usual units of reaction rate?
12.31 Concentrations of trace constituents of the atmosphere are sometimes expressed in molecules $/ \mathrm{cm}^{3}$. If those units are used for concentrations, what are the units of reaction rate?
12.32 Given the concentration-time data in Problem 12.8, calculate the average rate of decomposition of cyclopropane during the following time intervals:
(a) $0-5.0 \mathrm{~min}$
(b) $15.0-20.0 \mathrm{~min}$
12.33 Concentration-time data for the decomposition of nitrogen dioxide are given in Worked Example 12.8. What is the average rate of decomposition of $\mathrm{NO}_{2}$ during the following time periods?
(a) $50-100 \mathrm{~s}$
(b) $100-150 \mathrm{~s}$
12.34 From the plot of concentration-time data in Figure 12.1, estimate:
(a) the instantaneous rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ at $t=200 \mathrm{~s}$.
(b) the initial rate of decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$
12.35 From a plot of the concentration-time data in Worked Example 12.8, estimate:
(a) the instantaneous rate of decomposition of $\mathrm{NO}_{2}$ at $t=100 \mathrm{~s}$
(b) the initial rate of decomposition of $\mathrm{NO}_{2}$
12.36 Ammonia is manufactured in large amounts by the reaction

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g)
$$

(a) How is the rate of consumption of $\mathrm{H}_{2}$ related to the rate of consumption of $\mathrm{N}_{2}$ ?
(b) How is the rate of formation of $\mathrm{NH}_{3}$ related to the rate of consumption of $\mathrm{N}_{2}$ ?
12.37 In the first step of the Ostwald process for the synthesis of nitric acid, ammonia is converted to nitric oxide by the high-temperature reaction

$$
4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(g)
$$

(a) How is the rate of consumption of $\mathrm{O}_{2}$ related to the rate of consumption of $\mathrm{NH}_{3}$ ?
(b) How are the rates of formation of NO and $\mathrm{H}_{2} \mathrm{O}$ related to the rate of consumption of $\mathrm{NH}_{3}$ ?
12.38 For the reaction $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightarrow 2 \mathrm{NH}_{3}(g)$, what is the relationship among $\Delta\left[\mathrm{N}_{2}\right] / \Delta t, \Delta\left[\mathrm{H}_{2}\right] / \Delta t$, and $\Delta\left[\mathrm{NH}_{3}\right] / \Delta t$ ?
12.39 The oxidation of iodide ion by peroxydisulfate ion is described by the equation

$$
3 \mathrm{I}^{-}(a q)+\mathrm{S}_{2} \mathrm{O}_{8}{ }^{2-}(a q) \longrightarrow \mathrm{I}_{3}^{-}(a q)+2 \mathrm{SO}_{4}{ }^{2-}(a q)
$$

(a) If $-\Delta\left[\mathrm{S}_{2} \mathrm{O}_{8}{ }^{2-}\right] / \Delta t=1.5 \times 10^{-3} \mathrm{M} / \mathrm{s}$ for a particular time interval, what is the value of $-\Delta\left[\mathrm{I}^{-}\right] / \Delta t$ for the same time interval?
(b) What is the average rate of formation of $\mathrm{SO}_{4}{ }^{2-}$ during that time interval?

## Rate Laws

12.40 The gas-phase reaction of nitric oxide and bromine yields nitrosyl bromide:

$$
2 \mathrm{NO}(g)+\mathrm{Br}_{2}(g) \longrightarrow 2 \mathrm{NOBr}(g)
$$

The rate law is rate $=k[\mathrm{NO}]^{2}\left[\mathrm{Br}_{2}\right]$. What is the reaction order with respect to each of the reactants, and what is the overall reaction order?
12.41 The reaction of gaseous chloroform and chlorine is described by the equation

$$
\mathrm{CHCl}_{3}(g)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{CCl}_{4}(g)+\mathrm{HCl}(g)
$$

The rate law is rate $=k\left[\mathrm{CHCl}_{3}\right]\left[\mathrm{Cl}_{2}\right]^{1 / 2}$. What is the order of the reaction with respect to $\mathrm{CHCl}_{3}$ and $\mathrm{Cl}_{2}$ ? What is the overall reaction order?
12.42 The gas-phase reaction of hydrogen and iodine monochloride,

$$
\mathrm{H}_{2}(g)+2 \mathrm{ICl}(g) \longrightarrow 2 \mathrm{HCl}(g)+\mathrm{I}_{2}(g)
$$

is first order in $\mathrm{H}_{2}$ and first order in ICl. What is the rate law, and what are the units of the rate constant?
12.43 The reaction $2 \mathrm{NO}(g)+2 \mathrm{H}_{2}(g) \rightarrow \mathrm{N}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)$ is first order in $\mathrm{H}_{2}$ and second order in NO. Write the rate law, and specify the units of the rate constant.
12.44 Bromomethane is converted to methanol in an alkaline solution:

$$
\mathrm{CH}_{3} \mathrm{Br}(a q)+\mathrm{OH}^{-}(a q) \longrightarrow \mathrm{CH}_{3} \mathrm{OH}(a q)+\mathrm{Br}^{-}(a q)
$$

The reaction is first order in each reactant.
(a) Write the rate law.
(b) How does the reaction rate change if the $\mathrm{OH}^{-}$concentration is decreased by a factor of 5 ?
(c) What is the change in rate if the concentrations of both reactants are doubled?
12.45 The oxidation of $\mathrm{Br}^{-}$by $\mathrm{BrO}_{3}^{-}$in acidic solution is described by the equation

$$
\begin{array}{r}
5 \mathrm{Br}^{-}(a q)+\mathrm{BrO}_{3}^{-}(a q)+6 \mathrm{H}^{+}(a q) \longrightarrow \\
3 \mathrm{Br}_{2}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)
\end{array}
$$

The reaction is first order in $\mathrm{Br}^{-}$, first order in $\mathrm{BrO}_{3}{ }^{-}$, and second order in $\mathrm{H}^{+}$.
(a) Write the rate law.
(b) What is the overall reaction order?
(c) How does the reaction rate change if the $\mathrm{H}^{+}$concentration is tripled?
(d) What is the change in rate if the concentrations of both $\mathrm{Br}^{-}$and $\mathrm{BrO}_{3}{ }^{-}$are halved?
12.46 At $600^{\circ} \mathrm{C}$, acetone $\left(\mathrm{CH}_{3} \mathrm{COCH}_{3}\right)$ decomposes to ketene $\left(\mathrm{CH}_{2}=\mathrm{C}=\mathrm{O}\right)$ and various hydrocarbons. Initial rate data are given in the table:

## Initial Rate of

 Decomposition ofExperiment Initial $\left[\mathrm{CH}_{3} \mathbf{C O C H}_{3}\right]$
$\mathrm{CH}_{3} \mathrm{COCH}_{3}(\mathrm{M} / \mathrm{s})$

1

$$
6.0 \times 10^{-3}
$$

$5.2 \times 10^{-5}$
2
$9.0 \times 10^{-3}$
$7.8 \times 10^{-5}$
(a) Determine the rate law.
(b) Calculate the rate constant.
(c) Calculate the rate of decomposition when the acetone concentration is $1.8 \times 10^{-3} \mathrm{M}$.
12.47 The initial rates listed in the table were determined for the thermal decomposition of azomethane $\left(\mathrm{CH}_{3} \mathrm{NNCH}_{3}\right)$ :

$$
\mathrm{CH}_{3} \mathrm{NNCH}_{3}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{6}(g)+\mathrm{N}_{2}(g)
$$

|  | Initial | Initial Rate of <br> Decomposition of <br> Experiment |
| :--- | :--- | :--- |
| $\left[\mathbf{C H}_{\mathbf{3}} \mathbf{N N C H}_{\mathbf{3}}\right]$ | $\mathbf{C H}_{\mathbf{3}} \mathbf{N N C H}_{\mathbf{3}} \mathbf{( M / s )}$ |  |
| 1 | $2.4 \times 10^{-2}$ | $6.0 \times 10^{-6}$ |
| 2 | $8.0 \times 10^{-3}$ | $2.0 \times 10^{-6}$ |

(a) What is the rate law?
(b) What is the value of the rate constant?
(c) What is the rate of decomposition when the concentration of azomethane is 0.020 M ?
12.48 Initial rate data at $25^{\circ} \mathrm{C}$ are listed in the table for the reaction

$$
\mathrm{NH}_{4}^{+}(a q)+\mathrm{NO}_{2}^{-}(a q) \longrightarrow \mathrm{N}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

| Experiment | Initial <br> $\left[\mathbf{N H}_{\mathbf{4}}{ }^{+} \mathbf{]}\right.$ | Initial <br> $\mathbf{[} \mathbf{N O}_{\mathbf{2}}{ }^{-} \mathbf{]}$ | Initial Rate of <br> Consumption <br> $\mathbf{o f} \mathbf{N H}_{\mathbf{4}}{ }^{+} \mathbf{( M / \mathbf { s } )}$ |
| :--- | :--- | :--- | :--- |
| 1 | 0.24 | 0.10 | $7.2 \times 10^{-6}$ |
| 2 | 0.12 | 0.10 | $3.6 \times 10^{-6}$ |
| 3 | 0.12 | 0.15 | $5.4 \times 10^{-6}$ |

(a) What is the rate law?
(b) What is the value of the rate constant?
(c) What is the reaction rate when the concentrations are $\left[\mathrm{NH}_{4}{ }^{+}\right]=0.39 \mathrm{M}$ and $\left[\mathrm{NO}_{2}^{-}\right]=0.052 \mathrm{M}$ ?
12.49 The initial rates listed in the table were determined for the reaction

$$
2 \mathrm{NO}(g)+\mathrm{Cl}_{2}(g) \longrightarrow 2 \mathrm{NOCl}(g)
$$

| Experiment | Initial <br> [NO] | Initial <br> $\left[\mathbf{C l}_{\mathbf{2}}\right]$ | Initial Rate of <br> Consumption <br> of $\mathbf{C l}_{\mathbf{2}} \mathbf{( M / s )}$ |
| :--- | :--- | :--- | :--- |
| 1 | 0.13 | 0.20 | $1.0 \times 10^{-2}$ |
| 2 | 0.26 | 0.20 | $4.0 \times 10^{-2}$ |
| 3 | 0.13 | 0.10 | $5.0 \times 10^{-3}$ |

(a) What is the rate law?
(b) What is the value of the rate constant?
(c) What is the reaction rate when both reactant concentrations are 0.12 M ?

## Integrated Rate Law; Half-Life

12.50 At $500^{\circ} \mathrm{C}$, cyclopropane $\left(\mathrm{C}_{3} \mathrm{H}_{6}\right)$ rearranges to propene $\left(\mathrm{CH}_{3}-\mathrm{CH}=\mathrm{CH}_{2}\right)$. The reaction is first order, and the rate constant is $6.7 \times 10^{-4} \mathrm{~s}^{-1}$. If the initial concentration of $\mathrm{C}_{3} \mathrm{H}_{6}$ is 0.0500 M :
(a) What is the molarity of $\mathrm{C}_{3} \mathrm{H}_{6}$ after 30 min ?
(b) How many minutes does it take for the $\mathrm{C}_{3} \mathrm{H}_{6}$ concentration to drop to 0.0100 M ?
(c) How many minutes does it take for $25 \%$ of the $\mathrm{C}_{3} \mathrm{H}_{6}$ to react?
12.51 The rearrangement of methyl isonitrile $\left(\mathrm{CH}_{3} \mathrm{NC}\right)$ to acetonitrile $\left(\mathrm{CH}_{3} \mathrm{CN}\right)$ is a first-order reaction and has a rate constant of $5.11 \times 10^{-5} \mathrm{~s}^{-1}$ at 472 K .


If the initial concentration of $\mathrm{CH}_{3} \mathrm{NC}$ is 0.0340 M :
(a) What is the molarity of $\mathrm{CH}_{3} \mathrm{NC}$ after 2.00 h ?
(b) How many minutes does it take for the $\mathrm{CH}_{3} \mathrm{NC}$ concentration to drop to 0.0300 M ?
(c) How many minutes does it take for $20 \%$ of the $\mathrm{CH}_{3} \mathrm{NC}$ to react?
12.52 What is the half-life (in minutes) of the reaction in Problem 12.50? How many minutes will it take for the concentration of cyclopropane to drop to $6.25 \%$ of its initial value?
12.53 What is the half-life (in hours) of the reaction in Problem 12.51? How many hours will it take for the concentration of methyl isonitrile to drop to $12.5 \%$ of its initial value?
12.54 The decomposition of aqueous hydrogen peroxide to gaseous $\mathrm{O}_{2}$ and water is a first-order reaction. If it takes 8.0 h for the concentration of $\mathrm{H}_{2} \mathrm{O}_{2}$ to decrease from 0.80 M to 0.40 M , how many hours are required for the concentration to decrease from 0.60 M to 0.15 M ?
12.55 Sucrose (table sugar) reacts with water in acidic solution to give glucose and fructose, two simpler sugars that have the same molecular formulas but different structures.

$$
\begin{aligned}
& \mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \\
& \text { Sucrose } \\
& \underset{\text { Glucose }}{\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(a q)+}+\underset{\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(a q)}{\text { Fructose }}
\end{aligned}
$$

The reaction is first order in sucrose. At $25^{\circ} \mathrm{C}$, it takes 3.33 h for the concentration of sucrose to drop from 1.20 M to 0.600 M . How many hours are required for the concentration to drop from 0.800 M to 0.0500 M ?
12.56 Butadiene $\left(\mathrm{C}_{4} \mathrm{H}_{6}\right)$ reacts with itself to form a dimer with the formula $\mathrm{C}_{8} \mathrm{H}_{12}$. The reaction is second order in $\mathrm{C}_{4} \mathrm{H}_{6}$. If the rate constant at a particular temperature is $4.0 \times 10^{-2} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ and the initial concentration of $\mathrm{C}_{4} \mathrm{H}_{6}$ is 0.0200 M :
(a) What is its molarity after a reaction time of 1.00 h ?
(b) What is the time (in hours) when the $\mathrm{C}_{4} \mathrm{H}_{6}$ concentration reaches a value of 0.0020 M ?
12.57 Hydrogen iodide decomposes slowly to $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$ at 600 K . The reaction is second order in HI and the rate constant is $9.7 \times 10^{-6} \mathrm{M}^{-1} \mathrm{~s}^{-1}$. If the initial concentration of HI is 0.100 M :
(a) What is its molarity after a reaction time of 6.00 days?
(b) What is the time (in days) when the HI concentration reaches a value of 0.020 M ?
12.58 What is the half-life (in minutes) of the reaction in Problem 12.56 when the initial $\mathrm{C}_{4} \mathrm{H}_{6}$ concentration is 0.0200 M ? How many minutes does it take for the concentration of $\mathrm{C}_{4} \mathrm{H}_{6}$ to drop from 0.0100 M to 0.0050 M ?
12.59 What is the half-life (in days) of the reaction in Problem 12.57 when the initial HI concentration is 0.100 M ? How many days does it take for the concentration of HI to drop from 0.0250 M to 0.0125 M ?
12.60 At elevated temperatures, nitrous oxide decomposes according to the equation

$$
2 \mathrm{~N}_{2} \mathrm{O}(g) \longrightarrow 2 \mathrm{~N}_{2}(g)+\mathrm{O}_{2}(g)
$$

Given the following data, plot the appropriate graphs to determine whether the reaction is first order or second order. What is the value of the rate constant for consumption of $\mathrm{N}_{2} \mathrm{O}$ ?

| Time (min) | 0 | 60 | 90 | 120 | 180 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\left[\mathbf{N}_{\mathbf{2}} \mathbf{O}\right]$ | 0.250 | 0.218 | 0.204 | 0.190 | 0.166 |

12.61 Nitrosyl bromide decomposes at $10^{\circ} \mathrm{C}$ :

$$
2 \mathrm{NOBr}(g) \longrightarrow 2 \mathrm{NO}(g)+\mathrm{Br}_{2}(g)
$$

Use the following kinetic data to determine the order of the reaction and the value of the rate constant for consumption of NOBr .

| Time (s) | 0 | 10 | 20 | 30 | 40 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| [NOBr] | 0.0400 | 0.0303 | 0.0244 | 0.0204 | 0.0175 |

12.62 At $25^{\circ} \mathrm{C}$, the half-life of a certain first-order reaction is 248 s . What is the value of the rate constant at this temperature?
12.63 At $100^{\circ} \mathrm{C}$, a certain substance undergoes second-order decomposition with a half-life of 25 min . If the initial concentration of the substance is 0.036 M , what is the value of the rate constant at $100^{\circ} \mathrm{C}$ ?
12.64 A reaction of the type $A \rightarrow B+C$ has a rate constant $k=3.6 \times 10^{-5} \mathrm{M} / \mathrm{s}$.
(a) What is the order of the reaction?
(b) What is the molarity of A after a reaction time of 30.0 min if the initial concentration of A is 0.096 M ?
(c) What is the half-life (in minutes) of the reaction in part (b)?
12.65 Consider the following concentration-time data for the decomposition reaction $\mathrm{AB} \rightarrow \mathrm{A}+\mathrm{B}$.

| Time (min) | 0 | 20.0 | 40.0 | 60.0 | 80.0 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| [AB] | 0.200 | 0.185 | 0.170 | 0.155 | 0.140 |

(a) Determine the order of the reaction and the value of the rate constant.
(b) What is the molarity of AB after a reaction time of 126 min ?
(c) What is the time (in minutes) when the AB concentration reaches a value of 0.100 M ?

## Reaction Mechanisms

12.66 What is the difference between an elementary reaction and an overall reaction?
12.67 What is the difference between molecularity and reaction order?
12.68 What is the relationship between the coefficients in a balanced chemical equation for an overall reaction and the exponents in the rate law?
12.69 What distinguishes the rate-determining step from the other steps in a reaction mechanism? How does the rate-determining step affect the observed rate law?
12.70 Consider the following mechanism for the reaction of hydrogen and iodine monochloride:

Step 1. $\mathrm{H}_{2}(g)+\mathrm{ICl}(g) \longrightarrow \mathrm{HI}(g)+\mathrm{HCl}(g)$
Step 2. $\mathrm{HI}(g)+\mathrm{ICl}(g) \longrightarrow \mathrm{I}_{2}(g)+\mathrm{HCl}(g)$
(a) Write the equation for the overall reaction.
(b) Identify any reaction intermediates.
(c) What is the molecularity of each elementary step?
12.71 The following mechanism has been proposed for the reaction of nitric oxide and chlorine:

$$
\begin{array}{ll}
\text { Step 1. } & \mathrm{NO}(g)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{NOCl}_{2}(g) \\
\text { Step 2. } & \mathrm{NOCl}_{2}(g)+\mathrm{NO}(g) \longrightarrow 2 \mathrm{NOCl}_{(g)}
\end{array}
$$

(a) What is the overall reaction?
(b) Identify any reaction intermediates.
(c) What is the molecularity of each elementary step?
12.72 Give the molecularity and the rate law for each of the following elementary reactions:
(a) $\mathrm{O}_{3}(g)+\mathrm{Cl}(g) \rightarrow \mathrm{O}_{2}(g)+\mathrm{ClO}(g)$
(b) $\mathrm{NO}_{2}(g) \rightarrow \mathrm{NO}(g)+\mathrm{O}(g)$
(c) $\mathrm{ClO}(g)+\mathrm{O}(g) \rightarrow \mathrm{Cl}(g)+\mathrm{O}_{2}(g)$
(d) $\mathrm{Cl}(g)+\mathrm{Cl}(g)+\mathrm{N}_{2}(g) \rightarrow \mathrm{Cl}_{2}(g)+\mathrm{N}_{2}(g)$
12.73 Identify the molecularity and write the rate law for each of the following elementary reactions:
(a) $\mathrm{I}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{I}(\mathrm{g})$
(b) $2 \mathrm{NO}(g)+\mathrm{Br}_{2}(g) \rightarrow 2 \mathrm{NOBr}(g)$
(c) $\mathrm{CH}_{3} \mathrm{Br}(a q)+\mathrm{OH}^{-}(a q) \rightarrow \mathrm{CH}_{3} \mathrm{OH}(a q)+\mathrm{Br}^{-}(a q)$
(d) $\mathrm{N}_{2} \mathrm{O}_{5}(g) \rightarrow \mathrm{NO}_{2}(g)+\mathrm{NO}_{3}(g)$
12.74 The thermal decomposition of nitryl chloride, $\mathrm{NO}_{2} \mathrm{Cl}$, is believed to occur by the following mechanism:

$$
\begin{aligned}
& \mathrm{NO}_{2} \mathrm{Cl}(g) \xrightarrow{k_{1}} \mathrm{NO}_{2}(g)+\mathrm{Cl}(g) \\
& \mathrm{Cl}(g)+\mathrm{NO}_{2} \mathrm{Cl}(g) \xrightarrow{k_{2}} \mathrm{NO}_{2}(g)+\mathrm{Cl}_{2}(g)
\end{aligned}
$$

(a) What is the overall reaction?
(b) What is the molecularity of each of the elementary steps?
(c) What rate law is predicted by this mechanism if the first step is rate-determining?
12.75 The substitution reactions of molybdenum hexacarbonyl, $\mathrm{Mo}(\mathrm{CO})_{6}$, with a variety of other molecules L are believed to occur by the following mechanism:

$$
\begin{aligned}
& \mathrm{Mo}(\mathrm{CO})_{6} \xrightarrow{k_{1}} \underset{\mathrm{Mo}(\mathrm{CO})_{5}+\mathrm{CO}}{\mathrm{Mo}(\mathrm{CO})_{5}+\mathrm{L} \xrightarrow{k_{2}} \mathrm{Mo}(\mathrm{CO})_{5} \mathrm{~L}}
\end{aligned}
$$

(a) What is the overall reaction?
(b) What is the molecularity of each of the elementary steps?
(c) Write the rate law, assuming that the first step is rate-determining.
12.76 The reaction $2 \mathrm{NO}_{2}(g)+\mathrm{F}_{2}(g) \rightarrow 2 \mathrm{NO}_{2} \mathrm{~F}(g)$ has a second-order rate law, rate $=k\left[\mathrm{NO}_{2}\right]\left[\mathrm{F}_{2}\right]$. Suggest a mechanism that is consistent with this rate law.
12.77 The decomposition of ozone in the upper atmosphere is facilitated by nitric oxide. The overall reaction and the rate law are

$$
\mathrm{O}_{3}(g)+\mathrm{O}(g) \longrightarrow 2 \mathrm{O}_{2}(g) \quad \text { Rate }=k\left[\mathrm{O}_{3}\right][\mathrm{NO}]
$$

Write a mechanism that is consistent with the rate law.

## The Arrhenius Equation

12.78 Why don't all collisions between reactant molecules lead to chemical reaction?
12.79 Two reactions have the same activation energy, but their rates at the same temperature differ by a factor of 10. Explain.
12.80 Rate constants for the reaction $2 \mathrm{~N}_{2} \mathrm{O}_{5}(g) \rightarrow$ $4 \mathrm{NO}_{2}(g)+\mathrm{O}_{2}(g)$ exhibit the following temperature dependence:

| Temperature <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{k}$ <br> $\left(\mathbf{s}^{-\mathbf{1}}\right)$ | Temperature <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{k}$ <br> $(\mathbf{1} / \mathbf{s})$ |
| :--- | :--- | :--- | :--- |
| 25 | $3.7 \times 10^{-5}$ | 55 | $1.7 \times 10^{-3}$ |
| 45 | $5.1 \times 10^{-4}$ | 65 | $5.2 \times 10^{-3}$ |

Plot an appropriate graph of the data, and determine the activation energy (in $\mathrm{kJ} / \mathrm{mol}$ ) for this reaction.
12.81 The following rate constants describe the thermal decomposition of nitrogen dioxide:

$$
2 \mathrm{NO}_{2}(g) \longrightarrow 2 \mathrm{NO}(g)+\mathrm{O}_{2}(g)
$$

| Temperature <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{k}$ <br> $\left(\mathbf{M}^{-1} \mathbf{s}^{-\mathbf{1}}\right)$ | Temperature <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\boldsymbol{k}$ <br> $\left(\mathbf{M}^{\mathbf{- 1}} \mathbf{s}^{-\mathbf{1}}\right)$ |
| :--- | :--- | :--- | :--- |
| 330 | 0.77 | 378 | 4.1 |
| 354 | 1.8 | 383 | 4.7 |

Plot an appropriate graph of the data, and calculate the value of $E_{\mathrm{a}}$ for this reaction in $\mathrm{kJ} / \mathrm{mol}$.
12.82 Rate constants for the reaction $\mathrm{NO}_{2}(g)+\mathrm{CO}(g) \rightarrow$ $\mathrm{NO}(g)+\mathrm{CO}_{2}(g)$ are $1.3 \mathrm{M}^{-1} \mathrm{~s}^{-1}$ at 700 K and $23.0 \mathrm{M}^{-1} \mathrm{~s}^{-1}$ at 800 K .
(a) What is the value of the activation energy in $\mathrm{kJ} / \mathrm{mol}$ ?
(b) What is the rate constant at 750 K ?
12.83 A certain first-order reaction has a rate constant of $1.0 \times 10^{-3} \mathrm{~s}^{-1}$ at $25^{\circ} \mathrm{C}$.
(a) If the reaction rate doubles when the temperature is increased to $35^{\circ} \mathrm{C}$, what is the activation energy for this reaction in $\mathrm{kJ} / \mathrm{mol}$ ?
(b) What is the $E_{\mathrm{a}}$ (in $\mathrm{kJ} / \mathrm{mol}$ ) if the same temperature change causes the rate to triple?
12.84 Reaction of the anti-cancer drug cisplatin, $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$, with water is described by the equation

$$
\operatorname{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}(a q)+\underset{\operatorname{Pt}\left(\mathrm{NH}_{3}\right)_{2}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Cl}^{+}(a q)+\mathrm{Cl}^{-}(a q)}{\mathrm{H}_{2}(l)}
$$

The rate of this reaction increases by a factor of 15 on raising the temperature from $25^{\circ} \mathrm{C}$ to $50^{\circ} \mathrm{C}$. What is the value of the activation energy in $\mathrm{kJ} / \mathrm{mol}$ ?
12.85 The widely used solvent ethyl acetate undergoes the following reaction in basic solution:

$$
\begin{array}{r}
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{C}_{2} \mathrm{H}_{5}(\mathrm{aq})+\mathrm{OH}^{-}(a q) \longrightarrow \\
\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(\mathrm{aq})
\end{array}+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(a q)
$$

The rate of this reaction increases by a factor of 6.37 on raising the temperature from $15^{\circ} \mathrm{C}$ to $45^{\circ} \mathrm{C}$. Calculate the value of the activation energy in $\mathrm{kJ} / \mathrm{mol}$.
12.86 Values of $E_{\mathrm{a}}=183 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta E=9 \mathrm{~kJ} / \mathrm{mol}$ have been measured for the reaction

$$
2 \mathrm{HI}(g) \longrightarrow \mathrm{H}_{2}(g)+\mathrm{I}_{2}(g)
$$

Sketch a potential energy profile for this reaction that shows the potential energy of reactants, products, and the transition state. Include labels that define $E_{\mathrm{a}}$ and $\Delta E$.
12.87 Values of $E_{\mathrm{a}}=248 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta E=41 \mathrm{~kJ} / \mathrm{mol}$ have been measured for the reaction

$$
\mathrm{H}_{2}(g)+\mathrm{CO}_{2}(g) \longrightarrow \mathrm{H}_{2} \mathrm{O}(g)+\mathrm{CO}(g)
$$

(a) Sketch a potential energy profile for this reaction that shows the potential energy of reactants, products, and the transition state. Include labels that define $E_{\mathrm{a}}$ and $\Delta E$.
(b) Considering the geometry of the reactants and products, suggest a plausible structure for the transition state.

## Catalysis

12.88 Comment on the following statement: "A catalyst increases the rate of a reaction, but it is not consumed because it does not participate in the reaction."
12.89 Why doesn't a catalyst appear in the overall chemical equation for a reaction?
12.90 What effect does a catalyst have on the rate, mechanism, and activation energy of a chemical reaction?
12.91 Distinguish between a homogeneous catalyst and a heterogeneous catalyst, and give an example of each.
12.92 In the upper atmosphere, chlorofluorocarbons such as $\mathrm{CFCl}_{3}$ absorb sunlight, and subsequently fragment to Cl atoms. The Cl atoms then destroy ozone by the following mechanism:

$$
\begin{aligned}
\mathrm{Cl}(g)+\mathrm{O}_{3}(g) & \longrightarrow \mathrm{ClO}(g)+\mathrm{O}_{2}(g) \\
\mathrm{ClO}(g)+\mathrm{O}(g) & \longrightarrow \mathrm{Cl}(g)+\mathrm{O}_{2}(g)
\end{aligned}
$$

(a) Write the chemical equation for the overall reaction.
(b) What is the role of the Cl atoms in this reaction?
(c) Is ClO a catalyst or a reaction intermediate?
(d) What distinguishes a catalyst from an intermediate?
12.93 Sulfur dioxide is oxidized to sulfur trioxide in the following sequence of reactions:

$$
\begin{aligned}
2 \mathrm{SO}_{2}(g)+2 \mathrm{NO}_{2}(g) & \longrightarrow 2 \mathrm{SO}_{3}(g)+2 \mathrm{NO}(g) \\
2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) & \longrightarrow 2 \mathrm{NO}_{2}(g)
\end{aligned}
$$

(a) Write the chemical equation for the overall reaction.
(b) Identify any molecule that acts as a catalyst or intermediate in this reaction.
12.94 Consider the following mechanism for the decomposition of nitramide $\left(\mathrm{NH}_{2} \mathrm{NO}_{2}\right)$ in aqueous solution:

$$
\begin{aligned}
\mathrm{NH}_{2} \mathrm{NO}_{2}(a q)+\mathrm{OH}^{-}(a q) & \longrightarrow \mathrm{NHNO}_{2}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\
\mathrm{NHNO}_{2}^{-}(a q) & \longrightarrow \mathrm{N}_{2} \mathrm{O}(g)+\mathrm{OH}^{-}(a q)
\end{aligned}
$$

(a) Write the chemical equation for the overall reaction.
(b) Identify the catalyst and the reaction intermediate.
(c) How will the rate of the overall reaction be affected if HCl is added to the solution?
12.95 In Problem 12.77, you wrote a mechanism for the nitric oxide facilitated decomposition of ozone. Does your mechanism involve a catalyst or a reaction intermediate? Explain.

## General Problems

12.96 You wish to determine the reaction order and rate constant for the following thermal decomposition reaction:

$$
2 \mathrm{AB}_{2} \longrightarrow \mathrm{~A}_{2}+2 \mathrm{~B}_{2}
$$

(a) What data would you collect?
(b) How would you use these data to determine whether the reaction is zeroth order, first order, or second order?
(c) Describe how you would determine the value of the rate constant.
12.97 You wish to determine the activation energy for the following first-order reaction:

$$
A \longrightarrow B+C
$$

(a) What data would you collect?
(b) How would you use these data to determine the activation energy?
12.98 The rate of the reaction $\mathrm{A}+\mathrm{B}_{2} \rightarrow \mathrm{AB}+\mathrm{B}$ is directly proportional to the concentration of $B_{2}$, independent of the concentration of A , and directly proportional to the concentration of a substance C .
(a) What is the rate law?
(b) Write a mechanism that agrees with the experimental facts.
(c) What is the role of C in this reaction, and why doesn't $C$ appear in the chemical equation for the overall reaction?
12.99 Consider three reactions with different values of $E_{\mathrm{a}}$ and $\Delta E$ :

Reaction 1. $E_{\mathrm{a}}=20 \mathrm{~kJ} / \mathrm{mol} ; \Delta E=-60 \mathrm{~kJ} / \mathrm{mol}$
Reaction 2. $E_{\mathrm{a}}=10 \mathrm{~kJ} / \mathrm{mol} ; \Delta E=-20 \mathrm{~kJ} / \mathrm{mol}$
Reaction 3. $E_{\mathrm{a}}=40 \mathrm{~kJ} / \mathrm{mol} ; \Delta E=+15 \mathrm{~kJ} / \mathrm{mol}$
(a) Sketch a potential energy profile for each reaction that shows the potential energy of reactants, products, and the transition state. Include labels that define $E_{\mathrm{a}}$ and $\Delta E$.
(b) Assuming that all three reactions are carried out at the same temperature and that all three have the same frequency factor $A$, which reaction is the fastest and which is the slowest?
(c) Which reaction is the most endothermic, and which is the most exothermic?
12.100 Consider the potential energy profile in Figure 12.17a for the iodide ion-catalyzed decomposition of $\mathrm{H}_{2} \mathrm{O}_{2}$. What point on the profile represents the potential energy of the transition state for the first step in the reaction? What point represents the potential energy of the transition state for the second step? What point represents the potential energy of the intermediate products $\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{IO}^{-}(a q)$ ?
12.101 Decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ is a first-order reaction. At $25^{\circ} \mathrm{C}$, it takes 5.2 h for the concentration to drop from 0.120 M to 0.060 M . How many hours does it take for
the concentration to drop from 0.030 M to 0.015 M ? From 0.480 M to 0.015 M ?
12.102 Consider the reaction $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightarrow 2 \mathrm{HI}(g)$. The reaction of a fixed amount of $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$ is studied in a cylinder fitted with a movable piston. Indicate the effect of each of the following changes on the rate of the reaction:
(a) an increase in temperature at constant volume
(b) an increase in volume at constant temperature
(c) addition of a catalyst
(d) addition of argon (an inert gas) at constant volume
12.103 When the temperature of a gas is raised by $10^{\circ} \mathrm{C}$, the collision frequency increases by only about $2 \%$, but the reaction rate increases by $100 \%$ (factor of 2 ) or more. Explain.
12.104 The initial rates listed in the following table were measured in methanol solution for the reaction

$$
\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{Br}_{2}+3 \mathrm{I}^{-} \longrightarrow \mathrm{C}_{2} \mathrm{H}_{4}+2 \mathrm{Br}^{-}+\mathrm{I}_{3}^{-}
$$

| Experiment | Initial <br> $\left[\mathbf{C}_{\mathbf{2}} \mathbf{H}_{\mathbf{4}} \mathbf{B r}_{\mathbf{2}}\right]$ | Initial <br> $\left[\mathbf{I}^{-}\right]$ | Initial Rate <br> of Formation <br> of $\mathbf{I}_{\mathbf{3}}{ }^{-}(\mathbf{M} / \mathbf{s})$ |
| :--- | :--- | :--- | :--- |
| 1 | 0.127 | 0.102 | $6.45 \times 10^{-5}$ |
| 2 | 0.343 | 0.102 | $1.74 \times 10^{-4}$ |
| 3 | 0.203 | 0.125 | $1.26 \times 10^{-4}$ |

(a) What is the rate law?
(b) What is the value of the rate constant?
(c) What is the reaction rate when both reactant concentrations are 0.150 M ?
12.105 Concentration-time data for the conversion of $A$ and $B$ to D are listed in the following table:

|  | Time <br> Experiment | [A] | [B] | [C] | [D] |
| :--- | :---: | ---: | :--- | :--- | :--- |
| 1 | 0 | 5.00 | 2.00 | 1.00 | 0.00 |
|  | 60 | 4.80 | 1.90 | 1.00 | 0.10 |
| 2 | 0 | 10.00 | 2.00 | 1.00 | 0.00 |
|  | 60 | 9.60 | 1.80 | 1.00 | 0.20 |
| 3 | 0 | 5.00 | 4.00 | 1.00 | 0.00 |
|  | 60 | 4.80 | 3.90 | 1.00 | 0.10 |
| 4 | 0 | 5.00 | 2.00 | 2.00 | 0.00 |
|  | 60 | 4.60 | 1.80 | 2.00 | 0.20 |

(a) Write a balanced equation for the reaction.
(b) What is the reaction order with respect to A, B, and C , and what is the overall reaction order?
(c) What is the rate law?
(d) Is a catalyst involved in this reaction? Explain.
(e) Suggest a mechanism that is consistent with the data.
(f) Calculate the rate constant for the formation of D .
12.106 What fraction of the molecules in a gas at 300 K collide with an energy equal to or greater than $E_{\mathrm{a}}$ when $E_{\mathrm{a}}$ equals $50 \mathrm{~kJ} / \mathrm{mol}$ ? What is the value of this fraction when $E_{\mathrm{a}}$ is $100 \mathrm{~kJ} / \mathrm{mol}$ ?
12.107 If the rate of a reaction increases by a factor of 2.5 when the temperature is raised from $20^{\circ} \mathrm{C}$ to $30^{\circ} \mathrm{C}$, what is the value of the activation energy in $\mathrm{kJ} / \mathrm{mol}$ ? By what factor does the rate of this reaction increase when the temperature is raised from $120^{\circ} \mathrm{C}$ to $130^{\circ} \mathrm{C}$ ?
12.108 A two-step mechanism has been suggested for the reaction of nitric oxide and bromine:

$$
\begin{aligned}
& \mathrm{NO}(g)+\mathrm{Br}_{2}(g) \xrightarrow{k_{1}} \mathrm{NOBr}_{2}(g) \\
& \mathrm{NOBr}_{2}(g)+\mathrm{NO}(g) \xrightarrow{k_{2}} 2 \mathrm{NOBr}(g)
\end{aligned}
$$

(a) What is the overall reaction?
(b) What is the role of $\mathrm{NOBr}_{2}$ in this reaction?
(c) What is the predicted rate law if the first step is much slower than the second step?
(d) The observed rate law is Rate $=k\left[\mathrm{NO}^{2}\left[\mathrm{Br}_{2}\right]\right.$. What can you conclude about the rate-determining step?
12.109 Beginning with the integrated rate law, derive a general equation for the half-life of a zeroth-order reaction of the type $\mathrm{A} \rightarrow$ Products. How does the length of each half-life compare with the length of the previous one? Make the same comparison for first-order and secondorder reactions.
12.110 Consider the following mechanism for the reaction of nitric oxide and hydrogen:

$$
\begin{array}{cl}
2 \mathrm{NO}(g) \stackrel{k_{1}}{k_{-1}} \mathrm{~N}_{2} \mathrm{O}_{2}(g) & \text { Fast } \\
\mathrm{N}_{2} \mathrm{O}_{2}(g)+\mathrm{H}_{2}(g) \xrightarrow{k_{2}} \mathrm{~N}_{2} \mathrm{O}(g)+\mathrm{H}_{2} \mathrm{O}(g) & \begin{array}{l}
\text { Slow rate- } \\
\text { determining }
\end{array} \\
\mathrm{N}_{2} \mathrm{O}(g)+\mathrm{H}_{2}(g) \xrightarrow{k_{3}} \mathrm{~N}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(g) & \text { Fast }
\end{array}
$$

The first step, which is reversible, has a rate constant of $k_{1}$ for the forward reaction and $k_{-1}$ for the reverse reaction. The forward and reverse reactions in step 1 occur at the same rate, and both are fast compared with step 2 , the rate-determining step.
(a) Write an equation for the overall reaction.
(b) Identify all reaction intermediates.
(c) Write the rate law for the rate-determining step.
(d) Derive an equation for the rate of the overall reaction in terms of the concentrations of the reactants. (The concentrations of intermediates should not appear in the rate law for the overall reaction.)
12.111 Consider the following concentration-time data for the reaction of iodide ion and hypochlorite ion $\left(\mathrm{OCl}^{-}\right)$. The products are chloride ion and hypoiodite ion $\left(\mathrm{OI}^{-}\right)$.

| Experiment | Time (s) | $\left[\mathbf{I}^{-}\right]$ | $\left[\mathbf{O C l}^{-}\right]$ | $\left.\mathbf{[ O H}^{-}\right]$ |
| :--- | :---: | :--- | :--- | :--- |
| 1 | 0 | $2.40 \times 10^{-4}$ | $1.60 \times 10^{-4}$ | 1.00 |
|  | 10 | $2.17 \times 10^{-4}$ | $1.37 \times 10^{-4}$ | 1.00 |
| 2 | 0 | $1.20 \times 10^{-4}$ | $1.60 \times 10^{-4}$ | 1.00 |
|  | 10 | $1.08 \times 10^{-4}$ | $1.48 \times 10^{-4}$ | 1.00 |
| 3 | 0 | $2.40 \times 10^{-4}$ | $4.00 \times 10^{-5}$ | 1.00 |
|  | 10 | $2.34 \times 10^{-4}$ | $3.40 \times 10^{-5}$ | 1.00 |
| 4 | 0 | $1.20 \times 10^{-4}$ | $1.60 \times 10^{-4}$ | 2.00 |
|  | 10 | $1.14 \times 10^{-4}$ | $1.54 \times 10^{-4}$ | 2.00 |

(a) Write a balanced equation for the reaction.
(b) Determine the rate law, and calculate the value of the rate constant.
(c) Does the reaction occur by a single-step mechanism? Explain.
(d) Propose a mechanism that is consistent with the rate law, and express the rate constant in terms of the rate constants for the elementary steps in your mechanism. (Hint: Transfer of an $\mathrm{H}^{+}$ion between $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{OCl}^{-}$is a rapid reversible reaction.)
12.112 Consider the reversible, first-order interconversion of two molecules A and B:

$$
\mathrm{A} \underset{k_{\mathrm{r}}}{\stackrel{k_{\mathrm{f}}}{\rightleftharpoons}} \mathrm{~B}
$$

where $k_{\mathrm{f}}=3.0 \times 10^{-3} \mathrm{~s}^{-1}$ is the rate constant for the forward reaction and $k_{\mathrm{r}}=1.0 \times 10^{-3} \mathrm{~s}^{-1}$ is the rate constant for the reverse reaction. We'll see in the next chapter that a reaction does not go to completion, but instead reaches a state of equilibrium with comparable concentrations of reactants and products if the rate constants $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ have comparable values.
(a) What are the rate laws for the forward and reverse reactions?
(b) Draw a qualitative graph that shows how the rates of the forward and reverse reactions vary with time.
(c) What are the relative concentrations of B and A when the rates of the forward and reverse reactions become equal?
12.113 Radioactive decay exhibits a first-order rate law, rate $=-\Delta N / \Delta t=k N$, where $N$ denotes the number of radioactive nuclei present at time $t$. The half-life of stron-tium-90, a dangerous nuclear fission product, is 29 years.
(a) What fraction of the strontium-90 remains after three half-lives?
(b) What is the value of the rate constant for the decay of strontium-90?
(c) How many years are required for $99 \%$ of the stron-tium- 90 to disappear?
12.114 The age of any remains from a once-living organism can be determined by radiocarbon dating, a procedure that works by determining the concentration of radioactive ${ }^{14} \mathrm{C}$ in the remains. All living organisms contain an equilibrium concentration of radioactive ${ }^{14} \mathrm{C}$ that gives rise to an average of 15.3 nuclear decay events per minute per gram of carbon. At death, however, no additional ${ }^{14} \mathrm{C}$ is taken in, so the concentration slowly drops as radioactive decay occurs. What is the age of a bone fragment from an archaeological dig if the bone shows an average of 2.3 radioactive events per minute per gram of carbon? Radioactive decay is kinetically a first-order process, and $t_{1 / 2}$ for ${ }^{14} \mathrm{C}$ is 5730 years.
12.115 The gas-phase decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$ is a first-order reaction:

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \longrightarrow 2 \mathrm{NO}_{2}(g)
$$

Use the following data to calculate the activation energy $E_{\mathrm{a}}$ in $\mathrm{kJ} / \mathrm{mol}$.

| Experiment | Temperature <br> $\left({ }^{\circ} \mathbf{C}\right)$ | Initial <br> $\left[\mathbf{N}_{\mathbf{2}} \mathbf{O}_{\mathbf{4}}\right]$ | Initial Rate of <br> Decomposition <br> of $\mathbf{N}_{\mathbf{2}} \mathbf{O}_{\mathbf{4}}(\mathbf{M} / \mathbf{s})$ |
| :--- | :--- | :--- | :--- |
| 1 | 25 |  |  |
| 2 | 40 | 0.10 | $5.0 \times 10^{3}$ |

12.116 In the laboratory, you are studying the first-order conversion of a reactant $X$ to products in a reaction vessel with a constant volume of 1.000 L . At 1:00 p.m., you start the reaction at $25^{\circ} \mathrm{C}$ with 1.000 mol of X . At $2: 00$ p.m., you find that 0.600 mol of X remains, and you immediately increase the temperature of the reaction mixture to $35^{\circ} \mathrm{C}$. At 3:00 p.m., you discover that 0.200 mol of X is still present. You want to finish the reaction by $4: 00 \mathrm{p} . \mathrm{m}$. but need to continue it until only 0.010 mol of X remains, so you decide to increase the temperature once again. What is the minimum temperature required to convert all but 0.010 mol of X to products by 4:00 p.m.?
12.117 The half-life for the first-order decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$ is $1.3 \times 10^{-5} \mathrm{~s}$.

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \longrightarrow 2 \mathrm{NO}_{2}(g)
$$

If $\mathrm{N}_{2} \mathrm{O}_{4}$ is introduced into an evacuated flask at a pressure of 17.0 mm Hg , how many seconds are required for the pressure of $\mathrm{NO}_{2}$ to reach 1.3 mm Hg ?
12.118 Some reactions are so rapid that they are "diffusioncontrolled"; that is, the reactants react as quickly as they can collide. An example is the neutralization of $\mathrm{H}_{3} \mathrm{O}^{+}$by $\mathrm{OH}^{-}$, which has a second-order rate constant of $1.3 \times 10^{11} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ at $25^{\circ} \mathrm{C}$.
(a) If equal volumes of 2.0 M HCl and 2.0 M NaOH are mixed instantaneously, how much time is required for $99.999 \%$ of the acid to be neutralized?
(b) Under normal laboratory conditions, would you expect the rate of the acid-base neutralization to be limited by the rate of the reaction or by the speed of mixing?
12.119 The reaction $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{NO}_{2}(g)$ has the third-order rate law: Rate $=k\left[\mathrm{NO}^{2}\left[\mathrm{O}_{2}\right]\right.$, where $k=25 \mathrm{M}^{-2} \mathrm{~s}^{-1}$. Under the condition that $[\mathrm{NO}]=2\left[\mathrm{O}_{2}\right]$, the integrated rate law is

$$
\frac{1}{\left[\mathrm{O}_{2}\right]^{2}}=8 k t+\frac{1}{\left(\left[\mathrm{O}_{2}\right]_{0}\right)^{2}}
$$

What are the concentrations of $\mathrm{NO}, \mathrm{O}_{2}$, and $\mathrm{NO}_{2}$ after 100.0 s if the initial concentrations are $[\mathrm{NO}]=0.0200 \mathrm{M}$ and $\left[\mathrm{O}_{2}\right]=0.0100 \mathrm{M}$ ?
12.120 Consider the following data for the gas-phase decomposition of $\mathrm{NO}_{2}$ :

$$
2 \mathrm{NO}_{2}(g) \longrightarrow 2 \mathrm{NO}(g)+\mathrm{O}_{2}(g)
$$

| Temperature <br> (K) | Initial $\left[\mathbf{N O}_{\mathbf{2}}\right]$ | Initial Rate of <br> Decomposition <br> of $\mathbf{N O}_{\mathbf{2}}(\mathbf{M} / \mathbf{s})$ |
| :--- | :--- | :--- |
|  | 0.0010 | $5.4 \times 10^{-7}$ |
| 600 | 0.0020 | $2.2 \times 10^{-6}$ |
| 600 | 0.0020 | $5.2 \times 10^{-5}$ |
| 700 |  |  |

If 0.0050 mol of $\mathrm{NO}_{2}$ is introduced into a 1.0 L flask and allowed to decompose at 650 K , how many seconds does it take for the $\mathrm{NO}_{2}$ concentration to drop to 0.0010 M ?
12.121 Use the following initial rate data to determine the activation energy (in $\mathrm{kJ} / \mathrm{mol}$ ) for the reaction $\mathrm{A}+\mathrm{B} \rightarrow \mathrm{C}$ :

| Experiment | Temperature <br> $\mathbf{( K )}$ | Initial <br> [A] | Initial <br> $[\mathbf{B}]$ | Initial Rate of <br> Formation of $\mathbf{C} \mathbf{( M / s )}$ |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 700 | 0.20 | 0.10 | $1.8 \times 10^{-5}$ |
| 2 | 700 | 0.40 | 0.10 | $3.6 \times 10^{-5}$ |
| 3 | 700 | 0.10 | 0.20 | $3.6 \times 10^{-5}$ |
| 4 | 600 | 0.50 | 0.50 | $4.3 \times 10^{-5}$ |

12.122 The reaction $\mathrm{A} \rightarrow \mathrm{C}$ is first-order in the reactant A and is known to go to completion. The product C is colored and absorbs light strongly at 550 nm , while the reactant and intermediates are colorless. A solution of A was prepared, and the absorbance of $C$ at 550 nm was measured as a function of time. (Note that the absorbance of C is directly proportional to its concentration.) Use the following data to determine the half-life of the reaction:

| Time (s) | Absorbance |
| :---: | :--- |
| 0 | 0.000 |
| 10 | 0.444 |
| 20 | 0.724 |
| 100 | 1.188 |
| 200 | 1.200 |
| 500 | 1.200 |

12.123 The following experimental data were obtained in a study of the reaction $2 \mathrm{HI}(g) \rightarrow \mathrm{H}_{2}(g)+\mathrm{I}_{2}(g)$. Predict the concentration of HI that would give a rate of $1.0 \times 10^{-5} \mathrm{M} / \mathrm{s}$ at 650 K .

| Experiment | Temperature <br> $(\mathbf{K})$ | Initial <br> [HI] | Initial Rate <br> $(\mathbf{M} / \mathbf{s})$ |
| :--- | :--- | :--- | :--- |
| 1 | 700 | 0.10 | $1.8 \times 10^{-5}$ |
| 2 | 700 | 0.30 | $1.6 \times 10^{-4}$ |
| 3 | 800 | 0.20 | $3.9 \times 10^{-3}$ |
| 4 | 650 | $?$ | $1.0 \times 10^{-5}$ |

12.124 A proposed nuclear theory suggests that the relative abundances of the uranium isotopes ${ }^{235} \mathrm{U}$ and ${ }^{238} \mathrm{U}$ were approximately equal at the time they were formed. Today, the observed ratio of these isotopes ${ }^{235} \mathrm{U} /{ }^{238} \mathrm{U}$ is $7.25 \times 10^{-3}$. Given that the half-lives for radioactive decay are $7.1 \times 10^{8} \mathrm{y}$ for ${ }^{235} \mathrm{U}$ and $4.51 \times 10^{9} \mathrm{y}$ for ${ }^{238} \mathrm{U}$, calculate the age of the elements.

## Multi-Concept Problems

12.125 Values of $E_{\mathrm{a}}=6.3 \mathrm{~kJ} / \mathrm{mol}$ and $A=6.0 \times 10^{8} /(\mathrm{M} \cdot \mathrm{s})$ have been measured for the bimolecular reaction:

$$
\mathrm{NO}(g)+\mathrm{F}_{2}(g) \longrightarrow \mathrm{NOF}(g)+\mathrm{F}(g)
$$

(a) Calculate the rate constant at $25^{\circ} \mathrm{C}$.
(b) The product of the reaction is nitrosyl fluoride. Its formula is usually written as NOF, but its structure is actually ONF. Is the ONF molecule linear or bent?
(c) Draw a plausible transition state for the reaction. Use dashed lines to indicate the atoms that are weakly linked together in the transition state.
(d) Why does the reaction have such a low activation energy?
12.126 A 1.50 L sample of gaseous HI having a density of $0.0101 \mathrm{~g} / \mathrm{cm}^{3}$ is heated at $410^{\circ} \mathrm{C}$. As time passes, the HI decomposes to gaseous $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$. The rate law is $-\Delta[\mathrm{HI}] / \Delta t=k[\mathrm{HI}]^{2}$, where $k=0.031 /(\mathrm{M} \cdot \mathrm{min})$ at $410^{\circ} \mathrm{C}$.
(a) What is the initial rate of production of $\mathrm{I}_{2}$ in molecules/min?
(b) What is the partial pressure of $\mathrm{H}_{2}$ after a reaction time of 8.00 h ?
12.127 The rate constant for the decomposition of gaseous $\mathrm{NO}_{2}$ to NO and $\mathrm{O}_{2}$ is $4.7 /(\mathrm{M} \cdot \mathrm{s})$ at $383^{\circ} \mathrm{C}$. Consider the decomposition of a sample of pure $\mathrm{NO}_{2}$ having an initial pressure of 746 mm Hg in a 5.00 L reaction vessel at $383^{\circ} \mathrm{C}$.
(a) What is the order of the reaction?
(b) What is the initial rate of formation of $\mathrm{O}_{2}$ in $\mathrm{g} /(\mathrm{L} \cdot \mathrm{s})$ ?
(c) What is the mass of $\mathrm{O}_{2}$ in the vessel after a reaction time of 1.00 min ?
12.128 The rate constant for the first-order decomposition of gaseous $\mathrm{N}_{2} \mathrm{O}_{5}$ to $\mathrm{NO}_{2}$ and $\mathrm{O}_{2}$ is $1.7 \times 10^{-3} \mathrm{~s}^{-1}$ at $55^{\circ} \mathrm{C}$.
(a) If 2.70 g of gaseous $\mathrm{N}_{2} \mathrm{O}_{5}$ is introduced into an evacuated 2.00 L container maintained at a constant temperature of $55^{\circ} \mathrm{C}$, what is the total pressure in the container after a reaction time of 13.0 minutes?
(b) Use the data in Appendix B to calculate the initial rate at which the reaction mixture absorbs heat (in $\mathrm{J} / \mathrm{s}$ ). You may assume that the heat of the reaction is independent of temperature.
(c) What is the total amount of heat absorbed (in kilojoules) after a reaction time of 10.0 min ?
12.129 For the thermal decomposition of nitrous oxide, $2 \mathrm{~N}_{2} \mathrm{O}(g) \rightarrow 2 \mathrm{~N}_{2}(g)+\mathrm{O}_{2}(g)$, values of the parameters in the Arrhenius equation are $A=4.2 \times 10^{9} \mathrm{~s}^{-1}$ and $E_{\mathrm{a}}=222 \mathrm{~kJ} / \mathrm{mol}$. If a stream of $\mathrm{N}_{2} \mathrm{O}$ is passed through a tube 25 mm in diameter and 20 cm long at a flow rate of $0.75 \mathrm{~L} / \mathrm{min}$, at what temperature should the tube be maintained to have a partial pressure of 1.0 mm of $\mathrm{O}_{2}$ in the exit gas? Assume that the total pressure of the gas in the tube is 1.50 atm .
12.130 A 0.500 L reaction vessel equipped with a movable piston is filled completely with a $3.00 \%$ aqueous solution of hydrogen peroxide. The $\mathrm{H}_{2} \mathrm{O}_{2}$ decomposes to water and $\mathrm{O}_{2}$ gas in a first-order reaction that has a half-life of 10.7 h . As the reaction proceeds, the gas formed pushes the piston against a constant external atmospheric pressure of 738 mm Hg . Calculate the $P V$ work done (in joules) after a reaction time of 4.02 h . (You may assume that the density of the solution is $1.00 \mathrm{~g} / \mathrm{mL}$ and that the temperature of the system is maintained at $20^{\circ} \mathrm{C}$.)
12.131 At 791 K and relatively low pressures, the gas-phase decomposition of acetaldehyde $\left(\mathrm{CH}_{3} \mathrm{CHO}\right)$ is second order in acetaldehyde.

$$
\mathrm{CH}_{3} \mathrm{CHO}(g) \longrightarrow \mathrm{CH}_{4}(g)+\mathrm{CO}(g)
$$

The total pressure of a particular reaction mixture was found to vary as follows:

| Time (s) | 0 | 75 | 148 | 308 | 605 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Total pressure <br> (atm) | 0.500 | 0.583 | 0.641 | 0.724 | 0.808 |

(a) Use the pressure data to determine the value of the rate constant in units of $\mathrm{atm}^{-1} \mathrm{~s}^{-1}$.
(b) What is the rate constant in the usual units of $\mathrm{M}^{-1} \mathrm{~s}^{-1}$ ?
(c) If the volume of the reaction mixture is 1.00 L , what is the total amount of heat liberated (in joules) after a reaction time of 605 s ?

## eMedia Problems

12.132 Observe the Rate of Decomposition of $\mathrm{N}_{2} \mathrm{O}_{5}$ activity (eChapter 12.1). Determine the concentrations of all species present at 100 s and 500 s . How does the rate of appearance of $\mathrm{NO}_{2}$ compare to that of $\mathrm{O}_{2}$ ? What determines the rate of appearance of $\mathrm{NO}_{2}$ and $\mathrm{O}_{2}$ ? If you were able to carry out the reaction by starting with equal concentrations of $\mathrm{N}_{2} \mathrm{O}_{5}$ and $\mathrm{O}_{2}$, would it change the relative rates of appearance of $\mathrm{NO}_{2}$ and $\mathrm{O}_{2}$ ? Explain.
12.133 Use the Rates of Reaction simulation (eChapter 12.2) to determine the order of the $\mathrm{A} \rightarrow \mathrm{B}$ reaction at $0^{\circ} \mathrm{C}$. How does increasing the temperature to $10^{\circ} \mathrm{C}$ change the rate? How does it change the order? What part of the rate law must change when temperature changes?
12.134 Use the Rates of Reaction simulation (eChapter 12.2) to determine the value of the rate constant for the process at $0^{\circ} \mathrm{C}$. Calculate the half-life for the process from the value of $k$. Select a value for initial concentration and run the reaction. Determine the half-life using the [A] vs Time graph. How does doubling the initial concentration affect the half-life?
12.135 Look at the interactive graph of [A] vs Time for a second-order decomposition in eChapter 12.6. At what time would $[\mathrm{A}]=[\mathrm{A}]_{0} / 2$ if the original box contained 24 particles? Draw a similar graph, with pictures inserted at the appropriate concentrations, for a decay starting with 24 particles.
12.136 Assume each of the following are bimolecular reactions. Represent each reaction as was done in Question 1, eChapter 12.7 including the reactants, transition state, and products.
(a) $\mathrm{A}_{2}+\mathrm{B}_{2} \longrightarrow 2 \mathrm{AB}$
(b) $A+B_{2} \longrightarrow A B_{2}$
(c) $\mathrm{A}_{2}+\mathrm{B}_{2} \longrightarrow \mathrm{AB}_{2}+\mathrm{A}$
(d) $\mathrm{AB}+\mathrm{C} \longrightarrow \mathrm{AC}+\mathrm{B}$
12.137 (a) Using the Rates of Reaction simulation (eChapter 12.2), select an activation energy and determine the rate constant for the reaction at $0^{\circ} \mathrm{C}$.
(b) With the Arrhenius equation and your answer from part (a), determine what the rate constant will be at $30^{\circ} \mathrm{C}$ and at $50^{\circ} \mathrm{C}$. Verify your answers with the simulation.
(c) Based on your results, by approximately how much must the temperature increase for the rate of reaction to increase by a factor of 10 ?

## Chapter

## Chemical Equilibrium

At the beginning of Chapter 12, we raised three key questions about chemical reactions:
What happens? How fast does it happen? To what extent does it happen? The answer to the first question is given by the stoichiometry of the balanced chemical equation, and the answer to the second question is given by the kinetics of the reaction. In this chapter, we'll look at the answer to the third question: How far does a reaction proceed


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In the environment, water is involved in a dynamic equilibrium. The amount of surface water and atmospheric water vapor is roughly constant because evaporation and rain occur at the same rates on a global level.

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13.3 The Equilibrium Constant $K_{p}$
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13.11 The Link Between Chemical Equilibrium and Chemical Kinetics

- Interlude-Breathing and Oxygen Transport

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toward completion before it reaches a state of chemical equilibrium-a state in which the concentrations of reactants and products no longer change?

## - chemical equilibrium The state reached when the concentrations of reactants and products remain constant over time

We're already familiar with the concept of equilibrium from our study of the evaporation of liquids (Section 10.5). When a liquid evaporates in a closed container, it soon gives rise to a constant vapor pressure because of a dynamic equilibrium in which the number of molecules leaving the liquid equals the number returning from the vapor. Chemical reactions behave similarly. They can occur in both forward and reverse directions, and when the rates of the forward and reverse reactions become equal, the concentrations of reactants and products remain constant.

Chemical equilibria are important in numerous biological and environmental processes. For example, equilibria involving $\mathrm{O}_{2}$ molecules and the protein hemoglobin play a crucial role in the transport and delivery of oxygen from our lungs to our muscles. Similar equilibria involving CO molecules and hemoglobin account for the toxicity of carbon monoxide.

A mixture of reactants and products in the equilibrium state is called an equilibrium mixture. In this chapter, we'll address a number of important questions about the composition of equilibrium mixtures: What is the relationship between the concentrations of reactants and products in an equilibrium mixture? How can we determine equilibrium concentrations from initial concentrations? What factors can be exploited to alter the composition of an equilibrium mixture? This last question is particularly important when choosing conditions for the synthesis of industrial chemicals such as hydrogen, ammonia, and lime $(\mathrm{CaO})$.

## 13.1 | The Equilibrium State

In previous chapters, we've generally assumed that chemical reactions result in complete conversion of reactants to products. Many reactions, however, do not go to completion. Take, for example, the decomposition of the colorless gas dinitrogen tetroxide $\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$ to the dark brown gas nitrogen dioxide $\left(\mathrm{NO}_{2}\right)$.


Figure 13.1 shows the results of two experiments at $25^{\circ} \mathrm{C}$ that illustrate the interconversion of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$. In the first experiment (Figure 13.1a), 0.0400 mol of $\mathrm{N}_{2} \mathrm{O}_{4}$ is placed in a 1.000 L flask to give an initial $\mathrm{N}_{2} \mathrm{O}_{4}$ concentration of 0.0400 M . The formation of $\mathrm{NO}_{2}$ is indicated by the appearance of a brown color, and its concentration can be monitored by measuring the intensity of the color. According to the balanced equation, 2.0 mol of $\mathrm{NO}_{2}$ forms for each mole of $\mathrm{N}_{2} \mathrm{O}_{4}$ that disappears, so the concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ at any time equals the initial concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ minus half the concentration of $\mathrm{NO}_{2}$. As time passes, the concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ decreases and the concentration of $\mathrm{NO}_{2}$ increases until both concentrations level off at constant, equilibrium values: $\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]=0.0337 \mathrm{M}$; $\left[\mathrm{NO}_{2}\right]=0.0125 \mathrm{M}$.


4 FIGURE 13.1 Change in the concentrations of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ with time in two experiments at $25^{\circ} \mathrm{C}$ : (a) Only $\mathrm{N}_{2} \mathrm{O}_{4}$ is present initially; (b) only $\mathrm{NO}_{2}$ is present initially. In experiment (a), $\left[\mathrm{NO}_{2}\right]$ increases as $\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]$ decreases. In experiment (b), $\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]$ increases as $\left[\mathrm{NO}_{2}\right]$ decreases. In both experiments, a state of chemical equilibrium is reached when the concentrations level off at constant values: $\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]=0.0337 \mathrm{M} ;\left[\mathrm{NO}_{2}\right]=0.0125 \mathrm{M}$.

In the second experiment, shown in Figure 13.1b, we begin with $\mathrm{NO}_{2}$, rather than $\mathrm{N}_{2} \mathrm{O}_{4}$, at a concentration of 0.0800 M . The conversion of $\mathrm{NO}_{2}$ to $\mathrm{N}_{2} \mathrm{O}_{4}$ proceeds until the concentrations level off at the same values as obtained in the first experiment. Taken together, the two experiments demonstrate that the interconversion of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ is reversible and that the same equilibrium state is reached starting from either substance.

$$
\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g}) \rightleftharpoons 2 \mathrm{NO}_{2}(\mathrm{~g}) \quad \text { Reaction occurs in both directions }
$$

To indicate that the reaction can proceed in both forward and reverse directions, we write the balanced equation with two arrows, one pointing from reactants to products and the other pointing from products to reactants. (The terms "reactants" and "products" could be confusing in this context because the products of the forward reaction are reactants in the reverse reaction. To avoid confusion, we'll restrict the term reactants to the substances on the left side of the chemical equation and the term products to the substances on the right side of the equation.)

Strictly speaking, all chemical reactions are reversible. What we sometimes call irreversible reactions are simply those that proceed nearly to completion, so that the equilibrium mixture contains almost all products and almost no reactants. For such reactions, the reverse reaction is often too slow to be detected.

Why do the reactions of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ appear to stop after the concentrations reach their equilibrium values? We'll explore that question in more detail in Section 13.11, but note for now that the concentrations reach constant values, not because the reactions stop, but because the rates of the forward and reverse reactions become equal. Take, for example, the experiment in which $\mathrm{N}_{2} \mathrm{O}_{4}$ is converted to an equilibrium mixture of $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$. Because reaction rates depend on concentrations (Section 12.2), the rate of the forward reaction $\left(\mathrm{N}_{2} \mathrm{O}_{4} \rightarrow 2 \mathrm{NO}_{2}\right)$ decreases as the concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ decreases, while the rate of the reverse reaction ( $\mathrm{N}_{2} \mathrm{O}_{4} \leftarrow 2 \mathrm{NO}_{2}$ ) increases as the concentration of $\mathrm{NO}_{2}$ increases. Eventually, the decreasing rate of the forward reaction and the increasing rate of the


Lee R. Summerlin and James L. Ealy, Jr., "Equilibrium in the Gas Phase," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), pp. 60-61. Reddish-brown nitrogen dioxide is produced and placed in two test tubes where it exists in equilibrium with colorless dinitrogen tetroxide. One test tube is placed in a boiling water bath, causing an increase in the intensity of the color due to an increase in the amount of $\mathrm{NO}_{2}$. The second test tube is placed in an icewater bath, which causes the gaseous mixture to become almost colorless due to a decrease in the amount of $\mathrm{NO}_{2}$. When returned to room temperature, the gaseous mixtures in both test tubes exhibit the same brown color. Pressure and temperature effects on the equilibrium are related to the stoichiometry and enthalpy of the reaction.


A If the rate at which people move from the first floor to the second equals the rate at which people move from the second floor to the first, the number of people on each floor remains constant, and the two populations are in dynamic equilibrium.
reverse reaction become equal. At that point, there are no further changes in concentrations because $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ both disappear as fast as they're formed. Thus, chemical equilibrium is a dynamic state in which forward and reverse reactions continue at equal rates so that there is no net conversion of reactants to products (Figure 13.2).
re


A FIGURE 13.2 Rates of the forward and reverse reactions for the decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$ to $\mathrm{NO}_{2}$. As $\mathrm{N}_{2} \mathrm{O}_{4}$ is consumed, the rate of the forward reaction decreases; as $\mathrm{NO}_{2}$ is formed, the rate of the reverse reaction increases. When the two rates become equal, an equilibrium state is attained and there are no further changes in concentrations.

### 13.2 The Equilibrium Constant $K_{c}$

Table 13.1 lists concentration data for the experiments in Figure 13.1 along with data for three additional experiments. In experiments 1 and 2, the equilibrium mixtures have identical compositions because the initial concentration of $\mathrm{N}_{2} \mathrm{O}_{4}$ in experiment 1 is half the initial concentration of $\mathrm{NO}_{2}$ in experiment 2 (that is, the total number of N and O atoms is the same in both experiments). In experiments $3-5$, different initial concentrations of $\mathrm{N}_{2} \mathrm{O}_{4}$ and/ or $\mathrm{NO}_{2}$ give different equilibrium concentrations. In all the experiments, however, the equilibrium concentrations are related. The last column of Table 13.1 shows that, at equilibrium, the expression $\left[\mathrm{NO}_{2}\right]^{2} /\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]$ has a constant value of approximately $4.64 \times 10^{-3} \mathrm{M}$.

The expression $\left[\mathrm{NO}_{2}\right]^{2} /\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]$ appears to be related to the balanced equation for the reaction, $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$. That is, the concentration of the product is

TABLE 13.1 Concentration Data at $25^{\circ} \mathrm{C}$ for the Reaction $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$

| Experiment Number | Initial <br> Concentrations (M) |  | Equilibrium Concentrations (M) |  | Equilibrium Constant Expression |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\left[\mathbf{N}_{2} \mathrm{O}_{4}\right]$ | [ $\mathrm{NO}_{2}$ ] | $\left[\mathbf{N}_{2} \mathrm{O}_{4}\right.$ ] | [ $\mathbf{N O}_{2}$ ] | $\left[\mathbf{N O}_{\mathbf{2}}\right]^{\mathbf{2}} /\left[\mathbf{N}_{\mathbf{2}} \mathbf{O}_{\mathbf{4}}\right]$ |
| 1 | 0.0400 | 0.0000 | 0.0337 | 0.0125 | $4.64 \times 10^{-3}$ |
| 2 | 0.0000 | 0.0800 | 0.0337 | 0.0125 | $4.64 \times 10^{-3}$ |
| 3 | 0.0600 | 0.0000 | 0.0522 | 0.0156 | $4.66 \times 10^{-3}$ |
| 4 | 0.0000 | 0.0600 | 0.0246 | 0.0107 | $4.65 \times 10^{-3}$ |
| 5 | 0.0200 | 0.0600 | 0.0429 | 0.0141 | $4.63 \times 10^{-3}$ |

in the numerator, raised to the power of its coefficient in the balanced equation, and the concentration of the reactant is in the denominator. Is there an analogous expression with a constant value for every chemical reaction? If so, how is the form of that expression related to the balanced equation for the reaction?

To answer those questions, let's consider a general reversible reaction:

$$
a \mathrm{~A}+b \mathrm{~B} \rightleftharpoons c \mathrm{C}+d \mathrm{D}
$$

where A and B are the reactants, C and D are the products, and $a, b, c$, and $d$ are stoichiometric coefficients in the balanced chemical equation. On the basis of experimental studies of many reversible reactions, the Norwegian chemists Cato Maximilian Guldberg and Peter Waage proposed in 1864 that the concentrations in an equilibrium mixture are related by the following equilibrium equation, where $K_{c}$ is the equilibrium constant and the expression on the right side is called the equilibrium constant expression.

Equilibrium equation: $\quad K_{\mathrm{c}}=\frac{[\mathrm{C}]^{c}[\mathrm{D}]^{d}}{[\mathrm{~A}]^{a}[\mathrm{~B}]^{b}} \longleftarrow$ Products


As usual, square brackets indicate the molar concentration of the substance within the brackets (hence the subscript c for "concentration" in $K_{c}$ ). The substances in the equilibrium constant expression may be gases or molecules and ions in solutions. The equilibrium equation is also known as the law of mass action because in the early days of chemistry, concentration was called "active mass."

The equilibrium constant $K_{c}$ is the number obtained by multiplying the equilibrium concentrations of all the products and dividing by the product of the equilibrium concentrations of all the reactants, with the concentration of each substance raised to the power of its coefficient in the balanced chemical equation. No matter what the individual equilibrium concentrations may be in a particular experiment, the equilibrium constant for a reaction at a particular temperature always has the same value. Thus, the equilibrium equation for the decomposition reaction of $\mathrm{N}_{2} \mathrm{O}_{4}$ to give $2 \mathrm{NO}_{2}$ is

$$
K_{\mathrm{c}}=\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{~N}_{2} \mathrm{O}_{4}\right]}=4.64 \times 10^{-3} \quad \text { at } 25^{\circ} \mathrm{C}
$$

where the equilibrium constant expression is $\left[\mathrm{NO}_{2}\right]^{2} /\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]$ and the equilibrium constant $K_{c}$ has a value of $4.64 \times 10^{-3}$ at $25^{\circ} \mathrm{C}$ (Table 13.1).

Values of $K_{c}$ are generally reported without units because the concentrations in the equilibrium constant expression are considered to be concentration ratios in which the molarity of each substance is divided by its molarity ( 1 M ) in the thermodynamic standard state (Section 8.6). Because the units cancel, the concentration ratios and the values of $K_{c}$ are dimensionless. For experiment 1 in Table 13.1, for example,

$$
K_{\mathrm{c}}=\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{~N}_{2} \mathrm{O}_{4}\right]}=\frac{\left(\frac{0.0125 \mathrm{M}}{1 \mathrm{M}}\right)^{2}}{\left(\frac{0.0337 \mathrm{M}}{1 \mathrm{M}}\right)}=4.64 \times 10^{-3} \quad \text { at } 25^{\circ} \mathrm{C}
$$

Equilibrium constants are temperature-dependent, so the temperature must be given when citing a value of $K_{c}$. For example, $K_{c}$ for the decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$ increases from $4.64 \times 10^{-3}$ at $25^{\circ} \mathrm{C}$ to 1.53 at $127^{\circ} \mathrm{C}$.

The form of the equilibrium constant expression and the numerical value of the equilibrium constant depend on the form of the balanced chemical equation.

Both the equilibrium equation and the value of the equilibrium constant depend on how the chemical equation is written and balanced.

Equilibrium Constant activity

Consider again the chemical equation and the equilibrium equation for a general reaction:

$$
a \mathrm{~A}+b \mathrm{~B} \rightleftharpoons c \mathrm{C}+d \mathrm{D} \quad K_{\mathrm{c}}=\frac{[\mathrm{C}]^{c}[\mathrm{D}]^{d}}{[\mathrm{~A}]^{a}[\mathrm{~B}]^{b}}
$$

If we write the chemical equation in the reverse direction, the new equilibrium constant expression is the reciprocal of the original expression, and the new equilibrium constant $K_{\mathrm{c}}{ }^{\prime}$ is the reciprocal of the original equilibrium constant $K_{\mathrm{c}}$ :

$$
c \mathrm{C}+d \mathrm{D} \rightleftharpoons a \mathrm{~A}+b \mathrm{~B} \quad K_{\mathrm{c}}^{\prime}=\frac{[\mathrm{A}]^{a}[\mathrm{~B}]^{b}}{[\mathrm{C}]^{c}[\mathrm{D}]^{d}}=\frac{1}{K_{\mathrm{c}}}
$$

(The prime distinguishes $K_{c}{ }^{\prime}$ from $K_{\mathrm{c}}$.) Because the equilibrium constants $K_{\mathrm{c}}$ and $K_{c}{ }^{\prime}$ have different numerical values, it's important to specify the form of the balanced chemical equation when quoting the value of an equilibrium constant.

## Worked Example 13.1

Write the equilibrium equation for each of the following reactions:
(a) $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$
(b) $2 \mathrm{NH}_{3}(g) \rightleftharpoons \mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g)$

## Strategy

Put the concentration of the reaction products in the numerator of the equilibrium constant expression and the concentrations of the reactants in the denominator. Then raise the concentration of each substance to the power of its coefficient in the balanced chemical equation.

## SOlUTION

(a) $K_{\mathrm{c}}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}$ Coefficient of $\mathrm{H}_{2}$
(b) $K_{\mathrm{c}}{ }^{\prime}=\frac{\left[\mathrm{N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}{\left[\mathrm{NH}_{3}\right]^{2}} \quad K_{\mathrm{c}}{ }^{\prime}=\frac{1}{K_{\mathrm{c}}}$

Because the balanced equation in part (b) is the reverse of that in part (a), the equilibrium constant expression in part (b) is the reciprocal of the expression in part (a) and the equilibrium constant $K_{c}{ }^{\prime}$ is the reciprocal of $K_{c}$.

## Worked Example 13.2

The following concentrations were measured for an equilibrium mixture at 500 K : $\left[\mathrm{N}_{2}\right]=3.0 \times 10^{-2} \mathrm{M} ;\left[\mathrm{H}_{2}\right]=3.7 \times 10^{-2} \mathrm{M} ;\left[\mathrm{NH}_{3}\right]=1.6 \times 10^{-2} \mathrm{M}$. Calculate the equilibrium constant at 500 K for each of the reactions in Worked Example 13.1.

## Strategy

To calculate the value of the equilibrium constant, $K_{c}$, substitute the equilibrium concentrations into the equilibrium equation.

## Solution

(a) $K_{c}=\frac{\left[\mathrm{NH}_{3}\right]^{2}}{\left[\mathrm{~N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}=\frac{\left(1.6 \times 10^{-2}\right)^{2}}{\left(3.0 \times 10^{-2}\right)\left(3.7 \times 10^{-2}\right)^{3}}=1.7 \times 10^{2}$
(b) $K_{\mathrm{c}}{ }^{\prime}=\frac{\left[\mathrm{N}_{2}\right]\left[\mathrm{H}_{2}\right]^{3}}{\left[\mathrm{NH}_{3}\right]^{2}}=\frac{\left(3.0 \times 10^{-2}\right)\left(3.7 \times 10^{-2}\right)^{3}}{\left(1.6 \times 10^{-2}\right)^{2}}=5.9 \times 10^{-3}$

Note that $K_{\mathrm{c}}{ }^{\prime}$ is the reciprocal of $K_{\mathrm{c}}$. That is,

$$
5.9 \times 10^{-3}=\frac{1}{1.7 \times 10^{2}}
$$

## Worked Example 13.3

Methyl tert-butyl ether (MTBE), an octane booster in gasoline, can be synthesized by heating methanol and tert-butyl alcohol with sulfuric acid:

$$
\begin{gathered}
\mathrm{CH}_{3} \mathrm{OH}(\text { soln })+\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{OH}(\text { soln }) \\
\text { Methanol } \quad \text { tert-Butyl alcohol }
\end{gathered} \underset{\text { Methyl tert-butyl ether }}{\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{OCH}_{3}(\text { soln })+\mathrm{H}_{2} \mathrm{O}(\text { soln })}
$$

In this equation, soln denotes a largely organic solution that also contains water. Write the equilibrium constant expression for the reaction.

## Strategy

The rules for writing the equilibrium constant expression apply to reactions in solution as well as to gas-phase reactions. Put the concentrations of the products in the numerator and the concentrations of the reactants in the denominator. No exponents are needed because all the coefficients in the balanced chemical equation equal unity.

## Solution

$$
K_{\mathrm{c}}=\frac{\left[\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{OCH}_{3}\right]\left[\mathrm{H}_{2} \mathrm{O}\right]}{\left[\mathrm{CH}_{3} \mathrm{OH}\right]\left[\mathrm{C}_{4} \mathrm{H}_{9} \mathrm{OH}\right]} \longleftarrow \text { Products }
$$

PROBLEM 13.1 The oxidation of sulfur dioxide to give sulfur trioxide is an important step in the industrial process for synthesis of sulfuric acid. Write the equilibrium equation for each of the following reactions:
(a) $2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{SO}_{3}(g)$
(b) $2 \mathrm{SO}_{3}(g) \rightleftharpoons 2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g)$

PROBLEM 13.2 The following equilibrium concentrations were measured at 800 K : $\left[\mathrm{SO}_{2}\right]=3.0 \times 10^{-3} \mathrm{M} ;\left[\mathrm{O}_{2}\right]=3.5 \times 10^{-3} \mathrm{M} ;\left[\mathrm{SO}_{3}\right]=5.0 \times 10^{-2} \mathrm{M}$. Calculate the equilibrium constant at 800 K for each of the reactions in Problem 13.1.

- PROBLEM 13.3 Lactic acid, which builds up in muscle tissue upon strenuous exercise, is partially dissociated in aqueous solution:

(a) Write the equilibrium constant expression for $K_{c}$.
(b) What is the value of $K_{c}$ if the extent of dissociation in 0.100 M lactic acid is $3.65 \%$ at $25^{\circ} \mathrm{C}$ ?


## Worked Key Concept Example 13.4

The following pictures represent mixtures of A molecules (red spheres) and B molecules (blue spheres), which interconvert according to the equation $A \rightleftharpoons B$. If mixture (1) is at equilibrium, which of the other mixtures are also at equilibrium? Explain.

$\square$The subscript p in $K_{p}$ means that the amounts of reactants and products are expressed as partial pressures.

(1)

(2)

(3)

(4)

## Strategy

The equilibrium constant for the reaction is given by $K_{c}=[B] /[\mathrm{A}]$, where the concentrations are equilibrium concentrations in units of $\mathrm{mol} / \mathrm{L}$. Since the equilibrium constant expression has the same number of concentration terms in the numerator and denominator, the volume cancels and $K_{c}=($ moles of $B) /($ moles of $A)$. Because the number of moles is directly proportional to the number of molecules, $K_{c}=$ (molecules of B)/(molecules of A) in the equilibrium mixture (1). To determine whether the other mixtures are at equilibrium, count the number of molecules and compare the $B / A$ ratio in mixtures (2)-(4) with the $B / A$ ratio in the equilibrium mixture.

## Solution

For mixture (1), $K_{c}=[B] /[A]=2 / 6=1 / 3$.
For mixture (2), $[\mathrm{B}] /[\mathrm{A}]=4 / 4=1 \neq K_{\mathrm{c}}$.
For mixture (3), $[B] /[A]=3 / 9=1 / 3=K_{c}$.
For mixture (4), $[B] /[A]=9 / 3=3 \neq K_{c}$.
Mixture (3) is at equilibrium, but mixtures (2) and (4) are not at equilibrium because their equilibrium constant expression $[B] /[A]$ does not equal $K_{c}$.
-KEY CONCEPT PROBLEM 13.4 The following pictures represent mixtures that contain $A$ atoms (red), $B$ atoms (blue), and $A B$ and $B_{2}$ molecules, which interconvert according to the equation $A+B_{2} \rightleftharpoons A B+B$. If mixture (1) is at equilibrium, which of the other mixtures are also at equilibrium? Explain.

(1)

(2)

(3)

(4)

## 13.3 | The Equilibrium Constant $K_{p}$

Because gas pressures are easily measured, equilibrium equations for gas-phase reactions are often written using partial pressures rather than molar concentrations. For example, the equilibrium equation for the decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$ can be written as

$$
K_{\mathrm{p}}=\frac{\left(P_{\mathrm{NO}_{2}}\right)^{2}}{P_{\mathrm{N}_{2} \mathrm{O}_{4}}} \quad \text { for the reaction } \mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)
$$

where $P_{\mathrm{N}_{2} \mathrm{O}_{4}}$ and $P_{\mathrm{NO}_{2}}$ are the partial pressures (in atmospheres) of reactants and products at equilibrium, and the subscript $p$ on $K$ reminds us that the equilibrium constant $K_{p}$ is defined using partial pressures. As for $K_{c}$, values of $K_{\mathrm{p}}$ are dimensionless because the units cancel if we divide the partial pressure of each substance in atmospheres by its standard-state partial pressure of 1 atm . Note that the equilibrium equations for $K_{p}$ and $K_{c}$ have the same form except that the expression for $K_{\mathrm{p}}$ contains partial pressures instead of molar concentrations.

The constants $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ for the general gas-phase reaction $a \mathrm{~A}+b \mathrm{~B} \rightleftharpoons c \mathrm{C}+d \mathrm{D}$ are related because the pressure of each component in a mixture of ideal gases is directly proportional to its molar concentration. For component A, for example,

$$
\begin{aligned}
P_{\mathrm{A}} V & =n_{\mathrm{A}} R T \\
P_{\mathrm{A}} & =\frac{n_{\mathrm{A}}}{V} R T=[\mathrm{A}] R T
\end{aligned}
$$

Similarly, $P_{\mathrm{B}}=[\mathrm{B}] R T, P_{\mathrm{C}}=[\mathrm{C}] R T$, and $P_{\mathrm{D}}=[\mathrm{D}] R T$. The equilibrium equation for $K_{\mathrm{p}}$ is therefore given by

$$
K_{\mathrm{p}}=\frac{\left(P_{\mathrm{C}}\right)^{c}\left(P_{\mathrm{D}}\right)^{d}}{\left(P_{\mathrm{A}}\right)^{a}\left(P_{\mathrm{B}}\right)^{b}}=\frac{([\mathrm{C}] R T)^{c}([\mathrm{D}] R T)^{d}}{([\mathrm{~A}] R T)^{a}([\mathrm{~B}] R T)^{b}}=\frac{[\mathrm{C}]^{c}[\mathrm{D}]^{d}}{[\mathrm{~A}]^{a}[\mathrm{~B}]^{b}} \times(R T)^{(c+d)-(a+b)}
$$

Because the first term on the right side equals $K_{c}$, the values of $K_{p}$ and $K_{c}$ are related by the equation

$$
K_{\mathrm{p}}=K_{\mathrm{c}}(R T)^{\Delta n} \quad \text { for the reaction } a \mathrm{~A}+b \mathrm{~B} \rightleftharpoons c \mathrm{C}+d \mathrm{D}
$$

Here, $R$ is the gas constant, $0.08206(\mathrm{~L} \cdot \mathrm{~atm}) /(\mathrm{K} \cdot \mathrm{mol}), T$ is the absolute temperature, and $\Delta n=(c+d)-(a+b)$ is the number of moles of gaseous products minus the number of moles of gaseous reactants.

For the decomposition of 1 mol of $\mathrm{N}_{2} \mathrm{O}_{4}$ to 2 mol of $\mathrm{NO}_{2}, \Delta n=2-1=1$, and $K_{\mathrm{p}}=K_{\mathrm{c}}(R T):$

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g) \quad K_{\mathrm{p}}=K_{\mathrm{c}}(R T)
$$

For the reaction of 1 mol of hydrogen with 1 mol of iodine to give 2 mol of hydrogen iodide, $\Delta n=2-(1+1)=0$, and $K_{\mathrm{p}}=K_{\mathrm{c}}(R T)^{0}=K_{\mathrm{c}}$ :

$$
\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g) \quad K_{\mathrm{p}}=K_{\mathrm{c}}
$$

$$
8: \dot{0}=0: 0
$$

In general, $K_{\mathrm{p}}$ equals $K_{\mathrm{c}}$ only if the same number of moles of gases appear on both sides of the balanced chemical equation so that $\Delta n=0$.

## Worked Example 13.5

Methane $\left(\mathrm{CH}_{4}\right)$ reacts with hydrogen sulfide to yield $\mathrm{H}_{2}$ and carbon disulfide, a solvent used in manufacturing rayon and cellophane:

$$
\mathrm{CH}_{4}(g)+2 \mathrm{H}_{2} \mathrm{~S}(g) \rightleftharpoons \mathrm{CS}_{2}(g)+4 \mathrm{H}_{2}(g)
$$



What is the value of $K_{p}$ at 1000 K if the partial pressures in an equilibrium mixture at 1000 K are 0.20 atm of $\mathrm{CH}_{4}, 0.25 \mathrm{~atm}$ of $\mathrm{H}_{2} \mathrm{~S}, 0.52 \mathrm{~atm}$ of $\mathrm{CS}_{2}$, and 0.10 atm of $\mathrm{H}_{2}$ ?

## Strategy

Write the equilibrium equation by setting $K_{\mathrm{p}}$ equal to the equilibrium constant expression using partial pressures. Put the partial pressures of products in the numerator and the partial pressures of reactants in the denominator, with the pressure of each substance raised to the power of its coefficient in the balanced chemical equation. Then substitute the partial pressures into the equilibrium equation and solve for $K_{p}$.

## Solution

$$
\begin{gathered}
K_{\mathrm{p}}=\frac{\left(P_{\mathrm{CS}_{2}}\right)\left(P_{\mathrm{H}_{2}}\right)^{4}}{\left(P_{\mathrm{CH}_{4}}\right)\left(P_{\mathrm{H}_{2} \mathrm{~S}}\right)^{2}} \\
K_{\mathrm{p}}=\frac{\left(P_{\mathrm{CS}_{2}}\right)\left(P_{\mathrm{H}_{2}}\right)^{4}}{\left(P_{\mathrm{CH}_{4}}\right)\left(P_{\mathrm{H}_{2} \mathrm{~S}}\right)^{2}}=\frac{(0.52)(0.10)^{4}}{(0.20)(0.25)^{2}}=4.2 \times 10^{-3}
\end{gathered}
$$

Note that the partial pressures must be in units of atmospheres (not mm Hg ) because the standard-state partial pressure for gases is 1 atm .

## Worked Example 13.6

Hydrogen is produced industrially by the steam-hydrocarbon re-forming process. The reaction that takes place in the first step of this process is

$$
\mathrm{H}_{2} \mathrm{O}(g)+\mathrm{CH}_{4}(g) \rightleftharpoons \mathrm{CO}(g)+3 \mathrm{H}_{2}(g)
$$


(a) If $K_{\mathrm{c}}=3.8 \times 10^{-3}$ at 1000 K , what is the value of $K_{\mathrm{p}}$ at the same temperature?
(b) If $K_{\mathrm{p}}=6.1 \times 10^{4}$ at $1125^{\circ} \mathrm{C}$, what is the value of $K_{\mathrm{c}}$ at $1125^{\circ} \mathrm{C}$ ?

## Strategy

To calculate $K_{\mathrm{p}}$ from $K_{\mathrm{c}}$, or vice versa, use the equation $K_{\mathrm{p}}=K_{\mathrm{c}}(R T)^{\Delta n}$, where $R$ must be in units of $(\mathrm{L} \cdot \mathrm{atm}) /(\mathrm{K} \cdot \mathrm{mol}), T$ is the temperature in kelvins, and $\Delta n=$ $(c+d)-(a+b)$ is the number of moles of gaseous products minus the number of moles of gaseous reactants.

## Solution

(a) For this reaction, $\Delta n=(1+3)-(1+1)=2$. Therefore,

$$
K_{\mathrm{p}}=K_{\mathrm{c}}(R T)^{\Delta n}=K_{\mathrm{c}}(R T)^{2}=\left(3.8 \times 10^{-3}\right)[(0.08206)(1000)]^{2}=26
$$

(b) Solving the equation $K_{\mathrm{p}}=K_{\mathrm{c}}(R T)^{2}$ for $K_{\mathrm{c}}$ gives

$$
K_{\mathrm{c}}=\frac{K_{\mathrm{p}}}{(R T)^{2}}=\frac{6.1 \times 10^{4}}{[(0.08206)(1398)]^{2}}=4.6
$$

Note that the temperature in these equations is the absolute temperature; $1125^{\circ} \mathrm{C}$ corresponds to $1125+273=1398 \mathrm{~K}$.

- PROBLEM 13.5 In the industrial synthesis of hydrogen, mixtures of CO and $\mathrm{H}_{2}$ are enriched in $\mathrm{H}_{2}$ by allowing the CO to react with steam. The chemical equation for this so-called water-gas shift reaction is

$$
\mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g)
$$

What is the value of $K_{\mathrm{p}}$ at 700 K if the partial pressures in an equilibrium mixture at 700 K are 1.31 atm of $\mathrm{CO}, 10.0 \mathrm{~atm}$ of $\mathrm{H}_{2} \mathrm{O}, 6.12 \mathrm{~atm}$ of $\mathrm{CO}_{2}$, and 20.3 atm of $\mathrm{H}_{2}$ ?

- PROBLEM 13.6 Nitric oxide reacts with oxygen to give nitrogen dioxide, an important reaction in the Ostwald process for the industrial synthesis of nitric acid:

$$
2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)
$$

If $K_{c}=6.9 \times 10^{5}$ at $227^{\circ} \mathrm{C}$, what is the value of $K_{\mathrm{p}}$ at this temperature? If $K_{\mathrm{p}}=$ $1.3 \times 10^{-2}$ at 1000 K , what is the value of $K_{\mathrm{c}}$ at 1000 K ?

## 13.4 | Heterogeneous Equilibria

Thus far we've been discussing homogeneous equilibria, in which all reactants and products are in a single phase, usually either gaseous or solution. Heterogeneous equilibria, by contrast, are those in which reactants and products are present in more than one phase. Take, for example, the thermal decomposition of solid calcium carbonate, a reaction used in manufacturing cement:

$$
\underset{\text { Limestone }}{\mathrm{CaCO}_{3}(s)} \rightleftharpoons \underset{\text { Lime }}{\mathrm{CaO}(s)}+\mathrm{CO}_{2}(g)
$$

When the reaction is carried out in a closed container, three phases are present at equilibrium: solid calcium carbonate, solid calcium oxide, and gaseous carbon dioxide. If we were to write the usual equilibrium equation for the reaction, including all the reactants and products, we would have

$$
" \mathrm{~K}_{\mathrm{c}}^{\prime \prime}=\frac{[\mathrm{CaO}]\left[\mathrm{CO}_{2}\right]}{\left[\mathrm{CaCO}_{3}\right]}
$$

But because both CaO and $\mathrm{CaCO}_{3}$ are pure solids, their molar "concentrations" are constants. In general, the concentration of any pure solid (or pure liquid) is independent of its amount because its concentration is the ratio of its amount (in moles) to its volume (in liters). If, for example, you double the amount of $\mathrm{CaCO}_{3}$, you also double its volume, but the ratio of the two (the concentration) remains constant.

Rearranging the equilibrium equation for the decomposition of $\mathrm{CaCO}_{3}$ to combine the constants $\left[\mathrm{CaCO}_{3}\right],[\mathrm{CaO}]$, and " $\mathrm{K}_{\mathrm{c}}$ ", we obtain

$$
" \mathrm{~K}_{\mathrm{c}}^{\prime \prime} \times \frac{\left[\mathrm{CaCO}_{3}\right]^{2}}{[\mathrm{CaO}]^{\text {Constant }}}=\left[\mathrm{CO}_{2}\right]
$$



- The manufacture of cement begins with the thermal decomposition of limestone, $\mathrm{CaCO}_{3}$, in large kilns.

We can rewrite this equation as $K_{c}=\left[\mathrm{CO}_{2}\right]$, where the new equilibrium constant is $K_{c}=$ " $K_{c}$ " $\left[\mathrm{CaCO}_{3}\right] /[\mathrm{CaO}]$. The analogous equilibrium equation in terms of pressure is $K_{\mathrm{p}}=P_{\mathrm{CO}_{2}}$, where $P_{\mathrm{CO}_{2}}$ is the equilibrium pressure of $\mathrm{CO}_{2}$ in atmospheres:

$$
K_{\mathrm{c}}=\left[\mathrm{CO}_{2}\right] \quad K_{\mathrm{p}}=P_{\mathrm{CO}_{2}}
$$

As a general rule, the concentrations of pure solids and pure liquids are not included when writing an equilibrium equation because their concentrations are constants that are incorporated into the value of the equilibrium constant. We include only the concentrations of gases and the concentrations of solutes in solutions because only those concentrations can be varied.

To establish equilibrium between solid $\mathrm{CaCO}_{3}$, solid CaO , and gaseous $\mathrm{CO}_{2}$, all three components must be present. It follows from the equations $K_{c}=\left[\mathrm{CO}_{2}\right]$

FIGURE 13.3 Thermal decomposition of calcium carbonate: $\mathrm{CaCO}_{3}(s) \rightleftharpoons$ $\mathrm{CaO}(s)+\mathrm{CO}_{2}(g)$. At the same temperature, the equilibrium pressure of $\mathrm{CO}_{2}$ (measured with a closed-end manometer) is the same in (a) and (b), independent of how much solid $\mathrm{CaCO}_{3}$ and CaO are present. and $K_{\mathrm{p}}=P_{\mathrm{CO}_{2}}$, however, that the concentration and pressure of $\mathrm{CO}_{2}$ at equilibrium are constant, independent of how much solid CaO and $\mathrm{CaCO}_{3}$ is present (Figure 13.3). If the temperature is changed, the concentration and pressure of $\mathrm{CO}_{2}$ will also change because the values of $K_{\mathrm{c}}$ and $K_{\mathrm{p}}$ depend on temperature.

(a)

(b)

## Worked Example 13.7

Write the equilibrium equation for each of the following reactions:
(a) $\mathrm{CO}_{2}(g)+\mathrm{C}(s) \rightleftharpoons 2 \mathrm{CO}(g)$
(b) $\mathrm{Hg}(l)+\mathrm{Hg}^{2+}(a q) \rightleftharpoons \mathrm{Hg}_{2}{ }^{2+}(a q)$

## Strategy

We write the usual equilibrium constant expressions but omit the pure solid carbon in part (a) and the pure liquid mercury in part (b) because their concentrations are constants that are incorporated into the equilibrium constant $K_{c}$.

## Solution

(a) $K_{c}=\frac{[\mathrm{CO}]^{2}}{\left[\mathrm{CO}_{2}\right]}$

Alternatively, because CO and $\mathrm{CO}_{2}$ are gases, the equilibrium equation can be written using partial pressures:

$$
K_{\mathrm{p}}=\frac{\left(P_{\mathrm{CO}}\right)^{2}}{P_{\mathrm{CO}_{2}}}
$$

The relationship between $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ is $K_{\mathrm{p}}=K_{\mathrm{c}}(R T)^{\Delta n}$, where $\Delta n=2-1=1$.
(b) $K_{\mathrm{c}}=\frac{\left[\mathrm{Hg}_{2}{ }^{2+}\right]}{\left[\mathrm{Hg}^{2+}\right]}$

In this case, it's not appropriate to write an expression for $K_{\mathrm{p}}$ because none of the reactants and products is a gas.

- PROBLEM 13.7 For each of the following reactions, write the equilibrium constant expression for $K_{c}$. Where appropriate, also write the equilibrium constant expression for $K_{p}$, and relate $K_{p}$ to $K_{c}$.
(a) $2 \mathrm{Fe}(s)+3 \mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{H}_{2}(g)$
(b) $2 \mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g)$
(c) $\mathrm{SiCl}_{4}(g)+2 \mathrm{H}_{2}(g) \rightleftharpoons \mathrm{Si}(s)+4 \mathrm{HCl}(g)$
(d) $\mathrm{Hg}_{2}{ }^{2+}(a q)+2 \mathrm{Cl}^{-}(a q) \rightleftharpoons \mathrm{Hg}_{2} \mathrm{Cl}_{2}(s)$


## 13.5 | Using the Equilibrium Constant

Knowing the value of the equilibrium constant for a chemical reaction lets us judge the extent of the reaction, predict the direction of the reaction, and calculate equilibrium concentrations from any initial concentrations. Let's look at each possibility.

## Judging the Extent of Reaction

The numerical value of the equilibrium constant for a reaction indicates the extent to which reactants are converted to products; that is, it measures how far the reaction proceeds before the equilibrium state is reached. Consider, for example, the reaction of $\mathrm{H}_{2}$ with $\mathrm{O}_{2}$, which has a very large equilibrium constant $\left(K_{\mathrm{c}}=2.4 \times 10^{47}\right.$ at 500 K$)$ :

$$
\begin{aligned}
& 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}(g) \\
& K_{\mathrm{c}}=\frac{\left[\mathrm{H}_{2} \mathrm{O}\right]^{2}}{\left[\mathrm{H}_{2}\right]^{2}\left[\mathrm{O}_{2}\right]}=2.4 \times 10^{47} \quad \text { at } 500 \mathrm{~K}
\end{aligned}
$$

Because products appear in the numerator of the equilibrium constant expression and reactants are in the denominator, a very large value of $K_{c}$ means that the equilibrium ratio of products to reactants is very large. In other words, the reaction proceeds nearly to completion. For example, if stoichiometric amounts of $\mathrm{H}_{2}$ and $\mathrm{O}_{2}$ are allowed to react and $\left[\mathrm{H}_{2} \mathrm{O}\right]=1.0 \mathrm{M}$ at equilibrium, then the concentrations of $\mathrm{H}_{2}$ and $\mathrm{O}_{2}$ that remain at equilibrium are negligibly small: $\left[\mathrm{H}_{2}\right]=2.0 \times 10^{-16} \mathrm{M}$ and $\left[\mathrm{O}_{2}\right]=1.0 \times 10^{-16} \mathrm{M}$. (Try substituting these concentrations into the equilibrium equation to show that they satisfy the equation.)

By contrast, if a reaction has a very small value of $K_{c}$, the equilibrium ratio of products to reactants is very small and the reaction proceeds hardly at all before equilibrium is reached. For example, the reverse of the reaction of $\mathrm{H}_{2}$ with $\mathrm{O}_{2}$ gives the same equilibrium mixture as obtained from the forward reaction $\left(\left[\mathrm{H}_{2}\right]=\right.$ $\left.2.0 \times 10^{-16} \mathrm{M},\left[\mathrm{O}_{2}\right]=1.0 \times 10^{-16} \mathrm{M},\left[\mathrm{H}_{2} \mathrm{O}\right]=1.0 \mathrm{M}\right)$. The reverse reaction does not occur to any appreciable extent, however, because its equilibrium constant is so small: $K_{c}^{\prime}=1 / K_{c}=1 /\left(2.4 \times 10^{47}\right)=4.1 \times 10^{-48}$.

$$
\begin{aligned}
& 2 \mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \\
& K_{\mathrm{c}}^{\prime}=\frac{\left[\mathrm{H}_{2}\right]^{2}\left[\mathrm{O}_{2}\right]}{\left[\mathrm{H}_{2} \mathrm{O}\right]^{2}}=4.1 \times 10^{-48} \quad \text { At } 500 \mathrm{~K}
\end{aligned}
$$

If a reaction has an intermediate value of $K_{c}$ —say, a value in the range of $10^{3}$ to $10^{-3}$-then appreciable concentrations of both reactants and products are present


vFor an equilibrium system, the concentration of any reactant or product can never be zero. No matter how small or how large the equilibrium constant, there must always be some products and some reactants for an equilibrium to exist.
in the equilibrium mixture. The reaction of hydrogen with iodine, for example, has $K_{\mathrm{c}}=57.0$ at 700 K :

$$
\begin{aligned}
& \mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g) \\
& K_{\mathrm{c}}=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=57.0 \quad \text { at } 700 \mathrm{~K}
\end{aligned}
$$

If the equilibrium concentrations of $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$ are both 0.010 M , then the concentration of HI at equilibrium is 0.075 M :

$$
\begin{aligned}
{[\mathrm{HI}]^{2} } & =K_{\mathrm{c}}\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right] \\
{[\mathrm{HI}] } & =\sqrt{K_{\mathrm{c}}\left[\mathrm{H}_{2}\right]\left[I_{2}\right]}=\sqrt{(57.0)(0.010)(0.010)}=0.075 \mathrm{M}
\end{aligned}
$$

Thus, the concentrations of both reactants and products- 0.010 M and 0.075 M are appreciable.

The gas-phase decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$ to $\mathrm{NO}_{2}$ is another reaction with a value of $K_{c}$ that is neither large nor small: $K_{c}=4.64 \times 10^{-3}$ at $25^{\circ} \mathrm{C}$. Accordingly, equilibrium mixtures contain appreciable concentrations of both $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$, as shown previously in Table 13.1.

We can make the following generalizations concerning the composition of equilibrium mixtures:

- If $K_{\mathrm{c}}>10^{3}$, products predominate over reactants. If $K_{\mathrm{c}}$ is very large, the reaction proceeds nearly to completion.
- If $K_{c}<10^{-3}$, reactants predominate over products. If $K_{c}$ is very small, the reaction proceeds hardly at all.
- If $K_{\mathrm{c}}$ is in the range $10^{-3}$ to $10^{3}$, appreciable concentrations of both reactants and products are present.
These points are illustrated in Figure 13.4.

FIGURE 13.4 Judging the extent of a reaction. The larger the value of the equilibrium constant $K_{c}$, the farther the reaction proceeds to the right before reaching the equilibrium state.


PROBLEM 13.8 The value of $K_{c}$ for the dissociation reaction $\mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{H}(g)$ is $1.2 \times 10^{-42}$ at 500 K . Does the equilibrium mixture contain mainly $\mathrm{H}_{2}$ molecules or H atoms? Explain in light of the position of hydrogen in the periodic table.


## Predicting the Direction of Reaction

Consider again the gaseous reaction of hydrogen with iodine:

$$
\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g) \quad K_{\mathrm{c}}=57.0 \text { at } 700 \mathrm{~K}
$$

Suppose that we have a mixture of $\mathrm{H}_{2}(\mathrm{~g}), \mathrm{I}_{2}(\mathrm{~g})$, and $\mathrm{HI}(\mathrm{g})$ at 700 K with concentrations $\left[\mathrm{H}_{2}\right]_{t}=0.10 \mathrm{M},\left[\mathrm{I}_{2}\right]_{t}=0.20 \mathrm{M}$, and $[\mathrm{HI}]_{t}=0.40 \mathrm{M}$. (The subscript $t$ on the concentration symbols means that the concentrations were measured at some
arbitrary time $t$, not necessarily at equilibrium.) If we substitute these concentrations into the equilibrium constant expression, we obtain a value called the reaction quotient $Q_{c}$.

$$
\text { Reaction quotient: } \quad Q_{\mathrm{c}}=\frac{[\mathrm{HI}]_{t}^{2}}{\left[\mathrm{H}_{2}\right]_{t}\left[\mathrm{I}_{2}\right]_{t}}=\frac{(0.40)^{2}}{(0.10)(0.20)}=8.0
$$

The reaction quotient $Q_{c}$ is defined in the same way as the equilibrium constant $K_{c}$ except that the concentrations in $Q_{c}$ are not necessarily equilibrium values.

For the case at hand, the numerical value of $Q_{c}(8.0)$ does not equal $K_{c}(57.0)$, so the mixture of $\mathrm{H}_{2}(g), \mathrm{I}_{2}(g)$, and $\mathrm{HI}(g)$ is not at equilibrium. As time passes, though, reaction will occur, changing the concentrations and thus changing the value of $Q_{c}$ in the direction of $K_{c}$. After a sufficiently long time, an equilibrium state will be reached, and $Q_{c}=K_{c}$.

The reaction quotient $Q_{c}$ is useful because it lets us predict the direction of reaction by comparing the values of $Q_{c}$ and $K_{c}$. If $Q_{c}$ is less than $K_{c}$, movement toward equilibrium increases $Q_{c}$ by converting reactants to products (that is, net reaction proceeds from left to right). If $Q_{c}$ is greater than $K_{c}$, movement toward equilibrium decreases $Q_{\mathrm{c}}$ by converting products to reactants (that is, net reaction proceeds from right to left). If $Q_{c}$ equals $K_{c}$, the reaction mixture is already at equilibrium, and no net reaction occurs.

Thus, we can make the following generalizations concerning the direction of the reaction:

- If $Q_{c}<K_{c}$, net reaction goes from left to right.
- If $Q_{c}>K_{c}$, net reaction goes from right to left.
- If $Q_{c}=K_{c}$, no net reaction occurs.

These points are illustrated in Figure 13.5.


## Worked Example 13.8

A mixture of 1.57 mol of $\mathrm{N}_{2}, 1.92 \mathrm{~mol}$ of $\mathrm{H}_{2}$, and 8.13 mol of $\mathrm{NH}_{3}$ is introduced into a 20.0 L reaction vessel at 500 K . At this temperature, the equilibrium constant $K_{\mathrm{c}}$ for the reaction $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$ is $1.7 \times 10^{2}$. Is the reaction mixture at equilibrium? If not, what is the direction of the net reaction?

## Strategy

To determine whether the reaction mixture is at equilibrium, we need to calculate the value of the reaction quotient $Q_{c}$ and then compare it with the equilibrium constant $K_{\mathrm{c}}$. If the mixture is not at equilibrium, the relative values of $Q_{\mathrm{c}}$ and $K_{\mathrm{c}}$ tell us the direction of the net reaction. Because we are given amounts in moles, we must first convert moles to molar concentrations before substituting into the expression for $Q_{c}$.

V
The equilibrium constant expression $=K_{\mathrm{c}}$ only at equilibrium. The equilibrium constant expression $=Q_{c}$, the reaction quotient, whether or not the system is at equilibrium.


$\sqrt{ }$Students should apply these criteria results not by rote memorization but by analysis of what must occur when $Q_{c} \neq K_{c}$.

4 FIGURE 13.5 Predicting the direction of reaction. The direction of net reaction depends on the relative values of $Q_{c}$ and $K_{c}$. Note that movement toward equilibrium changes the value of $Q_{c}$ until it equals $K_{c}$, but the value of $K_{c}$ remains constant.


## Solution

The initial concentration of $\mathrm{N}_{2}$ is $(1.57 \mathrm{~mol}) /(20.0 \mathrm{~L})=0.0785 \mathrm{M}$. Similarly, $\left[\mathrm{H}_{2}\right]=0.0960 \mathrm{M}$ and $\left[\mathrm{NH}_{3}\right]=0.406 \mathrm{M}$. Substituting these concentrations into the equilibrium constant expression gives

$$
Q_{\mathrm{c}}=\frac{\left[\mathrm{NH}_{3}\right]_{t}^{2}}{\left[\mathrm{~N}_{2}\right]_{t}\left[\mathrm{H}_{2}\right]_{t}^{3}}=\frac{(0.406)^{2}}{(0.0785)(0.0960)^{3}}=2.37 \times 10^{3}
$$

Because $Q_{c}$ does not equal $K_{c}\left(1.7 \times 10^{2}\right)$, the reaction mixture is not at equilibrium. Because $Q_{c}$ is greater than $K_{c}$, net reaction will proceed from right to left, decreasing the concentration of $\mathrm{NH}_{3}$ and increasing the concentrations of $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ until $Q_{\mathrm{c}}=K_{\mathrm{c}}=1.7 \times 10^{2}$.
$\checkmark$ BALLPARK CHECK Approximate initial concentrations can be calculated by dividing rounded values of the number of moles of each substance by the volume; $\left[\mathrm{N}_{2}\right] \approx(1.6 \mathrm{~mol}) /(20 \mathrm{~L}) \approx 0.08 \mathrm{M},\left[\mathrm{H}_{2}\right] \approx(2 \mathrm{~mol}) /(20 \mathrm{~L}) \approx 0.1 \mathrm{M}$, and $\left[\mathrm{NH}_{3}\right] \approx$ $(8 \mathrm{~mol}) /(20 \mathrm{~L}) \approx 0.4 \mathrm{M}$. Substituting these concentrations into the expression for $Q_{\mathrm{c}}$ gives a ballpark estimate of $Q_{\mathrm{c}}$ :

$$
Q_{\mathrm{c}}=\frac{\left[\mathrm{NH}_{3}\right]_{t}^{2}}{\left[\mathrm{~N}_{2}\right]_{t}\left[\mathrm{H}_{2}\right]_{t}^{3}} \approx \frac{(0.4)^{2}}{(0.08)(0.1)^{3}} \approx 2 \times 10^{3}
$$

You can calculate this value without a calculator because it equals ( $16 \times$ $\left.10^{-2}\right) /\left(8 \times 10^{-5}\right)$. The ballpark estimate of $Q_{c}$ agrees with the more exact value of $Q_{\mathrm{c}}=2.37 \times 10^{3}$.

- PROBLEM 13.9 The equilibrium constant $K_{c}$ for the reaction $2 \mathrm{NO}(g)+$ $\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$ is $6.9 \times 10^{5}$ at 500 K . A 5.0 L reaction vessel at this temperature was filled with 0.060 mol of $\mathrm{NO}, 1.0 \mathrm{~mol}$ of $\mathrm{O}_{2}$, and 0.80 mol of $\mathrm{NO}_{2}$.
(a) Is the reaction mixture at equilibrium? If not, in which direction does the net reaction proceed?
(b) What is the direction of the net reaction if the initial amounts are $5.0 \times 10^{-3} \mathrm{~mol}$ of $\mathrm{NO}, 0.20 \mathrm{~mol}$ of $\mathrm{O}_{2}$, and 4.0 mol of $\mathrm{NO}_{2}$ ?
- KEY CONCEPT PROBLEM 13.10 The reaction $\mathrm{A}_{2}+\mathrm{B}_{2} \rightleftharpoons 2 \mathrm{AB}$ has an equilibrium constant $K_{c}=4$. The following pictures represent reaction mixtures that contain $A_{2}$ molecules (red), $B_{2}$ molecules (blue), and $A B$ molecules:

(a) Which reaction mixture is at equilibrium?
(b) For those reaction mixtures that are not at equilibrium, will the net reaction go in the forward or reverse direction to reach equilibrium?


## Calculating Equilibrium Concentrations

If the equilibrium constant and all the equilibrium concentrations but one are known, the unknown concentration can be calculated directly from the equilibrium equation. To illustrate, let's consider the following problem: What is the concentration of NO in an equilibrium mixture of gaseous $\mathrm{NO}, \mathrm{O}_{2}$, and $\mathrm{NO}_{2}$ at 500 K that contains $1.0 \times 10^{-3} \mathrm{M} \mathrm{O}_{2}$ and $5.0 \times 10^{-2} \mathrm{M} \mathrm{NO}_{2}$ ? At this temperature, the
equilibrium constant $K_{c}$ for the reaction $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$ is $6.9 \times 10^{5}$.

In this problem, $K_{c}$ and all the equilibrium concentrations except one are known, and we're asked to calculate the unknown equilibrium concentration. First, we write the equilibrium equation for the reaction and solve for the unknown concentration:

$$
K_{\mathrm{c}}=\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{NO}^{2}\left[\mathrm{O}_{2}\right]\right.} \quad[\mathrm{NO}]=\sqrt{\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{O}_{2}\right] K_{\mathrm{c}}}}
$$

Then we substitute the known values of $K_{c},\left[\mathrm{O}_{2}\right]$, and $\left[\mathrm{NO}_{2}\right]$ into the expression for [ NO ] and calculate its equilibrium concentration:

$$
[\mathrm{NO}]=\sqrt{\frac{\left(5.0 \times 10^{-2}\right)^{2}}{\left(1.0 \times 10^{-3}\right)\left(6.9 \times 10^{5}\right)}}=\sqrt{3.6 \times 10^{-6}}= \pm 1.9 \times 10^{-3} \mathrm{M}
$$

(Pressing the $\sqrt{x}$ key on a calculator gives a positive number. Remember, though, that the square root of a positive number can be positive or negative.) Of the two roots, we choose the positive one $\left([\mathrm{NO}]=1.9 \times 10^{-3} \mathrm{M}\right)$ because the concentration of a chemical substance is always a positive quantity.

To be sure that we haven't made any errors, it's a good idea to check the result by substituting it into the equilibrium equation:

$$
K_{\mathrm{c}}=6.9 \times 10^{5}=\frac{\left[\mathrm{NO}_{2}\right]^{2}}{\left[\mathrm{NO}^{2}\left[\mathrm{O}_{2}\right]\right.}=\frac{\left(5.0 \times 10^{-2}\right)^{2}}{\left(1.9 \times 10^{-3}\right)^{2}\left(1.0 \times 10^{-3}\right)}=6.9 \times 10^{5}
$$

Another type of problem is one in which we know the initial concentrations but do not know any of the equilibrium concentrations. To solve this kind of problem, follow the series of steps summarized in Figure 13.6 and illustrated in

Step 1. Write the balanced equation for the reaction.


Step 2. Under the balanced equation, make a table that lists for each substance involved in the reaction:
(a) The initial concentration
(b) The change in concentration on going to equilibrium
(c) The equilibrium concentration

In constructing the table, define $x$ as the concentration ( $\mathrm{mol} / \mathrm{L}$ ) of one of the substances that reacts on going to equilibrium, then use the stoichiometry of the reaction to determine the concentrations of the other substances in terms of $x$.


Step 3. Substitute the equilibrium concentrations into the equilibrium equation for the reaction and solve for $x$. If you must solve a quadratic equation, choose the mathematical solution that makes chemical sense.


Step 4. Calculate the equilibrium concentrations from the calculated value of $x$.


Step 5. Check your results by substituting them into the equilibrium equation.

FIGURE 13.6 Steps to follow in calculating equilibrium concentrations from initial concentrations.

Figure 13.6 Examples activity

v
Strongly encourage using tables. Although not necessary, it is less confusing for many students to make the coefficient used with the unknown, $x$, the same as the coefficient in the balanced chemical equation.

(1)John Olmsted III, "Amounts Tables as a Diagnostic Tool for Flawed Stoichiometric Reasoning," J. Chem. Educ., Vol. 76, 1999, 52-54.

Mathematical tricks are not apparent to many students. Point out the value of setting up the problem to obtain a perfect square.

Worked Examples 13.9 and 13.10. The same approach can be used to calculate equilibrium partial pressures from initial partial pressures and $K_{p}$, as shown in Worked Example 13.11.

## Worked Example 13.9

The equilibrium constant $K_{c}$ for the reaction of $\mathrm{H}_{2}$ with $\mathrm{I}_{2}$ is 57.0 at 700 K :

$$
\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g) \quad \mathrm{K}_{\mathrm{c}}=57.0 \text { at } 700 \mathrm{~K}
$$

If 1.00 mol of $\mathrm{H}_{2}$ is allowed to react with 1.00 mol of $\mathrm{I}_{2}$ in a 10.0 L reaction vessel at 700 K , what are the concentrations of $\mathrm{H}_{2}, \mathrm{I}_{2}$, and HI at equilibrium? What is the composition of the equilibrium mixture in moles?

## Strategy

We need to calculate equilibrium concentrations from initial concentrations, so we should use the method outlined in Figure 13.6.

## Solution

Step 1. The balanced equation is given: $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g)$.
Step 2. The initial concentrations are $\left[\mathrm{H}_{2}\right]=\left[\mathrm{I}_{2}\right]=(1.00 \mathrm{~mol}) /(10.0 \mathrm{~L})=0.100 \mathrm{M}$. For convenience, define an unknown, $x$, as the concentration ( $\mathrm{mol} / \mathrm{L}$ ) of $\mathrm{H}_{2}$ that reacts. According to the balanced equation for the reaction, $x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{H}_{2}$ reacts with $x$ $\mathrm{mol} / \mathrm{L}$ of $\mathrm{I}_{2}$ to give $2 x \mathrm{~mol} / \mathrm{L}$ of HI . This reduces the initial concentrations of $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$ from $0.100 \mathrm{~mol} / \mathrm{L}$ to $(0.100-x) \mathrm{mol} / \mathrm{L}$ at equilibrium. Let's summarize these results in a table under the balanced equation:

|  | $\mathbf{H}_{\mathbf{2}}(\mathbf{g})$ | $\mathbf{+}$ | $\mathbf{I}_{\mathbf{2}}(\mathbf{g})$ | $\rightleftharpoons$ |
| :--- | :--- | :--- | :--- | :--- |
| Initial concentration $(\mathrm{M})$ | 0.100 | $\mathbf{2 ~ H I}(\boldsymbol{g})$ |  |  |
| Change (M) | $-x$ | 0.100 |  | 0 |
| Equilibrium concentration $(\mathrm{M})$ | $(0.100-x)$ | $(0.100-x)$ |  | $2 x$ |

Step 3. Substitute the equilibrium concentrations into the equilibrium equation for the reaction:

$$
K_{\mathrm{c}}=57.0=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(2 x)^{2}}{(0.100-x)(0.100-x)}=\left(\frac{2 x}{0.100-x}\right)^{2}
$$

Because the right side of this equation is a perfect square, we can take the square root of both sides:

$$
\sqrt{57.0}= \pm 7.55=\frac{2 x}{0.100-x}
$$

Solving for $x$, we obtain two solutions. The equation with the positive square root of 57.0 gives

$$
\begin{aligned}
+7.55(0.100-x) & =2 x \\
0.755 & =2 x+7.55 x \\
x=\frac{0.755}{9.55} & =0.0791 \mathrm{M}
\end{aligned}
$$

The equation with the negative square root of 57.0 gives

$$
\begin{aligned}
-7.55(0.100-x) & =2 x \\
-0.755 & =2 x-7.55 x \\
x & =\frac{-0.755}{-5.55}=0.136 \mathrm{M}
\end{aligned}
$$

Because the initial concentrations of $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$ are $0.100 \mathrm{M}, x$ can't exceed 0.100 M . Therefore, discard $x=0.136 \mathrm{M}$ as chemically unreasonable and choose the first solution, $x=0.0791 \mathrm{M}$.
Step 4. Calculate the equilibrium concentrations from the calculated value of $x$ :

$$
\begin{aligned}
& {\left[\mathrm{H}_{2}\right]=\left[\mathrm{I}_{2}\right]=0.100-x=0.100-0.0791=0.021 \mathrm{M}} \\
& {[\mathrm{HI}]=2 x=(2)(0.0791)=0.158 \mathrm{M}}
\end{aligned}
$$

Step 5. Check the results by substituting them into the equilibrium equation:

$$
K_{c}=57.0=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(0.158)^{2}}{(0.021)(0.021)}=57
$$

The number of moles of each substance in the equilibrium mixture can be obtained by multiplying each concentration by the volume of the reaction vessel:

$$
\begin{aligned}
& \text { Moles of } \mathrm{H}_{2}=\text { Moles of } \mathrm{I}_{2}=(0.021 \mathrm{~mol} / \mathrm{L})(10.0 \mathrm{~L})=0.21 \mathrm{~mol} \\
& \text { Moles of } \mathrm{HI}=(0.158 \mathrm{~mol} / \mathrm{L})(10.0 \mathrm{~L})=1.58 \mathrm{~mol}
\end{aligned}
$$

## Worked Example 13.10

Calculate the equilibrium concentrations of $\mathrm{H}_{2}, \mathrm{I}_{2}$, and HI at 700 K if the initial concentrations are $\left[\mathrm{H}_{2}\right]=0.100 \mathrm{M}$ and $\left[\mathrm{I}_{2}\right]=0.200 \mathrm{M}$. The equilibrium constant $K_{\mathrm{c}}$ for the reaction $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g)$ is 57.0 at 700 K .

## Strategy

This problem is similar to Worked Example 13.9 except that the initial concentrations of $\mathrm{H}_{2}$ and $\mathrm{I}_{2}$ are unequal. Again, we follow the steps in Figure 13.6.

## Solution

Step 1. The balanced equation is $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g)$.
Step 2. Again, define $x$ as the concentration of $\mathrm{H}_{2}$ that reacts. Set up a table of concentrations under the balanced equation:

|  | $\mathbf{H}_{\mathbf{2}}(\mathbf{g})$ | $\mathbf{+}$ | $\mathbf{I}_{\mathbf{2}}(\mathbf{g})$ | $\rightleftharpoons$ |
| :--- | :--- | :--- | :--- | :--- |
| Initial concentration $(\mathrm{M})$ | 0.100 | 0.200 |  | 0 |
| Change $(\mathrm{M})$ | $-x$ | $-x$ |  | $+2 x$ |
| Equilibrium concentration $(\mathrm{M})$ | $(0.100-x)$ | $(0.200-x)$ | $2 x$ |  |

Step 3. Substitute the equilibrium concentrations into the equilibrium equation:

$$
K_{c}=57.0=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(2 x)^{2}}{(0.100-x)(0.200-x)}
$$

Because the right side of this equation is not a perfect square, we must put the equation into the standard quadratic form, $a x^{2}+b x+c=0$, and then solve for $x$ using the quadratic formula (Appendix A.4):

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Rearranging the equilibrium equation gives

$$
(57.0)\left(0.0200-0.300 x+x^{2}\right)=4 x^{2}
$$

or

$$
53.0 x^{2}-17.1 x+1.14=0
$$

Mathematics sometimes yields results that have no physical meaning. Students should learn to analyze answers to problems to determine whether they make sense.

William R. Smith and Ronald W. Munson, "Chemical Equilibrium and Polynomial Equations: Beware of Roots," J. Chem. Educ., Vol. 66, 1989, 489-490.

Substituting the values of $a, b$, and $c$ into the quadratic formula gives two solutions:

$$
x=\frac{17.1 \pm \sqrt{(-17.1)^{2}-4(53.0)(1.14)}}{2(53.0)}=\frac{17.1 \pm 7.1}{106}=0.228 \text { and } 0.0943
$$

Discard the solution that uses the positive square root ( $x=0.228$ ) because the $\mathrm{H}_{2}$ concentration can't change by more than its initial value ( 0.100 M ). Therefore, choose the solution that uses the negative square root ( $x=0.0943$ ).
Step 4. Calculate the equilibrium concentrations from the calculated value of $x$ :

$$
\begin{aligned}
& {\left[\mathrm{H}_{2}\right]=0.100-x=0.100-0.0943=0.006 \mathrm{M}} \\
& {\left[\mathrm{I}_{2}\right]=0.200-x=0.200-0.0943=0.106 \mathrm{M}} \\
& {[\mathrm{HI}]=2 x=(2)(0.0943)=0.189 \mathrm{M}}
\end{aligned}
$$

Step 5. Check the results by substituting them into the equilibrium equation:

$$
K_{c}=57.0=\frac{[\mathrm{HI}]^{2}}{\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]}=\frac{(0.189)^{2}}{(0.006)(0.106)}=56.2
$$

The calculated value of $K_{c}$ (56.2), which should be rounded to one significant figure $\left(6 \times 10^{1}\right)$, agrees with the value given in the problem (57.0).

## Worked Example 13.11

One reaction that occurs in producing steel from iron ore is the reduction of iron(II) oxide by carbon monoxide to give iron metal and carbon dioxide. The equilibrium constant $K_{\mathrm{p}}$ for the reaction at 1000 K is 0.259 .

$$
\mathrm{FeO}(s)+\mathrm{CO}(g) \rightleftharpoons \mathrm{Fe}(s)+\mathrm{CO}_{2}(g) \quad K_{\mathrm{p}}=0.259 \text { at } 1000 \mathrm{~K}
$$

What are the equilibrium partial pressures of CO and $\mathrm{CO}_{2}$ at 1000 K if the initial partial pressures are $P_{\mathrm{CO}}=1.000 \mathrm{~atm}$ and $P_{\mathrm{CO}_{2}}=0.500 \mathrm{~atm}$ ?

## Strategy

We can calculate equilibrium partial pressures from initial partial pressures and $K_{p}$ in the same way that equilibrium concentrations are calculated from initial concentrations and $K_{c}$. Follow the steps in Figure 13.6, but substitute partial pressures for concentrations.

## Solution

Step 1. The balanced equation is $\mathrm{FeO}(s)+\mathrm{CO}(g) \rightleftharpoons \mathrm{Fe}(s)+\mathrm{CO}_{2}(g)$
Step 2. Define $x$ as the partial pressure of CO that reacts. Set up a table of partial pressures of the gases under the balanced equation:

|  | $\mathbf{F e O}(\mathbf{s})+\mathbf{C O}(\mathbf{g})$ | $\rightleftharpoons$ | $\mathbf{F e}(\mathbf{s})+\mathbf{C O}_{\mathbf{2}}(\mathbf{g})$ |
| :--- | :---: | :---: | :---: |
| Initial pressure (atm) | 1.000 |  | 0.500 |
| Change (atm) | $-x$ | $+x$ |  |
| Equilibrium pressure (atm) | $(1.000-x)$ |  | $(0.500+x)$ |

Step 3. Substitute the equilibrium partial pressures into the equilibrium equation for $K_{\mathrm{p}}$ :

$$
K_{\mathrm{p}}=0.259=\frac{P_{\mathrm{CO}_{2}}}{P_{\mathrm{CO}}}=\frac{0.500+x}{1.000-x}
$$

As usual for a heterogeneous equilibrium, we omit the pure solids from the equilibrium equation. Rearranging the equilibrium equation and solving for $x$ gives

$$
\begin{aligned}
& 0.259-0.259 x=0.500+x \\
& x=\frac{-0.241}{1.259}=-0.191
\end{aligned}
$$

Step 4. Calculate the equilibrium partial pressures from the calculated value of $x$ :

$$
\begin{aligned}
& P_{\mathrm{CO}}=1.000-x=1.000-(-0.191)=1.191 \mathrm{~atm} \\
& P_{\mathrm{CO}_{2}}=0.500+x=0.500+(-0.191)=0.309 \mathrm{~atm}
\end{aligned}
$$

Step 5. Check the results by substituting them into the equilibrium equation:

$$
K_{\mathrm{p}}=0.259=\frac{P_{\mathrm{CO}_{2}}}{P_{\mathrm{CO}}}=\frac{0.309}{1.191}=0.259
$$

A negative value for $x$ means that the reaction goes from right to left to reach equilibrium. This makes sense because the reaction quotient, $Q_{p}=0.500 / 1.000=0.500$, is greater than the equilibrium constant, $K_{p}=0.259$. When $Q_{p}>K_{p}$, the net reaction always goes from right to left.

- PROBLEM 13.11 In Problem 13.8, we found that an equilibrium mixture of $\mathrm{H}_{2}$ molecules and H atoms at 500 K contains mainly $\mathrm{H}_{2}$ molecules because the equilibrium constant for the dissociation reaction $\mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{H}(g)$ is very small ( $K_{\mathrm{c}}=1.2 \times 10^{-42}$ ).
(a) What is the molar concentration of H atoms if $\left[\mathrm{H}_{2}\right]=0.10 \mathrm{M}$ ?
(b) How many H atoms and $\mathrm{H}_{2}$ molecules are present in 1.0 L of $0.10 \mathrm{M} \mathrm{H}_{2}$ at 500 K ?
- PROBLEM 13.12 The $\mathrm{H}_{2}$ /CO ratio in mixtures of carbon monoxide and hydrogen (called synthesis gas) is increased by the water-gas shift reaction $\mathrm{CO}(g)+$ $\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g)$, which has an equilibrium constant $K_{\mathrm{c}}=4.24$ at 800 K . Calculate the equilibrium concentrations of $\mathrm{CO}_{2}, \mathrm{H}_{2}, \mathrm{CO}$, and $\mathrm{H}_{2} \mathrm{O}$ at 800 K if only CO and $\mathrm{H}_{2} \mathrm{O}$ are present initially at concentrations of 0.150 M .

PROBLEM 13.13 Calculate the equilibrium concentrations of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ at $25^{\circ} \mathrm{C}$ in a vessel that contains an initial $\mathrm{N}_{2} \mathrm{O}_{4}$ concentration of 0.0500 M . The equilibrium constant $K_{\text {c }}$ for the reaction $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$ is $4.64 \times 10^{-3}$ at $25^{\circ} \mathrm{C}$.

PROBLEM 13.14 Calculate the equilibrium concentrations at $25^{\circ} \mathrm{C}$ for the reaction in Problem 13.13 for initial concentrations of $\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]=0.0200 \mathrm{M}$ and $\left[\mathrm{NO}_{2}\right]=$ 0.0300 M .

- PROBLEM 13.15 The equilibrium constant $K_{\mathrm{p}}$ for the reaction $\mathrm{C}(s)+$ $\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}(g)+\mathrm{H}_{2}(g)$ is 2.44 at 1000 K . What are the equilibrium partial pressures of $\mathrm{H}_{2} \mathrm{O}, \mathrm{CO}$, and $\mathrm{H}_{2}$ if the initial partial pressures are $P_{\mathrm{H}_{2} \mathrm{O}}=1.20 \mathrm{~atm}$, $P_{\mathrm{CO}}=1.00 \mathrm{~atm}$, and $P_{\mathrm{H}_{2}}=1.40 \mathrm{~atm}$ ?


### 13.6 Factors That Alter the Composition of an Equilibrium Mixture

One of the principal goals of chemical synthesis is to maximize the conversion of reactants to products while minimizing the expenditure of energy. This objective is achieved easily if the reaction goes nearly to completion at mild temperature and pressure. If the reaction gives an equilibrium mixture that is rich in reactants and poor in products, however, then the experimental conditions must be adjusted. For example, in the Haber process for the synthesis of ammonia from $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ (Figure 13.7), the choice of experimental conditions is of real economic importance. Annual U.S. production of ammonia is about 13 million tons, primarily for use as fertilizer.

Martin R. Feldman and Monica L. Tarver, "Fritz Haber," J. Chem. Educ., Vol. 60, 1983, 463-464.

FIGURE 13.7 Representation of the Haber process for the industrial production of ammonia. A mixture of gaseous $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ at 130-300 atm pressure is passed over a catalyst at $400-500^{\circ} \mathrm{C}$, and ammonia is produced by the reaction $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$. The $\mathrm{NH}_{3}$ in the gaseous mixture of reactants and products is liquefied, and the unreacted $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ are recycled.


Several factors can be exploited to alter the composition of an equilibrium mixture:

- The concentration of reactants or products can be changed.
- The pressure and volume can be changed.
- The temperature can be changed.
(A possible fourth factor, addition of a catalyst, increases only the rate at which equilibrium is reached. As we'll see in Section 13.10, a catalyst does not affect the equilibrium concentrations.)

The qualitative effect of the listed changes on the composition of an equilibrium mixture can be predicted using a principle first described by the French chemist Henri-Louis Le Châtelier:

Le Châtelier's Principle If a stress is applied to a reaction mixture at equilibrium, net reaction occurs in the direction that relieves the stress.

The word "stress" in this context means a change in concentration, pressure, volume, or temperature that disturbs the original equilibrium. Reaction then occurs to change the composition of the mixture until a new state of equilibrium is reached. The direction that the reaction takes (reactants to products or vice versa) is the one that reduces the stress. In the next three sections, we'll look at the different kinds of stress that can change the composition of an equilibrium mixture.

### 13.7 Altering an Equilibrium Mixture: Changes in Concentration

Let's consider the equilibrium that occurs in the Haber process for the synthesis of ammonia:


Suppose that we have an equilibrium mixture of $0.50 \mathrm{M} \mathrm{N}_{2}, 3.00 \mathrm{M} \mathrm{H}_{2}$, and 1.98 M $\mathrm{NH}_{3}$ at 700 K , and that we disturb the equilibrium by increasing the $\mathrm{N}_{2}$ concentration to 1.50 M . Le Châtelier's principle tells us that reaction will occur to relieve the stress of the increased concentration of $\mathrm{N}_{2}$ by converting some of the $\mathrm{N}_{2}$ to $\mathrm{NH}_{3}$. As the $\mathrm{N}_{2}$ concentration decreases, the $\mathrm{H}_{2}$ concentration must also decrease and the $\mathrm{NH}_{3}$ concentration must increase in accord with the stoichiometry of the balanced equation. These changes are illustrated in Figure 13.8.


In general, when an equilibrium is disturbed by the addition or removal of any reactant or product, Le Châtelier's principle predicts that

- The concentration stress of an added reactant or product is relieved by net reaction in the direction that consumes the added substance.
- The concentration stress of a removed reactant or product is relieved by net reaction in the direction that replenishes the removed substance.

If these rules are applied to the equilibrium $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$, then the yield of ammonia is increased by an increase in the $\mathrm{N}_{2}$ or $\mathrm{H}_{2}$ concentration or by a decrease in the $\mathrm{NH}_{3}$ concentration (Figure 13.9). In the industrial production of ammonia, the concentration of gaseous $\mathrm{NH}_{3}$ is decreased by liquefying the ammonia ( $\mathrm{bp}-33^{\circ} \mathrm{C}$ ) as it's formed, and so more ammonia is produced.


0When an equilibrium is upset by a change in concentration, pressure and volume, or temperature, equilibrium will be restored, but the concentrations of reactants and products will be different from those in the original equilibrium mixture.

FIGURE 13.8 Changes in concentrations when $\mathrm{N}_{2}$ is added to an equilibrium mixture of $\mathrm{N}_{2}, \mathrm{H}_{2}$, and $\mathrm{NH}_{3}$. Net conversion of $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ to $\mathrm{NH}_{3}$ occurs until a new equilibrium is established. That is, $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ concentrations decrease, while the $\mathrm{NH}_{3}$ concentration increases.


$\square$If a reactant or product is added to a system at equilibrium, the reaction will occur in a direction away from that reactant or product. If a reactant or product is removed from a system at equilibrium, the reaction will occur in a direction toward that reactant or product.


- FIGURE 13.9 Effect of concentration changes on the equilibrium $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons$ $2 \mathrm{NH}_{3}(g)$. An increase in the $\mathrm{N}_{2}$ or $\mathrm{H}_{2}$ concentration or a decrease in the $\mathrm{NH}_{3}$ concentration shifts the equilibrium from left to right. A decrease in the $\mathrm{N}_{2}$ or $\mathrm{H}_{2}$ concentration or an increase in the $\mathrm{NH}_{3}$ concentration shifts the equilibrium from right to left.

Altering an Equilibrium Mixture activity

Lee R. Summerlin and James L. Ealy, Jr., "Equilibrium and Le Châtelier's Principle" Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), p. 77-78.

FIGURE 13.10 Color changes produced by adding various reagents to an equilibrium mixture of $\mathrm{Fe}^{3+}$ (pale yellow), $\mathrm{SCN}^{-}$(colorless), and FeNCS ${ }^{2+}$ (red): (a) The original solution. (b) After adding $\mathrm{FeCl}_{3}$ to the original solution, the red color is darker because of an increase in $\left[\mathrm{FeNCS}^{2+}\right]$. (c) After adding KSCN to the original solution, the red color again deepens. (d) After adding $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ to the original solution, the red color disappears because of a decrease in [ $\mathrm{FeNCS}^{2+}$ ]; the yellow color is due to $\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}{ }^{3-}$. (e) After adding $\mathrm{HgCl}_{2}$ to the original solution, the red color again vanishes.

(a)

(b)

(c)

(d)

(e)
substance present in plants such as rhubarb, reacts with $\mathrm{Fe}^{3+}$ to form the stable complex ion $\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}{ }^{3-}$, thus decreasing the concentration of free $\mathrm{Fe}^{3+}(a q)$. In accord with Le Châtelier's principle, the concentration stress of removed $\mathrm{Fe}^{3+}$ is relieved by dissociation of $\mathrm{FeNCS}^{2+}$ to replenish the $\mathrm{Fe}^{3+}$ ions. Because the concentration of FeNCS ${ }^{2+}$ decreases, the red color disappears.

Addition of aqueous $\mathrm{HgCl}_{2}$ also eliminates the red color because $\mathrm{Hg}^{2+}$ reacts with $\mathrm{SCN}^{-}$ions to form the stable $\mathrm{Hg}-\mathrm{S}$ bonded complex ion $\mathrm{Hg}(\mathrm{SCN})_{4}{ }^{2-}$. Removal of free $\mathrm{SCN}^{-}(a q)$ shifts the equilibrium $\mathrm{Fe}^{3+}(a q)+\mathrm{SCN}^{-}(a q) \rightleftharpoons \mathrm{FeNCS}^{2+}(a q)$ from right to left to replenish the $\mathrm{SCN}^{-}$ions.

## Worked Example 13.12

The reaction of iron(III) oxide with carbon monoxide occurs in a blast furnace when iron ore is reduced to iron metal:

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \rightleftharpoons 2 \mathrm{Fe}(l)+3 \mathrm{CO}_{2}(g)
$$

Use Le Châtelier's principle to predict the direction of net reaction when an equilibrium mixture is disturbed by:
(a) Adding $\mathrm{Fe}_{2} \mathrm{O}_{3}$
(b) Removing $\mathrm{CO}_{2}$
(c) Removing CO; also account for the change using the reaction quotient $Q_{c}$.

## Strategy

To predict the direction of net reaction, recall that a concentration stress is relieved by reaction in the direction that consumes an added substance or replenishes a removed substance. This rule does not apply to pure solids or pure liquids because their concentrations are constant.

## Solution

(a) Because $\mathrm{Fe}_{2} \mathrm{O}_{3}$ is a solid, its "concentration" doesn't change when more $\mathrm{Fe}_{2} \mathrm{O}_{3}$ is added. Therefore, there is no concentration stress, and the original equilibrium is undisturbed.
(b) Le Châtelier's principle predicts that the concentration stress of removed $\mathrm{CO}_{2}$ will be relieved by net reaction from left to right to replenish the $\mathrm{CO}_{2}$.
(c) Le Châtelier's principle predicts that the concentration stress of removed CO will be relieved by net reaction from right to left to replenish the CO . The reaction quotient is

$$
Q_{\mathrm{c}}=\frac{\left[\mathrm{CO}_{2}\right]_{t}^{3}}{[\mathrm{CO}]_{t}^{3}}
$$

When the equilibrium is disturbed by reducing [CO], $Q_{\mathrm{c}}$ increases, so that $Q_{\mathrm{c}}>K_{\mathrm{c}}$. For the system to move to a new state of equilibrium, $Q_{c}$ must decrease-that is, $\left[\mathrm{CO}_{2}\right]$ must decrease and [CO] must increase. Therefore, the net reaction goes from right to left, as predicted by Le Châtelier's principle.

- PROBLEM 13.16 Consider the equilibrium for the water-gas shift reaction:

$$
\mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g)
$$

Use Le Châtelier's principle to predict how the concentration of $\mathrm{H}_{2}$ will change when the equilibrium is disturbed by:
(a) Adding CO
(b) Adding $\mathrm{CO}_{2}$
(c) Removing $\mathrm{H}_{2} \mathrm{O}$
(d) Removing $\mathrm{CO}_{2}$; also account for the change using the reaction quotient $Q_{\mathrm{c}}$.

Lee R. Summerlin and James L.
Ealy, Jr., "Equilibrium in the Gas Phase" Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), p. 85-86.

Ron DeLorenzo, "From
Chicken Breath to the Killer Lakes of Cameroon: Uniting Seven Interesting Phenomena with a Single Chemical Underpinning," J. Chem. Educ., Vol. 78, 2001, 191-194.

FIGURE 13.11 Qualitative effect of pressure and volume on the equilibrium $\mathrm{N}_{2}(g)+$ $3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$. (a) A mixture of gaseous $\mathrm{N}_{2}, \mathrm{H}_{2}$, and $\mathrm{NH}_{3}$ at equilibrium. (b) When the pressure is increased by decreasing the volume, the mixture is no longer at equilibrium ( $Q_{c}<K_{c}$ ). (c) Net reaction occurs from left to right, decreasing the total number of gaseous molecules until equilibrium is re-established $\left(Q_{c}=K_{c}\right)$.

### 13.8 Altering an Equilibrium Mixture: Changes in Pressure and Volume

To illustrate how an equilibrium mixture is affected by a change in pressure as a result of a change in the volume, let's return to the Haber synthesis of ammonia. The balanced equation for the reaction has 4 mol of gas on the left side of the equation and 2 mol on the right side:

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g) \quad K_{\mathrm{c}}=0.291 \text { at } 700 \mathrm{~K}
$$

What happens to the composition of the equilibrium mixture if we increase the pressure by decreasing the volume? (Recall from Sections 9.2 and 9.3 that the pressure of an ideal gas is inversely proportional to the volume at constant temperature and constant number of moles of gas; $P=n R T / V$.) According to Le Châtelier's principle, net reaction will occur in the direction that relieves the stress of the increased pressure, which means that the number of moles of gas must decrease. Therefore, we predict that the net reaction will proceed from left to right because the forward reaction converts 4 mol of gaseous reactants to 2 mol of gaseous products.

In general, Le Châtelier's principle predicts that

- An increase in pressure by reducing the volume will bring about net reaction in the direction that decreases the number of moles of gas.
- A decrease in pressure by enlarging the volume will bring about net reaction in the direction that increases the number of moles of gas.

To see why Le Châtelier's principle works for pressure (volume) changes, let's look again at the reaction quotient for the equilibrium mixture of $0.50 \mathrm{M} \mathrm{N}_{2}$, $3.00 \mathrm{M} \mathrm{H}_{2}$, and $1.98 \mathrm{M} \mathrm{NH}_{3}$ at 700 K :

$$
Q_{\mathrm{c}}=\frac{\left[\mathrm{NH}_{3}\right]_{t}^{2}}{\left[\mathrm{~N}_{2}\right]_{t}\left[\mathrm{H}_{2}\right]_{t}^{3}}=\frac{(1.98)^{2}}{(0.50)(3.00)^{3}}=0.29=K_{\mathrm{c}}
$$

If we disturb the equilibrium by reducing the volume by a factor of 2 , we not only double the total pressure, we also double the molar concentration of each reactant and product (because molarity $=n / V$ ). Because the balanced equation has more moles of gaseous reactants than gaseous products, the increase in the denominator of the equilibrium constant expression is greater than the increase in the numerator, and the new value of $Q_{c}$ is less than the equilibrium constant $K_{\mathrm{c}}$ :

$$
Q_{c}=\frac{\left[\mathrm{NH}_{3}\right]_{t}^{2}}{\left[\mathrm{~N}_{2}\right]_{t}\left[\mathrm{H}_{2}\right]_{t}^{3}}=\frac{(3.96)^{2}}{(1.00)(6.00)^{3}}=0.0726<K_{\mathrm{c}}
$$

For the system to move to a new state of equilibrium, $Q_{c}$ must increase, which means that the net reaction must go from left to right, as predicted by Le Châtelier's principle (Figure 13.11). In practice, the yield of ammonia in the


Haber process is increased by running the reaction at high pressure, typically 130-300 atm.

The composition of an equilibrium mixture is unaffected by a change in pressure if the reaction involves no change in the number of moles of gas. For example, the reaction of hydrogen with iodine has 2 mol of gas on both sides of the balanced equation:

$$
\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g)
$$

If we double the pressure by halving the volume, the numerator and denominator of the reaction quotient change by the same factor, and $Q_{c}$ remains unchanged:

$$
Q_{\mathrm{c}}=\frac{[\mathrm{HI}]_{t}^{2}}{\left[\mathrm{H}_{2}\right]_{t}\left[\mathrm{I}_{2}\right]_{t}}
$$

In applying Le Châtelier's principle to a heterogeneous equilibrium, the effect of pressure changes on solids and liquids can be ignored because the volume (and concentration) of a solid or a liquid is nearly independent of pressure. Consider, for example, the high-temperature reaction of carbon with steam, the first step in converting coal to gaseous fuels:

$$
\mathrm{C}(s)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}(g)+\mathrm{H}_{2}(g)
$$

Ignoring the carbon because it's a solid, we predict that a decrease in volume (increase in pressure) will shift the equilibrium from right to left because the reverse reaction decreases the amount of gas from 2 mol to 1 mol .

Throughout this section, we've been careful to limit the application of Le Châtelier's principle to pressure changes that result from a change in volume. What happens, though, if we keep the volume constant but increase the total pressure by adding a gas that is not involved in the reaction-say, an inert gas such as argon? In that case, the equilibrium remains undisturbed because adding an inert gas at constant volume does not change the partial pressures or the molar concentrations of the substances involved in the reaction. Only if the added gas is a reactant or product does the reaction quotient change.

## Worked Example 13.13

Does the number of moles of reaction products increase, decrease, or remain the same when each of the following equilibria is subjected to a decrease in pressure by increasing the volume?
(a) $\mathrm{PCl}_{5}(g) \rightleftharpoons \mathrm{PCl}_{3}(g)+\mathrm{Cl}_{2}(g)$
(b) $\mathrm{CaO}(s)+\mathrm{CO}_{2}(g) \rightleftharpoons \mathrm{CaCO}_{3}(s)$
(c) $3 \mathrm{Fe}(s)+4 \mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{Fe}_{3} \mathrm{O}_{4}(s)+4 \mathrm{H}_{2}(g)$

## Strategy

According to Le Châtelier's principle, the stress of a decrease in pressure is relieved by net reaction in the direction that increases the number of moles of gas.

## Solution

(a) Since the forward reaction converts 1 mol of gas to 2 mol of gas, net reaction will go from left to right, thus increasing the number of moles of $\mathrm{PCl}_{3}$ and $\mathrm{Cl}_{2}$.
(b) Because there is 1 mol of gas on the left side of the balanced equation and none on the right side, the stress of a decrease in pressure is relieved by net reaction from right to left. The number of moles of $\mathrm{CaCO}_{3}$ therefore decreases.
(c) Because there are 4 mol of gas on both sides of the balanced equation, the composition of the equilibrium mixture is unaffected by a change in pressure. The number of moles of $\mathrm{Fe}_{3} \mathrm{O}_{4}$ and $\mathrm{H}_{2}$ remains the same.

Reed A, Howard, "The Fizz Keeper, a Case Study in Chemical Education," J. Chem. Educ., Vol. 76, 1999, 208-209.

Lee R. Summerlin and James L. Ealy, Jr., "Effect of Temperature Change on Equilibrium: Cobalt Complex" Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), p. 60-61. Concentrated hydrochloric acid is added to pink $\left[\mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ until blue $\left[\mathrm{CoCl}_{4}\right]^{-}$is formed. When heated the solution turns darker blue; when cooled the solution turns pink, indicating that the reaction is endothermic. Students are asked to examine the equilibrium reaction and predict how the system will shift upon the addition of water.

FIGURE 13.12 Temperature dependence of the equilibrium constant for the reaction $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons$ $2 \mathrm{NH}_{3}(g)$. Note that $K_{\mathrm{c}}$ is plotted on a logarithmic scale and decreases by a factor of $10^{11}$ on raising the temperature from 300 K to 1000 K .

PROBLEM 13.17 Does the number of moles of products increase, decrease, or remain the same when each of the following equilibria is subjected to an increase in pressure by decreasing the volume?
(a) $\mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g)$
(b) $2 \mathrm{CO}(g) \rightleftharpoons \mathrm{C}(s)+\mathrm{CO}_{2}(g)$
(c) $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$

KEY CONCEPT PROBLEM 13.18 The following picture represents the equilibrium mixture for the gas-phase reaction $\mathrm{A}_{2} \rightleftharpoons 2 \mathrm{~A}$.


Draw a picture that shows how the concentrations change when the pressure is increased by reducing the volume.

### 13.9 Altering an Equilibrium Mixture: Changes in Temperature

When an equilibrium is disturbed by a change in concentration, pressure, or volume, the composition of the equilibrium mixture changes because the reaction quotient $Q_{\mathrm{c}}$ no longer equals the equilibrium constant $K_{c}$. As long as the temperature remains constant, however, concentration, pressure, or volume changes don't change the value of the equilibrium constant.

By contrast, a change in temperature nearly always changes the value of the equilibrium constant. For the Haber synthesis of ammonia, which is an exothermic reaction, the equilibrium constant $K_{c}$ decreases by a factor of $10^{11}$ over the temperature range 300-1000 K (Figure 13.12).

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)+92.2 \mathrm{~kJ} \quad \Delta H^{\circ}=-92.2 \mathrm{~kJ}
$$



At low temperatures, the equilibrium mixture is rich in $\mathrm{NH}_{3}$ because $K_{\mathrm{c}}$ is large. At high temperatures, the equilibrium shifts in the direction of $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$.

In general, the temperature dependence of the equilibrium constant depends on the sign of $\Delta H^{\circ}$ for the reaction.

- The equilibrium constant for an exothermic reaction (negative $\Delta H^{\circ}$ ) decreases as the temperature increases.
- The equilibrium constant for an endothermic reaction (positive $\Delta H^{\circ}$ ) increases as the temperature increases.
If you forget the way in which $K_{c}$ depends on temperature, you can predict it using Le Châtelier's principle. Take the endothermic decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$, for example:

$$
\begin{gathered}
\mathrm{N}_{2} \mathrm{O}_{4}(g)+57.2 \mathrm{~kJ} \rightleftharpoons 2 \mathrm{NO}_{2}(g) \\
\text { Colorless } \\
\text { Brown }
\end{gathered} \quad \Delta H^{\circ}=+57.2 \mathrm{~kJ}
$$

Le Châtelier's principle says that if heat is added to an equilibrium mixture (thus increasing its temperature), net reaction occurs in the direction that relieves the stress of the added heat. For an endothermic reaction, such as the decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$, heat is absorbed by reaction in the forward direction. The equilibrium therefore shifts to the right at the higher temperature, which means that $K_{c}$ increases with increasing temperature.

Because $\mathrm{N}_{2} \mathrm{O}_{4}$ is colorless and $\mathrm{NO}_{2}$ has a brown color, the effect of temperature on the $\mathrm{N}_{2} \mathrm{O}_{4}-\mathrm{NO}_{2}$ equilibrium is readily apparent from the color of the mixture (Figure 13.13). For an exothermic reaction, such as the Haber synthesis of $\mathrm{NH}_{3}$, heat is absorbed by net reaction in the reverse direction, so $K_{c}$ decreases with increasing temperature.

## Worked Example 13.14

In the first step of the Ostwald process for the synthesis of nitric acid, ammonia is oxidized to nitric oxide by the reaction

$$
4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \rightleftharpoons 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(g) \quad \Delta H^{\circ}=-905.6 \mathrm{~kJ}
$$

How does the equilibrium amount of NO vary with an increase in temperature?

## Strategy

Le Châtelier's principle predicts that the stress of added heat when the temperature is increased will be relieved by net reaction in the direction that absorbs the heat. It's helpful to include the heat in the balanced equation-on the reactant side if the reaction is endothermic, or on the product side if the reaction is exothermic.

## Solution

Because the oxidation of ammonia is exothermic, we include the heat $(905.6 \mathrm{~kJ})$ on the product side:

$$
4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \rightleftharpoons 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(g)+905.6 \mathrm{~kJ}
$$

The stress of added heat when the temperature is increased will be relieved by net reaction from right to left, which absorbs the added heat. The equilibrium will therefore shift to the left ( $K_{c}$ will decrease) with an increase in temperature. Consequently, the equilibrium mixture will contain less NO at higher temperatures.

- PROBLEM 13.19 When air is heated at very high temperatures in an automobile engine, the air pollutant nitric oxide is produced by the reaction

$$
\mathrm{N}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}(g) \quad \Delta H^{\circ}=+180.5 \mathrm{~kJ}
$$

How does the equilibrium amount of NO vary with an increase in temperature?


- FIGURE 13.13 Sample tubes containing an equilibrium mixture of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ immersed in ice water (left) and hot water (right). The darker brown color of the sample at the higher temperature indicates that the equilibrium $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$ shifts from left to right ( $K_{\mathrm{c}}$ increases) with increasing temperature, as expected for an endothermic reaction.



A Fingernail polish can be removed by dissolving it in ethyl acetate.

FIGURE 13.14 Potential energy profiles for a reaction whose activation energy is lowered by the presence of a catalyst. The activation energy for the catalyzed pathway (red curve) is lower than that for the uncatalyzed pathway (blue curve) by an amount $\Delta E_{\mathrm{a}}$. The catalyst lowers the activation energy barrier for the forward and reverse reactions by exactly the same amount. The catalyst therefore accelerates the forward and reverse reactions by the same factor, and the composition of the equilibrium mixture is unchanged.

PROBLEM 13.20 Ethyl acetate, a solvent used as fingernail-polish remover, is made by reaction of acetic acid with ethanol:

$$
\begin{array}{ccc}
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\text { soln })+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\text { soln }) & \rightleftharpoons \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{C}_{2} \mathrm{H}_{5}(\text { soln }) & +\mathrm{H}_{2} \mathrm{O}(\text { soln }) \\
\text { Acetic acid } & \text { Ethanol } & \text { Ethyl acetate }
\end{array} \Delta \mathrm{H}^{\circ}=-2.9 \mathrm{~kJ}
$$

Does the amount of ethyl acetate in an equilibrium mixture increase or decrease when the temperature is increased? How does $K_{c}$ change when the temperature is decreased? Justify your answers using Le Châtelier's principle.

KEY CONCEPT PROBLEM 13.21 The following pictures represent the composition of the equilibrium mixture for the reaction $\mathrm{A}(g)+\mathrm{B}(s) \rightleftharpoons \mathrm{AB}(g)$ at 400 K and $500 \mathrm{~K}:$

$T=400 \mathrm{~K}$

$T=500 \mathrm{~K}$

Is the reaction endothermic or exothermic? Explain using Le Châtelier's principle.

### 13.10 The Effect of a Catalyst on Equilibrium

Recall from Section 12.12 that a catalyst increases the rate of a chemical reaction by making available a new, lower-energy pathway for conversion of reactants to products. Because the forward and reverse reactions pass through the same transition state, a catalyst lowers the activation energy for the forward and reverse reactions by exactly the same amount. As a result, the rates of the forward and reverse reactions increase by the same factor (Figure 13.14).


If a reaction mixture is at equilibrium in the absence of a catalyst (that is, the forward and reverse rates are equal), it will still be at equilibrium after a catalyst is added because the forward and reverse rates, though faster, remain equal. If a reac-
tion mixture is not at equilibrium, a catalyst accelerates the rate at which equilibrium is reached but it does not affect the composition of the equilibrium mixture. Because a catalyst has no effect on the equilibrium concentrations, it does not appear in the balanced chemical equation or in the equilibrium constant expression.

Even though it doesn't change the position of an equilibrium, a catalyst can nevertheless significantly influence the choice of optimum conditions for a reaction. Consider again the Haber synthesis of ammonia. Because the reaction $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$ is exothermic, its equilibrium constant decreases with increasing temperature, and optimum yields of $\mathrm{NH}_{3}$ are obtained at low temperatures. At those low temperatures, however, the rate at which equilibrium is reached is too slow for the reaction to be practical. We thus have what appears to be a no-win situation: Low temperatures give good yields but slow rates, whereas high temperatures give satisfactory rates but poor yields. The answer to the dilemma is to find a catalyst.

In the early 1900s, the German chemist Fritz Haber discovered that a catalyst consisting of iron mixed with certain metal oxides causes the reaction to occur at a satisfactory rate at temperatures where the equilibrium concentration of $\mathrm{NH}_{3}$ is reasonably favorable. The yield of $\mathrm{NH}_{3}$ can be improved further by running the reaction at high pressures. Typical reaction conditions for the industrial synthesis of ammonia are $400-500^{\circ} \mathrm{C}$ and 130-300 atm.

- PROBLEM 13.22 A platinum catalyst is used in automobile catalytic converters to hasten the oxidation of carbon monoxide:

$$
2 \mathrm{CO}(g)+\mathrm{O}_{2}(g) \stackrel{\mathrm{Pt}}{\rightleftharpoons} 2 \mathrm{CO}_{2}(g) \quad \Delta \mathrm{H}^{\circ}=-566 \mathrm{~kJ}
$$

Suppose that you have a reaction vessel containing an equilibrium mixture of $\mathrm{CO}(g), \mathrm{O}_{2}(g)$, and $\mathrm{CO}_{2}(g)$. Will the amount of CO increase, decrease, or remain the same when:
(a) A platinum catalyst is added
(b) The temperature is increased
(c) The pressure is increased by decreasing the volume
(d) The pressure is increased by adding argon gas
(e) The pressure is increased by adding $\mathrm{O}_{2}$ gas

### 13.11 The Link Between Chemical Equilibrium and Chemical Kinetics

We emphasized in Section 13.1 that the equilibrium state is a dynamic one in which reactant and product concentrations remain constant, not because the reaction stops, but because the rates of the forward and reverse reactions are equal. To explore this idea further, let's consider the general, reversible reaction

$$
\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}+\mathrm{D}
$$

Let's assume that the forward and reverse reactions occur in a single bimolecular step; that is, they are elementary reactions (Section 12.8). We can then write the following rate laws:

$$
\begin{aligned}
\text { Rate of forward reaction } & =k_{\mathrm{f}}[\mathrm{~A}][\mathrm{B}] \\
\text { Rate of reverse reaction } & =k_{\mathrm{r}}[\mathrm{C}][\mathrm{D}]
\end{aligned}
$$

If we begin with a mixture that contains all reactants and no products, the initial rate of the reverse reaction is zero because $[C]=[D]=0$. As A and B are converted to $C$ and $D$ by the forward reaction, the rate of the forward reaction decreases because [A] and [B] are getting smaller. At the same time, the rate of the

vThe addition of a catalyst equally affects the rate of the forward and of the reverse reaction; hence, a catalyst does not change the equilibrium mixture or the value of the equilibrium constant, K.
reverse reaction increases because [C] and [D] are getting larger. Eventually, the rates of the forward and reverse reactions become equal, and thereafter the concentrations remain constant; that is, the system is at chemical equilibrium.

Because the forward and reverse rates are equal at equilibrium, we can write

$$
k_{\mathrm{f}}[\mathrm{~A}][\mathrm{B}]=k_{\mathrm{r}}[\mathrm{C}][\mathrm{D}] \quad \text { at equilibrium }
$$

which can be rearranged to give

$$
\frac{k_{\mathrm{f}}}{k_{\mathrm{r}}}=\frac{[\mathrm{C}][\mathrm{D}]}{[\mathrm{A}][\mathrm{B}]}
$$

The right side of this equation is the equilibrium constant expression for the forward reaction, which equals the equilibrium constant $K_{c}$ since the reaction mixture is at equilibrium.

$$
K_{\mathrm{c}}=\frac{[\mathrm{C}][\mathrm{D}]}{[\mathrm{A}][\mathrm{B}]}
$$

Therefore, the equilibrium constant is simply the ratio of the rate constants for the forward and reverse reactions:

$$
K_{\mathrm{c}}=\frac{k_{\mathrm{f}}}{k_{\mathrm{r}}}
$$

In deriving this equation for $K_{c}$, we have assumed a single-step mechanism. For a multistep mechanism, each step has a characteristic rate constant ratio, $k_{f} / k_{r}$. When equilibrium is reached, each step in the mechanism must be at equilibrium, and $K_{c}$ for the overall reaction is equal to the product of the rate constant ratios for the individual steps.

The equation relating $K_{\mathrm{c}}$ to $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ provides a fundamental link between chemical equilibrium and chemical kinetics: The relative values of the rate constants for the forward and reverse reactions determine the composition of the equilibrium mixture. When $k_{\mathrm{f}}$ is much larger than $k_{\mathrm{r}}, K_{\mathrm{c}}$ is very large and the reaction goes almost to completion. Such a reaction is said to be irreversible because the reverse reaction is often too slow to be detected. When $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ have comparable values, $K_{c}$ has a value near unity, and comparable concentrations of both reactants and products are present at equilibrium. This is the usual situation for a reversible reaction.

Addition of a catalyst to a reaction mixture increases both rate constants $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ because the reaction takes place by a different, lower-energy mechanism. Because $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ increase by the same factor, though, the ratio $k_{\mathrm{f}} / k_{\mathrm{r}}$ is unaffected, and the value of the equilibrium constant $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$ remains unchanged. Thus, addition of a catalyst does not alter the composition of an equilibrium mixture.

The equation $K_{c}=k_{f} / k_{r}$ also helps explain why equilibrium constants depend on temperature. Recall from Section 12.10 that rate constants increase as the temperature increases, in accord with the Arrhenius equation $k=A e^{-E_{\mathrm{a}} / R T}$. In general, the forward and reverse reactions have different values of the activation energy, so $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ increase by different amounts as the temperature increases. The ratio $k_{\mathrm{f}} / k_{\mathrm{r}}=K_{\mathrm{c}}$ is therefore temperature-dependent. For an exothermic reaction, which has $\Delta E=E_{\mathrm{a}}($ forward $)-E_{\mathrm{a}}($ reverse $)<0, E_{\mathrm{a}}$ (reverse) is greater than $E_{\mathrm{a}}$ (forward). Consequently, $k_{\mathrm{r}}$ increases by more than $k_{\mathrm{f}}$ increases as the temperature increases, and so $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$ for an exothermic reaction decreases as the temperature increases. Conversely, $K_{c}$ for an endothermic reaction increases as the temperature increases.

## Worked Example 13.15

The equilibrium constant $K_{c}$ for the reaction of hydrogen with iodine is 57.0 at 700 K , and the reaction is endothermic $(\Delta E=9 \mathrm{~kJ})$.

$$
\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \underset{k_{\mathrm{r}}}{\stackrel{k_{\mathrm{f}}}{\rightleftharpoons}} 2 \mathrm{HI}(g) \quad K_{\mathrm{c}}=57.0 \text { at } 700 \mathrm{~K}
$$

(a) Is the rate constant $k_{\mathrm{f}}$ for the formation of HI larger or smaller than the rate constant $k_{\mathrm{r}}$ for the decomposition of HI ?
(b) The value of $k_{\mathrm{r}}$ at 700 K is $1.16 \times 10^{-3} \mathrm{M}^{-1} \mathrm{~s}^{-1}$. What is the value of $k_{\mathrm{f}}$ at the same temperature?
(c) How are the values of $k_{\mathrm{f}}, k_{\mathrm{r}}$, and $K_{\mathrm{c}}$ affected by the addition of a catalyst?
(d) How are the values of $k_{\mathrm{f}}, k_{\mathrm{r}}$, and $K_{\mathrm{c}}$ affected by an increase in temperature?

## Strategy

To answer these questions, make use of the relationship $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$. Also, remember that a catalyst increases $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ by the same factor, and recall that the temperature dependence of a rate constant increases with increasing value of the activation energy (Section 12.11).

## Solution

(a) Because $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}=57.0$, the rate constant for the formation of HI (forward reaction) is larger than the rate constant for the decomposition of HI (reverse reaction) by a factor of 57.0.
(b) Since $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$,

$$
k_{\mathrm{f}}=\left(K_{\mathrm{c}}\right)\left(k_{\mathrm{r}}\right)=(57.0)\left(1.16 \times 10^{-3} \mathrm{M}^{-1} \mathrm{~s}^{-1}\right)=6.61 \times 10^{-2} \mathrm{M}^{-1} \mathrm{~s}^{-1}
$$

(c) A catalyst lowers the activation energy barrier for the forward and reverse reactions by the same amount, thus increasing the rate constants $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ by the same factor. Because the equilibrium constant $K_{c}$ equals the ratio of $k_{\mathrm{f}}$ to $k_{\mathrm{r}}$, the value of $K_{\mathrm{c}}$ is unaffected by the addition of a catalyst.
(d) Because the reaction is endothermic, $E_{\mathrm{a}}$ (forward) is greater than $E_{\mathrm{a}}$ (reverse). Consequently, as the temperature increases, $k_{\mathrm{f}}$ increases by more than $k_{\mathrm{r}}$ increases, and therefore $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$ increases. This result is consistent with Le Châtelier's principle.

PROBLEM 13.23 Nitric oxide emitted from the engines of supersonic transport planes can contribute to the destruction of stratospheric ozone:

$$
\mathrm{NO}(g)+\mathrm{O}_{3}(g) \underset{k_{\mathrm{r}}}{\stackrel{k_{\mathrm{f}}}{\rightleftharpoons}} \mathrm{NO}_{2}(g)+\mathrm{O}_{2}(g)
$$

This reaction is highly exothermic $(\Delta E=-200 \mathrm{~kJ})$, and its equilibrium constant $K_{\mathrm{c}}$ is $3.4 \times 10^{34}$ at 300 K .
(a) Which rate constant is larger, $k_{\mathrm{f}}$ or $k_{\mathrm{r}}$ ?
(b) The value of $k_{\mathrm{f}}$ at 300 K is $8.5 \times 10^{6} \mathrm{M}^{-1} \mathrm{~s}^{-1}$. What is the value of $k_{\mathrm{r}}$ at the same temperature?
(c) A typical temperature in the stratosphere is 230 K . Do the values of $k_{\mathrm{f}}, k_{\mathrm{r}}$, and $K_{\mathrm{c}}$ increase or decrease when the temperature is lowered from 300 K to 230 K ?


- Nitric oxide emissions from supersonic aircraft can contribute to destruction of the ozone layer.


## Interlude

## Breathing and Oxygen Transport

| TABLE 13.2 | Partial <br> Pressure of |
| :--- | :--- |
| Oxygen in the Lungs and <br> Blood at Sea Level |  |
| Source | $\mathbf{P}_{\mathbf{O}_{\mathbf{2}}}$ <br> $\mathbf{( m m} \mathbf{H g})$ |
| Dry air | 159 |
| Alveolar air | 100 |
| Arterial blood | 95 |
| Venous blood | 40 |

Humans, like all animals, need oxygen. The oxygen comes, of course, from breathing: About 500 mL of air is drawn into the lungs of an average person with each breath. When the freshly inspired air travels through the bronchial passages and enters the approximately 150 million alveolar sacs of the lungs, it picks up moisture and mixes with air remaining from the previous breath. As it mixes, the concentrations of both water vapor and carbon dioxide increase. These gas concentrations are measured by their partial pressures (Section 9.5), with the partial pressure of oxygen in the lungs usually around 100 mm Hg (Table 13.2). Oxygen then diffuses through the delicate walls of the lung alveoli and into arterial blood, which transports it to all body tissues.

Only about $3 \%$ of the oxygen in blood is dissolved; the rest is chemically bound to hemoglobin molecules ( Hb ), large proteins that contain heme groups embedded in them. Each hemoglobin molecule contains four heme groups, and each heme group contains an iron atom that is able to bind to one $\mathrm{O}_{2}$ molecule. Thus, a single hemoglobin molecule can bind four molecules of oxygen.



Heme - an $\mathrm{O}_{2}$ molecule binds
to the central iron atom.

The entire system of oxygen transport and delivery in the body depends on the pickup and release of $\mathrm{O}_{2}$ by hemoglobin according to the following series of equilibria:

$$
\begin{aligned}
& \mathrm{Hb}+\mathrm{O}_{2} \rightleftharpoons \mathrm{Hb}\left(\mathrm{O}_{2}\right) \\
& \mathrm{Hb}\left(\mathrm{O}_{2}\right)+\mathrm{O}_{2} \rightleftharpoons \mathrm{Hb}\left(\mathrm{O}_{2}\right)_{2} \\
& \mathrm{Hb}\left(\mathrm{O}_{2}\right)_{2}+\mathrm{O}_{2} \rightleftharpoons \mathrm{Hb}\left(\mathrm{O}_{2}\right)_{3} \\
& \mathrm{Hb}\left(\mathrm{O}_{2}\right)_{3}+\mathrm{O}_{2} \rightleftharpoons \mathrm{Hb}\left(\mathrm{O}_{2}\right)_{4}
\end{aligned}
$$

The positions of the different equilibria depend on the partial pressures of $\mathrm{O}_{2}\left(P_{\mathrm{O}_{2}}\right)$ in the various tissues. In hard-working, oxygen-starved muscles, where $P_{\mathrm{O}_{2}}$ is low, oxygen is released from hemoglobin as the equilibria shift toward the left, according to Le Châtelier's principle. In the lungs, where $P_{\mathrm{O}_{2}}$ is high, oxygen is absorbed by hemoglobin as the equilibria shift toward the right.

The amount of oxygen carried by hemoglobin at any given value of $P_{\mathrm{O}_{2}}$ is usually expressed as a percent saturation and can be found from the curve shown in Figure 13.15. The saturation is $97.5 \%$ in the lungs, where $P_{\mathrm{O}_{2}}=100 \mathrm{~mm} \mathrm{Hg}$, meaning that each hemoglobin molecule is carrying close to its maximum possible amount of $4 \mathrm{O}_{2}$ molecules. When $P_{\mathrm{O}_{2}}=26 \mathrm{~mm} \mathrm{Hg}$, however, the saturation drops to $50 \%$.


What about people who live at high altitudes? In Leadville, Colorado, for example, where the altitude is $10,156 \mathrm{ft}$, the partial pressure of $\mathrm{O}_{2}$ in the lungs is only about 68 mm Hg . Hemoglobin is only $90 \%$ saturated with $\mathrm{O}_{2}$ at this pressure, so less oxygen is available for delivery to the tissues. People who climb suddenly from sea level to high altitude thus experience a feeling of oxygen deprivation, or hypoxia, as their bodies are unable to supply enough oxygen to tissues. The body soon copes with the situation, though, by producing more hemoglobin molecules, which both provide more capacity for $\mathrm{O}_{2}$ transport and also drive the $\mathrm{Hb}+\mathrm{O}_{2}$ equilibria to the right. The time required to adapt to the lower $\mathrm{O}_{2}$ pressures is typically days to weeks, so athletes and hikers must train at high altitudes for some time.

PROBLEM 13.24 The affinity of hemoglobin ( Hb ) for CO is greater than its affinity for $\mathrm{O}_{2}$. Use Le Châtelier's principle to predict how CO affects the equilibrium $\mathrm{Hb}+\mathrm{O}_{2} \rightleftharpoons \mathrm{Hb}\left(\mathrm{O}_{2}\right)$. Suggest a reason for the toxicity of CO .

- PROBLEM 13.25 In which direction does the equilibrium $\mathrm{Hb}+\mathrm{O}_{2} \rightleftharpoons \mathrm{Hb}\left(\mathrm{O}_{2}\right)$ shift on taking an elevator to the top of the Empire State Building? Explain.
- PROBLEM 13.26 The inner core of the heme group, which consists of 20 C atoms and 4 N atoms, is planar. Just as the $\pi$ electrons in the ozone molecule are delocalized over all three O atoms, so the $\pi$ electrons of the heme group are delocalized over all 24 atoms in the inner core. How many $\pi$ electrons are there in the inner core? (Be careful when counting the $\pi$ electrons on the N atoms.)
- PROBLEM 13.27 How many $\mathrm{O}_{2}$ molecules are drawn into the lungs of an average person with each breath? Assume that the ambient air temperature is $25^{\circ} \mathrm{C}$.


A The bodies of mountain dwellers produce increased amounts of hemoglobin to cope with the low $\mathrm{O}_{2}$ pressures at high altitudes.

Summary

Chemical equilibrium is a dynamic state in which the concentrations of reactants and products remain constant because the rates of the forward and reverse reactions are equal. For the general reaction $a \mathrm{~A}+b \mathrm{~B} \rightleftharpoons c \mathrm{C}+d \mathrm{D}$, concentrations in the equilibrium mixture are related by the equilibrium equation:

$$
K_{\mathrm{c}}=\frac{[\mathrm{C}]^{c}[\mathrm{D}]^{d}}{[\mathrm{~A}]^{a}[\mathrm{~B}]^{b}}
$$

The quotient on the right side of the equation is called the equilibrium constant expression. The equilibrium constant $K_{c}$ is the number obtained when equilibrium concentrations (in $\mathrm{mol} / \mathrm{L}$ ) are substituted into the equilibrium constant expression. The value of $K_{c}$ varies with temperature and depends on the form of the balanced chemical equation.

The equilibrium constant $K_{\mathrm{p}}$ can be used for gas-phase reactions. It is defined in the same way as $K_{c}$ except that the equilibrium constant expression contains partial pressures (in atmospheres) instead of molar concentrations. The constants $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ are related by the equation $K_{\mathrm{p}}=K_{\mathrm{c}}(R T)^{\Delta n}$, where $\Delta n=(c+d)-(a+b)$.

Homogeneous equilibria are those in which all reactants and products are in a single phase; heterogeneous equilibria are those in which reactants and products are present in more than one phase. The equilibrium equation for a heterogeneous equilibrium does not include concentrations of pure solids or pure liquids.

The value of the equilibrium constant for a reaction makes it possible to judge the extent of reaction, predict the direction of reaction, and calculate equilibrium concentrations (or partial pressures) from initial concentrations (or partial pressures). The farther the reaction proceeds toward completion, the larger the value of $K_{\mathrm{c}}$. The direction of a reaction not at equilibrium depends on the relative values of $K_{c}$ and the reaction quotient $Q_{c}$, which is defined in the same way as $K_{c}$ except that the concentrations in the equilibrium constant expression are not necessarily equilibrium concentrations. If $Q_{\mathrm{c}}<K_{\mathrm{c}}$, net reaction goes from left to right to attain equilibrium; if $Q_{c}>K_{c}$, net reaction goes from right to left; if $Q_{\mathrm{c}}=K_{\mathrm{c}}$, the system is at equilibrium.

The composition of an equilibrium mixture can be altered by changes in concentration, pressure (volume), or temperature. The qualitative effect of these changes is predicted by Le Châtelier's principle, which says that if a stress is applied to a reaction mixture at equilibrium, net reaction occurs in the direction that relieves the stress. Temperature changes affect equilibrium concentrations because $K_{c}$ is temperature-dependent. As the temperature increases, $K_{c}$ for an exothermic reaction decreases, and $K_{c}$ for an endothermic reaction increases.

A catalyst increases the rate at which chemical equilibrium is reached, but it does not affect the equilibrium constant or the equilibrium concentrations. The equilibrium constant for a single-step reaction equals the ratio of the rate constants for the forward and reverse reactions: $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$.

## Key Words

chemical equilibrium 528<br>equilibrium constant $K_{c}$ 531<br>equilibrium constant $K_{p}$ 535

## equilibrium equation 531 <br> equilibrium mixture 528

## heterogeneous

equilibria 537
homogeneous equilibria 537

## Le Châtelier's principle 548 reaction quotient $Q_{c}$ 541

## Key Concept Summary



## Understanding Key Concepts

Problems 13.1-13.27 appear within the chapter.
13.28 Consider the interconversion of A molecules (red spheres) and B molecules (blue spheres) according to the reaction $A \rightleftharpoons B$. Each of the following series of pictures represents a separate experiment in which time increases from left to right:

(a) Which of the experiments has resulted in an equilibrium state?
(b) What is the value of the equilibrium constant $K_{c}$ for the reaction $\mathrm{A} \rightleftharpoons \mathrm{B}$ ?
(c) Explain why you can calculate $K_{\mathrm{c}}$ without knowing the volume of the reaction vessel.
13.29 The following pictures represent the equilibrium state for three different reactions of the type $\mathrm{A}_{2}+$ $\mathrm{X}_{2} \rightleftharpoons 2 \mathrm{AX}(\mathrm{X}=\mathrm{B}, \mathrm{C}$, or D$)$ :

(a) Which reaction has the largest equilibrium constant?
(b) Which reaction has the smallest equilibrium constant?
13.30 The reaction $\mathrm{A}_{2}+\mathrm{B} \rightleftharpoons \mathrm{A}+\mathrm{AB}$ has an equilibrium constant $K_{c}=2$. The following pictures represent reaction mixtures that contain A atoms (red), B atoms (blue), and $\mathrm{A}_{2}$ and AB molecules:

(1)

(2)

(3)
(a) Which reaction mixture is at equilibrium?
(b) For those mixtures that are not at equilibrium, will the reaction go in the forward or reverse direction to reach equilibrium?
13.31 The following pictures represent the initial state and the equilibrium state for the reaction of $\mathrm{A}_{2}$ molecules (red) with $B$ atoms (blue) to give $A B$ molecules:


Initial state


Equilibrium state
(a) Write a balanced chemical equation for the reaction.
(b) If the volume of the equilibrium mixture is decreased, will the number of AB molecules increase, decrease, or remain the same? Explain.
13.32 Consider the reaction $A+B \rightleftharpoons A B$. The vessel on the right contains an equilibrium mixture of A molecules (red spheres), B molecules (blue spheres), and AB molecules. If the stopcock is opened and the contents of the two vessels are allowed to mix, will the reaction go in the forward or reverse direction? Explain.

13.33 The following pictures represent the composition of the equilibrium mixture for the reaction $A+B \rightleftharpoons A B$ at 300 K and at 400 K :


Is the reaction exothermic or endothermic? Explain using Le Châtelier's principle.
13.34 The following pictures represent equilibrium mixtures at 325 K and 350 K for a reaction involving A atoms (red), $B$ atoms (blue), and AB molecules:

(a) Write a balanced equation for the reaction that occurs on raising the temperature.
(b) Is the reaction exothermic or endothermic? Explain using Le Châtelier's principle.
(c) If the volume of the container is increased, will the number of A atoms increase, decrease, or remain the same? Explain.
13.35 The following picture represents an equilibrium mixture of solid $\mathrm{BaCO}_{3}$, solid BaO , and gaseous $\mathrm{CO}_{2}$ obtained as a result of the endothermic decomposition of $\mathrm{BaCO}_{3}$ :

(a) Draw a picture that represents the equilibrium mixture after addition of four more $\mathrm{CO}_{2}$ molecules.
(b) Draw a picture that represents the equilibrium mixture at a higher temperature.
13.36 The following picture represents the composition of the equilibrium mixture for the endothermic reaction $\mathrm{A}_{2} \rightleftharpoons 2 \mathrm{~A}$ at 500 K :


Draw a picture that represents the equilibrium mixture after each of the following changes:
(a) Adding a catalyst
(b) Increasing the volume
(c) Decreasing the temperature
13.37 The following picture represents the equilibrium state for the reaction $2 \mathrm{AB} \rightleftharpoons \mathrm{A}_{2}+\mathrm{B}_{2}$ :


Which rate constant is larger, $k_{\mathrm{f}}$ or $k_{\mathrm{r}}$ ? Explain.

## Additional Problems

## Equilibrium Expressions and Equilibrium Constants

13.38 For each of the following equilibria, write the equilibrium constant expression for $K_{\mathrm{c}}$ :
(a) $\mathrm{CH}_{4}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}(g)+3 \mathrm{H}_{2}(g)$
(b) $3 \mathrm{~F}_{2}(g)+\mathrm{Cl}_{2}(g) \rightleftharpoons 2 \mathrm{ClF}_{3}(g)$
(c) $\mathrm{H}_{2}(g)+\mathrm{F}_{2}(g) \rightleftharpoons 2 \mathrm{HF}(g)$
13.39 For each of the following equilibria, write the equilibrium constant expression for $K_{c}$ :
(a) $2 \mathrm{C}_{2} \mathrm{H}_{4}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{CH}_{3} \mathrm{CHO}(g)$
(b) $2 \mathrm{NO}(g) \rightleftharpoons \mathrm{N}_{2}(g)+\mathrm{O}_{2}(g)$
(c) $4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \rightleftharpoons 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(g)$
13.40 For each of the equilibria in Problem 13.38, write the equilibrium constant expression for $K_{p}$ and give the equation that relates $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$.
13.41 For each of the equilibria in Problem 13.39, write the equilibrium constant expression for $K_{p}$ and give the equation that relates $K_{p}$ and $K_{c}$.
13.42 Diethyl ether, used as an anesthetic, is synthesized by heating ethanol with concentrated sulfuric acid. Write the equilibrium constant expression for $K_{\mathrm{c}}$.
$2 \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}($ soln $) \rightleftharpoons \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OC}_{2} \mathrm{H}_{5}($ soln $)+\mathrm{H}_{2} \mathrm{O}($ soln $)$
Ethanol Diethyl ether
13.43 Ethylene glycol, used as antifreeze in automobile radiators, is manufactured by hydration of ethylene oxide. Write the equilibrium constant expression for $K_{c}$.

13.44 Write the equilibrium constant expression for $K_{c}$ for the following metabolic reaction:

13.45 Write the equilibrium constant expression for $K_{c}$ for the following metabolic reaction:

13.46 If $K_{c}=7.5 \times 10^{-9}$ at 1000 K for the reaction $\mathrm{N}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}(g)$, what is $K_{\mathrm{c}}$ at 1000 K for the reaction $2 \mathrm{NO}(g) \rightleftharpoons \mathrm{N}_{2}(g)+\mathrm{O}_{2}(g)$ ?
13.47 At $400 \mathrm{~K}, K_{\mathrm{p}}=50.2$ for the reaction $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons$ $2 \mathrm{NO}_{2}(g)$. What is $K_{\mathrm{p}}$ at 400 K for the reaction $2 \mathrm{NO}_{2}(g) \rightleftharpoons \mathrm{N}_{2} \mathrm{O}_{4}(g)$ ?
13.48 An equilibrium mixture of $\mathrm{PCl}_{5}, \mathrm{PCl}_{3}$, and $\mathrm{Cl}_{2}$ at a certain temperature contains $8.3 \times 10^{-3} \mathrm{M} \mathrm{PCl}_{5}$, $1.5 \times 10^{-2} \mathrm{M} \mathrm{PCl}_{3}$, and $3.2 \times 10^{-2} \mathrm{M} \mathrm{Cl}_{2}$. Calculate the equilibrium constant $K_{\mathrm{c}}$ for the reaction $\mathrm{PCl}_{5}(g) \rightleftharpoons$ $\mathrm{PCl}_{3}(g)+\mathrm{Cl}_{2}(g)$.
13.49 The partial pressures in an equilibrium mixture of NO , $\mathrm{Cl}_{2}$, and NOCl at 500 K are as follows: $P_{\mathrm{NO}}=$ $0.240 \mathrm{~atm} ; P_{\mathrm{Cl}_{2}}=0.608 \mathrm{~atm} ; P_{\mathrm{NOCl}}=1.35 \mathrm{~atm}$. What is $K_{\mathrm{p}}$ at 500 K for the reaction $2 \mathrm{NO}(g)+\mathrm{Cl}_{2}(g) \rightleftharpoons$ $2 \mathrm{NOCl}(g)$ ?
13.50 A sample of $\mathrm{HI}\left(9.30 \times 10^{-3} \mathrm{~mol}\right)$ was placed in an empty 2.00 L container at 1000 K . After equilibrium was reached, the concentration of $\mathrm{I}_{2}$ was $6.29 \times 10^{-4} \mathrm{M}$. Calculate the value of $K_{c}$ at 1000 K for the reaction $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g)$.
13.51 Vinegar contains acetic acid, a weak acid that is partially dissociated in aqueous solution:
$\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)$
(a) Write the equilibrium constant expression for $K_{\mathrm{c}}$.
(b) What is the value of $K_{c}$ if the extent of dissociation in $1.0 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ is $0.42 \%$ ?
13.52 The industrial solvent ethyl acetate is produced by reaction of acetic acid with ethanol:

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\text { soln })+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\text { soln }) \rightleftharpoons
$$

Acetic acid
Ethanol

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{C}_{2} \mathrm{H}_{5}(\text { soln })+\mathrm{H}_{2} \mathrm{O}(\text { soln })
$$

Ethyl acetate
(a) Write the equilibrium constant expression for $K_{\mathrm{c}}$.
(b) A solution prepared by mixing 1.00 mol of acetic acid and 1.00 mol of ethanol contains 0.65 mol of ethyl acetate at equilibrium. Calculate the value of $K_{c}$. Explain why you can calculate $K_{c}$ without knowing the volume of the solution.
13.53 A characteristic reaction of ethyl acetate is hydrolysis, the reverse of the reaction in Problem 13.52. Write the equilibrium equation for hydrolysis of ethyl acetate, and use the data in Problem 13.52 to calculate $K_{c}$ for the hydrolysis reaction.
13.54 At $500 \mathrm{~K}, K_{\mathrm{c}}=0.575$ for the reaction $\mathrm{PCl}_{5}(g) \rightleftharpoons$ $\mathrm{PCl}_{3}(g)+\mathrm{Cl}_{2}(g)$. What is $K_{\mathrm{p}}$ at the same temperature?
13.55 One step in the manufacture of sulfuric acid is the oxidation of sulfur dioxide, $2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{SO}_{3}(g)$. If $K_{\mathrm{p}}$ for this reaction is 3.30 at 1000 K , what is the value of $K_{\mathrm{c}}$ at the same temperature?
13.56 The vapor pressure of water at $25^{\circ} \mathrm{C}$ is 0.0313 atm . Calculate the values of $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ at $25^{\circ} \mathrm{C}$ for the equilibrium $\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{2} \mathrm{O}(g)$.
13.57 Naphthalene, a white solid used to make mothballs, has a vapor pressure of 0.10 mm Hg at $27^{\circ} \mathrm{C}$. Calculate the values of $K_{p}$ and $K_{c}$ at $27^{\circ} \mathrm{C}$ for the equilibrium $\mathrm{C}_{10} \mathrm{H}_{8}(\mathrm{~s}) \rightleftharpoons \mathrm{C}_{10} \mathrm{H}_{8}(g)$.
13.58 For each of the following equilibria, write the equilibrium constant expression for $K_{c}$. Where appropriate, also write the equilibrium constant expression for $K_{p}$.
(a) $\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \rightleftharpoons 2 \mathrm{Fe}(l)+3 \mathrm{CO}_{2}(g)$
(b) $4 \mathrm{Fe}(s)+3 \mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{Fe}_{2} \mathrm{O}_{3}(s)$
(c) $\mathrm{BaSO}_{4}(s) \rightleftharpoons \mathrm{BaO}(s)+\mathrm{SO}_{3}(g)$
(d) $\mathrm{BaSO}_{4}(s) \rightleftharpoons \mathrm{Ba}^{2+}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q)$
13.59 For each of the following equilibria, write the equilibrium constant expression for $K_{c}$. Where appropriate, also write the equilibrium constant expression for $K_{\mathrm{p}}$.
(a) $\mathrm{WO}_{3}(s)+3 \mathrm{H}_{2}(g) \rightleftharpoons \mathrm{W}(s)+3 \mathrm{H}_{2} \mathrm{O}(g)$
(b) $\mathrm{Ag}^{+}(a q)+\mathrm{Cl}^{-}(a q) \rightleftharpoons \mathrm{AgCl}(s)$
(c) $2 \mathrm{FeCl}_{3}(s)+3 \mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{Fe}_{2} \mathrm{O}_{3}(s)+6 \mathrm{HCl}(g)$
(d) $\mathrm{MgCO}_{3}(s) \rightleftharpoons \mathrm{MgO}(s)+\mathrm{CO}_{2}(g)$

## Using the Equilibrium Constant

13.60 When the following reactions come to equilibrium, does the equilibrium mixture contain mostly reactants or mostly products?
(a) $\mathrm{H}_{2}(g)+\mathrm{S}(\mathrm{s}) \rightleftharpoons \mathrm{H}_{2} \mathrm{~S}(g) ; \mathrm{K}_{\mathrm{c}}=7.8 \times 10^{5}$
(b) $\mathrm{N}_{2}(g)+2 \mathrm{H}_{2}(g) \rightleftharpoons \mathrm{N}_{2} \mathrm{H}_{4}(g) ; K_{\mathrm{c}}=7.4 \times 10^{-26}$
13.61 Which of the following reactions goes almost all the way to completion, and which proceeds hardly at all?
(a) $\mathrm{N}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}(g) ; K_{\mathrm{c}}=2.7 \times 10^{-18}$
(b) $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g) ; K_{\mathrm{c}}=6.0 \times 10^{13}$
13.62 For which of the following reactions will the equilibrium mixture contain an appreciable concentration of both reactants and products?
(a) $\mathrm{Cl}_{2}(g) \rightleftharpoons 2 \mathrm{Cl}(g) ; K_{\mathrm{c}}=6.4 \times 10^{-39}$
(b) $\mathrm{Cl}_{2}(g)+2 \mathrm{NO}(g) \rightleftharpoons 2 \mathrm{NOCl}(g) ; \quad K_{\mathrm{c}}=3.7 \times 10^{8}$
(c) $\mathrm{Cl}_{2}(g)+2 \mathrm{NO}_{2}(g) \rightleftharpoons 2 \mathrm{NO}_{2} \mathrm{Cl}(g) ; K_{\mathrm{c}}=1.8$
13.63 Which of the following reactions yield appreciable equilibrium concentrations of both reactants and products?
(a) $2 \mathrm{Cu}(s)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{CuO}(s) ; K_{\mathrm{c}}=4 \times 10^{45}$
(b) $\mathrm{H}_{3} \mathrm{PO}_{4}(a q) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{H}_{2} \mathrm{PO}_{4}^{-}(a q)$;

$$
K_{\mathrm{c}}=7.5 \times 10^{-3}
$$

(c) $2 \operatorname{HBr}(g) \rightleftharpoons \mathrm{H}_{2}(g)+\mathrm{Br}_{2}(g) ; K_{\mathrm{c}}=2 \times 10^{-19}$
13.64 When wine spoils, ethanol is oxidized to acetic acid as $\mathrm{O}_{2}$ from the air reacts with the wine:

$$
\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(a q)+\mathrm{O}_{2}(a q) \rightleftharpoons \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Ethanol
Acetic acid
The value of $K_{c}$ for this reaction at $25^{\circ} \mathrm{C}$ is $1.2 \times 10^{82}$. Will much ethanol remain when the reaction has reached equilibrium? Explain.
13.65 The value of $K_{\text {c }}$ for the reaction $3 \mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{O}_{3}(g)$ is $1.7 \times 10^{-56}$ at $25^{\circ} \mathrm{C}$. Do you expect pure air at $25^{\circ} \mathrm{C}$ to contain much $\mathrm{O}_{3}$ (ozone) when $\mathrm{O}_{2}$ and $\mathrm{O}_{3}$ are in equilibrium? If the equilibrium concentration of $\mathrm{O}_{2}$ in air at $25^{\circ} \mathrm{C}$ is $8 \times 10^{-3} \mathrm{M}$, what is the equilibrium concentration of $\mathrm{O}_{3}$ ?
13.66 At $1400 \mathrm{~K}, K_{\mathrm{c}}=2.5 \times 10^{-3}$ for the reaction $\mathrm{CH}_{4}(g)+$ $2 \mathrm{H}_{2} \mathrm{~S}(g) \rightleftharpoons \mathrm{CS}_{2}(g)+4 \mathrm{H}_{2}(g)$. A 10.0 L reaction vessel at 1400 K contains 2.0 mol of $\mathrm{CH}_{4}, 3.0 \mathrm{~mol}$ of $\mathrm{CS}_{2}, 3.0$ mol of $\mathrm{H}_{2}$, and 4.0 mol of $\mathrm{H}_{2} \mathrm{~S}$. Is the reaction mixture at equilibrium? If not, in which direction does the reaction proceed to reach equilibrium?
13.67 The first step in the industrial synthesis of hydrogen is the reaction of steam and methane to give synthesis gas, a mixture of carbon monoxide and hydrogen:

$$
\begin{aligned}
\mathrm{H}_{2} \mathrm{O}(g)+\mathrm{CH}_{4}(g) \rightleftharpoons \mathrm{CO}(g)+3 \mathrm{H}_{2}(g) \\
K_{\mathrm{c}}=4.7 \text { at } 1400 \mathrm{~K}
\end{aligned}
$$

A mixture of reactants and products at 1400 K contains $0.035 \mathrm{M} \mathrm{H}_{2} \mathrm{O}, 0.050 \mathrm{M} \mathrm{CH}_{4}, 0.15 \mathrm{M} \mathrm{CO}$, and $0.20 \mathrm{M} \mathrm{H}_{2}$.

In which direction does the reaction proceed to reach equilibrium?
13.68 An equilibrium mixture of $\mathrm{N}_{2}, \mathrm{H}_{2}$, and $\mathrm{NH}_{3}$ at 700 K contains $0.036 \mathrm{M} \mathrm{N}_{2}$ and $0.15 \mathrm{M} \mathrm{H}_{2}$. At this temperature, $K_{\mathrm{c}}$ for the reaction $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$ is 0.29 . What is the concentration of $\mathrm{NH}_{3}$ ?
13.69 An equilibrium mixture of $\mathrm{O}_{2}, \mathrm{SO}_{2}$, and $\mathrm{SO}_{3}$ contains equal concentrations of $\mathrm{SO}_{2}$ and $\mathrm{SO}_{3}$. Calculate the concentration of $\mathrm{O}_{2}$ if $K_{\mathrm{c}}=2.7 \times 10^{2}$ for the reaction $2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{SO}_{3}(g)$.
13.70 The air pollutant NO is produced in automobile engines from the high-temperature reaction $\mathrm{N}_{2}(g)+$ $\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}(g) ; K_{\mathrm{c}}=1.7 \times 10^{-3}$ at 2300 K . If the initial concentrations of $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$ at 2300 K are both 1.40 M , what are the concentrations of $\mathrm{NO}, \mathrm{N}_{2}$, and $\mathrm{O}_{2}$ when the reaction mixture reaches equilibrium?
13.71 Recalculate the equilibrium concentrations in Problem 13.70 if the initial concentrations are $2.24 \mathrm{M} \mathrm{N}_{2}$ and $0.56 \mathrm{M} \mathrm{O}_{2}$. (This $\mathrm{N}_{2} / \mathrm{O}_{2}$ concentration ratio is the ratio found in air.)
13.72 At a certain temperature, the reaction $\mathrm{PCl}_{5}(g) \rightleftharpoons$ $\mathrm{PCl}_{3}(g)+\mathrm{Cl}_{2}(g)$ has an equilibrium constant $K_{\mathrm{c}}=$ $5.8 \times 10^{-2}$. Calculate the equilibrium concentrations of $\mathrm{PCl}_{5}, \mathrm{PCl}_{3}$, and $\mathrm{Cl}_{2}$ if only $\mathrm{PCl}_{5}$ is present initially, at a concentration of 0.160 M .
13.73 Recalculate the equilibrium concentrations in Problem 13.72 if the initial concentrations are $\left[\mathrm{PCl}_{5}\right]=$ $0.200 \mathrm{M},\left[\mathrm{PCl}_{3}\right]=0.100 \mathrm{M}$, and $\left[\mathrm{Cl}_{2}\right]=0.040 \mathrm{M}$.
13.74 The value of $K_{c}$ for the reaction of acetic acid with ethanol is 3.4 at $25^{\circ} \mathrm{C}$ :

```
\(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(\) soln \()+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(\) soln \() \rightleftharpoons\)
    Acetic acid Ethanol
            \(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{C}_{2} \mathrm{H}_{5}(\) soln \()+\mathrm{H}_{2} \mathrm{O}(\) soln \() \quad K_{\mathrm{c}}=3.4\)
                Ethyl acetate
```

(a) How many moles of ethyl acetate are present in an equilibrium mixture that contains 4.0 mol of acetic acid, 6.0 mol of ethanol, and 12.0 mol of water at $25^{\circ} \mathrm{C}$ ?
(b) Calculate the number of moles of all reactants and products in an equilibrium mixture prepared by mixing 1.00 mol of acetic acid and 10.00 mol of ethanol.
13.75 In a basic aqueous solution, chloromethane undergoes a substitution reaction in which $\mathrm{Cl}^{-}$is replaced by $\mathrm{OH}^{-}$:


The equilibrium constant $K_{c}$ is $1 \times 10^{16}$. Calculate the equilibrium concentrations of $\mathrm{CH}_{3} \mathrm{Cl}, \mathrm{CH}_{3} \mathrm{OH}, \mathrm{OH}^{-}$, and $\mathrm{Cl}^{-}$in a solution prepared by mixing equal volumes of $0.1 \mathrm{M} \mathrm{CH}_{3} \mathrm{Cl}$ and 0.2 M NaOH . (Hint: In defining $x$, assume that the reaction goes $100 \%$ to completion, and then take account of a small amount of the reverse reaction.)
13.76 At $700 \mathrm{~K}, K_{\mathrm{p}}=0.140$ for the reaction $\mathrm{ClF}_{3}(g) \rightleftharpoons$ $\mathrm{ClF}(g)+\mathrm{F}_{2}(g)$. Calculate the equilibrium partial pressures of $\mathrm{ClF}_{3}, \mathrm{ClF}$, and $\mathrm{F}_{2}$ if only $\mathrm{ClF}_{3}$ is present initially, at a partial pressure of 1.47 atm .
13.77 At $1000 \mathrm{~K}, \mathrm{~K}_{\mathrm{p}}=19.9$ for the reaction $\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+$ $3 \mathrm{CO}(g) \rightleftharpoons 2 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(g)$. What are the equilibrium partial pressures of CO and $\mathrm{CO}_{2}$ if CO is the only gas present initially, at a partial pressure of 0.978 atm ?

## Le Châtelier's Principle

13.78 Consider the following equilibrium: $\mathrm{Ag}^{+}(a q)+$ $\mathrm{Cl}^{-}(a q) \rightleftharpoons \mathrm{AgCl}(s)$. Use Le Châtelier's principle to predict how the amount of solid silver chloride will change when the equilibrium is disturbed by:
(a) Adding NaCl
(b) Adding $\mathrm{AgNO}_{3}$
(c) Adding $\mathrm{NH}_{3}$, which reacts with $\mathrm{Ag}^{+}$to form the complex ion, $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$
(d) Removing $\mathrm{Cl}^{-}$; also account for the change using the reaction quotient $Q_{c}$.
13.79 Will the concentration of $\mathrm{NO}_{2}$ increase, decrease, or remain the same when the equilibrium $\mathrm{NO}_{2} \mathrm{Cl}(g)+$ $\mathrm{NO}(g) \rightleftharpoons \mathrm{NOCl}(g)+\mathrm{NO}_{2}(g)$ is disturbed by:
(a) Adding NOCl
(b) Adding NO
(c) Removing NO
(d) Adding $\mathrm{NO}_{2} \mathrm{Cl}$; also account for the change using the reaction quotient $Q_{\mathrm{c}}$.
13.80 When each of the following equilibria is disturbed by increasing the pressure as a result of decreasing the volume, does the number of moles of reaction products increase, decrease, or remain the same?
(a) $2 \mathrm{CO}_{2}(g) \rightleftharpoons 2 \mathrm{CO}(g)+\mathrm{O}_{2}(g)$
(b) $\mathrm{N}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}(g)$
(c) $\mathrm{Si}(s)+2 \mathrm{Cl}_{2}(g) \rightleftharpoons \mathrm{SiCl}_{4}(g)$
13.81 For each of the following equilibria, use Le Châtelier's principle to predict the direction of reaction when the volume is increased.
(a) $\mathrm{C}(s)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}(g)+\mathrm{H}_{2}(g)$
(b) $2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}(g)$
(c) $2 \mathrm{Fe}(s)+3 \mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{H}_{2}(g)$
13.82 For the water-gas shift reaction $\mathrm{CO}(g)+$ $\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g), \Delta H^{\circ}=-41.2 \mathrm{~kJ}$, does the amount of $\mathrm{H}_{2}$ in an equilibrium mixture increase or decrease when the temperature is increased? How does $K_{c}$ change when the temperature is decreased? Justify your answers using Le Châtelier's principle.
13.83 The value of $\Delta H^{\circ}$ for the reaction $3 \mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{O}_{3}(g)$ is +285 kJ . Does the equilibrium constant for this reaction increase or decrease when the temperature increases? Justify your answer using Le Châtelier's principle.
13.84 Consider the exothermic reaction $\mathrm{CoCl}_{4}{ }^{2-}(a q)+$ $6 \mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}(a q)+4 \mathrm{Cl}^{-}(a q)$. Will the equilibrium concentration of $\mathrm{CoCl}_{4}{ }^{2-}$ increase or decrease when the following changes occur?
(a) HCl is added
(b) $\mathrm{Co}\left(\mathrm{NO}_{3}\right)_{2}$ is added
(c) The solution is diluted with water
(d) The temperature is increased
13.85 Consider the endothermic reaction $\mathrm{Fe}^{3+}(a q)+$ $\mathrm{Cl}^{-}(a q) \rightleftharpoons \mathrm{FeCl}^{2+}(a q)$. Use Le Châtelier's principle to predict how the equilibrium concentration of the complex ion $\mathrm{FeCl}^{2+}$ will change when:
(a) $\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}$ is added
(b) $\mathrm{Cl}^{-}$is precipitated as AgCl by addition of $\mathrm{AgNO}_{3}$
(c) The temperature is increased
(d) A catalyst is added
13.86 Methanol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$ is manufactured by reaction of carbon monoxide with hydrogen in the presence of a $\mathrm{ZnO} / \mathrm{Cr}_{2} \mathrm{O}_{3}$ catalyst:

$$
\mathrm{CO}(\mathrm{~g})+2 \mathrm{H}_{2}(\mathrm{~g}) \stackrel{\mathrm{ZnO} / \mathrm{Cr}_{2} \mathrm{O}_{3}}{\rightleftharpoons} \mathrm{CH}_{3} \mathrm{OH}(\mathrm{~g}) \quad \Delta H^{\circ}=-91 \mathrm{~kJ}
$$

Does the amount of methanol increase, decrease, or remain the same when an equilibrium mixture of reactants and products is subjected to the following changes?
(a) The temperature is increased
(b) The volume is decreased
(c) Helium is added
(d) CO is added
(e) The catalyst is removed
13.87 In the gas phase at $400^{\circ} \mathrm{C}$, isopropyl alcohol (rubbing alcohol) decomposes to acetone, an important industrial solvent:

$$
\left.\begin{array}{c}
\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHOH}(g) \\
\text { Isopropyl alcohol }
\end{array} \quad \text { Acetone } \Delta H^{\circ}=+57.3 \mathrm{~kJ} ~ ل \mathrm{H}_{3}\right)_{2} \mathrm{CO}(g)+\mathrm{H}_{2}(g)
$$

Does the amount of acetone increase, decrease, or remain the same when an equilibrium mixture of reactants and products is subjected to the following changes?
(a) The temperature is increased
(b) The volume is increased
(c) Argon is added
(d) $\mathrm{H}_{2}$ is added
(e) A catalyst is added

## Chemical Equilibrium and Chemical Kinetics

13.88 Consider a general, single-step reaction of the type $\mathrm{A}+\mathrm{B} \rightleftharpoons \mathrm{C}$. Show that the equilibrium constant is equal to the ratio of the rate constants for the forward and reverse reactions, $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$.
13.89 Which of the following relative values of $k_{\mathrm{f}}$ and $k_{\mathrm{r}}$ results in an equilibrium mixture that contains large amounts of reactants and small amounts of products?
(a) $k_{\mathrm{f}}>k_{\mathrm{r}}$
(b) $k_{\mathrm{f}}=k_{\mathrm{r}}$
(c) $k_{f}<k_{r}$
13.90 Consider the gas-phase hydration of hexafluoroacetone, $\left(\mathrm{CF}_{3}\right)_{2} \mathrm{CO}$ :

$$
\left(\mathrm{CF}_{3}\right)_{2} \mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \stackrel{k_{\mathrm{f}}}{\underset{k_{\mathrm{r}}}{\rightleftharpoons}}\left(\mathrm{CF}_{3}\right)_{2} \mathrm{C}(\mathrm{OH})_{2}(g)
$$

At $76^{\circ} \mathrm{C}$, the forward and reverse rate constants are $k_{\mathrm{f}}=0.13 \mathrm{M}^{-1} \mathrm{~s}^{-1}$ and $k_{\mathrm{r}}=6.2 \times 10^{-4} \mathrm{~s}^{-1}$. What is the value of the equilibrium constant $K_{c}$ ?
13.91 Consider the reaction of chloromethane with $\mathrm{OH}^{-}$in aqueous solution:

$$
\mathrm{CH}_{3} \mathrm{Cl}(a q)+\mathrm{OH}^{-}(a q) \underset{k_{\mathrm{r}}}{\stackrel{k_{\mathrm{f}}}{\rightleftharpoons}} \mathrm{CH}_{3} \mathrm{OH}(a q)+\mathrm{Cl}^{-}(a q)
$$

At $25^{\circ} \mathrm{C}$, the rate constant for the forward reaction is $6 \times 10^{-6} \mathrm{M}^{-1} \mathrm{~s}^{-1}$, and the equilibrium constant $K_{c}$ is $1 \times 10^{16}$. Calculate the rate constant for the reverse reaction at $25^{\circ} \mathrm{C}$.
13.92 Listed in the table are forward and reverse rate constants for the reaction $2 \mathrm{NO}(g) \rightleftharpoons \mathrm{N}_{2}(g)+\mathrm{O}_{2}(g)$.

| Temperature (K) | $\boldsymbol{k}_{\mathbf{f}}\left(\mathbf{M}^{\mathbf{- 1}} \mathbf{s}^{\mathbf{- 1}}\right)$ | $\boldsymbol{k}_{\mathbf{r}}\left(\mathbf{M}^{\mathbf{1}} \mathbf{s}^{\mathbf{- 1}}\right)$ |
| :--- | :--- | :--- |
| 1400 | 0.29 | $1.1 \times 10^{-6}$ |
| 1500 | 1.3 | $1.4 \times 10^{-5}$ |

Is the reaction endothermic or exothermic? Explain in terms of kinetics.
13.93 Forward and reverse rate constants for the reaction $\mathrm{CO}_{2}(g)+\mathrm{N}_{2}(g) \rightleftharpoons \mathrm{CO}(g)+\mathrm{N}_{2} \mathrm{O}(g)$ exhibit the following temperature dependence:

| Temperature (K) | $\boldsymbol{k}_{\mathbf{f}}\left(\mathbf{M}^{-\mathbf{1}} \mathbf{s}^{\mathbf{- 1}}\right)$ | $\boldsymbol{k}_{\mathbf{r}}\left(\mathbf{M}^{-\mathbf{1}} \mathbf{s}^{\mathbf{- 1}}\right)$ |
| :--- | :--- | :--- |
| 1200 | $9.1 \times 10^{-11}$ | $1.5 \times 10^{5}$ |
| 1300 | $2.7 \times 10^{-9}$ | $2.6 \times 10^{5}$ |

Is the reaction endothermic or exothermic? Explain in terms of kinetics.

## General Problems

13.94 When 0.500 mol of $\mathrm{N}_{2} \mathrm{O}_{4}$ is placed in a 4.00 L reaction vessel and heated at $400 \mathrm{~K}, 79.3 \%$ of the $\mathrm{N}_{2} \mathrm{O}_{4}$ decomposes to $\mathrm{NO}_{2}$.
(a) Calculate $K_{\mathrm{c}}$ and $K_{\mathrm{p}}$ at 400 K for the reaction $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$.
(b) Draw an electron-dot structure for $\mathrm{NO}_{2}$, and rationalize the structure of $\mathrm{N}_{2} \mathrm{O}_{4}$.
13.95 At $25^{\circ} \mathrm{C}, K_{\mathrm{c}}=1.6 \times 10^{24}$ for the reaction $\mathrm{CaO}(s)+$ $\mathrm{CO}_{2}(g) \rightleftharpoons \mathrm{CaCO}_{3}(s)$. Use the value of $K_{\mathrm{c}}$ to estimate the extent of this reaction. Verify your estimate by calculating the concentration of $\mathrm{CO}_{2}$ gas that is in equilibrium with solid CaO and solid $\mathrm{CaCO}_{3}$ at $25^{\circ} \mathrm{C}$.
13.96 What concentration of $\mathrm{NH}_{3}$ is in equilibrium with $1.0 \times 10^{-3} \mathrm{M} \mathrm{N}_{2}$ and $2.0 \times 10^{-3} \mathrm{M} \mathrm{H}_{2}$ at 700 K ? At this temperature, $K_{c}=0.291$ for the reaction $\mathrm{N}_{2}(g)+$ $3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$.
13.97 The F-F bond in $\mathrm{F}_{2}$ is relatively weak because the lone pairs of electrons on one F atom repel the lone pairs on the other F atom; $K_{\mathrm{p}}=7.83$ at 1500 K for the reaction $\mathrm{F}_{2}(g) \rightleftharpoons 2 \mathrm{~F}(g)$.
(a) If the equilibrium partial pressure of $\mathrm{F}_{2}$ molecules at 1500 K is 0.200 atm , what is the equilibrium partial pressure of F atoms in atm?
(b) What fraction of the $\mathrm{F}_{2}$ molecules dissociate at 1500 K ?
(c) Why is the F-F bond in $\mathrm{F}_{2}$ weaker than the $\mathrm{Cl}-\mathrm{Cl}$ bond in $\mathrm{Cl}_{2}$ ?
13.98 The equilibrium concentrations in a gas mixture at a particular temperature are $0.13 \mathrm{M} \mathrm{H}_{2}, 0.70 \mathrm{M} \mathrm{I}_{2}$, and 2.1 M HI . What equilibrium concentrations are obtained at the same temperature when 0.20 mol of HI is injected into an empty 500.0 mL container?
13.99 A 5.00 L reaction vessel is filled with 1.00 mol of $\mathrm{H}_{2}$, 1.00 mol of $\mathrm{I}_{2}$, and 2.50 mol of HI . Calculate the equilibrium concentrations of $\mathrm{H}_{2}, \mathrm{I}_{2}$, and HI at 500 K . The equilibrium constant $K_{c}$ at 500 K for the reaction $\mathrm{H}_{2}(g)+\mathrm{I}_{2}(g) \rightleftharpoons 2 \mathrm{HI}(g)$ is 129.
13.100 At 1000 K , the value of $K_{c}$ for the reaction $\mathrm{C}(s)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}(g)+\mathrm{H}_{2}(g)$ is $3.0 \times 10^{-2}$. Calculate the equilibrium concentrations of $\mathrm{H}_{2} \mathrm{O}, \mathrm{CO}_{2}$, and $\mathrm{H}_{2}$ in a reaction mixture obtained by heating 6.00 mol of steam and an excess of solid carbon in a 5.00 L container. What is the molar composition of the equilibrium mixture?
13.101 The equilibrium constant $K_{\mathrm{p}}$ for the reaction $\mathrm{PCl}_{5}(g) \rightleftharpoons \mathrm{PCl}_{3}(g)+\mathrm{Cl}_{2}(g)$ is $3.81 \times 10^{2}$ at 600 K and $2.69 \times 10^{3}$ at 700 K .
(a) Is the reaction endothermic or exothermic?
(b) How are the equilibrium amounts of reactants and products affected by (i) an increase in volume, (ii) addition of an inert gas, or (iii) addition of a catalyst?
13.102 Consider the following gas-phase reaction: $2 \mathrm{~A}(g)+$ $\mathrm{B}(g) \rightleftharpoons \mathrm{C}(g)+\mathrm{D}(g)$. An equilibrium mixture of reactants and products is subjected to the following changes:
(a) A decrease in volume
(b) An increase in temperature
(c) Addition of reactants
(d) Addition of a catalyst
(e) Addition of an inert gas

Which of these changes affect the composition of the equilibrium mixture, but leave the value of the equilibrium constant $K_{c}$ unchanged? Which of the changes affect the value of $K_{c}$ ? Which affect neither the composition of the equilibrium mixture nor $K_{c}$ ?
13.103 Baking soda (sodium bicarbonate) decomposes when it is heated:

$$
\begin{array}{r}
2 \mathrm{NaHCO}_{3}(s) \rightleftharpoons \mathrm{Na}_{2} \mathrm{CO}_{3}(s)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(g) \\
\Delta H^{\mathrm{o}}=+136 \mathrm{~kJ}
\end{array}
$$

Consider an equilibrium mixture of reactants and products in a closed container. How does the number of moles of $\mathrm{CO}_{2}$ change when the mixture is disturbed by the following:
(a) Adding solid $\mathrm{NaHCO}_{3}$
(b) Adding water vapor
(c) Decreasing the volume of the container
(d) Increasing the temperature
13.104 Acetic acid tends to form dimers, $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)_{2}$, because of hydrogen bonding:


The equilibrium constant $K_{c}$ for this reaction is $1.51 \times 10^{2}$ in benzene solution, but only $3.7 \times 10^{-2}$ in water solution.
(a) Calculate the ratio of dimers to monomers for 0.100 M acetic acid in benzene.
(b) Calculate the ratio of dimers to monomers for 0.100 M acetic acid in water.
(c) Why is $K_{c}$ for the water solution so much smaller than $K_{\mathrm{c}}$ for the benzene solution?
13.105 Consider the reaction $\mathrm{C}(s)+\mathrm{CO}_{2}(g) \rightleftharpoons 2 \mathrm{CO}(g)$. When 1.50 mol of $\mathrm{CO}_{2}$ and an excess of solid carbon are heated in a 20.0 L container at 1100 K , the equilibrium concentration of CO is $7.00 \times 10^{-2} \mathrm{M}$.
(a) What is the equilibrium concentration of $\mathrm{CO}_{2}$ ?
(b) What is the value of the equilibrium constant $K_{\mathrm{c}}$ at 1100 K ?
13.106 When 1.000 mol of $\mathrm{PCl}_{5}$ is introduced into a 5.000 L container at $500 \mathrm{~K}, 78.50 \%$ of the $\mathrm{PCl}_{5}$ dissociates to give an equilibrium mixture of $\mathrm{PCl}_{5}, \mathrm{PCl}_{3}$, and $\mathrm{Cl}_{2}$ :

$$
\mathrm{PCl}_{5}(g) \rightleftharpoons \mathrm{PCl}_{3}(g)+\mathrm{Cl}_{2}(g)
$$

(a) Calculate the values of $K_{\mathrm{c}}$ and $K_{\mathrm{p}}$.
(b) If the initial concentrations in a particular mixture of reactants and products are $\left[\mathrm{PCl}_{5}\right]=0.500 \mathrm{M}$, $\left[\mathrm{PCl}_{3}\right]=0.150 \mathrm{M}$, and $\left[\mathrm{Cl}_{2}\right]=0.600 \mathrm{M}$, in which direction does the reaction proceed to reach equilibrium? What are the concentrations when the mixture reaches equilibrium?
13.107 At a certain temperature, $K_{\mathrm{p}}=1.42$ for the reaction $\mathrm{PCl}_{5}(g) \rightleftharpoons \mathrm{PCl}_{3}(g)+\mathrm{Cl}_{2}(g)$. Calculate the equilibrium partial pressures and the total pressure if the initial partial pressures are $P_{\mathrm{PCl}_{5}}=3.00 \mathrm{~atm}, P_{\mathrm{PCl}_{3}}=$ 2.00 atm , and $P_{\mathrm{Cl}_{2}}=1.50 \mathrm{~atm}$.
13.108 Refining petroleum involves cracking large hydrocarbon molecules into smaller, more volatile pieces. A simple example of hydrocarbon cracking is the gasphase thermal decomposition of butane to give ethane and ethylene:


Butane, $\mathrm{C}_{4} \mathrm{H}_{10}$




Ethane, $\mathrm{C}_{2} \mathrm{H}_{6} \quad$ Ethylene, $\mathrm{C}_{2} \mathrm{H}_{4}$
(a) Write the equilibrium constant expressions for $K_{p}$ and $K_{c}$.
(b) The value of $K_{\mathrm{p}}$ at $500^{\circ} \mathrm{C}$ is 12 . What is the value of $K_{c}$ ?
(c) A sample of butane having a pressure of 50 atm is heated at $500^{\circ} \mathrm{C}$ in a closed container at constant volume. When equilibrium is reached, what percentage of the butane has been converted to ethane and ethylene? What is the total pressure at equilibrium?
(d) How would the percent conversion in part (c) be affected by a decrease in volume?
13.109 The equilibrium constant $K_{c}$ for the gas-phase thermal decomposition of cyclopropane to propene is $1.0 \times 10^{5}$ at 500 K :

(a) What is the value of $K_{\mathrm{p}}$ at 500 K ?
(b) What is the equilibrium partial pressure of cyclopropane at 500 K when the partial pressure of propene is 5.0 atm ?
(c) Can you alter the ratio of the two concentrations at equilibrium by adding cyclopropane or by decreasing the volume of the container? Explain.
(d) Which has the larger rate constant, the forward reaction or the reverse reaction?
(e) Why is cyclopropane so reactive? (Hint: Consider the hybrid orbitals used by the C atoms.)
13.110 The equilibrium constant $K_{\mathrm{p}}$ for the gas-phase thermal decomposition of tert-butyl chloride is 3.45 at 500 K :

(a) Calculate the value of $K_{c}$ at 500 K .
(b) Calculate the molar concentrations of reactants and products in an equilibrium mixture obtained by heating 1.00 mol of tert-butyl chloride in a 5.00 L vessel at 500 K .
(c) A mixture of isobutylene ( 0.400 atm partial pressure at 500 K ) and HCl ( 0.600 atm partial pressure at 500 K ) is allowed to reach equilibrium at 500 K . What are the equilibrium partial pressures of tertbutyl chloride, isobutylene, and HCl ?
13.111 As shown in Figure 13.14, a catalyst lowers the activation energy for the forward and reverse reactions by the same amount, $\Delta E_{\mathrm{a}}$.
(a) Apply the Arrhenius equation, $k=A e^{-E_{\mathrm{a}} / R T}$, to the forward and reverse reactions, and show that a catalyst increases the rates of both reactions by the same factor.
(b) Use the relation between the equilibrium constant and the forward and reverse rate constants, $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$, to show that a catalyst does not affect the value of the equilibrium constant.
13.112 Given the Arrhenius equation, $k=A e^{-E_{a} / R T}$, and the relation between the equilibrium constant and the forward and reverse rate constants, $K_{\mathrm{c}}=k_{\mathrm{f}} / k_{\mathrm{r}}$, explain why $K_{c}$ for an exothermic reaction decreases with increasing temperature.
13.113 At $1000 \mathrm{~K}, K_{\mathrm{p}}=2.1 \times 10^{6}$ and $\Delta H^{0}=-107.7 \mathrm{~kJ}$ for the reaction $\mathrm{H}_{2}(g)+\mathrm{Br}_{2}(g) \rightleftharpoons 2 \mathrm{HBr}(g)$
(a) A 0.974 mol quantity of $\mathrm{Br}_{2}$ is added to a 1.00 L reaction vessel that contains 1.22 mol of $\mathrm{H}_{2}$ gas at 1000 K . What are the partial pressures of $\mathrm{H}_{2}, \mathrm{Br}_{2}$, and HBr at equilibrium?
(b) For the equilibrium in part (a), each of the following changes will increase the equilibrium partial pressure of HBr . Choose the change that will cause the greatest increase in the pressure of HBr , and explain your choice.
(i) Adding 0.10 mol of $\mathrm{H}_{2}$
(ii) Adding 0.10 mol of $\mathrm{Br}_{2}$
(iii) Decreasing the temperature to 700 K .
13.114 Consider the gas-phase decomposition of NOBr:

$$
2 \mathrm{NOBr}(g) \rightleftharpoons 2 \mathrm{NO}(g)+\mathrm{Br}_{2}(g)
$$

(a) When 0.0200 mol of NOBr is added to an empty 1.00 L flask and the decomposition reaction is allowed to reach equilibrium at 300 K , the total pressure in the flask is 0.588 atm . What is the equilibrium constant $K_{\mathrm{c}}$ for this reaction at 300 K ?
(b) What is the value of $K_{\mathrm{p}}$ for this reaction at 300 K ?
13.115 At $100^{\circ} \mathrm{C}, K_{\mathrm{c}}=4.72$ for the reaction $2 \mathrm{NO}_{2}(g) \rightleftharpoons$ $\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})$. An empty 10.0 L flask is filled with 4.60 g of $\mathrm{NO}_{2}$ at $100^{\circ} \mathrm{C}$. What is the total pressure in the flask at equilibrium?
13.116 Halogen lamps are ordinary tungsten filament lamps in which the lamp bulb contains a small amount of a halogen (often bromine). At the high temperatures of the lamp, the halogens dissociate and exist as single atoms.
(a) In an ordinary tungsten lamp, the hot tungsten filament is constantly evaporating, and the tungsten condenses on the relatively cool walls of the bulb. In a Br-containing halogen lamp, the tungsten reacts with the Br atoms to give gaseous $\mathrm{WBr}_{4}$ :

$$
\mathrm{W}(s)+4 \mathrm{Br}(g) \rightleftharpoons \mathrm{WBr}_{4}(g)
$$

At the walls of the lamp, where the temperature is about 900 K , this reaction has an equilibrium constant $K_{p}$ of about 100. If the equilibrium pressure of $\operatorname{Br}(g)$ is 0.010 atm , what is the equilibrium pressure of $\mathrm{WBr}_{4}(g)$ near the walls of the bulb.
(b) Near the tungsten filament, where the temperature is about 2800 K , the reaction in part (a) has a $K_{p}$ value of about 5.0. Is the reaction exothermic or endothermic?
(c) When the $\mathrm{WBr}_{4}(g)$ diffuses back toward the filament, it decomposes, depositing tungsten back onto the filament. Show quantitatively that the pressure of $\mathrm{WBr}_{4}$ from part (a) will cause the reaction in part (a) to go in reverse direction at 2800 K . [The pressure of $\operatorname{Br}(g)$ is still 0.010 atm .] Thus, tungsten is continually recycled from the walls of the bulb back to the filament, allowing the bulb to last longer and burn brighter.
13.117 The decomposition of solid ammonium carbamate, $\left(\mathrm{NH}_{4}\right)\left(\mathrm{NH}_{2} \mathrm{CO}_{2}\right)$, to gaseous ammonia and carbon dioxide is an endothermic reaction.

$$
\left(\mathrm{NH}_{4}\right)\left(\mathrm{NH}_{2} \mathrm{CO}_{2}\right)(s) \rightleftharpoons 2 \mathrm{NH}_{3}(g)+\mathrm{CO}_{2}(g)
$$

(a) When solid $\left(\mathrm{NH}_{4}\right)\left(\mathrm{NH}_{2} \mathrm{CO}_{2}\right)$ is introduced into an evacuated flask at $25^{\circ} \mathrm{C}$, the total pressure of gas at equilibrium is 0.116 atm . What is the value of $K_{\mathrm{p}}$ at $25^{\circ} \mathrm{C}$ ?
(b) Given that the decomposition reaction is at equilibrium, how would the following changes affect the total quantity of $\mathrm{NH}_{3}$ in the flask once equilibrium is re-established?
(i) Adding $\mathrm{CO}_{2}$
(ii) Adding $\left(\mathrm{NH}_{4}\right)\left(\mathrm{NH}_{2} \mathrm{CO}_{2}\right)$
(iii) Removing $\mathrm{CO}_{2}$
(iv) Increasing the total volume
(v) Adding neon
13.118 At $25^{\circ} \mathrm{C}, K_{\mathrm{c}}=216$ for the reaction $2 \mathrm{NO}_{2}(g) \rightleftharpoons$ $\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})$. A 1.00 L flask containing a mixture of $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ at $25^{\circ} \mathrm{C}$ has a total pressure of 1.50 atm . What is the partial pressure of each gas?
13.119 At $500^{\circ} \mathrm{C}, \mathrm{F}_{2}$ gas is stable and does not dissociate, but at $840^{\circ} \mathrm{C}$, some dissociation occurs: $\mathrm{F}_{2}(g) \rightleftharpoons 2 \mathrm{~F}(g)$. A flask filled with 0.600 atm of $\mathrm{F}_{2}$ at $500^{\circ} \mathrm{C}$ was heated to $840^{\circ} \mathrm{C}$, and the pressure at equilibrium was measured to be 0.984 atm . What is the equilibrium constant $K_{\mathrm{p}}$ for the dissociation of $\mathrm{F}_{2}$ gas at $840^{\circ} \mathrm{C}$ ?
13.120 The equilibrium constant $K_{c}$ for the reaction $\mathrm{N}_{2}(g)+$ $3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$ is 4.20 at 600 K . When a quantity of gaseous $\mathrm{NH}_{3}$ was placed in a 1.00 L reaction vessel at 600 K and the reaction was allowed to reach equilibrium, the vessel was found to contain 0.200 mol of $\mathrm{N}_{2}$. How many moles of $\mathrm{NH}_{3}$ were placed in the vessel?

## Multi-Concept Problems

13.121 A 125.4 g quantity of water and an equal molar amount of carbon monoxide were placed in an empty 10.0 L vessel, and the mixture was heated to 700 K . At equilibrium, the partial pressure of CO was 9.80 atm . The reaction is

$$
\mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightleftharpoons \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g)
$$

(a) What is the value of $K_{\mathrm{p}}$ at 700 K ?
(b) An additional 31.4 g of water was added to the reaction vessel, and a new state of equilibrium was achieved. What are the equilibrium partial pressures of each gas in the mixture? What is the concentration of $\mathrm{H}_{2}$ in molecules $/ \mathrm{cm}^{3}$ ?
13.122 A 79.2 g chunk of dry ice (solid $\mathrm{CO}_{2}$ ) and 30.0 g of graphite (carbon) were placed in an empty 5.00 L container, and the mixture was heated to achieve equilibrium. The reaction is

$$
\mathrm{CO}_{2}(g)+\mathrm{C}(s) \rightleftharpoons 2 \mathrm{CO}(g)
$$

(a) What is the value of $K_{\mathrm{p}}$ at 1000 K if the gas density at 1000 K is $16.3 \mathrm{~g} / \mathrm{L}$ ?
(b) What is the value of $K_{\mathrm{p}}$ at 1100 K if the gas density at 1100 K is $16.9 \mathrm{~g} / \mathrm{L}$ ?
(c) Is the reaction exothermic or endothermic? Explain.
13.123 The amount of carbon dioxide in a gaseous mixture of $\mathrm{CO}_{2}$ and CO can be determined by passing the gas into an aqueous solution that contains an excess of $\mathrm{Ba}(\mathrm{OH})_{2}$. The $\mathrm{CO}_{2}$ reacts, yielding a precipitate of $\mathrm{BaCO}_{3}$, but the CO does not react. This method was used to analyze the equilibrium composition of the gas obtained when 1.77 g of $\mathrm{CO}_{2}$ reacted with 2.0 g of graphite in a 1.000 L container at 1100 K . The analysis yielded 3.41 g of $\mathrm{BaCO}_{3}$. Use these data to calculate $K_{\mathrm{p}}$ at 1100 K for the reaction

$$
\mathrm{CO}_{2}(g)+\mathrm{C}(s) \rightleftharpoons 2 \mathrm{CO}(g)
$$

13.124 A 14.58 g quantity of $\mathrm{N}_{2} \mathrm{O}_{4}$ was placed in a 1.000 L reaction vessel at 400 K . The $\mathrm{N}_{2} \mathrm{O}_{4}$ decomposed to an equilibrium mixture of $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ that had a total pressure of 9.15 atm .
(a) What is the value of $K_{c}$ for the reaction $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$ at 400 K ?
(b) How much heat (in kilojoules) was absorbed when the $\mathrm{N}_{2} \mathrm{O}_{4}$ decomposed to give the equilibrium mixture? (Standard heats of formation may be found in Appendix B.)
13.125 Consider the sublimation of moth balls at $27^{\circ} \mathrm{C}$ in a room having dimensions $8.0 \mathrm{ft} \times 10.0 \mathrm{ft} \times 8.0 \mathrm{ft}$. Assume that the moth balls are pure solid naphthalene (density $1.16 \mathrm{~g} / \mathrm{cm}^{3}$ ) and that they are spheres with a diameter of 12.0 mm . The equilibrium constant $K_{c}$ for sublimation of naphthalene is $5.40 \times 10^{-6}$ at $27^{\circ} \mathrm{C}$.

$$
\mathrm{C}_{10} \mathrm{H}_{8}(\mathrm{~s}) \rightleftharpoons \mathrm{C}_{10} \mathrm{H}_{8}(\mathrm{~g})
$$

(a) When excess moth balls are present, how many gaseous naphthalene molecules are in the room at equilibrium?
(b) How many moth balls are required to saturate the room with gaseous naphthalene?
13.126 Ozone is unstable with respect to decomposition to ordinary oxygen:

$$
2 \mathrm{O}_{3}(g) \rightleftharpoons 3 \mathrm{O}_{2}(g) \quad K_{\mathrm{p}}=1.3 \times 10^{57}
$$

How many $\mathrm{O}_{3}$ molecules are present at equilibrium in 10 million cubic meters of air at $25^{\circ} \mathrm{C}$ and 720 mm Hg pressure?
13.127 The equilibrium constant for the dimerization of acetic acid in benzene solution is $1.51 \times 10^{2}$ at $25^{\circ} \mathrm{C}$ (see Problem 13.104)

$$
\begin{aligned}
2 \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H} & \rightleftharpoons\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)_{2} \\
K_{\mathrm{c}} & =1.51 \times 10^{2} \text { at } 25^{\circ} \mathrm{C}
\end{aligned}
$$

(a) What are the equilibrium concentrations of monomer and dimer at $25^{\circ} \mathrm{C}$ in a solution prepared by dissolving 0.0300 mol of pure acetic acid in enough benzene to make 250.0 mL of solution?
(b) What is the osmotic pressure of the solution at $25^{\circ} \mathrm{C}$ ?
13.128 For the decomposition reaction $\mathrm{PCl}_{5}(g) \rightleftharpoons \mathrm{PCl}_{3}(g)+$ $\mathrm{Cl}_{2}(g), K_{p}=381$ at 600 K and $K_{\mathrm{c}}=46.9$ at 700 K .
(a) Is the reaction endothermic or exothermic? Explain. Does your answer agree with what you would predict based on bond energies?
(b) If 1.25 g of $\mathrm{PCl}_{5}$ is introduced into an evacuated 0.500 L flask at 700 K and the decomposition reaction is allowed to reach equilibrium, what percent of the $\mathrm{PCl}_{5}$ will decompose and what will be the total pressure in the flask?
(c) Write electron-dot structures for $\mathrm{PCl}_{5}$ and $\mathrm{PCl}_{3}$, and indicate whether these molecules have a dipole moment. Explain.

## eMedia Problems

13.129 Run each of the three experiments in the $\mathbf{N}_{2} \mathrm{O}_{4} / \mathrm{NO}_{2}$ Equilibrium Experiment activity (eChapter 13.1).
(a) For each experiment, identify the compound being decomposed and the compound being produced as the experiment begins.
(b) In each experiment, the concentration of the compound being decomposed becomes constant after a period of time even though the reaction is continuing. Explain.
(c) Determine the value of $\left[\mathrm{NO}_{2}\right]^{2} /\left[\mathrm{N}_{2} \mathrm{O}_{4}\right]$ for each of the reactions. Compare these values.
13.130 Use the Chemical Equilibrium activity (eChapter 13.1) to explore the reaction between the iron(III) ion and the thiocyanate ion.
(a) Write the equilibrium constant expression for the reaction as it appears in the activity.
(b) Does the equilibrium lie to the right or to the left? How would the graph be different if the opposite were true?
(c) Would it be possible to establish equilibrium starting with only the product and none of the reactants? Explain.
(d) Write the equilibrium constant expression for the reverse reaction.
13.131 Using the Equilibrium Constant activity (eChapter 13.2), compare the reactions $\mathrm{A} \rightleftharpoons \mathrm{B}$ and $\mathrm{A} \rightleftharpoons 2$ B in Worked Key Concept Example 13.4 (page 534). (Each picture represents the contents of a $1.00 \times 10^{-24} \mathrm{~L}$ vessel.)
(a) If picture 1 represents an equilibrium mixture for the reaction $\mathrm{A} \rightleftharpoons \mathrm{B}$, what is the value of $K_{\mathrm{c}}$ for the reaction?
(b) If picture 1 represents an equilibrium mixture for the reaction $\mathrm{A} \rightleftharpoons 2 \mathrm{~B}$, what is the value of $K_{\mathrm{c}}$ for the reaction?
(c) Which (if any) of the other pictures also represents an equilibrium mixture for the reaction $\mathrm{A} \rightleftharpoons 2 \mathrm{~B}$ ? Explain your answer.
13.132 The following questions refer to the Equilibrium Expressions activity in eChapter 13.4:
(a) If $\mathrm{K}_{\mathrm{c}}$ for the first reaction is 1.83 , calculate $K_{\mathrm{p}}$.
(b) Why are $\mathrm{CaCO}_{3}$ and CaO not included in the equilibrium constant expressions for the second reaction?
(c) Why is a $K_{\mathrm{p}}$ expression not given for the third reaction?
13.133 Use the Altering an Equilibrium Mixture activity (eChapter 13.7) to determine the direction the reaction shifts to re-establish equilibrium when more $A$ is added. What direction would the reaction shift if:
(a) More AB is added?
(b) Reactant B is removed?
(c) Reactant A is removed?

## Chapter

## Hydrogen, Oxygen, and Water

## Hydrogen is the most abundant element in the universe, and oxygen is the most abundant element on the earth's

surface. When chemically combined, they yield water, perhaps the most important and familiar of all chemical compounds.

Hydrogen combines with every element in the periodic table except the noble gases and forms more compounds than any other element. Industrially, large amounts of elemental hydrogen are produced for use in the synthesis of such chemicals as ammonia and

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■ Interlude-A "Hydrogen Economy"


- The Lagoon Nebula in the constellation Sagittarius. These interstellar gas clouds consist largely of atomic hydrogen, the most abundant element in the universe. The gas is heated by radiation from nearby stars. Can you explain its characteristic red glow? (Recall Section 5.3.)


Isotopes of Hydrogen activity
methanol. Oxygen is essential for respiration and is the oxidizing agent in the energy-generating combustion processes that maintain our industrialized civilization. Approximately 26 million tons of oxygen are produced annually in the United States, largely for use in making steel.

In this chapter, we'll take a detailed look at the chemistry of hydrogen and oxygen, and we'll discuss some of the properties of water, the solvent for all the reactions to be discussed in Chapters 15 and 16.

## 14.1 | Hydrogen

Henry Cavendish (1731-1810), an English chemist and physicist, was the first person to isolate hydrogen in pure form. Cavendish showed that the action of acids on metals, such as zinc, iron, and tin, produces a flammable gas that can be distinguished from other gases by its unusually low density:

$$
2 \mathrm{H}^{+}(a q)+\mathrm{Zn}(s) \longrightarrow \mathrm{H}_{2}(g)+\mathrm{Zn}^{2+}(a q)
$$

The French chemist Lavoisier called the gas "hydrogen," meaning "water former," because it combines with oxygen to produce water.

At ordinary temperatures and pressures, hydrogen is a colorless, odorless, and tasteless gas comprised of diatomic $\mathrm{H}_{2}$ molecules. Because $\mathrm{H}_{2}$ is a nonpolar molecule that contains only two electrons, intermolecular forces are extremely weak (Section 10.2). As a result, hydrogen has a very low melting point $\left(-259.2^{\circ} \mathrm{C}\right)$ and a very low boiling point $\left(-252.8^{\circ} \mathrm{C}\right)$. The bonding forces within the $\mathrm{H}_{2}$ molecule are exceptionally strong, however: The $\mathrm{H}-\mathrm{H}$ bond dissociation energy is $436 \mathrm{~kJ} / \mathrm{mol}$, greater than that for any other single bond between two atoms of the same element (Section 7.2):

$$
\mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{H}(g) \quad D=436 \mathrm{~kJ} / \mathrm{mol}
$$

By comparison, the bond dissociation energies of the halogens range from $151 \mathrm{~kJ} / \mathrm{mol}$ for $\mathrm{I}_{2}$ to $243 \mathrm{~kJ} / \mathrm{mol}$ for $\mathrm{Cl}_{2}$. Because of the strong $\mathrm{H}-\mathrm{H}$ bond, $\mathrm{H}_{2}$ is thermally stable. Even at 2000 K , only 1 of every $2500 \mathrm{H}_{2}$ molecules is dissociated into H atoms at 1 atm pressure.

Hydrogen is thought to account for approximately $75 \%$ of the mass of the universe. Our sun and other stars, for instance, are composed mainly of hydrogen, which serves as their nuclear fuel. On Earth, though, hydrogen is rarely found in uncombined form because the earth's gravity is too weak to hold such a light molecule. Nearly all the $\mathrm{H}_{2}$ originally present in the earth's atmosphere has been lost to space, so that the atmosphere now contains only 0.53 ppm of $\mathrm{H}_{2}$ by volume. In the earth's crust and oceans, hydrogen is the ninth most abundant element on a mass basis ( 0.9 mass \%) and the third most abundant on an atom basis ( 15.4 atom $\%)$. Hydrogen is found in water, petroleum, proteins, carbohydrates, fats, and literally millions of other compounds.

- PROBLEM 14.1 Hydrogen is used to inflate weather balloons because it is much less dense than air. Calculate the density of gaseous $\mathrm{H}_{2}$ at $25^{\circ} \mathrm{C}$ and 1 atm pressure. Compare your result with the density of dry air under the same conditions $\left(1.185 \times 10^{-3} \mathrm{~g} / \mathrm{cm}^{3}\right)$.


## 14.2 | Isotopes of Hydrogen

As mentioned in Section 2.5, there are three isotopes of hydrogen: protium, or ordinary hydrogen $\left({ }_{1}^{1} \mathrm{H}\right)$; deuterium, or heavy hydrogen $\left({ }_{1}^{2} \mathrm{H}\right.$ or D); and tritium $\left({ }_{1}^{3} \mathrm{H}\right.$ or T). Nearly all ( $99.985 \%$ ) the atoms in naturally occurring hydrogen are protium. The terrestrial abundance of deuterium is only 0.015 atom \%, and tritium is present only in trace amounts ( $\sim 10^{-16}$ atom $\%$ ).

The properties of protium, deuterium, and tritium are similar (Table 14.1), because chemical behavior is determined primarily by electronic structure and all three isotopes have the same electron configuration $\left(1 s^{1}\right)$. There are, however, quantitative differences in properties, known as isotope effects, that arise from the differences in the masses of the isotopes. For example, $D_{2}$ has a higher melting point, a higher boiling point, and a greater bond dissociation energy than $\mathrm{H}_{2}$. Similarly, $\mathrm{D}_{2} \mathrm{O}$ has a higher melting point and a higher boiling point than $\mathrm{H}_{2} \mathrm{O}$, and the equilibrium constant for dissociation of $\mathrm{D}_{2} \mathrm{O}$ is about one-fifth that for $\mathrm{H}_{2} \mathrm{O}$ :

$$
\begin{aligned}
\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{OH}^{-}(a q) & K=1.01 \times 10^{-14} \\
\mathrm{D}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{D}^{+}(a q)+\mathrm{OD}^{-}(a q) & K=0.195 \times 10^{-14}
\end{aligned}
$$

| Properties of Hydrogen Isotopes |  |  |  |
| :---: | :---: | :---: | :---: |
| Property | Protium | Deuterium | Tritium |
| Atomic hydrogen (H) |  |  |  |
| Mass, amu | 1.0078 | 2.0141 | 3.0160 |
| Ionization energy, $\mathrm{kJ} / \mathrm{mol}$ | 1311.7 | 1312.2 |  |
| Nuclear stability | Stable | Stable | Radioactive |
| Molecular hydrogen ( $\mathbf{H}_{\mathbf{2}}$ ) |  |  |  |
| Melting point, K | 13.96 | 18.73 | 20.62 |
| Boiling point, K | 20.39 | 23.67 | 25.04 |
| Bond dissociation energy, $\mathrm{kJ} / \mathrm{mol}$ | 435.9 | 443.4 | 446.9 |
| Water ( $\mathrm{H}_{2} \mathrm{O}$ ) |  |  |  |
| Melting point, ${ }^{\circ} \mathrm{C}$ | 0.00 | 3.81 | 4.48 |
| Boiling point, ${ }^{\circ} \mathrm{C}$ | 100.00 | 101.42 | 101.51 |
| Density at $25^{\circ} \mathrm{C}, \mathrm{g} / \mathrm{mL}$ | 0.997 | 1.104 | 1.214 |
| Dissociation constant at $25^{\circ} \mathrm{C}$ | $1.01 \times 10^{-14}$ | $0.195 \times 10^{-14}$ | $\sim 0.06 \times 10^{-14}$ |

Isotope effects are much greater for hydrogen than for any other element because the percentage differences between the masses of the various isotopes are considerably larger for hydrogen than for heavier elements. For example, a deuterium $\left({ }^{2} \mathrm{H}\right)$ atom is $100 \%$ heavier than a protium $\left({ }^{1} \mathrm{H}\right)$ atom, whereas a ${ }^{37} \mathrm{Cl}$ atom is only $6 \%$ heavier than a ${ }^{35} \mathrm{Cl}$ atom.

The effect of isotopic mass on the rate of a chemical reaction is called a kineticisotope effect. For example, deuterium can be separated from protium by passing an electric current through a solution of an inert electrolyte in ordinary water. (Electrolysis, the process of using an electric current to bring about chemical change, is discussed in Section 18.11.) Because the heavier D atom forms stronger bonds than the lighter H atom, $\mathrm{O}-\mathrm{D}$ bonds break more slowly than $\mathrm{O}-\mathrm{H}$ bonds. As a result, $\mathrm{D}_{2}$ evolves from $\mathrm{D}_{2} \mathrm{O}$ more slowly than $\mathrm{H}_{2}$ evolves from $\mathrm{H}_{2} \mathrm{O}$, so the remaining water is enriched in $\mathrm{D}_{2} \mathrm{O}$ as the electrolysis proceeds.

$$
\begin{array}{ll}
2 \mathrm{H}_{2} \mathrm{O}(l) \xrightarrow{\text { Electrolysis }} 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) & \text { Faster } \\
2 \mathrm{D}_{2} \mathrm{O}(l) \xrightarrow{\text { Electrolysis }} 2 \mathrm{D}_{2}(g)+\mathrm{O}_{2}(g) & \text { Slower }
\end{array}
$$

In a typical experiment, reduction of the water's volume from 2400 L to 83 mL yields $99 \%$ pure $\mathrm{D}_{2} \mathrm{O}$. Large amounts of $\mathrm{D}_{2} \mathrm{O}$ (about 160 tons per year in the United States) are manufactured by this method for use as a coolant and a moderator in nuclear reactors.

$\Delta$ Electrolysis of water gives $\mathrm{H}_{2}$ gas at one electrode and $\mathrm{O}_{2}$ gas at the other electrode. Which gas is at which electrode?

©Review bond dissociation energies and Hess's law to show that the formation of hydrogen from the decomposition of water requires energy, mainly due to the relative strength of the O-H bonds broken compared to the strength of $\mathrm{H}-\mathrm{H}$ and $\mathrm{O}=\mathrm{O}$ bonds formed.

Electrolysis of Water movie

Bassam Z. Shakhashiri, "Preparation and Properties of Hydrogen," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp.128-130. Hydrogen is produced by the reaction of zinc with hydrochloric acid and collected by displacing water from an inverted Erlenmeyer flask. The flame of a burning candle is extinguished when inserted into the flask, but an almost imperceptible flame is seen at the mouth of the flask, demonstrating the flammability of hydrogen in the presence of oxygen from the air.

[^16]- PROBLEM 14.2 The most abundant elements (by mass) in the body of a healthy human adult are oxygen ( $61.4 \%$ ), carbon ( $22.9 \%$ ), hydrogen ( $10.0 \%$ ), and nitrogen ( $2.6 \%$ ).
(a) Calculate the percent D if all the hydrogen atoms in a human were deuterium atoms.
(b) Calculate the percent C if all the carbon atoms were atoms of the isotope having a mass of $13 \mathrm{amu}\left({ }_{6}^{13} \mathrm{C}\right)$.
(c) Are isotope effects larger for hydrogen or for carbon? Explain.


## 14.3 | Preparation and Uses of Hydrogen

The purest hydrogen ( $>99.95 \%$ pure) is made by electrolysis of water. However, this process requires a large amount of energy- 286 kJ per mole of $\mathrm{H}_{2}$ producedand thus is not economical for large-scale production.

$$
2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \quad \Delta H^{\circ}=+572 \mathrm{~kJ}
$$

Small amounts of hydrogen are conveniently prepared in the laboratory by reaction of dilute acid with an active metal such as zinc:


This is a redox reaction (Section 4.6) in which hydrogen in $\mathrm{H}^{+}$is reduced from the +1 to the 0 oxidation state, while zinc is oxidized from the 0 to the +2 oxidation state. A typical apparatus for generating and collecting hydrogen is shown in Figure 14.1.


A FIGURE 14.1 Preparation of hydrogen by reaction of zinc metal with dilute acid. The $\mathrm{H}_{2}$ gas, which is nearly insoluble in water, displaces the water in the collection vessel.

Because water is the cheapest and most readily available source of hydrogen, all large-scale, industrial methods for producing hydrogen use an inexpensive reducing agent such as hot iron, carbon, or methane (natural gas) to extract the oxygen from steam:

$$
\begin{aligned}
4 \mathrm{H}_{2} \mathrm{O}(g)+3 \mathrm{Fe}(s) \xrightarrow{\text { Heat }} \mathrm{Fe}_{3} \mathrm{O}_{4}(s)+4 \mathrm{H}_{2}(g) & \Delta H^{\circ}=-151 \mathrm{~kJ} \\
\mathrm{H}_{2} \mathrm{O}(g)+\mathrm{C}(s) \xrightarrow{1000^{\circ} \mathrm{C}} \mathrm{CO}(g)+\mathrm{H}_{2}(g) & \Delta H^{\circ}=+131 \mathrm{~kJ}
\end{aligned}
$$

At present, the most important industrial method for producing hydrogen is the three-step, steam-hydrocarbon re-forming process. The first step in the process is the conversion of steam and methane to a mixture of carbon monoxide and hydrogen known as synthesis gas (so-called because it can be used as the starting material for the synthesis of liquid fuels). The reaction requires high temperature, moderately high pressure, and a nickel catalyst:

$$
\mathrm{H}_{2} \mathrm{O}(g)+\mathrm{CH}_{4}(g) \xrightarrow[\text { Ni catalyst }]{1100^{\circ} \mathrm{C}} \mathrm{CO}(g)+3 \mathrm{H}_{2}(g) \quad \Delta H^{\circ}=+206 \mathrm{~kJ}
$$

In the second step, the synthesis gas and additional steam are passed over a metal oxide catalyst at about $400^{\circ} \mathrm{C}$. Under these conditions, the carbon monoxide component of the synthesis gas and the steam are converted to carbon dioxide and more hydrogen. This reaction of CO with $\mathrm{H}_{2} \mathrm{O}$ is called the water-gas shift reaction because it shifts the composition of synthesis gas by removing the toxic carbon monoxide and producing more of the economically important hydrogen:

$$
\mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \xrightarrow[\text { Catalyst }]{400^{\circ} \mathrm{C}} \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g) \quad \Delta H^{\circ}=-41 \mathrm{~kJ}
$$

Finally, the unwanted carbon dioxide is removed in a third step by passing the $\mathrm{H}_{2} / \mathrm{CO}_{2}$ mixture through a basic aqueous solution. This treatment converts the carbon dioxide to carbonate ion, which remains in the aqueous phase:

$$
\mathrm{CO}_{2}(g)+2 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{CO}_{3}^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Approximately $95 \%$ of the $\mathrm{H}_{2}$ produced in industry is synthesized and consumed in industrial plants that manufacture other chemicals. The largest single consumer of hydrogen is the Haber process for synthesizing ammonia (Sections 13.6-13.10):

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)
$$

Large amounts of hydrogen are also used for the synthesis of methanol, $\mathrm{CH}_{3} \mathrm{OH}$, from carbon monoxide:

$$
\mathrm{CO}(g)+2 \mathrm{H}_{2}(g) \xrightarrow[\text { catalyst }]{\text { Cobalt }} \mathrm{CH}_{3} \mathrm{OH}(l)
$$

Methanol is an industrial solvent, a precursor to additives in unleaded gasolines, and a starting material for the manufacture of formaldehyde, $\mathrm{CH}_{2} \mathrm{O}$, used in making plastics. Annual U.S. production of methanol, about 1.7 billion gallons, consumes about 700,000 tons of hydrogen.

- PROBLEM 14.3 Write a balanced net ionic equation for the reaction of gallium metal with dilute acid.


## 14.4 | Reactivity of Hydrogen

The hydrogen atom is the simplest of all atoms, containing only a single 1 s electron and a single proton. In most versions of the periodic table, hydrogen is located in group 1A above the alkali metals because they too have just one valence electron. Alternatively, hydrogen could be placed in group 7A above the halogens because, like the halogens, it is just one electron short of a noble gas configuration (He). Thus, hydrogen has properties similar to those of both alkali metals and halogens. A hydrogen atom can lose an electron to form a hydrogen cation, $\mathrm{H}^{+}$, or it can gain an electron to yield a hydride anion, $\mathrm{H}^{-}$:

$$
\begin{array}{lll}
\text { Alkali-metal-like reaction: } & \mathrm{H}(g) \longrightarrow \mathrm{H}^{+}(g)+\mathrm{e}^{-} & E_{\mathrm{i}}=+1312 \mathrm{~kJ} / \mathrm{mol} \\
\text { Halogen-like reaction: } & \mathrm{H}(g)+\mathrm{e}^{-} \longrightarrow \mathrm{H}^{-}(g) & E_{\mathrm{ea}}=-73 \mathrm{~kJ} / \mathrm{mol}
\end{array}
$$

0 Alton Banks, "What's the Use? Hydrogen," J. Chem. Educ., Vol 66, 1989, 801.

vThe properties of molecular hydrogen compounds are best predicted if H is assigned a position in the periodic table based on its electronegativity (between B and C).

©
Chemical species with high charge-to-radius ratios, such as $\mathrm{H}^{+}$, are unstable and tend to form new species with lower charge and/or charge dispersed over a greater volume.


Because the amount of energy needed to ionize a hydrogen atom is so large ( $E_{\mathrm{i}}=1312 \mathrm{~kJ} / \mathrm{mol}$ ), hydrogen doesn't completely transfer its valence electron in chemical reactions. Instead, it shares this electron with a nonmetallic element to give a covalent compound such as $\mathrm{CH}_{4}, \mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{O}$, or HF. In this regard, hydrogen differs markedly from the alkali metals, which have much smaller ionization energies (ranging from $520 \mathrm{~kJ} / \mathrm{mol}$ for Li to $376 \mathrm{~kJ} / \mathrm{mol}$ for Cs ) and form ionic compounds with nonmetals.

Complete ionization of a hydrogen atom is possible in the gas phase, where the hydrogen ion is present as a bare proton of radius $\sim 1.5 \times 10^{-3} \mathrm{pm}$, about 100,000 times smaller than the radius of a hydrogen atom. In liquids and solids, however, the bare proton is too reactive to exist by itself. Instead, the proton bonds to a molecule that has a lone pair of electrons. In water, for example, the proton bonds to an $\mathrm{H}_{2} \mathrm{O}$ molecule to give a hydronium ion, $\mathrm{H}_{3} \mathrm{O}^{+}(a q)$.

Although adding an electron to hydrogen ( $E_{\text {ea }}=-73 \mathrm{~kJ} / \mathrm{mol}$ ) releases less energy than adding an electron to the halogens ( $E_{\text {ea }}=-295$ to $-349 \mathrm{~kJ} / \mathrm{mol}$ ), hydrogen will accept an electron from an active metal to give an ionic hydride, such as NaH or $\mathrm{CaH}_{2}$. In this regard, the behavior of hydrogen parallels that of the halogens, which form ionic halides such as NaCl and $\mathrm{CaCl}_{2}$.

At room temperature, $\mathrm{H}_{2}$ is relatively unreactive because of its strong $\mathrm{H}-\mathrm{H}$ bond, although it does react with $\mathrm{F}_{2}$ to give HF and with $\mathrm{Cl}_{2}$ in the presence of light to give HCl . Reactions of $\mathrm{H}_{2}$ with $\mathrm{O}_{2}, \mathrm{~N}_{2}$, or C , however, require high temperatures, the presence of a catalyst, or both. Catalysts such as metallic iron, nickel, palladium, or platinum facilitate the dissociation of $\mathrm{H}_{2}$ into highly reactive H atoms (Section 12.13). The reaction of hydrogen and oxygen is highly exothermic , and gas mixtures that contain as little as $4 \%$ by volume hydrogen in air are highly flammable and potentially explosive.

$$
2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H^{\circ}=-572 \mathrm{~kJ}
$$

Explosive burning of the hydrogen-filled dirigible Hindenburg during landing at Lakehurst, New Jersey, on May 6, 1937, killed 36 of the 97 persons aboard.


## 14.5 | Binary Hydrides

The binary hydrides are compounds that contain hydrogen and just one other element. Formulas and melting points of the simplest hydrides of the main-group elements are listed in Figure 14.2. Binary hydrides can be classified as ionic, covalent, or metallic.

## Ionic Hydrides

Ionic hydrides are saltlike, high-melting, white, crystalline compounds formed by the alkali metals and the heavier alkaline earth metals $\mathrm{Ca}, \mathrm{Sr}$, and Ba . They can be prepared by direct reaction of the elements at about $400^{\circ} \mathrm{C}$ :

$$
\begin{aligned}
2 \mathrm{Na}(l)+\mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NaH}(s) & \Delta H^{\circ}=-112.6 \mathrm{~kJ} \\
\mathrm{Ca}(s)+\mathrm{H}_{2}(g) \longrightarrow \mathrm{CaH}_{2}(s) & \Delta H^{\circ}=-181.5 \mathrm{~kJ}
\end{aligned}
$$



The alkali metal hydrides contain alkali metal cations and $\mathrm{H}^{-}$anions in a facecentered cubic crystal structure like that of sodium chloride (Section 10.9). Alkali metal hydrides are also ionic in the liquid state, as shown by the fact that the molten compounds conduct electricity.

The $\mathrm{H}^{-}$anion is a good proton acceptor, and ionic hydrides therefore react with water to give $\mathrm{H}_{2}$ gas and $\mathrm{OH}^{-}$ions:

$$
\mathrm{CaH}_{2}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{H}_{2}(g)+\mathrm{Ca}^{2+}(a q)+2 \mathrm{OH}^{-}(a q)
$$

This reaction of an ionic hydride with water is a redox reaction because the hydride reduces the water ( +1 oxidation state for H ) to $\mathrm{H}_{2}$ ( 0 oxidation state). In turn, the hydride ( -1 oxidation state for H ) is oxidized to $\mathrm{H}_{2}$. In general, ionic hydrides are good reducing agents. Some, such as potassium hydride, catch fire in air because of a rapid redox reaction with oxygen:

$$
2 \mathrm{KH}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{H}_{2} \mathrm{O}(g)+\mathrm{K}_{2} \mathrm{O}(s)
$$

## Covalent Hydrides

Covalent hydrides, as their name implies, are compounds in which hydrogen is attached to another element by a covalent bond. The most common examples are hydrides of nonmetallic elements, such as diborane $\left(\mathrm{B}_{2} \mathrm{H}_{6}\right)$, methane $\left(\mathrm{CH}_{4}\right)$, ammonia $\left(\mathrm{NH}_{3}\right)$, water $\left(\mathrm{H}_{2} \mathrm{O}\right)$, and the hydrogen halides ( HX ). Only the simplest covalent hydrides are listed in Figure 14.2, though more complex examples, such as hydrogen peroxide $\left(\mathrm{H}_{2} \mathrm{O}_{2}\right)$ and hydrazine $\left(\mathrm{N}_{2} \mathrm{H}_{4}\right)$, are also known. Because most covalent hydrides consist of discrete, small molecules that have relatively weak intermolecular forces, they are gases or volatile liquids at ordinary temperatures.

## Metallic Hydrides

Metallic hydrides are formed by reaction of the lanthanide and actinide metals and certain of the $d$-block transition metals with variable amounts of hydrogen. These hydrides have the general formula $\mathrm{MH}_{x}$, where the $x$ subscript represents

4 FIGURE 14.2 Formulas and melting points $\left({ }^{\circ} \mathrm{C}\right)$ of the simplest hydrides of the maingroup elements. The group 1A and the heavier group 2A hydrides, shown in blue, are ionic, while the other maingroup hydrides, shown in red, are covalent. The change in bond type, however, is gradual and continuous. Transition metal hydrides (not shown) are classified as metallic. The letter "d" indicates decomposition rather than melting on heating to the indicated temperature. The existence of $\mathrm{InH}_{3}$ and $\mathrm{TlH}_{3}$ is uncertain.

© Calcium hydride reacts with water to give bubbles of $\mathrm{H}_{2}$ gas and $\mathrm{OH}^{-}$ions. The red color is due to added phenolphthalein, which turns from colorless to red in the presence of a base.

$v$Like all molecular compounds which have weak intermolecular forces of attraction, covalent hydrides are gases, liquids, or low-melting solids.

© FIGURE 14.3 One plane of the structure of an interstitial metallic hydride. The metal atoms (larger spheres) have a face-centered cubic structure, and the hydrogen atoms (smaller spheres) occupy interstices (holes) between the metal atoms.

the number of H atoms in the simplest formula. They are often called interstitial hydrides because they are thought to consist of a crystal lattice of metal atoms with the smaller hydrogen atoms occupying holes, or interstices, between the larger metal atoms (Figure 14.3).

The nature of the bonding in metallic hydrides is not well understood, and it's not known whether the hydrogens are present as neutral H atoms, $\mathrm{H}^{+}$cations, or $\mathrm{H}^{-}$anions. Because the hydrogen atoms can fill a variable number of interstices, many metallic hydrides are nonstoichiometric compounds, meaning that their atomic composition can't be expressed as a ratio of small whole numbers. Examples are $\mathrm{TiH}_{1.7}, \mathrm{ZrH}_{1.9}$, and $\mathrm{PdH}_{x}(x<1)$. Other metallic hydrides, however, such as $\mathrm{TiH}_{2}$ and $\mathrm{UH}_{3}$, are stoichiometric compounds.

The properties of metallic hydrides depend on their composition, which is a function of the partial pressure of $\mathrm{H}_{2}$ gas in the surroundings. For example, $\mathrm{PdH}_{x}$ behaves as a metallic conductor for small values of $x$ but becomes a semiconductor when $x$ reaches about 0.5. (Semiconductors are discussed in Section 21.5.) The H atoms in $\mathrm{PdH}_{x}$ are highly mobile, and $\mathrm{H}_{2}$ can pass through a membrane of palladium metal. The process probably involves dissociation of $\mathrm{H}_{2}$ into H atoms on one surface of the membrane, diffusion of H atoms through the membrane as they jump from one interstice to another, and recombination to form $\mathrm{H}_{2}$ on the opposite surface of the membrane. Because other gases don't penetrate palladium, this process can be used to separate $\mathrm{H}_{2}$ or $\mathrm{D}_{2}$ from other components of gas mixtures.

Interstitial hydrides are of interest as potential hydrogen-storage devices because they can contain a remarkably large amount of hydrogen. Palladium, for example, absorbs up to 935 times its own volume of $\mathrm{H}_{2}$. This amount corresponds to a density of hydrogen comparable to that in liquid hydrogen. For use as a fuel, hydrogen could be stored as $\mathrm{PdH}_{x}$ and then liberated when needed, simply by heating the $\mathrm{PdH}_{x}$.

Favored at
higher temperature
$\mathrm{Pd}(s)+\frac{x}{2} \mathrm{H}_{2}(g) \rightleftharpoons \mathrm{PdH}_{x}(s) \quad \begin{aligned} & \text { Favored at } \\ & \text { lower temperature }\end{aligned}$
This approach, however, may not be economical compared to other methods of storing and transporting hydrogen because of the high cost and weight of palladium.

## Worked Example 14.1

Write a balanced net ionic equation for reaction of each of the following hydrides with water:
(a) Lithium hydride
(b) Barium hydride

## Strategy

Because lithium is a group 1A metal and barium is a group 2A metal, their hydrides have the formulas LiH and $\mathrm{BaH}_{2}$, respectively. Both are ionic hydrides and therefore react with water to give $\mathrm{H}_{2}$ gas and $\mathrm{OH}^{-}$ions. Balance the equations either by inspec-
 tion or by using the method of oxidation numbers (Section 4.9).

## Solution

(a) The $\mathrm{H}^{-}$ion reduces water to $\mathrm{H}_{2}$ gas, and in the process $\mathrm{H}^{-}$is oxidized to $\mathrm{H}_{2}$ gas.

(b)

Oxidation
numbers

## Worked EXample 14.2

How many grams of barium hydride must be treated with water to obtain 4.36 L of hydrogen at $20^{\circ} \mathrm{C}$ and 0.975 atm pressure?

## Strategy

The balanced equation for the reaction is given in Worked Example 14.1(b). We need to calculate the mass of $\mathrm{BaH}_{2}$ required to produce the given volume of $\mathrm{H}_{2}$. First, convert the volume of $\mathrm{H}_{2}$ to moles of $\mathrm{H}_{2}$ by using the ideal gas law. Next, use the balanced equation to calculate the number of moles of $\mathrm{BaH}_{2}$ required to produce the calculated number of moles of $\mathrm{H}_{2}$. Finally, use the molar mass of $\mathrm{BaH}_{2}(139.3 \mathrm{~g} / \mathrm{mol})$ to convert moles of $\mathrm{BaH}_{2}$ to grams of $\mathrm{BaH}_{2}$.

## SOlUTION

$$
\begin{aligned}
& n=\frac{P V}{R T}=\frac{(0.975 \mathrm{~atm})(4.36 \mathrm{~L})}{\left(0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)(293 \mathrm{~K})}=0.177 \mathrm{~mol} \mathrm{H}_{2} \\
& \text { Moles of } \mathrm{BaH}_{2}=0.177 \mathrm{~mol} \mathrm{H}_{2} \times \frac{1 \mathrm{~mol} \mathrm{BaH}_{2}}{2 \mathrm{~mol} \mathrm{H}_{2}}=0.0885 \mathrm{~mol} \mathrm{BaH}_{2} \\
& \text { Grams of } \mathrm{BaH}_{2}=0.0885 \mathrm{~mol} \mathrm{BaH}_{2} \times \frac{139.3 \mathrm{~g} \mathrm{BaH}_{2}}{1 \mathrm{~mol} \mathrm{BaH}_{2}}=12.3 \mathrm{~g} \mathrm{BaH}_{2}
\end{aligned}
$$


#### Abstract

$\checkmark$ BALLPARK CHECK Although the 4.36 L of $\mathrm{H}_{2}$ is not at STP ( 273 K and 1 atm pressure), the actual temperature ( 293 K ) and pressure ( 0.975 atm ) of the gas differ from STP by less than $10 \%$. Therefore, we can ignore the difference. Since 1 mol of an ideal gas occupies a volume of about 22 L at STP (Section 9.3), the number of moles of $\mathrm{H}_{2}$ in the 4.36 L volume of gas is approximately 4.4 L divided by $22 \mathrm{~L} / \mathrm{mol}$, or 0.20 mol of $\mathrm{H}_{2}$. According to the balanced equation for the reaction, 2 mol of $\mathrm{H}_{2}$ are obtained for every 1 mol of $\mathrm{BaH}_{2}$ that reacts. Therefore, the amount of $\mathrm{BaH}_{2}$ needed is approximately $0.20 / 2=0.10 \mathrm{~mol}$, or about 14 g , since the molar mass of $\mathrm{BaH}_{2}$ is $139.3 \mathrm{~g} / \mathrm{mol}$. The ballpark check agrees with the solution.


PROBLEM 14.4 Write a balanced net ionic equation for the reaction of each of the following hydrides with water:
(a) Strontium hydride
(b) Potassium hydride

PROBLEM 14.5 Calcium hydride is a convenient, portable source of hydrogen that is used, for example, to inflate weather balloons. If the reaction of $\mathrm{CaH}_{2}$ with water is used to inflate a balloon with $2.0 \times 10^{5} \mathrm{~L}$ of $\mathrm{H}_{2}$ gas at $25^{\circ} \mathrm{C}$ and 1.00 atm pressure, how many kilograms of $\mathrm{CaH}_{2}$ is needed?

## Worked Key Concept Example 14.3

The following pictures represent binary hydrides $\mathrm{AH}_{\mathrm{x}}$, where $\mathrm{A}=\mathrm{K}, \mathrm{Ti}, \mathrm{C}$, or F . Ivory spheres represent H atoms or ions, and burgundy spheres represent atoms or ions of the element A.

(a) Write the formula of each hydride, and classify each as ionic, covalent, or interstitial.
(b) Which hydride has the lowest melting point? Explain.
(c) Which hydride reacts with water at $25^{\circ} \mathrm{C}$ to give $\mathrm{H}_{2}$ gas?

## Strategy

(a) The location of each element $\mathrm{A}(\mathrm{K}, \mathrm{Ti}, \mathrm{C}$, or F$)$ in the periodic table tells us the formula and the type of hydride. Alkali metals in group 1A form ionic hydrides, have the formula AH, and have extended three-dimensional crystal structures. Certain transition elements form interstitial hydrides, often have nonstoichiometric formulas $\mathrm{AH}_{\mathrm{x}}$, and also have extended three-dimensional structures. Nonmetals form covalent hydrides, which exist as discrete molecules and have formulas that depend on the periodic group of the element $A$.
(b) Covalent hydrides have lower melting points than ionic and interstitial hydrides because they have only relatively weak intermolecular forces between molecules.
(c) Only ionic hydrides react with water at $25^{\circ} \mathrm{C}$ to give $\mathrm{H}_{2}$ gas.

## Solution

(a) The pictures indicate that hydrides (1) and (2) contain discrete AH and $\mathrm{AH}_{4}$ molecules, respectively, and are therefore covalent hydrides of the nonmetallic elements F and C. Fluorine in group 7A forms a hydride with formula HF, and C in group 4A forms a tetrahedral hydride with formula $\mathrm{CH}_{4}$. Therefore, hydride (1) is HF, and (2) is $\mathrm{CH}_{4}$. Picture (3) shows a two-dimensional piece of the extended three-dimensional face-centered-cubic crystal structure of a solid ionic hydride with formula AH. (The structure is the same as that of NaCl .) Therefore, hydride (3) is the ionic hydride KH. Picture (4) represents a piece of the structure of a solid, nonstoichiometric interstitial hydride. The transition metal Ti forms such a hydride, so hydride (4) is the interstitial hydride $\mathrm{TiH}_{\mathrm{x}}$.
(b) The hydride with the lowest melting point will be one of the covalent hydrides, HF or $\mathrm{CH}_{4}$. Intermolecular forces for the polar HF molecules include dipole-dipole forces and hydrogen bonding, in addition to London dispersion forces, whereas only weak London dispersion forces exist for the nonpolar $\mathrm{CH}_{4}$ molecules. Therefore, $\mathrm{CH}_{4}$ has the lowest melting point, as confirmed by the data in Figure 14.2.
(c) KH is the only ionic hydride and is therefore the hydride that reacts with water at $25^{\circ} \mathrm{C}$ to give $\mathrm{H}_{2}$ gas:

$$
\mathrm{KH}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{H}_{2}(g)+\mathrm{K}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

-KEY CONCEPT PROBLEM 14.6 The following pictures represent binary hydrides $\mathrm{AH}_{\mathrm{x}}$, where $\mathrm{A}=\mathrm{Br}, \mathrm{Li}, \mathrm{P}$, or Zr . Ivory spheres represent H atoms or ions, and burgundy spheres represent atoms or ions of the element $A$.

(a) Write the formula of each hydride, and classify each as ionic, covalent, or interstitial.
(b) Which hydrides are likely to be solids at $25^{\circ} \mathrm{C}$, and which are likely to be gases? Explain.
(c) Which hydride reacts with water at $25^{\circ} \mathrm{C}$ to give a basic solution?

- PROBLEM 14.7 If palladium metal (density $12.0 \mathrm{~g} / \mathrm{cm}^{3}$ ) dissolves 935 times its own volume of $\mathrm{H}_{2}$ at STP, what is the value of $x$ in the formula $\mathrm{PdH}_{x}$ ? What is the density of hydrogen in $\mathrm{PdH}_{x}$ ? What is the molarity of H atoms in $\mathrm{PdH}_{x}$ ? Assume that the volume of palladium is unchanged when the H atoms go into the interstices.


## 14.6 | Oxygen

Oxygen was first isolated and characterized in the period 1771-1774 by the English chemist Joseph Priestley and the Swedish chemist Karl Wilhelm Scheele. Priestley and Scheele found that heating certain compounds such as mercury(II) oxide generates a colorless, odorless, tasteless gas that supports combustion better than air does:

$$
2 \mathrm{HgO}(\mathrm{~s}) \xrightarrow{\text { Heat }} 2 \mathrm{Hg}(\mathrm{l})+\mathrm{O}_{2}(\mathrm{~g})
$$

Priestley called the gas "dephlogisticated air," but Lavoisier soon recognized it as an element and named it "oxygen."

Gaseous $\mathrm{O}_{2}$ condenses at $-183^{\circ} \mathrm{C}$ to form a pale blue liquid and freezes at $-219^{\circ} \mathrm{C}$ to give a pale blue solid. In all three phases-gas, liquid, and solid- $\mathrm{O}_{2}$ is paramagnetic, as illustrated previously in Figure 7.17. The bond length in $\mathrm{O}_{2}$ is 121 pm , appreciably shorter than the $\mathrm{O}-\mathrm{O}$ single bond in $\mathrm{H}_{2} \mathrm{O}_{2}(148 \mathrm{pm})$, and the bond dissociation energy of $\mathrm{O}_{2}(498 \mathrm{~kJ})$ is intermediate between that for the single bond in $\mathrm{F}_{2}(158 \mathrm{~kJ})$ and the triple bond in $\mathrm{N}_{2}(945 \mathrm{~kJ})$. These properties are consistent with the presence of a double bond in $\mathrm{O}_{2}$ (Section 7.14).

Oxygen is the most abundant element on the surface of our planet and is crucial to human life. It's in the air we breathe, the water we drink, and the food we eat. It's the oxidizing agent in the metabolic "burning" of foods, and it's an important component of biological molecules: Approximately one-fourth of the atoms in living organisms are oxygen. Moreover, oxygen is the oxidizing agent in the combustion processes that provide thermal and electrical energy for maintaining our industrialized civilization.

On a mass basis, oxygen constitutes $23 \%$ of the atmosphere ( $21 \%$ by volume), $46 \%$ of the lithosphere (the earth's crust), and more than $85 \%$ of the hydrosphere. In the atmosphere, oxygen is found primarily as $\mathrm{O}_{2}$, sometimes called dioxygen. The oxygen in the hydrosphere is in the form of $\mathrm{H}_{2} \mathrm{O}$, but enough dissolved $\mathrm{O}_{2}$ is present to maintain aquatic life. In the lithosphere, oxygen is combined with other
 Foil A. Miller, "Joseph Priestly, Preeminent Amateur Chemist," J. Chem. Educ., Vol 66, 1989, 801.

© Liquid oxygen has a pale blue color.

VRemember from Chapter 7 that double bonds are shorter and stronger than single
bonds but longer and weaker than triple bonds formed from the same two atoms.

$\Delta$ Oxygen in the earth's atmosphere is produced by photosynthesis in plants, such as this underwater elodea.

$\delta$Bassam Z. Shakhashiri, "Preparation and Properties of Oxygen," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp. 137-141. Oxygen is produced by the reaction of hydrogen peroxide with potassium permanganate and is collected by displacing water from an inverted Erlenmeyer flask. The oxygen is shown to support vigorous combustion when a glowing wooden ember and hot steel wool burst into flames when placed in an atmosphere of oxygen gas.


A Crude iron is converted to steel by oxidizing impurities with $\mathrm{O}_{2}$ gas.
elements in crustal rocks composed of silicates, carbonates, oxides, and other oxygen-containing minerals.

The amount of oxygen in the atmosphere remains fairly constant at about $1.18 \times 10^{18} \mathrm{~kg}$ because the combustion and respiration processes that remove $\mathrm{O}_{2}$ are balanced by photosynthesis, the complex process in which green plants use solar energy to produce $\mathrm{O}_{2}$ and glucose from carbon dioxide and water:

$$
6 \mathrm{CO}_{2}+6 \mathrm{H}_{2} \mathrm{O} \xrightarrow{h \nu} 6 \mathrm{O}_{2}+\underset{\text { Glucose }}{\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}}
$$

The metabolism of carbohydrates in our bodies to give carbon dioxide and water is essentially the reverse of the photosynthesis reaction. The energy from the sun that is absorbed in the endothermic photosynthetic process is released when organic matter is burned or metabolized to carbon dioxide and water. This cycling of oxygen between the atmosphere and the biosphere acts as the mechanism for converting solar energy to the chemical energy needed for metabolic processes. Ultimately, therefore, nearly all our energy comes from the sun.

## 14.7 | Preparation and Uses of Oxygen

Small amounts of $\mathrm{O}_{2}$ can be prepared in the laboratory by electrolysis of water, by decomposition of aqueous hydrogen peroxide in the presence of a catalyst such as $\mathrm{Fe}^{3+}$, or by thermal decomposition of an oxoacid salt, such as potassium chlorate, $\mathrm{KClO}_{3}$ :

$$
\begin{aligned}
& 2 \mathrm{H}_{2} \mathrm{O}(l) \xrightarrow{\text { Electrolysis }} 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \\
& 2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \xrightarrow{\text { Catalyst }} 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g) \\
& 2 \mathrm{KClO}_{3}(s) \xrightarrow[\mathrm{MnO}_{2} \text { catalyst }]{\text { Heat }} 2 \mathrm{KCl}(s)+3 \mathrm{O}_{2}(g)
\end{aligned}
$$

Because oxygen is relatively insoluble in water, it can be collected by water displacement using the same apparatus employed to collect hydrogen (Figure 14.1). Oxygen is seldom prepared in the laboratory, though, because it is commercially available as a compressed gas in high-pressure steel cylinders.

Oxygen is produced on an industrial scale, along with nitrogen and argon, by fractional distillation of liquefied air. When liquid air warms in a suitable distilling column, the more volatile components-nitrogen (bp $-196^{\circ} \mathrm{C}$ ) and argon (bp $-186^{\circ} \mathrm{C}$ )—can be removed as gases from the top of the column. The less volatile oxygen (bp $-183^{\circ} \mathrm{C}$ ) remains as a liquid at the bottom. Oxygen is the third-ranking industrial chemical produced in the United States ( 26 million tons); only sulfuric acid ( 40 million tons) and nitrogen ( 35 million tons) are produced in greater quantities.

More than two-thirds of the oxygen produced industrially is used in making steel. The crude iron obtained from a blast furnace contains impurities, such as carbon, silicon, and phosphorus, which adversely affect the mechanical properties of the metal. In refining crude iron to strong steels, the impurity levels are lowered by treating the iron with a controlled amount of $\mathrm{O}_{2}$, thus converting the impurities to the corresponding oxides.

Among its other uses, oxygen is used in sewage treatment to destroy malodorous compounds and in paper bleaching to oxidize compounds that impart unwanted colors. In the oxyacetylene torch, the highly exothermic reaction between $\mathrm{O}_{2}$ and acetylene provides the high temperatures $\left(>3000^{\circ} \mathrm{C}\right)$ needed for cutting and welding metals:

$$
\begin{aligned}
& 2 \mathrm{HC} \equiv \mathrm{CH}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 4 \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \quad \Delta H^{\circ}=-2511 \mathrm{~kJ} \\
& \text { Acetylene }
\end{aligned}
$$

In all its applications, $\mathrm{O}_{2}$ serves as an inexpensive and readily available oxidizing agent.

## Worked Example 14.4

How many milliliters of $\mathrm{O}_{2}$ gas at $25^{\circ} \mathrm{C}$ and 1.00 atm pressure can be obtained by thermal decomposition of 0.200 g of $\mathrm{KClO}_{3}$ ?

$$
2 \mathrm{KClO}_{3}(s) \longrightarrow 2 \mathrm{KCl}(s)+3 \mathrm{O}_{2}(g)
$$

## Strategy

Follow a three-step procedure. First, use the molar mass of $\mathrm{KClO}_{3}(122.6 \mathrm{~g} / \mathrm{mol})$ to convert the number of grams of $\mathrm{KClO}_{3}$ to moles of $\mathrm{KClO}_{3}$. Next, use the balanced equation and the number of moles of $\mathrm{KClO}_{3}$ to calculate the number of moles of $\mathrm{O}_{2}$ produced. Finally, use the ideal gas law and the number of moles of $\mathrm{O}_{2}$ to calculate the volume of $\mathrm{O}_{2}$.

## Solution

$$
\begin{aligned}
& \text { Moles of } \mathrm{KClO}_{3}=0.200 \mathrm{~g} \mathrm{KClO}_{3} \times \frac{1 \mathrm{~mol} \mathrm{KClO}_{3}}{122.6 \mathrm{~g} \mathrm{KClO}_{3}}=1.63 \times 10^{-3} \mathrm{~mol} \mathrm{KClO}_{3} \\
& \text { Moles of } \mathrm{O}_{2}=\left(\frac{3 \mathrm{~mol} \mathrm{O}_{2}}{2 \mathrm{~mol} \mathrm{KClO}_{3}}\right)\left(1.63 \times 10^{-3} \mathrm{~mol} \mathrm{KClO}_{3}\right)=2.44 \times 10^{-3} \mathrm{~mol} \mathrm{O}_{2} \\
& V=\frac{n R T}{P}=\frac{\left(2.44 \times 10^{-3} \mathrm{~mol}\right)\left(0.08206 \frac{\mathrm{~L} \cdot \mathrm{~atm}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)(298 \mathrm{~K})}{1.00 \mathrm{~atm}} \\
& \quad=5.97 \times 10^{-2} \mathrm{~L}=59.7 \mathrm{~mL}
\end{aligned}
$$

$\checkmark$ Ballpark Check Since 1 mol of $\mathrm{KClO}_{3}$ contains a bit more than $100 \mathrm{~g}, 0.200 \mathrm{~g}$ of $\mathrm{KClO}_{3}$ is a bit less than $2 \times 10^{-3} \mathrm{~mol}$. According to the balanced equation, decomposition of $2 \times 10^{-3} \mathrm{~mol}$ of $\mathrm{KClO}_{3}$ yields $3 \times 10^{-3} \mathrm{~mol}$ of $\mathrm{O}_{2}$. Because the experimental conditions are close to STP and 1 mol of an ideal gas at STP occupies about 22 L , the volume of $\mathrm{O}_{2}$ is a bit less than $\left(3 \times 10^{-3} \mathrm{~mol}\right)(22 \mathrm{~L} / \mathrm{mol})=66 \times 10^{-3} \mathrm{~L}$, or 66 mL . The ballpark check agrees with the solution.

PROBLEM 14.8 How many milliliters of $\mathrm{O}_{2}$ gas at $25^{\circ} \mathrm{C}$ and 1.00 atm pressure are obtained by thermal decomposition of 0.200 g of $\mathrm{KMnO}_{4}$ ? The balanced equation for the reaction is $2 \mathrm{KMnO}_{4}(s) \rightarrow \mathrm{K}_{2} \mathrm{MnO}_{4}(s)+\mathrm{MnO}_{2}(s)+\mathrm{O}_{2}(g)$.

## 14.8 | Reactivity of Oxygen

We can anticipate the reactivity of oxygen from the electron configuration of an oxygen atom $\left(1 s^{2} 2 s^{2} 2 p^{4}\right)$ and its high electronegativity (3.5). With six valence electrons, oxygen is just two electrons short of the stable octet configuration of neon, the next noble gas. Oxygen can therefore achieve an octet configuration either by accepting two electrons from an active metal or by gaining a share in two additional electrons through covalent bonding. Thus, oxygen reacts with active metals, such as lithium and magnesium, to give ionic oxides:

$$
\begin{aligned}
4 \mathrm{Li}(s)+\mathrm{O}_{2}(g) & \longrightarrow 2 \mathrm{Li}_{2} \mathrm{O}(s) \\
2 \mathrm{Mg}(s)+\mathrm{O}_{2}(g) & \longrightarrow 2 \mathrm{MgO}(s)
\end{aligned}
$$

On the other hand, with nonmetals, such as hydrogen, carbon, sulfur, and phosphorus, oxygen forms covalent oxides:

$$
\begin{aligned}
2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) & \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l) \\
\mathrm{C}(s)+\mathrm{O}_{2}(g) & \longrightarrow \mathrm{CO}_{2}(g) \\
\mathrm{S}_{8}(s)+8 \mathrm{O}_{2}(g) & \longrightarrow 8 \mathrm{SO}_{2}(g) \\
\mathrm{P}_{4}(s)+5 \mathrm{O}_{2}(g) & \longrightarrow \mathrm{P}_{4} \mathrm{O}_{10}(s)
\end{aligned}
$$



Bassam Z. Shakhashiri, "Combining Volume of Oxygen with Sulfur," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985) pp. 190-192. $\mathrm{SO}_{2}$, not $\mathrm{SO}_{3}$, is produced in the combustion reaction of sulfur and oxygen.

FIGURE 14.5 Some reactions of oxygen. (a) Magnesium metal burns in oxygen with a bright white flame, producing a white smoke of solid magnesium oxide, MgO .
(b) Hot, molten sulfur burns in oxygen with a blue flame, forming gaseous sulfur dioxide, $\mathrm{SO}_{2}$. (c) White phosphorus spontaneously inflames in oxygen, yielding an incandescent white smoke of solid $\mathrm{P}_{4} \mathrm{O}_{10}$.



In covalent compounds, oxygen generally achieves an octet configuration either by forming two single bonds, as in $\mathrm{H}_{2} \mathrm{O}$, or one double bond, as in $\mathrm{CO}_{2}$. Oxygen often forms a double bond to small atoms such as carbon and nitrogen because there is good $\pi$ overlap between the relatively compact $p$ orbitals of second-row atoms. With larger atoms such as silicon, however, there is less efficient $\pi$ overlap, and double bond formation is therefore less common (Figure 14.4).

FIGURE 14.4 Pi overlap between the $p$ orbitals of oxygen and other atoms. (a) With a second-row atom, such as carbon, oxygen forms a strong $\pi$ bond. (b) With a larger atom, such as silicon, oxygen tends not to form $\pi$ bonds because the longer $\mathrm{Si}-\mathrm{O}$ distance and the larger, more diffuse silicon orbitals result in poor $\pi$ overlap. double (occasionally triple) bonds with other period 2 nonmetals in order to attain a complete octet. Less commonly does it form multiple bonds with period 3 and higher-period elements.


Basic oxides, also called base anhydrides, are ionic and are formed by metals on the left side of the periodic table. Water-soluble basic oxides, such as $\mathrm{Na}_{2} \mathrm{O}$, dissolve by reacting with water to produce $\mathrm{OH}^{-}$ions:

$$
\mathrm{Na}_{2} \mathrm{O}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{Na}^{+}(a q)+2 \mathrm{OH}^{-}(a q)
$$

Water-insoluble basic oxides, such as MgO , can dissolve in strong acids because $\mathrm{H}^{+}$ions from the acid combine with the $\mathrm{O}^{2-}$ ion to produce water:

$$
\mathrm{MgO}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Mg}^{2+}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Acidic oxides, also called acid anhydrides, are covalent and are formed by the nonmetals on the right side of the periodic table. Water-soluble acidic oxides, such as $\mathrm{N}_{2} \mathrm{O}_{5}$, dissolve by reacting with water to produce aqueous $\mathrm{H}^{+}$ions:

$$
\mathrm{N}_{2} \mathrm{O}_{5}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{H}^{+}(a q)+2 \mathrm{NO}_{3}^{-}(a q)
$$

Water-insoluble acidic oxides, such as $\mathrm{SiO}_{2}$, can dissolve in strong bases:

$$
\mathrm{SiO}_{2}(s)+2 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{SiO}_{3}^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Amphoteric oxides exhibit both acidic and basic properties. (The term amphoteric [am-fo-tare-ic] comes from the Greek word amphoteros, meaning "in both ways.") For example, $\mathrm{Al}_{2} \mathrm{O}_{3}$ is insoluble in water, but it dissolves both in strong acids and in strong bases. $\mathrm{Al}_{2} \mathrm{O}_{3}$ behaves as a base when it reacts with acids, giving the $\mathrm{Al}^{3+}$ ion, but it behaves as an acid when it reacts with bases, yielding the aluminate ion, $\mathrm{Al}(\mathrm{OH})_{4}{ }^{-}$.

$$
\begin{array}{ll}
\text { Basic behavior: } & \mathrm{Al}_{2} \mathrm{O}_{3}(s)+6 \mathrm{H}^{+}(a q) \longrightarrow 2 \mathrm{Al}^{3+}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l) \\
\text { Acidic behavior: } & \mathrm{Al}_{2} \mathrm{O}_{3}(s)+2 \mathrm{OH}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{Al}(\mathrm{OH})_{4}^{-}(a q)
\end{array}
$$

The elements that form amphoteric oxides have intermediate electronegativities, and the bonds in their oxides have intermediate ionic-covalent character.

The acid-base properties and the ionic-covalent character of an element's oxide depend on both the element's position in the periodic table and its oxidation number. As Figure 14.6 shows, both the acidic character and the covalent character of an oxide increase across the periodic table from the active metals on the left to the electronegative nonmetals on the right. In the third row, for example, $\mathrm{Na}_{2} \mathrm{O}$
© FIGURE 14.6 Formulas, acid-base properties, and the covalent-ionic character of the oxides of main-group elements in their highest oxidation states. Basic oxides are shown in blue, acidic oxides are shown in red, and amphoteric oxides are shown in violet.


$\nabla$
The most basic oxides are ionic solids formed by the reaction of oxygen with elements at the left and bottom of the periodic table; the most acidic oxides are covalent and formed by the reaction of oxygen with elements at the right and top of the periodic table.

Like ionic hydrides, ionic oxides are crystalline solids with high melting points.

Like covalent hydrides, most covalent oxides are gases, liquids, or low-melting solids.

Melting Point of Oxides activity


- Telephone messages are transmitted by light passing through optical fibers made of $\mathrm{SiO}_{2}$.
and MgO are basic, $\mathrm{Al}_{2} \mathrm{O}_{3}$ is amphoteric, and $\mathrm{SiO}_{2}, \mathrm{P}_{4} \mathrm{O}_{10}, \mathrm{SO}_{3}$, and $\mathrm{Cl}_{2} \mathrm{O}_{7}$ are acidic. Within a group in the periodic table, both the basic character and the ionic character of an oxide increase from the more electronegative elements at the top to the less electronegative ones at the bottom. In group 3 A , for example, $\mathrm{B}_{2} \mathrm{O}_{3}$ is acidic, $\mathrm{Al}_{2} \mathrm{O}_{3}$ and $\mathrm{Ga}_{2} \mathrm{O}_{3}$ are amphoteric, and $\mathrm{In}_{2} \mathrm{O}_{3}$ and $\mathrm{Tl}_{2} \mathrm{O}_{3}$ are basic. Combining the horizontal and vertical trends in acidity, we find the most acidic oxides in the upper right of the periodic table, the most basic oxides in the lower left, and the amphoteric oxides in a roughly diagonal band stretching across the middle.

Both the acidic character and the covalent character of different oxides of the same element increase with increasing oxidation number of the element. Thus, sulfur $(\mathrm{VI})$ oxide $\left(\mathrm{SO}_{3}\right)$ is more acidic than sulfur $(\mathrm{IV})$ oxide $\left(\mathrm{SO}_{2}\right)$. Reaction of $\mathrm{SO}_{3}$ with water gives a strong acid (sulfuric acid, $\mathrm{H}_{2} \mathrm{SO}_{4}$ ), whereas reaction of $\mathrm{SO}_{2}$ with water yields a weak acid (sulfurous acid, $\mathrm{H}_{2} \mathrm{SO}_{3}$ ). The oxides of chromium exhibit the same trend. Chromium(VI) oxide $\left(\mathrm{CrO}_{3}\right)$ is acidic, chromium(III) oxide $\left(\mathrm{Cr}_{2} \mathrm{O}_{3}\right)$ is amphoteric, and chromium(II) oxide ( CrO ) is basic.

As the bonding in oxides gradually changes from ionic to covalent, a corresponding change in structure, from extended three-dimensional structures to discrete molecular structures, occurs. This results in a change in physical properties, as illustrated by the melting points in Figure 14.7 MgO , an ionic oxide with the face-centered cubic NaCl crystal structure, has a very high melting point because of its high lattice energy (Section 6.6). $\mathrm{Al}_{2} \mathrm{O}_{3}$ and $\mathrm{SiO}_{2}$ also have extended three-dimensional structures (Section 10.10), but they exhibit increasingly covalent character and have increasingly lower melting points. The trend continues to $\mathrm{P}_{4} \mathrm{O}_{10}, \mathrm{SO}_{3}$, and $\mathrm{Cl}_{2} \mathrm{O}_{7}$, which are molecular substances with strong covalent bonds within each molecule but only weak intermolecular forces between molecules. Thus, $\mathrm{P}_{4} \mathrm{O}_{10}$ is a volatile, relatively low-melting solid, and $\mathrm{SO}_{3}$ and $\mathrm{Cl}_{2} \mathrm{O}_{7}$ are volatile liquids.


The uses of oxides are determined by their properties. Because of their high thermal stability, mechanical strength, and electrical resistance, MgO and $\mathrm{Al}_{2} \mathrm{O}_{3}$ are used as high-temperature electrical insulators in products such as electrical heaters and spark plugs. $\mathrm{SiO}_{2}$ is the main component of the optical fibers used for communications. The acidic oxides of the nonmetals are important as precursors to industrial acids, such as $\mathrm{HNO}_{3}, \mathrm{H}_{3} \mathrm{PO}_{4}$, and $\mathrm{H}_{2} \mathrm{SO}_{4}$.

- KEY CONCEPT PROBLEM 14.9 Look at the location of elements A, B, and C in the accompanying periodic table.

(a) Write the formula of the oxide of each element.
(b) Which oxide is the most ionic, and which is the most covalent?
(c) Which oxide is the most acidic, and which is the most basic?
(d) Which oxide can react with both $\mathrm{H}^{+}(a q)$ and $\mathrm{OH}^{-}(a q)$ ?

PROBLEM 14.10 Write balanced net ionic equations for the following reactions:
(a) Dissolution of solid $\mathrm{Li}_{2} \mathrm{O}$ in water
(b) Dissolution of $\mathrm{SO}_{3}$ in water
(c) Dissolution of the amphoteric oxide $\mathrm{Cr}_{2} \mathrm{O}_{3}$ in strong acid
(d) Dissolution of $\mathrm{Cr}_{2} \mathrm{O}_{3}$ in strong base to give $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}$ions

## $14.10 \mid$ Peroxides and Superoxides

When the heavier group 1 A and 2 A metals are heated in an excess of oxygen, they form either peroxides, such as $\mathrm{Na}_{2} \mathrm{O}_{2}$ and $\mathrm{BaO}_{2}$, or superoxides, such as $\mathrm{KO}_{2}$, $\mathrm{RbO}_{2}$, and $\mathrm{CsO}_{2}$. Under the same conditions, however, the lighter group 1 A and 2 A metals form normal oxides, such as $\mathrm{Li}_{2} \mathrm{O}, \mathrm{MgO}, \mathrm{CaO}$, and SrO . All these compounds are ionic solids, and the nature of the product obtained depends on the amount of $\mathrm{O}_{2}$ present, the temperature, the sizes of the ions and how they pack together, and the resultant lattice energies of the various crystalline solids (Section 6.6).

The metal peroxides contain the peroxide ion, $\mathrm{O}_{2}{ }^{2-}$, and the metal superoxides contain the superoxide ion, $\mathrm{O}_{2}{ }^{-}$:


Peroxide ion


Superoxide ion

The peroxide ion is diamagnetic and has an $\mathrm{O}-\mathrm{O}$ single bond length of 149 pm . The superoxide ion, with one unpaired electron, is paramagnetic and has an $\mathrm{O}^{-} \mathrm{O}$ bond length of 133 pm , intermediate between the bond length of the peroxide ion $\left(\mathrm{O}_{2}{ }^{2-}\right)$ and the $\mathrm{O}=\mathrm{O}$ double bond length of 121 pm in $\mathrm{O}_{2}$. This suggests a bond order of 1.5 for $\mathrm{O}_{2}{ }^{-}$.

The trend in bond lengths and the magnetic properties of $\mathrm{O}_{2}, \mathrm{O}_{2}{ }^{-}$, and $\mathrm{O}_{2}{ }^{2-}$ are all nicely explained by the molecular orbital (MO) theory discussed in Section 7.14. Recall that the occupied MOs of highest energy in $\mathrm{O}_{2}$ are the two, degenerate, antibonding $\pi^{*} 2 p$ orbitals. Each of these orbitals contains one electron, and the two electrons have the same spin, in accord with Hund's rule. Thus, the $\mathrm{O}_{2}$ molecule is paramagnetic and has a bond order of 2. The $\mathrm{O}_{2}{ }^{-}$ion has one additional electron (a total of 3 ) in the $\pi^{*} 2 p$ orbitals, and the $\mathrm{O}_{2}{ }^{2-}$ ion has two additional electrons (a total of 4) in the $\pi^{*}{ }_{2 p}$ orbitals. As the electron population of the antibonding $\pi^{*} 2 p$ orbitals increases, the bond order decreases and the bond length increases (Table 14.2).

TABLE 14.2 Bond and Magnetic Properties of Diatomic Oxygen Species

|  | Number <br> of $\boldsymbol{\pi}^{*} \boldsymbol{2} \boldsymbol{p}$ <br> Electrons | Number of <br> Unpaired <br> Electrons | Bond <br> Order | Bond <br> Length <br> (pm) | Magnetic <br> Properties |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{O}_{2}$ | 2 | 2 | 2 | 121 | Paramagnetic |
| $\mathrm{O}_{2}{ }^{-}$ | 3 | 1 | 1.5 | 133 | Paramagnetic |
| $\mathrm{O}_{2}{ }^{2-}$ | 4 | 0 | 1 | 149 | Diamagnetic |

17. Michael Laing, "The Three Forms of Molecular Oxygen," J. Chem. Educ., Vol 66, 1989, 453-455.

$\sqrt{ }$Note that the presence of an $\mathrm{O}-\mathrm{O}$ bond indicates that the compound is a peroxide (or, less commonly, a superoxide).


- Dissolution of sodium peroxide in water that contains phenolphthalein gives a red color because of formation of $\mathrm{OH}^{-}$ions.

Like the oxide ion, the peroxide ion is a basic anion. When a metal peroxide dissolves in water, the $\mathrm{O}_{2}{ }^{2-}$ ion picks up a proton from water, forming $\mathrm{HO}_{2}{ }^{-}$and $\mathrm{OH}^{-}$ions. The dissolution of $\mathrm{Na}_{2} \mathrm{O}_{2}$ is typical:

$$
\mathrm{Na}_{2} \mathrm{O}_{2}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{Na}^{+}(a q)+\mathrm{HO}_{2}^{-}(a q)+\mathrm{OH}^{-}(a q)
$$

In the presence of a strong acid, the $\mathrm{O}_{2}{ }^{2-}$ ion combines with two protons, yielding hydrogen peroxide, $\mathrm{H}_{2} \mathrm{O}_{2}$. For example, aqueous solutions of $\mathrm{H}_{2} \mathrm{O}_{2}$ are conveniently prepared in the laboratory by reaction of barium peroxide with a stoichiometric amount of sulfuric acid:

$$
\mathrm{BaO}_{2}(s)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \longrightarrow \mathrm{BaSO}_{4}(s)+\mathrm{H}_{2} \mathrm{O}_{2}(a q)
$$

The by-product, barium sulfate, is insoluble and easily removed by filtration.
When metal superoxides, such as $\mathrm{KO}_{2}$, dissolve in water, they decompose with evolution of oxygen:
Oxidation numbers


This decomposition is a redox reaction in which the oxygen in $\mathrm{KO}_{2}$ is simultaneously oxidized from the $-1 / 2$ oxidation state in $\mathrm{O}_{2}{ }^{-}$to the 0 oxidation state in $\mathrm{O}_{2}$ and reduced from the $-1 / 2$ oxidation state in $\mathrm{O}_{2}{ }^{-}$to the -1 oxidation state in $\mathrm{HO}_{2}{ }^{-}$. A reaction in which a substance is both oxidized and reduced is called a disproportionation reaction. One useful consequence of the $\mathrm{KO}_{2}$ disproportionation reaction in water is that potassium superoxide can serve as a convenient source of oxygen in masks worn by firefighters. The oxygen results from reaction of $\mathrm{KO}_{2}$ with exhaled water vapor.

A self-contained breathing apparatus used by firefighters. The source of $\mathrm{O}_{2}$ is the reaction of $\mathrm{KO}_{2}$ with exhaled water vapor.


## Worked Example 14.5

What is the oxidation number of oxygen in each of the following compounds? Tell whether the compound is an oxide, a peroxide, or a superoxide.
(a) $\mathrm{KO}_{2}$
(b) $\mathrm{BaO}_{2}$
(c) $\mathrm{SiO}_{2}$

## Strategy

First determine the oxidation number of the other element, which is generally equal to the periodic group number. Then assign an oxidation number to oxygen so that the sum of the oxidation numbers is zero.

## Solution

(a) Because K in group 1 A has an oxidation number of +1 , the oxidation number of oxygen in $\mathrm{KO}_{2}$ must be $-1 / 2$. Thus, $\mathrm{KO}_{2}$ is a superoxide.
(b) Because Ba in group 2A has an oxidation number of +2 , the oxidation number of oxygen in $\mathrm{BaO}_{2}$ must be -1 . Thus, $\mathrm{BaO}_{2}$ is a peroxide.
(c) Because Si in group 4 A has an oxidation number of +4 , the oxidation number of oxygen in $\mathrm{SiO}_{2}$ must be -2 . Thus, $\mathrm{SiO}_{2}$ is an oxide.


What is the oxidation number of oxygen in each of the following compounds? Tell whether the compound is an oxide, a peroxide, or a superoxide.
(a) $\mathrm{Rb}_{2} \mathrm{O}_{2}$
(b) CaO
(c) $\mathrm{CsO}_{2}$
(d) $\mathrm{SrO}_{2}$
(e) $\mathrm{CO}_{2}$

PROBLEM 14.12 Write a balanced net ionic equation for the reaction of water with each of the oxygen compounds listed in Problem 14.11.

- KEY CONCEPT PROBLEM 14.13 Draw a molecular orbital (MO) energy-level diagram for $\mathrm{O}_{2}{ }^{-}$, including the MOs derived from the oxygen $2 s$ and $2 p$ orbitals. Show the electron population of the MOs, and verify that $\mathrm{O}_{2}{ }^{-}$is paramagnetic and has a bond order of 1.5.


### 14.11 Hydrogen Peroxide

Hydrogen peroxide $(\mathrm{HOOH})$ is sold in drugstores as a $3 \%$ aqueous solution for domestic use and is marketed as a $30 \%$ aqueous solution for industrial and laboratory use. Because of its oxidizing properties, hydrogen peroxide is used as a mild antiseptic and as a bleach for textiles, paper pulp, and hair. In the chemical industry, hydrogen peroxide is a starting material for the synthesis of other peroxide compounds, some of which are used in the manufacture of plastics.

Pure hydrogen peroxide is an almost colorless, syrupy liquid that freezes at $-0.4^{\circ} \mathrm{C}$ and boils at an estimated $150^{\circ} \mathrm{C}$. The exact boiling point is not known with certainty, however, because pure $\mathrm{H}_{2} \mathrm{O}_{2}$ explodes when heated. The relatively high estimated boiling point indicates strong hydrogen bonding between $\mathrm{H}_{2} \mathrm{O}_{2}$ molecules in the liquid (Section 10.2). In aqueous solutions, hydrogen peroxide behaves as a weak acid, partially dissociating to give $\mathrm{H}^{+}$and $\mathrm{HO}_{2}^{-}$ions.

Hydrogen peroxide is both a strong oxidizing agent and a reducing agent. When hydrogen peroxide acts as an oxidizing agent, oxygen is reduced from the -1 oxidation state in $\mathrm{H}_{2} \mathrm{O}_{2}$ to the -2 oxidation state in $\mathrm{H}_{2} \mathrm{O}\left(\right.$ or $\left.\mathrm{OH}^{-}\right)$. For example, hydrogen peroxide oxidizes $\mathrm{Br}^{-}$to $\mathrm{Br}_{2}$ in acidic solution:

## Oxidation numbers

$$
\underset{\uparrow}{\mathrm{H}_{2} \mathrm{O}_{2}(a q)}+2 \mathrm{H}^{+}(a q)+\underset{\uparrow}{-1} \underset{-1}{\mathrm{Br}^{-}(a q)} \longrightarrow \underset{\uparrow}{2 \mathrm{H}_{2} \mathrm{O}}(l)+\underset{\uparrow}{\mathrm{Br}_{2}}(a q)
$$

VBecause the oxygen atom in a peroxide is in an oxidation state ( -1 ) intermediate between two more stable oxidation states ( 0 and -2 ), hydrogen peroxide can be either an oxidizing agent or a reducing agent.

FIGURE 14.8 Some reactions of hydrogen peroxide. (a) Addition of a colorless aqueous solution of $\mathrm{H}_{2} \mathrm{O}_{2}$ to a colorless acidic solution of NaBr produces a yelloworange color because of the formation of bromine, $\mathrm{Br}_{2}$. (b) Addition of aqueous $\mathrm{H}_{2} \mathrm{O}_{2}$ to a violet acidic solution of $\mathrm{KMnO}_{4}$ produces (c) bubbles of $\mathrm{O}_{2}$ gas and decolorizes the solution as the violet $\mathrm{MnO}_{4}{ }^{-}$ ion is converted to the nearly colorless $\mathrm{Mn}^{2+}$ ion.

When hydrogen peroxide acts as a reducing agent, oxygen is oxidized from the -1 oxidation state in $\mathrm{H}_{2} \mathrm{O}_{2}$ to the 0 oxidation state in $\mathrm{O}_{2}$. A typical example is the reaction of hydrogen peroxide with permanganate ion in acidic solution:

$$
\begin{array}{ccc}
5 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \\
-1 & \underset{\uparrow}{\mathrm{MnO}_{4}-(a q)}+6 \mathrm{H}^{+}(a q) & \underset{\uparrow}{-1} \underset{\mathrm{H}_{2}}{5}(g)+\underset{\uparrow}{2 \mathrm{Mn}^{2+}(a q)}+8 \mathrm{H}_{2} \mathrm{O}(l) \\
+7 & 0 & +2
\end{array}
$$

The reduction of manganese in this reaction from the +7 oxidation state in $\mathrm{MnO}_{4}^{-}$ to the +2 oxidation state in the manganese(II) ion, $\mathrm{Mn}^{2+}$, is accompanied by a beautiful color change (Figure 14.8).


Because it is both an oxidizing agent and a reducing agent, $\mathrm{H}_{2} \mathrm{O}_{2}$ can oxidize and reduce itself. Thus, hydrogen peroxide is unstable and undergoes disproportionation to water and oxygen:


In the absence of a catalyst, the disproportionation is too slow to be observed at room temperature. Rapid, exothermic, and potentially explosive decomposition of hydrogen peroxide is initiated, however, by heat and by a broad range of catalysts, including transition metal ions, certain anions (such as $\mathrm{I}^{-}$), metal surfaces, blood (Figure 14.9), and even tiny particles of dust. Because decomposition is accelerated by light, hydrogen peroxide is stored in dark bottles. It is best handled in dilute aqueous solutions; concentrated solutions and the pure liquid are extremely hazardous materials.

FIGURE 14.9 When a few drops of blood are added to aqueous hydrogen peroxide (left), the hydrogen peroxide decomposes rapidly, evolving bubbles of oxygen that produce a thick foam (right). The reaction is catalyzed by catalase, an enzyme present in blood.


- PROBLEM 14.14 Draw an electron-dot structure for $\mathrm{H}_{2} \mathrm{O}_{2}$. Is your structure consistent with its O-O bond length of 148 pm ? (Look at Table 14.2 to see how bond length and bond order are related.)
- PROBLEM 14.15 The discoloration and restoration of old oil paintings involves some interesting chemistry. On exposure to polluted air containing $\mathrm{H}_{2} \mathrm{~S}$, white lead carbonate pigments are converted to PbS , a black solid. Hydrogen peroxide has been used to restore the original white color. Write a balanced equation for the reaction, which involves oxidation of black PbS to white $\mathrm{PbSO}_{4}$.


## $14.12 \mid$ Ozone

Oxygen exists in two allotropes (Section 10.10): ordinary dioxygen $\left(\mathrm{O}_{2}\right)$ and ozone $\left(\mathrm{O}_{3}\right)$. Ozone is a toxic, pale blue gas with a characteristic sharp, penetrating odor that you can detect at concentrations as low as 0.01 ppm . You've probably noticed the odor of ozone around photocopy machines or after a severe electrical storm. Ozone is produced when an electric discharge passes through $\mathrm{O}_{2}$, providing the energy needed to bring about the following endothermic reaction:

$$
3 \mathrm{O}_{2}(g) \xrightarrow[\text { discharge }]{\text { Electric }} 2 \mathrm{O}_{3}(g) \quad \Delta H^{\circ}=+285 \mathrm{~kJ}
$$

Although ozone can be prepared in the laboratory by passing $\mathrm{O}_{2}$ through an electrical device like that shown in Figure 14.10, it is unstable and decomposes exothermically to $\mathrm{O}_{2}$. Decomposition of the dilute gas is slow, but the concentrated gas, liquid ozone ( $\mathrm{bp}-112^{\circ} \mathrm{C}$ ), or solid ozone $\left(\mathrm{mp}-192^{\circ} \mathrm{C}\right.$ ) can decompose explosively.


As discussed in Section 7.7, two resonance structures are required to explain the structure of ozone because the two $\mathrm{O}-\mathrm{O}$ bonds have equal lengths:

FIGURE 14.10 Generator for preparing ozone. A stream of $\mathrm{O}_{2}$ gas flows through the ozonizer tube and is partially converted to $\mathrm{O}_{3}$ when an electric discharge passes through the gas.

## re



The bent structure is in accord with the VSEPR model described in Section 7.9, which predicts a bond angle near $120^{\circ}$ for a triatomic molecule having a central atom surrounded by three charge clouds. The $\pi$ electrons are shared by the three oxygen atoms, giving a net bond order of 1.5 between each pair of oxygen atoms ( $1 \sigma$ bond $+0.5 \pi$ bond) This bonding description is in agreement with the $\mathrm{O}-\mathrm{O}$ bond length of 128 pm , intermediate between the lengths of an $\mathrm{O}-\mathrm{O}$ single bond (148 pm) and an $\mathrm{O}=\mathrm{O}$ double bond ( 121 pm ).


A Addition of aqueous iodine to a starch solution gives the blue starch-iodine complex. The complex forms when $\mathrm{I}^{-}$is oxidized to $\mathrm{I}_{2}$ in the presence of starch. What is the brown color?


Ozone is an extremely powerful oxidizing agent. In fact, of the common oxidizing agents, only $\mathrm{F}_{2}$ is more potent. A standard method for detecting ozone in polluted air is to pass the air through a basic solution of potassium iodide that contains a starch indicator. The ozone oxidizes iodide ion to iodine, $\mathrm{I}_{2}$, which combines with the starch to give the deep blue starch-iodine complex:


Because of its oxidizing properties, ozone is sometimes used to kill bacteria in drinking water.

### 14.13 Water

Water, the most important compound of hydrogen and oxygen, is the most familiar and abundant compound on earth. Nearly three-fourths of the earth's surface is covered with water, and an estimated $1.35 \times 10^{18} \mathrm{~m}^{3}$ of water is present in the oceans. (It's interesting to note that the volume of the oceans in milliliters [1.35 $\times 10^{24} \mathrm{~mL}$ ] is roughly twice Avogadro's number.) Water accounts for nearly two-thirds of the mass of the adult human body and $93 \%$ of the mass of the human embryo in the first month.

Approximately $97.3 \%$ of the world's vast supply of water is in the oceans. Most of the rest is in the form of polar ice caps and glaciers ( $2.0 \%$ ) and underground fresh water $(0.6 \%)$. Freshwater lakes and rivers account for less than $0.01 \%$ of the total, yet they nevertheless contain an enormous amount of water $\left(1.26 \times 10^{14} \mathrm{~m}^{3}\right)$.

Seawater is unfit for drinking or agriculture because each kilogram contains about 35 g of dissolved salts. The most abundant salt in seawater is sodium chloride, but more than 60 different elements are present in small amounts. Table 14.3 lists the ions that account for more than $99 \%$ of the mass of the dissolved salts. Although the oceans represent an almost unlimited source of chemicals, ion concentrations are so low that recovery costs are high. Only three substances are obtained from seawater commercially: sodium chloride, magnesium, and bromine.

Water for use in homes, agriculture, and industry is generally obtained from freshwater lakes, rivers, or underground sources. The water you drink must be purified to remove solid particles, colloidal material, bacteria, and other harmful impurities. Important steps in a typical purification process include preliminary filtration, sedimentation, sand filtration, aeration, and sterilization (Figure 14.11).


A FIGURE 14.11 Purification of drinking water.

The sedimentation, or settling, of suspended matter takes place in large tanks and is accelerated by the addition of lime, CaO , and aluminum sulfate, $\mathrm{Al}_{2}\left(\mathrm{SO}_{4}\right)_{3}$. The lime makes the water slightly basic, which precipitates the added $\mathrm{Al}^{3+}$ ions as aluminum hydroxide:

$$
\begin{aligned}
& \mathrm{CaO}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Ca}^{2+}(a q)+2 \mathrm{OH}^{-}(a q) \\
& \mathrm{Al}^{3+}(a q)+3 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{Al}(\mathrm{OH})_{3}(s)
\end{aligned}
$$

As the gelatinous precipitate of aluminum hydroxide slowly settles, it carries with it suspended solids, colloidal material, and most of the bacteria. The water is then filtered through a bed of sand and subsequently sprayed into the air to oxidize dissolved organic impurities. Finally, the water is sterilized by adding chlorine or ozone, which kills the remaining bacteria. The water still contains up to $0.5 \mathrm{~g} / \mathrm{L}$ of inorganic ions such as $\mathrm{Na}^{+}, \mathrm{K}^{+}, \mathrm{Mg}^{2+}, \mathrm{Ca}^{2+}, \mathrm{Cl}^{-}, \mathrm{F}^{-}, \mathrm{SO}_{4}{ }^{2-}$, and $\mathrm{HCO}_{3}{ }^{-}$, but in such low concentrations that they aren't harmful.

Water that contains appreciable concentrations of doubly charged cations such as $\mathrm{Ca}^{2+}, \mathrm{Mg}^{2+}$, and $\mathrm{Fe}^{2+}$ is called hard water. These cations combine with longchain organic anions in soaps to give the undesirable, insoluble precipitates (soap scum) often observed in sinks and bathtubs. They also form the unwanted metal carbonate precipitates, known as boiler scale, that deposit in boilers, hot water heaters, and teakettles, thus reducing the efficiency of heat transfer. You can understand the formation of boiler scale in terms of Le Châtelier's principle (Section 13.6). When hard water containing $\mathrm{HCO}_{3}{ }^{-}$anions is heated, the equilibrium for the decomposition of $\mathrm{HCO}_{3}{ }^{-}$to $\mathrm{CO}_{2}$ and $\mathrm{CO}_{3}{ }^{2-}$ shifts to the right as $\mathrm{CO}_{2}$ gas escapes from the solution. The resulting $\mathrm{CO}_{3}{ }^{2-}$ ions then combine with cations, such as $\mathrm{Ca}^{2+}$, to form insoluble metal carbonates.

$$
\begin{aligned}
& 2 \mathrm{HCO}_{3}^{-}(a q) \stackrel{\text { Heat }}{\rightleftharpoons} \mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CO}_{3}^{2-}(a q) \\
& \mathrm{Ca}^{2+}(a q)+\mathrm{CO}_{3}^{2-}(a q) \longrightarrow \mathrm{CaCO}_{3}(s)
\end{aligned}
$$

Hard water can be softened by ion exchange, a process in which the $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$ ions are replaced by $\mathrm{Na}^{+}$. The exchange occurs when hard water is passed through a resin that has ionic $\mathrm{SO}_{3}{ }^{-} \mathrm{Na}^{+}$groups attached to it. The more highly charged $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$ cations bond to the negative $\mathrm{SO}_{3}{ }^{-}$groups more strongly than $\mathrm{Na}^{+}$, and so the $\mathrm{Na}^{+}$ions are replaced as the hard water passes through the resin. The ion-exchange process can be represented by the following equation, where $\mathrm{RSO}_{3}{ }^{-}$represents the ionic groups on the resin:

$$
2 \mathrm{RSO}_{3}^{-} \mathrm{Na}^{+}(s)+\mathrm{Ca}^{2+}(a q) \longrightarrow\left(\mathrm{RSO}_{3}^{-}\right)_{2} \mathrm{Ca}^{2+}(s)+2 \mathrm{Na}^{+}(a q)
$$

Ion-exchange resins make convenient household water softeners because the $\mathrm{Na}^{+}$ ion form of the resin is easily regenerated by treating it with a concentrated solution of NaCl . For use by persons who must restrict their sodium intake, the resin can be regenerated with a concentrated solution of KCl .

### 14.14 Reactivity of Water

Water reacts with the alkali metals, the heavier alkaline earth metals ( $\mathrm{Ca}, \mathrm{Sr}, \mathrm{Ba}$, and Ra ), and the halogens. With most other elements, water is unreactive at room temperature. Water is reduced to hydrogen by the alkali and alkaline earth metals, which are oxidized to aqueous metal hydroxides:

Oxidation numbers


A Boiler scale, consisting of insoluble metal carbonates, such as $\mathrm{CaCO}_{3}$ and $\mathrm{MgCO}_{3}$, forms when hard water is heated.


A common household accident occurs when chlorine bleach is mixed with a second cleaning agent containing acid. The added $\mathrm{H}^{+}$shifts this equilibrium to the left and liberates toxic chlorine gas.

$\nabla$Notice that many hydrates form when the metal cation is very small relative to the anion. Compared with the bare cation, the hydrated cation is larger, packs better with the anion, and forms a more stable crystalline solid.


FIGURE 14.12 Octahedral structure of the $\mathrm{Mg}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}$ cation. (a) A regular octahedron is a polyhedron that has eight equilateral triangular faces and six vertices. (b) Octahedral structure of the hydrated metal cation in $\left[\mathrm{Mg}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]\left(\mathrm{ClO}_{4}\right)_{2}$. The six $\mathrm{Mg}-\mathrm{O}$ bonds point toward the six vertices of a regular octahedron. (c) A view of the $\mathrm{Mg}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}$ cation showing only the location of the atoms and the octahedral arrangement of the bonds to the six $\mathrm{H}_{2} \mathrm{O}$ molecules.


(b)

(c)

When hydrates are heated, the water is driven off. If you heat blue crystals of $\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ above $350^{\circ} \mathrm{C}$, for example, you'll observe formation of anhydrous copper sulfate, $\mathrm{CuSO}_{4}$, a white compound (Figure 14.13).

Some anhydrous compounds are so prone to forming hydrates that they absorb water from the atmosphere. Anhydrous $\mathrm{Mg}\left(\mathrm{ClO}_{4}\right)_{2}$, for example, picks up water from air, yielding $\mathrm{Mg}\left(\mathrm{ClO}_{4}\right)_{2} \cdot 6 \mathrm{H}_{2} \mathrm{O}$. Compounds that absorb water from the air are said to be hygroscopic and are often useful as drying agents.

## Worked Example 14.6

When 1.823 g of the hydrate $\mathrm{CaCrO}_{4} \cdot x \mathrm{H}_{2} \mathrm{O}$ was heated at $200^{\circ} \mathrm{C}, 1.479 \mathrm{~g}$ of anhydrous $\mathrm{CaCrO}_{4}$ was obtained. What is the formula of the hydrate?

## Strategy

The value of $x$ in the formula of the hydrate is the number of moles of $\mathrm{H}_{2} \mathrm{O}$ per mole of $\mathrm{CaCrO}_{4}$, so we need to use the masses and the molar masses of $\mathrm{H}_{2} \mathrm{O}(18.02 \mathrm{~g} / \mathrm{mol})$ and $\mathrm{CaCrO}_{4}(156.1 \mathrm{~g} / \mathrm{mol})$ to calculate their mole ratio.

## Solution

Grams of $\mathrm{H}_{2} \mathrm{O}=1.823 \mathrm{~g}-1.479 \mathrm{~g}=0.344 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}$
Moles of $\mathrm{H}_{2} \mathrm{O}=0.344 \mathrm{~g} \mathrm{H}_{2} \mathrm{O} \times \frac{1 \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}}{18.02 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}}=1.91 \times 10^{-2} \mathrm{~mol} \mathrm{H}_{2} \mathrm{O}$
Moles of $\mathrm{CaCrO}_{4}=1.479 \mathrm{~g} \mathrm{CaCrO}_{4} \times \frac{1 \mathrm{~mol} \mathrm{CaCrO}_{4}}{156.1 \mathrm{~g} \mathrm{CaCrO}_{4}}=9.475 \times 10^{-3} \mathrm{~mol} \mathrm{CaCrO}_{4}$
$x=\frac{\text { Moles of } \mathrm{H}_{2} \mathrm{O}}{\text { Moles of } \mathrm{CaCrO}_{4}}=\frac{1.91 \times 10^{-2} \mathrm{~mol}}{9.475 \times 10^{-3} \mathrm{~mol}}=2.02$
Since $x=2$ within experimental uncertainty, the formula of the hydrate is $\mathrm{CaCrO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}$.
$\checkmark$ BALLPARK Check If the hydrate contained 1 mol of $\mathrm{H}_{2} \mathrm{O}$ per mole of $\mathrm{CaCrO}_{4}$, the mass ratio of $\mathrm{H}_{2} \mathrm{O}$ to $\mathrm{CaCrO}_{4}$ would be $18 \mathrm{~g} / \mathrm{mol}$ divided by $156 \mathrm{~g} / \mathrm{mol}$, or about 0.1. The actual mass ratio of $\mathrm{H}_{2} \mathrm{O}$ to $\mathrm{CaCrO}_{4}$ in the hydrate is approximately (1.8-1.5) $\mathrm{g} / 1.5 \mathrm{~g}=0.2$, so the hydrate must contain 2 mol of $\mathrm{H}_{2} \mathrm{O}$ per mole of $\mathrm{CaCrO}_{4}$. The ballpark check agrees with the solution.

PROBLEM 14.17 A 3.10 g sample of anhydrous $\mathrm{NiSO}_{4}$ was exposed to moist air. If 5.62 g of a hydrate of nickel sulfate was obtained, what is the formula of the hydrate?


A FIGURE 14.13 Blue crystals of $\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ are converted to white anhydrous $\mathrm{CuSO}_{4}$ when the sample is heated with a Bunsen flame.

## Interlude A "Hydrogen Economy"



Hydrogen is an enormously attractive fuel because it's environmentally clean, giving only water as a combustion product. If hydrogen is burned in air, small amounts of nitrogen oxides can be produced because of the high-temperature combination of nitrogen and oxygen, but the combustion products are free of $\mathrm{CO}, \mathrm{CO}_{2}, \mathrm{SO}_{2}$, unburned hydrocarbons, and other environmental pollutants that result from the combustion of petroleum fuels. In addition, the amount of heat liberated when hydrogen burns is $242 \mathrm{~kJ} / \mathrm{mol}(121 \mathrm{~kJ} / \mathrm{g})$, more than twice that of gasoline, oil, or natural gas on a mass basis.

$$
\mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \longrightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{~g}) \quad \Delta H^{\circ}=-242 \mathrm{~kJ}
$$

As a result, some people envision what they call a "hydrogen economy" in which our energy needs are met by gaseous, liquid, and solid hydrogen. For heating homes, gaseous hydrogen could be conveyed through underground pipes, while liquid hydrogen could be shipped by truck or by rail in large vacuum-insulated tanks. Automobiles might be powered by compressed hydrogen gas, liquid hydrogen, or "solid hydrogen" in the form of solid interstitial hydrides or hydrogen stored in the recently discovered tube-shaped molecules called carbon nanotubes. Prototype cars have already been built with their engines modified to run on hydrogen. Current work centers on development of electric vehicles powered by fuel cells, a type of battery that uses hydrogen as an energy source. (Fuel cells are discussed in Section 18.9.)

What is keeping us from reaching a hydrogen economy? Before a hydrogen economy can become a reality, cheaper ways of producing hydrogen must be found. Since hydrogen is not a naturally occurring energy source like coal, oil, or natural gas, energy must first be expended to produce the hydrogen before it can be used. Current research therefore focuses on finding cheaper methods for extracting hydrogen from its compounds.

At present, hydrogen is produced mainly by the steam-hydrocarbon reforming process (Section 14.3). This method can contribute to global warming because it produces $\mathrm{CO}_{2}$ as a by-product. It may be possible, however, to capture the $\mathrm{CO}_{2}$ and sequester it in depleted gas wells or deep saline aquifers, thus avoiding addition of $\mathrm{CO}_{2}$ to the atmosphere.

Where inexpensive electric power is available, for example off-peak hydropower or nuclear power, hydrogen can be produced by electrolysis of water. Another approach is to use solar energy to "split" water into $\mathrm{H}_{2}$ and $\mathrm{O}_{2}$. The feasibility of this scheme depends on the development of catalysts that absorb sunlight and then use the energy to reduce water to hydrogen.

Liquid hydrogen has been used as a fuel in the U.S. space program for many years. Hydrogen powered the Saturn $V$ rocket that carried the first astronauts to the moon, and it fuels the rocket engines of the space shuttle (Figure 14.14a).

$\triangle$ FIGURE 14.14 (a) The space shuttle, consisting of the orbiter, two solid-fuel rocket boosters, and the huge external fuel tank. The fuel tank, which is 47.0 m high and 8.4 m in diameter, contains $1.45 \times 10^{6} \mathrm{~L}$ of liquid hydrogen and $5.41 \times 10^{5} \mathrm{~L}$ of liquid oxygen at liftoff. (b) Breakup of the Challenger space shuttle. The rocket boosters are at the top of the photo, and the orbiter is at the bottom left, with its rocket engines still firing. Wreckage of the external fuel tank is obscured by vapor and smoke.

Although liquid hydrogen has been handled safely for many years, it is an extremely dangerous substance. The disastrous breakup of the Challenger space shuttle (Figure 14.14b), which took the lives of seven astronauts in 1986, resulted from a leak in the O-ring of the solid-fuel rocket boosters and subsequent explosive burning of massive amounts of hydrogen. Before liquid hydrogen can come into more general use as a fuel, the hazards of storing and distributing this flammable and explosive material must be solved.

- PROBLEM 14.18 Hydrogen is a gas at ordinary temperatures. Explain how it can be stored as a solid.
- PROBLEM 14.19 The space shuttle fuel tank contains $1.45 \times 10^{6} \mathrm{~L}$ of liquid hydrogen, which has a density of $0.088 \mathrm{~g} / \mathrm{L}$. How much heat (in kilojoules) is liberated when the hydrogen burns in an excess of oxygen? How many kilograms of oxygen are needed to oxidize the hydrogen?


## Summary

Hydrogen, the most abundant element in the universe, has three isotopes: protium $\left({ }_{1}^{1} \mathrm{H}\right)$, deuterium $\left({ }_{1}^{2} \mathrm{H}\right)$, and tritium $\left({ }_{1}^{3} \mathrm{H}\right)$. The isotopes of hydrogen exhibit small differences in properties, known as isotope effects. A hydrogen atom, which has the electron configuration $1 s^{1}$, can lose its electron, forming a hydrogen cation $\left(\mathrm{H}^{+}\right)$, or it can gain an electron, yielding a hydride anion $\left(\mathrm{H}^{-}\right)$. At ordinary temperatures, hydrogen exists as diatomic $\mathrm{H}_{2}$ molecules, which are thermally stable and unreactive because of the strong $\mathrm{H}-\mathrm{H}$ bond.

Hydrogen for industrial purposes is produced by the steam-hydrocarbon re-forming process and is used in the synthesis of ammonia and methanol. In the laboratory, hydrogen is prepared by reaction of dilute acid with an active metal, such as zinc.

Hydrogen forms three types of binary hydrides. Active metals give ionic hydrides, such as LiH and $\mathrm{CaH}_{2}$; nonmetals give covalent hydrides, such as $\mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{O}$, and HF; and transition metals give metallic, or interstitial, hydrides, such as $\mathrm{PdH}_{x}$. Interstitial hydrides are often nonstoichiometric compounds.

Oxygen is the most abundant element in the earth's crust. Dioxygen $\left(\mathrm{O}_{2}\right)$ can be prepared in the laboratory by electrolysis of water, by catalytic decomposition of hydrogen peroxide, or by thermal decomposition of $\mathrm{KClO}_{3}$. Oxygen is manufactured by fractional distillation of liquefied air and is used in making steel. The $\mathrm{O}_{2}$ molecule is paramagnetic and has an
$\mathrm{O}=\mathrm{O}$ double bond. Ozone $\left(\mathrm{O}_{3}\right)$, an allotrope of oxygen, is a powerful oxidizing agent.

Oxygen forms ionic oxides, such as $\mathrm{Li}_{2} \mathrm{O}$ and MgO , with active metals, and covalent oxides, such as $\mathrm{P}_{4} \mathrm{O}_{10}$ and $\mathrm{SO}_{3}$, with nonmetals. Oxides can also be classified according to their acid-base properties. Basic oxides are ionic, and acidic oxides are covalent. Amphoteric oxides, such as $\mathrm{Al}_{2} \mathrm{O}_{3}$, exhibit both acidic and basic properties.

Metal peroxides, such as $\mathrm{Na}_{2} \mathrm{O}_{2}$, are ionic compounds that contain the $\mathrm{O}_{2}{ }^{2-}$ anion and have oxygen in the -1 oxidation state. Metal superoxides, such as $\mathrm{KO}_{2}$, contain the $\mathrm{O}_{2}{ }^{-}$ anion and have oxygen in the $-1 / 2$ oxidation state. Hydrogen peroxide $\left(\mathrm{H}_{2} \mathrm{O}_{2}\right)$, a strong oxidizing agent and also a reducing agent, is unstable with respect to disproportionation to $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{O}_{2}$. A disproportionation reaction is one in which a substance is simultaneously oxidized and reduced.

Water is the most abundant compound on earth. Seawater, which accounts for $97.3 \%$ of the world's water supply, contains 3.5 mass \% of dissolved salts. Purification of drinking water involves preliminary filtration, sedimentation, sand filtration, aeration, and sterilization. Hard water, which contains appreciable concentrations of doubly charged cations such as $\mathrm{Ca}^{2+}, \mathrm{Mg}^{2+}$, and $\mathrm{Fe}^{2+}$, can be softened by ion exchange. Water is reduced to $\mathrm{H}_{2}$ by the alkali metals and heavier alkaline earth metals, and is oxidized to $\mathrm{O}_{2}$ by fluorine. Solid compounds that contain water are known as hydrates.

## Key Words

amphoteric 589
binary hydride 580
covalent hydride 581
disproportionation 592
hard water 597
hydrate 598
hygroscopic 599 interstitial hydride 582 ion exchange 597 ionic hydride 580 isotope effect 577
metallic hydride 581
nonstoichiometric compound 582
oxide 588
peroxide 588
steam-hydrocarbon reforming process 579 superoxide 588 water-gas shift reaction 579


## Understanding Key Concepts

Problems 14.1-14.19 appear within the chapter.
14.20 In the following pictures of binary hydrides, ivory
\%/e spheres represent H atoms or ions, and burgundy spheres represent atoms or ions of the other element.

(a) Identify each binary hydride as ionic, covalent, or interstitial.
(b) What is the oxidation state of hydrogen in compounds (1), (2), and (3)? What is the oxidation state of the other element?
14.21 Look at the location of elements A, B, C, and D in the following periodic table:

(a) Write the formula of the simplest binary hydride of each element.
(b) Classify each binary hydride as ionic, covalent, or interstitial.
(c) Which of these hydrides are molecular? Which are solids with an infinitely extended three-dimensional crystal structure?
(d) What are the oxidation states of hydrogen and the other element in the hydrides of $\mathrm{A}, \mathrm{C}$, and D ?
14.22 The following molecular orbital energy-level diagram shows the energies and electron occupancies of the MOs derived from the atomic $2 p$ orbitals for an oxygencontaining binary compound of potassium.

(a) Is the compound a peroxide or a superoxide? Write its chemical formula.
(b) Is the compound attracted or repelled by magnetic fields?
(c) Compare the oxygen-oxygen bond energy and bond length in this compound with the corresponding properties in the $\mathrm{O}_{2}$ molecule.
(d) When this compound is treated with water, is the resulting aqueous solution acidic or basic? Explain.
14.23 In the following pictures of oxides, red spheres represent $O$ atoms or ions, and green spheres represent atoms or ions of a second- or third-row element in its highest oxidation state.

(a) What is the oxidation state of oxygen in each oxide? What is the oxidation state of the other element?
(b) Identify each oxide as ionic or covalent.
(c) Identify each oxide as acidic or basic.
(d) What is the identity of the other element in (1) and (2)?
14.24 In the following pictures of oxides, red spheres represent $O$ atoms or ions, and green spheres represent atoms or ions of a first- or second-row element in its highest oxidation state.

(1)

(2)

(3)
(a) What is the oxidation state of oxygen in each oxide? What is the oxidation state of the other element?
(b) Which of these oxides is (are) molecular, and which has (have) an infinitely extended three-dimensional structure?
(c) Which of these oxides is (are) likely to be a gas or a liquid, and which is (are) likely to be a high-melting solid?
(d) Identify the other element in (2) and (3).
14.25 Look at the location of elements A, B, C, and D in the following periodic table:

(a) Write the formula of the oxide that has each of these elements in its highest oxidation state.
(b) Classify each oxide as basic, acidic, or amphoteric.
(c) Which oxide is the most ionic? Which is the most covalent?
(d) Which of these oxides are molecular? Which are solids with an infinitely extended three-dimensional crystal structure?
(e) Which of these oxides has the highest melting point? Which has the lowest melting point?
14.26 The following pictures represent structures of the hydrides of four second-row elements.

(a) Which compound has the highest melting point?
(b) Which compound has the lowest boiling point?
(c) Which compounds yield $\mathrm{H}_{2}$ gas when they are mixed together?
14.27 The following pictures represent the structures of oxides of carbon and sulfur. Which has the stronger bonds? Explain.

(1)

(2)

## Additional Problems

## Chemistry of Hydrogen

14.28 Explain what is meant by an isotope effect, and give two examples.
14.29 How can protium and deuterium be separated?
14.30 Calculate the percentage mass difference between:
(a) ${ }^{1} \mathrm{H}$ and ${ }^{2} \mathrm{H}$
(b) ${ }^{2} \mathrm{H}$ and ${ }^{3} \mathrm{H}$

Would you expect the differences in properties for $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{D}_{2} \mathrm{O}$ to be larger or smaller than the differences in properties for $\mathrm{D}_{2} \mathrm{O}$ and $\mathrm{T}_{2} \mathrm{O}$ ? Do the data in Table 14.1 support your prediction?
14.31 (a) If the volume of the oceans is $1.35 \times 10^{18} \mathrm{~m}^{3}$ and the abundance of deuterium is 0.0156 atom $\%$, how many kilograms of deuterium are present in the oceans? (Neglect the presence of dissolved substances, and assume that the density of water is $1.00 \mathrm{~g} / \mathrm{cm}^{3}$.)
(b) Do the same calculation for tritium, assuming that the abundance of tritium is approximately $10^{-16}$ atom $\%$.
14.32 There are three isotopes of hydrogen and three naturally occurring isotopes of oxygen ( ${ }^{16} \mathrm{O},{ }^{17} \mathrm{O}$, and ${ }^{18} \mathrm{O}$ ). How many kinds of water are possible? Draw their structures.
14.33 There are three isotopes of hydrogen and just one naturally occurring isotope of phosphorus $\left({ }^{31} \mathrm{P}\right)$. How many kinds of phosphine $\left(\mathrm{PH}_{3}\right)$ are possible? Draw their structures.
14.34 Write a balanced equation for the synthesis of hydrogen using each of the following starting materials.
(a) Zn
(b) C
(c) $\mathrm{CH}_{4}$
(d) $\mathrm{H}_{2} \mathrm{O}$
14.35 Complete and balance the equation for each of the following reactions:
(a) $\mathrm{Fe}(s)+\mathrm{H}^{+}(a q) \rightarrow$
(b) $\mathrm{Ca}(s)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow$
(c) $\mathrm{Al}(s)+\mathrm{H}^{+}(a q) \rightarrow$
(d) $\mathrm{C}_{2} \mathrm{H}_{6}(g)+\mathrm{H}_{2} \mathrm{O}(g) \xrightarrow[\text { Catalyst }]{\text { Heat }}$
14.36 What is the most important method for the industrial production of hydrogen? Write balanced equations for the reactions involved.
14.37 Write a balanced equation for each of the following reactions:
(a) Reduction of steam by hot iron
(b) Production of synthesis gas from propane, $\mathrm{C}_{3} \mathrm{H}_{8}$
(c) The water-gas shift reaction
14.38 Ionic metal hydrides react with water to give hydrogen gas and an aqueous solution of the metal hydroxide.
(a) On reaction of equal masses of LiH and $\mathrm{CaH}_{2}$ with water, which compound gives more hydrogen?
(b) How many kilograms of $\mathrm{CaH}_{2}$ are needed to fill a 100 L tank with compressed $\mathrm{H}_{2}$ gas at 150 atm pressure and $25^{\circ} \mathrm{C}$ ?
14.39 The hydrogen-filled dirigible Hindenburg had a volume of $1.99 \times 10^{8} \mathrm{~L}$. If the hydrogen used was produced by reaction of carbon with steam, how many kilograms of carbon would have been needed to produce enough hydrogen to fill the dirigible at $20^{\circ} \mathrm{C}$ and 740 mm pressure?

$$
\mathrm{C}(s)+\mathrm{H}_{2} \mathrm{O}(g) \longrightarrow \mathrm{CO}(g)+\mathrm{H}_{2}(g)
$$

14.40 In the following compounds, is hydrogen present as $\mathrm{H}^{+}, \mathrm{H}^{-}$, or a covalently bound H atom?
(a) $\mathrm{MgH}_{2}$
(b) $\mathrm{PH}_{3}$
(c) KH
(d) HBr
14.41 In the following compounds, is hydrogen present as $\mathrm{H}^{+}, \mathrm{H}^{-}$, or a covalently bound H atom?
(a) $\mathrm{H}_{2} \mathrm{Se}$
(b) RbH
(c) $\mathrm{CaH}_{2}$
(d) $\mathrm{GeH}_{4}$
14.42 Compare some of the physical properties of $\mathrm{H}_{2} \mathrm{~S}, \mathrm{NaH}$, and $\mathrm{PdH}_{x}$.
14.43 Compare some of the physical properties of $\mathrm{TiH}_{1.7}$, HCl , and $\mathrm{CaH}_{2}$.
14.44 Describe the bonding in:
(a) $\mathrm{CH}_{4}$
(b) NaH
14.45 Describe the bonding in:
(a) $\mathrm{CaH}_{2}$
(b) $\mathrm{NH}_{3}$
14.46 Predict the molecular structure of:
(a) $\mathrm{H}_{2} \mathrm{Se}$
(b) $\mathrm{AsH}_{3}$
(c) $\mathrm{SiH}_{4}$
14.47 Describe the molecular geometry of:
(a) $\mathrm{GeH}_{4}$
(b) $\mathrm{H}_{2} \mathrm{~S}$
(c) $\mathrm{NH}_{3}$
14.48 What is a nonstoichiometric compound? Give an example, and account for its lack of stoichiometry in terms of structure.
14.49 Explain why the hydrogen atoms in interstitial hydrides are mobile.
14.50 Titanium hydride, $\mathrm{TiH}_{2}$, has a density of $3.9 \mathrm{~g} / \mathrm{cm}^{3}$.
(a) Calculate the density of hydrogen in $\mathrm{TiH}_{2}$, and compare it with that in liquid $\mathrm{H}_{2}\left(0.070 \mathrm{~g} / \mathrm{cm}^{3}\right)$.
(b) How many cubic centimeters of $\mathrm{H}_{2}$ at STP are absorbed in making $1.00 \mathrm{~cm}^{3}$ of $\mathrm{TiH}_{2}$ ?
14.51 The density of LiH is $0.82 \mathrm{~g} / \mathrm{cm}^{3}$.
(a) Calculate the density of hydrogen in LiH and the number of H atoms in $5.0 \mathrm{~cm}^{3}$ of LiH .
(b) How many liters of $\mathrm{H}_{2}$ at $20^{\circ} \mathrm{C}$ and 740 mm Hg are required to make $5.0 \mathrm{~cm}^{3}$ of LiH ?

## Chemistry of Oxygen

14.52 How is $\mathrm{O}_{2}$ prepared (a) in industry and (b) in the laboratory? Write balanced equations for the reactions involved.
14.53 In what forms is oxygen commonly found in nature?
14.54 How many liters of $\mathrm{O}_{2}$ gas at $25^{\circ} \mathrm{C}$ and 0.985 atm pressure can be obtained by catalytic decomposition of 20.4 g of hydrogen peroxide?
14.55 In the oxyacetylene torch, how many grams of acetylene and how many liters of $\mathrm{O}_{2}$ at STP are needed to generate 1000 kJ of heat?
14.56 Write a balanced equation for the reaction of an excess of $\mathrm{O}_{2}$ with each of the following elements:
(a) Li
(b) P
(c) Al
(d) Si
14.57 Write a balanced equation for the reaction of an excess of $\mathrm{O}_{2}$ with each of the following elements:
(a) Ca
(b) C
(c) As
(d) B
14.58 Draw some electron-dot structures for $\mathrm{O}_{2}$, and explain why they are inconsistent with the paramagnetism of $\mathrm{O}_{2}$ and its $\mathrm{O}=\mathrm{O}$ double bond.
14.59 Use molecular orbital theory to account for the paramagnetism of $\mathrm{O}_{2}$ and its $\mathrm{O}=\mathrm{O}$ double bond.
14.60 Arrange the following oxides in order of increasing covalent character: $\mathrm{B}_{2} \mathrm{O}_{3}, \mathrm{BeO}, \mathrm{CO}_{2}, \mathrm{Li}_{2} \mathrm{O}, \mathrm{N}_{2} \mathrm{O}_{5}$.
14.61 Arrange the following oxides in order of increasing ionic character: $\mathrm{SiO}_{2}, \mathrm{~K}_{2} \mathrm{O}, \mathrm{P}_{4} \mathrm{O}_{10}, \mathrm{Ga}_{2} \mathrm{O}_{3}, \mathrm{GeO}_{2}$.
14.62 Arrange the following oxides in order of increasing basic character: $\mathrm{Al}_{2} \mathrm{O}_{3}, \mathrm{Cs}_{2} \mathrm{O}, \mathrm{K}_{2} \mathrm{O}, \mathrm{N}_{2} \mathrm{O}_{5}$.
14.63 Arrange the following oxides in order of increasing acidic character: $\mathrm{BaO}, \mathrm{Cl}_{2} \mathrm{O}_{7}, \mathrm{SO}_{3}, \mathrm{SnO}_{2}$.
14.64 Which is more acidic?
(a) $\mathrm{Cr}_{2} \mathrm{O}_{3}$ or $\mathrm{CrO}_{3}$
(b) $\mathrm{N}_{2} \mathrm{O}_{5}$ or $\mathrm{N}_{2} \mathrm{O}_{3}$
(c) $\mathrm{SO}_{2}$ or $\mathrm{SO}_{3}$
14.65 Which is more basic?
(a) CrO or $\mathrm{Cr}_{2} \mathrm{O}_{3}$
(b) $\mathrm{SnO}_{2}$ or SnO
(c) $\mathrm{As}_{2} \mathrm{O}_{3}$ or $\mathrm{As}_{2} \mathrm{O}_{5}$
14.66 Write a balanced net ionic equation for reaction of each of the following oxides with water:
(a) $\mathrm{Cl}_{2} \mathrm{O}_{7}$
(b) $\mathrm{K}_{2} \mathrm{O}$
(c) $\mathrm{SO}_{3}$
14.67 Write a balanced net ionic equation for reaction of each of the following oxides with water:
(a) BaO
(b) $\mathrm{Cs}_{2} \mathrm{O}$
(c) $\mathrm{N}_{2} \mathrm{O}_{5}$
14.68 Write a balanced net ionic equation for reaction of the amphoteric oxide ZnO with:
(a) Hydrochloric acid
(b) Aqueous sodium hydroxide; the product is $\mathrm{Zn}(\mathrm{OH})_{4}{ }^{2-}$
14.69 Write a balanced net ionic equation for reaction of the amphoteric oxide $\mathrm{Ga}_{2} \mathrm{O}_{3}$ with:
(a) Aqueous sulfuric acid
(b) Aqueous potassium hydroxide; the product is $\mathrm{Ga}(\mathrm{OH})_{4}{ }^{-}$
14.70 Distinguish between a peroxide and a superoxide, and give an example of each.
14.71 Classify each of the following compounds as an oxide, a peroxide, or a superoxide:
(a) $\mathrm{Na}_{2} \mathrm{O}_{2}$
(b) $\mathrm{GeO}_{2}$
(c) $\mathrm{RbO}_{2}$
(d) $\mathrm{BaO}_{2}$
14.72 What products are formed when the following metals are burned in an excess of air?
(a) Ba
(b) Ca
(c) Cs
(d) Li
(e) Na
14.73 Write balanced net ionic equations for the reaction of water with:
(a) $\mathrm{BaO}_{2}$
(b) $\mathrm{RbO}_{2}$
14.74 Draw MO energy-level diagrams for $\mathrm{O}_{2}, \mathrm{O}_{2}{ }^{-}$, and $\mathrm{O}_{2}{ }^{2-}$, including only MOs derived from the oxygen $2 p$ atomic orbitals. Show the electron population of the MOs. (See Section 7.14.)
(a) Why does the $\mathrm{O}-\mathrm{O}$ bond length increase in the series $\mathrm{O}_{2}, \mathrm{O}_{2}{ }^{-}, \mathrm{O}_{2}{ }^{2-}$ ?
(b) Why is $\mathrm{O}_{2}{ }^{-}$paramagnetic, whereas $\mathrm{O}_{2}{ }^{2-}$ is diamagnetic?
14.75 Draw an MO energy-level diagram for $\mathrm{O}_{2}{ }^{+}$, including only MOs derived from the oxygen $2 p$ atomic orbitals. Show the electron population of the MOs.
(a) Predict the bond order in $\mathrm{O}_{2}{ }^{+}$, and tell whether the $\mathrm{O}-\mathrm{O}$ bond should be longer or shorter than that in $\mathrm{O}_{2}$.
(b) Is $\mathrm{O}_{2}{ }^{+}$paramagnetic or diamagnetic?
14.76 Write a balanced net ionic equation for each of the following reactions:
(a) Oxidation by $\mathrm{H}_{2} \mathrm{O}_{2}$ of $\mathrm{I}^{-}$to $\mathrm{I}_{2}$ in acidic solution
(b) Reduction by $\mathrm{H}_{2} \mathrm{O}_{2}$ of $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}$ to $\mathrm{Cr}^{3+}$ in acidic solution
14.77 Write a balanced net ionic equation for each of the following reactions:
(a) Oxidation by $\mathrm{H}_{2} \mathrm{O}_{2}$ of $\mathrm{Fe}^{2+}$ to $\mathrm{Fe}^{3+}$ in acidic solution
(b) Reduction by $\mathrm{H}_{2} \mathrm{O}_{2}$ of $\mathrm{IO}_{4}^{-}$to $\mathrm{IO}_{3}^{-}$in basic solution
14.78 Give a description of the electronic structure of ozone that is consistent with the two $\mathrm{O}-\mathrm{O}$ bond lengths being equal.
14.79 What experiment could you perform to distinguish $\mathrm{O}_{3}$ from $\mathrm{O}_{2}$ ?
14.80 How is ozone made in the laboratory?
14.81 How many kilojoules must be supplied to convert 10.0 g of $\mathrm{O}_{2}$ to $\mathrm{O}_{3}$ ?

## Chemistry of Water

14.82 Write a balanced net ionic equation for the reaction of water with each of the following:
(a) $\mathrm{F}_{2}$
(b) $\mathrm{Cl}_{2}$
(c) $\mathrm{I}_{2}$
(d) Ba
14.83 Can water undergo a disproportionation reaction? Explain.
14.84 Give an example of a hydrate, and indicate how the water is bound.
14.85 Describe the structure of the cation in $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]\left(\mathrm{NO}_{3}\right)_{3}$.
14.86 What is the mass percent of water in plaster of paris, $\mathrm{CaSO}_{4} \cdot 1 / 2 \mathrm{H}_{2} \mathrm{O}$ ?
14.87 Calculate the mass percent of water in $\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}$.
14.88 When 3.44 g of the mineral gypsum, $\mathrm{CaSO}_{4} \cdot x \mathrm{H}_{2} \mathrm{O}$, is heated to $128^{\circ} \mathrm{C}, 2.90 \mathrm{~g}$ of $\mathrm{CaSO}_{4} \cdot 1 / 2 \mathrm{H}_{2} \mathrm{O}$ is obtained. What is the value of $x$ in the formula of gypsum?
14.89 Anhydrous, hygroscopic, blue $\mathrm{CoCl}_{2}$ forms red-violet $\mathrm{CoCl}_{2} \cdot x \mathrm{H}_{2} \mathrm{O}$ on exposure to moist air. If the color change is accompanied by an $83.0 \%$ increase in mass, what is the formula of the hydrate?
14.90 If seawater contains 3.5 mass \% of dissolved salts, how many kilograms of salts are present in $1.0 \mathrm{mi}^{3}$ of seawater? ( $1 \mathrm{mi}=1609 \mathrm{~m}$; density of seawater $=$ $1.025 \mathrm{~g} / \mathrm{cm}^{3}$.)
14.91 How many kilograms of magnesium are present in a cubic meter of seawater? Assume the $\mathrm{Mg}^{2+}$ ion concentration listed in Table 14.3 and a density for seawater of $1.025 \mathrm{~g} / \mathrm{cm}^{3}$.

## General Problems

14.92 To prepare $\mathrm{H}_{2}$ from water, would you allow water to react with an oxidizing agent or a reducing agent? Which of the following metals could be used in the reaction? (Hint: Recall the activity series, Section 4.8.)
(a) Ag
(b) Al
(c) Au
(d) Ca
14.93 How many tons of hydrogen are required for the annual U.S. production of ammonia ( 13 million tons)?
14.94 How many liters of $\mathrm{H}_{2}$ at STP are required for the hydrogenation of 2.7 kg of butadiene?


14.95 Give the chemical formula for each of the following compounds:
(a) Calcium hydroxide
(b) Chromium(III) oxide
(c) Rubidium superoxide
(d) Sodium peroxide
(e) Barium hydride
(f) Hydrogen selenide
14.96 Name each of the following compounds:
(a) $\mathrm{B}_{2} \mathrm{O}_{3}$
(b) $\mathrm{H}_{2} \mathrm{O}_{2}$
(c) $\mathrm{SrH}_{2}$
(d) $\mathrm{CsO}_{2}$
(e) $\mathrm{HClO}_{4}$
(f) $\mathrm{BaO}_{2}$
14.97 Which of the following molecules have similar properties, and which have quite different properties?
(a) $\mathrm{H}_{2}{ }^{16} \mathrm{O}$
(b) $\mathrm{D}_{2}{ }^{17} \mathrm{O}$
(c) $\mathrm{H}_{2}{ }^{16} \mathrm{O}_{2}$
(d) $\mathrm{H}_{2}{ }^{17} \mathrm{O}$
(e) $\mathrm{D}_{2}{ }^{17} \mathrm{O}_{2}$

Draw the structure of each molecule.
14.98 Three isotopes of oxygen exist $\left({ }^{16} \mathrm{O},{ }^{17} \mathrm{O}\right.$, and $\left.{ }^{18} \mathrm{O}\right)$.
(a) How many kinds of dioxygen $\left(\mathrm{O}_{2}\right)$ molecules are possible? Draw their structures.
(b) How many kinds of ozone $\left(\mathrm{O}_{3}\right)$ molecules are possible? Draw their structures.
14.99 What is the oxidation number of oxygen in each of the following compounds?
(a) $\mathrm{Al}_{2} \mathrm{O}_{3}$
(b) $\mathrm{SrO}_{2}$
(c) $\mathrm{SnO}_{2}$
(d) $\mathrm{CsO}_{2}$
14.100 Write a balanced equation for a reaction in which each of the following acts as an oxidizing agent:
(a) $\mathrm{O}_{2}$
(b) $\mathrm{O}_{3}$
(c) $\mathrm{H}_{2} \mathrm{O}_{2}$
(d) $\mathrm{H}_{2}$
(e) $\mathrm{H}_{2} \mathrm{O}$
14.101 Write a balanced equation for a reaction in which each of the following acts as a reducing agent:
(a) $\mathrm{H}_{2}$
(b) $\mathrm{H}_{2} \mathrm{O}_{2}$
(c) $\mathrm{H}_{2} \mathrm{O}$
14.102 Which of the following elements are oxidized by water? Which are reduced by water? Which undergo a disproportionation reaction when treated with water?
(a) $\mathrm{Cl}_{2}$
(b) $\mathrm{F}_{2}$
(c) K
(d) $\mathrm{Br}_{2}$
14.103 How many liters of seawater (density $1.025 \mathrm{~g} / \mathrm{cm}^{3}$ ) must be processed to obtain 2.0 million kg of bromine? Assume the $\mathrm{Br}^{-}$ion concentration listed in Table 14.3 and a recovery rate of $20 \%$.
14.104 Use the standard heats of formation in Appendix B to calculate $\Delta H^{\circ}$ (in kilojoules) for each of the following reactions:
(a) $\mathrm{CO}(g)+2 \mathrm{H}_{2}(g) \rightarrow \mathrm{CH}_{3} \mathrm{OH}(l)$
(b) $\mathrm{CO}(g)+\mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{CO}_{2}(g)+\mathrm{H}_{2}(g)$
(c) $2 \mathrm{KClO}_{3}(s) \rightarrow 2 \mathrm{KCl}(s)+3 \mathrm{O}_{2}(g)$
(d) $6 \mathrm{CO}_{2}(g)+6 \mathrm{H}_{2} \mathrm{O}(l) \rightarrow 6 \mathrm{O}_{2}(g)+\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(s)$
14.105 One model of an acid-base reaction involves proton transfer from the acid to a solvent water molecule to give an $\mathrm{H}_{3} \mathrm{O}^{+}$ion. Write balanced chemical equations that show how aqueous solutions of acidic oxides such as $\mathrm{SO}_{2}$ and $\mathrm{SO}_{3}$ can yield $\mathrm{H}_{3} \mathrm{O}^{+}$ions. Which of these two oxides gives a higher concentration of $\mathrm{H}_{3} \mathrm{O}^{+}$ions? Explain.

## Multi-Concept Problems

14.106 How much heat (in joules) is liberated when 1.000 L of ozone at $20^{\circ} \mathrm{C}$ and 63.6 mm Hg decomposes to ordinary oxygen, $\mathrm{O}_{2}$ ?
14.107 Sodium hydride, which has the NaCl crystal structure, has a density of $0.92 \mathrm{~g} / \mathrm{cm}^{3}$. If the ionic radius of $\mathrm{Na}^{+}$ is 102 pm , what is the ionic radius of $\mathrm{H}^{-}$in NaH ?
14.108 A 1.84 g sample of an alkaline earth metal hydride was treated with an excess of dilute hydrochloric acid, and the resulting gas was collected in a 1.000 L container at $20^{\circ} \mathrm{C}$. The measured pressure of the gas was 750.0 mm Hg . Identify the alkaline earth metal, and write the formula for the metal hydride.
14.109 A 250.0 mL gaseous sample of a sulfur oxide at $77^{\circ} \mathrm{C}$ and 720.0 mm Hg pressure was allowed to react completely with an excess of water. Prior to reaction, the density of the gas was determined to be $2.64 \mathrm{~g} / \mathrm{L}$.
(a) What is the formula for the sulfur oxide?
(b) How much heat (in kilojoules) is released when the gas reacts with the water?
(c) How many milliliters of 0.160 M NaOH is needed to neutralize the aqueous solution?
14.110 A 300.0 mL sample of ordinary water was allowed to react with 5.4 g of $\mathrm{N}_{2} \mathrm{O}_{5}$, and an excess of zinc metal was then added. The resulting gas was collected in a 500.0 mL container at $25^{\circ} \mathrm{C}$.
(a) What is the partial pressure (in mm Hg ) of HD in the container?
(b) How many HD molecules are present in the container?
(c) How many $\mathrm{D}_{2}$ molecules are present in the container?
14.111 Sodium amalgam is an alloy of sodium and mercury. The percent sodium in the alloy can be determined by reacting the amalgam with an excess of hydrochloric acid and collecting the liberated $\mathrm{H}_{2}$ gas.
(a) When a 5.26 g sample of amalgam was treated with 250.0 mL of 0.2000 M HCl and the liberated $\mathrm{H}_{2}$ was collected in a 500.0 mL container at $22^{\circ} \mathrm{C}$, the gas had a pressure of 434 mm Hg . What is the mass percent of sodium in the amalgam?
(b) After the reaction in part (a), a 50.00 mL portion of the solution was titrated with 0.1000 M NaOH . How many milliliters of the NaOH solution is needed to neutralize the excess HCl ?
14.112 Direct measurement of the normal boiling point of hydrogen peroxide is dangerous because pure $\mathrm{H}_{2} \mathrm{O}_{2}$ explodes on heating. The boiling point can be estimated, however, from vapor-pressure data. Use the vapor pressures of 75.0 mm Hg at $89.0^{\circ} \mathrm{C}$ and 319.2 mm Hg at $125.0^{\circ} \mathrm{C}$ to estimate the boiling point. Compare your result with the value given in Section 14.11.
14.113 Use the data in this chapter to calculate the number of $\mathrm{Mg}^{2+}$ ions and $\mathrm{Br}^{-}$ions in the earth's oceans. How many tons of $\mathrm{MgBr}_{2}$ could be made from these ions assuming $100 \%$ recovery? (The density of seawater is $1.025 \mathrm{~g} / \mathrm{cm}^{3}$.)

## eMedia Problems

14.114 As shown in the Formation of Water movie (eChapter 14.4), hydrogen and oxygen react explosively to form water. Is the reaction between hydrogen and oxygen an oxidation-reduction reaction? If so, which substance is the reducing agent and which is the oxidizing agent?
14.115 Compare the reaction of white phosphorus and the reaction of sulfur in the Reactions with Oxygen movie (eChapter 14.8). Which of these two reactions do you think has the higher activation energy? For each reaction, sketch an energy profile similar to the one in Figure 12.14 (page 500).
14.116 Watch the Carbon Dioxide Behaves as an Acid in Water movie (eChapter 14.9), and write the equation for the reaction that occurs between carbon dioxide and
water. Carbon dioxide is known as the anhydride of carbonic acid. What is meant by the term anhydride? What are the acid anhydrides of sulfuric and nitric acids?
14.117 The Periodic Trends: Acid-Base Behavior of Oxides movie (eChapter 14.9) shows oxides of strongly metallic elements forming basic solutions with water. Explain how a compound such as $\mathrm{Na}_{2} \mathrm{O}$ can produce a basic solution with water when the compound does not contain the hydroxide ion.
14.118 The reaction between sodium metal and water is shown in the Sodium and Potassium in Water movie (eChapter 14.14). Write and balance the equation for this reaction. Is this an oxidation-reduction reaction? If so, identify the oxidizing and reducing agents.

## Chapter

## Aqueous Equilibria: Acids and Bases

## Acids and bases are among the most familiar of all chemical compounds. Acetic

 acid in vinegar, citric acid in lemons and other citrus fruits, magnesium hydroxide (milk of magnesia) in commercial antacids, and ammonia in household cleaning products are among the acids and bases that we encounter every day. Hydrochloric acid is
## CONTENTS

The sour taste of citrus fruits is due to acids such as citric acid and ascorbic acid (vitamin C).
15.1 Acid-Base Concepts: The Brønsted-Lowry Theory
15.2 Acid Strength and Base Strength
15.3 Hydrated Protons and Hydronium Ions
15.4 Dissociation of Water
15.5 The pH Scale
15.6 Measuring pH
15.7 The pH in Solutions of Strong Acids and Strong Bases
15.8 Equilibria in Solutions of Weak Acids
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15.12 Equilibria in Solutions of Weak Bases
15.13 Relation Between $K_{\mathrm{a}}$ and $K_{\mathrm{b}}$
15.14 Acid-Base Properties of Salts
15.15 Factors That Affect Acid Strength
15.16 Lewis Acids and Bases

- Interlude—Acid Rain

Doris Kolb, "Acids and Bases," J. Chem. Educ., Vol. 55, 1978, 459-464.

aGeorge B. Kauffman, "The Brønsted-Lowry Acid-Base Concept," J. Chem. Educ., Vol. 65, 1988, 28-31

Jamie L. Adcock, "Teaching Brønsted-Lowry Acid-Base Theory in a Direct Comprehensive Way," J. Chem. Educ., Vol. 78, 2001, 1495-1496.
the acid in gastric juice; it is essential to digestion and is secreted by the lining of our stomachs in quantities of 1.2-1.5 L per day.

The characteristic properties of acids and bases have been known for centuries. Acids react with metals such as iron and zinc to yield $\mathrm{H}_{2}$ gas, and they change the color of the plant dye litmus from blue to red. By contrast, bases feel slippery, and they change the color of litmus from red to blue. When acids and bases are mixed in the right proportion, the characteristic acidic and basic properties disappear, and new substances known as salts are obtained.

What is it that makes an acid an acid and a base a base? We first raised those questions in Section 4.5, and we now take a closer look at some of the concepts that chemists have developed to describe the chemical behavior of acids and bases. We'll also apply the principles of chemical equilibrium discussed in Chapter 13 to determine the concentrations of the substances present in aqueous solutions of acids and bases. An enormous amount of chemistry can be understood in terms of acid-base reactions, perhaps the most important reaction type in all of chemistry.

### 15.1 Acid-Base Concepts: The Brønsted-Lowry Theory

Thus far we've been using the Arrhenius theory of acids and bases (Section 4.5). According to Arrhenius, acids are substances that dissociate in water to produce hydrogen ions $\left(\mathrm{H}^{+}\right)$, and bases are substances that dissociate in water to yield hydroxide ions $\left(\mathrm{OH}^{-}\right)$. Thus, HCl and $\mathrm{H}_{2} \mathrm{SO}_{4}$ are acids, and NaOH and $\mathrm{Ba}(\mathrm{OH})_{2}$ are bases.

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- a generalized Arrhenius acid \(\mathrm{HA}(a q) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{A}^{-}(a q)\)
- a generalized Arrhenius base \(\mathrm{MOH}(a q) \rightleftharpoons \mathrm{M}^{+}(a q)+\mathrm{OH}^{-}(a q)\)
```

The Arrhenius theory accounts for the properties of many common acids and bases, but it has important limitations. For one thing, the Arrhenius theory is restricted to aqueous solutions; for another, it doesn't account for the basicity of substances like ammonia $\left(\mathrm{NH}_{3}\right)$ that don't contain OH groups. In 1923, a more general theory of acids and bases was proposed independently by the Danish chemist Johannes Brønsted and the English chemist Thomas Lowry. According to the Bronsted-Lowry theory, an acid is any substance (molecule or ion) that can transfer a proton $\left(\mathrm{H}^{+}\right.$ion) to another substance, and a base is any substance that can accept a proton. In short, acids are proton donors, bases are proton acceptors, and acid-base reactions are proton-transfer reactions:

## - Brønsted-Lowry acid A substance that can transfer $\mathrm{H}^{+}$ <br> - Brønsted-Lowry base A substance that can accept $\mathrm{H}^{+}$



It follows from this equation that the products of a Brønsted-Lowry acid-base reaction, $\mathrm{BH}^{+}$and $\mathrm{A}^{-}$, are themselves acids and bases. The species $\mathrm{BH}^{+}$produced when the base $B$ accepts a proton from HA can itself donate a proton back to $A^{-}$, meaning that it is a Brønsted-Lowry acid. Similarly, the species $A^{-}$produced when HA loses a proton can itself accept a proton back from $\mathrm{BH}^{+}$, meaning that it is a Brønsted-Lowry base. Chemical species whose formulas differ only by one
proton are said to be conjugate acid-base pairs. Thus, $\mathrm{A}^{-}$is the conjugate base of the acid HA, and HA is the conjugate acid of the base $A^{-}$. Similarly, $B$ is the conjugate base of the acid $\mathrm{BH}^{+}$, and $\mathrm{BH}^{+}$is the conjugate acid of the base B .

To see what's going on in an acid-base reaction, keep your eye on the proton. For example, when a Brønsted-Lowry acid HA is placed in water, it reacts reversibly with water in an acid-dissociation equilibrium. The acid transfers a proton to the solvent, which acts as a base (a proton acceptor). The products are the hydronium ion, $\mathrm{H}_{3} \mathrm{O}^{+}$(the conjugate acid of $\mathrm{H}_{2} \mathrm{O}$ ), and $\mathrm{A}^{-}$(the conjugate base of HA):


In the reverse reaction, $\mathrm{H}_{3} \mathrm{O}^{+}$acts as the proton donor (acid) and $\mathrm{A}^{-}$acts as the proton acceptor (base). Typical examples of Brønsted-Lowry acids include not only electrically neutral molecules, such as $\mathrm{HCl}, \mathrm{HNO}_{3}$, and HF , but also cations and anions of salts that contain transferable protons, such as $\mathrm{NH}_{4}{ }^{+}, \mathrm{HSO}_{4}^{-}$, and $\mathrm{HCO}_{3}{ }^{-}$.

When a Brønsted-Lowry base such as $\mathrm{NH}_{3}$ dissolves in water, it accepts a proton from the solvent, which acts as an acid. The products are the hydroxide ion, $\mathrm{OH}^{-}$(the conjugate base of water), and the ammonium ion, $\mathrm{NH}_{4}{ }^{+}$(the conjugate acid of $\mathrm{NH}_{3}$ ). In the reverse reaction, $\mathrm{NH}_{4}{ }^{+}$acts as the proton donor, and $\mathrm{OH}^{-}$ acts as the proton acceptor:


For a molecule or ion to accept a proton, it must have at least one unshared pair of electrons that it can use for bonding to the proton. As shown by the following electron-dot structures, all Brønsted-Lowry bases have one or more lone pairs of electrons:


Some Brønsted-Lowry bases

## Worked Example 15.1

Account for the acidic properties of nitrous acid $\left(\mathrm{HNO}_{2}\right)$ in terms of the Arrhenius theory and the Brønsted-Lowry theory, and identify the conjugate base of $\mathrm{HNO}_{2}$.

## Strategy

To account for the acidity of a substance, consider how it can produce $\mathrm{H}^{+}$ions in water (Arrhenius theory) and how it can act as a proton donor (Brønsted-Lowry theory).

## Solution

$\mathrm{HNO}_{2}$ is an Arrhenius acid because it dissociates in water to produce $\mathrm{H}^{+}$ions:

$$
\mathrm{HNO}_{2}(a q) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{NO}_{2}^{-}(a q)
$$

Nitrous acid is a Brønsted-Lowry acid because it acts as a proton donor when it dissociates, transferring a proton to water to give the hydronium ion:


The conjugate base of $\mathrm{HNO}_{2}$ is $\mathrm{NO}_{2}^{-}$, the species that remains after $\mathrm{HNO}_{2}$ has lost a proton.

PROBLEM 15.1 Write a balanced equation for the dissociation of each of the following Brønsted-Lowry acids in water:
(a) $\mathrm{H}_{2} \mathrm{SO}_{4}$
(b) $\mathrm{HSO}_{4}^{-}$
(c) $\mathrm{H}_{3} \mathrm{O}^{+}$
(d) $\mathrm{NH}_{4}^{+}$

What is the conjugate base of the acid in each case?

- PROBLEM 15.2 What is the conjugate acid of each of the following BrønstedLowry bases?
(a) $\mathrm{HCO}_{3}{ }^{-}$
(b) $\mathrm{CO}_{3}{ }^{2-}$
(c) $\mathrm{OH}^{-}$
(d) $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$


## Worked Key Concept Example 15.2

For the following reaction in aqueous solution, identify the Brønsted-Lowry acids, bases, and conjugate acid-base pairs:


## Strategy

The simplest approach is to identify the conjugate acid-base pairs, the species whose formulas differ by just one proton.

## Solution

The second reactant is HF , and the first product is its conjugate base $\mathrm{F}^{-}$. The second product is $\mathrm{H}_{2} \mathrm{~S}$, and the first reactant is its conjugate base $\mathrm{HS}^{-}$. Therefore, the Brønsted-Lowry acids, bases, and conjugate acid-base pairs are as follows:

-KEY CONCEPT PROBLEM 15.3 For the following reaction in aqueous solution, identify the Brønsted-Lowry acids, bases, and conjugate acid-base pairs:


### 15.2 Acid Strength and Base Strength

A helpful way of viewing an acid-dissociation equilibrium is to realize that the two bases, $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{A}^{-}$, are competing for protons:

$$
\underset{\text { Acid }}{\mathrm{HA}(a q)}+\underset{\text { Base }}{\mathrm{H}_{2} \mathrm{O}(l)} \rightleftharpoons \underset{\text { Acid }}{\mathrm{H}_{3} \mathrm{O}^{+}(a q)}+\mathrm{A}^{-}(a q)
$$



Introduction to Aqueous Acids movie; Introduction to Aqueous Bases movie

If $\mathrm{H}_{2} \mathrm{O}$ is a stronger base (a stronger proton acceptor) than $\mathrm{A}^{-}$, the $\mathrm{H}_{2} \mathrm{O}$ molecules will get the protons, and the solution will contain mainly $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{A}^{-}$. If $\mathrm{A}^{-}$is a stronger base than $\mathrm{H}_{2} \mathrm{O}$, the $\mathrm{A}^{-}$ions will get the protons, and the solution will contain mainly HA and $\mathrm{H}_{2} \mathrm{O}$. When beginning with equal concentrations of reactants and products, the proton is always transferred to the stronger base. This means that the direction of reaction to reach equilibrium is proton transfer from the stronger acid to the stronger base to give the weaker acid and the weaker base:

$$
\text { Stronger acid }+ \text { Stronger base } \longrightarrow \text { Weaker acid }+ \text { Weaker base }
$$

Stronger $\mathrm{H}^{+}$donor + Stronger $\mathrm{H}^{+}$acceptor $\longrightarrow$ Weaker $\mathrm{H}^{+}$donor + Weaker $\mathrm{H}^{+}$acceptor
Different acids differ in their ability to donate protons (Table 15.1). A strong acid is one that is almost completely dissociated in water (Section 4.5). Thus, the acid-dissociation equilibrium of a strong acid lies nearly $100 \%$ to the right, and the solution contains almost entirely $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{A}^{-}$ions with only a negligible amount of undissociated HA molecules. Typical strong acids are perchloric acid $\left(\mathrm{HClO}_{4}\right)$, hydrochloric acid $(\mathrm{HCl})$, hydrobromic acid $(\mathrm{HBr})$, hydroiodic acid ( HI ), nitric acid $\left(\mathrm{HNO}_{3}\right)$, and sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$. It follows from this definition that strong acids have very weak conjugate bases. The ions $\mathrm{ClO}_{4}^{-}, \mathrm{Cl}^{-}, \mathrm{Br}^{-}, \mathrm{I}^{-}, \mathrm{NO}_{3}^{-}$, and $\mathrm{HSO}_{4}^{-}$have only a negligible tendency to combine with a proton in aqueous solution, and they are therefore much weaker bases than $\mathrm{H}_{2} \mathrm{O}$.

TABLE 15.1 Relative Strengths of Conjugate Acid-Base Pairs


FIGURE 15.1 Dissociation of HA involves $\mathrm{H}^{+}$transfer to $\mathrm{H}_{2} \mathrm{O}$, yielding $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{A}^{-}$. The extent of dissociation is nearly $100 \%$ for a strong acid (a), considerably less than $100 \%$ for a weak acid (b), and nearly $0 \%$ for a very weak acid (c).

A weak acid is one that is only partially dissociated in water. Only a small fraction of the weak acid molecules transfer a proton to water, and the solution therefore contains mainly undissociated HA molecules along with small amounts of $\mathrm{H}_{3} \mathrm{O}^{+}$and the conjugate base $\mathrm{A}^{-}$. Typical weak acids are nitrous acid $\left(\mathrm{HNO}_{2}\right)$, hydrofluoric acid (HF), and acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$. In the case of very weak acids such as $\mathrm{NH}_{3}, \mathrm{OH}^{-}$, and $\mathrm{H}_{2}$, the acid has practically no tendency to transfer a proton to water, and the acid-dissociation equilibrium lies essentially $100 \%$ to the left. It follows from this definition that very weak acids have strong conjugate
bases. For example, the $\mathrm{NH}_{2}^{-}, \mathrm{O}^{2-}$, and $\mathrm{H}^{-}$ions are essentially $100 \%$ protonated in aqueous solution and are much stronger bases than $\mathrm{H}_{2} \mathrm{O}$.

The equilibrium concentrations of $\mathrm{HA}, \mathrm{H}_{3} \mathrm{O}^{+}$, and $\mathrm{A}^{-}$for strong acids, weak acids, and very weak acids are represented graphically in Figure 15.1. The inverse relationship between the strength of an acid and the strength of its conjugate base is illustrated in Table 15.1.

## Worked Example 15.3

If you mix equal concentrations of reactants and products, which of the following reactions proceed to the right and which proceed to the left?
(a) $\mathrm{H}_{2} \mathrm{SO}_{4}(a q)+\mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{NH}_{4}{ }^{+}(a q)+\mathrm{HSO}_{4}^{-}(a q)$
(b) $\mathrm{HCO}_{3}^{-}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q) \rightleftharpoons \mathrm{HSO}_{4}^{-}(a q)+\mathrm{CO}_{3}{ }^{2-}(a q)$

## Strategy

To predict the direction of reaction, use the balanced equation to identify the proton donors (acids) and proton acceptors (bases), and then use Table 15.1 to identify the stronger acid and the stronger base. When equal concentrations of reactants and products are present, proton transfer always occurs from the stronger acid to the stronger base.

## SOlUTION

(a) In this reaction, $\mathrm{H}_{2} \mathrm{SO}_{4}$ and $\mathrm{NH}_{4}{ }^{+}$are the acids, and $\mathrm{NH}_{3}$ and $\mathrm{HSO}_{4}{ }^{-}$are the bases. According to Table 15.1, $\mathrm{H}_{2} \mathrm{SO}_{4}$ is a stronger acid than $\mathrm{NH}_{4}{ }^{+}$, and $\mathrm{NH}_{3}$ is a stronger base than $\mathrm{HSO}_{4}^{-}$. Therefore, $\mathrm{NH}_{3}$ gets the proton, and the reaction proceeds from left to right.

$$
\begin{aligned}
& \mathrm{H}_{2} \mathrm{SO}_{4}(a q)+\mathrm{NH}_{3}(a q) \longrightarrow \mathrm{NH}_{4}^{+}(a q)+\mathrm{HSO}_{4}^{-}(a q) \\
& \text { Stronger acid } \quad \text { Stronger base } \quad \text { Weaker acid } \quad \text { Weaker base }
\end{aligned}
$$

(b) $\mathrm{HCO}_{3}{ }^{-}$and $\mathrm{HSO}_{4}^{-}$are the acids, and $\mathrm{SO}_{4}{ }^{2-}$ and $\mathrm{CO}_{3}{ }^{2-}$ are the bases. Table 15.1 indicates that $\mathrm{HSO}_{4}^{-}$is the stronger acid, and $\mathrm{CO}_{3}{ }^{2-}$ is the stronger base. Therefore, $\mathrm{CO}_{3}{ }^{2-}$ gets the proton, and the reaction proceeds from right to left.


- PROBLEM 15.4 If you mix equal concentrations of reactants and products, which of the following reactions proceed to the right and which proceed to the left?
(a) $\mathrm{HF}(a q)+\mathrm{NO}_{3}^{-}(a q) \rightleftharpoons \mathrm{HNO}_{3}(a q)+\mathrm{F}^{-}(a q)$
(b) $\mathrm{NH}_{4}^{+}(a q)+\mathrm{CO}_{3}^{2-}(a q) \rightleftharpoons \mathrm{HCO}_{3}^{-}(a q)+\mathrm{NH}_{3}(a q)$
- KEY CONCEPT PROBLEM 15.5 The following pictures represent aqueous solutions of two acids HA ( $\mathrm{A}=\mathrm{X}$ or Y ); water molecules have been omitted for clarity.


(a) Which is the stronger acid, HX or HY ?
(b) Which is the stronger base, $\mathrm{X}^{-}$or $\mathrm{Y}^{-}$?
(c) If you mix equal concentrations of reactants and products, will the following reaction proceed to the right or to the left?

$$
\mathrm{HX}+\mathrm{Y}^{-} \rightleftharpoons \mathrm{HY}+\mathrm{X}^{-}
$$

## 15.3 | Hydrated Protons and Hydronium Ions

The proton is fundamental to both the Arrhenius and the Brønsted-Lowry definitions of an acid. Dissociation of an Arrhenius acid HA gives an aqueous hydrogen ion, or hydrated proton, written as $\mathrm{H}^{+}(a q)$ :

$$
\mathrm{HA}(a q) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{A}^{-}(a q)
$$

As a bare proton, the positively charged $\mathrm{H}^{+}$ion is too reactive to exist in aqueous solution, and so it bonds to the oxygen atom of a solvent water molecule to give the trigonal pyramidal hydronium ion, $\mathrm{H}_{3} \mathrm{O}^{+}$. The $\mathrm{H}_{3} \mathrm{O}^{+}$ion, which can be regarded as the simplest hydrate of the proton, $\left[\mathrm{H}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{+}$, can associate through hydrogen bonding with additional water molecules to give higher hydrates with the general formula $\left[\mathrm{H}\left(\mathrm{H}_{2} \mathrm{O}\right)_{n}\right]^{+}(n=2,3$, or 4$)$, such as $\mathrm{H}_{5} \mathrm{O}_{2}{ }^{+}, \mathrm{H}_{7} \mathrm{O}_{3}{ }^{+}$, and $\mathrm{H}_{9} \mathrm{O}_{4}^{+}$. It's likely that acidic aqueous solutions contain a distribution of $\left[\mathrm{H}\left(\mathrm{H}_{2} \mathrm{O}\right)_{n}\right]^{+}$ions having different values of $n$. In this book, though, we'll use the symbols $\mathrm{H}^{+}(a q)$ and $\mathrm{H}_{3} \mathrm{O}^{+}(a q)$ to mean the same thing-namely, a proton hydrated by an unspecified number of water molecules. Ordinarily, we use $\mathrm{H}_{3} \mathrm{O}^{+}$ in acid-base reactions to emphasize the proton-transfer character of these reactions.

$\mathrm{H}_{3} \mathrm{O}^{+}$- the hydronium ion, or hydrated $\mathrm{H}^{+}$

## 15.4 | Dissociation of Water

One of the most important properties of water is its ability to act both as an acid and as a base. In the presence of an acid, water acts as a base, whereas in the presence of a base, water acts as an acid (Section 15.1). It's not surprising, therefore, that in pure water one molecule can donate a proton to another in a reaction in which water acts as both an acid and a base at the same time:


Called the dissociation of water, this reaction is characterized by the equilibrium equation $K_{w}=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]$.

$$
\begin{aligned}
& 2 \mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) \\
& K_{\mathrm{w}}=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]
\end{aligned}
$$

The concentration of water is omitted from the equilibrium constant expression because, as a pure liquid, its concentration is a constant that is incorporated into
the equilibrium constant (Section 13.4). The equilibrium constant $K_{w}$ is called the ion-product constant for water.

There are two important aspects of the dynamic equilibrium in the dissociation of water. First, the forward and reverse reactions are rapid; $\mathrm{H}_{2} \mathrm{O}$ molecules, $\mathrm{H}_{3} \mathrm{O}^{+}$ions, and $\mathrm{OH}^{-}$ions continually interconvert as protons transfer quickly from one species to another. Second, the position of the equilibrium lies far to the left; at any given instant, only a tiny fraction of the water molecules are dissociated into $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$ions. The vast majority of the molecules are undissociated.

We can calculate the extent of dissociation of the water molecules starting from experimental measurements that show the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration in pure water to be $1.0 \times 10^{-7} \mathrm{M}$ at $25^{\circ} \mathrm{C}$ :

$$
\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.0 \times 10^{-7} \mathrm{M} \quad \text { at } 25^{\circ} \mathrm{C}
$$

Since the dissociation reaction of water produces equal concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$ and $\mathrm{OH}^{-}$ions, the $\mathrm{OH}^{-}$concentration in pure water is also $1.0 \times 10^{-7} \mathrm{M}$ at $25^{\circ} \mathrm{C}$ :

$$
\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M} \quad \text { at } 25^{\circ} \mathrm{C}
$$

Furthermore, we know that the molar concentration of pure water, calculated from its density and molar mass, is 55.4 M at $25^{\circ} \mathrm{C}$ :

$$
\left[\mathrm{H}_{2} \mathrm{O}\right]=\left(\frac{997 \mathrm{~g}}{\mathrm{~L}}\right)\left(\frac{1 \mathrm{~mol}}{18.0 \mathrm{~g}}\right)=55.4 \mathrm{~mol} / \mathrm{L} \quad \text { at } 25^{\circ} \mathrm{C}
$$

From these facts, we can conclude that the ratio of dissociated to undissociated water molecules is about 2 in $10^{9}$, a very small number indeed:

$$
\frac{1.0 \times 10^{-7} \mathrm{M}}{55.4 \mathrm{M}}=1.8 \times 10^{-9} \quad \text { about } 2 \text { in } 10^{9}
$$

In addition, we can calculate that the numerical value of $K_{\mathrm{w}}$ at $25^{\circ} \mathrm{C}$ is $1.0 \times 10^{-14}$ :

$$
\begin{aligned}
K_{\mathrm{w}} & =\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]=\left(1.0 \times 10^{-7}\right)\left(1.0 \times 10^{-7}\right) \\
& =1.0 \times 10^{-14} \quad \text { at } 25^{\circ} \mathrm{C}
\end{aligned}
$$

In very dilute solutions, the product of the $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$concentrations is unaffected by the presence of solutes. This is not true in more concentrated solutions, but we'll neglect that complication and assume that the product of the $\mathrm{H}_{3} \mathrm{O}^{+}$ and $\mathrm{OH}^{-}$concentrations is always $1.0 \times 10^{-14}$ at $25^{\circ} \mathrm{C}$ in any aqueous solution.

We can distinguish acidic, neutral, and basic aqueous solutions by the relative values of the $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$concentrations:

$$
\begin{aligned}
& \text { Acidic: }\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]>\left[\mathrm{OH}^{-}\right] \\
& \text {Neutral: }\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right] \\
& \text {Basic: }\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]<\left[\mathrm{OH}^{-}\right]
\end{aligned}
$$

At $25^{\circ} \mathrm{C},\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]>1.0 \times 10^{-7} \mathrm{M}$ in an acidic solution, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=$ $1.0 \times 10^{-7} \mathrm{M}$ in a neutral solution, and $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]<1.0 \times 10^{-7} \mathrm{M}$ in a basic solution (Figure 15.2). If one of the concentrations, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$or $\left[\mathrm{OH}^{-}\right]$, is known, the other is readily calculated:

$$
\begin{array}{ll}
\text { Since } & {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]=K_{\mathrm{w}}=1.0 \times 10^{-14}} \\
\text { then } & {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{1.0 \times 10^{-14}}{\left[\mathrm{OH}^{-}\right]} \text {and }\left[\mathrm{OH}^{-}\right]=\frac{1.0 \times 10^{-14}}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]}}
\end{array}
$$

In the previous discussion, we were careful to emphasize that the value of $K_{\mathrm{w}}=1.0 \times 10^{-14}$ applies only at $25^{\circ} \mathrm{C}$. This is because $K_{\mathrm{w}}$, like all equilibrium constants, is affected by temperature, and the $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$concentrations in

FIGURE 15.2 Values of the $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$concentrations at $25^{\circ} \mathrm{C}$ in acidic, neutral, and basic solutions.

neutral aqueous solutions at temperatures other than $25^{\circ} \mathrm{C}$ deviate from $1.0 \times 10^{-7} \mathrm{M}$ (see Problem 15.7). Unless otherwise indicated, we'll always assume a temperature of $25^{\circ} \mathrm{C}$.

## Worked Example 15.4

The concentration of $\mathrm{H}_{3} \mathrm{O}^{+}$ions in a sample of lemon juice is $2.5 \times 10^{-3} \mathrm{M}$. Calculate the concentration of $\mathrm{OH}^{-}$ions, and classify the solution as acidic, neutral, or basic.

## Strategy

When $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$is known, the $\mathrm{OH}^{-}$concentration can be found from the expression $\left[\mathrm{OH}^{-}\right]=K_{\mathrm{w}} /\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$.

## Solution

$$
\left[\mathrm{OH}^{-}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]}=\frac{1.0 \times 10^{-14}}{2.5 \times 10^{-3}}=4.0 \times 10^{-12} \mathrm{M}
$$

Because $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]>\left[\mathrm{OH}^{-}\right]$, the solution is acidic.
$\checkmark$ Ballpark Check Because the product of the $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$concentrations must equal $10^{-14}$, and because the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration is in the range $10^{-3} \mathrm{M}$ to $10^{-2} \mathrm{M}$, the $\mathrm{OH}^{-}$concentration must be in the range $10^{-11} \mathrm{M}$ to $10^{-12} \mathrm{M}$. The ballpark check and the solution agree.

- PROBLEM 15.6 The concentration of $\mathrm{OH}^{-}$in a sample of seawater is $5.0 \times 10^{-6} \mathrm{M}$. Calculate the concentration of $\mathrm{H}_{3} \mathrm{O}^{+}$ions, and classify the solution as acidic, neutral, or basic.

PROBLEM 15.7 At $50^{\circ} \mathrm{C}$ the value of $K_{\mathrm{w}}$ is $5.5 \times 10^{-14}$. What are the concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$in a neutral solution at $50^{\circ} \mathrm{C}$ ?

## 15.5 | The pH Scale

Rather than write hydronium ion concentrations in molarity, it's more convenient to express them on a logarithmic scale known as the pH scale. The term $\mathbf{p H}$ is derived from the French puissance d'hydrogène ("power of hydrogen") and refers to the power of 10 (the exponent) used to express the molar $\mathrm{H}_{3} \mathrm{O}^{+}$concentration. The pH of a solution is defined as the negative base-10 logarithm (log) of the molar hydronium ion concentration:

$$
\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right] \text {or }\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\operatorname{antilog}(-\mathrm{pH})=10^{-\mathrm{pH}}
$$

Thus, an acidic solution having $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=10^{-2} \mathrm{M}$ has a pH of 2, a basic solution having $\left[\mathrm{OH}^{-}\right]=10^{-2} \mathrm{M}$ and $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=10^{-12} \mathrm{M}$ has a pH of 12 , and a neutral solution having $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=10^{-7} \mathrm{M}$ has a pH of 7 . Note that we can take the log of $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$because $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] is a dimensionless ratio of the actual concentration to the concentration ( 1 M ) in the standard state. (The pOH can be defined in the same way as the pH . Just as $\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$, so $\mathrm{pOH}=-\log \left[\mathrm{OH}^{-}\right]$. It follows from the equation $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-14}$ that $\mathrm{pH}+\mathrm{pOH}=14.00$.)

If you use a calculator to find the pH from the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration, your answer will have more decimal places than the proper number of significant figures. For example, the pH of the lemon juice in Worked Example 15.4 $\left(\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=2.5 \times 10^{-3} \mathrm{M}\right)$ is found on a calculator to be

$$
\mathrm{pH}=-\log \left(2.5 \times 10^{-3}\right)=2.60206
$$

This result should be rounded to pH 2.60 (two significant figures) because $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] has only two significant figures. Note that the only significant figures in a logarithm are the digits to the right of the decimal point; the number to the left of the decimal point is an exact number related to the integral power of 10 in the exponential expression for $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$:


Because the pH scale is logarithmic, the pH changes by 1 unit when $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$ changes by a factor of 10 , by 2 units when $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$changes by a factor of 100 , and by 6 units when $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$changes by a factor of $1,000,000$. To appreciate the extent to which the pH scale is a compression of the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$scale, compare the amounts of 12 M HCl required to change the pH of the water in a backyard swimming pool: Only about 100 mL of 12 M HCl is needed to change the pH from 7 to 6 , but a $10,000 \mathrm{~L}$ truckload of 12 M HCl is needed to change the pH from 7 to 1 .

The pH scale and pH values for some common substances are shown in Figure 15.3. Because the pH is the negative $\log$ of $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$, the pH decreases as $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] increases. Thus, when $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] increases from $10^{-7} \mathrm{M}$ to $10^{-6} \mathrm{M}$, the pH decreases from 7 to 6 . As a result, acidic solutions have pH less than 7 , and basic solutions have pH greater than 7 .

$$
\begin{array}{ll}
\text { Acidic solution: } & \mathrm{pH}<7 \\
\text { Neutral solution: } & \mathrm{pH}=7 \\
\text { Basic solution: } & \mathrm{pH}>7
\end{array}
$$

## Worked Example 15.5

Calculate the pH of an aqueous ammonia solution that has an $\mathrm{OH}^{-}$concentration of $1.9 \times 10^{-3} \mathrm{M}$.

## Strategy

First calculate the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration from the $\mathrm{OH}^{-}$concentration, and then take the negative of the logarithm of $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$to convert to pH .

## Solution

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{1.9 \times 10^{-3}}=5.3 \times 10^{-12} \mathrm{M}} \\
& \mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=-\log \left(5.3 \times 10^{-12}\right)=11.28
\end{aligned}
$$

Stephen J. Hawkes, "Teaching the Truth about pH," J. Chem. Educ., Vol. 71, 1994, 747-749.

7. Addison Ault, "Do pH in Your Head," J. Chem. Educ., Vol. 76, 1999, 936-938.


A FIGURE 15.3 The pH scale and pH values for some common substances.

Typically pH measurements fall within the range $0-14$; however, the scale extends beyond those values in both directions and includes negative pHs .

B. J. Fortman and K. M. Stubbs, "Demonstrations with RedCabbage Indicator," J. Chem. Educ., Vol. 69, 1992, 66. Anthocyanin pigment extract from red cabbage is used as a pH indicator exhibiting colors that range from green to aqua to violet to red in the presence of various concentrations of household ammonia and white vinegar.

The pH is quoted to two significant figures (.28) because $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$is known to two significant figures (5.3).
$\checkmark$ BALLPARK CHECK Because $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$is between $10^{-3} \mathrm{M}$ and $10^{-2} \mathrm{M},\left[\mathrm{OH}^{-}\right]$is between $10^{-11} \mathrm{M}$ and $10^{-12} \mathrm{M}$. Therefore, the pH is between 11 and 12 , in agreement with the solution.

## Worked Example 15.6

Acid rain is a matter of serious concern because most species of fish die in waters having a pH lower than 4.5-5.0. Calculate the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration in a lake that has a pH of 4.5.

## Strategy

Calculate the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration by taking the antilogarithm of the negative of the pH .
SOlution

$$
\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\operatorname{antilog}(-\mathrm{pH})=10^{-\mathrm{pH}}=10^{-4.5}=3 \times 10^{-5} \mathrm{M}
$$

[ $\mathrm{H}_{3} \mathrm{O}^{+}$] is reported to only one significant figure because the pH has only one digit beyond the decimal point. (If you need help in finding the antilog of a number, see Appendix A.2.)
$\checkmark$ BALLPARK CHECK Because a pH of 4.5 is between 4 and $5,\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$is between $10^{-4} \mathrm{M}$ and $10^{-5} \mathrm{M}$, in agreement with the solution.

- PROBLEM 15.8 Calculate the pH of each of the following solutions:
(a) A sample of seawater that has an $\mathrm{OH}^{-}$concentration of $1.58 \times 10^{-6} \mathrm{M}$
(b) A sample of acid rain that has an $\mathrm{H}_{3} \mathrm{O}^{+}$concentration of $6.0 \times 10^{-5} \mathrm{M}$
- PROBLEM 15.9 Calculate the concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$in each of the following solutions:
(a) Human blood (pH 7.40)
(b) A cola beverage ( pH 2.8 )


## 15.6 | Measuring pH

The approximate pH of a solution can be determined by using an acid-base indicator, a substance that changes color in a specific pH range (Figure 15.4). Indicators (abbreviated HIn) exhibit pH -dependent color changes because they are weak acids and have different colors in their acid (HIn) and conjugate base ( $\mathrm{In}^{-}$) forms:

$$
\operatorname{HIn}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{In}^{-}(a q)
$$

Bromthymol blue, for example, changes color in the pH range $6.0-7.6$ from yellow in its acid form to blue in its base form. Phenolphthalein changes in the pH range 8.2-9.8 from colorless in its acid form to pink in its base form.

Because indicators change color over a range of about 2 pH units, it's possible to determine the pH of a solution to within approximately $\pm 1$ unit simply by adding to the solution a few drops of an indicator that changes color in the appropriate pH range. To make the determination particularly easy, a mixture of indicators known as universal indicator is commercially available for making approximate pH measurements in the range 3-10 (Figure 15.5). More accurate values can be determined with an electronic instrument called a pH meter (Figure 15.6), a device that measures the pH -dependent electrical potential of the test solution. We'll learn more about pH meters in Section 18.7.

(a)

(b)


A FIGURE 15.5 (a) The color of universal indicator in solutions of known pH from 1 to 12. (b) The color of universal indicator in some familiar products gives the following approximate pH values: vinegar, pH 3 ; club soda, $\mathrm{pH} 4-5$; household ammonia, $\mathrm{pH} \geq 10$.

### 15.7 The pH in Solutions of Strong Acids and Strong Bases

The commonly encountered strong acids listed in Table 15.1 include three monoprotic acids $\left(\mathrm{HClO}_{4}, \mathrm{HCl}\right.$, and $\left.\mathrm{HNO}_{3}\right)$, which contain a single dissociable proton, and one diprotic acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$, which has two dissociable protons. Because strong monoprotic acids are $100 \%$ dissociated in aqueous solution, the $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{A}^{-}$concentrations are equal to the initial concentration of the acid, and the concentration of undissociated HA molecules is essentially zero.

$$
\mathrm{HA}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \xrightarrow{100 \%} \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{A}^{-}(a q)
$$

The pH of a solution of a strong monoprotic acid is easily calculated from the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration, as shown in Worked Example 15.7. Calculation of the pH of an $\mathrm{H}_{2} \mathrm{SO}_{4}$ solution is more complicated because $100 \%$ of the $\mathrm{H}_{2} \mathrm{SO}_{4}$ molecules

A FIGURE 15.4 Some common acid-base indicators and their color changes. The color of an indicator changes over a range of about 2 pH units.


A FIGURE 15.6 A pH meter with its electrical probe dipping into a grapefruit. An accurate value of the pH (3.7) is shown on the meter.


A Lime is spread on lawns and gardens to raise the pH of acidic soils.

dissociate to give $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{HSO}_{4}^{-}$ions, but less than $100 \%$ of the resulting $\mathrm{HSO}_{4}{ }^{-}$ions dissociate to give $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{SO}_{4}{ }^{2-}$ ions (we'll have more to say about diprotic acids in Section 15.11).

The most familiar examples of strong bases are alkali metal hydroxides, MOH , such as NaOH (caustic soda) and KOH (caustic potash). These compounds are water-soluble ionic solids that exist in aqueous solution as alkali metal cations $\left(\mathrm{M}^{+}\right)$and $\mathrm{OH}^{-}$anions:

$$
\mathrm{MOH}(s) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{MOH}(a q) \xrightarrow{100 \%} \mathrm{M}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

Thus, 0.10 M NaOH contains $0.10 \mathrm{M} \mathrm{Na}^{+}$and $0.10 \mathrm{M} \mathrm{OH}^{-}$, and the pH is readily calculated from the $\mathrm{OH}^{-}$concentration, as shown in Worked Example 15.8a.

The alkaline earth metal hydroxides $\mathrm{M}(\mathrm{OH})_{2}(\mathrm{M}=\mathrm{Mg}, \mathrm{Ca}, \mathrm{Sr}$, or Ba$)$ are also strong bases ( $\sim 100 \%$ dissociated), but they give lower $\mathrm{OH}^{-}$concentrations because they are less soluble. Their solubility at room temperature varies from $38 \mathrm{~g} / \mathrm{L}$ for the relatively soluble $\mathrm{Ba}(\mathrm{OH})_{2}$ to $\sim 10^{-2} \mathrm{~g} / \mathrm{L}$ for the relatively insoluble $\mathrm{Mg}(\mathrm{OH})_{2}$. Aqueous suspensions of $\mathrm{Mg}(\mathrm{OH})_{2}$, called milk of magnesia, are used as an antacid. The most common and least expensive alkaline earth hydroxide is $\mathrm{Ca}(\mathrm{OH})_{2}$, which is used in making mortars and cements. It is called slaked lime because it is made by treating lime $(\mathrm{CaO})$ with water. Aqueous solutions of the slightly soluble $\mathrm{Ca}(\mathrm{OH})_{2}$ (solubility $\sim 1.3 \mathrm{~g} / \mathrm{L}$ ) are known as limewater.

Alkaline earth oxides, such as CaO , are even stronger bases than the corresponding hydroxides because the oxide ion $\left(\mathrm{O}^{2-}\right)$ is a stronger base than $\mathrm{OH}^{-}$ (Table 15.1). In fact, the $\mathrm{O}^{2-}$ ion can't exist in aqueous solutions because it is immediately and completely protonated by water, yielding $\mathrm{OH}^{-}$ions:

$$
\mathrm{O}^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \xrightarrow{100 \%} \mathrm{OH}^{-}(a q)+\mathrm{OH}^{-}(a q)
$$

Thus, when lime is dissolved in water, it gives $2 \mathrm{OH}^{-}$ions per CaO formula unit:

$$
\mathrm{CaO}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Ca}^{2+}(a q)+2 \mathrm{OH}^{-}(a q)
$$

Lime is the world's most important strong base. It is produced in enormous quantities ( 21 million tons per year in the United States) for use in steelmaking, water purification, and chemical manufacture. Lime is made by decomposition of limestone, $\mathrm{CaCO}_{3}$, at temperatures of $800-1000^{\circ} \mathrm{C}$ :

$$
\mathrm{CaCO}_{3}(s) \xrightarrow{\text { Heat }} \mathrm{CaO}(s)+\mathrm{CO}_{2}(g)
$$

## Worked Example 15.7

Calculate the pH of a $0.025 \mathrm{M} \mathrm{HNO}_{3}$ solution.

## Strategy

Since nitric acid is a strong acid, it is almost completely dissociated in aqueous solution. Therefore, the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$equals the initial concentration of the $\mathrm{HNO}_{3}$, and the pH equals the negative $\log$ of the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$.

## SOlUTION

$$
\begin{aligned}
& \mathrm{HNO}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \xrightarrow{100 \%} \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NO}_{3}^{-}(a q) \\
& \mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=-\log \left(2.5 \times 10^{-2}\right)=1.60
\end{aligned}
$$

$\checkmark$ Ballpark Check Because the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$is between $10^{-1} \mathrm{M}$ and $10^{-2} \mathrm{M}$, the pH is between 1 and 2, in agreement with the solution.

## Worked Example 15.8

Calculate the pH of each of the following solutions:
(a) A 0.10 M solution of NaOH
(b) A 0.0050 M solution of slaked lime $\left[\mathrm{Ca}(\mathrm{OH})_{2}\right]$
(c) A solution prepared by dissolving 0.28 g of lime $(\mathrm{CaO})$ in enough water to make 1.00 L of limewater $\left[\mathrm{Ca}(\mathrm{OH})_{2}(\mathrm{aq})\right]$

## Strategy

Because NaOH and $\mathrm{Ca}(\mathrm{OH})_{2}$ are strong bases, they are $100 \%$ dissociated and their $\left[\mathrm{OH}^{-}\right]$is directly related to their initial concentrations. To calculate the $\left[\mathrm{OH}^{-}\right.$] in a solution prepared by dissolving CaO , we must first do a mass-to-mole conversion and then use the balanced equation for the reaction of CaO with water to find the number of moles of $\mathrm{OH}^{-}$in the solution. In each case, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=K_{\mathrm{w}} /\left[\mathrm{OH}^{-}\right]$and $\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$.

## Solution

(a) Because NaOH is a strong base, $\left[\mathrm{OH}^{-}\right]=0.10 \mathrm{M},\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.0 \times 10^{-13} \mathrm{M}$, and $\mathrm{pH}=13.00$.

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{0.10}=1.0 \times 10^{-13} \mathrm{M}} \\
& \mathrm{pH}=-\log \left(1.0 \times 10^{-13}\right)=13.00
\end{aligned}
$$

(b) Because slaked lime is a strong base, it provides $2 \mathrm{OH}^{-}$per $\mathrm{Ca}(\mathrm{OH})_{2}$ formula unit. Therefore, $\left[\mathrm{OH}^{-}\right]=2(0.0050 \mathrm{M})=0.010 \mathrm{M},\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.0 \times 10^{-12} \mathrm{M}$, and $\mathrm{pH}=12.00$ :

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{0.010}=1.0 \times 10^{-12} \mathrm{M}} \\
& \mathrm{pH}=-\log \left(1.0 \times 10^{-12}\right)=12.00
\end{aligned}
$$

(c) First calculate the number of moles of CaO dissolved from the given mass of CaO and its molar mass ( $56.1 \mathrm{~g} / \mathrm{mol}$ ):

$$
\text { Moles of } \mathrm{CaO}=0.28 \mathrm{~g} \mathrm{CaO} \times \frac{1 \mathrm{~mol} \mathrm{CaO}}{56.1 \mathrm{~g} \mathrm{CaO}}=0.0050 \mathrm{~mol} \mathrm{CaO}
$$

Protonation of the $\mathrm{O}^{2-}$ ion produces 2 mol of $\mathrm{OH}^{-}$per mole of CaO dissolved:

$$
\begin{aligned}
& \mathrm{CaO}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Ca}^{2+}(a q)+2 \mathrm{OH}^{-}(a q) \\
& \text { Moles of } \mathrm{OH}^{-} \text {produced }=2(0.0050 \mathrm{~mol})=0.010 \mathrm{~mol}
\end{aligned}
$$

Since the solution volume is 1.00 L ,

$$
\left[\mathrm{OH}^{-}\right]=\frac{0.010 \mathrm{~mol}}{1.00 \mathrm{~L}}=0.010 \mathrm{M}
$$

The $\left[\mathrm{OH}^{-}\right]$happens to be identical to that in part (b). Therefore, $\mathrm{pH}=12.00$.

- PROBLEM 15.10 Calculate the pH of:
(a) $0.050 \mathrm{M} \mathrm{HClO}_{4}$
(b) 6.0 M HCl
(c) 4.0 M KOH
(d) $0.010 \mathrm{M} \mathrm{Ba}(\mathrm{OH})_{2}$
- PROBLEM 15.11 Calculate the pH of a solution prepared by dissolving 0.25 g of BaO in enough water to make 0.500 L of solution.


## 15.8 | Equilibria in Solutions of Weak Acids

A weak acid is not the same thing as a dilute solution of a strong acid. Whereas a strong acid is $100 \%$ dissociated in aqueous solution, a weak acid is only partially dissociated. It might therefore happen by chance that the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration

$\square$Todd P. Silverstein, "Weak vs Strong Acids and Bases," J. Chem. Educ., Vol. 77, 2000, 849-850.

John J. Fortman, "Pictoral Analogies XI: Concentrations and Acidity of Solutions," J. Chem. Educ., Vol. 71, 1994, 430-432.
from complete dissociation of a dilute strong acid is the same as that from partial dissociation of a more concentrated weak acid.

Like the equilibrium reactions discussed in Chapter 13, the dissociation of a weak acid in water is characterized by an equilibrium equation. The equilibrium constant for the dissociation reaction, denoted $K_{\mathrm{a}}$, is called the acid-dissociation constant:

$$
\begin{aligned}
& \mathrm{HA}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{A}^{-}(a q) \\
& K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}
\end{aligned}
$$

Note that $\left[\mathrm{H}_{2} \mathrm{O}\right]$, which is essentially constant in dilute aqueous solutions, has been incorporated into the equilibrium constant $K_{\mathrm{a}}$ and is therefore omitted from the equilibrium constant expression for $K_{\mathrm{a}}$.

Values of $K_{\mathrm{a}}$ and $\mathrm{p} K_{\mathrm{a}}=-\log K_{\mathrm{a}}$ for some typical weak acids are listed in Table 15.2. (Just as the pH is defined as $-\log \left[\mathrm{H}^{+}\right]$, so the $\mathrm{p} K_{\mathrm{a}}$ of an acid is defined as $-\log K_{\mathrm{a}}$.) Also included in Table 15.2 for comparison are values for HCl, a typical strong acid. As indicated by the equilibrium equation, the larger the value of $K_{\mathrm{a}}$, the stronger the acid. Thus, methanol $\left(K_{\mathrm{a}}=2.9 \times 10^{-16}\right)$ is the weakest of the acids listed in Table 15.2, and nitrous acid ( $K_{\mathrm{a}}=4.5 \times 10^{-4}$ ) is the strongest of the weak acids. Strong acids, such as HCl , have $K_{\mathrm{a}}$ values that are much greater than 1. A more complete list of $K_{\mathrm{a}}$ values for weak acids is given in Appendix C.

Numerical values of acid-dissociation constants are determined from pH measurements, as shown in Worked Example 15.9.

## Worked Example 15.9

The pH of 0.250 M HF is 2.036 . What is the value of $K_{\mathrm{a}}$ for hydrofluoric acid?

## Strategy

First, write the balanced equation for the dissociation equilibrium and the equilibrium equation that defines $K_{\mathrm{a}}$. To obtain a value for $K_{a}$, we need to calculate the concentrations of the various species in the equilibrium mixture. We begin by calculating the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration from the pH . Because dissociation of one HF molecule gives one $\mathrm{H}_{3} \mathrm{O}^{+}$ion and one $\mathrm{F}^{-}$ion, the $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{F}^{-}$concentrations are equal. The HF concentration equals the initial concentration of HF minus whatever dissociates $\left(=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\right)$. Finally, we substitute the equilibrium concentrations into the equilibrium equation to obtain the value of $K_{\mathrm{a}}$.

## Solution

$$
\begin{aligned}
& \mathrm{HF}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{F}^{-}(a q) \\
& K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{F}^{-}\right]}{[\mathrm{HF}]} \\
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\operatorname{antilog}(-\mathrm{pH})=10^{-} \mathrm{pH}=10^{-2.036}=9.20 \times 10^{-3} \mathrm{M}} \\
& {\left[\mathrm{~F}^{-}\right]=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=9.20 \times 10^{-3} \mathrm{M}} \\
& {[\mathrm{HF}]=0.250-0.00920=0.241 \mathrm{M}} \\
& K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{F}^{-}\right]}{[\mathrm{HF}]}=\frac{\left(9.20 \times 10^{-3}\right)\left(9.20 \times 10^{-3}\right)}{0.241}=3.52 \times 10^{-4}
\end{aligned}
$$


$\checkmark$ BALLPARK CHECK Because the pH is about $2,\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] and $\left[\mathrm{F}^{-}\right]$are about $10^{-2} \mathrm{M}$, and [HF] is about $0.25 \mathrm{M}\left(0.250 \mathrm{M}-10^{-2} \mathrm{M}\right)$. The value of $K_{\mathrm{a}}$ is therefore about $\left(10^{-2}\right)\left(10^{-2}\right) / 0.25$, or $4 \times 10^{-4}$. The ballpark check and solution agree.

TABLE 15.2 Acid-Dissociation Constants at $25^{\circ} \mathrm{C}$


[^17]- PROBLEM 15.12 The pH of 0.10 M HOCl is 4.23 . Calculate $K_{\mathrm{a}}$ for hypochlorous acid, and check your answer against the value given in Table 15.2.
- KEY CONCEPT PROBLEM 15.13 The following pictures represent aqueous solutions of three acids HA ( $\mathrm{A}=\mathrm{X}, \mathrm{Y}$, or Z ); water molecules have been omitted for clarity:

(a) Arrange the three acids in order of increasing value of $K_{\mathrm{a}}$.
(b) Which acid, if any, is a strong acid?
(c) Which solution has the highest pH , and which has the lowest pH ?


### 15.9 Calculating Equilibrium Concentrations in Solutions of Weak Acids

Once the $K_{\mathrm{a}}$ value for a weak acid has been measured, it can be used to calculate equilibrium concentrations and the pH in a solution of the acid. We'll illustrate the approach to such a problem by calculating the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{CN}^{-}, \mathrm{HCN}\right.$, and $\left.\mathrm{OH}^{-}\right)$and the pH in a 0.10 M HCN solution. The approach we'll take is quite general and will be useful on numerous later occasions.

The key to solving acid-base equilibrium problems is to think about the chem-istry-that is, to consider the possible proton-transfer reactions that can take place between Brønsted-Lowry acids and bases.
Step 1. Let's begin by listing the species present initially before any dissociation reactions and by identifying them as acids or bases. We'll include in our list the acid HCN and the solvent $\mathrm{H}_{2} \mathrm{O}$, but won't include the species that are produced by dissociation reactions $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{CN}^{-}\right.$, and $\left.\mathrm{OH}^{-}\right)$because they are present only in small concentrations. Since water can behave either as an acid or a base, our list of species present initially is

| HCN | $\mathrm{H}_{2} \mathrm{O}$ |
| :---: | :---: |
| Acid | Acid or base |

Step 2. Because we have two acids $\left(\mathrm{HCN}\right.$ and $\left.\mathrm{H}_{2} \mathrm{O}\right)$ and just one base $\left(\mathrm{H}_{2} \mathrm{O}\right)$, two proton-transfer reactions are possible:

$$
\begin{aligned}
\mathrm{HCN}(a q)+\mathrm{H}_{2} \mathrm{O}(l) & \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CN}^{-}(a q)
\end{aligned} \quad K_{\mathrm{a}}=4.9 \times 10^{-10} 0
$$

The value of $K_{\mathrm{a}}$ for HCN comes from Table 15.2.
Step 3. The proton-transfer reaction that proceeds farther to the right-the one that has the larger equilibrium constant-is called the principal reaction. Any other proton-transfer reactions are called subsidiary reactions. Since $K_{\mathrm{a}}$ for HCN is more than 1000 times greater than $K_{\mathrm{w}}$, the principal reaction in this case is
dissociation of HCN, and dissociation of water is a subsidiary reaction. Although the principal reaction and the subsidiary reaction both produce $\mathrm{H}_{3} \mathrm{O}^{+}$ions, there is only one $\mathrm{H}_{3} \mathrm{O}^{+}$concentration in the solution, which must simultaneously satisfy the equilibrium equations for both reactions. To make life simple, we'll assume that essentially all the $\mathrm{H}_{3} \mathrm{O}^{+}$comes from the principal reaction:

$$
\begin{aligned}
{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right](\text {total }) } & =\left[\mathrm{H}_{3} \mathrm{O}^{+}\right](\text {from principal reaction })+\left[\mathrm{H}_{3} \mathrm{O}^{+}\right] \text {(from subsidiary reaction) } \\
& \approx\left[\mathrm{H}_{3} \mathrm{O}^{+}\right] \text {(from principal reaction) }
\end{aligned}
$$

In other words, we'll assume that the equilibrium concentration of $\mathrm{H}_{3} \mathrm{O}^{+}$is established entirely by the dissociation of the stronger acid, HCN , while dissociation of the weaker acid, $\mathrm{H}_{2} \mathrm{O}$, makes a negligible contribution.

$$
\left[\mathrm{H}_{3} \mathrm{O}^{+}\right](\text {total }) \approx\left[\mathrm{H}_{3} \mathrm{O}^{+}\right](\text {from } \mathrm{HCN})
$$

Step 4. Next, we express the concentrations of the species involved in the principal reaction in terms of the concentration of HCN that dissociates-say, $x \mathrm{~mol} / \mathrm{L}$. According to the balanced equation for the dissociation of HCN , if $x \mathrm{~mol} / \mathrm{L}$ of HCN dissociates, then $x \mathrm{~mol} / \mathrm{L}^{2}$ of $\mathrm{H}_{3} \mathrm{O}^{+}$and $x \mathrm{~mol} / \mathrm{L}^{\text {of }} \mathrm{CN}^{-}$are formed, and the initial concentration of HCN before dissociation ( $0.10 \mathrm{~mol} / \mathrm{L}$ in our example) is reduced to $(0.10-x) \mathrm{mol} / \mathrm{L}$ at equilibrium. Let's summarize these considerations in a table under the principal reaction:

| Principal reaction: | $\mathbf{H C N}(\boldsymbol{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H}_{\mathbf{3}} \mathbf{O}^{+}(\boldsymbol{a q})+\mathbf{C N}^{-}(\boldsymbol{a q})$ |  |  |
| :--- | :--- | :--- | :---: |
| Initial conc $(\mathrm{M})$ | 0.10 | $\sim 0$ | 0 |
| Change $(\mathrm{M})$ | $-x$ | $+x$ | $+x$ |
| Equilibrium conc $(\mathrm{M})$ | $0.10-x$ | $x$ | $x$ |

Step 5. Substituting the equilibrium concentrations into the equilibrium equation for the principal reaction gives

$$
K_{\mathrm{a}}=4.9 \times 10^{-10}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CN}^{-}\right]}{[\mathrm{HCN}]}=\frac{(x)(x)}{(0.10-x)}
$$

Because $K_{\mathrm{a}}$ is very small, the principal reaction will not proceed very far to the right, and $x$ will be negligibly small compared to 0.10 . Therefore, we can make the approximation that $(0.10-x) \approx 0.10$, which greatly simplifies the solution:

$$
\begin{aligned}
& 4.9 \times 10^{-10}=\frac{(x)(x)}{(0.10-x)} \approx \frac{x^{2}}{0.10} \\
& x^{2}=4.9 \times 10^{-11} \\
& x=7.0 \times 10^{-6}
\end{aligned}
$$

Step 6. Next, we use the calculated value of $x$ to obtain the equilibrium concentration of all species involved in the principal reaction:

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{CN}^{-}\right]=x=7.0 \times 10^{-6} \mathrm{M}} \\
& {[\mathrm{HCN}]=0.10-x=0.10-\left(7.0 \times 10^{-6}\right)=0.10 \mathrm{M}}
\end{aligned}
$$

Note that our simplifying approximation, $0.10-x \approx 0.10$, is valid because $x$ is only $7.0 \times 10^{-6}$ and the initial [HCN] is 0.10 . It's important to check the validity of the simplifying approximation in every problem because $x$ is not always negligible compared to the initial concentration of the acid. Worked Example 15.10 illustrates such a case.
Step 7. The concentrations of the species involved in the principal reaction are the "big" concentrations. The species involved in the subsidiary reaction(s) are present in smaller concentrations that can be calculated from equilibrium equations for the subsidiary reaction(s) and the big concentrations already determined. In
the present problem, only the $\mathrm{OH}^{-}$concentration remains to be calculated. It is determined from the subsidiary equilibrium equation, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]=K_{\mathrm{w}}$, and the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration $\left(7.0 \times 10^{-6} \mathrm{M}\right)$ already calculated from the principal reaction:

$$
\left[\mathrm{OH}^{-}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]}=\frac{1.0 \times 10^{-14}}{7.0 \times 10^{-6}}=1.4 \times 10^{-9} \mathrm{M}
$$

Note that $\left[\mathrm{OH}^{-}\right]$is 5000 times smaller than $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$.
At this point, we can check the initial assumption that essentially all the $\mathrm{H}_{3} \mathrm{O}^{+}$ comes from the principal reaction. Because dissociation of water gives one $\mathrm{H}_{3} \mathrm{O}^{+}$ ion for each $\mathrm{OH}^{-}$ion and because water is the only source of $\mathrm{OH}^{-},\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$from the dissociation of water is equal to $\left[\mathrm{OH}^{-}\right]$, which we just calculated to be $1.4 \times 10^{-9} \mathrm{M}$. This value is negligible compared with $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$from the dissociation of $\mathrm{HCN}\left(7.0 \times 10^{-6} \mathrm{M}\right)$.

$$
\begin{aligned}
{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right](\text {total }) } & =\left[\mathrm{H}_{3} \mathrm{O}^{+}\right](\text {from HCN })+\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left(\text {from } \mathrm{H}_{2} \mathrm{O}\right) \\
& =\left(7.0 \times 10^{-6} \mathrm{M}\right)+\left(1.4 \times 10^{-9} \mathrm{M}\right)=7.0 \times 10^{-6} \mathrm{M}
\end{aligned}
$$

Step 8. Finally, we can calculate the pH :

$$
\mathrm{pH}=-\log \left(\operatorname{total}\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\right)=-\log \left(7.0 \times 10^{-6}\right)=5.15
$$

Step 1. List the species present before dissociation and identify them as Brønsted-Lowry
follow in solving problems involving weak acids.
acids or bases.

Step 2. Write balanced equations for all possible proton-transfer reactions.

Step 3. Identify the principal reaction-the reaction that has the largest equilibrium constant.


Step 4. Make a table that lists the following values for each of the species involved in the principal reaction:
(a) The initial concentration
(b) The change in concentration on proceeding to equilibrium
(c) The equilibrium concentration

In constructing this table, define $x$ as the concentration (mol/L) of the acid that dissociates.

Step 5. Substitute the equilibrium concentrations into the equilibrium equation for the principal reaction, and solve for $x$.


Step 6. Calculate the "big" concentrations-the concentrations of the species involved in the principal reaction.

Step 7. Use the big concentrations and the equilibrium equations for the subsidiary reactions to calculate the small concentrations-the concentrations of the species involved in the subsidiary equilibria.

Step 8. Calculate the $\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$.

Figure 15.7 summarizes the steps followed in solving this problem. This same systematic approach is applied to all aqueous equilibrium problems in this chapter and in Chapter 16.

## Worked Example 15.10

Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{F}^{-}, \mathrm{HF}\right.$, and $\mathrm{OH}^{-}$) in 0.050 M HF .

## Strategy

Follow the eight-step sequence outlined in Figure 15.7.

## Solution

Step 1. The species present initially are

| HF | $\mathrm{H}_{2} \mathrm{O}$ |
| :---: | :---: |
| Acid | Acid or base |

Step 2. The possible proton-transfer reactions are

$$
\begin{array}{ll}
\mathrm{HF}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{F}^{-}(a q) & K_{\mathrm{a}}=3.5 \times 10^{-4} \\
\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) & K_{\mathrm{w}}=1.0 \times 10^{-14}
\end{array}
$$

Step 3. Since $K_{\mathrm{a}} \gg K_{\mathrm{w}}$, the principal reaction is dissociation of HF.
Step 4.

| Principal reaction: | $\mathbf{H F}(\boldsymbol{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H}_{\mathbf{3}} \mathbf{O}^{+}(\boldsymbol{a q})+\mathbf{F}^{-}(\boldsymbol{a q} \boldsymbol{q}$ |  |  |
| :--- | :--- | :--- | :---: |
| Initial conc (M) | 0.050 | $\sim 0$ | 0 |
| Change $(\mathrm{M})$ | $-x$ | $+x$ | $+x$ |
| Equilibrium conc $(\mathrm{M})$ | $0.050-x$ | $x$ | $x$ |

Step 5. Substituting the equilibrium concentrations into the equilibrium equation for the principal reaction gives

$$
K_{\mathrm{a}}=3.5 \times 10^{-4}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{F}^{-}\right]}{[\mathrm{HF}]}=\frac{(x)(x)}{(0.050-x)}
$$

Making the usual approximation that $x$ is negligible compared with the initial concentration of the acid, we assume that $(0.050-x) \approx 0.050$ and then solve for an approximate value of $x$ :

$$
\begin{aligned}
& x^{2} \approx\left(3.5 \times 10^{-4}\right)(0.050) \\
& x \approx 4.2 \times 10^{-3}
\end{aligned}
$$

Since the initial concentration of $\mathrm{HF}(0.050 \mathrm{M})$ is known to the third decimal place, $x$ is negligible compared with the initial [HF] only if $x$ is less than 0.001 M. Our approximate value of $x(0.0042 \mathrm{M})$ is not negligible compared with 0.050 M , and so our approximation, $0.050-x \approx 0.050$, is invalid. We must therefore solve the quadratic equation without making approximations:

$$
\begin{aligned}
& 3.5 \times 10^{-4}=\frac{x^{2}}{(0.050-x)} \\
& x^{2}+\left(3.5 \times 10^{-4}\right) x-\left(1.75 \times 10^{-5}\right)=0
\end{aligned}
$$

We use the standard quadratic formula (Appendix A.4):

$$
\begin{aligned}
x & =\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a} \\
x & =\frac{-\left(3.5 \times 10^{-4}\right) \pm \sqrt{\left(3.5 \times 10^{-4}\right)^{2}-4\left(-1.75 \times 10^{-5}\right)}}{2} \\
& =\frac{-\left(3.5 \times 10^{-4}\right) \pm\left(8.37 \times 10^{-3}\right)}{2} \\
& =+4.0 \times 10^{-3} \quad \text { or }-4.4 \times 10^{-3}
\end{aligned}
$$

Of the two solutions for $x$, only the positive value has physical meaning, since $x$ is the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration. Therefore,

$$
x=4.0 \times 10^{-3}
$$

Step 6. The big concentrations are

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{F}^{-}\right]=x=4.0 \times 10^{-3} \mathrm{M}} \\
& {[\mathrm{HF}]=(0.050-x)=(0.050-0.0040)=0.046 \mathrm{M}}
\end{aligned}
$$

Step 7. The small concentration, $\left[\mathrm{OH}^{-}\right]$, is obtained from the subsidiary equilibrium, the dissociation of water:

$$
\left[\mathrm{OH}^{-}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]}=\frac{1.0 \times 10^{-14}}{4.0 \times 10^{-3}}=2.5 \times 10^{-12} \mathrm{M}
$$

## Step 8.

$$
\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=-\log \left(4.0 \times 10^{-3}\right)=2.40
$$

$\checkmark$ Ballpark Check Arithmetic errors in solving quadratic equations are common, so it's a good idea to check that the value of $x$ obtained from the quadratic is reasonable. If the approximate value of $x\left(4.2 \times 10^{-3}\right)$ is fairly small compared to the initial concentration of the acid $(0.050 \mathrm{M})$, as is the case in this problem, then the value of $x$ obtained from the quadratic $\left(4.0 \times 10^{-3}\right)$ should be fairly close to the approximate value of $x$. The approximate and more exact values of $x$ agree.

- PROBLEM 15.14 Acetic acid, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$, is the solute that gives vinegar its characteristic odor and sour taste. Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{CH}_{3} \mathrm{CO}_{2}^{-}, \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right.$, and $\left.\mathrm{OH}^{-}\right)$in:
(a) $1.00 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$
(b) $0.0100 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$
- PROBLEM 15.15 A vitamin C tablet containing 250 mg of ascorbic acid $\left(\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{6} ; K_{\mathrm{a}}=8.0 \times 10^{-5}\right)$ is dissolved in a 250 mL glass of water. What is the pH of the solution?


## $15.10 \mid$ Percent Dissociation in Solutions of Weak Acids

In addition to $K_{a}$, another useful measure of the strength of a weak acid is the percent dissociation, defined as the concentration of the acid that dissociates divided by the initial concentration of the acid times $100 \%$ :

$$
\text { Percent dissociation }=\frac{[\mathrm{HA}] \text { dissociated }}{[\mathrm{HA}] \text { initial }} \times 100 \%
$$

Take, for example, the 1.00 M acetic acid solution in Problem 15.14a. If you solved that problem correctly, you found that $1.00 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ has an $\mathrm{H}_{3} \mathrm{O}^{+}$ concentration of $4.2 \times 10^{-3} \mathrm{M}$. Because $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] equals the concentration of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ that dissociates, the percent dissociation in $1.00 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ is $0.42 \%$ :

$$
\begin{aligned}
\text { Percent dissociation }= & \frac{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right] \text { dissociated }}{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right] \text { initial }} \times 100 \% \\
& =\frac{4.2 \times 10^{-3} \mathrm{M}}{1.00 \mathrm{M}} \times 100 \%=0.42 \%
\end{aligned}
$$

In general, the percent dissociation depends on the acid and increases with increasing value of $K_{\mathrm{a}}$. For a given weak acid, the percent dissociation increases with increasing dilution, as shown in Figure 15.8. The $0.0100 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ solution in Problem 15.14b, for example, has $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=4.2 \times 10^{-4} \mathrm{M}$, and the percent dissociation is $4.2 \%$ :

$$
\begin{aligned}
\text { Percent dissociation } & =\frac{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right] \text { dissociated }}{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right] \text { initial }} \times 100 \% \\
& =\frac{4.2 \times 10^{-4} \mathrm{M}}{0.0100 \mathrm{M}} \times 100 \%=4.2 \%
\end{aligned}
$$




Equilibrium Constant for Acids activity

〔FIGURE 15.8 The percent dissociation of acetic acid increases as the concentration of the acid decreases. A 100fold decrease in $\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]$ results in a 10 -fold increase in the percent dissociation.

© Soft drinks contain polyprotic acids such as carbonic acid and phosphoric acid.

### 15.11 Polyprotic Acids

Acids that contain more than one dissociable proton are called polyprotic acids. Polyprotic acids dissociate in a stepwise manner, and each dissociation step is characterized by its own acid-dissociation constant, $K_{\mathrm{a} 1}, K_{\mathrm{a} 2}$, and so forth. For example, carbonic acid $\left(\mathrm{H}_{2} \mathrm{CO}_{3}\right)$, the diprotic acid that forms when gaseous carbon dioxide dissolves in water, is important in maintaining a constant pH in human blood. It undergoes the following dissociation reactions:
(a) 0.050 M HF
(b) 0.50 M HF

$$
\begin{array}{ll}
\mathrm{H}_{2} \mathrm{CO}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{HCO}_{3}^{-}(a q) & \mathrm{K}_{\mathrm{a} 1}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{HCO}_{3}^{-}\right]}{\left[\mathrm{H}_{2} \mathrm{CO}_{3}\right]}=4.3 \times 10^{-7} \\
\mathrm{HCO}_{3}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CO}_{3}^{2-}(a q) & K_{\mathrm{a} 2}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CO}_{3}^{2-}\right]}{\left[\mathrm{HCO}_{3}^{-}\right]}=5.6 \times 10^{-11}
\end{array}
$$

A polyprotic acid has two or more dissociable protons. Acetic acid, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$, contains four protons, only one of which is dissociable. Hence, acetic acid is not a polyprotic acid.

As shown in Table 15.3, the values of stepwise dissociation constants of polyprotic acids decrease, typically by a factor of $10^{4}$ to $10^{6}$, in the order $K_{\mathrm{a} 1}>K_{\mathrm{a} 2}>K_{\mathrm{a} 3}$. Because of electrostatic forces, it's more difficult to remove a positively charged proton from a negative ion such as $\mathrm{HCO}_{3}{ }^{-}$than from an uncharged molecule such as $\mathrm{H}_{2} \mathrm{CO}_{3}$, so $K_{\mathrm{a} 2}<K_{\mathrm{a} 1}$. In the case of triprotic acids (such as $\mathrm{H}_{3} \mathrm{PO}_{4}$ ), it's more difficult to remove $\mathrm{H}^{+}$from an anion with a double negative charge (such as $\mathrm{HPO}_{4}{ }^{2-}$ ), than from an anion with a single negative charge (such as $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$), so $K_{\mathrm{a} 3}<K_{\mathrm{a} 2}$.

TABLE 15.3 Stepwise Dissociation Constants for Polyprotic Acids at $25^{\circ} \mathrm{C}$

| Name | Formula | $\boldsymbol{K}_{\mathbf{a} \mathbf{1}}$ | $\boldsymbol{K}_{\mathbf{a} \mathbf{2}}$ | $\boldsymbol{K}_{\mathbf{a} \mathbf{3}}$ |
| :--- | :--- | :--- | :--- | :--- |
| Carbonic acid | $\mathrm{H}_{2} \mathrm{CO}_{3}$ | $4.3 \times 10^{-7}$ | $5.6 \times 10^{-11}$ |  |
| Hydrogen sulfide | $\mathrm{H}_{2} \mathrm{~S}$ | $1.0 \times 10^{-7}$ | $\sim 10^{-19}$ |  |
| Oxalic acid | $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ | $5.9 \times 10^{-2}$ | $6.4 \times 10^{-5}$ |  |
| Phosphoric acid | $\mathrm{H}_{3} \mathrm{PO}_{4}$ | $7.5 \times 10^{-3}$ | $6.2 \times 10^{-8}$ | $4.8 \times 10^{-13}$ |
| Sulfuric acid | $\mathrm{H}_{2} \mathrm{SO}_{4}$ | Very large | $1.2 \times 10^{-2}$ |  |
| Sulfurous acid | $\mathrm{H}_{2} \mathrm{SO}_{3}$ | $1.5 \times 10^{-2}$ | $6.3 \times 10^{-8}$ |  |

* Because of its very small size, $K_{\mathrm{a} 2}$ for $\mathrm{H}_{2} \mathrm{~S}$ is difficult to measure and its value is uncertain.

Polyprotic acid solutions contain a mixture of acids- $\mathrm{H}_{2} \mathrm{~A}, \mathrm{HA}^{-}$, and $\mathrm{H}_{2} \mathrm{O}$ in the case of a diprotic acid. Because $\mathrm{H}_{2} \mathrm{~A}$ is by far the stronger acid, the principal reaction is dissociation of $\mathrm{H}_{2} \mathrm{~A}$, and essentially all the $\mathrm{H}_{3} \mathrm{O}^{+}$in the solution comes from the first dissociation step. Worked Example 15.11 shows how calculations are done.

## Worked Example 15.11

Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{2} \mathrm{CO}_{3}, \mathrm{HCO}_{3}{ }^{-}\right.$, $\mathrm{CO}_{3}{ }^{2-}, \mathrm{H}_{3} \mathrm{O}^{+}$, and $\mathrm{OH}^{-}$) in a 0.020 M carbonic acid solution.

## Strategy

Use the eight-step procedure summarized in Figure 15.7.
Steps 1-3. The species present initially are $\mathrm{H}_{2} \mathrm{CO}_{3}$ (acid) and $\mathrm{H}_{2} \mathrm{O}$ (acid or base). Because $K_{\mathrm{a} 1} \gg K_{\mathrm{w}}$, the principal reaction is dissociation of $\mathrm{H}_{2} \mathrm{CO}_{3}$.


Carbonic acid

Step 4.

| Principal reaction: | $\mathbf{H}_{\mathbf{2}} \mathbf{C O}_{\mathbf{3}}(\mathbf{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H}_{\mathbf{3}} \mathbf{O}^{+}\left(\mathbf{a q} \boldsymbol{)}+\mathbf{H C O}_{\mathbf{3}}{ }^{-}(\boldsymbol{a q})\right.$ |  |  |
| :--- | :--- | :---: | :---: |
| Initial conc $(\mathrm{M})$ | 0.020 | $\sim 0$ | 0 |
| Change (M) | $-x$ | $+x$ | $+x$ |
| Equilibrium conc (M) | $0.020-x$ | $x$ | $x$ |

Step 5. Substituting the equilibrium concentrations into the equilibrium equation for the principal reaction gives

$$
K_{\mathrm{a} 1}=4.3 \times 10^{-7}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{HCO}_{3}^{-}\right]}{\left[\mathrm{H}_{2} \mathrm{CO}_{3}\right]}=\frac{(x)(x)}{(0.020-x)}
$$

where the $K_{\mathrm{a} 1}$ value and the $K_{\mathrm{a} 2}$ value below come from Table 15.3. Assuming that $(0.020-x) \approx 0.020$,

$$
\begin{aligned}
& x^{2}=\left(4.3 \times 10^{-7}\right)(0.020) \\
& x=9.3 \times 10^{-5} \quad \text { Approximation }(0.020-x) \approx 0.020 \text { is justified. }
\end{aligned}
$$

Step 6. The big concentrations are

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{HCO}_{3}^{-}\right]=x=9.3 \times 10^{-5} \mathrm{M}} \\
& {\left[\mathrm{H}_{2} \mathrm{CO}_{3}\right]=0.020-x=0.020-0.000093=0.020 \mathrm{M}}
\end{aligned}
$$

Step 7. The small concentrations are obtained from the subsidiary equilibria-(1) dissociation of $\mathrm{HCO}_{3}^{-}$and (2) dissociation of water-and from the big concentrations already determined:
(1) $\mathrm{HCO}_{3}{ }^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CO}_{3}{ }^{2-}(a q)$

$$
\begin{aligned}
& K_{\mathrm{a} 2}=5.6 \times 10^{-11}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CO}_{3}{ }^{2-}\right]}{\left[\mathrm{HCO}_{3}{ }^{-}\right]}=\frac{\left(9.3 \times 10^{-5}\right)\left[\mathrm{CO}_{3}{ }^{2-}\right]}{9.3 \times 10^{-5}} \\
& {\left[\mathrm{CO}_{3}{ }^{2-}\right]=K_{\mathrm{a} 2}=5.6 \times 10^{-11} \mathrm{M}}
\end{aligned}
$$

(In general, for a solution of a weak diprotic acid $H_{2} A,\left[A^{2-}\right]=K_{a 2}$.)
(2) $\left[\mathrm{OH}^{-}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]}=\frac{1.0 \times 10^{-14}}{9.3 \times 10^{-5}}=1.1 \times 10^{-10} \mathrm{M}$

The second dissociation of $\mathrm{H}_{2} \mathrm{CO}_{3}$ produces a negligible amount of $\mathrm{H}_{3} \mathrm{O}^{+}$compared with the $\mathrm{H}_{3} \mathrm{O}^{+}$obtained from the first dissociation. Of the $9.3 \times 10^{-5} \mathrm{~mol} / \mathrm{L}$ of $\mathrm{HCO}_{3}{ }^{-}$produced by the first dissociation, only $5.6 \times 10^{-11} \mathrm{~mol} / \mathrm{L}$ dissociates to form $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{CO}_{3}{ }^{2-}$.

Step 8. $\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=-\log \left(9.3 \times 10^{-5}\right)=4.03$
$\checkmark$ Ballpark Check When the value of $x$ can be neglected compared with the initial concentration of the acid (Step 5), the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$equals the square root of the product of $K_{\mathrm{a} 1}$ and the initial concentration of the acid. In this problem, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$is the square root of approximately $\left(4 \times 10^{-7}\right)\left(2 \times 10^{-2}\right)$, or about $10^{-4} \mathrm{M}$. Therefore, the $\mathrm{pH} \approx 4$, in agreement with the solution.

- PROBLEM 15.17 Calculate the pH and the concentrations of all species present in $0.10 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{3}$. Values of $K_{\mathrm{a}}$ are in Table 15.3.
- PROBLEM 15.18 Calculate the pH and the concentrations of all species present in $0.50 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$. (Hint: All the $\mathrm{H}_{2} \mathrm{SO}_{4}$ molecules dissociate to give $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{HSO}_{4}^{-}$ ions, but less than $100 \%$ of the resulting $\mathrm{HSO}_{4}^{-}$ions dissociate to give $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{SO}_{4}{ }^{2-}$ ions. The second dissociation step takes place in the presence of $\mathrm{H}_{3} \mathrm{O}^{+}$from the first step.) Values of $K_{\mathrm{a}}$ are given in Table 15.3.


### 15.12 Equilibria in Solutions of Weak Bases

Weak bases, such as ammonia, accept a proton from water to give the conjugate acid of the base and $\mathrm{OH}^{-}$ions:

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

The equilibrium reaction of any base $B$ with water is characterized by an equilibrium equation similar in form to that for the dissociation of a weak acid. The equilibrium constant $K_{\mathbf{b}}$ is called the base-dissociation constant:

$$
\begin{aligned}
& \mathrm{B}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{BH}^{+}(a q)+\mathrm{OH}^{-}(a q) \\
& K_{\mathrm{b}}=\frac{\left[\mathrm{BH}^{+}\right]\left[\mathrm{OH}^{-}\right]}{[\mathrm{B}]}
\end{aligned}
$$




A Many over-the-counter drugs contain salts formed from amines and hydrochloric acid.

As usual, $\left[\mathrm{H}_{2} \mathrm{O}\right]$ is omitted from the equilibrium constant expression. Table 15.4 lists some typical weak bases and gives their $K_{\mathrm{b}}$ values. (The term base-protonation constant might be a more descriptive name for $K_{\mathrm{b}}$, but the term base-dissociation constant is still widely used.)

| TABLE 15.4 | $K_{\mathrm{b}}$ Values for Some Weak Bases and $K_{\mathrm{a}}$ Values for Their Conjugate Acids |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Base | Formula, B | $K_{\text {b }}$ | Conjugate Acid, $\mathrm{BH}^{+}$ | $K_{\text {a }}$ |
| Ammonia | $\mathrm{NH}_{3}$ | $1.8 \times 10^{-5}$ | $\mathrm{NH}_{4}{ }^{+}$ | $5.6 \times 10^{-10}$ |
| Aniline | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}$ | $4.3 \times 10^{-10}$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{3}{ }^{+}$ | $2.3 \times 10^{-5}$ |
| Dimethylamine | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$ | $5.4 \times 10^{-4}$ | $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}_{2}{ }^{+}$ | $1.9 \times 10^{-11}$ |
| Hydrazine | $\mathrm{N}_{2} \mathrm{H}_{4}$ | $8.9 \times 10^{-7}$ | $\mathrm{N}_{2} \mathrm{H}_{5}{ }^{+}$ | $1.1 \times 10^{-8}$ |
| Hydroxylamine | $\mathrm{NH}_{2} \mathrm{OH}$ | $9.1 \times 10^{-9}$ | $\mathrm{NH}_{3} \mathrm{OH}^{+}$ | $1.1 \times 10^{-6}$ |
| Methylamine | $\mathrm{CH}_{3} \mathrm{NH}_{2}$ | $3.7 \times 10^{-4}$ | $\mathrm{CH}_{3} \mathrm{NH}_{3}{ }^{+}$ | $2.7 \times 10^{-11}$ |

Many weak bases are organic compounds called amines, derivatives of ammonia in which one or more hydrogen atoms are replaced by another group. Methylamine, for example, is an organic amine responsible for the odor of rotting fish.


Methylamine


Dimethylamine

The basicity of an amine is due to the lone pair of electrons on the nitrogen atom, which can be used for bonding to a proton.

Equilibria in solutions of weak bases are treated by the same procedure used for solving problems involving weak acids. Worked Example 15.12 illustrates the procedure.

## Worked Example 15.12

Codeine $\left(\mathrm{C}_{18} \mathrm{H}_{21} \mathrm{NO}_{3}\right)$, a drug used in painkillers and cough medicines, is a naturally occurring amine that has $K_{\mathrm{b}}=1.6 \times 10^{-6}$. Calculate the pH and the concentrations of all species present in a 0.0012 M solution of codeine.

## Strategy

Use the procedure outlined in Figure 15.7.

## Solution

Step 1. Let's use Cod as an abbreviation for codeine and $\mathrm{CodH}^{+}$for its conjugate acid. The species present initially are Cod (base) and $\mathrm{H}_{2} \mathrm{O}$ (acid or base).


Codeine

Step 2. There are two possible proton-transfer reactions:

$$
\begin{aligned}
\mathrm{Cod}(a q)+\mathrm{H}_{2} \mathrm{O}(l) & \rightleftharpoons \mathrm{CodH}^{+}(a q)+\mathrm{OH}^{-}(a q)
\end{aligned} \quad K_{\mathrm{b}}=1.6 \times 10^{-6}, ~=\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) \quad K_{\mathrm{w}}=1.0 \times 10^{-14}
$$

Step 3. Since Cod is a much stronger base than $\mathrm{H}_{2} \mathrm{O}\left(K_{\mathrm{b}} \gg K_{\mathrm{w}}\right)$, the principal reaction involves protonation of codeine.

## Step 4.

| Principal reaction: | $\mathbf{C o d}(\boldsymbol{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{C o d H}^{+}(\boldsymbol{a q})+\mathbf{O H}^{-}(\boldsymbol{a q})$ |  |  |
| :--- | :--- | :---: | :---: |
| Initial conc $(\mathrm{M})$ | 0.0012 | 0 | $\sim 0$ |
| Change $(M)$ | $-x$ | $+x$ | $+x$ |
| Equilibrium conc $(M)$ | $0.0012-x$ | $x$ | $x$ |

Step 5. The value of $x$ is obtained from the equilibrium equation:

$$
K_{\mathrm{b}}=1.6 \times 10^{-6}=\frac{\left[\mathrm{CodH}^{+}\right]\left[\mathrm{OH}^{-}\right]}{[\mathrm{Cod}]}=\frac{(x)(x)}{(0.0012-x)}
$$

Assuming that $(0.0012-x) \approx 0.0012$,

$$
\begin{aligned}
& x^{2}=\left(1.6 \times 10^{-6}\right)(0.0012) \\
& x=4.4 \times 10^{-5} \quad \text { Approximation }(0.0012-x) \approx 0.0012 \text { is justified. }
\end{aligned}
$$

Step 6. The big concentrations are

$$
\begin{aligned}
& {\left[\mathrm{CodH}^{+}\right]=\left[\mathrm{OH}^{-}\right]=x=4.4 \times 10^{-5} \mathrm{M}} \\
& {[\mathrm{Cod}]=0.0012-x=0.0012-0.000044=0.0012 \mathrm{M}}
\end{aligned}
$$

Step 7. The small concentration is obtained from the subsidiary equilibrium, the dissociation of water:

$$
\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{4.4 \times 10^{-5}}=2.3 \times 10^{-10} \mathrm{M}
$$

Step 8. $\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=-\log \left(2.3 \times 10^{-10}\right)=9.64$
The pH is greater than 7, as expected for a solution of a weak base.
$\checkmark$ Ballpark Check Because x is negligible compared with the initial concentration of codeine (Step 5), the $\left[\mathrm{OH}^{-}\right.$] equals the square root of the product of $K_{\mathrm{b}}$ and the initial concentration of codeine. Therefore, $\left[\mathrm{OH}^{-}\right]$equals the square root of approximately $\left(16 \times 10^{-7}\right)\left(1 \times 10^{-3}\right)$, or about $4 \times 10^{-5}$. Since the $\left[\mathrm{OH}^{-}\right]$is between $10^{-5} \mathrm{M}$ and $10^{-4} \mathrm{M}$, the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] is between $10^{-9} \mathrm{M}$ and $10^{-10} \mathrm{M}$, and so the pH is between 9 and 10. The ballpark check and the solution agree.

- PROBLEM 15.19 Calculate the pH and the concentrations of all species present in $0.40 \mathrm{M} \mathrm{NH}_{3}\left(K_{\mathrm{b}}=1.8 \times 10^{-5}\right)$.
- PROBLEM 15.20 Strychnine $\left(\mathrm{C}_{21} \mathrm{H}_{22} \mathrm{~N}_{2} \mathrm{O}_{2}\right)$, a deadly poison used for killing rodents, is a weak base having $K_{\mathrm{b}}=1.8 \times 10^{-6}$. Calculate the pH of a saturated solution of strychnine ( $16 \mathrm{mg} / 100 \mathrm{~mL}$ ).


### 15.13 Relation Between $K_{a}$ and $K_{b}$

Strychnine
We've seen in previous sections that the strength of an acid can be expressed by its $K_{a}$, and the strength of a base can be expressed by its $K_{b}$. For a conjugate acid-base pair, the two equilibrium constants are related in a simple way that makes it possible to calculate either one from the other. Let's consider the conjugate acid-base pair $\mathrm{NH}_{4}{ }^{+}$and $\mathrm{NH}_{3}$, for example, where $K_{\mathrm{a}}$ refers to proton transfer from the acid
$\mathrm{NH}_{4}{ }^{+}$to water, and $K_{\mathrm{b}}$ refers to proton transfer from water to the base $\mathrm{NH}_{3}$. The sum of the two reactions is simply the dissociation of water:

$$
\begin{aligned}
\mathrm{NH}_{4}^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NH}_{3}(a q) & K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{NH}_{3}\right]}{\left[\mathrm{NH}_{4}^{+}\right]}=5.6 \times 10^{-10} \\
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q) & K_{\mathrm{b}}=\frac{\left[\mathrm{NH}_{4}^{+}\right]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{NH}_{3}\right]}=1.8 \times 10^{-5} \\
\hline \text { Net: } \quad 2 \mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) &
\end{aligned}
$$

The equilibrium constant for the net reaction equals the product of the equilibrium constants for the reactions added:
Caution students that the equilibrium constants are multiplied, and they should not confuse this principle with Hess's Law for which enthalpy changes are added.

Relationship Between $K_{\mathrm{a}}$ and $K_{\mathrm{b}}$ activity

$$
\begin{aligned}
K_{\mathrm{a}} \times K_{\mathrm{b}} & =\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{NH}_{3}\right]}{\left[\mathrm{NH}_{4}{ }^{+}\right]} \times \frac{\left[\mathrm{NH}_{4}^{+}\right]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{NH}_{3}\right]}=\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]=K_{\mathrm{w}} \\
& =\left(5.6 \times 10^{-10}\right)\left(1.8 \times 10^{-5}\right)=1.0 \times 10^{-14}
\end{aligned}
$$

What we've shown in this particular case is true in general. Whenever chemical equations for two (or more) reactions are added to get the equation for a net reaction, the equilibrium constant for the net reaction equals the product of the equilibrium constants for the individual reactions:

$$
K_{\mathrm{net}}=K_{1} \times K_{2} \times \ldots
$$

For any conjugate acid-base pair, the product of the acid-dissociation constant for the acid and the base-dissociation constant for the base always equals the ionproduct constant for water:

$$
K_{\mathrm{a}} \times K_{\mathrm{b}}=K_{\mathrm{w}}
$$

As the strength of an acid increases (larger $K_{\mathrm{a}}$ ), the strength of its conjugate base decreases (smaller $K_{\mathrm{b}}$ ) because the product $K_{\mathrm{a}} \times K_{\mathrm{b}}$ remains constant at $1.0 \times 10^{-14}$. This inverse relationship between the strength of an acid and the strength of its conjugate base was illustrated qualitatively in Table 15.1.

Compilations of equilibrium constants, such as Appendix C, generally list either $K_{\mathrm{a}}$ or $K_{\mathrm{b}}$, but not both, because $K_{\mathrm{a}}$ is easily calculated from $K_{\mathrm{b}}$ and vice versa:

$$
K_{\mathrm{a}}=\frac{K_{\mathrm{w}}}{K_{\mathrm{b}}} \quad \text { and } \quad K_{\mathrm{b}}=\frac{K_{\mathrm{w}}}{K_{\mathrm{a}}}
$$

## Worked Example 15.13

(a) $K_{\mathrm{b}}$ for trimethylamine is $6.5 \times 10^{-5}$. Calculate $K_{\mathrm{a}}$ for the trimethylammonium ion, $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{NH}^{+}$.
(b) $K_{\mathrm{a}}$ for HCN is $4.9 \times 10^{-10}$. Calculate $K_{\mathrm{b}}$ for $\mathrm{CN}^{-}$.

## Strategy

To calculate $K_{\mathrm{a}}$ from $K_{\mathrm{b}}$ (or vice versa) use the equation $K_{\mathrm{a}}=K_{\mathrm{w}} / K_{\mathrm{b}}$, or $K_{\mathrm{b}}=K_{\mathrm{w}} / K_{\mathrm{a}}$.

## SOLUTION

(a) $K_{\mathrm{a}}$ for $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{NH}^{+}$is the equilibrium constant for the acid-dissociation reaction

$$
\left(\mathrm{CH}_{3}\right)_{3} \mathrm{NH}^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N}(a q)
$$

Because $K_{\mathrm{a}}=K_{\mathrm{w}} / K_{\mathrm{b}}$, we can find $K_{\mathrm{a}}$ for $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{NH}^{+}$from $K_{\mathrm{b}}$ for its conjugate base $\left(\mathrm{CH}_{3}\right)_{3} \mathrm{~N}$ :

$$
K_{\mathrm{a}}=\frac{K_{\mathrm{w}}}{K_{\mathrm{b}}}=\frac{1.0 \times 10^{-14}}{6.5 \times 10^{-5}}=1.5 \times 10^{-10}
$$

(b) $K_{\mathrm{b}}$ for $\mathrm{CN}^{-}$is the equilibrium constant for the base-protonation reaction

$$
\mathrm{CN}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HCN}(a q)+\mathrm{OH}^{-}(a q)
$$

Because $K_{\mathrm{b}}=K_{\mathrm{w}} / K_{\mathrm{a}}$, we can find $K_{\mathrm{b}}$ for $\mathrm{CN}^{-}$from $K_{\mathrm{a}}$ for its conjugate acid HCN:

$$
K_{\mathrm{b}}=\frac{K_{\mathrm{w}}}{K_{\mathrm{a}}}=\frac{1.0 \times 10^{-14}}{4.9 \times 10^{-10}}=2.0 \times 10^{-5}
$$

## - PROBLEM 15.21

(a) Piperidine $\left(\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{~N}\right)$ is an amine found in black pepper. Find $K_{\mathrm{b}}$ for piperidine in Appendix C, and then calculate $K_{\mathrm{a}}$ for the $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{NH}^{+}$cation.
(b) Find $K_{\mathrm{a}}$ for HOCl in Appendix C, and then calculate $K_{\mathrm{b}}$ for $\mathrm{OCl}^{-}$.

### 15.14 Acid-Base Properties of Salts

When an acid neutralizes a base (Section 4.1), an ionic compound called a salt is formed. Salt solutions can be neutral, acidic, or basic, depending on the acid-base properties of the constituent cations and anions (Figure 15.9). As a general rule, salts formed by reaction of a strong acid with a strong base are neutral, salts formed by reaction of a strong acid with a weak base are acidic, and salts formed by reaction of a weak acid with a strong base are basic. It's as if the influence of the stronger partner dominates:

$$
\begin{gathered}
\text { Strong acid + Strong base } \longrightarrow \text { Neutral solution } \\
\text { Strong Acid + Weak base } \longrightarrow \text { Acidic solution } \\
\text { Weak acid + Strong base } \longrightarrow \text { Basic solution }
\end{gathered}
$$



## Salts That Yield Neutral Solutions

Salts such as NaCl that are derived from a strong base $(\mathrm{NaOH})$ and a strong acid $(\mathrm{HCl})$ yield neutral solutions because neither the cation nor the anion reacts appreciably with water to produce $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$ions. As the conjugate base of a strong acid, $\mathrm{Cl}^{-}$has no tendency to make the solution basic by picking up a proton from water. As the cation of a strong base, the hydrated $\mathrm{Na}^{+}$ion has only a negligible tendency to make the solution acidic by transferring a proton to a solvent water molecule.


Piperidine


4 FIGURE 15.9 Some 0.10 M aqueous salt solutions (left to right): $\mathrm{NaCl}, \mathrm{NH}_{4} \mathrm{Cl}, \mathrm{AlCl}_{3}$, NaCN , and $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$. A few drops of universal indicator (Figure 15.5a) have been added to each solution. The color of the indicator shows that the NaCl solution is neutral, the $\mathrm{NH}_{4} \mathrm{Cl}$ and $\mathrm{AlCl}_{3}$ solutions are acidic, and the NaCN and $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ solutions are basic.

Bassam Z. Shakhashiri,
"Hydrolysis: Acidic and Basic Properties of Salts," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 103-108.

The following ions do not react appreciably with water to produce either $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$ions:

- Cations from strong bases:

Alkali metal cations of group $1 \mathrm{~A}\left(\mathrm{Li}^{+}, \mathrm{Na}^{+}, \mathrm{K}^{+}\right)$
Alkaline earth cations of group $2 \mathrm{~A}\left(\mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}, \mathrm{Ba}^{2+}\right)$, except for $\mathrm{Be}^{2+}$

- Anions from strong monoprotic acids:

$$
\mathrm{Cl}^{-}, \mathrm{Br}^{-}, \mathrm{I}^{-}, \mathrm{NO}_{3}^{-} \text {, and } \mathrm{ClO}_{4}^{-}
$$

Salts that contain only these ions give neutral solutions in pure water ( $\mathrm{pH}=7$ ). (Usually, water is slightly acidic because of dissolved atmospheric $\mathrm{CO}_{2}$. To prepare a neutral salt solution, you would first have to remove the dissolved $\mathrm{CO}_{2}$.)

## Salts That Yield Acidic Solutions

Salts such as $\mathrm{NH}_{4} \mathrm{Cl}$ that are derived from a weak base $\left(\mathrm{NH}_{3}\right)$ and a strong acid $(\mathrm{HCl})$ produce acidic solutions. In such a case, the anion is neither an acid nor a base, but the cation is a weak acid:

$$
\mathrm{NH}_{4}^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NH}_{3}(a q)
$$

Related ammonium salts derived from amines, such as $\left[\mathrm{CH}_{3} \mathrm{NH}_{3}\right] \mathrm{Cl}$, [ $\left.\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}_{2}\right] \mathrm{Cl}$, and $\left[\left(\mathrm{CH}_{3}\right)_{3} \mathrm{NH}\right] \mathrm{Cl}$, also give acidic solutions because they too have cations with at least one dissociable proton. The pH of a solution that contains an acidic cation can be calculated by the standard procedure outlined in Figure 15.7. For a $0.10 \mathrm{M} \mathrm{NH}_{4} \mathrm{Cl}$ solution, the pH is 5.12 . Although the reaction of a cation or anion of a salt with water to produce $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$ions is sometimes called a salt hydrolysis reaction, there is no fundamental difference between a salt hydrolysis reaction and any other Brønsted-Lowry acid-base reaction.

Another type of acidic cation is a hydrated cation of a small, highly charged metal ion, such as $\mathrm{Al}^{3+}$. In aqueous solution, the $\mathrm{Al}^{3+}$ ion bonds to six water molecules to give the hydrated cation $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$. All metal ions exist in aqueous solution as hydrated cations, but their acidity varies greatly depending on the charge and size of the unhydrated metal ion. Because of the high (3+) charge on the $\mathrm{Al}^{3+}$ ion, electrons in the $\mathrm{O}-\mathrm{H}$ bonds of the bound water molecules are attracted toward the $\mathrm{Al}^{3+}$ ion. The attraction is strong because the $\mathrm{Al}^{3+}$ ion is small and the electrons in the $\mathrm{O}-\mathrm{H}$ bonds are relatively close to the center of positive charge. As a result, electron density shifts from the $\mathrm{O}-\mathrm{H}$ bonds toward the $\mathrm{Al}^{3+}$ ion, thus weakening the $\mathrm{O}-\mathrm{H}$ bonds and increasing their polarity, which in


The acid-dissociation constant for $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}, \mathrm{K}_{\mathrm{a}}=1.4 \times 10^{-5}$, is much larger than $K_{\mathrm{w}}=1.0 \times 10^{-14}$, which means that the water molecules in the
hydrated cation are much stronger proton donors than are free solvent water molecules. In fact, the acid strength of $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ is comparable to that of acetic acid, which has $K_{a}=1.8 \times 10^{-5}$. In general, the acidity of hydrated main-group cations increases from left to right in the periodic table as the metal ion charge increases and the metal ion size decreases $\left(\mathrm{Li}^{+}<\mathrm{Be}^{2+} ; \mathrm{Na}^{+}<\mathrm{Mg}^{2+}<\mathrm{Al}^{3+}\right)$. Transition metal cations, such as $\mathrm{Zn}^{2+}, \mathrm{Cr}^{3+}$, and $\mathrm{Fe}^{3+}$, also give acidic solutions; their $K_{a}$ values are listed in Table C. 2 of Appendix C.

## Worked Example 15.14

Calculate the pH of a 0.10 M solution of $\mathrm{AlCl}_{3} ; \mathrm{K}_{\mathrm{a}}$ for $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ is $1.4 \times 10^{-5}$.

## Strategy

Because this problem is similar to others done earlier, we'll abbreviate the procedure in Figure 15.7.

## Solution

Steps 1-4. The species present initially are $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ (acid), $\mathrm{Cl}^{-}$(inert), and $\mathrm{H}_{2} \mathrm{O}$ (acid or base). Because $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ is a much stronger acid than water $\left(K_{\mathrm{a}} \gg K_{\mathrm{w}}\right)$, the principal reaction is dissociation of $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$

| Principal reaction: | $\mathbf{A l}\left(\mathbf{H}_{\mathbf{2}} \mathbf{O}\right)_{\mathbf{6}}{ }^{\mathbf{3 +}}(\boldsymbol{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H}_{\mathbf{3}} \mathbf{O}^{+}(\boldsymbol{a q})+\mathbf{A l ( \mathbf { H } _ { \mathbf { 2 } } \mathbf { O } ) _ { \mathbf { 5 } } ( \mathbf { O H } ) ^ { \mathbf { 2 + } } ( \boldsymbol { a q } )}$ |  |
| :--- | :--- | :--- |
| Equilibrium conc $(\mathrm{M})$ | $0.10-x$ | $x$ |

Step 5. The value of $x$ is obtained from the equilibrium equation:

$$
\begin{aligned}
K_{\mathrm{a}} & =1.4 \times 10^{-5}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{5}(\mathrm{OH})^{2+}\right]}{\left[\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}\right]}=\frac{(x)(x)}{(0.10-x)} \approx \frac{x^{2}}{0.10} \\
x & =\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.2 \times 10^{-3} \mathrm{M}
\end{aligned}
$$

Step 8. $\mathrm{pH}=-\log \left(1.2 \times 10^{-3}\right)=2.92$
Thus, $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ is a much stronger acid than $\mathrm{NH}_{4}{ }^{+}$, which agrees with the colors of the indicator in Figure 15.9.

- PROBLEM 15.22 Predict whether the following salt solutions are neutral or acidic, and calculate the pH of each:
(a) $0.25 \mathrm{M} \mathrm{NH}_{4} \mathrm{Br}$
(b) $0.40 \mathrm{M} \mathrm{ZnCl}_{2} ; K_{\mathrm{a}}$ for $\mathrm{Zn}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}$ is $2.5 \times 10^{-10}$.


## Salts That Yield Basic Solutions

Salts such as NaCN that are derived from a strong base $(\mathrm{NaOH})$ and a weak acid (HCN) yield basic solutions. In this case, the cation is neither an acid nor a base, but the anion is a weak base:

$$
\mathrm{CN}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HCN}(a q)+\mathrm{OH}^{-}(a q)
$$

Other anions that exhibit basic properties are listed in Table 15.1 and include $\mathrm{NO}_{2}^{-}, \mathrm{F}^{-}, \mathrm{CH}_{3} \mathrm{CO}_{2}^{-}$, and $\mathrm{CO}_{3}{ }^{2-}$. The pH of a basic salt solution can be calculated by the standard procedure, as shown in Worked Example 15.15.

## Worked Example 15.15

Calculate the pH of a 0.10 M solution of NaCN ; $K_{\mathrm{a}}$ for HCN is $4.9 \times 10^{-10}$.

## Strategy

Use the procedure summarized in Figure 15.7.

## Solution

Step 1. The species present initially are $\mathrm{Na}^{+}$(inert), $\mathrm{CN}^{-}$(base), and $\mathrm{H}_{2} \mathrm{O}$ (acid or base).

Step 2. There are two possible proton-transfer reactions:

$$
\begin{aligned}
& \mathrm{CN}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HCN}(a q)+\mathrm{OH}^{-}(a q) \\
& K_{\mathrm{b}} \\
& \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q)
\end{aligned} K_{\mathrm{w}}
$$

Step 3. As shown in Worked Example 15.13b, $K_{\mathrm{b}}=K_{\mathrm{w}} /\left(K_{\mathrm{a}}\right.$ for HCN $)=2.0 \times 10^{-5}$. Because $K_{\mathrm{b}} \gg K_{\mathrm{w}}, \mathrm{CN}^{-}$is a stronger base than $\mathrm{H}_{2} \mathrm{O}$, and the principal reaction is proton transfer from $\mathrm{H}_{2} \mathrm{O}$ to $\mathrm{CN}^{-}$.

Step 4.

| Principal reaction: | $\mathbf{C N}^{-}(\boldsymbol{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H C N}(\boldsymbol{a q})+\mathbf{O H}^{-}(\boldsymbol{a q})$ |  |  |
| :--- | :--- | :---: | :---: |
| Equilibrium conc $(\mathrm{M})$ | $0.10-x$ | $x$ | $x$ |

Step 5. The value of $x$ is obtained from the equilibrium equation:

$$
\begin{aligned}
K_{\mathrm{b}}=2.0 \times 10^{-5} & =\frac{\left[{\mathrm{HCN}]\left[\mathrm{OH}^{-}\right]}_{\left[\mathrm{CN}^{-}\right]}\right]}{=} \frac{(x)(x)}{(0.10-x)} \approx \frac{x^{2}}{0.10} \\
x & =\left[\mathrm{OH}^{-}\right]=1.4 \times 10^{-3} \mathrm{M}
\end{aligned}
$$

## Step 7.

$$
\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{1.4 \times 10^{-3}}=7.1 \times 10^{-12}
$$

Step 8. $\mathrm{pH}=-\log \left(7.1 \times 10^{-12}\right)=11.15$
The solution is basic, which agrees with the color of the indicator in Figure 15.9.
PROBLEM 15.23 Calculate the pH of $0.20 \mathrm{M} \mathrm{NaNO}_{2} ; K_{\mathrm{a}}$ for $\mathrm{HNO}_{2}$ is $4.6 \times 10^{-4}$.

## Salts That Contain Acidic Cations and Basic Anions

Finally, let's look at a salt such as $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ in which both the cation and the anion can undergo proton-transfer reactions. Because $\mathrm{NH}_{4}{ }^{+}$is a weak acid and $\mathrm{CO}_{3}{ }^{2-}$ is a weak base, the pH of an $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ solution depends on the relative acid strength of the cation and base strength of the anion:

$$
\begin{array}{ll}
\mathrm{NH}_{4}^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NH}_{3}(a q) & \text { Acid strength }\left(K_{\mathrm{a}}\right) \\
\mathrm{CO}_{3}{ }^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HCO}_{3}^{-}(a q)+\mathrm{OH}^{-}(a q) & \text { Base strength }\left(K_{\mathrm{b}}\right)
\end{array}
$$

We can distinguish three possible cases:

- $K_{\mathrm{a}}>K_{\mathrm{b}}$ : If $K_{\mathrm{a}}$ for the cation is greater than $K_{\mathrm{b}}$ for the anion, the solution will contain an excess of $\mathrm{H}_{3} \mathrm{O}^{+}$ions $(\mathrm{pH}<7)$.
- $K_{\mathrm{a}}<K_{\mathrm{b}}$ : If $K_{\mathrm{a}}$ for the cation is less than $K_{\mathrm{b}}$ for the anion, the solution will contain an excess of $\mathrm{OH}^{-}$ions ( $\mathrm{pH}>7$ ).
- $K_{\mathrm{a}} \approx K_{\mathrm{b}}$ : If $K_{\mathrm{a}}$ for the cation and $K_{\mathrm{b}}$ for the anion are comparable, the solution will contain approximately equal concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$ions ( $\mathrm{pH} \approx 7$ ).

To determine whether an $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ solution is acidic, basic, or neutral, let's work out the values of $K_{\mathrm{a}}$ for $\mathrm{NH}_{4}{ }^{+}$and $K_{\mathrm{b}}$ for $\mathrm{CO}_{3}{ }^{2-}$ :

$$
\begin{gathered}
K_{\mathrm{a}} \text { for } \mathrm{NH}_{4}^{+}=\frac{K_{\mathrm{w}}}{K_{\mathrm{b}} \text { for } \mathrm{NH}_{3}}=\frac{1.0 \times 10^{-14}}{1.8 \times 10^{-5}}=5.6 \times 10^{-10} \\
K_{\mathrm{b}} \text { for } \mathrm{CO}_{3}^{2-}=\frac{K_{\mathrm{w}}}{K_{\mathrm{a}} \text { for } \mathrm{HCO}_{3}^{-}}=\frac{K_{\mathrm{w}}}{K_{a 2} \text { for } \mathrm{H}_{2} \mathrm{CO}_{3}}=\frac{1.0 \times 10^{-14}}{5.6 \times 10^{-11}}=1.8 \times 10^{-4}
\end{gathered}
$$

Because $K_{\mathrm{a}}<K_{\mathrm{b}}$, the solution is basic ( $\mathrm{pH}>7$ ), in accord with the color of the indicator in Figure 15.9.

A summary of the acid-base properties of salts is given in Table 15.5.

TABLE 15.5 Acid-Base Properties of Salts

| Type of Salt | Examples | Ions That React with Water | pH of Solution |
| :---: | :---: | :---: | :---: |
| Cation from strong base; anion from strong acid | $\begin{aligned} & \mathrm{NaCl}, \mathrm{KNO}_{3}, \\ & \mathrm{BaI}_{2} \end{aligned}$ | None | $\sim 7$ |
| Cation from weak base; anion from strong acid | $\mathrm{NH}_{4} \mathrm{Cl}, \mathrm{NH}_{4} \mathrm{NO}_{3}$, $\left[\left(\mathrm{CH}_{3}\right)_{3} \mathrm{NH}\right] \mathrm{Cl}$ | Cation | $<7$ |
| Small, highly charged cation; anion from strong acid | $\mathrm{AlCl}_{3}, \mathrm{Cr}\left(\mathrm{NO}_{3}\right)_{3}$, <br> $\mathrm{Fe}\left(\mathrm{ClO}_{4}\right)_{3}$ | Hydrated cation | $<7$ |
| Cation from strong base; anion from weak acid | $\begin{aligned} & \mathrm{NaCN}, \mathrm{KF}, \\ & \mathrm{Na}_{2} \mathrm{CO}_{3} \end{aligned}$ | Anion | $>7$ |
| Cation from weak base; anion from weak acid | $\mathrm{NH}_{4} \mathrm{CN}, \mathrm{NH}_{4} \mathrm{~F}$, <br> $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ | Cation and anion | $\begin{aligned} & <7 \text { if } K_{\mathrm{a}}>K_{\mathrm{b}} \\ & >7 \text { if } K_{\mathrm{a}}<K_{\mathrm{b}} \\ & \sim 7 \text { if } K_{\mathrm{a}} \approx K_{\mathrm{b}} \end{aligned}$ |

- PROBLEM 15.24 Calculate $K_{\mathrm{a}}$ for the cation, and $K_{\mathrm{b}}$ for the anion in an aqueous $\mathrm{NH}_{4} \mathrm{CN}$ solution. Is the solution acidic, basic, or neutral?
- PROBLEM 15.25 Classify each of the following salt solutions as acidic, basic, or neutral:
(a) KBr
(b) $\mathrm{NaNO}_{2}$
(c) $\mathrm{NH}_{4} \mathrm{Br}$
(d) $\mathrm{ZnCl}_{2}$
(e) $\mathrm{NH}_{4} \mathrm{~F}$


### 15.15 Factors That Affect Acid Strength

Why is one acid stronger than another? Although a complete analysis of the factors that determine the strength of an acid is complex, the extent of dissociation of an acid HA is often determined by the strength and polarity of the $\mathrm{H}-\mathrm{A}$ bond. The strength of the $\mathrm{H}-\mathrm{A}$ bond, as we saw in Section 8.11 , is the enthalpy required to dissociate HA into an H atom and an A atom. The polarity of the $\mathrm{H}-\mathrm{A}$ bond increases with an increase in the electronegativity of $A$ and is related to the ease of electron transfer from an H atom to an A atom to give an $\mathrm{H}^{+}$cation and an $\mathrm{A}^{-}$ anion. In general, the weaker the $\mathrm{H}-\mathrm{A}$ bond, the stronger the acid, and the more polar the $\mathrm{H}-\mathrm{A}$ bond, the stronger the acid.

Bassam Z. Shakhashiri, "Effect
of Molecular Structure on the Strength of Organic Acids in Aqueous Solutions," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 158-161.

Let's look first at the hydrohalic acids $\mathrm{HF}, \mathrm{HCl}, \mathrm{HBr}$, and HI. Electrostatic potential maps (Section 7.4) show that all these molecules are polar, with the halogen atom being electron rich (red) and the H atom being electron poor (blue).


The variation in polarity in this series, however, is much less important than the variation in bond strength, which decreases markedly from $567 \mathrm{~kJ} / \mathrm{mol}$ for HF to $299 \mathrm{~kJ} / \mathrm{mol}$ for HI.

In general, for binary acids of elements in the same group of the periodic table, the $\mathrm{H}-\mathrm{A}$ bond strength is the most important determinant of acidity. The $\mathrm{H}-\mathrm{A}$ bond strength generally decreases with increasing size of element A down a group, so acidity increases. For $\mathrm{HA}(\mathrm{A}=\mathrm{F}, \mathrm{Cl}, \mathrm{Br}$, or I$)$, for example, the size of A increases from F to I, so bond strength decreases and acidity increases from HF to HI. Hydrofluoric acid is a weak acid $\left(K_{\mathrm{a}}=3.5 \times 10^{-4}\right)$, whereas $\mathrm{HCl}, \mathrm{HBr}$, and HI are strong acids.


As a further example of this effect, $\mathrm{H}_{2} \mathrm{~S}\left(\mathrm{~K}_{\mathrm{a} 1}=1.0 \times 10^{-7}\right)$ is a stronger acid than $\mathrm{H}_{2} \mathrm{O}$.

For binary acids of elements in the same row of the periodic table, changes in the $\mathrm{H}-\mathrm{A}$ bond strength are smaller, and the polarity of the $\mathrm{H}-\mathrm{A}$ bond is the most important determinant of acid strength. The strengths of binary acids of the second-row elements, for example, increase as the electronegativity of A increases:


As the electrostatic potential maps show, the $\mathrm{C}-\mathrm{H}$ bond is relatively nonpolar, and methane has no tendency to dissociate in water into $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{CH}_{3}{ }^{-}$ions. The $\mathrm{N}-\mathrm{H}$ bond is more polar, but dissociation of $\mathrm{NH}_{3}$ into $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{NH}_{2}^{-}$ions is still negligibly small. Water and hydrofluoric acid, however, are increasingly stronger acids.

Periodic trends in the strength of binary acids are summarized in Figure 15.10.


Oxoacids, such as $\mathrm{H}_{2} \mathrm{CO}_{3}, \mathrm{HNO}_{3}, \mathrm{H}_{2} \mathrm{SO}_{4}$, and HClO , have the general formula $\mathrm{H}_{n} \mathrm{YO}_{m}$, where Y is a nonmetallic atom, such as $\mathrm{C}, \mathrm{N}, \mathrm{S}$, or Cl , and $n$ and $m$ are integers. The atom Y is always bonded to one or more hydroxyl $(\mathrm{OH})$ groups and can be bonded, in addition, to one or more oxygen atoms:


Carbonic acid


Sulfuric acid


Nitric acid


Hypochlorous acid

FIGURE 15.10 The acid strength of a binary acid HA increases from left to right in the periodic table, with increasing electronegativity of A , and from top to bottom, with decreasing $\mathrm{H}-\mathrm{A}$ bond strength.

Because dissociation of an oxoacid requires breaking an $\mathrm{O}-\mathrm{H}$ bond, any factor that weakens the $\mathrm{O}-\mathrm{H}$ bond or increases its polarity increases the strength of the acid. Two such factors are the electronegativity of $Y$ and the oxidation number of $Y$ in the general reaction


- For oxoacids that contain the same number of OH groups and the same number of O atoms, acid strength increases as the electronegativity of Y increases. For example, the acid strength of the hypohalous acids $\mathrm{HOY}(\mathrm{Y}=\mathrm{Cl}, \mathrm{Br}$, or I$)$ increases as the electronegativity of the halogen increases:

|  | Acid strength |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
|  | $\mathrm{H}-\mathrm{O}-\mathrm{I}$ | $<$ | $\mathrm{H}-\mathrm{O}-\mathrm{Br}$ |  |$<\quad \mathrm{H}-\mathrm{O}-\mathrm{Cl}$,

As the halogen becomes more electronegative, an increasing amount of electron density shifts from the $\mathrm{O}-\mathrm{H}$ bond toward the halogen, thus weakening the $\mathrm{O}-\mathrm{H}$ bond and increasing its polarity. As a result, the proton is more easily transferred to a solvent water molecule, and so the acid strength increases.

- For oxoacids that contain the same atom $Y$ but different numbers of oxygen atoms, acid strength increases as the oxidation number of $Y$ increases. The oxidation number of Y increases, in turn, as the number of oxygen atoms increases. This effect is illustrated by the oxoacids of chlorine:

Acid strength


As the number of O atoms in $\mathrm{HClO}_{m}$ increases, an increasing amount of electron density shifts from the Cl atom toward the more electronegative O atoms. The amount of positive charge on the Cl atom therefore increases as its oxidation number increases. The increased positive charge on the Cl atom in turn attracts an increasing amount of electron density from the $\mathrm{O}-\mathrm{H}$ bond, thus weakening the $\mathrm{O}-\mathrm{H}$ bond and increasing its polarity. [Recall that this same charge effect was discussed in Section 15.14 for $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$.] As a result, the proton is more easily transferred to a solvent water molecule.

Another factor that affects the acid strength of oxoacids is the relative stability of the corresponding oxoanions. The $\mathrm{ClO}_{m}{ }^{-}$anion becomes more stable as the number of O atoms increases in the series $\mathrm{ClO}^{-}<\mathrm{ClO}_{2}^{-}<\mathrm{ClO}_{3}^{-}<\mathrm{ClO}_{4}^{-}$ because a larger number of electronegative O atoms can better accommodate the anion's negative charge. As the stability of the anion increases, the corresponding acid has a greater tendency to dissociate. The increase in acid strength with increasing number of O atoms is further illustrated by the oxoacids of sulfur: $\mathrm{H}_{2} \mathrm{SO}_{4}$ is a stronger acid than $\mathrm{H}_{2} \mathrm{SO}_{3}$.

- PROBLEM 15.26 Identify the stronger acid in each of the following pairs:
(a) $\mathrm{H}_{2} \mathrm{~S}$ or $\mathrm{H}_{2} \mathrm{Se}$
(b) HI or $\mathrm{H}_{2} \mathrm{Te}$
(c) $\mathrm{HNO}_{2}$ or $\mathrm{HNO}_{3}$
(d) $\mathrm{H}_{2} \mathrm{SO}_{3}$ or $\mathrm{H}_{2} \mathrm{SeO}_{3}$


### 15.16 Lewis Acids and Bases

Lewis Acid-Base
Theory movie

In 1923, the same year in which Brønsted and Lowry defined acids and bases in terms of their proton donor/acceptor properties, the American chemist G. N. Lewis proposed an even more general concept of acids and bases. Lewis noticed
that when a base accepts a proton, it shares a lone pair of electrons with the proton to form a new covalent bond. Using ammonia as an example, the reaction can be written in the following format, in which the curved arrow represents donation of the nitrogen lone pair to form a bond with $\mathrm{H}^{+}$:


In this reaction, the proton behaves as an electron-pair acceptor, and the ammonia molecule behaves as an electron-pair donor. Consequently, the Lewis definition of acids and bases states that a Lewis acid is an electron-pair acceptor, and a Lewis base is an electron-pair donor.

## Lewis acid An electron-pair acceptor <br> Lewis base An electron-pair donor

Since all proton acceptors have an unshared pair of electrons, and since all electron-pair donors can accept a proton, the Lewis and the Brønsted-Lowry definitions of a base are simply different ways of looking at the same property. All Lewis bases are Brønsted-Lowry bases, and all Brønsted-Lowry bases are Lewis bases. The Lewis definition of an acid, however, is considerably more general than the Brønsted-Lowry definition. Lewis acids include not only $\mathrm{H}^{+}$but also other cations and neutral molecules having vacant valence orbitals that can accept a share in a pair of electrons donated by a Lewis base.

Common examples of cationic Lewis acids are metal ions, such as $\mathrm{Al}^{3+}$ and $\mathrm{Cu}^{2+}$. Hydration of the $\mathrm{Al}^{3+}$ ion, for example, is a Lewis acid-base reaction in which each of six $\mathrm{H}_{2} \mathrm{O}$ molecules donates a pair of electrons to $\mathrm{Al}^{3+}$ to form the hydrated cation $\mathrm{Al}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ :


Lewis acid Lewis base
Similarly, the reaction of $\mathrm{Cu}^{2+}$ ion with ammonia is a Lewis acid-base reaction in which each of four $\mathrm{NH}_{3}$ molecules donates a pair of electrons to $\mathrm{Cu}^{2+}$ to form the deep blue ion $\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$ (Figure 15.11).


Examples of neutral Lewis acids are halides of group 3A elements, such as $\mathrm{BF}_{3}$. Boron trifluoride, a colorless gas, is an excellent Lewis acid because the boron atom in the trigonal planar $\mathrm{BF}_{3}$ molecule is surrounded by only six valence electrons (Figure 15.12). The boron atom uses three $s p^{2}$ hybrid orbitals to bond to the three F atoms and has a vacant $2 p$ valence orbital that can accept a share in a pair of electrons from a Lewis base, such as $\mathrm{NH}_{3}$. The Lewis acid and base sites are evident in electrostatic potential maps, which show the electron poor B atom (blue) and the electron rich N atom (red). In the product, called an acid-base adduct, the boron atom has acquired a stable octet of electrons.

Additional examples of neutral Lewis acids are oxides of nonmetals, such as $\mathrm{CO}_{2}, \mathrm{SO}_{2}$, and $\mathrm{SO}_{3}$. The reaction of $\mathrm{SO}_{3}$ with water, for example, can be viewed as Educ., Vol. 61, 1984, 93-100.

FIGURE 15.11 Addition of aqueous ammonia to a solution of the light blue $\mathrm{Cu}^{2+}(a q)$ ion (left) gives a light blue precipitate of $\mathrm{Cu}(\mathrm{OH})_{2}$ (center). Addition of an excess of ammonia yields the deep blue ion $\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$ (right).

FIGURE 15.12 The reaction of the Lewis acid $\mathrm{BF}_{3}$ with the Lewis base $\mathrm{NH}_{3}$. The electrostatic potential maps show that the $B$ atom is electron poor (blue) and the N atom is electron rich (red). The geometry about boron changes from trigonal planar in $\mathrm{BF}_{3}$ to tetrahedral in the adduct. Both boron and nitrogen use $s p^{3}$ hybrid orbitals in the adduct.
$\mathrm{BF}_{3} \mathrm{NH}_{3} 3 \mathrm{D}$ model

a Lewis acid-base reaction in which $\mathrm{SO}_{3}$ accepts a lone pair of electrons from a water molecule:


Because the $\mathrm{S}=\mathrm{O}$ bond is polar, with a partial positive charge ( $\delta+$ ) on the less electronegative S atom, the S atom attracts an electron pair from $\mathrm{H}_{2} \mathrm{O}$. Formation of a bond from the water O atom to the S atom in the first step is helped along by the shift of a shared pair of electrons to oxygen. In the second step, a proton shifts from one oxygen atom to another, yielding sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$.

Worked Example 15.16
For each of the following reactions, identify the Lewis acid and the Lewis base.
(a) $\mathrm{CO}_{2}+\mathrm{OH}^{-} \rightarrow \mathrm{HCO}_{3}^{-}$
(b) $\mathrm{B}(\mathrm{OH})_{3}+\mathrm{OH}^{-} \rightarrow \mathrm{B}(\mathrm{OH})_{4}^{-}$
(c) $6 \mathrm{CN}^{-}+\mathrm{Fe}^{3+} \rightarrow \mathrm{Fe}(\mathrm{CN})_{6}{ }^{3-}$

## Strategy

To identify the Lewis acid and the Lewis base, see which molecule or ion can accept an electron pair and which can donate an electron pair.

## Solution

(a) The carbon atom of $\mathrm{O}=\mathrm{C}=\mathrm{O}$ bears a partial positive charge $(\delta+)$ because oxygen is more electronegative than carbon. Therefore, the carbon atom attracts an electron pair from $\mathrm{OH}^{-}$. Formation of a covalent bond from $\mathrm{OH}^{-}$to $\mathrm{CO}_{2}$ is helped along by a shift of a shared electron pair to oxygen:


The Lewis acid (electron-pair acceptor) is $\mathrm{CO}_{2}$; the Lewis base (electron-pair donor) is $\mathrm{OH}^{-}$.
(b) The Lewis acid is boric acid, $\mathrm{B}(\mathrm{OH})_{3}$, a weak acid and mild antiseptic used in eyewash. The boron atom in $\mathrm{B}(\mathrm{OH})_{3}$ has a vacant valence orbital and completes its octet by accepting a pair of electrons from the Lewis base, $\mathrm{OH}^{-}$.
(c) The Lewis acid is $\mathrm{Fe}^{3+}$, and the Lewis base is $\mathrm{CN}^{-}$.

PROBLEM 15.27 For each of the following reactions, identify the Lewis acid and the Lewis base.
(a) $\mathrm{AlCl}_{3}+\mathrm{Cl}^{-} \rightarrow \mathrm{AlCl}_{4}^{-}$
(b) $2 \mathrm{NH}_{3}+\mathrm{Ag}^{+} \rightarrow \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$
(c) $\mathrm{SO}_{2}+\mathrm{OH}^{-} \rightarrow \mathrm{HSO}_{3}^{-}$
(d) $6 \mathrm{H}_{2} \mathrm{O}+\mathrm{Cr}^{3+} \rightarrow \mathrm{Cr}\left(\mathrm{OH}_{2}\right)_{6}{ }^{3+}$

- KEY CONCEPT PROBLEM 15.28 For the following Lewis acid-base reaction, draw electron dot structures for the reactants and products, and use the curved arrow notation to represent the donation of a lone pair of electrons from the Lewis base to the Lewis acid.

$$
\mathrm{BeCl}_{2}+2 \mathrm{Cl}^{-} \longrightarrow \mathrm{BeCl}_{4}^{2-}
$$

## Interlude <br> Acid Rain

TThe problem of acid rain has emerged as one of the more important environmental issues of recent times. Both the causes and the effects of acid rain are well understood. The problem is what to do about it. As the water that has evaporated from oceans and lakes condenses into raindrops, it dissolves small quantities of gases from the atmosphere. Under normal conditions, rain is slightly acidic, with a pH close to 5.6 , because of dissolved $\mathrm{CO}_{2}$. In recent decades, however, the acidity of rainwater in many industrialized areas of the world has increased by a factor of over 100, to a pH between 3 and 3.5.

The primary cause of acid rain is industrial and automotive pollution. Each year in industrialized countries, large power plants and smelters that burn sulfur-containing fossil fuels pour millions of tons of sulfur dioxide $\left(\mathrm{SO}_{2}\right)$ gas into the atmosphere, where some is oxidized by air to produce sulfur trioxide $\left(\mathrm{SO}_{3}\right)$. Sulfur oxides then dissolve in rain to form dilute sulfurous acid and sulfuric acid:

$$
\begin{array}{ll}
\mathrm{SO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{H}_{2} \mathrm{SO}_{3}(a q) & \text { Sulfurous acid } \\
\mathrm{SO}_{3}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{H}_{2} \mathrm{SO}_{4}(a q) & \text { Sulfuric acid }
\end{array}
$$

Nitrogen oxides produced by the high-temperature reaction of $\mathrm{N}_{2}$ with $\mathrm{O}_{2}$ in coal-burning plants and in automobile engines further contribute to the problem. Nitrogen dioxide $\left(\mathrm{NO}_{2}\right)$ dissolves in water to form dilute nitric acid $\left(\mathrm{HNO}_{3}\right)$ and nitric oxide ( NO ):

$$
3 \mathrm{NO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{HNO}_{3}(a q)+\mathrm{NO}(g)
$$

Oxides of both sulfur and nitrogen have always been present in the atmosphere, produced by such natural sources as volcanoes and lightning bolts, but their amounts have increased dramatically over the last century because of industrialization.

Many processes in nature require such a fine pH balance that they are dramatically upset by the shift that has occurred in the pH of rain. Thousands of lakes in the Adirondack region of upper New York State and in southeastern Canada have become so acidic that all fish life has disappeared. Massive tree die-offs have occurred throughout central and eastern Europe as acid rain has lowered the pH of the soil and leached nutrients from leaves. Countless marble statues have been slowly dissolved away as their calcium carbonate has been attacked by acid rain.

$$
\mathrm{CaCO}_{3}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Ca}^{2+}(a q)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CO}_{2}(g)
$$

Fortunately, acidic emissions from automobiles and power plants have been greatly reduced in recent years. Nitrogen oxide emissions have been lowered by equipping automobiles with catalytic converters (Section 12.13), which catalyze the decomposition of nitrogen oxides to $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$. Sulfur dioxide emissions from power plants have been reduced by scrubbing combustion products before they are emitted from plant smoke stacks. In this process an aqueous suspension of lime $(\mathrm{CaO})$ is added to the combustion chamber and the stack. The lime reacts with $\mathrm{SO}_{2}$ to give calcium sulfite $\left(\mathrm{CaSO}_{3}\right)$ :

$$
\mathrm{CaO}(s)+\mathrm{SO}_{2}(g) \longrightarrow \mathrm{CaSO}_{3}(s)
$$

Unfortunately, scrubbers are expensive, and the $\mathrm{CaSO}_{3}$, which has no commercial uses, must be disposed of in land fills. Much more work on methods to control acidic emissions remains to be done because the problem will grow more serious as sources of low-sulfur coal are exhausted and power plants are forced to rely on more abundant sources of highsulfur coal.

- PROBLEM 15.29 The reaction of lime $(\mathrm{CaO})$ with $\mathrm{SO}_{2}$ in the scrubber of a power plant can be regarded as a Lewis acid-base reaction. Explain.

PROBLEM 15.30 What is the pH of 1.00 L of rainwater that has dissolved 5.47 mg of $\mathrm{NO}_{2}$ ? Assume that all of the $\mathrm{NO}_{2}$ has reacted with water to give nitric acid.


A A marble statue is being slowly dissolved by reaction of calcium carbonate with acid rain (top). A researcher examines tree branches damaged by acid rain on Mount Mitchell in North Carolina (bottom).

## Summary

According to the Arrhenius theory, acids (HA) are substances that dissociate in water to produce $\mathrm{H}^{+}(a q)$. Bases (MOH) are substances that dissociate to yield $\mathrm{OH}^{-}(a q)$. The more general Brønsted-Lowry theory defines an acid as a proton donor, a base as a proton acceptor, and an acid-base reaction as a proton-transfer reaction. Examples of Brønsted-Lowry acids are $\mathrm{HCl}, \mathrm{NH}_{4}{ }^{+}$, and $\mathrm{HSO}_{4}^{-}$; examples of Brønsted-Lowry bases are $\mathrm{OH}^{-}, \mathrm{F}^{-}$, and $\mathrm{NH}_{3}$.

A strong acid HA is nearly $100 \%$ dissociated, whereas a weak acid HA is only partially dissociated, existing as an equilibrium mixture of $\mathrm{HA}, \mathrm{H}_{3} \mathrm{O}^{+}$, and $\mathrm{A}^{-}$:

$$
\mathrm{HA}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{A}^{-}(a q)
$$

The strength of an acid (HA) and the strength of its conjugate base ( $\mathrm{A}^{-}$) are inversely related. The $\mathrm{H}_{3} \mathrm{O}^{+}$ion, a hydrated proton, is called the hydronium ion.

Water, which can act both as an acid and as a base, undergoes the dissociation reaction $\mathrm{H}_{2} \mathrm{O}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{OH}^{-}$. In pure water at $25^{\circ} \mathrm{C},\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$. The ion-product constant for water, $K_{w}$, is given by $K_{w}=$ $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-14}$. The acidity of an aqueous solution is expressed on the $\mathbf{p H}$ scale, where $\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$. Acidic solutions have $\mathrm{pH}<7$, basic solutions have $\mathrm{pH}>7$, and neutral solutions have $\mathrm{pH}=7$. The pH of a solution can be determined using an acid-base indicator or a pH meter. The extent of dissociation of a weak acid HA is measured by the aciddissociation constant, $K_{\mathrm{a}}$ :

$$
K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}
$$

Polyprotic acids contain more than one dissociable proton and dissociate in a stepwise manner. Because the stepwise dis-
sociation constants decrease in the order $K_{\mathrm{a} 1} \gg K_{\mathrm{a} 2} \gg K_{\mathrm{a} 3}$, nearly all the $\mathrm{H}_{3} \mathrm{O}^{+}$in a polyprotic acid solution comes from the first dissociation step.

The extent of dissociation of a weak base B is measured by the base-dissociation constant, $K_{\mathbf{b}}$ :

$$
\begin{aligned}
& \mathrm{B}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{BH}^{+}(a q)+\mathrm{OH}^{-}(a q) \\
& K_{\mathrm{b}}=\frac{\left[\mathrm{BH}^{+}\right]\left[\mathrm{OH}^{-}\right]}{[\mathrm{B}]}
\end{aligned}
$$

Examples of weak bases are $\mathrm{NH}_{3}$ and derivatives of $\mathrm{NH}_{3}$ called amines. For any conjugate acid-base pair, $\left(K_{\mathrm{a}}\right.$ for the acid $) \times\left(K_{\mathrm{b}}\right.$ for the base $)=K_{\mathrm{w}}$.

Aqueous solutions of salts can be neutral, acidic, or basic, depending on the acid-base properties of the constituent ions. Group 1A and 2A cations (except $\mathrm{Be}^{2+}$ ) and anions that are conjugate bases of strong acids, such as $\mathrm{Cl}^{-}$, do not react appreciably with water to produce $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$ions. Cations that are conjugate acids of weak bases, such as $\mathrm{NH}_{4}{ }^{+}$, and hydrated cations of small, highly charged metal ions, such as $\mathrm{Al}^{3+}$, yield acidic solutions, whereas anions that are conjugate bases of weak acids, such as $\mathrm{CN}^{-}$, yield basic solutions.

The acid strength of a binary acid HA increases with decreasing strength of the $\mathrm{H}-\mathrm{A}$ bond and increasing polarity of the $\mathrm{H}-\mathrm{A}$ bond. The acid strength of an oxoacid, $\mathrm{H}_{n} \mathrm{YO}_{m}(\mathrm{Y}=\mathrm{C}, \mathrm{N}, \mathrm{S}, \mathrm{Cl})$, increases with increasing electronegativity and increasing oxidation number of the atom Y .

A Lewis acid is an electron-pair acceptor and a Lewis base is an electron-pair donor. Lewis acids include not only $\mathrm{H}^{+}$but also other cations and neutral molecules that can accept a share in a pair of electrons from a Lewis base. Examples of Lewis acids are $\mathrm{Al}^{3+}, \mathrm{Cu}^{2+}, \mathrm{BF}_{3}, \mathrm{SO}_{3}$, and $\mathrm{CO}_{2}$.

## Key Words

acid-base indicator 622
acid-dissociation
constant ( $K_{\mathrm{a}}$ ) 626
Arrhenius acid 612
Arrhenius base 612
base-dissociation constant ( $K_{\mathbf{b}}$ ) 635
Bronsted-Lowry acid 612

Bronsted-Lowry base 612
Bronsted-Lowry theory 612
conjugate acid 613 conjugate acid-base pair 613
conjugate base 613
diprotic acid 623
dissociation of water 618
hydronium ion, $\mathrm{H}_{3} \mathrm{O}^{+}$ 613
ion-product constant for water $\left(\boldsymbol{K}_{\mathbf{w}}\right) \quad 619$
Lewis acid 647
Lewis base 647
monoprotic acid 623
percent dissociation 632
pH 620
polyprotic acid 633
principal reaction 628
strong acid 615
subsidiary reaction 628
weak acid 616

## Key Concept Summary



## Understanding Key Concepts

Problems 15.1-15.30 appear within the chapter.
15.31 For each of the following reactions, identify the BrønstedLowry acids and bases:
-


15.32 The following pictures represent aqueous solutions of three acids HA ( $\mathrm{A}=\mathrm{X}, \mathrm{Y}$, or Z ); water molecules have

- been omitted for clarity:

(a) What is the conjugate base of each acid?
(b) Arrange the three acids in order of increasing acid strength.
(c) Which acid, if any, is a strong acid?
(d) Which acid has the smallest value of $K_{\mathrm{a}}$ ?
(e) What is the percent dissociation in the solution of HZ?
15.33 Which of the following pictures represents a solution of a weak diprotic acid $\mathrm{H}_{2} \mathrm{~A}$ ? (Water molecules are omitted for clarity.) Which pictures represent an impossible situation? Explain.

15.34 Which of the following pictures best represents an aqueous solution of sulfuric acid? Explain. (Water molecules have been omitted for clarity.)
$=\mathrm{H}_{2} \mathrm{SO}_{4}$

(a)
- $=\mathrm{H}_{3} \mathrm{O}^{+}$
(
$=\mathrm{HSO}_{4}^{-}$$=\mathrm{SO}_{4}{ }^{2-}$
(b)

(c)
15.35 The following pictures represent aqueous solutions of three acids HA ( $\mathrm{A}=\mathrm{X}, \mathrm{Y}$, or Z ); water molecules have been omitted for clarity:

(a) Which conjugate base $\left(\mathrm{A}^{-}=\mathrm{X}^{-}, \mathrm{Y}^{-}\right.$, or $\left.\mathrm{Z}^{-}\right)$has the largest value of $K_{\mathrm{b}}$ ?
(b) Which $\mathrm{A}^{-}$ion is the weakest base?
15.36 The following pictures represent solutions of three salts $\mathrm{NaA}\left(\mathrm{A}^{-}=\mathrm{X}^{-}, \mathrm{Y}^{-}\right.$, or $\left.\mathrm{Z}^{-}\right)$; water molecules and $\mathrm{Na}^{+}$ ions have been omitted for clarity:


NaX

D $=\mathrm{HA}$


NaY

(a) Arrange the three $\mathrm{A}^{-}$anions in order of increasing base strength.
(b) Which $\mathrm{A}^{-}$anion has the strongest conjugate acid?
(c) Why does each box contain the same number of HA molecules and $\mathrm{OH}^{-}$anions?
15.37 Locate sulfur, selenium, chlorine, and bromine in the periodic table:

(a) Which binary acid $\left(\mathrm{H}_{2} \mathrm{~S}, \mathrm{H}_{2} \mathrm{Se}, \mathrm{HCl}\right.$, or HBr$)$ is the strongest? Which is the weakest? Explain.
(b) Which oxoacid $\left(\mathrm{H}_{2} \mathrm{SO}_{3}, \mathrm{H}_{2} \mathrm{SeO}_{3}, \mathrm{HClO}_{3}\right.$, or $\left.\mathrm{HBrO}_{3}\right)$ is the strongest? Which is the weakest? Explain.
15.38 Look at the electron-dot structures of the following molecules and ions:





(a) Which of these molecules and ions can behave as a Brønsted-Lowry acid? Which can behave as a Brønsted-Lowry base?
(b) Which can behave as a Lewis acid? Which can behave as a Lewis base?
15.39 The reaction of $\mathrm{PCl}_{4}^{+}$with $\mathrm{Cl}^{-}$is a Lewis acid-base reaction. Draw electron-dot structures for the reactants and products, and use the curved arrow notation (Section 15.16) to represent the donation of a lone pair of electrons from the Lewis base to the Lewis acid.


## Additional Problems

## Acid-Base Concepts

15.40 Give three examples of molecules or ions that are Brønsted-Lowry bases but not Arrhenius bases.
15.41 Give an example of an anion that can behave both as a Brønsted-Lowry acid and as a Brønsted-Lowry base.
15.42 Give the formula for the conjugate base of each of the following Brønsted-Lowry acids:
(a) $\mathrm{HSO}_{4}^{-}$
(b) $\mathrm{H}_{2} \mathrm{SO}_{3}$
(c) $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$
(d) $\mathrm{NH}_{4}{ }^{+}$
(e) $\mathrm{H}_{2} \mathrm{O}$
(f) $\mathrm{NH}_{3}$
15.43 Give the formula for the conjugate acid of each of the following Brønsted-Lowry bases:
(a) $\mathrm{SO}_{3}{ }^{2-}$
(b) $\mathrm{H}_{2} \mathrm{O}$
(c) $\mathrm{CH}_{3} \mathrm{NH}_{2}$
(d) $\mathrm{OH}^{-}$
(e) $\mathrm{HCO}_{3}^{-}$
(f) $\mathrm{H}^{-}$
15.44 For each of the following reactions, identify the Brønsted-Lowry acids and bases and the conjugate acid-base pairs:
(a) $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{NH}_{3}(a q) \rightleftharpoons$

$$
\mathrm{NH}_{4}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)
$$

(b) $\mathrm{CO}_{3}{ }^{2-}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q) \rightleftharpoons$

$$
\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{HCO}_{3}^{-}(a q)
$$

(c) $\mathrm{HSO}_{3}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons$

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{SO}_{3}^{2-}(a q)
$$

(d) $\mathrm{HSO}_{3}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons$

$$
\mathrm{H}_{2} \mathrm{SO}_{3}(a q)+\mathrm{OH}^{-}(a q)
$$

15.45 For each of the following reactions, identify the Brøn-sted-Lowry acids and bases and the conjugate acid-base pairs:
(a) $\mathrm{CN}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{OH}^{-}(a q)+\mathrm{HCN}(a q)$
(b) $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons$

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{HPO}_{4}{ }^{2-}(a q)
$$

(c) $\mathrm{HPO}_{4}{ }^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \underset{\mathrm{OH}^{-}(a q)+\mathrm{H}_{2} \mathrm{PO}_{4}^{-}(a q)}{\rightleftharpoons}$
(d) $\mathrm{NH}_{4}^{+}(a q)+\mathrm{NO}_{2}^{-}(a q) \rightleftharpoons \mathrm{HNO}_{2}(a q)+\mathrm{NH}_{3}(a q)$
15.46 Which of the following species behave as strong acids or as strong bases in aqueous solution? See Table 15.1 to check your answers.
(a) $\mathrm{HNO}_{2}$
(b) $\mathrm{HNO}_{3}$
(c) $\mathrm{NH}_{4}^{+}$
(d) $\mathrm{Cl}^{-}$
(e) $\mathrm{H}^{-}$
(f) $\mathrm{O}^{2-}$
(g) $\mathrm{H}_{2} \mathrm{SO}_{4}$
15.47 Which acid in each of the following pairs has the stronger conjugate base? See Table 15.1 for help with parts (c) and (d).
(a) $\mathrm{H}_{2} \mathrm{CO}_{3}$ or $\mathrm{H}_{2} \mathrm{SO}_{4}$
(b) HCl or HF
(c) HF or $\mathrm{NH}_{4}^{+}$
(d) HCN or $\mathrm{HSO}_{4}^{-}$
15.48 If you mix equal concentrations of reactants and products, which of the following reactions proceed to the right and which proceed to the left? Use the data in Table 15.1, and remember that the stronger base gets the proton.
(a) $\mathrm{H}_{2} \mathrm{CO}_{3}(a q)+\mathrm{HSO}_{4}^{-}(a q) \rightleftharpoons$

$$
\mathrm{H}_{2} \mathrm{SO}_{4}(a q)+\mathrm{HCO}_{3}^{-}(a q)
$$

(b) $\mathrm{HF}(a q)+\mathrm{Cl}^{-}(a q) \rightleftharpoons \mathrm{HCl}(a q)+\mathrm{F}^{-}(a q)$
(c) $\mathrm{HF}(a q)+\mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{NH}_{4}{ }^{+}(a q)+\mathrm{F}^{-}(a q)$
(d) $\mathrm{HSO}_{4}^{-}(a q)+\mathrm{CN}^{-}(a q) \rightleftharpoons$

$$
\mathrm{HCN}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q)
$$

15.49 If you mix equal concentrations of reactants and products, which of the following reactions proceed to the right and which proceed to the left? Use the data in Table 15.1.
(a) $\mathrm{HSO}_{4}^{-}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q) \rightleftharpoons$

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q)
$$

(b) $\mathrm{HNO}_{2}(a q)+\mathrm{NO}_{3}^{-}(a q) \rightleftharpoons$

$$
\mathrm{HNO}_{3}(a q)+\mathrm{NO}_{2}^{-}(a q)
$$

(c) $\mathrm{HCO}_{3}{ }^{-}(a q)+\mathrm{F}^{-}(a q) \rightleftharpoons \mathrm{HF}(a q)+\mathrm{CO}_{3}{ }^{2-}(a q)$
(d) $\mathrm{NH}_{4}{ }^{+}(a q)+\mathrm{CN}^{-}(a q) \rightleftharpoons \mathrm{HCN}(a q)+\mathrm{NH}_{3}(a q)$

## Dissociation of Water; pH

15.50 For each of the following solutions, calculate $\left[\mathrm{OH}^{-}\right]$ from $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$, or $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$from $\left[\mathrm{OH}^{-}\right.$]. Classify each solution as acidic, basic, or neutral.
(a) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=3.4 \times 10^{-9} \mathrm{M}$
(b) $\left[\mathrm{OH}^{-}\right]=0.010 \mathrm{M}$
(c) $\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-10} \mathrm{M}$
(d) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.0 \times 10^{-7} \mathrm{M}$
(e) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=8.6 \times 10^{-5} \mathrm{M}$
15.51 For each of the following solutions, calculate $\left[\mathrm{OH}^{-}\right]$ from $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$], or $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] from $\left[\mathrm{OH}^{-}\right]$. Classify each solution as acidic, basic, or neutral.
(a) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=2.5 \times 10^{-4} \mathrm{M}$
(b) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=2.0 \mathrm{M}$
(c) $\left[\mathrm{OH}^{-}\right]=5.6 \times 10^{-9} \mathrm{M}$
(d) $\left[\mathrm{OH}^{-}\right]=1.5 \times 10^{-3} \mathrm{M}$
(e) $\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$
15.52 Calculate the pH to the correct number of significant figures for solutions with the following concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$:
(a) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=2.0 \times 10^{-5} \mathrm{M}$
(b) $\left[\mathrm{OH}^{-}\right]=4 \times 10^{-3} \mathrm{M}$
(c) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=3.56 \times 10^{-9} \mathrm{M}$
(d) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=10^{-3} \mathrm{M}$
(e) $\left[\mathrm{OH}^{-}\right]=12 \mathrm{M}$
15.53 What is the pH to the correct number of significant figures for solutions with the following concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$?
(a) $\left[\mathrm{OH}^{-}\right]=7.6 \times 10^{-3} \mathrm{M}$
(b) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=10^{-8} \mathrm{M}$
(c) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=5.0 \mathrm{M}$
(d) $\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$
(e) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=2.18 \times 10^{-10} \mathrm{M}$
15.54 Calculate the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration to the correct number of significant figures for solutions with the following pH values:
(a) 4.1
(b) 10.82
(c) 0.00
(d) 14.25
(e) -1.0
(f) 5.238
15.55 What is the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration to the correct number of significant figures for solutions with the following pH values?
(a) 9.0
(b) 7.00
(c) -0.3
(d) 15.18
(e) 2.63
(f) 10.756
15.56 What is the change in pH if $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$changes by each of the following factors?
(a) 1000
(b) $1.0 \times 10^{5}$
(c) 2.0
15.57 By what factor must $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$change to produce the following pH changes?
(a) 1.0 unit
(b) 10.00 units
(c) 0.10 unit
15.58 Given the following approximate concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$for various biological fluids, calculate the pH .
(a) Gastric juice, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=10^{-2} \mathrm{M}$
(b) Spinal fluid, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=4 \times 10^{-8} \mathrm{M}$
(c) Bile, $\left[\mathrm{OH}^{-}\right]=8 \times 10^{-8} \mathrm{M}$
(d) Urine, $\left[\mathrm{OH}^{-}\right]=6 \times 10^{-10} \mathrm{M}$ to $2 \times 10^{-6} \mathrm{M}$
(e) Human milk, $\left[\mathrm{OH}^{-}\right]=2 \times 10^{-7} \mathrm{M}$
15.59 What is the pH of each of the following foods?
(a) Sauerkraut, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=3 \times 10^{-4} \mathrm{M}$
(b) Eggs, $\left[\mathrm{OH}^{-}\right]=6 \times 10^{-7} \mathrm{M}$
(c) Apples, $\left[\mathrm{OH}^{-}\right]=10^{-11} \mathrm{M}$
(d) Limes, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.3 \times 10^{-2} \mathrm{M}$
(e) Potatoes, $\left[\mathrm{OH}^{-}\right]=6.3 \times 10^{-9} \mathrm{M}$

## Strong Acids and Strong Bases

15.60 Calculate the pH of each of the following solutions:
(a) 0.40 M HBr
(b) $3.7 \times 10^{-4} \mathrm{M} \mathrm{KOH}$
(c) $5.0 \times 10^{-5} \mathrm{M} \mathrm{Ca}(\mathrm{OH})_{2}$
15.61 What is the pH of each of the following solutions?
(a) $1.8 \mathrm{M} \mathrm{HClO}_{4}$
(b) 1.2 M LiOH
(c) $5.3 \times 10^{-3} \mathrm{M} \mathrm{Ba}(\mathrm{OH})_{2}$
15.62 Calculate the pH of solutions prepared by:
(a) dissolving 4.8 g of lithium hydroxide in water to give 250 mL of solution
(b) dissolving 0.93 g of hydrogen chloride in water to give 0.40 L of solution
(c) diluting 50.0 mL of 0.10 M HCl to a volume of 1.00 L
(d) mixing 100.0 mL of $2.0 \times 10^{-3} \mathrm{M} \mathrm{HCl}$ and 400.0 mL of $1.0 \times 10^{-3} \mathrm{M} \mathrm{HClO}_{4}$ (Assume that volumes are additive.)
15.63 Calculate the pH of solutions prepared by:
(a) dissolving 0.20 g of sodium oxide in water to give 100.0 mL of solution
(b) dissolving 1.26 g of pure nitric acid in water to give 0.500 L of solution
(c) diluting 40.0 mL of $0.075 \mathrm{M} \mathrm{Ba}(\mathrm{OH})_{2}$ to a volume of 300.0 mL
(d) mixing equal volumes of 0.20 M HCl and 0.50 M $\mathrm{HNO}_{3}$ (Assume that volumes are additive.)

## Weak Acids

15.64 Write a balanced net ionic equation and the corresponding equilibrium equation for dissociation of the following weak acids:
(a) Chlorous acid, $\mathrm{HClO}_{2}$
(b) Hypobromous acid, HOBr
(c) Formic acid, $\mathrm{HCO}_{2} \mathrm{H}$
15.65 Write a balanced net ionic equation and the corresponding equilibrium equation for dissociation of the following weak acids:
(a) Hydrazoic acid, $\mathrm{HN}_{3}$
(b) Benzoic acid, $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}$
(c) Hydrogen peroxide, $\mathrm{H}_{2} \mathrm{O}_{2}$
15.66 Using values of $K_{\mathrm{a}}$ in Appendix C, arrange the following acids in order of (a) increasing acid strength, and (b) decreasing percent dissociation: $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OH}, \mathrm{HNO}_{3}$, $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}, \mathrm{HOCl}$. Also estimate $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$in a 1.0 M solution of each acid.
15.67 Use the values of $K_{\mathrm{a}}$ in Appendix C to arrange the following acids in order of (a) increasing acid strength, and (b) decreasing percent dissociation: $\mathrm{HCO}_{2} \mathrm{H}, \mathrm{HCN}$, $\mathrm{HClO}_{4}, \mathrm{HOBr}$. Also estimate $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$in a 1.0 M solution of each acid.
15.68 The pH of 0.040 M hypobromous acid ( HOBr ) is 5.05. Set up the equilibrium equation for dissociation of HOBr , and calculate the value of the acid-dissociation constant.
15.69 Lactic acid $\left(\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}_{3}\right)$, which occurs in sour milk and foods such as sauerkraut, is a weak monoprotic acid. The pH of a 0.10 M solution of lactic acid is 2.43 . What is the value of $K_{\mathrm{a}}$ for lactic acid?
15.70 Phenol $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OH}\right)$ is a weak acid used as a general disinfectant and in the manufacture of plastics. Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{O}^{-}, \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OH}\right.$, and $\left.\mathrm{OH}^{-}\right)$in a 0.10 M solution of phenol ( $K_{\mathrm{a}}=1.3 \times 10^{-10}$ ). Also calculate the percent dissociation.
15.71 Formic acid $\left(\mathrm{HCO}_{2} \mathrm{H}\right)$ is an organic acid secreted by ants and stinging nettles. Calculate the pH and the concentrations of all species present $\left(\mathrm{HCO}_{2} \mathrm{H}, \mathrm{HCO}_{2}{ }^{-}\right.$, $\mathrm{H}_{3} \mathrm{O}^{+}$, and $\left.\mathrm{OH}^{-}\right)$in $0.20 \mathrm{M} \mathrm{HCO}_{2} \mathrm{H}\left(K_{\mathrm{a}}=1.8 \times 10^{-4}\right)$. Also calculate the percent dissociation.
15.72 Calculate the pH and the percent dissociation in 1.5 M $\mathrm{HNO}_{2}\left(K_{\mathrm{a}}=4.5 \times 10^{-4}\right)$.
15.73 A typical aspirin tablet contains 324 mg of aspirin (acetylsalicylic acid, $\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}_{4}$ ), a monoprotic acid having $K_{\mathrm{a}}=3.0 \times 10^{-4}$. If you dissolve two aspirin tablets in a 300 mL glass of water, what is the pH of the solution and the percent dissociation?

## Polyprotic Acids

15.74 Write balanced net ionic equations and the corresponding equilibrium equations for the stepwise dissociation of the diprotic acid $\mathrm{H}_{2} \mathrm{SeO}_{4}$.
15.75 Write balanced net ionic equations and the corresponding equilibrium equations for the stepwise dissociation of the triprotic acid $\mathrm{H}_{3} \mathrm{PO}_{4}$.
15.76 Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{2} \mathrm{CO}_{3}, \mathrm{HCO}_{3}^{-}, \mathrm{CO}_{3}{ }^{2-}, \mathrm{H}_{3} \mathrm{O}^{+}\right.$, and $\left.\mathrm{OH}^{-}\right)$in $0.010 \mathrm{M} \mathrm{H}_{2} \mathrm{CO}_{3}\left(K_{\mathrm{a} 1}=4.3 \times 10^{-7} ; K_{\mathrm{a} 2}=5.6 \times 10^{-11}\right)$.
15.77 Calculate the pH and the concentrations of $\mathrm{H}_{2} \mathrm{SO}_{3}, \mathrm{HSO}_{3}{ }^{-}, \mathrm{SO}_{3}{ }^{2-}, \mathrm{H}_{3} \mathrm{O}^{+}$, and $\mathrm{OH}^{-}$in 0.025 M $\mathrm{H}_{2} \mathrm{SO}_{3}\left(K_{\mathrm{a} 1}=1.5 \times 10^{-2} ; K_{\mathrm{a} 2}=6.3 \times 10^{-8}\right)$.
15.78 Oxalic acid $\left(\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$ is a diprotic acid that occurs in plants such as rhubarb and spinach. Calculate the pH and the concentration of $\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}$ ions in 0.20 M $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\left(K_{\mathrm{a} 1}=5.9 \times 10^{-2} ; K_{\mathrm{a} 2}=6.4 \times 10^{-5}\right)$.
15.79 Calculate the concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{SO}_{4}{ }^{2-}$ in a solution prepared by mixing equal volumes of 0.2 M HCl and $0.6 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}\left(K_{\mathrm{a} 2}\right.$ for $\mathrm{H}_{2} \mathrm{SO}_{4}$ is $1.2 \times 10^{-2}$ ).

## Weak Bases; Relation Between $\boldsymbol{K}_{\mathrm{a}}$ and $\boldsymbol{K}_{\mathrm{b}}$

15.80 Write a balanced net ionic equation and the corresponding equilibrium equation for reaction of the following weak bases with water:
(a) Dimethylamine, $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{NH}$
(b) Aniline, $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}$
(c) Cyanide ion, $\mathrm{CN}^{-}$
15.81 Write a balanced net ionic equation and the corresponding equilibrium equation for reaction of the following weak bases with water:
(a) Pyridine, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}$
(b) Ethylamine, $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{2}$
(c) Acetate ion, $\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}$
15.82 Morphine $\left(\mathrm{C}_{17} \mathrm{H}_{19} \mathrm{NO}_{3}\right)$, a narcotic used in painkillers, is a weak organic base. If the pH of a $7.0 \times 10^{-4} \mathrm{M}$ solution of morphine is 9.5 , what is the value of $K_{\mathrm{b}}$ ?
15.83 A $1.00 \times 10^{-3} \mathrm{M}$ solution of quinine, a drug used in treating malaria, has a pH of 9.75 . What is the value of $K_{\mathrm{b}}$ for quinine?
15.84 Using the values of $K_{\mathrm{b}}$ in Appendix C, calculate $\left[\mathrm{OH}^{-}\right.$] and the pH for each of the following solutions:
(a) 0.24 M methylamine
(b) 0.040 M pyridine
(c) 0.075 M hydroxylamine
15.85 Aniline $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}\right)$ is an organic base used in the manufacture of dyes. Calculate the pH and the concentrations of all species present $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}\right.$, $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{3}{ }^{+}, \mathrm{OH}^{-}$, and $\mathrm{H}_{3} \mathrm{O}^{+}$) in a 0.15 M solution of aniline ( $K_{\mathrm{b}}=4.3 \times 10^{-10}$ ).
15.86 Using values of $K_{\mathrm{b}}$ in Appendix C, calculate values of $K_{\mathrm{a}}$ for each of the following ions:
(a) Propylammonium ion, $\mathrm{C}_{3} \mathrm{H}_{7} \mathrm{NH}_{3}{ }^{+}$
(b) Hydroxylammonium ion, $\mathrm{NH}_{3} \mathrm{OH}^{+}$
(c) Anilinium ion, $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{3}{ }^{+}$
(d) Pyridinium ion, $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{NH}^{+}$
15.87 Using values of $K_{\mathrm{a}}$ in Appendix C, calculate values of $K_{\mathrm{b}}$ for each of the following ions:
(a) Fluoride ion, $\mathrm{F}^{-}$
(b) Hypobromite ion, $\mathrm{OBr}^{-}$
(c) Hydrogen sulfide ion, $\mathrm{HS}^{-}$
(d) Sulfide ion, $\mathrm{S}^{2-}$

## Acid-Base Properties of Salts

15.88 Write a balanced net ionic equation for the reaction of each of the following ions with water. In each case, identify the Brønsted-Lowry acids and bases and the conjugate acid-base pairs.
(a) $\mathrm{CH}_{3} \mathrm{NH}_{3}{ }^{+}$
(b) $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$
(c) $\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}$
(d) $\mathrm{PO}_{4}{ }^{3-}$
15.89 Write a balanced net ionic equation for the principal reaction in solutions of each of the following salts. In each case, identify the Brønsted-Lowry acids and bases and the conjugate acid-base pairs.
(a) $\mathrm{Na}_{2} \mathrm{CO}_{3}$
(b) $\mathrm{NH}_{4} \mathrm{NO}_{3}$
(c) NaCl
(d) $\mathrm{ZnCl}_{2}$
15.90 Classify each of the following ions according to whether they react with water to give a neutral, acidic, or basic solution:
(a) $\mathrm{F}^{-}$
(b) $\mathrm{Br}^{-}$
(c) $\mathrm{NH}_{4}^{+}$
(d) $\mathrm{K}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{+}$
(e) $\mathrm{SO}_{3}{ }^{2-}$
(f) $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$
15.91 Classify each of the following salt solutions as neutral, acidic, or basic. See Appendix $C$ for values of equilibrium constants.
(a) $\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}$
(b) $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$
(c) NaOCl
(d) $\mathrm{NH}_{4} \mathrm{I}$
(e) $\mathrm{NH}_{4} \mathrm{NO}_{2}$
(f) $\left(\mathrm{CH}_{3} \mathrm{NH}_{3}\right) \mathrm{Cl}$
15.92 Calculate the concentrations of all species present and the pH in 0.10 M solutions of the following substances. See Appendix C for values of equilibrium constants.
(a) Ethylammonium nitrate, $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{3}\right) \mathrm{NO}_{3}$
(b) Sodium acetate, $\mathrm{Na}\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)$
(c) Sodium nitrate, $\mathrm{NaNO}_{3}$.
15.93 Calculate the pH and the percent dissociation of the hydrated cation in 0.020 M solutions of the following substances. See Appendix $C$ for values of equilibrium constants.
(a) $\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{2}$
(b) $\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}$

## Factors That Affect Acid Strength

15.94 Arrange each group of compounds in order of increasing acid strength. Explain your reasoning.
(a) $\mathrm{HCl}, \mathrm{H}_{2} \mathrm{~S}, \mathrm{PH}_{3}$
(b) $\mathrm{NH}_{3}, \mathrm{PH}_{3}, \mathrm{AsH}_{3}$
(c) $\mathrm{HBrO}, \mathrm{HBrO}_{2}, \mathrm{HBrO}_{3}$
15.95 Arrange each group of compounds in order of decreasing acid strength. Explain your reasoning.
(a) $\mathrm{H}_{2} \mathrm{O}, \mathrm{H}_{2} \mathrm{~S}, \mathrm{H}_{2} \mathrm{Se}$
(b) $\mathrm{HClO}_{3}, \mathrm{HBrO}_{3}, \mathrm{HIO}_{3}$
(c) $\mathrm{PH}_{3}, \mathrm{H}_{2} \mathrm{~S}, \mathrm{HCl}$
15.96 Identify the strongest acid in each of the following sets. Explain your reasoning.
(a) $\mathrm{H}_{2} \mathrm{O}, \mathrm{HF}$, or HCl
(b) $\mathrm{HClO}_{2}, \mathrm{HClO}_{3}$, or $\mathrm{HBrO}_{3}$
(c) $\mathrm{HBr}, \mathrm{H}_{2} \mathrm{~S}$, or $\mathrm{H}_{2} \mathrm{Se}$
15.97 Identify the weakest acid in each of the following sets. Explain your reasoning.
(a) $\mathrm{H}_{2} \mathrm{SO}_{3}, \mathrm{HClO}_{3}, \mathrm{HClO}_{4}$
(b) $\mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{O}, \mathrm{H}_{2} \mathrm{~S}$
(c) $\mathrm{B}(\mathrm{OH})_{3}, \mathrm{Al}(\mathrm{OH})_{3}, \mathrm{Ga}(\mathrm{OH})_{3}$
15.98 Identify the stronger acid in each of the following pairs. Explain your reasoning.
(a) $\mathrm{H}_{2} \mathrm{Se}$ or $\mathrm{H}_{2} \mathrm{Te}$
(b) $\mathrm{H}_{3} \mathrm{PO}_{4}$ or $\mathrm{H}_{3} \mathrm{AsO}_{4}$
(c) $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$or $\mathrm{HPO}_{4}{ }^{2-}$
(d) $\mathrm{CH}_{4}$ or $\mathrm{NH}_{4}^{+}$
15.99 Identify the stronger base in each of the following pairs. Explain your reasoning.
(a) $\mathrm{ClO}_{2}^{-}$or $\mathrm{ClO}_{3}^{-}$
(b) $\mathrm{HSO}_{4}^{-}$or $\mathrm{HSeO}_{4}^{-}$
(c) $\mathrm{HS}^{-}$or $\mathrm{OH}^{-}$
(d) $\mathrm{HS}^{-}$or $\mathrm{Br}^{-}$

## Lewis Acids and Bases

15.100 For each of the following reactions, identify the Lewis acid and the Lewis base:
(a) $\mathrm{SiF}_{4}+2 \mathrm{~F}^{-} \rightarrow \mathrm{SiF}_{6}{ }^{2-}$
(b) $4 \mathrm{NH}_{3}+\mathrm{Zn}^{2+} \rightarrow \mathrm{Zn}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$
(c) $2 \mathrm{Cl}^{-}+\mathrm{HgCl}_{2} \rightarrow \mathrm{HgCl}_{4}^{2-}$
(d) $\mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{H}_{2} \mathrm{CO}_{3}$
15.101 For each of the following reactions, identify the Lewis acid and the Lewis base:
(a) $2 \mathrm{Cl}^{-}+\mathrm{BeCl}_{2} \rightarrow \mathrm{BeCl}_{4}{ }^{2-}$
(b) $\mathrm{Mg}^{2+}+6 \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{Mg}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}$
(c) $\mathrm{SO}_{3}+\mathrm{OH}^{-} \rightarrow \mathrm{HSO}_{4}^{-}$
(d) $\mathrm{F}^{-}+\mathrm{BF}_{3} \rightarrow \mathrm{BF}_{4}^{-}$
15.102 For each of the Lewis acid-base reactions in Problem 15.100, draw electron-dot structures for the reactants and products, and use the curved arrow notation (Section 15.16) to represent the donation of a lone pair of electrons from the Lewis base to the Lewis acid.
15.103 For each of the Lewis acid-base reactions in Problem 15.101, draw electron-dot structures for the reactants and products, and use the curved arrow notation (Section 15.16) to represent the donation of a lone pair of electrons from the Lewis base to the Lewis acid.
15.104 Classify each of the following as a Lewis acid or a Lewis base:
(a) $\mathrm{CN}^{-}$
(b) $\mathrm{H}^{+}$
(c) $\mathrm{H}_{2} \mathrm{O}$
(d) $\mathrm{Fe}^{3+}$
(e) $\mathrm{OH}^{-}$
(f) $\mathrm{CO}_{2}$
(g) $\mathrm{P}\left(\mathrm{CH}_{3}\right)_{3}$
(h) $\mathrm{B}\left(\mathrm{CH}_{3}\right)_{3}$
15.105 Which would you expect to be the stronger Lewis acid in each of the following pairs? Explain.
(a) $\mathrm{BF}_{3}$ or $\mathrm{BH}_{3}$
(b) $\mathrm{SO}_{2}$ or $\mathrm{SO}_{3}$
(c) $\mathrm{Sn}^{2+}$ or $\mathrm{Sn}^{4+}$
(d) $\mathrm{CH}_{3}{ }^{+}$or $\mathrm{CH}_{4}$

## General Problems

15.106 Aqueous solutions of hydrogen sulfide contain $\mathrm{H}_{2} \mathrm{~S}$, $\mathrm{HS}^{-}, \mathrm{S}^{2-}, \mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{OH}^{-}$, and $\mathrm{H}_{2} \mathrm{O}$ in varying concentrations. Which of these species can act only as an acid? Which can act only as a base? Which can act both as an acid and as a base?
15.107 Given the following pH values for some common foods, calculate $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$and $\left[\mathrm{OH}^{-}\right]$.
(a) Dill pickles, 3.2
(b) Eggs, 7.8
(c) Apples, 3.1
(d) Milk, 6.4
(e) Tomatoes, 4.2
(f) Limes, 1.9
15.108 Draw an electron-dot structure for $\mathrm{H}_{3} \mathrm{O}^{+}$, and explain how $\mathrm{H}_{3} \mathrm{O}^{+}$can form higher hydrates such as $\mathrm{H}_{5} \mathrm{O}_{2}{ }^{+}, \mathrm{H}_{7} \mathrm{O}_{3}{ }^{+}$, and $\mathrm{H}_{9} \mathrm{O}_{4}{ }^{+}$.
15.109 The hydronium ion $\mathrm{H}_{3} \mathrm{O}^{+}$is the strongest acid that can exist in aqueous solution because stronger acids dissociate by transferring a proton to water. What is the strongest base that can exist in aqueous solution?
15.110 Baking powder contains baking soda $\left(\mathrm{NaHCO}_{3}\right)$ and an acidic substance such as sodium alum, $\mathrm{NaAl}\left(\mathrm{SO}_{4}\right)_{2} \cdot 12 \mathrm{H}_{2} \mathrm{O}$. These components react in an aqueous medium to produce $\mathrm{CO}_{2}$ gas, which "raises" the dough. Write a balanced net ionic equation for the reaction.
15.111 Arrange the following substances in order of increasing $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$for a 0.10 M solution of each:
(a) $\mathrm{Zn}\left(\mathrm{NO}_{3}\right)_{2}$
(b) $\mathrm{Na}_{2} \mathrm{O}$
(c)
NaOCl
(d) $\mathrm{NaClO}_{4}$
(e) $\mathrm{HClO}_{4}$
15.112 At $0^{\circ} \mathrm{C}$, the density of liquid water is $0.9998 \mathrm{~g} / \mathrm{mL}$ and the value of $K_{\mathrm{w}}$ is $1.14 \times 10^{-15}$. What fraction of the molecules in liquid water are dissociated at $0^{\circ} \mathrm{C}$ ? What is the percent dissociation at $0^{\circ} \mathrm{C}$ ? What is the pH of a neutral solution at $0^{\circ} \mathrm{C}$ ?
15.113 Use the conjugate acid-base pair HCN and $\mathrm{CN}^{-}$to derive the relationship between $K_{\mathrm{a}}$ and $K_{\mathrm{b}}$.
15.114 Nicotine $\left(\mathrm{C}_{10} \mathrm{H}_{14} \mathrm{~N}_{2}\right)$ can accept two protons because it has two basic N atoms $\left(K_{\mathrm{b} 1}=1.0 \times 10^{-6}\right.$; $K_{\mathrm{b} 2}=1.3 \times 10^{-11}$ ). Calculate the values of $K_{\mathrm{a}}$ for the conjugate acids $\mathrm{C}_{10} \mathrm{H}_{14} \mathrm{~N}_{2} \mathrm{H}^{+}$and $\mathrm{C}_{10} \mathrm{H}_{14} \mathrm{~N}_{2} \mathrm{H}_{2}{ }^{2+}$.
15.115 Sodium benzoate $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{Na}\right)$ is used as a food preservative. Calculate the pH and the concentrations of all species present $\left(\mathrm{Na}^{+}, \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2}^{-}, \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right.$, $\mathrm{H}_{3} \mathrm{O}^{+}$, and $\mathrm{OH}^{-}$) in 0.050 M sodium benzoate; $K_{\mathrm{a}}$ for benzoic acid $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right)$ is $6.5 \times 10^{-5}$.
15.116 The hydrated cation $\mathrm{M}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ has $K_{\mathrm{a}}=10^{-4}$, and the acid HA has $K_{\mathrm{a}}=10^{-5}$. Identify the principal reaction in an aqueous solution of each of the following salts, and classify each solution as acidic, basic, or neutral:
(a) NaA
(b) $\mathrm{M}\left(\mathrm{NO}_{3}\right)_{3}$
(c) $\mathrm{NaNO}_{3}$
(d) $\mathrm{MA}_{3}$
15.117 Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{F}^{-}, \mathrm{HF}, \mathrm{Cl}^{-}\right.$, and $\left.\mathrm{OH}^{-}\right)$in a solution that contains $0.10 \mathrm{M} \mathrm{HF}\left(K_{\mathrm{a}}=3.5 \times 10^{-4}\right)$ and 0.10 M HCl .
15.118 Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{OH}^{-}, \mathrm{HIO}_{3}\right.$, and $\left.\mathrm{IO}_{3}^{-}\right)$in 0.0500 M $\mathrm{HIO}_{3}$. $K_{\mathrm{a}}$ for $\mathrm{HIO}_{3}$ is $1.7 \times 10^{-1}$.
15.119 Many home pools are disinfected by adding calcium hypochlorite, $\mathrm{Ca}(\mathrm{OCl})_{2}$. Reaction of the hypochlorite ion with water yields hypochlorous acid. Given that $K_{\mathrm{a}}$ for HOCl is $3.5 \times 10^{-8}$, calculate the pH of a 0.100 M solution of $\mathrm{Ca}(\mathrm{OCl})_{2}$.
15.120 Calculate the pH of a 0.100 M solution of $\mathrm{Na}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$. For $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}, K_{\mathrm{a} 1}=5.9 \times 10^{-2}$, and $K_{\mathrm{a} 2}=6.4 \times 10^{-5}$.
15.121 Sulfur dioxide is quite soluble in water:

$$
\mathrm{SO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{2} \mathrm{SO}_{3}(a q) \quad K=1.33
$$

The $\mathrm{H}_{2} \mathrm{SO}_{3}$ produced is a weak diprotic acid $\left(K_{\mathrm{a} 1}=1.5 \times 10^{-2} ; K_{\mathrm{a} 2}=6.3 \times 10^{-8}\right)$. Calculate the pH and the concentrations of $\mathrm{H}_{2} \mathrm{SO}_{3}, \mathrm{HSO}_{3}{ }^{-}$, and $\mathrm{SO}_{3}{ }^{2-}$ in a solution prepared by continuously bubbling $\mathrm{SO}_{2}$ at a pressure of 1.00 atm into pure water.
15.122 Classify each of the following salt solutions as neutral, acidic, or basic. See Appendix C for values of equilibrium constants.
(a) $\mathrm{NH}_{4} \mathrm{~F}$
(b) $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{SO}_{3}$
15.123 Calculate the percent dissociation in each of the following solutions. What is the quantitative relationship between the percent dissociation and the concentration of the acid? What is the quantitative relationship between the percent dissociation and the value of $K_{\mathrm{a}}$ ?
(a) $2.0 \mathrm{M} \mathrm{HOCl}\left(K_{\mathrm{a}}=3.5 \times 10^{-8}\right)$
(b) 0.020 M HOCl
(c) $2.0 \mathrm{M} \mathrm{HF}\left(K_{\mathrm{a}}=3.5 \times 10^{-4}\right)$
15.124 Beginning with the equilibrium equation for the dissociation of a weak acid HA, show that the percent dissociation varies directly as the square root of $K_{\mathrm{a}}$ and inversely as the square root of the initial concentration of HA when the concentration of HA that dissociates is negligible compared with its initial concentration.
15.125 Calculate the pH and the concentrations of all species present in 0.25 M solutions of each of the salts in Problem 15.122. (Hint: The principal reaction is proton transfer from the cation to the anion.)
15.126 For a solution of two weak acids with comparable values of $K_{\mathrm{a}}$, there is no single principal reaction. The two acid-dissociation equilibrium equations must therefore be solved simultaneously. Calculate the pH in a solution that is 0.10 M in acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}, \mathrm{K}_{\mathrm{a}}=\right.$ $\left.1.8 \times 10^{-5}\right)$ and 0.10 M in benzoic acid $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right.$, $\left.K_{\mathrm{a}}=6.5 \times 10^{-5}\right)$. (Hint: Let $x=\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]$ that dissociates and $y=\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right]$ that dissociates; then $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=x+y$.)
15.127 What is the pH and the principal source of $\mathrm{H}_{3} \mathrm{O}^{+}$ions in $1.0 \times 10^{-10} \mathrm{M} \mathrm{HCl}$ ? (Hint: The pH of an acid solution can't exceed 7.) What is the pH of $1.0 \times 10^{-7} \mathrm{M} \mathrm{HCl}$ ?
15.128 When $\mathrm{NO}_{2}$ is bubbled into water, it disproportionates completely into $\mathrm{HNO}_{3}$ and $\mathrm{HNO}_{2}$ :

$$
2 \mathrm{NO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{HNO}_{3}(a q)+\mathrm{HNO}_{2}(a q)
$$

Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{O}^{+}, \mathrm{OH}^{-}, \mathrm{HNO}_{2}, \mathrm{NO}_{2}^{-}\right.$, and $\left.\mathrm{NO}_{3}^{-}\right)$in a solution prepared by dissolving 0.0500 mol of $\mathrm{NO}_{2}$ in 1.00 L of water. $K_{\mathrm{a}}$ for $\mathrm{HNO}_{2}$ is $4.5 \times 10^{-4}$.
15.129 Acid and base behavior can be observed in solvents other than water. One commonly used solvent is dimethyl sulfoxide (DMSO), which can be treated as a monoprotic acid "HSol." Just as water can behave either as an acid or a base, so HSol can behave either as a Brønsted-Lowry acid or base.
(a) The equilibrium constant for self-dissociation of HSol (call it $K_{\mathrm{HSol}}$ ) is $1 \times 10^{-35}$. Write the chemical equation for the self-dissociation reaction and the corresponding equilibrium equation. (Hint: The equilibrium equation is analogous to the equilibrium equation for $K_{\mathrm{w}}$ in the case of water.)
(b) The weak acid HCN has an acid dissociation constant $K_{\mathrm{a}}=1.3 \times 10^{-13}$ in the solvent HSol. If 0.010 mol of NaCN is dissolved in 1.00 L of HSol, what is the equilibrium concentration of $\mathrm{H}_{2} \mathrm{Sol}^{+}$?

## Multi-Concept Problems

15.130 A 7.0 mass \% solution of $\mathrm{H}_{3} \mathrm{PO}_{4}$ in water has a density of $1.0353 \mathrm{~g} / \mathrm{mL}$. Calculate the pH and the concentrations of all species present $\left(\mathrm{H}_{3} \mathrm{PO}_{4}, \mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}, \mathrm{HPO}_{4}{ }^{2-}\right.$, $\mathrm{PO}_{4}{ }^{3-}, \mathrm{H}_{3} \mathrm{O}^{+}$, and $\mathrm{OH}^{-}$) in the solution. Values of equilibrium constants are listed in Appendix C.
15.131 In the case of very weak acids, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$from the dissociation of water is significant compared with $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$from dissociation of the weak acid. The sugar substitute saccha$\operatorname{rin}\left(\mathrm{C}_{7} \mathrm{H}_{5} \mathrm{NO}_{3} \mathrm{~S}\right)$, for example, is a very weak acid having $K_{\mathrm{a}}=2.1 \times 10^{-12}$ and a solubility in water of $348 \mathrm{mg} / 100$ mL . Calculate $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$in a saturated solution of saccharin. (Hint: Equilibrium equations for the dissociation of saccharin and water must be solved simultaneously.)
15.132 In aqueous solution, sodium acetate behaves as a strong electrolyte, yielding $\mathrm{Na}^{+}$cations and $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$ anions. A particular solution of sodium acetate has a pH of 9.07 and a density of $1.0085 \mathrm{~g} / \mathrm{mL}$. What is the molality of this solution, and what is its freezing point?
15.133 During a certain time period, 4.0 million tons of $\mathrm{SO}_{2}$ was released into the atmosphere and was subsequently oxidized to $\mathrm{SO}_{3}$. As explained in the Interlude, the acid rain produced when the $\mathrm{SO}_{3}$ dissolves in water can damage marble statues:

$$
\begin{aligned}
& \mathrm{CaCO}_{3}(s)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \longrightarrow \\
& \mathrm{CaSO}_{4}(a q)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

(a) How many 500 pound marble statues could be damaged by the acid rain? (Assume that the statues are pure $\mathrm{CaCO}_{3}$ and that a statue is damaged when $3.0 \%$ of its mass is dissolved.)
(b) How many liters of $\mathrm{CO}_{2}$ gas at $20^{\circ} \mathrm{C}$ and 735 mm Hg is produced as a by-product?
(c) The cation in aqueous $\mathrm{H}_{2} \mathrm{SO}_{4}$ is trigonal pyramidal rather than trigonal planar. Explain.
15.134 Neutralization reactions involving either a strong acid or a strong base go essentially to completion, and therefore we must take such neutralizations into
account before calculating concentrations in mixtures of acids and bases. Consider a mixture of 3.28 g of $\mathrm{Na}_{3} \mathrm{PO}_{4}$ and 300.0 mL of 0.180 M HCl . Write balanced net ionic equations for the neutralization reactions, and calculate the pH of the solution.
15.135 We've said that alkali metal cations do not react appreciably with water to produce $\mathrm{H}_{3} \mathrm{O}^{+}$ions, but in fact, all cations are acidic to some extent. The most acidic alkali metal cation is the smallest one, $\mathrm{Li}^{+}$, which has $K_{\mathrm{a}}=2.5 \times 10^{-14}$ for the reaction

$$
\begin{array}{r}
\mathrm{Li}\left(\mathrm{H}_{2} \mathrm{O}\right)_{4}{ }^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \\
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{Li}\left(\mathrm{H}_{2} \mathrm{O}\right)_{3}(\mathrm{OH})(a q)
\end{array}
$$

This reaction and the dissociation of water must be considered simultaneously in calculating the pH of $\mathrm{Li}^{+}$solutions, which nevertheless have $\mathrm{pH} \approx 7$. Check this by calculating the pH of 0.10 M LiCl .
15.136 A 1.000 L sample of HF gas at $20.0^{\circ} \mathrm{C}$ and 0.601 atm pressure was dissolved in enough water to make 50.0 mL of hydrofluoric acid.
(a) What is the pH of the solution?
(b) To what volume must you dilute the solution to triple the percent dissociation. Why can't you solve this problem by using the result obtained in Problem 15.124?
15.137 A 200.0 mL sample of 0.350 M acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$ was allowed to react with 2.000 L of gaseous ammonia at $25^{\circ} \mathrm{C}$ and a pressure of 650.8 mm Hg . Assuming no change in the volume of the solution, calculate the pH and the equilibrium concentrations of all species present $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}, \mathrm{CH}_{3} \mathrm{CO}_{2}^{-}, \mathrm{NH}_{3}, \mathrm{NH}_{4}^{+}, \mathrm{H}_{3} \mathrm{O}^{+}\right.$, and $\mathrm{OH}^{-}$). Values of equilibrium constants are listed in Appendix C.
15.138 You may have been told not to mix bleach and ammonia. The reason is that bleach (sodium hypochlorite) reacts with ammonia to produce toxic chloramines, such as $\mathrm{NH}_{2} \mathrm{Cl}$. For example, in basic solution:

$$
\mathrm{OCl}^{-}(a q)+\mathrm{NH}_{3}(a q) \longrightarrow \mathrm{OH}^{-}(a q)+\mathrm{NH}_{2} \mathrm{Cl}(a q)
$$

(a) The following initial rate data for this reaction were obtained in basic solution at $25^{\circ} \mathrm{C}$ :

| $\mathbf{p H}$ | Initial <br> $\left[\mathbf{O C l}^{-} \mathbf{]}\right.$ | Initial <br> $\left[\mathbf{N H}_{\mathbf{3}}\right]$ | Initial <br> Rate (M/s) |
| :--- | :--- | :--- | :--- |
| 12 | 0.001 | 0.01 | 0.017 |
| 12 | 0.002 | 0.01 | 0.033 |
| 12 | 0.002 | 0.03 | 0.100 |
| 13 | 0.002 | 0.03 | 0.010 |

What is the rate law for the reaction? What is the numerical value of the rate constant $k$, including the correct units?
(b) The following mechanism has been proposed for this reaction in basic solution:

$$
\begin{gathered}
\mathrm{H}_{2} \mathrm{O}+\mathrm{OCl}^{-} \rightleftharpoons \mathrm{HOCl}+\mathrm{OH}^{-} \\
\text {Fast, equilibrium constant } K_{1} \rightleftharpoons \\
\mathrm{HOCl}+\mathrm{NH}_{3} \longrightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{NH}_{2} \mathrm{Cl} \\
\text { Slow, rate constant } k_{2}
\end{gathered}
$$

Assuming that the first step is in equilibrium and the second step is rate-determining, calculate the value of the rate constant $k_{2}$ for the second step. $K_{\mathrm{a}}$ for HOCl is $3.5 \times 10^{-8}$.

## eMedia Problems

15.139 For each of the compounds in the center column of the Conjugate Acid-Base Pairs activity (eChapter 15.1), write the dissociation equations that convert it to its conjugate acid and its conjugate base.
15.140 The activity in eChapter 15.4 allows you to determine the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$and the $\left[\mathrm{OH}^{-}\right]$as acid is added to the beaker of water. Complete the activity, and answer the following questions:
(a) What is the relationship between $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$and $\left[\mathrm{OH}^{-}\right]$?
(b) Why does the $\left[\mathrm{OH}^{-}\right]$concentration decrease as acid is added?
15.141 Measure the pH of a 0.10 M solution of each of the compounds available in the Testing $\mathbf{p H}$ activity (eChapter 15.7), and list the compounds from strongest acid to strongest base. Identify each of the compounds as a strong acid, a weak acid, a strong base, or a weak base. Would changing the concentration change your list? What is the relationship between the strength of an acid and its concentration?
15.142 Use data from the Testing $\mathbf{p H}$ activity (eChapter 15.7) to determine the $K_{\mathrm{b}}$ of methylamine, $\mathrm{CH}_{3} \mathrm{NH}_{2}$. Determine the percent dissociation of methylamine at $0.10 \mathrm{M}, 0.0010 \mathrm{M}$, and $1.0 \times 10^{-5} \mathrm{M}$ concentrations. What is the relationship between the percent dissociation and the pH for a weak base? Would you expect the same relationship for a weak acid? Explain.
15.143 Use the Equilibrium Constant for Acids activity (eChapter 15.9) to experiment with the dissociation of a weak acid. What would be the hydronium ion concentration and pH of 0.10 M solutions of weak acids with $K_{\mathrm{a}}=1 \times 10^{-5} ; K_{\mathrm{a}}=1 \times 10^{-10}$; and $K_{\mathrm{a}}=1 \times 10^{-15}$ ? Describe the relationship between the pH and the strength of an acid for acids at equal concentrations.
15.144 For each of the compounds in the Acid-Base Properties of Salts activity (eChapter 15.14), write the reaction that takes place when the compound is placed in water. Identify the conjugate base pairs in each reaction.

## Chapter

## Applications of Aqueous Equilibria

## Aqueous equilibria play a crucial role in many biological and environmental

processes. The pH of human blood, for example, is carefully controlled at a value of 7.4 by equilibria involving, primarily, the conjugate acid-base pair $\mathrm{H}_{2} \mathrm{CO}_{3}$ and $\mathrm{HCO}_{3}{ }^{-}$. The pH of many lakes and streams must remain near 5.5 for plant and aquatic life to flourish.

We began a study of aqueous equilibria in Chapter 15, where we examined the dissociation of weak acids and

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These downward-growing, icicle-shaped structures called stalactites and the upward-growing columns called stalagmites are formed in limestone caves by the slow precipitation of calcium carbonate from dripping water.
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Strong Acid-Strong Base Neutralization activity


Weak Acid-Strong Base Neutralization activity
weak bases. In this chapter, we'll continue the study. First we'll see how to calculate the pH of mixtures of acids and bases. Then we'll look at the dissolution and precipitation of slightly soluble salts and the factors that affect solubility. Aqueous equilibria involving the dissolution and precipitation of salts are important in a great many natural processes, from tooth decay to the formation of limestone caves.

## 16.1 | Neutralization Reactions

We've seen on numerous occasions that the neutralization reaction of an acid with a base produces water and a salt. But to what extent does a neutralization reaction go to completion? We must answer that question before we can make pH calculations on mixtures of acids and bases. Let's look at four types of neutralization reactions: (1) strong acid-strong base, (2) weak acid-strong base, (3) strong acid-weak base, and (4) weak acid-weak base.

## Strong Acid-Strong Base

Let's consider the reaction of hydrochloric acid with aqueous sodium hydroxide to give water and an aqueous solution of sodium chloride:

$$
\mathrm{HCl}(a q)+\mathrm{NaOH}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{NaCl}(a q)
$$

Because $\mathrm{HCl}(a q), \mathrm{NaOH}(a q)$, and $\mathrm{NaCl}(a q)$ are all completely dissociated, the net ionic equation for the neutralization reaction is

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}(l)
$$

If we mix equal numbers of moles of $\mathrm{HCl}(a q)$ and $\mathrm{NaOH}(a q)$, the concentrations of $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{OH}^{-}$remaining in the NaCl solution after neutralization will be the same as those in pure water, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$. In other words, the reaction of HCl with NaOH proceeds far to the right.

We come to the same conclusion by looking at the equilibrium constant for the reaction. Because the neutralization reaction of any strong acid with a strong base is the reverse of the dissociation of water, its equilibrium constant, $K_{n}$ (" $n$ " for neutralization), is just the reciprocal of the ion-product constant for water, $K_{\mathrm{n}}=1 / K_{\mathrm{w}}$ :

$$
\begin{aligned}
& \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}(l) \\
& K_{\mathrm{n}}=\frac{1}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{OH}^{-}\right]}=\frac{1}{K_{\mathrm{w}}}=\frac{1}{1.0 \times 10^{-14}}=1.0 \times 10^{14}
\end{aligned}
$$

The value of $K_{\mathrm{n}}\left(1.0 \times 10^{14}\right)$ for a strong acid-strong base reaction is a large number, which means that the neutralization reaction proceeds essentially $100 \%$ to completion. After neutralization of equal molar amounts of acid and base, the solution contains a salt derived from a strong base and a strong acid. Because neither the cation nor the anion of the salt has acidic or basic properties, the pH is 7 (Section 15.14).

## Weak Acid-Strong Base

Because a weak acid HA is largely undissociated, the net ionic equation for the neutralization reaction involves proton transfer from HA to the strong base, $\mathrm{OH}^{-}$:

$$
\mathrm{HA}(a q)+\mathrm{OH}^{-}(a q) \rightleftharpoons \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{A}^{-}(a q)
$$

Acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$, for example, reacts with aqueous NaOH to give water and aqueous sodium acetate $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}\right)$ :

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{OH}^{-}(a q) \rightleftharpoons \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)
$$

$\mathrm{Na}^{+}$ions do not appear in the net ionic equation because both NaOH and $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}$ are completely dissociated.

To obtain the equilibrium constant, $K_{n}$, we multiply known equilibrium constants for reactions that add to give the net ionic equation for the neutralization reaction. Because $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ is on the left side of the equation and $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$is on the right side, one of the reactions needed is the dissociation of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$. Since $\mathrm{H}_{2} \mathrm{O}$ is on the right side of the equation and $\mathrm{OH}^{-}$is on the left side, the other reaction needed is the reverse of the dissociation of $\mathrm{H}_{2} \mathrm{O}$. Note that $\mathrm{H}_{3} \mathrm{O}^{+}$and one $\mathrm{H}_{2} \mathrm{O}$ molecule cancel when the two equations are added:


As we saw in Section 15.13, the equilibrium constant for a net reaction equals the product of the equilibrium constants for the reactions added. Therefore, we multiply $K_{\mathrm{a}}$ for $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ by the reciprocal of $K_{\mathrm{w}}$ to get $K_{\mathrm{n}}$ for the neutralization reaction. (We use $1 / K_{\mathrm{w}}$ because the $\mathrm{H}_{2} \mathrm{O}$ dissociation reaction is written in the reverse direction.) The resulting large value of $K_{\mathrm{n}}\left(1.8 \times 10^{9}\right)$ means that the neutralization reaction proceeds nearly $100 \%$ to completion.

As a general rule, the neutralization of any weak acid by a strong base will go $100 \%$ to completion because $\mathrm{OH}^{-}$has a great affinity for protons. After neutralization of equal molar amounts of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ and NaOH , the solution contains $\mathrm{Na}^{+}$, which has no acidic or basic properties, and $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$, which is a weak base. Therefore, the pH is greater than 7 (Section 15.14).

## Strong Acid-Weak Base

A strong acid HA is completely dissociated into $\mathrm{H}_{3} \mathrm{O}^{+}$and $\mathrm{A}^{-}$ions, and the neutralization reaction therefore involves proton transfer from $\mathrm{H}_{3} \mathrm{O}^{+}$to the weak base B:

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{B}(a q) \rightleftharpoons \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{BH}^{+}(a q)
$$

For example, the net ionic equation for neutralization of hydrochloric acid with aqueous ammonia is

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{NH}_{4}^{+}(a q)
$$

As in the weak acid-strong base case, we can obtain the equilibrium constant for the neutralization reaction by multiplying known equilibrium constants for reactions that add to give the net ionic equation:


Again, the neutralization reaction proceeds nearly $100 \%$ to the right because its equilibrium constant $K_{n}$ is a very large number $\left(1.8 \times 10^{9}\right)$. (It's purely coincidental that the neutralization reactions of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ with NaOH and of HCl with $\mathrm{NH}_{3}$ have the same value of $K_{\mathrm{n}}$. The two $K_{\mathrm{n}}$ values are the same because $K_{\mathrm{a}}$ for $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ happens to have the same value as $K_{\mathrm{b}}$ for $\mathrm{NH}_{3}$.)


A When hydrochloric acid is added to aqueous ammonia containing the acid-base indicator methyl red, the color of the indicator changes from yellow to red in the pH range 6.0-4.2 because of neutralization of the $\mathrm{NH}_{3}$.

The neutralization of any weak base with a strong acid generally goes $100 \%$ to completion because $\mathrm{H}_{3} \mathrm{O}^{+}$is a powerful proton donor. After neutralization of equal molar amounts of $\mathrm{NH}_{3}$ and HCl , the solution contains $\mathrm{NH}_{4}{ }^{+}$, which is a weak acid, and $\mathrm{Cl}^{-}$, which has no acidic or basic properties. Therefore, the pH is less than 7 (Section 15.14).

## Weak Acid-Weak Base

Both a weak acid HA and a weak base B are largely undissociated, and the neutralization reaction therefore involves proton transfer from the weak acid to the weak base. For example, the net ionic equation for neutralization of acetic acid with aqueous ammonia is

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)
$$

The equilibrium constant $K_{n}$ can be obtained by adding equations for (1) the acid dissociation of acetic acid, (2) the base protonation of ammonia, and (3) the reverse of the dissociation of water:

$$
\begin{array}{rlrl}
\text { li- } \\
\text { ed } \\
\text { e } & \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{H}_{2} \mathrm{O}(l) & \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q) & K_{\mathrm{a}}=1.8 \times 10^{-5} \\
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) & \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q) & K_{\mathrm{b}}=1.8 \times 10^{-5} \\
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) & \rightleftharpoons 2 \mathrm{H}_{2} \mathrm{O}(l) & & 1 / K_{\mathrm{w}}=1.0 \times 10^{14} \\
\hline \text { Net: } \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{NH}_{3}(a q) & \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q) & K_{\mathrm{n}}=\left(K_{\mathrm{a}}\right)\left(K_{\mathrm{b}}\right)\left(1 / K_{\mathrm{w}}\right)
\end{array}
$$

$$
K_{\mathrm{n}}=\left(K_{\mathrm{a}}\right)\left(K_{\mathrm{b}}\right)\left(\frac{1}{K_{\mathrm{w}}}\right)=\left(1.8 \times 10^{-5}\right)\left(1.8 \times 10^{-5}\right)\left(1.0 \times 10^{14}\right)=3.2 \times 10^{4}
$$

The value of $K_{\mathrm{n}}$ in this case is smaller than it is for the preceding three cases, so the neutralization does not proceed as far toward completion.

In general, weak acid-weak base neutralizations have less tendency to proceed to completion than neutralizations involving strong acids or strong bases. The neutralization of HCN with aqueous ammonia, for example, has a value of $K_{\mathrm{n}}$ less than unity, which means that the reaction proceeds less than halfway to completion:

$$
\mathrm{HCN}(a q)+\mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{CN}^{-}(a q) \quad K_{\mathrm{n}}=0.88
$$

## Worked Example 16.1

Write a balanced net ionic equation for the neutralization of equal molar amounts of nitric acid and methylamine $\left(\mathrm{CH}_{3} \mathrm{NH}_{2}\right)$. Indicate whether the pH after neutralization is greater than, equal to, or less than 7.

## Strategy

The formulas that should appear in the net ionic equation depend on whether the acid and base are strong (completely dissociated) or weak (largely undissociated). The pH after neutralization depends on the acid-base properties of the cation and anion in the resulting salt solution (Section 15.14).

## Solution

Because $\mathrm{HNO}_{3}$ is a strong acid and $\mathrm{CH}_{3} \mathrm{NH}_{2}$ is a weak base, the net ionic equation is

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CH}_{3} \mathrm{NH}_{2}(a q) \rightleftharpoons \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CH}_{3} \mathrm{NH}_{3}^{+}(a q)
$$

After neutralization, the solution contains $\mathrm{CH}_{3} \mathrm{NH}_{3}{ }^{+}$, a weak acid, and $\mathrm{NO}_{3}{ }^{-}$, which has no acidic or basic properties. Therefore, the pH is less than 7 .

PROBLEM 16.1 Write a balanced net ionic equation for the neutralization of equal molar amounts of the following acids and bases. Indicate whether the pH after neutralization is greater than, equal to, or less than 7 . Values of $K_{\mathrm{a}}$ and $K_{\mathrm{b}}$ are listed in Appendix C.
(a) $\mathrm{HNO}_{2}$ and KOH
(b) HBr and $\mathrm{NH}_{3}$
(c) KOH and $\mathrm{HClO}_{4}$

- PROBLEM 16.2 Write a balanced net ionic equation for the neutralization of the following acids and bases, calculate the value of $K_{\mathrm{n}}$ for each neutralization reaction, and arrange the reactions in order of increasing tendency to proceed to completion. Values of $K_{\mathrm{a}}$ and $K_{\mathrm{b}}$ are listed in Appendix C.
(a) HF and NaOH
(b) HCl and KOH
(c) HF and $\mathrm{NH}_{3}$


### 16.2 The Common-Ion Effect

A solution of a weak acid and its conjugate base is an important acid-base mixture because such mixtures regulate the pH in biological systems. To illustrate pH calculations for weak acid-conjugate base mixtures, let's calculate the pH of a solution prepared by dissolving 0.10 mol of acetic acid and 0.10 mol of sodium acetate in water and then diluting the solution to a volume of 1.00 L . This problem, like those discussed in Chapter 15, can be solved by thinking about the chemistry involved. First, identify the acid-base properties of the various species in solution, and then consider the possible proton-transfer reactions these species can undergo. We'll follow the procedure outlined in Figure 15.7.
Step 1. Since acetic acid is largely undissociated in aqueous solution and since the salt sodium acetate is essentially $100 \%$ dissociated, the species present initially are

| $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ | $\mathrm{Na}^{+}$ | $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$ | $\mathrm{H}_{2} \mathrm{O}$ |
| :---: | :---: | :---: | :---: |
| Acid | Inert | Base | Acid or base |

Steps 2-3. Because we have two acids and two bases, there are four possible proton-transfer reactions. We know, however, that acetic acid is a stronger acid than water and that the principal reaction therefore involves proton transfer from $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ to either $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$or $\mathrm{H}_{2} \mathrm{O}$ :

$$
\begin{array}{ll}
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q) \rightleftharpoons \mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q) & \mathrm{K}=1 \\
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q) & K_{\mathrm{a}}=1.8 \times 10^{-5}
\end{array}
$$

Although the first of these reactions has the larger equilibrium constant, we can't consider it to be the principal reaction because the reactants and products are identical. Proton transfer from acetic acid to its conjugate base is constantly occurring, but that reaction doesn't change any concentrations and therefore can't be used to calculate equilibrium concentrations. Consequently, the principal reaction is dissociation of acetic acid.

Step 4. Now we can set up a table of concentrations for the species involved in the principal reaction. As in Section 15.9, we define $x$ as the concentration of acid that dissociates-here, acetic acid—but we need to remember that the acetate ions come from two sources: $0.10 \mathrm{~mol} / \mathrm{L}$ of acetate comes from the sodium acetate present initially, and $x \mathrm{~mol} / \mathrm{L}$ comes from the dissociation of acetic acid.

| Principal reaction: | $\left.\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}} \mathbf{H}(\boldsymbol{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H}_{\mathbf{3}} \mathbf{O}^{+}(\mathbf{a q})+\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}}{ }^{\mathbf{(}} \mathbf{( a q}\right)$ |  |  |
| :--- | :--- | :--- | :--- |
| Initial conc (M) | 0.10 | $\sim 0$ | 0.10 |
| Change (M) | $-x$ | $+x$ | $+x$ |
| Equilibrium conc (M) | $0.10-x$ | $x$ | $0.10+x$ |

> Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Equilibrium: The Dissociation of Acetic Acid," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 160-161.

Bassam Z. Shakhashiri, "Effect of Acetate Ion on the Acidity of Acetic Acid: The Common Ion Effect," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 155-157.

The value of $x$ is negligible compared with the initial concentration and can be ignored when subtracted from or added to the initial concentration. However, by itself $x$ is significant.

Step 5. Substituting the equilibrium concentrations into the equilibrium equation for the principal reaction, we obtain

$$
K_{\mathrm{a}}=1.8 \times 10^{-5}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]}{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]}=\frac{(x)(0.10+x)}{0.10-x}
$$

Because $K_{\mathrm{a}}$ is small, $x$ is small compared to 0.10 , and we can make the approximation that $(0.10+x) \approx(0.10-x) \approx 0.10$, which simplifies the solution of the equation to

$$
\begin{aligned}
1.8 \times 10^{-5} & =\frac{(x)(0.10+x)}{0.10-x} \approx \frac{(x)(0.10)}{0.10} \\
x & =\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.8 \times 10^{-5} \mathrm{M}
\end{aligned}
$$

Step 8. $\mathrm{pH}=-\log \left(1.8 \times 10^{-5}\right)=4.74$
It's interesting to compare the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$in a 0.10 M acetic acid- 0.10 M sodium acetate solution with the $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$in a 0.10 M solution of pure acetic acid. The principal reaction is the same in both cases, but in 0.10 M acetic acid all the acetate ions come from the dissociation of acetic acid:

| Principal reaction: | $\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}} \mathbf{H}(\mathbf{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H}_{\mathbf{3}} \mathbf{O}^{+}(\boldsymbol{a q})+\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}}{ }^{-}(\boldsymbol{a q})$ |  |  |
| :--- | :--- | :--- | :--- |
| Equilibrium conc (M) | $0.10-x$ | $x$ | $x$ |

The calculated $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$of 0.10 M acetic acid is $1.3 \times 10^{-3} \mathrm{M}$, and the pH is 2.89 versus a pH of 4.74 for the acetic acid-sodium acetate solution. The difference in pH is illustrated in Figure 16.1.

FIGURE 16.1 The 0.10 M acetic acid- 0.10 M sodium acetate solution on the left has a lower $\mathrm{H}_{3} \mathrm{O}^{+}$concentration $\left(\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.8 \times 10^{-5} \mathrm{M} ; \mathrm{pH}\right.$ $4.74)$ than the 0.10 M acetic acid solution on the right $\left(\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.3 \times 10^{-3} \mathrm{M} ; \mathrm{pH}\right.$ 2.89). The difference in pH is revealed by the color of the indicator methyl orange, which changes from yellow to red in the pH range 4.4-3.2.


The decrease in $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$on adding acetate ions to an acetic acid solution is an example of the common-ion effect, the shift in an equilibrium on adding a substance that provides more of an ion already involved in the equilibrium. Thus, added acetate ions shift the acetic acid-dissociation equilibrium to the left, as shown in Figure 16.2.

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)
$$

The common-ion effect is just another example of Le Châtelier's principle (Section 13.6), in which the stress on the equilibrium that results from raising one of the product concentrations is relieved by shifting the equilibrium to the left. Another case is discussed in Worked Example 16.2.


## Worked Example 16.2

In $0.15 \mathrm{M} \mathrm{NH}_{3}$, the pH is 11.21 and the percent dissociation is $1.1 \%$. Calculate the concentrations of all species present, the pH , and the percent dissociation of ammonia in a solution that is $0.15 \mathrm{M}^{2} \mathrm{NH}_{3}$ and 0.45 M in $\mathrm{NH}_{4} \mathrm{Cl}$.

## Strategy

The solution contains a weak base $\left(\mathrm{NH}_{3}\right)$ and its conjugate acid $\left(\mathrm{NH}_{4}{ }^{+}\right)$. Because this problem is similar to the acetic acid-sodium acetate problem, we'll abbreviate the procedure in Figure 15.7.

## Solution

Steps 1-3. The principal reaction is proton transfer to $\mathrm{NH}_{3}$ from $\mathrm{H}_{2} \mathrm{O}$ :

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

Step 4. Since $\mathrm{NH}_{4}{ }^{+}$ions come both from the $\mathrm{NH}_{4} \mathrm{Cl}$ present initially ( 0.45 M ) and from the reaction of $\mathrm{NH}_{3}$ with $\mathrm{H}_{2} \mathrm{O}$, the concentrations of the species involved in the principal reaction are as follows:

| Principal reaction: | $\mathbf{N H}_{\mathbf{3}}(\mathbf{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons$ | $\mathbf{N H}_{\mathbf{4}}{ }^{+}(\boldsymbol{a q})+\mathbf{O H}^{-}(\boldsymbol{a q})$ |  |
| :--- | :--- | :--- | :--- |
| Initial conc $(\mathrm{M})$ | 0.15 | 0.45 | $\sim 0$ |
| Change $(\mathrm{M})$ | $-x$ | $+x$ | $+x$ |
| Equilibrium conc $(M)$ | $0.15-x$ | $0.45+x$ | $x$ |

Steps 5-6. The equilibrium equation for the principal reaction is

$$
K_{\mathrm{b}}=1.8 \times 10^{-5}=\frac{\left[\mathrm{NH}_{4}^{+}\right]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{NH}_{3}\right]}=\frac{(0.45+x)(x)}{0.15-x} \approx \frac{(0.45)(x)}{0.15}
$$

We assume $x$ is negligible compared to 0.45 and 0.15 because (1) the equilibrium constant $K_{\mathrm{b}}$ is small and (2) the equilibrium is shifted to the left by the common-ion effect. Therefore,

$$
\begin{aligned}
x & =\left[\mathrm{OH}^{-}\right]=\frac{\left(1.8 \times 10^{-5}\right)(0.15)}{0.45}=6.0 \times 10^{-6} \mathrm{M} \\
{\left[\mathrm{NH}_{3}\right] } & =0.15-x=0.15-\left(6.0 \times 10^{-6}\right)=0.15 \mathrm{M} \\
{\left[\mathrm{NH}_{4}^{+}\right] } & =0.45+x=0.45+\left(6.0 \times 10^{-6}\right)=0.45 \mathrm{M}
\end{aligned}
$$

Thus, the assumption concerning the size of $x$ is justified.

4 FIGURE 16.2 The common-ion effect. The concentration of $\mathrm{H}_{3} \mathrm{O}^{+}$in a 0.10 M acetic acid solution decreases as the concentration of added sodium acetate increases because added acetate ions shift the acid-dissociation equilibrium to the left. Note that $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] is plotted on a logarithmic scale.

Lee R. Summerlin and James L. Ealy, Jr., "The Common Ion Effect: Ammonium Hydroxide and Ammonium Acetate," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), p. 95 .

Steps 7-8. The $\mathrm{H}_{3} \mathrm{O}^{+}$concentration and the pH are

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{6.0 \times 10^{-6}}=1.7 \times 10^{-9} \mathrm{M}} \\
& \mathrm{pH}=-\log \left(1.7 \times 10^{-9}\right)=8.77
\end{aligned}
$$

The percent dissociation of ammonia is
Percent dissociation $=\frac{\left[\mathrm{NH}_{3}\right]_{\text {dissociated }}}{\left[\mathrm{NH}_{3}\right]_{\text {initial }}} \times 100 \%=\frac{6.0 \times 10^{-6}}{0.15} \times 100 \%=0.0040 \%$
$\checkmark$ BALLPARK CHECK In the $\mathrm{NH}_{3}-\mathrm{NH}_{4} \mathrm{Cl}$ solution, $\mathrm{NH}_{4}{ }^{+}$is the common ion, and raising its concentration shifts the equilibrium for the principal reaction to the left.

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

Thus, the percent dissociation in the $0.15 \mathrm{M} \mathrm{NH}_{3}-0.45 \mathrm{M} \mathrm{NH}_{4} \mathrm{Cl}$ solution will be less than the $1.1 \%$ in $0.15 \mathrm{M} \mathrm{NH}_{3}$. Also, the $\left[\mathrm{OH}^{-}\right]$will be less than that in $0.15 \mathrm{M} \mathrm{NH}_{3}$, and so the pH will be less than 11.21 .

PROBLEM 16.3 Calculate the concentrations of all species present, the pH , and the percent dissociation of $\operatorname{HCN}\left(K_{\mathrm{a}}=4.9 \times 10^{-10}\right)$ in a solution that is 0.025 M in HCN and 0.010 M in NaCN .

PROBLEM 16.4 Calculate the pH in a solution prepared by dissolving 0.10 mol of solid $\mathrm{NH}_{4} \mathrm{Cl}$ in 0.500 L of $0.40 \mathrm{M} \mathrm{NH}_{3}$. Assume that there is no volume change.

## Worked Key Concept Example 16.3

The following pictures represent solutions of a weak acid HA that may also contain the sodium salt NaA . Which solution has the highest pH , and which has the largest percent dissociation of HA ? ( $\mathrm{Na}^{+}$ions and solvent water molecules have been omitted for clarity.)


## Strategy

The pH and the percent dissociation of HA are determined by the extent of the reaction $\mathrm{HA}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{A}^{-}(a q)$. The dissociation equilibrium shifts to the left on adding more of the common ion $\mathrm{A}^{-}$, thus decreasing the $\mathrm{H}_{3} \mathrm{O}^{+}$ concentration (increasing the pH ) and decreasing the percent dissociation. To answer the questions posed, simply count the number of $\mathrm{A}^{-}$ions.

## Solution

All three solutions contain the same number of HA molecules, but different numbers of $\mathrm{A}^{-}$ions-none for solution (1), three for solution (2), and six for solution (3). The dissociation equilibrium lies farthest to the left for solution (3), and therefore solution (3) has the highest pH . The dissociation equilibrium lies farthest to the right for solution (1), and therefore solution (1) has the largest percent dissociation of HA.

- KEY CONCEPT PROBLEM 16.5 The following pictures represent solutions of a weak base B that may also contain the chloride salt $\mathrm{BH}^{+} \mathrm{Cl}^{-}$. Which solution has the lowest pH , and which has the largest percent dissociation of B ? $\left(\mathrm{Cl}^{-}\right.$ions and solvent water molecules have been omitted for clarity.)



## 16.3 | Buffer Solutions

Solutions like those discussed in Section 16.2, which contain a weak acid and its conjugate base, are called buffer solutions because they resist drastic changes in pH . If a small amount of $\mathrm{OH}^{-}$is added to a buffer solution, the pH increases, but not by much because the acid component of the buffer solution neutralizes the added $\mathrm{OH}^{-}$. If a small amount of $\mathrm{H}_{3} \mathrm{O}^{+}$is added to a buffer solution, the pH decreases, but again not by much because the base component of the buffer solution neutralizes the added $\mathrm{H}_{3} \mathrm{O}^{+}$.


Buffer solutions are very important in biological systems. Blood, for example, is a buffer solution that can soak up the acids and bases produced in biological reactions. The pH of human blood is carefully controlled at a value very close to 7.4 by conjugate acid-base pairs, primarily $\mathrm{H}_{2} \mathrm{CO}_{3}$ and its conjugate base $\mathrm{HCO}_{3}{ }^{-}$. The oxygen-carrying ability of blood depends on control of the pH to within 0.1 pH unit.

To see how a buffer solution works, let's return to the 0.10 M acetic acid- 0.10 M sodium acetate solution discussed in Section 16.2. The principal reaction and the equilibrium concentrations for the solution are

Charles L. Bering, "A Good Idea Leads to a Better Buffer," J. Chem. Educ., Vol. 64, 1987, 803.

Edwin S. Gould, "Phosphate Buffers and Telephone Poles-A Useful Analogy with Limitations," J. Chem. Educ., Vol. 76, 1999, 1511.

Bassam Z. Shakhashiri, "Buffer-
ing Action of Alka-Seltzer," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 186-187.

## Buffer pH activity

A mixture of a weak acid with a salt of its conjugate base is an acidic buffer. In calculations involving an acidic buffer, the only chemical equation needed is that for the dissociation of the weak acid: $\mathrm{HA}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons$ $\mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{A}^{-}$.

©Use the following approach for any neutralization reaction: (1) Determine the moles (or concentration) of each species before reaction. (2) Allow the reaction to go to completion, and determine the moles of each species "after reaction." (3) Allow the system to equilibrate, and calculate the concentration of each species at equilibrium.

| Principal reaction: | $\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}} \mathbf{H}(\boldsymbol{a q})+\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l}) \rightleftharpoons \mathbf{H}_{\mathbf{3}} \mathbf{O}^{+}(\boldsymbol{a q})+\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}}{ }^{-}(\boldsymbol{a q})$ |  |  |
| :--- | :--- | :--- | :--- |
| Equilibrium conc $(\mathrm{M})$ | $0.10-x$ | $x$ | $0.10+x$ |

If we solve the equilibrium equation for $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$, we obtain

$$
\begin{aligned}
& K_{\mathrm{a}}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]}{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]} \\
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=K_{\mathrm{a}} \frac{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]}{\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]}}
\end{aligned}
$$

Thus, the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration in a buffer solution has a value close to the value of $K_{\mathrm{a}}$ for the weak acid but differs by a factor equal to the concentration ratio [weak acid]/[conjugate base]. In the 0.10 M acetic acid -0.10 M sodium acetate solution, where the concentration ratio is unity, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$equals $K_{\mathrm{a}}$ :

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=K_{\mathrm{a}} \frac{(0.10-x)}{(0.10+x)}=K_{\mathrm{a}}\left(\frac{0.10}{0.10}\right)=K_{\mathrm{a}}=1.8 \times 10^{-5} \mathrm{M}} \\
& \mathrm{pH}=-\log \left(1.8 \times 10^{-5}\right)=4.74
\end{aligned}
$$

Note that in calculating this result we have set the equilibrium concentrations, $(0.10-x)$ and $(0.10+x)$, equal to the initial concentrations, 0.10 , because $x$ is negligible compared with the initial concentrations. For commonly used buffer solutions, $K_{\mathrm{a}}$ is small and the initial concentrations are relatively large. As a result, $x$ is generally negligible compared with the initial concentrations, and we can use initial concentrations in the calculations.

## Addition of $\mathrm{OH}^{-}$to a Buffer

Now let's consider what happens when we add $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$to a buffer solution. First, suppose that we add 0.01 mol of solid NaOH to 1.00 L of the 0.10 M acetic acid -0.10 M sodium acetate solution. Because neutralization reactions involving strong acids or strong bases go essentially $100 \%$ to completion (Section 16.1), we must take account of neutralization before calculating $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$. Initially, we have $(1.00 \mathrm{~L})(0.10 \mathrm{~mol} / \mathrm{L})=0.10 \mathrm{~mol}$ of acetic acid and an equal amount of acetate ion. When we add 0.01 mol of NaOH , the neutralization reaction will alter the numbers of moles:

| Neutralization <br> reaction: | $\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}} \mathbf{H}(\mathbf{a q})+\mathbf{O H}^{-}(\mathbf{a q}) \xrightarrow{\mathbf{1 0 0 \%}}$ | $\mathbf{H}_{\mathbf{2}} \mathbf{O}(\boldsymbol{l})+\mathbf{C H}_{\mathbf{3}} \mathbf{C O}_{\mathbf{2}}{ }^{-}(\boldsymbol{a q})$ |  |
| :--- | :---: | :---: | :---: |
| Before reaction (mol) | 0.10 | 0.01 | 0.10 |
| Change (mol) | -0.01 | -0.01 | +0.01 |
| After reaction (mol) | 0.09 | $\sim 0$ | 0.11 |

If we assume that the solution volume remains constant at 1.00 L , the concentrations of the buffer components after neutralization are

$$
\begin{aligned}
& {\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]=\frac{0.09 \mathrm{~mol}}{1.00 \mathrm{~L}}=0.09 \mathrm{M}} \\
& {\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]=\frac{0.11 \mathrm{~mol}}{1.00 \mathrm{~L}}=0.11 \mathrm{M}}
\end{aligned}
$$

Substituting these concentrations into the expression for $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$, we can then calculate the pH :

$$
\begin{aligned}
{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right] } & =K_{\mathrm{a}} \frac{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]}{\left[\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}\right]} \\
& =\left(1.8 \times 10^{-5}\right)\left(\frac{0.09}{0.11}\right)=1.5 \times 10^{-5} \mathrm{M}
\end{aligned}
$$

$$
\mathrm{pH}=4.82
$$

Adding 0.01 mol of NaOH changes $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$by only a small amount because the concentration ratio [weak acid]/[conjugate base] changes by only a small amount, from unity to $9 / 11$ (Figure 16.3a). The corresponding change in pH , from 4.74 to 4.82 , is only 0.08 pH unit.


## Addition of $\mathrm{H}_{3} \mathrm{O}^{+}$to a Buffer

Now suppose that we add 0.01 mol of HCl to 1.00 L of the 0.10 M acetic acid- 0.10 M sodium acetate buffer solution. The added strong acid will convert 0.01 mol of acetate ions to 0.01 mol of acetic acid because of the neutralization reaction

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q) \xrightarrow{100 \%} \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)
$$

The concentrations after neutralization will be $\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]=0.11 \mathrm{M}$ and $\left[\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}\right]=0.09 \mathrm{M}$, and the pH of the solution will be 4.66:

$$
\begin{aligned}
& \begin{aligned}
{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right] } & =K_{\mathrm{a}} \frac{\left[\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right]}{\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]} \\
& =\left(1.8 \times 10^{-5}\right)\left(\frac{0.11}{0.09}\right)=2.2 \times 10^{-5} \mathrm{M}
\end{aligned} \\
& \mathrm{pH}=4.66
\end{aligned}
$$

Again, the change in pH , from 4.74 to 4.66 , is small because the concentration ratio [weak acid]/[conjugate base] remains close to its original value (Figure 16.3b).

## Buffer Capacity

To appreciate the ability of a buffer solution to maintain a nearly constant pH , let's contrast the behavior of the 0.10 M acetic acid -0.10 M sodium acetate buffer with that of a $1.8 \times 10^{-5} \mathrm{M} \mathrm{HCl}$ solution. This very dilute HCl solution has the same $\mathrm{pH}(4.74)$ as the buffer solution, but it doesn't have the capacity to soak up added is used to calculate the pH of a buffer solution as shown in the next section.

4 FIGURE 16.3 (a) When $\mathrm{OH}^{-}$is added to a buffer solution, some of the weak acid is neutralized and thus converted to the conjugate base. (b) When $\mathrm{H}_{3} \mathrm{O}^{+}$is added to a buffer solution, some of the conjugate base is neutralized and thus converted to the weak acid. However, as long as the concentration ratio [weak acid]/[conjugate base] stays close to its original value, $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$and the pH won't change very much in either of these cases.
-


A FIGURE 16.4 The color of each solution is due to the presence of a few drops of methyl red, an acid-base indicator that is red at pH less than about 5.4 and yellow at pH greater than about 5.4. (a) 1.00 L of $1.8 \times 10^{-5} \mathrm{M} \mathrm{HCl}(\mathrm{pH}=4.74)$; (b) the solution from part (a) turns yellow ( $\mathrm{pH}>5.4$ ) after addition of only a few drops of 0.10 M NaOH ; (c) 1.00 L of a 0.10 M acetic acid- 0.10 M sodium acetate buffer solution ( $\mathrm{pH}=4.74$ ); (d) the solution from part (c) is still red ( $\mathrm{pH}<5.4$ ) after addition of 100 mL of 0.10 M NaOH .

Bassam Z. Shakhashiri, "Buffering Action and Capacity," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 173-185.
acid or base. For example, if we add 0.01 mol of solid NaOH to 1.00 L of $1.8 \times 10^{-5} \mathrm{M} \mathrm{HCl}$, a negligible amount of $\mathrm{OH}^{-}\left(1.8 \times 10^{-5} \mathrm{~mol}\right)$ is neutralized and the concentration of $\mathrm{OH}^{-}$after neutralization is $0.01 \mathrm{~mol} / 1.00 \mathrm{~L}=0.01 \mathrm{M}$. As a result, the pH rises from 4.74 to 12.0:

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{\left(1.0 \times 10^{-14}\right)}{(0.01)}=1 \times 10^{-12} \mathrm{M}} \\
& \mathrm{pH}=12.0
\end{aligned}
$$

The abilities of the HCl solution and the buffer solution to absorb added base are contrasted in Figure 16.4.


We sometimes talk about the buffering ability of a solution using the term buffer capacity as a measure of the amount of acid or base that the solution can absorb without a significant change in pH . Buffer capacity is also a measure of how little the pH changes with the addition of a given amount of acid or base. Buffer capacity depends on how many moles of weak acid and conjugate base are present. For equal volumes of solution, the more concentrated the solution, the greater the buffer capacity. For solutions having the same concentration, the greater the volume, the greater the buffer capacity.

KEY CONCEPT PROBLEM 16.6 The following pictures represent solutions that contain a weak acid HA and/or its sodium salt NaA. ( $\mathrm{Na}^{+}$ions and solvent water molecules have been omitted for clarity.)

(a) Which of the solutions are buffer solutions?
(b) Which solution has the greatest buffer capacity?

PROBLEM 16.7 Calculate the pH of 0.100 L of a buffer solution that is 0.25 M in HF and 0.50 M in NaF . What is the change in pH on addition of the following?
(a) 0.002 mol of $\mathrm{HNO}_{3}$
(b) 0.004 mol of KOH

- PROBLEM 16.8 Calculate the change in pH when 0.002 mol of $\mathrm{HNO}_{3}$ is added to 0.100 L of a buffer solution that is 0.050 M in HF and 0.100 M in NaF. Does this solution have more or less buffer capacity than the one in Problem 16.7?


## 16.4 | The Henderson-Hasselbalch Equation

We saw in Section 16.3 that the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration in a buffer solution depends on the dissociation constant of the weak acid and on the concentration ratio [weak acid]/[conjugate base]:

$$
\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=K_{\mathrm{a}} \frac{[\text { Acid }]}{[\text { Base }]}
$$

This equation can be rewritten in logarithmic form by taking the negative base-10 logarithm of both sides:

$$
\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=-\log K_{\mathrm{a}}-\log \frac{[\text { Acid }]}{[\text { Base }]}
$$

If we then define $\mathrm{p} K_{\mathrm{a}}=-\log K_{\mathrm{a}}$ by analogy with $\mathrm{pH}=-\log \left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$and recognize that

$$
-\log \frac{[\text { Acid }]}{[\text { Base }]}=\log \frac{[\text { Base }]}{[\text { Acid }]}
$$

we obtain an expression called the Henderson-Hasselbalch equation:
Henderson-Hasselbalch equation $\quad \mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+\log \frac{\text { [Base] }}{\text { [Acid] }}$
The Henderson-Hasselbalch equation says that the pH of a buffer solution has a value close to the $\mathrm{p} K_{\mathrm{a}}$ of the weak acid, differing only by the amount log [base]/[acid]. When [base] $/$ acid] $=1$, then $\log$ [base]/[acid] $=0$, and the pH equals the $\mathrm{p} K_{\mathrm{a}}$.

The real importance of the Henderson-Hasselbalch equation, particularly in biochemistry, is that it tells us how the pH affects the percent dissociation of a weak acid. Suppose, for example, that you have a solution containing the amino acid glycine, one of the molecules from which proteins are made, and that the pH of the solution is 2.00 pH units greater than the $\mathrm{p} K_{\mathrm{a}}$ of glycine:


$$
\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+2.00=11.60
$$

Since $\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+2.00$, then $\log [$ base $] /[$ acid $]=2.00$, and [base] $/[$ acid $]=$ $1.0 \times 10^{2}=100 / 1$. According to the Henderson-Hasselbalch equation, therefore, 100 of every 101 glycine molecules are dissociated, which corresponds to $99 \%$ dissociation:

Henry N. Po and N. M. Senozan, "The HendersonHasselbalch Equation: Its History and Limitations," J. Chem. Educ., Vol. 78, 2001, 1499-1503.

v
The acid and base in this expression refers to a conjugate acid/base pair, such as $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H} / \mathrm{CH}_{3} \mathrm{CO}_{2}^{-}$or $\mathrm{NH}_{4}{ }^{+} / \mathrm{NH}_{3} . \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ is the conjugate acid of $\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}$and $\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}$is the conjugate base of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$. Similarly, $\mathrm{NH}_{4}{ }^{+}$is the conjugate acid of $\mathrm{NH}_{3}$ and $\mathrm{NH}_{3}$ is the conjugate base of $\mathrm{NH}_{4}{ }^{+}$.

$\checkmark$
This expression contains a ratio of the concentration of a conjugate base to the concentration of its conjugate acid remaining after reaction. Because the base and its conjugate acid are contained in the same volume, moles of base and conjugate acid remaining after reaction can be used instead of molarities.


Glycine

$$
\begin{aligned}
& \log \frac{[\text { Base }]}{[\text { Acid }]}=\mathrm{pH}-\mathrm{p} K_{\mathrm{a}}=2.00 \\
& \frac{[\text { Base }]}{[\text { Acid }]}=1.0 \times 10^{2}=\frac{100}{1} \quad 99 \% \text { dissociation }
\end{aligned}
$$



A FIGURE 16.5 Prepackaged buffer solutions of known pH , and solid ingredients for preparing buffer solutions of known pH .


The Henderson-Hasselbalch equation thus gives the following relationships:

$$
\begin{array}{ll}
\text { At } \mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+2.00: & \frac{[\text { Base }]}{[\text { Acid }]}=1.0 \times 10^{2}=\frac{100}{1} \\
99 \% \text { dissociation } \\
\text { At } \mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+1.00: & \frac{[\text { Base }]}{[\text { Acid] }}=1.0 \times 10^{1}=\frac{10}{1} \\
91 \% \text { dissociation } \\
\text { At } \mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+0.00: & \frac{[\text { Base }]}{[\text { Acid] }}=1.0 \times 10^{0}=\frac{1}{1} \\
\text { At } \mathrm{pH}=\mathrm{p} K_{\mathrm{a}}-1.00: & \frac{[\text { Base }]}{[\text { Acid] }}=1.0 \times 10^{-1}=\frac{1}{10} \\
\text { At } \mathrm{pH}=\mathrm{p} K_{\mathrm{a}}-2.00: & \frac{\text { [Base] }}{[\text { Acid] }}=1.0 \times 10^{-2}=\frac{1}{100} \\
1 \% \text { dissociation dissociation }
\end{array}
$$

The Henderson-Hasselbalch equation also tells us how to prepare a buffer solution with a given pH . The general idea is to select a weak acid whose $\mathrm{p} K_{\mathrm{a}}$ is close to the desired pH and then adjust the [base]/[acid] ratio to the value specified by the Henderson-Hasselbalch equation. For example, to prepare a buffer having pH near 7 , we might use the $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}-\mathrm{HPO}_{4}{ }^{2-}$ conjugate acid-base pair because $\mathrm{p} K_{\mathrm{a}}$ for $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$is $-\log \left(6.2 \times 10^{-8}\right)=7.21$. Similarly, a mixture of $\mathrm{NH}_{4} \mathrm{Cl}$ and $\mathrm{NH}_{3}$ would be a good choice for a buffer having pH near 9 because $\mathrm{p} K_{\mathrm{a}}$ for $\mathrm{NH}_{4}{ }^{+}$is $-\log \left(5.6 \times 10^{-10}\right)=9.25$. As a rule of thumb, the $\mathrm{p} K_{\mathrm{a}}$ of the weak acid component of a buffer should be within $\pm 1 \mathrm{pH}$ unit of the desired pH .

Because buffer solutions are widely used in the laboratory and in medicine, prepackaged buffers having a variety of precisely known pH values are commercially available (Figure 16.5). The manufacturer prepares these buffers by choosing a buffer system having an appropriate $\mathrm{p} K_{\mathrm{a}}$ value and then adjusting the amounts of the ingredients so that the [base]/[acid] ratio has the proper value.

The pH of a buffer solution does not depend on the volume of the solution. Because a change in solution volume changes the concentrations of the acid and base by the same amount, the [base]/[acid] ratio and the pH remain unchanged. As a result, the volume of water used to prepare a buffer solution is not critical, and you can dilute a buffer without a change in pH . The pH depends only on $\mathrm{p} K_{\mathrm{a}}$ and on the relative molar amounts of weak acid and conjugate base.

## Worked Example 16.4

(a) Use the Henderson-Hasselbalch equation to calculate the pH of a buffer solution that is 0.45 M in $\mathrm{NH}_{4} \mathrm{Cl}$ and 0.15 M in $\mathrm{NH}_{3}$.
(b) How would you prepare an $\mathrm{NH}_{4} \mathrm{Cl}-\mathrm{NH}_{3}$ buffer that has a pH of 9.00 ?

## Strategy

(a) We've already solved this problem by another method in Worked Example 16.2. Now that we've discussed equilibria in buffer solutions, though, we can use the Henderson-Hasselbalch equation as a shortcut. Since $\mathrm{NH}_{4}{ }^{+}$is the weak acid in an $\mathrm{NH}_{4}{ }^{+}-\mathrm{NH}_{3}$ buffer solution, we need to find the $\mathrm{p} K_{\mathrm{a}}$ for $\mathrm{NH}_{4}{ }^{+}$from the tabulated $K_{\mathrm{b}}$ value for $\mathrm{NH}_{3}$ (Appendix C). Then, substitute $\left[\mathrm{NH}_{3}\right],\left[\mathrm{NH}_{4}{ }^{+}\right]$, and the $\mathrm{p} K_{\mathrm{a}}$ value into the Henderson-Hasselbalch equation to find the pH .
(b) Use the Henderson-Hasselbalch equation to calculate the $\left[\mathrm{NH}_{3}\right] /\left[\mathrm{NH}_{4}{ }^{+}\right]$ratio from the desired pH and the $\mathrm{p} K_{\mathrm{a}}$ value for $\mathrm{NH}_{4}{ }^{+}$.

## Solution

(a) Since $K_{\mathrm{b}}$ for $\mathrm{NH}_{3}$ is $1.8 \times 10^{-5}, K_{\mathrm{a}}$ for $\mathrm{NH}_{4}{ }^{+}$is $5.6 \times 10^{-10}$ and $\mathrm{p} K_{\mathrm{a}}=9.25$.

$$
\begin{aligned}
& K_{\mathrm{a}}=\frac{K_{\mathrm{w}}}{K_{\mathrm{b}}}=\frac{1.0 \times 10^{-14}}{1.8 \times 10^{-5}}=5.6 \times 10^{-10} \\
& \mathrm{p} K_{\mathrm{a}}=-\log K_{\mathrm{a}}=-\log \left(5.6 \times 10^{-10}\right)=9.25
\end{aligned}
$$

Since $[$ base $]=\left[\mathrm{NH}_{3}\right]=0.15 \mathrm{M}$ and $[$ acid $]=\left[\mathrm{NH}_{4}{ }^{+}\right]=0.45 \mathrm{M}$,

$$
\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+\log \frac{[\text { Base }]}{[\text { Acid }]}=9.25+\log \left(\frac{0.15}{0.45}\right)=9.25-0.48=8.77
$$

The pH of the buffer solution is 8.77 .
(b) Rearrange the Henderson-Hasselbalch equation to obtain an expression for the relative amounts of $\mathrm{NH}_{3}$ and $\mathrm{NH}_{4}{ }^{+}$in a solution having $\mathrm{pH}=9.00$ :

$$
\log \frac{[\text { Base }]}{[\text { Acid }]}=\mathrm{pH}-\mathrm{p} K_{\mathrm{a}}=9.00-9.25=-0.25
$$

Therefore,

$$
\frac{\left[\mathrm{NH}_{3}\right]}{\left[\mathrm{NH}_{4}^{+}\right]}=\operatorname{antilog}(-0.25)=10^{-0.25}=0.56
$$

The solution must contain 0.56 mol of $\mathrm{NH}_{3}$ for every 1.00 mol of $\mathrm{NH}_{4} \mathrm{Cl}$, but the volume of the solution isn't critical. One way of preparing the buffer would be to combine 1.00 mol of $\mathrm{NH}_{4} \mathrm{Cl}\left(53.5 \mathrm{~g}\right.$ ) with 0.56 mol of $\mathrm{NH}_{3}$ (say, 560 mL of $1.00 \mathrm{M} \mathrm{NH}_{3}$ ).
$\checkmark$ BALLPARK CHECK A common error in using the Henderson-Hasselbalch equation is to invert the [base]/[acid] ratio. It is therefore wise to check that your answer makes chemical sense. If the concentrations of the acid and its conjugate base are equal, the pH will equal the $\mathrm{p} K_{\mathrm{a}}$. If the acid predominates, the pH will be less than the $\mathrm{p} K_{\mathrm{a}}$, and if the conjugate base predominates, the pH will be greater than the $\mathrm{p} K_{\mathrm{a}}$. In part (a), [acid] $=\left[\mathrm{NH}_{4}{ }^{+}\right]$is greater than [base] $=\left[\mathrm{NH}_{3}\right]$, and so the calculated pH (8.77) should be less than the $\mathrm{p} K_{\mathrm{a}}$ (9.25). In part (b), the desired pH is less than the $\mathrm{p} K_{\mathrm{a}}$, so the buffer should contain more moles of acid than base, in agreement with the solution.

## Worked Example 16.5

What $\left[\mathrm{NH}_{3}\right] /\left[\mathrm{NH}_{4}{ }^{+}\right]$ratio is required for a buffer solution that has $\mathrm{pH}=7.00$ ? Why is a mixture of $\mathrm{NH}_{3}$ and $\mathrm{NH}_{4} \mathrm{Cl}$ a poor choice for a buffer having $\mathrm{pH}=7.00$ ?

## Strategy

We can calculate the required $\left[\mathrm{NH}_{3}\right] /\left[\mathrm{NH}_{4}{ }^{+}\right]$ratio from the Henderson-Hasselbalch equation.

## Solution

$$
\begin{aligned}
& \log \frac{\left[\mathrm{NH}_{3}\right]}{\left[\mathrm{NH}_{4}{ }^{+}\right]}=\mathrm{pH}-\mathrm{p} K_{\mathrm{a}}=7.00-9.25=-2.25 \\
& \frac{\left[\mathrm{NH}_{3}\right]}{\left[\mathrm{NH}_{4}{ }^{+}\right]}=\operatorname{antilog}(-2.25)=10^{-2.25}=5.6 \times 10^{-3}
\end{aligned}
$$

For a typical value of $\left[\mathrm{NH}_{4}{ }^{+}\right]$-say, 1.0 M -the $\mathrm{NH}_{3}$ concentration would have to be very small $(0.0056 \mathrm{M})$. Such a solution is a poor buffer because it has little capacity to absorb added acid. Also, because the $\left[\mathrm{NH}_{3}\right] /\left[\mathrm{NH}_{4}{ }^{+}\right]$ratio is far from unity, addition of a small amount of $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$will result in a large change in pH .

Ballpark Check Because the desired pH is much less than the $\mathrm{p} K_{\mathrm{a}}$ value, the buffer must contain much more weak acid than conjugate base, in agreement with the solution.


Serine
Acid-Base Titration movie

Dennis Barnum, "Predicting Acid-Base Titration Curves Without Calculations," J. Chem. Educ., Vol 76, 1999, 938-942.

- PROBLEM 16.9 Use the Henderson-Hasselbalch equation to calculate the pH of a buffer solution prepared by mixing equal volumes of $0.20 \mathrm{M} \mathrm{NaHCO}_{3}$ and $0.10 \mathrm{M} \mathrm{Na}_{2} \mathrm{CO}_{3}$. ( $K_{\mathrm{a}}$ values are given in Appendix C.)
- PROBLEM 16.10 Give a recipe for preparing a $\mathrm{NaHCO}_{3}-\mathrm{Na}_{2} \mathrm{CO}_{3}$ buffer solution that has $\mathrm{pH}=10.40$.

PROBLEM 16.11 Suppose you are performing an experiment that requires a constant pH of 7.50 . Suggest an appropriate buffer system based on the $K_{\mathrm{a}}$ values in Appendix C.

- PROBLEM 16.12 The $\mathrm{p} K_{\mathrm{a}}$ of the amino acid serine is 9.15 . At what pH is serine:
(a) $66 \%$ dissociated?
(b) 5\% dissociated?


Serine
$\mathrm{p} K_{\mathrm{a}}=9.15$

## $16.5 \mid \mathrm{pH}$ Titration Curves

In a typical acid-base titration (Section 3.10), a solution containing a known concentration of base (or acid) is added slowly from a buret to a second solution containing an unknown concentration of acid (or base). The progress of the titration is monitored, either by using a pH meter (Figure 16.6a) or by observing the color of a suitable acid-base indicator. With a pH meter, you can record data to produce a pH titration curve, a plot of the pH of the solution as a function of the volume of added titrant (Figure 16.6b).


A FIGURE 16.6 A strong acid-strong base titration curve. (a) In this pH titration, 0.100 M NaOH is added slowly from a buret to an HCl solution of unknown concentration. The pH of the solution is measured with a pH meter and is recorded as a function of the volume of NaOH added. (b) The pH titration curve for titration of 40.0 mL of 0.100 M HCl with 0.100 M NaOH . The pH increases gradually in the regions before and after the equivalence point, but increases rapidly in the region near the equivalence point. The equivalence point comes after addition of 40.0 mL of 0.100 M NaOH . The pH at the equivalence point is 7.00 .

Why study titration curves? The shape of a pH titration curve makes it possible to identify the equivalence point in a titration, the point at which stoichiometrically equivalent quantities of acid and base have been mixed together. Knowing the shape of the titration curve is also useful in selecting a suitable indicator to signal the equivalence point. We'll explore both of these points later.

We can calculate pH titration curves using the principles of aqueous solution equilibria. To understand why titration curves have certain characteristic shapes, let's calculate these curves for four important types of titration: (1) strong acid-strong base, (2) weak acid-strong base, (3) weak base-strong acid, and (4) polyprotic acid-strong base. For convenience, we'll express amounts of solute in millimoles ( mmol ) and solution volumes in milliliters ( mL ). Molar concentration can thus be expressed in $\mathrm{mmol} / \mathrm{mL}$, a unit that is equivalent to $\mathrm{mol} / \mathrm{L}$ :

$$
\text { Molarity }=\frac{\mathrm{mmol} \text { of solute }}{\mathrm{mL} \text { of solution }}=\frac{10^{-3} \mathrm{~mol} \text { of solute }}{10^{-3} \mathrm{~L} \text { of solution }}=\frac{\mathrm{mol} \text { of solute }}{\mathrm{L} \text { of solution }}
$$

## 16.6 | Strong Acid-Strong Base Titrations

As an example of a strong acid-strong base titration, let's consider the titration of 40.0 mL of 0.100 M HCl with 0.100 M NaOH . We'll calculate the pH at selected points in the course of the titration to illustrate the procedures we use to calculate the entire curve.

1. Before Addition of Any NaOH Since HCl is a strong acid, the initial concentration of $\mathrm{H}_{3} \mathrm{O}^{+}$is 0.100 M and the pH is 1.00 . (We've rounded the value of the pH to two significant figures.)
2. Before the Equivalence Point Let's calculate the pH after addition of 10.0 mL of 0.100 M NaOH . The added $\mathrm{OH}^{-}$ions will decrease $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$because of the neutralization reaction

$$
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) \xrightarrow{100 \%} 2 \mathrm{H}_{2} \mathrm{O}(l)
$$

The number of millimoles of $\mathrm{H}_{3} \mathrm{O}^{+}$present initially is the product of the initial volume of HCl and its molarity:

$$
\text { mmol } \mathrm{H}_{3} \mathrm{O}^{+} \text {initial }=(40.0 \mathrm{~mL})(0.100 \mathrm{mmol} / \mathrm{mL})=4.00 \mathrm{mmol}
$$

Similarly, the number of millimoles of $\mathrm{OH}^{-}$added is the product of the volume of NaOH added and its molarity:

$$
\mathrm{mmol} \mathrm{OH}{ }^{-} \text {added }=(10.0 \mathrm{~mL})(0.100 \mathrm{mmol} / \mathrm{mL})=1.00 \mathrm{mmol}
$$

For each mmol of $\mathrm{OH}^{-}$added, an equal amount of $\mathrm{H}_{3} \mathrm{O}^{+}$will disappear because of the neutralization reaction. The number of millimoles of $\mathrm{H}_{3} \mathrm{O}^{+}$ remaining after neutralization is therefore

$$
\begin{aligned}
\text { mmol } \mathrm{H}_{3} \mathrm{O}^{+} \text {after neutralization } & =\mathrm{mmol} \mathrm{H}_{3} \mathrm{O}^{+}{ }_{\text {initial }}-\mathrm{mmol} \mathrm{OH}^{-} \text {added } \\
& =4.00 \mathrm{mmol}-1.00 \mathrm{mmol}=3.00 \mathrm{mmol}
\end{aligned}
$$

We've carried out this calculation using amounts of acid and base (mmol) rather than concentrations (molarity) because the volume changes as the titration proceeds. If we divide the number of millimoles of $\mathrm{H}_{3} \mathrm{O}^{+}$after neutralization by the total volume (now $40.0+10.0=50.0 \mathrm{~mL}$ ), we obtain $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$ after neutralization:

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right] \text {after neutralization }=\frac{3.00 \mathrm{mmol}}{50.0 \mathrm{~mL}}=6.00 \times 10^{-2} \mathrm{M}} \\
& \mathrm{pH}=-\log \left(6.00 \times 10^{-2}\right)=1.22
\end{aligned}
$$



v
The change in pH seen in a titration curve is due primarily to the neutralization reaction, but it is also due to the dilution effect of mixing two solutions. Volume changes constantly during a titration.

This same procedure can be used to calculate the pH at other points prior to the equivalence point, giving the results summarized in Table 16.1.

TABLE 16.1 Sample Results for pH Calculations at Various Points in the Titration of 40.0 mL of 0.100 M HCl with 0.100 M NaOH

| $\mathbf{m L}$ <br> NaOH <br> Added | mmol <br> $\mathbf{O H}^{-}$ <br> Added | mmol $\mathrm{H}_{3} \mathrm{O}^{+}$ <br> After <br> Neutr. | Total <br> Volume (mL) | $\left[\mathbf{H}_{3} \mathbf{O}^{+}\right]$ <br> After <br> Neutr. | pH |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Before the equivalence point: |  |  |  |  |  |
| 0.0 | 0.0 | 4.00 | 40.0 | $1.00 \times 10^{-1}$ | 1.00 |
| 10.0 | 1.00 | 3.00 | 50.0 | $6.00 \times 10^{-2}$ | 1.22 |
| 20.0 | 2.00 | 2.00 | 60.0 | $3.33 \times 10^{-2}$ | 1.48 |
| 30.0 | 3.00 | 1.00 | 70.0 | $1.43 \times 10^{-2}$ | 1.84 |
| 39.0 | 3.90 | 0.10 | 79.0 | $1.27 \times 10^{-3}$ | 2.90 |
| 39.9 | 3.99 | 0.01 | 79.9 | $1.3 \times 10^{-4}$ | 3.9 |
| At the equivalence point: |  |  |  |  |  |
| 40.0 | 4.00 | 0.00 | 80.0 | $1.0 \times 10^{-7}$ | 7.00 |

Beyond the equivalence point:

|  |  | mmol OH <br>  <br> After Neutr. |  | $\left[\mathbf{O H}^{-}\right]$ <br> After Neutr. |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 40.1 | 4.01 | 0.01 | 80.1 | $1.2 \times 10^{-4}$ | $8.3 \times 10^{-11}$ | 10.1 |
| 41.0 | 4.10 | 0.10 | 81.0 | $1.2 \times 10^{-3}$ | $8.3 \times 10^{-12}$ | 11.08 |
| 50.0 | 5.00 | 1.00 | 90.0 | $1.11 \times 10^{-2}$ | $9.0 \times 10^{-13}$ | 12.05 |
| 60.0 | 6.00 | 2.00 | 100.0 | $2.00 \times 10^{-2}$ | $5.0 \times 10^{-13}$ | 12.30 |
| 70.0 | 7.00 | 3.00 | 110.0 | $2.73 \times 10^{-2}$ | $3.7 \times 10^{-13}$ | 12.43 |
| 80.0 | 8.00 | 4.00 | 120.0 | $3.33 \times 10^{-2}$ | $3.0 \times 10^{-13}$ | 12.52 |

Titration curve points of particular interest are pH values (1) before any base (or acid) is added, (2) before the equivalence point (especially halfway to the equivalence point), (3) at the equivalence point, and (4) beyond the equivalence point.
3. At the Equivalence Point After addition of 40.0 mL of 0.100 M NaOH , we have added $(40.0 \mathrm{~mL})(0.100 \mathrm{mmol} / \mathrm{mL})=4.00 \mathrm{mmol}$ of NaOH , which is just enough $\mathrm{OH}^{-}$to neutralize all the 4.00 mmol of HCl initially present. This is the equivalence point of the titration, and the pH is 7.00 because the solution contains only water and NaCl , a salt derived from a strong base and a strong acid.
4. Beyond the Equivalence Point After addition of 60.0 mL of 0.100 M NaOH , we have added $(60.0 \mathrm{~mL})(0.100 \mathrm{mmol} / \mathrm{mL})=6.00 \mathrm{mmol}$ of NaOH , which is more than enough to neutralize the 4.00 mmol of HCl initially present. Consequently, an excess of $\mathrm{OH}^{-}(6.00-4.00=2.00 \mathrm{mmol})$ is present. Since the total volume is now $40.0+60.0=100.0 \mathrm{~mL}$, the concentration of $\mathrm{OH}^{-}$is

$$
\left[\mathrm{OH}^{-}\right] \text {after neutralization }=\frac{2.00 \mathrm{mmol}}{100.0 \mathrm{~mL}}=2.00 \times 10^{-2} \mathrm{M}
$$

The $\mathrm{H}_{3} \mathrm{O}^{+}$concentration and the pH are

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{2.00 \times 10^{-2}}=5.0 \times 10^{-13} \mathrm{M}} \\
& \mathrm{pH}=-\log \left(5.0 \times 10^{-13}\right)=12.30
\end{aligned}
$$

Sample results for pH calculations at other places beyond the equivalence point are also included in Table 16.1.

Plotting the pH data in Table 16.1 as a function of milliliters of NaOH added gives the pH titration curve in Figure 16.6b (page 678). This curve exhibits a gradual increase in pH in the regions before and after the equivalence point but a very
sharp increase in pH in the region near the equivalence point. Thus, when the volume of added NaOH increases from 39.9 to $40.1 \mathrm{~mL}(0.2 \mathrm{~mL}$ is only about 4 drops from a buret), the pH increases from 3.9 to 10.1 (Table 16.1). This very sharp increase in pH in the region of the equivalence point is characteristic of the titration curve for any strong acid-strong base reaction. It is this feature that allows us to identify the equivalence point when the concentration of the acid is unknown.

The pH curve for the titration of a strong base with a strong acid is similar except that the initial pH is high and then decreases as acid is added.

- PROBLEM 16.13 Calculate the pH of the solution resulting from titration of 40.0 mL of 0.100 M HCl with (a) 35.0 mL and (b) 45.0 mL of 0.100 M NaOH . Are your results consistent with the pH data in Table 16.1?
- PROBLEM 16.14 A 40.0 mL volume of 0.100 M NaOH is titrated with 0.0500 M HCl . Calculate the pH after addition of the following volumes of acid:
(a) 60.0 mL
(b) 80.2 mL
(c) 100.0 mL


## 16.7 | Weak Acid-Strong Base Titrations

As an example of a weak acid-strong base titration, let's consider the titration of 40.0 mL of 0.100 M acetic acid with 0.100 M NaOH . Calculation of the pH at selected points along the titration curve is straightforward because we've already met all the equilibrium problems that arise.

1. Before Addition of Any NaOH The equilibrium problem at this point is the familiar one of calculating the pH of a solution of a weak acid. The calculated pH of 0.100 M acetic acid is 2.89 .
2. Before the Equivalence Point Since acetic acid is largely undissociated and NaOH is completely dissociated, the neutralization reaction is

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{OH}^{-}(a q) \xrightarrow{100 \%} \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)
$$

After addition of 20.0 mL of 0.100 M NaOH , we have added ( 20.0 mL ) $(0.100 \mathrm{mmol} / \mathrm{mL})=2.00 \mathrm{mmol}$ of NaOH , which is enough $\mathrm{OH}^{-}$to neutralize exactly half the 4.00 mmol of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ present initially. Neutralization gives a buffer solution that contains 2.00 mmol of $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$and $4.00-2.00=2.00$ mmol of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$. Consequently, the [base]/[acid] ratio is unity, and $\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}:$

$$
\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+\log \frac{[\text { Base }]}{[\text { Acid }]}=\mathrm{p} K_{\mathrm{a}}=4.74
$$

3. At the Equivalence Point The equivalence point is reached after adding 40.0 mL of $0.100 \mathrm{M} \mathrm{NaOH}(4.00 \mathrm{mmol})$, which is just enough $\mathrm{OH}^{-}$to neutralize all the 4.00 mmol of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ initially present. After neutralization, the solution contains $0.0500 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$:

$$
\left[\mathrm{Na}^{+}\right]=\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]=\frac{4.00 \mathrm{mmol}}{40.0 \mathrm{~mL}+40.0 \mathrm{~mL}}=0.0500 \mathrm{M}
$$

Because $\mathrm{Na}^{+}$is neither an acid nor a base and $\mathrm{CH}_{3} \mathrm{CO}_{2}{ }^{-}$is a weak base, we have a basic salt solution (Section 15.14), whose pH can be calculated as 8.72 by the method outlined in Worked Example 15.15. For a weak monoprotic acid-strong base titration, the pH at the equivalence point is always greater than 7 because the anion of the weak acid is a base.
4. After the Equivalence Point After addition of 60.0 mL of 0.100 M NaOH , we have added $(60.0 \mathrm{~mL})(0.100 \mathrm{mmol} / \mathrm{mL})=6.00 \mathrm{mmol}$ of NaOH , which is more than


A A strong base-strong acid titration curve. The curve shown is for titration of 40.0 mL of 0.100 M NaOH with 0.100 M HCl . The pH at the equivalence point is 7.00 .


0For an acid-base titration the pH at the equivalence point will be $>7$ if the base is stronger than the acid, $=7$ if the acid and base have equal strengths, and $<7$ if the acid is stronger than the base.

Weak Acid-Strong Base Titration activity
enough $\mathrm{OH}^{-}$to neutralize the 4.00 mmol of $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ present initially. The total volume is $40.0+60.0=100.0 \mathrm{~mL}$, and the concentrations after neutralization are

$$
\begin{aligned}
& {\left[\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right]=\frac{4.00 \mathrm{mmol}}{100.0 \mathrm{~mL}}=0.0400 \mathrm{M}} \\
& {\left[\mathrm{OH}^{-}\right]=\frac{6.00 \mathrm{mmol}-4.00 \mathrm{mmol}}{100.0 \mathrm{~mL}}=0.0200 \mathrm{M}}
\end{aligned}
$$

The principal reaction is the same as that at the equivalence point:

$$
\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+\mathrm{OH}^{-}(a q)
$$

In this case, however, $\left[\mathrm{OH}^{-}\right]$from the principal reaction is negligible compared with $\left[\mathrm{OH}^{-}\right]$from the excess NaOH . The hydronium ion concentration and the pH can be calculated from that $\left[\mathrm{OH}^{-}\right]$:

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{0.0200}=5.0 \times 10^{-13} \mathrm{M}} \\
& \mathrm{pH}=12.30
\end{aligned}
$$

In general, $\left[\mathrm{OH}^{-}\right]$from the reaction of the anion of a weak acid with water is negligible beyond the equivalence point, and the pH is determined by the concentration of $\mathrm{OH}^{-}$from the excess NaOH .

The results of pH calculations for the titration of $0.100 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ with 0.100 M NaOH are plotted in Figure 16.7. Comparison of the titration curves for the weak acid-strong base titration and the strong acid-strong base case shows several significant differences:


A FIGURE 16.7 A weak acid-strong base titration curve (a) compared with a strong acid-strong base curve (b). The curves shown are for titration of (a) 40.0 mL of $0.100 \mathrm{M} \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ with 0.100 M NaOH (blue curve) and (b) 40.0 mL of 0.100 M HCl with 0.100 M NaOH (red curve). The pH ranges in which the acid-base indicators phenolphthalein and methyl red change color are indicated. Note that phenolphthalein is an excellent indicator for the weak acid-strong base titration because the equivalence point (a) is at pH 8.72 ; methyl red is an unsatisfactory indicator because it changes color well before the equivalence point. Either phenolphthalein or methyl red can be used for the strong acid-strong base titration because the curve rises very steeply in the region of the equivalence point (b) at pH 7.00 .

- The initial rise in pH is greater for the titration of the weak acid, but the curve then becomes more level in the region midway to the equivalence point. Both effects are due to the buffering action of the weak acid-conjugate base mixture. The curve has minimum slope exactly halfway to the equivalence point, where the buffering action is maximized and the $\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}$ for the weak acid.
- The increase in pH in the region near the equivalence point is smaller than in the strong acid-strong base case. The weaker the acid, the smaller the increase in the pH , as illustrated in Figure 16.8.
- The pH at the equivalence point is greater than 7 because the anion of a weak acid is a base.


Beyond the equivalence point, the curves for the weak acid-strong base and strong acid-strong base titrations are identical because the pH in both cases is determined by the concentration of $\mathrm{OH}^{-}$from the excess NaOH .

Figure 16.7 shows how knowing the shape of a pH titration curve makes it possible to select a suitable acid-base indicator to signal the equivalence point of a titration. Phenolphthalein is an excellent indicator for the $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}-\mathrm{NaOH}$ titration because the pH at the equivalence point (8.72) falls within the pH range (8.2-9.8) in which phenolphthalein changes color. Methyl red, however, is an unacceptable indicator for this titration because the pH range in which it changes color (4.2-6.0) corresponds to a pH well before the equivalence point. Anyone who tried to determine the acetic acid content in a solution of unknown concentration would badly underestimate the amount of acid present if methyl red were used as the indicator.

Either phenolphthalein or methyl red can be used as the indicator for a strong acid-strong base titration. The increase in pH in the region of the equivalence point is so steep that any indicator changing color in the pH range $4-10$ can be used without making a significant error in locating the equivalence point.

FIGURE 16.8 Various weak acid-strong base pH titration curves. The curves shown are for titration of 40.0 mL of 0.100 M solutions of various weak acids with 0.100 M NaOH . In each case, the equivalence point comes after addition of 40.0 mL of 0.100 M NaOH , but the increase in pH at the equivalence point gets smaller and the equivalence point gets more difficult to detect as the $K_{\mathrm{a}}$ value of the weak acid decreases.

$\nabla$
The weaker the acid, the shorter is the steeply rising portion of the titration curve. If the acid is very weak, the equivalence point is difficult to detect.


[].Ara S. Kooser, Judith L. Jenkins, and Lawrence E. Welch, "Acid-Base Indicators: A New Look at an Old Topic," J. Chem. Educ., Vol. 78, 2001, 1504-1506.

Th Robert C. Mebane and Thomas R. Rybolt, "Edible Acid-Base Indicators," J. Chem. Educ., Vol. 62, 1985, 285.
§ Dianne N. Epp, "Teas as Natural Indicators," J. Chem. Educ., Vol. 70, 1993, 326.

Weak Base-Strong Acid Titration activity

- KEY CONCEPT PROBLEM 16.15 The following pictures represent solutions at various points in the titration of a weak acid HA with aqueous $\mathrm{NaOH} .\left(\mathrm{Na}^{+}\right.$ions and solvent water molecules have been omitted for clarity.)
- 


(1)

(2)

(3)

(4)

To which of the following points do solutions (1)-(4) correspond?
(a) Before addition of any NaOH
(b) Before the equivalence point
(c) At the equivalence point
(d) After the equivalence point

- PROBLEM 16.16 Consider the titration of 100.0 mL of $0.016 \mathrm{M} \mathrm{HOCl}\left(K_{\mathrm{a}}=\right.$ $3.5 \times 10^{-8}$ ) with 0.0400 M NaOH . How many milliliters of 0.0400 M NaOH are required to reach the equivalence point? Calculate the pH :
(a) After addition of 10.0 mL of 0.0400 M NaOH
(b) Halfway to the equivalence point
(c) At the equivalence point
- PROBLEM 16.17 The following acid-base indicators change color in the indicated pH ranges: bromthymol blue (6.0-7.6), thymolphthalein (9.4-10.6), and alizarin yellow (10.1-12.0). Which indicator is best for the titration in Problem 16.16? Which indicator is unacceptable? Explain.


## 16.8 | Weak Base-Strong Acid Titrations

Figure 16.9 shows the pH titration curve for a typical weak base-strong acid titration, the titration of $40.0 \mathrm{~mL}^{2}$ of $0.100 \mathrm{M} \mathrm{NH}_{3}$ with 0.100 M HCl . The pH calculations are simply outlined to save space; you should verify the results yourself.

1. Before Addition of Any HCl The equilibrium problem at the start of the titration is the familiar one of calculating the pH of a solution of a weak base (Section 15.12). The principal reaction at this point is the reaction of ammonia with water:

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q) \quad K_{\mathrm{b}}=1.8 \times 10^{-5}
$$

The initial pH is 11.12 .
2. Before the Equivalence Point As HCl is added to the $\mathrm{NH}_{3}$ solution, $\mathrm{NH}_{3}$ is converted to $\mathrm{NH}_{4}{ }^{+}$because of the neutralization reaction

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{3} \mathrm{O}^{+}(a q) \xrightarrow{100 \%} \mathrm{NH}_{4}^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

The neutralization reaction goes to completion, but the amount of $\mathrm{H}_{3} \mathrm{O}^{+}$ added before the equivalence point is not sufficient to convert all the $\mathrm{NH}_{3}$ to $\mathrm{NH}_{4}{ }^{+}$. We therefore have an $\mathrm{NH}_{4}{ }^{+}-\mathrm{NH}_{3}$ buffer solution, which accounts for the leveling of the titration curve in the buffer region between the start of the

titration and the equivalence point. The pH at any specific point can be calculated from the Henderson-Hasselbalch equation. After addition of 20.0 mL of 0.100 M HCl (halfway to the equivalence point), $\left[\mathrm{NH}_{3}\right]=\left[\mathrm{NH}_{4}{ }^{+}\right]$and the pH equals pK a for $\mathrm{NH}_{4}{ }^{+}$(9.25).
3. At the Equivalence Point The equivalence point is reached after adding 40.0 mL of $0.100 \mathrm{M} \mathrm{HCl}(4.00 \mathrm{mmol})$. At this point, the 4.00 mmol of $\mathrm{NH}_{3}$ present initially has been converted to 4.00 mmol of $\mathrm{NH}_{4}{ }^{+} ;\left[\mathrm{NH}_{4}{ }^{+}\right]=$ $(4.00 \mathrm{mmol}) /(80.0 \mathrm{~mL})=0.0500 \mathrm{M}$. Since $\mathrm{NH}_{4}{ }^{+}$is a weak acid and $\mathrm{Cl}^{-}$is neither an acid nor a base, we have an acidic salt solution (Section 15.14). The principal reaction is
$\mathrm{NH}_{4}{ }^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NH}_{3}(a q) \quad K_{\mathrm{a}}=K_{\mathrm{w}} / K_{\mathrm{b}}=5.6 \times 10^{-10}$
The pH at the equivalence point is 5.28 .
4. Beyond the Equivalence Point In this region, all the $\mathrm{NH}_{3}$ has been converted to $\mathrm{NH}_{4}{ }^{+}$, and an excess of $\mathrm{H}_{3} \mathrm{O}^{+}$is present from the excess HCl . Because the acid dissociation of $\mathrm{NH}_{4}{ }^{+}$produces a negligible $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] compared with $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right.$] from the excess HCl , the pH can be calculated directly from the concentration of the excess HCl . For example, after addition of 60.0 mL of 0.100 M HCl :

$$
\begin{aligned}
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{6.00 \mathrm{mmol}-4.00 \mathrm{mmol}}{100.0 \mathrm{~mL}}=0.0200 \mathrm{M}} \\
& \mathrm{pH}=1.70
\end{aligned}
$$

## 16.9 | Polyprotic Acid-Strong Base Titrations

As a final example of an acid-base titration, let's consider the gradual addition of NaOH to the protonated form of the amino acid alanine $\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right)$, a substance that acts as a diprotic acid. Amino acids (which are discussed in more detail in Chapter 24) are both acidic and basic and can be protonated by strong acids such as HCl , yielding salts such as $\mathrm{H}_{2} \mathrm{~A}^{+} \mathrm{Cl}^{-}$. The protonated form of the amino acid has two

FIGURE 16.9 A weak base-strong acid titration curve. The curve shown is for titration of 40.0 mL of $0.100 \mathrm{M} \mathrm{NH}_{3}$ with 0.100 M HCl . The pH is 11.12 at the start of the titration, 9.25 (the $\mathrm{p} K_{\mathrm{a}}$ value for $\mathrm{NH}_{4}{ }^{+}$) in the buffer region halfway to the equivalence point, and 5.28 at the equivalence point. Note that methyl red is a good indicator for this titration, but phenolphthalein is unacceptable.


Alanine

Polyprotic Acid-Strong Base Titration activity

FIGURE 16.10 Change in the pH of 1.00 L of a 1.00 M solution of $\mathrm{H}_{2} \mathrm{~A}^{+}$on addition of solid NaOH . The protonated form of alanine, $\mathrm{H}_{2} \mathrm{~A}^{+}$, is a diprotic acid, so the titration curve exhibits two equivalence points, at pH 6.02 and pH 11.85 , and two buffer regions, near pH 2.34 and pH 9.69 .
dissociable protons and can react with two molar amounts of $\mathrm{OH}^{-}$to give first the neutral form and then the anionic form:


The proton of the $-\mathrm{CO}_{2} \mathrm{H}$ group is more acidic than the proton of the $-\mathrm{NH}_{3}{ }^{+}$ group and is neutralized first. The neutral form of alanine (HA) that results has a plus charge on the $-\mathrm{NH}_{3}{ }^{+}$group and a minus charge on the $-\mathrm{CO}_{2}{ }^{-}$group but is electrically neutral overall. In a second step, the proton of the $-\mathrm{NH}_{3}{ }^{+}$group is neutralized, yielding the anionic form of alanine ( $\mathrm{A}^{-}$). The dissociation equilibria and their $K_{\mathrm{a}}$ values are

$$
\begin{aligned}
\mathrm{H}_{2} \mathrm{~A}^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) & \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{HA}(a q) \\
\mathrm{HA}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{A}^{-}(a q) & K_{\mathrm{a} 2}=2.0 \times 10^{-3} ; \mathrm{p}_{\mathrm{a} 1}=2.34 \\
& =10^{-10} ; \mathrm{pK}_{\mathrm{a} 2}=9.69
\end{aligned}
$$

Figure 16.10 shows the pH titration curve for addition of NaOH to 1.00 L of a 1.00 M solution of $\mathrm{H}_{2} \mathrm{~A}^{+}(1.00 \mathrm{~mol})$. To simplify the calculations, we've assumed that the added base is solid NaOH so that we can neglect volume changes in the course of the titration. Let's calculate the pH at some of the more important points.

1. Before Addition of Any NaOH The equilibrium problem at the start of the titration is the familiar one of calculating the pH of a diprotic acid (Section 15.11). The principal reaction is dissociation of $\mathrm{H}_{2} \mathrm{~A}^{+}$, and $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$can be calculated from the equilibrium equation

$$
K_{\mathrm{a} 1}=4.6 \times 10^{-3}=\frac{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right][\mathrm{HA}]}{\left[\mathrm{H}_{2} \mathrm{~A}^{+}\right]}=\frac{(x)(x)}{1.00-x}
$$

Solving the quadratic equation gives $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=0.066 \mathrm{M}$ and $\mathrm{pH}=1.18$.

2. Halfway to the First Equivalence Point As NaOH is added, $\mathrm{H}_{2} \mathrm{~A}^{+}$is converted to HA because of the neutralization reaction

$$
\mathrm{H}_{2} \mathrm{~A}^{+}(a q)+\mathrm{OH}^{-}(a q) \xrightarrow{100 \%} \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{HA}(a q)
$$

Halfway to the first equivalence point, we have an $\mathrm{H}_{2} \mathrm{~A}^{+}-\mathrm{HA}$ buffer solution with $\left[\mathrm{H}_{2} \mathrm{~A}^{+}\right]=[\mathrm{HA}]$. The Henderson-Hasselbalch equation gives $\mathrm{pH}=$ $\mathrm{p} K_{\mathrm{a} 1}=2.34$.
3. At the First Equivalence Point At this point, we have added just enough NaOH to convert all the $\mathrm{H}_{2} \mathrm{~A}^{+}$to HA. The principal reaction at the first equivalence point is proton transfer between HA molecules:

$$
2 \mathrm{HA}(a q) \rightleftharpoons \mathrm{H}_{2} \mathrm{~A}^{+}(a q)+\mathrm{A}^{-}(a q) \quad K=K_{\mathrm{a} 2} / K_{\mathrm{a} 1}=4.3 \times 10^{-8}
$$

It can be shown (see Problem 16.140) that the pH at this point equals the average of the two $\mathrm{p} K_{\mathrm{a}}$ values:

$$
\mathrm{pH}(\text { at first equivalence point })=\frac{\mathrm{p} K_{\mathrm{a} 1}+\mathrm{p} K_{\mathrm{a} 2}}{2}
$$

Since $\mathrm{H}_{2} \mathrm{~A}^{+}$has $\mathrm{p} K_{\mathrm{a} 1}=2.34$ and $\mathrm{p} K_{\mathrm{a} 2}=9.69$, the pH at the first equivalence point is $(2.34+9.69) / 2=6.02$. The same situation holds for most polyprotic acids: The pH at the first equivalence point equals the average of $\mathrm{p} K_{\mathrm{a} 1}$ and $\mathrm{p} K_{\mathrm{a} 2}$.

For an amino acid, the pH value, $\left(\mathrm{p} K_{\mathrm{a} 1}+\mathrm{p} K_{\mathrm{a} 2}\right) / 2$, is called the isoelectric point (Figure 16.10). At that point, the concentration of the neutral HA is at a maximum, and the very small concentrations of $\mathrm{H}_{2} \mathrm{~A}^{+}$and $\mathrm{A}^{-}$are equal. Biochemists use isoelectric points to separate mixtures of amino acids and proteins.
4. Halfway Between the First and Second Equivalence Points At this point, half the HA has been converted to $\mathrm{A}^{-}$because of the neutralization reaction

$$
\mathrm{HA}(a q)+\mathrm{OH}^{-}(a q) \xrightarrow{100 \%} \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{A}^{-}(a q)
$$

We thus have an HA-A ${ }^{-}$buffer solution with $[\mathrm{HA}]=\left[\mathrm{A}^{-}\right]$. Therefore, $\mathrm{pH}=\mathrm{p} K_{\mathrm{a} 2}=9.69$.
5. At the Second Equivalence Point At this point, we have added enough NaOH to convert all the HA to $\mathrm{A}^{-}$, and we have a 1.00 M solution of a basic salt (Section 15.14). The principal reaction is

$$
\mathrm{A}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HA}(a q)+\mathrm{OH}^{-}(a q)
$$

and its equilibrium constant is

$$
K_{\mathrm{b}}=\frac{K_{\mathrm{w}}}{K_{\mathrm{a}} \text { for } \mathrm{HA}}=\frac{K_{\mathrm{w}}}{K_{\mathrm{a} 2}}=\frac{1.0 \times 10^{-14}}{2.0 \times 10^{-10}}=5.0 \times 10^{-5}
$$

We can obtain $\left[\mathrm{OH}^{-}\right]$from the equilibrium equation for the principal reaction and then calculate $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$and pH in the usual way:

$$
\begin{aligned}
& K_{\mathrm{b}}=5.0 \times 10^{-5}=\frac{[\mathrm{HA}]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{A}^{-}\right]}=\frac{(x)(x)}{1.00-x} \quad x=\left[\mathrm{OH}^{-}\right]=7.1 \times 10^{-3} \mathrm{M} \\
& {\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\frac{K_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{1.0 \times 10^{-14}}{7.1 \times 10^{-3}}=1.4 \times 10^{-12} \mathrm{M}} \\
& \mathrm{pH}=11.85
\end{aligned}
$$

Since the initial solution of $\mathrm{H}_{2} \mathrm{~A}^{+}$contained 1.00 mol of $\mathrm{H}_{2} \mathrm{~A}^{+}$, the amount of NaOH required to reach the second equivalence point is 2.00 mol . Beyond the second equivalence point, the pH is determined by $\left[\mathrm{OH}^{-}\right]$from the excess NaOH .

V
As noted earlier, the weaker the acid, the shorter is the steeply rising portion of the titration curve. If the acid is very weak, the equivalence point is difficult to detect. Although $\mathrm{H}_{3} \mathrm{PO}_{4}$ is a triprotic acid, $\mathrm{HPO}_{4}{ }^{2-}$ is such a weak acid that the third equivalence point is not observed in the $\mathrm{H}_{3} \mathrm{PO}_{4} / \mathrm{NaOH}$ titration curve.

## Worked Example 16.6

Consider the titration of 30.0 mL of a 0.0600 M solution of the protonated form of the amino acid methionine $\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right)$with 0.0900 M NaOH . Calculate the pH after addition of 20.0 mL of base.


Methionine cation $\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right)$

$$
\begin{aligned}
& K_{\mathrm{a} 1}=5.2 \times 10^{-3} \\
& K_{\mathrm{a} 2}=6.2 \times 10^{-10}
\end{aligned}
$$

## Strategy

First calculate the number of millimoles of $\mathrm{H}_{2} \mathrm{~A}^{+}$present initially and of NaOH added. Then we can tell which species remain after neutralization and therefore what type of equilibrium problem we must solve.

## Solution

The number of millimoles of $\mathrm{H}_{2} \mathrm{~A}^{+}$present initially and of NaOH added are

$$
\begin{aligned}
& \mathrm{mmol} \mathrm{H}_{2} \mathrm{~A}^{+} \text {initial }=(30.0 \mathrm{~mL})(0.0600 \mathrm{mmol} / \mathrm{mL})=1.80 \mathrm{mmol} \\
& \mathrm{mmol} \mathrm{NaOH} \text { added }=(20.0 \mathrm{~mL})(0.0900 \mathrm{mmol} / \mathrm{mL})=1.80 \mathrm{mmol}
\end{aligned}
$$

The added base is just enough to reach the first equivalence point, converting all the $\mathrm{H}_{2} \mathrm{~A}^{+}$to HA because of the neutralization reaction

$$
\mathrm{H}_{2} \mathrm{~A}^{+}(a q)+\mathrm{OH}^{-}(a q) \xrightarrow{100 \%} \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{HA}(a q)
$$

Therefore, the pH equals the average of $\mathrm{p} K_{\mathrm{a} 1}$ and $\mathrm{p} K_{\mathrm{a} 2}$ :

$$
\begin{aligned}
\mathrm{pH} & =\frac{\mathrm{p} K_{\mathrm{a} 1}+\mathrm{p} K_{\mathrm{a} 2}}{2}=\frac{\left[-\log \left(5.2 \times 10^{-3}\right)\right]+\left[-\log \left(6.2 \times 10^{-10}\right)\right]}{2} \\
& =\frac{2.28+9.21}{2}=5.74
\end{aligned}
$$

PROBLEM 16.18 Consider the titration of 40.0 mL of $0.0800 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{3}$ $\left(K_{\mathrm{a} 1}=1.5 \times 10^{-2} ; K_{\mathrm{a} 2}=6.3 \times 10^{-8}\right)$ with 0.160 M NaOH . Calculate the pH after addition of the following volumes of 0.160 M NaOH :
(a) 20.0 mL
(b) 30.0 mL
(c) 35.0 mL

- PROBLEM 16.19 Consider the titration of 40.0 mL of a 0.0250 M solution of the protonated form of the amino acid valine $\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right)$with 0.100 M NaOH . Calculate the pH after addition of the following volumes of 0.100 M NaOH :
(a) 10.0 mL
(b) 15.0 mL
(c) 20.0 mL


Solubility Product Constant activity


$$
\begin{gathered}
\text { Valine cation }\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right) \\
K_{\mathrm{a} 1}=4.8 \times 10^{-3} \\
K_{\mathrm{a} 2}=2.4 \times 10^{-10}
\end{gathered}
$$

### 16.10 Solubility Equilibria

Many biological and environmental processes involve the dissolution or precipitation of a sparingly soluble ionic compound. Tooth decay, for example, begins when tooth enamel, composed of the mineral hydroxyapatite, $\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{OH}$,
dissolves on reaction with organic acids produced by bacterial decomposition of foods rich in sugar. Kidney stones form when moderately insoluble calcium salts, such as calcium oxalate, $\mathrm{CaC}_{2} \mathrm{O}_{4}$, precipitate slowly over a long period of time. To understand the quantitative aspects of such solubility and precipitation phenomena, we must examine the principles of solubility equilibria.

Let's consider the solubility equilibrium in a saturated solution of calcium fluoride in contact with an excess of solid calcium fluoride. Like most sparingly soluble ionic solutes, calcium fluoride is a strong electrolyte in water and exists in the aqueous phase as dissociated hydrated ions, $\mathrm{Ca}^{2+}(a q)$ and $\mathrm{F}^{-}(a q)$. At equilibrium, the ion concentrations remain constant because the rate at which solid $\mathrm{CaF}_{2}$ dissolves to give $\mathrm{Ca}^{2+}(a q)$ and $\mathrm{F}^{-}(a q)$ exactly equals the rate at which the ions crystallize to form solid $\mathrm{CaF}_{2}$ :

$$
\mathrm{CaF}_{2}(s) \rightleftharpoons \mathrm{Ca}^{2+}(a q)+2 \mathrm{~F}^{-}(a q)
$$

The equilibrium equation for the dissolution reaction is

$$
K_{\mathrm{sp}}=\left[\mathrm{Ca}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}
$$

where the equilibrium constant $K_{\text {sp }}$ is called the solubility product constant, or simply the solubility product. As usual for a heterogeneous equilibrium, the concentration of the solid, $\mathrm{CaF}_{2}$, has been omitted from the equilibrium equation because it is constant (Section 13.4).

For the general solubility equilibrium

$$
\mathrm{M}_{m} \mathrm{X}_{x}(s) \rightleftharpoons m \mathrm{M}^{n+}(a q)+x \mathrm{X}^{y-}(a q)
$$

the equilibrium constant expression for $K_{\mathrm{sp}}$ is

$$
K_{\mathrm{sp}}=\left[\mathrm{M}^{n+}\right]^{m}\left[\mathrm{X}^{y-}\right]^{x}
$$

Thus, $K_{\text {sp }}$ always equals the product of the equilibrium concentrations of all the ions on the right side of the chemical equation, with the concentration of each ion raised to the power of its coefficient in the balanced equation.

## Worked Example 16.7

Write the expression for the solubility product of silver chromate, $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$.

## Strategy and Solution

First write the balanced equation for the solubility equilibrium:

$$
\mathrm{Ag}_{2} \mathrm{CrO}_{4}(s) \rightleftharpoons 2 \mathrm{Ag}^{+}(a q)+\mathrm{CrO}_{4}^{2-}(a q)
$$

The exponents in the equilibrium constant expression for $K_{s p}$ are the coefficients in the balanced equation. Therefore,

$$
K_{\mathrm{sp}}=\left[\mathrm{Ag}^{+}\right]^{2}\left[\mathrm{CrO}_{4}{ }^{2-}\right]
$$

- PROBLEM 16.20 Write the expression for $K_{\text {sp }}$ of:
(a) AgCl
(b) $\mathrm{PbI}_{2}$
(c) $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$
(d) $\mathrm{Cr}(\mathrm{OH})_{3}$


### 16.11 Measuring $K_{\text {sp }}$ and Calculating Solubility from $K_{\text {sp }}$

The numerical value of a solubility product $K_{\mathrm{sp}}$ is measured by experiment. For example, we could determine $K_{\text {sp }}$ for $\mathrm{CaF}_{2}$ by adding an excess of solid $\mathrm{CaF}_{2}$ to water, stirring the mixture to give a saturated solution of $\mathrm{CaF}_{2}$, and then


- Most kidney stones consist of insoluble calcium salts, such as calcium oxalate.

$\sqrt{ }$The solubility product constant, $K_{\text {sp }}$, is for a saturated solution.


A A saturated solution of calcium fluoride in contact with solid $\mathrm{CaF}_{2}$ contains constant equilibrium concentrations of $\mathrm{Ca}^{2+}(a q)$ and $\mathrm{F}^{-}(a q)$ because at equilibrium the ions crystallize at the same rate as the solid dissolves.

V
No ionic compound is $100 \%$ insoluble. In order for an equilibrium to exist, all ionic compounds must dissolve to some extent.

Stephen J. Hawkes, "What Should We Teach Beginners about Solubility and Solubility Product?" J. Chem. Educ., Vol. 75, 1998, 1179-1181.

Roy W. Clark and Judith M. Bonicamp, "The $K_{\text {sp }}$-Solubility Conundrum," J. Chem. Educ., Vol. 75, 1998, 1182-1185.

Andres Raviolo, "Assessing Students' Conceptual Understanding of Solubility Equilibrium," J. Chem. Educ., Vol. 78, 2001, 629-631.

Lee R. Summerlin, Christie L.
Borgford, and Julie B. Ealy, "Solubility of Some Silver Compounds," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 83-85.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Red and White Precipitates in Sodium Silicate," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), p. 131.
measuring the concentrations of $\mathrm{Ca}^{2+}$ and $\mathrm{F}^{-}$in the saturated solution. To make sure that the concentrations had reached constant equilibrium values, we would want to stir the mixture for an additional period of time and then repeat the measurements. Suppose that we found $\left[\mathrm{Ca}^{2+}\right]=3.3 \times 10^{-4} \mathrm{M}$ and $\left[\mathrm{F}^{-}\right]=6.7 \times 10^{-4} \mathrm{M}$. (The value of $\left[\mathrm{F}^{-}\right]$is twice the value of $\left[\mathrm{Ca}^{2+}\right]$ because each mole of $\mathrm{CaF}_{2}$ that dissolves yields 1 mol of $\mathrm{Ca}^{2+}$ ions and 2 mol of $\mathrm{F}^{-}$ions.) We could then calculate $K_{\text {sp }}$ for $\mathrm{CaF}_{2}$ :

$$
K_{\mathrm{sp}}=\left[\mathrm{Ca}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}=\left(3.3 \times 10^{-4}\right)\left(6.7 \times 10^{-4}\right)^{2}=1.5 \times 10^{-10}
$$

Another way to measure $K_{\text {sp }}$ for $\mathrm{CaF}_{2}$ is to approach the equilibrium from the opposite direction-that is, by mixing sources of $\mathrm{Ca}^{2+}$ and $\mathrm{F}^{-}$ions to give a precipitate of solid $\mathrm{CaF}_{2}$ and a saturated solution of $\mathrm{CaF}_{2}$. Suppose, for example, that we mix solutions of $\mathrm{CaCl}_{2}$ and NaF , allow time for equilibrium to be reached, and then measure $\left[\mathrm{Ca}^{2+}\right]=1.5 \times 10^{-4} \mathrm{M}$ and $\left[\mathrm{F}^{-}\right]=1.0 \times 10^{-3} \mathrm{M}$. These ion concentrations yield the same value of $K_{\mathrm{sp}}$ :

$$
K_{\mathrm{sp}}=\left[\mathrm{Ca}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}=\left(1.5 \times 10^{-4}\right)\left(1.0 \times 10^{-3}\right)^{2}=1.5 \times 10^{-10}
$$

Values of $K_{\mathrm{sp}}$ are unaffected by the presence of other ions in solution, such as $\mathrm{Na}^{+}$from NaF and $\mathrm{Cl}^{-}$from $\mathrm{CaCl}_{2}$, as long as the solution is very dilute. As ion concentrations increase, $K_{\mathrm{sp}}$ values are somewhat modified because of electrostatic interactions between ions. We'll ignore that complication here.

If the saturated solution is prepared by a method other than dissolution of $\mathrm{CaF}_{2}$ in pure water, there are no separate restrictions on $\left[\mathrm{Ca}^{2+}\right]$ and $\left[\mathrm{F}^{-}\right]$; the only restriction on the ion concentrations is that the equilibrium constant expression $\left[\mathrm{Ca}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}$ must equal the $K_{\mathrm{sp}}$. That condition is satisfied by an infinite number of combinations of $\left[\mathrm{Ca}^{2+}\right]$ and $\left[\mathrm{F}^{-}\right]$, and therefore we can prepare many different solutions that are saturated with respect to $\mathrm{CaF}_{2}$. For example, if $\left[\mathrm{F}^{-}\right]$is $1.0 \times 10^{-2} \mathrm{M}$, then $\left[\mathrm{Ca}^{2+}\right]$ must be $1.5 \times 10^{-6} \mathrm{M}$ :

$$
\left[\mathrm{Ca}^{2+}\right]=\frac{K_{\mathrm{sp}}}{\left[\mathrm{~F}^{-}\right]^{2}}=\frac{1.5 \times 10^{-10}}{\left(1.0 \times 10^{-2}\right)^{2}}=1.5 \times 10^{-6} \mathrm{M}
$$

Selected values of $K_{\text {sp }}$ for various ionic compounds at $25^{\circ} \mathrm{C}$ are listed in Table 16.2, and additional values can be found in Appendix C. Like all equilibrium constants, values of $K_{\mathrm{sp}}$ depend on temperature (Section 13.9).

TABLE $16.2 \quad K_{\text {sp }}$ Values for Some lonic Compounds at $25^{\circ} \mathrm{C}$

| Name | Formula | $\boldsymbol{K}_{\text {sp }}$ |
| :--- | :--- | :--- |
| Aluminum hydroxide | $\mathrm{Al}(\mathrm{OH})_{3}$ | $1.9 \times 10^{-33}$ |
| Barium carbonate | $\mathrm{BaCO}_{3}$ | $2.6 \times 10^{-9}$ |
| Calcium carbonate | $\mathrm{CaCO}_{3}$ | $5.0 \times 10^{-9}$ |
| Calcium fluoride | $\mathrm{CaF}_{2}$ | $1.5 \times 10^{-10}$ |
| Lead(II) chloride | $\mathrm{PbCl}_{2}$ | $1.2 \times 10^{-5}$ |
| Lead(II) chromate | $\mathrm{PbCrO}_{4}$ | $2.8 \times 10^{-13}$ |
| Silver chloride | $\mathrm{AgCl}^{\text {Silver sulfate }}$ | $\mathrm{Ag}_{2} \mathrm{SO}_{4}$ |

Once the $K_{\text {sp }}$ value for a compound has been measured, you can use it to calculate the solubility of the compound-the amount of compound that dissolves per unit volume of saturated solution. Because of two complications, however, calculated solubilities are often approximate. First, $K_{\text {sp }}$ values can be difficult to measure, and values listed in different sources might differ by a factor of 10 or more. Second, calculated solubilities can be less than observed solubilities because
of side reactions. For example, dissolution of $\mathrm{PbCl}_{2}$ gives both $\mathrm{Pb}^{2+}$ and $\mathrm{PbCl}^{+}$ because of some ion association between $\mathrm{Pb}^{2+}$ and $\mathrm{Cl}^{-}$ions:

$$
\begin{aligned}
& \text { (1) } \mathrm{PbCl}_{2}(s) \rightleftharpoons \mathrm{Pb}^{2+}(a q)+2 \mathrm{Cl}^{-}(a q) \\
& (2) \mathrm{Pb}^{2+}(a q)+\mathrm{Cl}^{-}(a q) \rightleftharpoons \mathrm{PbCl}^{+}(a q)
\end{aligned}
$$

In this book, we will calculate approximate solubilities assuming that ionic solutes are completely dissociated [reaction (1)]. In the case of $\mathrm{PbCl}_{2}$, ignoring the second equilibrium gives a calculated solubility that is too low by a factor of about 2 .

## Worked Example 16.8

A particular saturated solution of silver chromate, $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$, has $\left[\mathrm{Ag}^{+}\right]=5.0 \times 10^{-5} \mathrm{M}$ and $\left[\mathrm{CrO}_{4}{ }^{2-}\right]=4.4 \times 10^{-4} \mathrm{M}$. What is the value of $K_{\mathrm{sp}}$ for $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ ?

## Strategy

Substituting the equilibrium concentrations into the expression for $K_{\text {sp }}$ of $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ (Worked Example 16.7) gives the value of $K_{\mathrm{sp}}$.

## Solution

$$
K_{\mathrm{sp}}=\left[\mathrm{Ag}^{+}\right]^{2}\left[\mathrm{CrO}_{4}{ }^{2-}\right]=\left(5.0 \times 10^{-5}\right)^{2}\left(4.4 \times 10^{-4}\right)=1.1 \times 10^{-12}
$$

$\checkmark$ BALLPARK CHECK $K_{\text {sp }}$ is approximately $(5)^{2}(4)=100$ times $\left(10^{-5}\right)^{2}\left(10^{-4}\right)=$ $10^{-14}$. So $K_{\text {sp }}$ is about $10^{-12}$, in agreement with the solution.

Addition of aqueous $\mathrm{K}_{2} \mathrm{CrO}_{4}$ to aqueous $\mathrm{AgNO}_{3}$ gives a red precipitate of $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ and a saturated solution of $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$.


## Worked Example 16.9

A saturated solution of $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ prepared by dissolving solid $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ in water has $\left[\mathrm{CrO}_{4}{ }^{2-}\right]=6.5 \times 10^{-5} \mathrm{M}$. Calculate $K_{\text {sp }}$ for $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$.

## Strategy

Because both the $\mathrm{Ag}^{+}$and $\mathrm{CrO}_{4}{ }^{2-}$ ions come from dissolution of solid $\mathrm{Ag}_{2} \mathrm{CrO}_{4},\left[\mathrm{Ag}^{+}\right]$ must be twice $\left[\mathrm{CrO}_{4}{ }^{2-}\right]$. Substituting $\left[\mathrm{Ag}^{+}\right]$and $\left[\mathrm{CrO}_{4}{ }^{2-}\right]$ into the equilibrium equation gives the value of $K_{\mathrm{sp}}$.

## Solution

$$
\begin{aligned}
& {\left[\mathrm{Ag}^{+}\right]=(2)\left[\mathrm{CrO}_{4}{ }^{2-}\right]=(2)\left(6.5 \times 10^{-5}\right)=1.3 \times 10^{-4} \mathrm{M}} \\
& K_{\mathrm{sp}}=\left[\mathrm{Ag}^{+}\right]^{2}\left[\mathrm{CrO}_{4}{ }^{2-}\right]=\left(1.3 \times 10^{-4}\right)^{2}\left(6.5 \times 10^{-5}\right)=1.1 \times 10^{-12}
\end{aligned}
$$

## Worked Example 16.10

Calculate the solubility of $\mathrm{MgF}_{2}$ in water at $25^{\circ} \mathrm{C}$ in units of:
(a) Moles per liter
(b) Grams per liter

## Strategy

(a) Write the balanced equation for the solubility equilibrium assuming complete dissociation of $\mathrm{MgF}_{2}$, and then look up $K_{\text {sp }}$ for $\mathrm{MgF}_{2}$ in Appendix C. If we define $x$ as the number of moles per liter of $\mathrm{MgF}_{2}$ that dissolves, then the saturated solution contains

0The relative solubilities of two ionic compounds can be determined by comparing their $K_{\text {sp }}$ values only if they have the same number of ions. It is possible for a 1:1 compound, such as $\mathrm{CaCO}_{3}$, to have a larger $K_{\text {sp }}$ value but a lower solubility than a 1:2 compound, such as $\mathrm{CaF}_{2}$.


A This X-ray photograph of the small intestine was taken soon after the patient drank a barium sulfate "cocktail."
$x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{Mg}^{2+}$ and $2 x \mathrm{~mol} / \mathrm{L}^{2}$ of $\mathrm{F}^{-}$. Substituting these equilibrium concentrations into the expression for $K_{\mathrm{sp}}$ and solving for $x$ gives the molar solubility.
(b) To convert the solubility from units of moles per liter to units of grams per liter, multiply the molar solubility of $\mathrm{MgF}_{2}$ by its molar mass ( $62.3 \mathrm{~g} / \mathrm{mol}$ ).

## Solution

(a) $\mathrm{MgF}_{2}(s) \rightleftharpoons \mathrm{Mg}^{2+}(a q)+2 \mathrm{~F}^{-}(a q) \quad K_{\mathrm{sp}}=7.4 \times 10^{-11}$

$$
\begin{aligned}
K_{\mathrm{sp}} & =7.4 \times 10^{-11}=\left[\mathrm{Mg}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}=(x)(2 x)^{2} \\
4 x^{3} & =7.4 \times 10^{-11} \\
x^{3} & =1.8 \times 10^{-11} \\
x & =\left[\mathrm{Mg}^{2+}\right]=\text { Molar solubility }=2.6 \times 10^{-4} \mathrm{~mol} / \mathrm{L}
\end{aligned}
$$

Thus, the molar solubility of $\mathrm{MgF}_{2}$ in water at $25^{\circ} \mathrm{C}$ is $2.6 \times 10^{-4} \mathrm{M}$. (Taking account of the side reaction that produces $\mathrm{MgF}^{+}$would increase the calculated solubility by about 6\%.)

Note that the number 2 appears twice in the expression $(x)(2 x)^{2}$. The exponent 2 is required because of the equilibrium equation, $K_{\mathrm{sp}}=\left[\mathrm{Mg}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}$. The coefficient 2 in $2 x$ is required because each mole of $\mathrm{MgF}_{2}$ that dissolves gives 2 mol of $\mathrm{F}^{-}(a q)$.
(b) Solubility $($ in $g / L)=\frac{2.6 \times 10^{-4} \mathrm{~mol}}{\mathrm{~L}} \times \frac{62.3 \mathrm{~g}}{\mathrm{~mol}}=1.6 \times 10^{-2} \mathrm{~g} / \mathrm{L}$

## $\checkmark$ Ballpark Check

(a) The molar solubility of $\mathrm{MgF}_{2}$ is the cube root of $K_{\text {sp }} / 4$, which equals the cube root of approximately $20 \times 10^{-12}$. Because $(2)^{3}=8,(3)^{3}=27$, and $\left(10^{-4}\right)^{3}=10^{-12}$, the molar solubility is between $2 \times 10^{-4} \mathrm{M}$ and $3 \times 10^{-4} \mathrm{M}$. The ballpark check and the solution agree.

PROBLEM 16.21 A saturated solution of $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$ has $\left[\mathrm{Ca}^{2+}\right]=2.01 \times 10^{-8} \mathrm{M}$ and $\left[\mathrm{PO}_{4}{ }^{3-}\right]=1.6 \times 10^{-5} \mathrm{M}$. Calculate $K_{\mathrm{sp}}$ for $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$.

- PROBLEM 16.22 Prior to having an X-ray exam of the upper gastrointestinal tract, a patient drinks an aqueous suspension of solid $\mathrm{BaSO}_{4}$. (Scattering of X rays by barium greatly enhances the quality of the photograph.) Although $\mathrm{Ba}^{2+}$ is toxic, ingestion of $\mathrm{BaSO}_{4}$ is safe because it is quite insoluble. If a saturated solution prepared by dissolving solid $\mathrm{BaSO}_{4}$ in water has $\left[\mathrm{Ba}^{2+}\right]=1.05 \times 10^{-5} \mathrm{M}$, what is the value of $K_{\text {sp }}$ for $\mathrm{BaSO}_{4}$ ?

PROBLEM 16.23 Which has the greater molar solubility: AgCl with $K_{\text {sp }}=$ $1.8 \times 10^{-10}$ or $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ with $K_{\text {sp }}=1.1 \times 10^{-12}$ ? Which has the greater solubility in grams per liter?

- KEY CONCEPT PROBLEM 16.24 The following pictures represent saturated solutions of three silver salts: $\mathrm{AgX}, \mathrm{AgY}$, and AgZ . (Other ions and solvent water molecules have been omitted for clarity.)

(a) Which salt has the largest value of $K_{\mathrm{sp}}$ ?
(b) Which salt has the smallest value of $K_{\text {sp }}$ ?


## $16.12 \mid$ Factors That Affect Solubility

## The Common-Ion Effect

We've already discussed the common-ion effect in connection with the dissociation of weak acids and bases (Section 16.2). To see how a common ion affects the position of a solubility equilibrium, let's look again at the solubility of $\mathrm{MgF}_{2}$ :

$$
\operatorname{MgF}_{2}(s) \rightleftharpoons \operatorname{Mg}^{2+}(a q)+2 \mathrm{~F}^{-}(a q)
$$

In Worked Example 16.10, we found that the molar solubility of $\mathrm{MgF}_{2}$ in pure water at $25^{\circ} \mathrm{C}$ is $2.6 \times 10^{-4} \mathrm{M}$. Thus,

$$
\left[\mathrm{Mg}^{2+}\right]=2.6 \times 10^{-4} \mathrm{M} \quad\left[\mathrm{~F}^{-}\right]=5.2 \times 10^{-4} \mathrm{M}
$$

When $\mathrm{MgF}_{2}$ dissolves in a solution that contains a common ion from another source-say, $\mathrm{F}^{-}$from NaF -the position of the solubility equilibrium is shifted to the left by the common-ion effect. If [ $\mathrm{F}^{-}$] is larger than $5.2 \times 10^{-4} \mathrm{M}$, then $\left[\mathrm{Mg}^{2+}\right]$ must be correspondingly smaller than $2.6 \times 10^{-4} \mathrm{M}$ to maintain the equilibrium expression $\left[\mathrm{Mg}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}$ at a constant value of $K_{\text {sp }}=7.4 \times 10^{-11}$. A smaller value of $\left[\mathrm{Mg}^{2+}\right]$ thus means that $\mathrm{MgF}_{2}$ is less soluble in a sodium fluoride solution than it is in pure water. Similarly, the presence of $\mathrm{Mg}^{2+}$ from another source-say, $\mathrm{MgCl}_{2}$-shifts the solubility equilibrium to the left and decreases the solubility of $\mathrm{MgF}_{2}$.


In general, the solubility of a slightly soluble ionic compound is decreased by the presence of a common ion in the solution, as illustrated in Figure 16.11. The quantitative aspects of the common-ion effect are explored in Worked Example 16.11.



4 FIGURE 16.11 The common-ion effect. The solubility of $\mathrm{MgF}_{2}$ at $25^{\circ} \mathrm{C}$ decreases markedly on addition of $\mathrm{F}^{-}$ ions. Note that the calculated solubility is plotted on a logarithmic scale.

The addition of a common ion to a solution of sparingly soluble ionic compound lowers the solubility of that compound.
 movie

## Worked Example 16.11

Calculate the molar solubility of $\mathrm{MgF}_{2}$ in 0.10 M NaF at $25^{\circ} \mathrm{C}$.

## Strategy

Once again, we define $x$ as the molar solubility of $\mathrm{MgF}_{2}$. Dissolution of $x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{MgF}_{2}$ provides $x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{Mg}^{2+}$ and $2 x \mathrm{~mol} / \mathrm{L}^{2}$ of $\mathrm{F}^{-}$, but the total concentration of $\mathrm{F}^{-}$is $(0.10+2 x) \mathrm{mol} / \mathrm{L}$ because the solution already contains $0.10 \mathrm{~mol} / \mathrm{L}$ of $\mathrm{F}^{-}$from the NaF. Substituting the equilibrium concentrations into the expression for $K_{\text {sp }}$ and solving for $x$ gives the molar solubility.

## Solution

It's helpful to summarize the equilibrium concentrations under the balanced equation:

| Solubility equilibrium: | $\mathbf{M g F}_{\mathbf{2}}(\mathbf{s}) \rightleftharpoons \mathbf{M g}^{\mathbf{2 +}}(\boldsymbol{a q})+\mathbf{2} \mathbf{F}^{-}(\boldsymbol{a q})$ |  |
| :--- | :---: | ---: |
| Equilibrium conc $(\mathrm{M})$ | $x$ | $0.10+2 x$ |

Substituting the equilibrium concentrations into the expression for $K_{\text {sp }}$ gives

$$
K_{\mathrm{sp}}=7.4 \times 10^{-11}=\left[\mathrm{Mg}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}=(x)(0.10+2 x)^{2}
$$

Because $K_{\text {sp }}$ is small, $2 x$ will be small compared to 0.10 , and we can make the approximation that $(0.10+2 x) \approx 0.10$. Therefore,

$$
\begin{aligned}
& 7.4 \times 10^{-11}=(x)(0.10+2 x)^{2} \approx(x)(0.10)^{2} \\
& x=\left[\mathrm{Mg}^{2+}\right]=\text { Molar solubility }=\frac{7.4 \times 10^{-11}}{(0.10)^{2}}=7.4 \times 10^{-9} \mathrm{M}
\end{aligned}
$$

Note that the calculated solubility of $\mathrm{MgF}_{2}$ in 0.10 M NaF is less than that in pure water by a factor of about 35,000 ! (See Figure 16.11.) (Taking account of the equilibrium $\mathrm{Mg}^{2+}+\mathrm{F}^{-} \rightleftharpoons \mathrm{MgF}^{+}$would increase the calculated solubility by a factor of about 10. In this case, quite a bit of the $\mathrm{Mg}^{2+}$ is converted to $\mathrm{MgF}^{+}$because of the relatively high $\mathrm{F}^{-}$concentration in 0.10 M NaF .)
$\checkmark$ BALLPARK Check We can check our results by substituting the calculated equilibrium concentrations into the expression for $K_{\mathrm{sp}}$ :

$$
K_{\mathrm{sp}}=7.4 \times 10^{-11}=\left[\mathrm{Mg}^{2+}\right]\left[\mathrm{F}^{-}\right]^{2}=\left(7.4 \times 10^{-9}\right)(0.10)^{2}=7.4 \times 10^{-11}
$$

PROBLEM 16.25 Calculate the molar solubility of $\mathrm{MgF}_{2}$ in $0.10 \mathrm{M} \mathrm{MgCl}_{2}$ at $25^{\circ} \mathrm{C}$.

## The pH of the Solution

An ionic compound that contains a basic anion becomes more soluble as the acidity of the solution increases. The solubility of $\mathrm{CaCO}_{3}$, for example, increases with decreasing pH (Figure 16.12) because the $\mathrm{CO}_{3}{ }^{2-}$ ions combine with protons to give $\mathrm{HCO}_{3}{ }^{-}$ions. As $\mathrm{CO}_{3}{ }^{2-}$ ions are removed from the solution, the solubility equilibrium shifts to the right, as predicted by Le Châtelier's principle. The net reaction is dissolution of $\mathrm{CaCO}_{3}$ in acidic solution to give $\mathrm{Ca}^{2+}$ ions and $\mathrm{HCO}_{3}{ }^{-}$ions:

$$
\begin{aligned}
\mathrm{CaCO}_{3}(s) & \rightleftharpoons \mathrm{Ca}^{2+}(a q)+\mathrm{CO}_{3}^{2-}(a q) \\
\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CO}_{3}^{2-}(a q) & \rightleftharpoons \mathrm{HCO}_{3}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\
\hline \text { Net: } \quad \mathrm{CaCO}_{3}(s)+\mathrm{H}_{3} \mathrm{O}^{+}(a q) & \rightleftharpoons \mathrm{Ca}^{2+}(a q)+\mathrm{HCO}_{3}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$


$\triangle$ FIGURE 16.12 The solubility of $\mathrm{CaCO}_{3}$ at $25^{\circ} \mathrm{C}$ increases as the solution becomes more acidic because the $\mathrm{CO}_{3}{ }^{2-}$ ions combine with protons, thus driving the solubility equilibrium to the right. Note that the solubility is plotted on a logarithmic scale.

Other salts that contain basic anions, such as $\mathrm{CN}^{-}, \mathrm{PO}_{4}{ }^{3-}, \mathrm{S}^{2-}$, or $\mathrm{F}^{-}$, behave similarly. By contrast, pH has no effect on the solubility of salts that contain anions of strong acids $\left(\mathrm{Cl}^{-}, \mathrm{Br}^{-}, \mathrm{I}^{-}, \mathrm{NO}_{3}^{-}\right.$, and $\left.\mathrm{ClO}_{4}^{-}\right)$because these anions are not protonated by $\mathrm{H}_{3} \mathrm{O}^{+}$.

The effect of pH on the solubility of $\mathrm{CaCO}_{3}$ has important environmental consequences. For instance, the formation of limestone caves, such as Mammoth Cave in Kentucky, is due to the slow dissolution of limestone $\left(\mathrm{CaCO}_{3}\right)$ in the slightly acidic natural water of underground streams. Marble, another form of $\mathrm{CaCO}_{3}$, also dissolves in acid, which accounts for the deterioration of marble monuments on exposure to acid rain (Interlude, pages 650-651).

The effect of pH on solubility is also important in understanding how fluoride ion reduces tooth decay. When tooth enamel comes in contact with $\mathrm{F}^{-}$ions in drinking water or fluoride-containing toothpaste, $\mathrm{OH}^{-}$ions in hydroxyapatite, $\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{OH}$, are replaced by $\mathrm{F}^{-}$ions, giving the mineral fluorapatite, $\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{~F}$. Because $\mathrm{F}^{-}$is a much weaker base than $\mathrm{OH}^{-}, \mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{~F}$ is much more resistant than $\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{OH}$ to dissolving in acids.

- PROBLEM 16.26 Which of the following compounds are more soluble in acidic solution than in pure water?
(a) AgCN
(b) $\mathrm{PbI}_{2}$
(c) $\mathrm{Al}(\mathrm{OH})_{3}$
(d) ZnS


## Formation of Complex Ions

The solubility of an ionic compound increases dramatically if the solution contains a Lewis base that can form a coordinate covalent bond (Section 7.5) to the metal cation. Silver chloride, for example, is insoluble in water and in acid, but it dissolves in an excess of aqueous ammonia, forming the complex ion $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$ (Figure 16.13). A complex ion is an ion that contains a metal cation bonded to one or more small molecules or ions, such as $\mathrm{NH}_{3}, \mathrm{CN}^{-}$, or $\mathrm{OH}^{-}$. In accord with Le Châtelier's principle, ammonia shifts the solubility equilibrium to the right by tying up the $\mathrm{Ag}^{+}$ion in the form of the complex ion:

$$
\begin{aligned}
& \mathrm{AgCl}(s) \rightleftharpoons \mathrm{Ag}^{+}(a q)+\mathrm{Cl}^{-}(a q) \\
& \mathrm{Ag}^{+}(a q)+2 \mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}(a q)
\end{aligned}
$$

Bassam Z. Shakhashiri, "Fizzing and Foaming: Reactions of Acids with Carbonates," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 96-99.

VThe solubility of a sparingly soluble ionic compound is increased on addition of $\mathrm{H}_{3} \mathrm{O}^{+}$if the anion of the compound is the conjugate base of a weak acid.

[^18]FIGURE 16.13 Silver chloride is insoluble in water (left) but dissolves on addition of an excess of aqueous ammonia (right).


The formation of a complex ion is a stepwise process, and each step has its own characteristic equilibrium constant. For formation of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$, the reactions are

$$
\begin{aligned}
\mathrm{Ag}^{+}(a q)+\mathrm{NH}_{3}(a q) & \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}(a q)
\end{aligned} \quad \begin{aligned}
& K_{1}=2.1 \times 10^{3} \\
& \mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}(a q)+\mathrm{NH}_{3}(a q) \\
& \hline \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}(a q)
\end{aligned} \begin{aligned}
& K_{2}=8.1 \times 10^{3} \\
& \text { Net: } \quad \mathrm{Ag}^{+}(a q)+2 \mathrm{NH}_{3}(a q) \\
& \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}(a q)
\end{aligned} \begin{aligned}
& K_{\mathrm{f}}=1.7 \times 10^{7} \\
& K_{1}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]}{\left[\mathrm{Ag}^{+}\right]\left[\mathrm{NH}_{3}\right]}=2.1 \times 10^{3} \quad K_{2}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]}{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]\left[\mathrm{NH}_{3}\right]}=8.1 \times 10^{3} \\
& K_{\mathrm{f}}=K_{1} K_{2}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]}{\left[\mathrm{Ag}^{+}\right]\left[\mathrm{NH}_{3}\right]^{2}}=1.7 \times 10^{7} \quad \text { at } 25^{\circ} \mathrm{C}
\end{aligned}
$$

The stability of a complex ion is measured by its formation constant $K_{f}$ (or stability constant), the equilibrium constant for formation of the complex ion from the hydrated metal cation. The large value of $K_{\mathrm{f}}$ for $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$means that this complex ion is quite stable, and nearly all the $\mathrm{Ag}^{+}$ion in an aqueous ammonia solution is therefore present in the form of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$(see Worked Example 16.12).

The net reaction for dissolution of AgCl in aqueous ammonia is the sum of the equations for the dissolution of AgCl in water and the reaction of $\mathrm{Ag}^{+}(a q)$ with $\mathrm{NH}_{3}(\mathrm{aq})$ to give $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$:

$$
\begin{aligned}
& \mathrm{AgCl}(s) \rightleftharpoons \mathrm{Ag}^{+}(a q)+\mathrm{Cl}^{-}(a q) \\
& \mathrm{Ag}^{+}(a q)+2 \mathrm{NH}_{3}(a q) \\
& \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}(a q) \\
& \text { Net: } \quad \mathrm{AgCl}(s)+2 \mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}(a q)+\mathrm{Cl}^{-}(a q)
\end{aligned}
$$

Its equilibrium constant $K$ is the product of the equilibrium constants for the reactions added:

$$
K=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}\right]\left[\mathrm{Cl}^{-}\right]}{\left[\mathrm{NH}_{3}\right]^{2}}=\left(K_{\mathrm{sp}}\right)\left(K_{\mathrm{f}}\right)=\left(1.8 \times 10^{-10}\right)\left(1.7 \times 10^{7}\right)=3.1 \times 10^{-3}
$$

Because $K$ is much larger than $K_{\text {sp }}$, the solubility equilibrium for AgCl in the presence of ammonia lies much farther to the right than it does in the absence of ammonia. The increase in the solubility of AgCl on addition of ammonia is shown graphically in Figure 16.14. In general, the solubility of an ionic compound increases when the metal cation is tied up in the form of a complex ion. The quantitative effect of complex formation on the solubility of AgCl is explored in Worked Example 16.13.


## Worked Example 16.12

What are the concentrations of $\mathrm{Ag}^{+}, \mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}$, and $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$in a solution prepared by adding 0.10 mol of $\mathrm{AgNO}_{3}$ to 1.0 L of $3.0 \mathrm{M} \mathrm{NH}_{3}$ ? $K_{\mathrm{f}}=1.7 \times 10^{7}$, $K_{1}=2.1 \times 10^{3}, K_{2}=8.1 \times 10^{3}$

## Strategy

Because $K_{1}, K_{2}$, and $K_{\mathrm{f}}$ for $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$are all large numbers, nearly all the $\mathrm{Ag}^{+}$from $\mathrm{AgNO}_{3}$ will be converted to $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$:

$$
\mathrm{Ag}^{+}(a q)+2 \mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}(a q) \quad K_{\mathrm{f}}=1.7 \times 10^{7}
$$

To calculate the concentrations, $\mathrm{it}^{\prime}$ 's convenient to imagine that $100 \%$ of the $\mathrm{Ag}^{+}$is converted to $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$, followed by a tiny amount of back-reaction [dissociation of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$] to give a small equilibrium concentration of $\mathrm{Ag}^{+}$.

## Solution

Conversion of $0.10 \mathrm{~mol} / \mathrm{L}$ of $\mathrm{Ag}^{+}$to $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$consumes $0.20 \mathrm{~mol} / \mathrm{L}$ of $\mathrm{NH}_{3}$. Assuming $100 \%$ conversion to $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$, the following concentrations are obtained:

$$
\begin{aligned}
& {\left[\mathrm{Ag}^{+}\right]=0 \mathrm{M}} \\
& {\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]=0.10 \mathrm{M}} \\
& {\left[\mathrm{NH}_{3}\right]=3.0-0.20=2.8 \mathrm{M}}
\end{aligned}
$$

Dissociation of $x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$in the back-reaction produces $x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{Ag}^{+}$ and $2 x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{NH}_{3}$. Therefore, the equilibrium concentrations (in mol/L) are

$$
\begin{aligned}
& {\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}\right]=0.10-x} \\
& {\left[\mathrm{Ag}^{+}\right]=x} \\
& {\left[\mathrm{NH}_{3}\right]=2.8+2 x}
\end{aligned}
$$

4 FIGURE 16.14 The solubility of AgCl in aqueous ammonia at $25^{\circ} \mathrm{C}$ increases with increasing ammonia concentration owing to formation of the complex ion $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$. Note that the solubility is plotted on a logarithmic scale.

As with acid-base neutralization reactions, the best approach to doing complex ion formation problems is to allow the reaction to go to completion and then let the system equilibrate.

Let's summarize our reasoning in a table under the balanced equation:

| $\mathbf{A g}^{+}(\boldsymbol{a q})+\mathbf{2} \mathbf{N H}_{\mathbf{3}}(\mathbf{a q})$ | $\rightleftharpoons$ | $\mathbf{A g}\left(\mathbf{N H}_{\mathbf{3}} \mathbf{)}_{\mathbf{2}}{ }^{+}(\boldsymbol{a q})\right.$ |
| :--- | :--- | :--- |
| 0.10 | 3.0 | 0 |
| 0 | 2.8 | 0.10 |
| $x$ | $2.8+2 x$ | $0.10-x$ |

Substituting the equilibrium concentrations into the expression for $K_{\mathrm{f}}$, and making the approximation that $x$ is negligible compared to 0.10 (and to 2.8 ) gives

$$
\begin{aligned}
& K_{\mathrm{f}}=1.7 \times 10^{7}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]}{\left[\mathrm{Ag}^{+}\right]\left[\mathrm{NH}_{3}\right]^{2}}=\frac{0.10-x}{(x)(2.8+2 x)^{2}} \approx \frac{0.10}{(x)(2.8)^{2}} \\
& {\left[\mathrm{Ag}^{+}\right]=x=\frac{0.10}{\left(1.7 \times 10^{7}\right)(2.8)^{2}}=7.5 \times 10^{-10} \mathrm{M}} \\
& {\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]=0.10-x=0.10-\left(7.5 \times 10^{-10}\right)=0.10 \mathrm{M}}
\end{aligned}
$$

The concentration of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}$can be calculated from either of the stepwise equilibria. Let's use the equilibrium equation for formation of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}$from $\mathrm{Ag}^{+}$:

$$
\begin{aligned}
& K_{1}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]}{\left[\mathrm{Ag}^{+}\right]\left[\mathrm{NH}_{3}\right]}=2.1 \times 10^{3} \\
& {\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]=K_{1}\left[\mathrm{Ag}^{+}\right]\left[\mathrm{NH}_{3}\right]=\left(2.1 \times 10^{3}\right)\left(7.5 \times 10^{-10}\right)(2.8)=4.4 \times 10^{-6} \mathrm{M}}
\end{aligned}
$$

Thus, nearly all the $\mathrm{Ag}^{+}$is in the form of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$.
$\checkmark$ BALLPARK CHECK The approximate equilibrium concentrations are $\left[\mathrm{Ag}^{+}\right]=$ $7 \times 10^{-10} \mathrm{M},\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]=4 \times 10^{-6} \mathrm{M},\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]=0.1 \mathrm{M}$, and $\left[\mathrm{NH}_{3}\right]=3 \mathrm{M}$. We can check these results by substituting them into the equilibrium constant expressions for $K_{f}$ and $K_{1}$ :

$$
\begin{aligned}
& K_{\mathrm{f}}=1.7 \times 10^{7}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]}{\left[\mathrm{Ag}^{+}\right]\left[\mathrm{NH}_{3}\right]^{2}} \approx \frac{0.1}{\left(7 \times 10^{-10}\right)(3)^{2}}=2 \times 10^{7} \\
& K_{1}=2.1 \times 10^{3}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)^{+}\right]}{\left[\mathrm{Ag}^{+}\right]\left[\mathrm{NH}_{3}\right]} \approx \frac{4 \times 10^{-6}}{\left(7 \times 10^{-10}\right)(3)}=2 \times 10^{3}
\end{aligned}
$$

The ballpark estimates of $K_{f}$ and $K_{1}$ agree with the experimental values.

## Worked Example 16.13

Calculate the molar solubility of AgCl at $25^{\circ} \mathrm{C}$ in:
(a) pure water
(b) $3.0 \mathrm{M} \mathrm{NH}_{3}$

## Strategy

Write the balanced equation for the dissolution reaction, and define $x$ as the number of moles per liter of AgCl that dissolves. Then, express the equilibrium concentrations in terms of $x$ and substitute them into the appropriate equilibrium equation. Solving for $x$ gives the molar solubility.

## Solution

(a) In pure water, the solubility equilibrium is

$$
\mathrm{AgCl}(s) \rightleftharpoons \mathrm{Ag}^{+}(a q)+\mathrm{Cl}^{-}(a q)
$$

Substituting the equilibrium concentrations $(x \mathrm{~mol} / \mathrm{L})$ into the expression for $K_{\text {sp }}$ gives

$$
\begin{aligned}
& K_{\mathrm{sp}}=1.8 \times 10^{-10}=\left[\mathrm{Ag}^{+}\right]\left[\mathrm{Cl}^{-}\right]=(x)(x) \\
& x=\text { Molar solubility }=\sqrt{1.8 \times 10^{-10}}=1.3 \times 10^{-5} \mathrm{M}
\end{aligned}
$$

(b) The balanced equation for dissolution of AgCl in aqueous $\mathrm{NH}_{3}$ is

$$
\mathrm{AgCl}(s)+2 \mathrm{NH}_{3}(a q) \rightleftharpoons \mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}(a q)+\mathrm{Cl}^{-}(a q) \quad K=3.1 \times 10^{-3}
$$

If we define $x$ as the number of moles per liter of AgCl that dissolves, then the saturated solution contains $x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}, x \mathrm{~mol} / \mathrm{L}$ of $\mathrm{Cl}^{-}$, and $(3.0-2 x) \mathrm{mol} / \mathrm{L}$ of $\mathrm{NH}_{3}$. (We're assuming that essentially all the $\mathrm{Ag}^{+}$is in the form of $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$, as proved in Worked Example 16.12.) Substituting the equilibrium concentrations into the equilibrium equation gives

$$
K=3.1 \times 10^{-3}=\frac{\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}^{+}\right]\left[\mathrm{Cl}^{-}\right]}{\left[\mathrm{NH}_{3}\right]^{2}}=\frac{(x)(x)}{(3.0-2 x)^{2}}
$$

Taking the square root of both sides, we obtain

$$
\begin{aligned}
& 5.6 \times 10^{-2}=\frac{x}{3.0-2 x} \\
& x=\left(5.6 \times 10^{-2}\right)(3.0-2 x)=0.17-0.11 x \\
& x=\frac{0.17}{1.11}=0.15 \mathrm{M}
\end{aligned}
$$

The molar solubility of AgCl in $3.0 \mathrm{M} \mathrm{NH}_{3}$ is 0.15 M . Thus, AgCl is much more soluble in aqueous $\mathrm{NH}_{3}$ than in pure water, as shown in Figure 16.14.
$\checkmark$ BALLPARK CHECK Check the calculated equilibrium concentrations by substituting them into the appropriate equilibrium equation. For part (b), for example, $\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]=\left[\mathrm{Cl}^{-}\right]=x=0.15 \mathrm{M}$ and $\left[\mathrm{NH}_{3}\right]=3.0-2 x=2.7 \mathrm{M}$. Since $\left[\mathrm{NH}_{3}\right]$ is $10 \%$ less than $3 \mathrm{M}, \mathrm{K}=\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}\right]\left[\mathrm{Cl}^{-}\right] /\left[\mathrm{NH}_{3}\right]^{2}$ is about $20 \%$ greater than $(0.15 / 3)^{2}=(0.05)^{2}=2.5 \times 10^{-3}$. The ballpark estimate and the experimental value of $K=3.1 \times 10^{-3}$ agree .

- PROBLEM 16.27 In an excess of $\mathrm{NH}_{3}(a q), \mathrm{Cu}^{2+}$ ion forms a deep blue complex ion, $\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$, which has a formation constant $K_{\mathrm{f}}=5.6 \times 10^{11}$. Calculate the concentration of $\mathrm{Cu}^{2+}$ in a solution prepared by adding $5.0 \times 10^{-3} \mathrm{~mol}^{2} \mathrm{CuSO}_{4}$ to 0.500 L of $0.40 \mathrm{M} \mathrm{NH}_{3}$.
- PROBLEM 16.28 The "fixing" of photographic film involves dissolving unexposed silver bromide in a thiosulfate $\left(\mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}\right)$ solution:

$$
\operatorname{AgBr}(s)+2 \mathrm{~S}_{2} \mathrm{O}_{3}{ }^{2-}(a q) \rightleftharpoons \mathrm{Ag}\left(\mathrm{~S}_{2} \mathrm{O}_{3}\right)_{2}{ }^{3-}(a q)+\mathrm{Br}^{-}(a q)
$$

Using $K_{\text {sp }}=5.4 \times 10^{-13}$ for AgBr and $K_{\mathrm{f}}=4.7 \times 10^{13}$ for $\mathrm{Ag}\left(\mathrm{S}_{2} \mathrm{O}_{3}\right)_{2}{ }^{3-}$, calculate the equilibrium constant $K$ for the dissolution reaction, and calculate the molar solubility of AgBr in $0.10 \mathrm{M} \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$.

## Amphoterism

We saw in Section 14.9 that amphoteric oxides, such as aluminum oxide, are soluble both in strongly acidic and in strongly basic solutions:

$$
\begin{array}{ll}
\text { In acid: } & \mathrm{Al}_{2} \mathrm{O}_{3}(s)+6 \mathrm{H}_{3} \mathrm{O}^{+}(a q) \rightleftharpoons 2 \mathrm{Al}^{3+}(a q)+9 \mathrm{H}_{2} \mathrm{O}(l) \\
\text { In base: } & \mathrm{Al}_{2} \mathrm{O}_{3}(s)+2 \mathrm{OH}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons 2 \mathrm{Al}(\mathrm{OH})_{4}^{-}(a q)
\end{array}
$$

The corresponding hydroxides behave similarly (Figure 16.15):
In acid: $\mathrm{Al}(\mathrm{OH})_{3}(s)+3 \mathrm{H}_{3} \mathrm{O}^{+}(a q) \rightleftharpoons \mathrm{Al}^{3+}(a q)+6 \mathrm{H}_{2} \mathrm{O}(l)$
In base: $\mathrm{Al}(\mathrm{OH})_{3}(s)+\mathrm{OH}^{-}(a q) \rightleftharpoons \mathrm{Al}(\mathrm{OH})_{4}{ }^{-}(a q)$


- This photographic film was immersed in a thiosulfate solution to dissolve the unexposed silver bromide (Interlude, pages 146-147. Because the film is light-sensitive, the light used in photographic darkrooms is low-intensity red light, which has a wavelength in the least energetic region of the visible spectrum (Figure 5.3, page 162).

0Remember from Chapter 14 that amphoteric means able to react as an acid or as a base.

Edward Koubek, Cole McWherter, and George L. Gilbert, "Acid-Base Chemistry of Aluminum Ion in Aqueous Solution," J. Chem. Educ., Vol. 75, 1998, 60.

[^19]FIGURE 16.15 (a) Aluminum hydroxide, a gelatinous white precipitate, forms on addition of aqueous NaOH to $\mathrm{Al}^{3+}(a q)$. (b) The precipitate dissolves on addition of excess aqueous NaOH , yielding the colorless $\mathrm{Al}(\mathrm{OH})_{4}{ }^{-}$ion. (The precipitate also dissolves in aqueous HCl , yielding the colorless $\mathrm{Al}^{3+}$ ion.)

(a)

(b)

Dissolution of $\mathrm{Al}(\mathrm{OH})_{3}$ in excess base is just a special case of the effect of complex-ion formation on solubility: $\mathrm{Al}(\mathrm{OH})_{3}$ dissolves because excess $\mathrm{OH}^{-}$ions convert it to the soluble complex ion $\mathrm{Al}(\mathrm{OH})_{4}{ }^{-}$(aluminate ion). The effect of pH on the solubility of $\mathrm{Al}(\mathrm{OH})_{3}$ is shown in Figure 16.16.

FIGURE 16.16 A plot of solubility versus pH shows that $\mathrm{Al}(\mathrm{OH})_{3}$ is an amphoteric hydroxide. $\mathrm{Al}(\mathrm{OH})_{3}$ is essentially insoluble between pH 4 and 10, but it dissolves both in strongly acidic and in strongly basic solutions.

## r



Other examples of amphoteric hydroxides include $\mathrm{Zn}(\mathrm{OH})_{2}, \mathrm{Cr}(\mathrm{OH})_{3}, \mathrm{Sn}(\mathrm{OH})_{2}$, and $\mathrm{Pb}(\mathrm{OH})_{2}$, which react with excess $\mathrm{OH}^{-}$ions to form the soluble complex ions $\mathrm{Zn}(\mathrm{OH})_{4}{ }^{2-}$ (zincate ion), $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}$(chromite ion), $\mathrm{Sn}(\mathrm{OH})_{3}{ }^{-}$(stannite ion), and $\mathrm{Pb}(\mathrm{OH})_{3}{ }^{-}$(plumbite ion), respectively. By contrast, basic hydroxides, such as $\mathrm{Mn}(\mathrm{OH})_{2}, \mathrm{Fe}(\mathrm{OH})_{2}$, and $\mathrm{Fe}(\mathrm{OH})_{3}$, dissolve in strong acid but not in strong base.

The dissolution of $\mathrm{Al}_{2} \mathrm{O}_{3}$ in base is important in the production of aluminum metal from its ore. Aluminum is mined as bauxite $\left(\mathrm{Al}_{2} \mathrm{O}_{3} \cdot x \mathrm{H}_{2} \mathrm{O}\right)$, a hydrated oxide that is always contaminated with $\mathrm{Fe}_{2} \mathrm{O}_{3}$ and $\mathrm{SiO}_{2}$. In the Bayer process, $\mathrm{Al}_{2} \mathrm{O}_{3}$ is purified by treating bauxite with hot aqueous NaOH . Aluminum oxide and $\mathrm{SiO}_{2}$ dissolve, forming $\mathrm{Al}(\mathrm{OH})_{4}{ }^{-}$and $\mathrm{SiO}_{3}{ }^{2-}$ (silicate ion), but $\mathrm{Fe}_{2} \mathrm{O}_{3}$ remains undissolved. Subsequent filtration removes $\mathrm{Fe}_{2} \mathrm{O}_{3}$, and treatment of the filtrate with a weak acid ( $\mathrm{CO}_{2}$ in air) precipitates $\mathrm{Al}(\mathrm{OH})_{3}$, leaving $\mathrm{SiO}_{3}{ }^{2-}$ in solution. Removal of water from $\mathrm{Al}(\mathrm{OH})_{3}$ by heating gives pure $\mathrm{Al}_{2} \mathrm{O}_{3}$, which is then converted to aluminum metal by electrolysis (see Section 18.12).

### 16.13 Precipitation of Ionic Compounds

A common problem in chemistry is to decide whether a precipitate of an ionic compound will form when solutions that contain the constituent ions are mixed. For example, will $\mathrm{CaF}_{2}$ precipitate on mixing solutions of $\mathrm{CaCl}_{2}$ and NaF ? In
other words, will the dissolution reaction proceed in the reverse direction, from right to left?

$$
\mathrm{CaF}_{2}(s) \rightleftharpoons \mathrm{Ca}^{2+}(a q)+2 \mathrm{~F}^{-}(a q)
$$

We touched on this question briefly in Section 4.4 when we looked at solubility rules, but we can now get a more quantitative view. The answer depends on the value of the ion product (IP), a number defined by the expression

$$
\mathrm{IP}=\left[\mathrm{Ca}^{2+}\right]_{t}\left[\mathrm{~F}^{-}\right]_{t}^{2}
$$

The IP is defined in the same way as $K_{\text {sp }}$, except that the concentrations in the expression for IP are initial concentrations (that is, arbitrary concentrations at time $t$ ), not necessarily equilibrium concentrations. Thus, the IP is actually a reaction quotient $Q_{c}$ (Section 13.5), but the term ion product is more descriptive because the equilibrium constant expression isn't a quotient.

If the value of IP is greater than $K_{\text {sp }}$, the solution is supersaturated with respect to $\mathrm{CaF}_{2}$-a nonequilibrium situation. In that case, $\mathrm{CaF}_{2}$ will precipitate, thus reducing the ion concentrations until IP equals $K_{\mathrm{sp}}$. At that point, solubility equilibrium is reached and the solution is saturated.

In general, we only need to calculate the value of IP and then compare it with $K_{\mathrm{sp}}$ to decide whether an ionic compound will precipitate. Three cases arise:

- If IP $>K_{\text {sp }}$, the solution is supersaturated and precipitation will occur.
- If IP $=K_{\text {sp }}$, the solution is saturated and equilibrium exists already.
- If IP $<K_{s p}$, the solution is unsaturated and precipitation will not occur.
R. A. Pacer, "Will a precipitate form? Will it dissolve?" J. Chem. Educ., Vol. 71, 1994, 69. Principles of ionic compound precipitate formation are shown in a series of four colorful demonstrations: (1) Yellow $\mathrm{PbI}_{2}$ is formed only when $Q>K_{\text {sp }}$. (2) Upon addition of aqueous ammonia, green $\mathrm{NiCO}_{3}(s)$ is dissolved due to the formation of the blue complex ion $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right]^{2+}$. (3) Kinetic effects are seen when $\mathrm{MgC}_{2} \mathrm{O}_{4}(s)$ fails to form at room temperature from a solution having $Q>K_{\text {sp }}$ but does form when the solution is heated with stirring to $90^{\circ} \mathrm{C}$. (4) Several $\mathrm{Ag}(\mathrm{I})$ precipitates and complex ions are formed when $\mathrm{OH}^{-}, \mathrm{Cl}^{-}, \mathrm{NH}_{3}, \mathrm{Br}^{-}, \mathrm{S}_{2} \mathrm{O}_{3}{ }^{2-}, \mathrm{I}^{-}$, and $\mathrm{S}^{2-}$ are successively added to a solution containing $\mathrm{Ag}^{+}$.


## Worked Example 16.14

Will a precipitate form when 0.150 L of $0.10 \mathrm{M} \mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}$ and 0.100 L of 0.20 M NaCl are mixed?

## Strategy

Use the solubility rules (Section 4.4) to decide which ions might form a precipitate, and calculate their concentrations after mixing. Then calculate the IP for the possible precipitate and compare it with the value of $K_{\text {sp }}$.

## Solution

After the two solutions are mixed, the combined solution contains $\mathrm{Pb}^{2+}, \mathrm{NO}_{3}{ }^{-}, \mathrm{Na}^{+}$, and $\mathrm{Cl}^{-}$ions and has a volume of $0.150 \mathrm{~L}+0.100 \mathrm{~L}=0.250 \mathrm{~L}$. Because sodium salts and nitrate salts are soluble in water, the only compound that might precipitate is $\mathrm{PbCl}_{2}$, which has $K_{\mathrm{sp}}=1.2 \times 10^{-5}$ (Appendix C ). To calculate the value of IP for $\mathrm{PbCl}_{2}$, first calculate the number of moles of $\mathrm{Pb}^{2+}$ and $\mathrm{Cl}^{-}$in the combined solution:

$$
\begin{aligned}
& \text { Moles } \mathrm{Pb}^{2+}=(0.150 \mathrm{~L})(0.10 \mathrm{~mol} / \mathrm{L})=1.5 \times 10^{-2} \mathrm{~mol} \\
& \text { Moles } \mathrm{Cl}^{-}=(0.100 \mathrm{~L})(0.20 \mathrm{~mol} / \mathrm{L})=2.0 \times 10^{-2} \mathrm{~mol}
\end{aligned}
$$

Then convert moles to molar concentrations:

$$
\begin{aligned}
& {\left[\mathrm{Pb}^{2+}\right]=\frac{1.5 \times 10^{-2} \mathrm{~mol}}{0.250 \mathrm{~L}}=6.0 \times 10^{-2} \mathrm{M}} \\
& {\left[\mathrm{Cl}^{-}\right]=\frac{2.0 \times 10^{-2} \mathrm{~mol}}{0.250 \mathrm{~L}}=8.0 \times 10^{-2} \mathrm{M}}
\end{aligned}
$$



The ion product is

$$
\mathrm{IP}=\left[\mathrm{Pb}^{2+}\right]_{t}\left[\mathrm{Cl}^{-}\right]_{t}^{2}=\left(6.0 \times 10^{-2}\right)\left(8.0 \times 10^{-2}\right)^{2}=3.8 \times 10^{-4}
$$

Since $K_{\mathrm{sp}}=1.2 \times 10^{-5}$, IP is greater than $K_{\text {sp }}$, and therefore $\mathrm{PbCl}_{2}$ will precipitate.

Like oxides, which react with $\mathrm{H}^{+}$to form $\mathrm{H}_{2} \mathrm{O}$, sulfides become more soluble on addition of $\mathrm{H}^{+}$due to the formation of the weak acid $\mathrm{H}_{2} \mathrm{~S}$.

Separation of lons by Selective Precipitation activity

- PROBLEM 16.29 Will a precipitate form on mixing equal volumes of the following solutions?
(a) $3.0 \times 10^{-3} \mathrm{M} \mathrm{BaCl}_{2}$ and $2.0 \times 10^{-3} \mathrm{M} \mathrm{Na}_{2} \mathrm{CO}_{3}$
(b) $1.0 \times 10^{-5} \mathrm{M} \mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$ and $4.0 \times 10^{-5} \mathrm{M} \mathrm{Na}_{2} \mathrm{CO}_{3}$

PROBLEM 16.30 Will a precipitate form on mixing 25 mL of $1.0 \times 10^{-3} \mathrm{M} \mathrm{MnSO}_{4}$, 25 mL of $1.0 \times 10^{-3} \mathrm{M} \mathrm{FeSO}_{4}$, and 200 mL of a buffer solution that is $0.20 \mathrm{M} \mathrm{in}^{2} \mathrm{NH}_{4} \mathrm{Cl}$ and 0.20 M in $\mathrm{NH}_{3}$ ? Values of $K_{\mathrm{sp}}$ can be found in Appendix C.

### 16.14 Separation of Ions by Selective Precipitation

A convenient method for separating a mixture of ions is to add a solution that will precipitate some of the ions but not others. The anions $\mathrm{SO}_{4}{ }^{2-}$ and $\mathrm{Cl}^{-}$, for example, can be separated by addition of a solution of $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$. Insoluble $\mathrm{BaSO}_{4}$ precipitates, but $\mathrm{Cl}^{-}$remains in solution because $\mathrm{BaCl}_{2}$ is soluble. Similarly, the cations $\mathrm{Ag}^{+}$and $\mathrm{Zn}^{2+}$ can be separated by addition of dilute HCl . Silver chloride, AgCl , precipitates, but $\mathrm{Zn}^{2+}$ stays in solution because $\mathrm{ZnCl}_{2}$ is soluble.

In Section 16.15, we'll see that mixtures of metal cations, $\mathrm{M}^{2+}$, can be separated into two groups by selective precipitation of metal sulfides, MS. For example, $\mathrm{Pb}^{2+}, \mathrm{Cu}^{2+}$, and $\mathrm{Hg}^{2+}$, which form very insoluble sulfides, can be separated from $\mathrm{Mn}^{2+}, \mathrm{Fe}^{2+}, \mathrm{Co}^{2+}, \mathrm{Ni}^{2+}$, and $\mathrm{Zn}^{2+}$, which form more soluble sulfides. The separation is carried out in an acidic solution and makes use of the following solubility equilibrium:

$$
\mathrm{MS}(s)+2 \mathrm{H}_{3} \mathrm{O}^{+}(a q) \rightleftharpoons \mathrm{M}^{2+}(a q)+\mathrm{H}_{2} \mathrm{~S}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

The equilibrium constant for this reaction, called the solubility product in acid, is given the symbol $K_{\text {spa }}$ :

$$
K_{\mathrm{spa}}=\frac{\left[\mathrm{M}^{2+}\right]\left[\mathrm{H}_{2} \mathrm{~S}\right]}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]^{2}}
$$

The separation depends on adjusting the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration so that the reaction quotient $Q_{c}$ exceeds $K_{\text {spa }}$ for the very insoluble sulfides but not for the more soluble ones (Table 16.3).

TABLE 16.3 Solubility Products in Acid ( $K_{\text {spa }}$ ) at $25^{\circ} \mathrm{C}$ for Metal Sulfides

| Metal Sulfide, MS | $\boldsymbol{K}_{\text {spa }}$ | Metal Sulfide, MS | $\boldsymbol{K}_{\text {spa }}$ |
| :--- | :--- | :--- | :--- |
| MnS | $3 \times 10^{10}$ | ZnS | $3 \times 10^{-2}$ |
| FeS | $6 \times 10^{2}$ | PbS | $3 \times 10^{-7}$ |
| CoS | 3 | CuS | $6 \times 10^{-16}$ |
| NiS | $8 \times 10^{-1}$ | HgS | $2 \times 10^{-32}$ |

We use $K_{\text {spa }}$ for metal sulfides rather than $K_{\text {sp }}$ for two reasons. First, the ion separations are carried out in acidic solution, so use of $K_{\text {spa }}$ is more convenient. Second, the $K_{\text {sp }}$ values given in many reference books for the reaction $\mathrm{MS}(s) \rightleftharpoons \mathrm{M}^{2+}+\mathrm{S}^{2-}$ are incorrect because they are based on a $K_{\mathrm{a} 2}$ value for
$\mathrm{H}_{2} \mathrm{~S}\left(1.3 \times 10^{-14}\right)$ that is greatly in error. The correct value of $K_{\mathrm{a} 2}$ for $\mathrm{H}_{2} \mathrm{~S}\left(\sim 10^{-19}\right)$ is very small, which means that $\mathrm{S}^{2-}$, like $\mathrm{O}^{2-}$, is highly basic and is not an important species in aqueous solutions. The principal sulfide-containing species in aqueous solutions are $\mathrm{H}_{2} \mathrm{~S}$ in acidic solutions and $\mathrm{HS}^{-}$in basic solutions. The relation between $K_{\text {spa }}$ and the traditional $K_{\mathrm{sp}}, K_{\mathrm{a} 1}$, and $K_{\mathrm{a} 2}$ values is $K_{\mathrm{spa}}=K_{\mathrm{sp}} /\left(K_{\mathrm{a} 1} K_{\mathrm{a} 2}\right)$.

In a typical experiment, the $\mathrm{M}^{2+}$ concentrations are about 0.01 M , and the $\mathrm{H}_{3} \mathrm{O}^{+}$concentration is adjusted to about 0.3 M by adding HCl . The solution is then saturated with $\mathrm{H}_{2} \mathrm{~S}$ gas, which gives an $\mathrm{H}_{2} \mathrm{~S}$ concentration of about 0.10 M . Substituting these concentrations into the equilibrium constant expression, we find that the reaction quotient $Q_{\mathrm{c}}$ is $1 \times 10^{-2}$ :

$$
Q_{\mathrm{c}}=\frac{\left[\mathrm{M}^{2+}\right]_{t}\left[\mathrm{H}_{2} \mathrm{~S}\right]_{t}}{\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]_{t}^{2}}=\frac{(0.01)(0.10)}{(0.3)^{2}}=1 \times 10^{-2}
$$

This value of $Q_{c}$ exceeds $K_{\text {spa }}$ for $\mathrm{PbS}, \mathrm{CuS}$, and HgS (Table 16.3) but does not exceed $K_{\text {spa }}$ for $\mathrm{MnS}, \mathrm{FeS}, \mathrm{CoS}, \mathrm{NiS}$, or ZnS . As a result, $\mathrm{PbS}, \mathrm{CuS}$, and HgS precipitate under these acidic conditions, but $\mathrm{Mn}^{2+}, \mathrm{Fe}^{2+}, \mathrm{Co}^{2+}, \mathrm{Ni}^{2+}$, and $\mathrm{Zn}^{2+}$ remain in solution.

- PROBLEM 16.31 Determine whether $\mathrm{Cd}^{2+}$ can be separated from $\mathrm{Zn}^{2+}$ by bubbling $\mathrm{H}_{2} \mathrm{~S}$ through a 0.3 M HCl solution that contains $0.005 \mathrm{M} \mathrm{Cd}^{2+}$ and $0.005 \mathrm{M} \mathrm{Zn}^{2+}$. ( $K_{\text {spa }}$ for CdS is $8 \times 10^{-7}$.)


### 16.15 Qualitative Analysis

Qualitative analysis is a procedure for identifying the ions present in an unknown solution. The ions are identified by specific chemical tests, but because one ion can interfere with the test for another, the ions must first be separated. In the traditional scheme of analysis for metal cations, some 20 cations are separated initially into five groups by selective precipitation (Figure 16.17).


$\Delta$ Adding $\mathrm{H}_{2} \mathrm{~S}$ to an acidic solution of $\mathrm{Hg}^{2+}$ and $\mathrm{Ni}^{2+}$ precipitates $\mathrm{Hg}^{2+}$ as black HgS but leaves green $\mathrm{Ni}^{2+}$ in solution.


Dale D. Clyde, "Swimming Pools, Hot Rods, and Qualitative Analysis," J. Chem. Educ., Vol. 65, 1988, 911-913.
< FIGURE 16.17 Flowchart for separation of metal cations in qualitative analysis.

FIGURE 16.18 Flame tests for (a) sodium (persistent yellow) and (b) potassium (fleeting violet).

- Group I: $\mathrm{Ag}^{+}, \mathrm{Hg}_{2}{ }^{2+}$, and $\mathrm{Pb}^{2+}$ When aqueous HCl is added to the unknown solution, the cations of group I precipitate as insoluble chlorides- AgCl , $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$, and $\mathrm{PbCl}_{2}$. The cations of groups II-V, which form soluble chlorides, remain in solution. A small amount of the $\mathrm{Pb}^{2+}$ also remains in solution because $\mathrm{PbCl}_{2}$ is slightly soluble.
- Group II: $\mathrm{Pb}^{2+}, \mathrm{Cu}^{2+}, \mathrm{Hg}^{2+}, \mathrm{Cd}^{2+}, \mathrm{Bi}^{3+}$, and $\mathrm{Sn}^{4+}$ After the insoluble chlorides have been removed, the solution is treated with $\mathrm{H}_{2} \mathrm{~S}$ to precipitate the cations of group II as insoluble sulfides- $\mathrm{PbS}, \mathrm{CuS}, \mathrm{HgS}, \mathrm{CdS}, \mathrm{Bi}_{2} \mathrm{~S}_{3}$, and $\mathrm{SnS}_{2}$. Because the solution is strongly acidic at this point $\left(\left[\mathrm{H}_{3} \mathrm{O}^{+}\right] \approx 0.3 \mathrm{M}\right)$, only the most insoluble sulfides precipitate. The acid-insoluble sulfides are then removed from the solution.
- Group III: $\mathrm{Mn}^{2+}, \mathrm{Fe}^{2+}, \mathrm{Co}^{2+}, \mathrm{Ni}^{2+}, \mathrm{Zn}^{2+}, \mathrm{Al}^{3+}$, and $\mathrm{Cr}^{3+}$ At this point, aqueous $\mathrm{NH}_{3}$ is added, neutralizing the acidic solution and giving an $\mathrm{NH}_{4}{ }^{+}-\mathrm{NH}_{3}$ buffer that is slightly basic $(\mathrm{pH} \approx 8)$. The decrease in $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]$shifts the metal sulfide solubility equilibrium to the left, thus precipitating the $2+$ cations of group III as insoluble sulfides- $\mathrm{MnS}, \mathrm{FeS}, \mathrm{CoS}, \mathrm{NiS}$, and ZnS . The $3+$ cations precipitate from the basic solution, not as sulfides, but as insoluble hydrox-ides- $\mathrm{Al}(\mathrm{OH})_{3}$ and $\mathrm{Cr}(\mathrm{OH})_{3}$.
- Group IV: $\mathrm{Ca}^{2+}$ and $\mathrm{Ba}^{2+}$ After the base-insoluble sulfides and the insoluble hydroxides have been removed, the solution is treated with $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ to precipitate the cations of group IV as insoluble carbonates- $\mathrm{CaCO}_{3}$ and $\mathrm{BaCO}_{3}$. Magnesium carbonate does not precipitate at this point because $\left[\mathrm{CO}_{3}{ }^{2-}\right]$ in the $\mathrm{NH}_{4}{ }^{+}-\mathrm{NH}_{3}$ buffer is maintained at a low value.
- Group $V$ : $\mathrm{Na}^{+}, \mathrm{K}^{+}$, and $\mathrm{Mg}^{2+}$ The only ions remaining in solution at this point are those whose chlorides, sulfides, and carbonates are soluble under conditions of the previous reactions. Magnesium ion is separated and identified by addition of a solution of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}$; if $\mathrm{Mg}^{2+}$ is present, a white precipitate of $\mathrm{Mg}\left(\mathrm{NH}_{4}\right) \mathrm{PO}_{4}$ forms. The alkali metal ions are usually identified by the characteristic colors that they impart to a Bunsen flame (Figure 16.18).

(a)

(b)

Once the cations have been separated into groups, further separations and specific tests are carried out to determine the presence or absence of the ions in each group. In group I, for example, lead can be separated from silver and mercury by treating the precipitate with hot water. The more soluble $\mathrm{PbCl}_{2}$ dissolves, but the less soluble AgCl and $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$ do not. To test for $\mathrm{Pb}^{2+}$, the solid chlorides are removed, and the solution is treated with a solution of $\mathrm{K}_{2} \mathrm{CrO}_{4}$. If $\mathrm{Pb}^{2+}$ is present, a yellow precipitate of $\mathrm{PbCrO}_{4}$ forms.

Detailed procedures for separating and identifying all the ions can be found in general chemistry laboratory manuals. Although modern methods of metal-ion analysis employ sophisticated analytical instruments, qualitative analysis is still included in many general chemistry laboratory courses because it is an excellent vehicle for developing laboratory skills and for learning about acid-base, solubility, and complex-ion equilibria.


A When aqueous potassium chromate is added to a solution that contains $\mathrm{Pb}^{2+}$, a yellow precipitate of $\mathrm{PbCrO}_{4}$ forms.

## Interlude Analyzing Proteins by Electrophoresis



- Muscle tissue is made of protein filaments.



High pH; basic sites are uncharged

FIGURE 16.19 An electrophoresis apparatus for protein separation. An aqueous mixture of proteins is buffered to a given pH and placed in an electric field. Different proteins migrate toward one or the other of the electrodes at a rate dependent on the protein's overall charge. $t$ has been estimated that there are as many as 140,000 different proteins in the human body. Many of these proteins act as enzymes, biological catalysts that regulate the tens of thousands of different reactions going on in your body each minute. Other proteins protect against disease, act as transport agents to move ions and small molecules through the body, or provide mechanical support for muscle, skin, and bone. Regardless of the exact details, virtually all biological processes involve proteins in some way.

As you might imagine, a biochemist faced with the need to purify one specific protein out of a mixture of thousands of substances with similar structures has a very difficult task. Using some knowledge of acid-base chemistry, however, makes the job easier. Proteins have various acidic and basic sites spread throughout their structures. Each of these acidic or basic sites in a given protein has its own $\mathrm{p} K_{\mathrm{a}}$ or $\mathrm{p} K_{\mathrm{b}}$, and each site is therefore either charged or uncharged at a given pH . A protein with an abundance of acidic sites $(\mathrm{AH})$, for example, will be uncharged at a low pH , where dissociation is suppressed, but will gain successively more negative charges as the pH is raised and dissociations begin to occur. Conversely, a protein with an abundance of basic sites (B) will have many positive charges at a low pH , where the basic sites are protonated, but will become successively less charged as the pH is raised and the basic sites are deprotonated. Different proteins have different numbers of acidic and basic sites and therefore have different overall charges at a given pH . By taking advantage of these different overall charges, biochemists can separate protein molecules from one another.




When an aqueous solution of a protein is placed in an electric field between two electrodes, a positively charged protein migrates toward the negative electrode, and a negatively charged protein migrates toward the positive electrode (Figure 16.19). The amount of this movement, called electrophoresis, varies with the size and shape of the protein, with the strength of the electric field, and with the number of charges on the protein. The number of charges, in turn, is determined by the number of acidic and basic sites on the protein and by the pH of the aqueous solution through which the protein moves.

Electrophoresis is routinely used both in research laboratories for isolating new proteins and in clinical laboratories for determining protein concentrations in blood serum. In the protein separation shown in Figure 16.20, blood serum is separated by electrophoresis into a pattern of five or six different protein fractionsalbumin, two $\alpha$-globulins, one or two $\beta$-globulins, and the $\gamma$-globulins. An abnormally high or low reading for a particular fraction can indicate a specific clinical condition.


PROBLEM 16.32 In an electrophoresis experiment, a particular protein migrates toward the negative electrode in the presence of an $\mathrm{H}_{3} \mathrm{PO}_{4}-\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$buffer but migrates toward the positive electrode in the presence of an $\mathrm{H}_{3} \mathrm{BO}_{3}-\mathrm{H}_{2} \mathrm{BO}_{3}{ }^{-}$buffer. Explain.

- PROBLEM 16.33 Consider the separation of proteins by electrophoresis in the presence of an $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}-\mathrm{HPO}_{4}{ }^{2-}$ buffer. If you want to increase the rate at which the proteins migrate toward the negative electrode, should you increase or decrease the concentration ratio $\left[\mathrm{HPO}_{4}{ }^{2-}\right] /\left[\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}\right]$? Explain.

FIGURE 16.20 (a) A normal electrophoresis pattern of blood serum. (b) An abnormal pattern, with elevated $\gamma$-globulin, indicating the possibility of liver disease, collagen disorder, or infection.

Summary

Neutralization reactions involving a strong acid and/or a strong base have very large equilibrium constants $\left(K_{n}\right)$ and proceed nearly $100 \%$ to completion. Weak acid-weak base neutralizations tend not to go to completion.

The common-ion effect is the shift in the position of an equilibrium that occurs when a substance is added that provides more of an ion already involved in the equilibrium. An example is the decrease in percent dissociation of a weak acid on addition of its conjugate base.

A solution of a weak acid and its conjugate base is called a buffer solution because it resists drastic changes in pH . The ability of a buffer solution to absorb small amounts of added $\mathrm{H}_{3} \mathrm{O}^{+}$or $\mathrm{OH}^{-}$without a significant change in pH (buffer capacity) increases with increasing amounts of weak acid and conjugate base. The pH of a buffer solution has a value close to the $\mathrm{p} K_{\mathrm{a}}\left(-\log \mathrm{K}_{\mathrm{a}}\right)$ of the weak acid and can be calculated from the Henderson-Hasselbalch equation:

$$
\mathrm{pH}=\mathrm{p} K_{\mathrm{a}}+\log \frac{\text { [Conjugate base }]}{[\text { Weak acid }]}
$$

A $\mathbf{p H}$ titration curve is a plot of the pH of a solution as a function of the volume of base (or acid) added in the course of an acid-base titration. For a strong acid-strong base titration, the titration curve exhibits a sharp change in pH in the region of the equivalence point, the point at which stoichiometri-
cally equivalent amounts of acid and base have been mixed together. For weak acid-strong base and weak base-strong acid titrations, the titration curves display a relatively flat region midway to the equivalence point, a smaller change in pH in the region of the equivalence point, and a pH at the equivalence point that is not equal to 7.00.

The solubility product, $\boldsymbol{K}_{\text {sp }}$, for an ionic compound is the equilibrium constant for dissolution of the compound in water. The solubility of the compound and $K_{\text {sp }}$ are related by the equilibrium equation for the dissolution reaction. The solubility of an ionic compound is (1) suppressed by the presence of a common ion in the solution; (2) increased by decreasing the pH if the compound contains a basic anion, such as $\mathrm{OH}^{-}, \mathrm{S}^{2-}$, or $\mathrm{CO}_{3}{ }^{2-}$; and (3) increased by the presence of a Lewis base, such as $\mathrm{NH}_{3}, \mathrm{CN}^{-}$, or $\mathrm{OH}^{-}$, that can bond to the metal cation to form a complex ion. The stability of a complex ion is measured by its formation constant, $K_{\mathbf{f}}$.

When solutions of soluble ionic compounds are mixed, an insoluble compound will precipitate if the ion product (IP) for the insoluble compound exceeds its $K_{\text {sp }}$. The IP is defined in the same way as $K_{\text {sp }}$, except that the concentrations in the expression for IP are not necessarily equilibrium concentrations. Certain metal cations can be separated by selective precipitation of metal sulfides. Selective precipitation is important in qualitative analysis, a procedure for identifying the ions present in an unknown solution.

## Key Words

## Bayer process 700

buffer capacity 674
buffer solution 671
common-ion effect 668
complexion 695
equivalence point 679
formation constant ( $K_{f}$ ) 696
Henderson-Hasselbalch equation 675
ion product (IP) 701
pH titration curve 678
qualitative analysis 703
solubility product ( $K_{\text {sp }}$ ) 689

## solubility product

constant 689
stability constant 696

## Key Concept Summary



## Understanding Key Concepts

Problems 16.1-16.33 appear within the chapter.
16.34 The following pictures represent solutions that contain one or more of the compounds $\mathrm{H}_{2} \mathrm{~A}, \mathrm{NaHA}$, and $\mathrm{Na}_{2} \mathrm{~A}$, where $\mathrm{H}_{2} \mathrm{~A}$ is a weak diprotic acid. ( $\mathrm{Na}^{+}$ions and solvent water molecules have been omitted for clarity.)

(a) Which of the solutions are buffer solutions?
(b) Which solution has the greatest buffer capacity?
16.35 The following pictures represent solutions that contain a weak acid HA ( $\mathrm{p} K_{\mathrm{a}}=6.0$ ) and its sodium salt NaA . $\left(\mathrm{Na}^{+}\right.$ions and solvent water molecules have been omitted for clarity.)


(3)

(4)
(a) Which solution has the highest pH ? Which has the lowest pH ?
(b) Draw a picture that represents the equilibrium state of solution (1) after addition of two $\mathrm{H}_{3} \mathrm{O}^{+}$ ions.
(c) Draw a picture that represents the equilibrium state of solution (1) after addition of two $\mathrm{OH}^{-}$ ions.
16.36 The strong acid HA is mixed with an equal molar amount of aqueous NaOH . Which of the following pictures represents the equilibrium state of the solution? $\left(\mathrm{Na}^{+}\right.$ions and solvent water molecules have been omitted for clarity.)

(1)

(3)

(4)
16.37 The following pictures represent solutions at various stages in the titration of a weak diprotic acid $\mathrm{H}_{2} \mathrm{~A}$ with aqueous NaOH . ( $\mathrm{Na}^{+}$ions and solvent water molecules have been omitted for clarity.)

(a) To which of the following stages do solutions (1)-(4) correspond?
(i) Halfway to the first equivalence point
(ii) At the first equivalence point
(iii) Halfway between the first and second equivalence points
(iv) Beyond the second equivalence point
(b) Which solution has the highest pH ? Which has the lowest pH ?
16.38 The following pictures represent solutions at various stages in the titration of a weak base $B$ with aqueous $\mathrm{HCl} .\left(\mathrm{Cl}^{-}\right.$ions and solvent water molecules have been omitted for clarity.)


(a) To which of the following stages do solutions (1)-(4) correspond?
(i) The initial solution before addition of any HCl
(ii) Halfway to the equivalence point
(iii) At the equivalence point
(iv) Beyond the equivalence point
(b) Is the pH at the equivalence point more or less than 7 ?
16.39 The following pictures represent solutions of AgCl , which also may contain ions other than $\mathrm{Ag}^{+}$and $\mathrm{Cl}^{-}$ that are not shown. If solution (1) is a saturated solution of AgCl , classify solutions (2)-(4) as unsaturated, saturated, or supersaturated.

16.40 The following pictures represent solutions of $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$, which also may contain ions other than $\mathrm{Ag}^{+}$and $\mathrm{CrO}_{4}{ }^{2-}$ that are not shown. Solution (1) is in equilibrium with solid $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$. Will a precipitate of solid $\mathrm{Ag}_{2} \mathrm{CrO}_{4}$ form in solutions (2)-(4)? Explain.

16.41 The following plot shows two titration curves, each representing the titration of 50.0 mL of 0.100 M acid with 0.100 M NaOH :

(a) Which of the two curves represents the titration of a strong acid, and which a weak acid?
(b) What is the approximate pH at the equivalence point for each of the acids?
(c) What is the approximate $\mathrm{p} K_{\mathrm{a}}$ of the weak acid?

## Additional Problems

## Neutralization Reactions

16.42 Is the pH greater than, equal to, or less than 7 after neutralization of each of the following pairs of acids and bases?
(a) HI and NaOH
(b) HOCl and $\mathrm{Ba}(\mathrm{OH})_{2}$
(c) $\mathrm{HNO}_{3}$ and aniline $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}\right)$
(d) Benzoic acid $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right)$ and KOH
16.43 Is the pH greater than, equal to, or less than 7 after neutralization of each of the following pairs of acids and bases?
(a) CsOH and $\mathrm{HNO}_{2}$
(b) $\mathrm{NH}_{3}$ and HBr
(c) KOH and $\mathrm{HClO}_{4}$
(d) $\mathrm{NH}_{3}$ and HOBr
16.44 Calculate the equilibrium constant, $K_{n}$, for each neutralization reaction in Problem 16.42, and arrange the four reactions in order of increasing tendency to proceed to completion. See Appendix C for values of $K_{\mathrm{a}}$ and $K_{\mathrm{b}}$.
16.45 Calculate the equilibrium constant, $K_{n}$, for each neutralization reaction in Problem 16.43, and arrange the four reactions in order of increasing tendency to proceed to completion. See Appendix C for values of $K_{\mathrm{a}}$ and $K_{\mathrm{b}}$.
16.46 Which of the following mixtures has the higher pH ?
(a) Equal volumes of 0.10 M HF and 0.10 M NaOH
(b) Equal volumes of 0.10 M HCl and 0.10 M NaOH
16.47 Which of the following mixtures has the lower pH ?
(a) Equal volumes of $0.10 \mathrm{M} \mathrm{HClO}_{4}$ and 0.10 M NaOH
(b) Equal volumes of $0.10 \mathrm{M} \mathrm{HClO}_{4}$ and $0.10 \mathrm{M} \mathrm{NH}_{3}$
16.48 Phenol $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{OH}, \mathrm{K}_{\mathrm{a}}=1.3 \times 10^{-10}\right)$ is a weak acid used in mouthwashes, and pyridine $\left(\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}\right.$, $K_{\mathrm{b}}=1.8 \times 10^{-9}$ ) is a weak base used as a solvent. Calculate the value of $K_{\mathrm{n}}$ for neutralization of phenol by pyridine. Does the neutralization reaction proceed very far toward completion?
16.49 Aniline $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}, K_{\mathrm{b}}=4.3 \times 10^{-10}\right)$ is a weak base used in the manufacture of dyes. Calculate the value of $K_{\mathrm{n}}$ for neutralization of aniline by vitamin C (ascorbic acid, $\mathrm{C}_{6} \mathrm{H}_{8} \mathrm{O}_{6}, \mathrm{~K}_{\mathrm{a}}=8.0 \times 10^{-5}$ ). Does much aniline remain at equilibrium?

## The Common-Ion Effect

16.50 Which of the following substances affects the percent dissociation of $\mathrm{HNO}_{2}$ ?
(a) $\mathrm{NaNO}_{2}$
(b) NaCl
(c) HCl
(d) $\mathrm{Ba}\left(\mathrm{NO}_{2}\right)_{2}$
16.51 Which of the following substances affects the pH of an aqueous $\mathrm{NH}_{3}$ solution?
(a) KOH
(b) $\mathrm{NH}_{4} \mathrm{NO}_{3}$
(c) $\mathrm{NH}_{4} \mathrm{Br}$
(d) KBr
16.52 Does the pH increase, decrease, or remain the same on addition of each of the following?
(a) LiF to an HF solution
(b) KI to an HI solution
(c) $\mathrm{NH}_{4} \mathrm{Cl}$ to an $\mathrm{NH}_{3}$ solution
16.53 Does the pH increase, decrease, or remain the same on addition of each of the following?
(a) $\mathrm{NH}_{4} \mathrm{NO}_{3}$ to an $\mathrm{NH}_{3}$ solution
(b) $\mathrm{Na}_{2} \mathrm{CO}_{3}$ to an $\mathrm{NaHCO}_{3}$ solution
(c) $\mathrm{NaClO}_{4}$ to an NaOH solution
16.54 Calculate the pH of a solution that is 0.25 M in HF and 0.10 M in NaF .
16.55 Calculate the pH of a solution prepared by mixing equal volumes of 0.20 M methylamine $\left(\mathrm{CH}_{3} \mathrm{NH}_{2}\right.$, $K_{\mathrm{b}}=3.7 \times 10^{-4}$ ) and $0.60 \mathrm{M} \mathrm{CH}_{3} \mathrm{NH}_{3} \mathrm{Cl}$.
16.56 Calculate the percent dissociation of 0.10 M hydrazoic acid $\left(\mathrm{HN}_{3}, K_{\mathrm{a}}=1.9 \times 10^{-5}\right)$. Recalculate the percent dissociation of $0.10 \mathrm{M} \mathrm{HN}_{3}$ in the presence of 0.10 M HCl , and explain the change.
16.57 Calculate the pH of 100 mL of $0.30 \mathrm{M} \mathrm{NH}_{3}$ before and after addition of 4.0 g of $\mathrm{NH}_{4} \mathrm{NO}_{3}$, and account for the change. Assume that the volume remains constant.

## Buffer Solutions

16.58 Which of the following gives a buffer solution when equal volumes of the two solutions are mixed?
(a) 0.10 M HF and 0.10 M NaF
(b) 0.10 M HF and 0.10 M NaOH
(c) 0.20 M HF and 0.10 M NaOH
(d) 0.10 M HCl and 0.20 M NaF
16.59 Which of the following gives a buffer solution when equal volumes of the two solutions are mixed?
(a) $0.10 \mathrm{M} \mathrm{NH}_{3}$ and 0.10 M HCl
(b) $0.20 \mathrm{M} \mathrm{NH}_{3}$ and 0.10 M HCl
(c) $0.10 \mathrm{M} \mathrm{NH}_{4} \mathrm{Cl}$ and $0.10 \mathrm{M} \mathrm{NH}_{3}$
(d) $0.20 \mathrm{M} \mathrm{NH}_{4} \mathrm{Cl}$ and 0.10 M NaOH
16.60 Which of the following solutions has the greater buffer capacity: (a) 100 mL of $0.30 \mathrm{M} \mathrm{HNO}_{2}-0.30 \mathrm{M} \mathrm{NaNO}_{2}$ or (b) 100 mL of $0.10 \mathrm{M} \mathrm{HNO}_{2}-0.10 \mathrm{M} \mathrm{NaNO}_{2}$ ? Explain.
16.61 Which of the following solutions has the greater buffer capacity: (a) 50 mL of $0.20 \mathrm{M} \mathrm{NH}_{4} \mathrm{Br}-0.30 \mathrm{M} \mathrm{NH}_{3}$ or (b) 50 mL of $0.40 \mathrm{M} \mathrm{NH}_{4} \mathrm{Br}-0.60 \mathrm{M} \mathrm{NH}_{3}$ ? Explain.
16.62 The following reaction is important in maintaining the pH of blood at a nearly constant value of about 7.4: $\mathrm{H}_{2} \mathrm{CO}_{3}+\mathrm{H}_{2} \mathrm{O} \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}+\mathrm{HCO}_{3}^{-}$. What happens to the position of this equilibrium and the pH when blood absorbs added acid or base?
16.63 Explain how the $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}-\mathrm{HPO}_{4}{ }^{2-}$ buffer system can help to maintain the pH of intracellular fluid at a value close to 7.4.
16.64 Calculate the pH of a buffer solution that is 0.20 M in HCN and 0.12 M in NaCN . Will the pH change if the solution is diluted by a factor of 2 ? Explain.
16.65 Calculate the pH of a buffer solution prepared by dissolving 4.2 g of $\mathrm{NaHCO}_{3}$ and 5.3 g of $\mathrm{Na}_{2} \mathrm{CO}_{3}$ in 0.20 L of water. Will the pH change if the solution volume is increased by a factor of 10 ? Explain.
16.66 Calculate the pH of 0.500 L of a $0.200 \mathrm{M} \mathrm{NH}_{4} \mathrm{Cl}$ $-0.200 \mathrm{M} \mathrm{NH}_{3}$ buffer before and after addition of (a) 0.0050 mol of NaOH and (b) 0.020 mol of HCl . Assume that the volume remains constant.
16.67 Calculate the pH of 0.300 L of a $0.500 \mathrm{M} \mathrm{NaHSO}_{3}-$ $0.300 \mathrm{M} \mathrm{Na}_{2} \mathrm{SO}_{3}$ buffer before and after addition of (a) 5.0 mL of 0.20 M HCl and (b) 5.0 mL of 0.10 M NaOH .
16.68 What is the $\mathrm{p} K_{\mathrm{a}}$ value for each of the following acids? ( $K_{\mathrm{a}}$ values are listed in Appendix C.)
(a) Boric acid $\left(\mathrm{H}_{3} \mathrm{BO}_{3}\right)$
(b) Formic acid $\left(\mathrm{HCO}_{2} \mathrm{H}\right)$
(c) Hypochlorous acid ( HOCl )

How does $\mathrm{p} K_{\mathrm{a}}$ vary as acid strength increases?
16.69 What is the value of $K_{\mathrm{a}}$ for an acid that has the following?
(a) $\mathrm{p} K_{\mathrm{a}}=5.00$
(b) $\mathrm{p} K_{\mathrm{a}}=8.70$

Which of the two acids is weaker?
16.70 Use the Henderson-Hasselbalch equation to calculate the pH of a buffer solution that is 0.25 M in formic acid $\left(\mathrm{HCO}_{2} \mathrm{H}\right)$ and 0.50 M in sodium formate $\left(\mathrm{HCO}_{2} \mathrm{Na}\right)$.
16.71 Use the Henderson-Hasselbalch equation to calculate the ratio of $\mathrm{H}_{2} \mathrm{CO}_{3}$ to $\mathrm{HCO}_{3}{ }^{-}$in blood having a pH of 7.40.
16.72 In what volume ratio should you mix 1.0 M solutions of $\mathrm{NH}_{4} \mathrm{Cl}$ and $\mathrm{NH}_{3}$ to produce a buffer solution having $\mathrm{pH}=9.80$ ?
16.73 Give a recipe for preparing a $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}-\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{Na}$ buffer solution that has $\mathrm{pH}=4.44$.
16.74 You need a buffer solution that has $\mathrm{pH}=7.00$. Which of the following buffer systems should you choose? Explain.
(a) $\mathrm{H}_{3} \mathrm{PO}_{4}$ and $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$
(b) $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$and $\mathrm{HPO}_{4}{ }^{2-}$
(c) $\mathrm{HPO}_{4}{ }^{2-}$ and $\mathrm{PO}_{4}{ }^{3-}$
16.75 Which of the following conjugate acid-base pairs should you choose to prepare a buffer solution that has $\mathrm{pH}=4.50$ ? Explain.
(a) $\mathrm{HSO}_{4}{ }^{-}$and $\mathrm{SO}_{4}{ }^{2-}$
(b) HOCl and $\mathrm{OCl}^{-}$
(c) $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}$ and $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2}{ }^{-}$

## pH Titration Curves

16.76 Consider the titration of 60.0 mL of $0.150 \mathrm{M} \mathrm{HNO}_{3}$ with 0.450 M NaOH .
(a) How many millimoles of $\mathrm{HNO}_{3}$ are present at the start of the titration?
(b) How many milliliters of NaOH are required to reach the equivalence point?
(c) What is the pH at the equivalence point?
(d) Sketch the general shape of the pH titration curve.
16.77 Make a rough plot of pH versus milliliters of acid added for the titration of 50.0 mL of 1.0 M NaOH with 1.0 M HCl . Indicate the pH at the following points, and tell how many milliliters of acid are required to reach the equivalence point.
(a) At the start of the titration
(b) At the equivalence point
(c) After addition of a large excess of acid
16.78 A 60.0 mL sample of a monoprotic acid is titrated with 0.150 M NaOH . If 20.0 mL of base is required to reach the equivalence point, what is the concentration of the acid?
16.79 A 25.0 mL sample of a diprotic acid is titrated with 0.240 M KOH . If 60.0 mL of base is required to reach the second equivalence point, what is the concentration of the acid?
16.80 A 50.0 mL sample of 0.120 M HBr is titrated with 0.240 M NaOH . Calculate the pH after addition of the following volumes of base, and construct a plot of pH versus milliliters of NaOH added.
(a) 0.0 mL
(b) 20.0 mL
(c) 24.9 mL
(d) 25.0 mL
(e) 25.1 mL
(f) 40.0 mL
16.81 A 40.0 mL sample of $0.150 \mathrm{M} \mathrm{Ba}(\mathrm{OH})_{2}$ is titrated with $0.400 \mathrm{M} \mathrm{HNO}_{3}$. Calculate the pH after addition of the following volumes of acid, and plot the pH versus milliliters of $\mathrm{HNO}_{3}$ added.
(a) 0.0 mL
(b) 10.0 mL
(c) 20.0 mL
(d) 30.0 mL
(e) 40.0 mL
16.82 Consider the titration of 40.0 mL of 0.250 M HF with 0.200 M NaOH . How many milliliters of base are required to reach the equivalence point? Calculate the pH at each of the following points:
(a) After addition of 10.0 mL of base
(b) Halfway to the equivalence point
(c) At the equivalence point
(d) After addition of 80.0 mL of base
16.83 A 100.0 mL sample of 0.100 M methylamine $\left(\mathrm{CH}_{3} \mathrm{NH}_{2}\right.$, $\left.K_{\mathrm{b}}=3.7 \times 10^{-4}\right)$ is titrated with $0.250 \mathrm{M} \mathrm{HNO}_{3}$. Calculate the pH after addition of each of the following volumes of acid:
(a) 0.0 mL
(b) 20.0 mL
(c) 40.0 mL
(d) 60.0 mL
16.84 Consider the titration of 50.0 mL of a 0.100 M solution of the protonated form of the amino acid alanine $\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right.$; $K_{\mathrm{a} 1}=4.6 \times 10^{-3}, K_{\mathrm{a} 2}=2.0 \times 10^{-10}$ ) with 0.100 M NaOH . Calculate the pH after addition of each of the following volumes of base:
(a) 10.0 mL
(b) 25.0 mL
(c) 50.0 mL
(d) 75.0 mL
(e) 100.0 mL
16.85 Consider the titration of 25.0 mL of $0.0200 \mathrm{M} \mathrm{H}_{2} \mathrm{CO}_{3}$ with 0.0250 M KOH . Calculate the pH after addition of each of the following volumes of base:
(a) 10.0 mL
(b) 20.0 mL
(c) 30.0 mL
(d) 40.0 mL
(e) 50.0 mL
16.86 What is the pH at the equivalence point for titration of 0.10 M solutions of the following acids and bases, and which of the indicators in Figure 15.4 would be suitable for each titration?
(a) $\mathrm{HNO}_{2}$ and NaOH
(b) HI and NaOH
(c) $\mathrm{CH}_{3} \mathrm{NH}_{2}$ (methylamine) and HCl
16.87 What is the pH at the equivalence point for titration of 0.20 M solutions of the following acids and bases, and which of the indicators in Figure 15.4 would be suitable for each titration?
(a) $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{~N}$ (piperidine) and $\mathrm{HNO}_{3}$
(b) $\mathrm{NaHSO}_{3}$ and NaOH
(c) $\mathrm{Ba}(\mathrm{OH})_{2}$ and HBr

## Solubility Equilibria

16.88 For each of the following compounds, write a balanced net ionic equation for dissolution of the compound in water, and write the equilibrium expression for $K_{\text {sp }}$ :
(a) $\mathrm{Ag}_{2} \mathrm{CO}_{3}$
(b) $\mathrm{PbCrO}_{4}$
(c) $\mathrm{Al}(\mathrm{OH})_{3}$
(d) $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$
16.89 For each of the following, write the equilibrium expression for $K_{\text {sp }}$ :
(a) $\mathrm{Ca}(\mathrm{OH})_{2}$
(b) $\mathrm{Ag}_{3} \mathrm{PO}_{4}$
(c) $\mathrm{BaCO}_{3}$
(d) $\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{OH}$
16.90 A particular saturated solution of $\mathrm{PbI}_{2}$ has $\left[\mathrm{Pb}^{2+}\right]=$ $5.0 \times 10^{-3} \mathrm{M}$ and $\left[\mathrm{I}^{-}\right]=1.3 \times 10^{-3} \mathrm{M}$.
(a) What is the value of $K_{\text {sp }}$ for $\mathrm{PbI}_{2}$ ?
(b) What is $\left[\mathrm{I}^{-}\right]$in a saturated solution of $\mathrm{PbI}_{2}$ that has $\left[\mathrm{Pb}^{2+}\right]=2.5 \times 10^{-4} \mathrm{M}$ ?
(c) What is $\left[\mathrm{Pb}^{2+}\right]$ in a saturated solution that has $\left[\mathrm{I}^{-}\right]=2.5 \times 10^{-4} \mathrm{M}$ ?
16.91 A particular saturated solution of $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$ has $\left[\mathrm{Ca}^{2+}\right]=\left[\mathrm{PO}_{4}{ }^{3-}\right]=2.9 \times 10^{-7} \mathrm{M}$.
(a) What is the value of $K_{\text {sp }}$ for $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$ ?
(b) What is $\left[\mathrm{Ca}^{2+}\right]$ in a saturated solution of $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$ that has $\left[\mathrm{PO}_{4}{ }^{3-}\right]=0.010 \mathrm{M}$ ?
(c) What is $\left[\mathrm{PO}_{4}{ }^{3-}\right]$ in a saturated solution that has $\left[\mathrm{Ca}^{2+}\right]=0.010 \mathrm{M}$ ?
16.92 If a saturated solution prepared by dissolving $\mathrm{Ag}_{2} \mathrm{CO}_{3}$ in water has $\left[\mathrm{Ag}^{+}\right]=2.56 \times 10^{-4} \mathrm{M}$, what is the value of $K_{\text {sp }}$ for $\mathrm{Ag}_{2} \mathrm{CO}_{3}$ ?
16.93 Use the following solubility data to calculate a value of $K_{\text {sp }}$ for each compound:
(a) $\mathrm{CdCO}_{3} ; 2.5 \times 10^{-6} \mathrm{M}$
(b) $\mathrm{Ca}(\mathrm{OH})_{2} ; 1.06 \times 10^{-2} \mathrm{M}$
(c) $\mathrm{PbBr}_{2} ; 4.34 \mathrm{~g} / \mathrm{L}$
(d) $\mathrm{BaCrO}_{4} ; 2.8 \times 10^{-3} \mathrm{~g} / \mathrm{L}$
16.94 Use the values of $K_{\text {sp }}$ in Appendix $C$ to calculate the molar solubility of the following compounds:
(a) $\mathrm{BaCrO}_{4}$
(b) $\mathrm{Mg}(\mathrm{OH})_{2}$
(c) $\mathrm{Ag}_{2} \mathrm{SO}_{3}$
16.95 Use the values of $K_{\text {sp }}$ in Appendix $C$ to calculate the solubility of the following compounds (in $\mathrm{g} / \mathrm{L}$ ):
(a) $\mathrm{Ag}_{2} \mathrm{CO}_{3}$
(b) CuBr
(c) $\mathrm{Cu}_{3}\left(\mathrm{PO}_{4}\right)_{2}$

## Factors That Affect Solubility

16.96 Use Le Châtelier's principle to explain the following changes in the solubility of $\mathrm{Ag}_{2} \mathrm{CO}_{3}$ in water:
(a) Decrease on addition of $\mathrm{AgNO}_{3}$
(b) Increase on addition of $\mathrm{HNO}_{3}$
(c) Decrease on addition of $\mathrm{Na}_{2} \mathrm{CO}_{3}$
(d) Increase on addition of $\mathrm{NH}_{3}$
16.97 Use Le Châtelier's principle to predict whether the solubility of $\mathrm{BaF}_{2}$ will increase, decrease, or remain the same on addition of each of the following substances:
(a) HCl
(b) KF
(c) $\mathrm{NaNO}_{3}$
(d) $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$
16.98 Calculate the molar solubility of $\mathrm{PbCrO}_{4}$ in:
(a) Pure water
(b) $1.0 \times 10^{-3} \mathrm{M} \mathrm{K}_{2} \mathrm{CrO}_{4}$
16.99 Calculate the molar solubility of $\mathrm{SrF}_{2}$ in:
(a) $0.010 \mathrm{M} \mathrm{Sr}\left(\mathrm{NO}_{3}\right)_{2}$
(b) 0.010 M NaF
16.100 Which of the following compounds are more soluble in acidic solution than in pure water? Write a balanced net ionic equation for each dissolution reaction.
(a) AgBr
(b) $\mathrm{CaCO}_{3}$
(c) $\mathrm{Ni}(\mathrm{OH})_{2}$
(d) $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$
16.101 Which of the following compounds are more soluble in acidic solution than in pure water? Write a balanced net ionic equation for each dissolution reaction.
(a) MnS
(b) $\mathrm{Fe}(\mathrm{OH})_{3}$
(c) AgCl
(d) $\mathrm{BaCO}_{3}$
16.102 Silver ion reacts with excess $\mathrm{CN}^{-}$to form a colorless complex ion, $\mathrm{Ag}(\mathrm{CN})_{2}{ }^{-}$, which has a formation constant $K_{\mathrm{f}}=3.0 \times 10^{20}$. Calculate the concentration of $\mathrm{Ag}^{+}$in a solution prepared by mixing equal volumes of $2.0 \times 10^{-3} \mathrm{M} \mathrm{AgNO}_{3}$ and 0.20 M NaCN .
16.103 Dissolution of $5.0 \times 10^{-3} \mathrm{~mol}$ of $\mathrm{Cr}(\mathrm{OH})_{3}$ in 1.0 L of 1.0 M NaOH gives a solution of the complex ion $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}\left(K_{\mathrm{f}}=8 \times 10^{29}\right)$. What fraction of the chromium in such a solution is present as uncomplexed $\mathrm{Cr}^{3+}$ ?
16.104 Write a balanced net ionic equation for each of the following dissolution reactions, and use the appropriate $K_{\mathrm{sp}}$ and $K_{\mathrm{f}}$ values in Appendix C to calculate the equilibrium constant for each.
(a) AgI in aqueous NaCN to form $\mathrm{Ag}(\mathrm{CN})_{2}{ }^{-}$
(b) $\mathrm{Al}(\mathrm{OH})_{3}$ in aqueous NaOH to form $\mathrm{Al}(\mathrm{OH})_{4}{ }^{-}$
(c) $\mathrm{Zn}(\mathrm{OH})_{2}$ in aqueous $\mathrm{NH}_{3}$ to form $\mathrm{Zn}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$
16.105 Write a balanced net ionic equation for each of the following dissolution reactions, and use the appropriate $K_{\text {sp }}$ and $K_{\mathrm{f}}$ values in Appendix C to calculate the equilibrium constant for each.
(a) $\mathrm{Zn}(\mathrm{OH})_{2}$ in aqueous NaOH to form $\mathrm{Zn}(\mathrm{OH})_{4}{ }^{2-}$
(b) $\mathrm{Cu}(\mathrm{OH})_{2}$ in aqueous $\mathrm{NH}_{3}$ to form $\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$
(c) AgBr in aqueous $\mathrm{NH}_{3}$ to form $\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}{ }^{+}$
16.106 Calculate the molar solubility of AgI in:
(a) Pure water
(b) $0.10 \mathrm{M} \mathrm{NaCN} ; K_{\mathrm{f}}$ for $\operatorname{Ag}(\mathrm{CN})_{2}{ }^{-}$is $3.0 \times 10^{20}$
16.107 Calculate the molar solubility of $\mathrm{Cr}(\mathrm{OH})_{3}$ in 0.50 M $\mathrm{NaOH} ; \mathrm{K}_{\mathrm{f}}$ for $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}$is $8 \times 10^{29}$.

## Precipitation; Qualitative Analysis

16.108 Will a precipitate of $\mathrm{BaSO}_{4}$ form when 100 mL of $4.0 \times 10^{-3} \mathrm{M} \mathrm{BaCl}_{2}$ and 300 mL of $6.0 \times 10^{-4} \mathrm{M}$ $\mathrm{Na}_{2} \mathrm{SO}_{4}$ are mixed? Explain.
16.109 Will a precipitate of $\mathrm{PbCl}_{2}$ form on mixing equal volumes of $0.010 \mathrm{M} \mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}$ and 0.010 M HCl ? Explain. What minimum $\mathrm{Cl}^{-}$concentration is required to begin precipitation of $\mathrm{PbCl}_{2}$ from $5.0 \times 10^{-3} \mathrm{M} \mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}$ ?
16.110 What compound, if any, will precipitate when 80 mL of $1.0 \times 10^{-5} \mathrm{M} \mathrm{Ba}(\mathrm{OH})_{2}$ is added to 20 mL of $1.0 \times$ $10^{-5} \mathrm{M} \mathrm{Fe}_{2}\left(\mathrm{SO}_{4}\right)_{3}$ ?
16.111 "Hard" water contains alkaline earth cations such as $\mathrm{Ca}^{2+}$, which reacts with $\mathrm{CO}_{3}{ }^{2-}$ to form insoluble deposits of $\mathrm{CaCO}_{3}$. Will a precipitate of $\mathrm{CaCO}_{3}$ form if a 250 mL sample of hard water having $\left[\mathrm{Ca}^{2+}\right]=$ $8.0 \times 10^{-4} \mathrm{M}$ is treated with the following?
(a) 0.10 mL of $2.0 \times 10^{-3} \mathrm{M} \mathrm{Na}_{2} \mathrm{CO}_{3}$
(b) 10 mg of solid $\mathrm{Na}_{2} \mathrm{CO}_{3}$
16.112 The pH of a sample of hard water (Problem 16.111) having $\left[\mathrm{Mg}^{2+}\right]=2.5 \times 10^{-4} \mathrm{M}$ is adjusted to pH 10.80. Will $\mathrm{Mg}(\mathrm{OH})_{2}$ precipitate?
16.113 In qualitative analysis, $\mathrm{Al}^{3+}$ and $\mathrm{Mg}^{2+}$ are separated in an $\mathrm{NH}_{4}{ }^{+}-\mathrm{NH}_{3}$ buffer having $\mathrm{pH} \approx 8$. Assuming cation concentrations of 0.010 M , show why $\mathrm{Al}(\mathrm{OH})_{3}$ precipitates but $\mathrm{Mg}(\mathrm{OH})_{2}$ does not.
16.114 $\mathrm{Can} \mathrm{Fe}^{2+}$ be separated from $\mathrm{Sn}^{2+}$ by bubbling $\mathrm{H}_{2} \mathrm{~S}$ through a 0.3 M HCl solution that contains $0.01 \mathrm{M} \mathrm{Fe}^{2+}$ and $0.01 \mathrm{M} \mathrm{Sn}^{2+}$ ? A saturated solution of $\mathrm{H}_{2} \mathrm{~S}$ has $\left[\mathrm{H}_{2} \mathrm{~S}\right] \approx 0.10 \mathrm{M}$. Values of $K_{\text {spa }}$ are $6 \times 10^{2}$ for FeS and $1 \times 10^{-5}$ for SnS .
16.115 Will CoS precipitate in a solution that is 0.10 M in $\mathrm{Co}\left(\mathrm{NO}_{3}\right)_{2}, 0.5 \mathrm{M}$ in HCl , and 0.10 M in $\mathrm{H}_{2} \mathrm{~S}$ ? Will CoS precipitate if the pH of the solution is adjusted to pH 8 with an $\mathrm{NH}_{4}{ }^{+}-\mathrm{NH}_{3}$ buffer? $\mathrm{K}_{\text {spa }}=3$ for CoS .
16.116 Using the qualitative analysis flowchart in Figure 16.17, tell how you could separate the following pairs of ions:
(a) $\mathrm{Ag}^{+}$and $\mathrm{Cu}^{2+}$
(b) $\mathrm{Na}^{+}$and $\mathrm{Ca}^{2+}$
(c) $\mathrm{Mg}^{2+}$ and $\mathrm{Mn}^{2+}$
(d) $\mathrm{K}^{+}$and $\mathrm{Cr}^{3+}$
16.117 Give a method for separating the following pairs of ions by addition of no more than two substances:
(a) $\mathrm{Hg}_{2}{ }^{2+}$ and $\mathrm{Co}^{2+}$
(b) $\mathrm{Na}^{+}$and $\mathrm{Mg}^{2+}$
(c) $\mathrm{Fe}^{2+}$ and $\mathrm{Hg}^{2+}$
(d) $\mathrm{Ba}^{2+}$ and $\mathrm{Pb}^{2+}$

## General Problems

16.118 Assume that you have three white solids: $\mathrm{NaCl}, \mathrm{KCl}$, and $\mathrm{MgCl}_{2}$. What tests could you do to tell which is which?
16.119 Which of the following pairs of substances, when mixed in any proportion you wish, can be used to prepare a buffer solution?
(a) NaCN and HCN
(b) NaCN and NaOH
(c) HCl and NaCN
(d) HCl and NaOH
(e) HCN and NaOH
16.120 Which of the following pairs gives a buffer solution when equal volumes of the two solutions are mixed?
(a) $0.10 \mathrm{M} \mathrm{NaHCO}_{3}$ and $0.10 \mathrm{M} \mathrm{H}_{2} \mathrm{CO}_{3}$
(b) $0.10 \mathrm{M} \mathrm{NaHCO}_{3}$ and $0.10 \mathrm{M} \mathrm{Na}_{2} \mathrm{CO}_{3}$
(c) $0.10 \mathrm{M} \mathrm{NaHCO}_{3}$ and 0.10 M HCl
(d) $0.20 \mathrm{M} \mathrm{NaHCO}_{3}$ and 0.10 M NaOH
16.121 On the same graph, sketch pH titration curves for titration of (1) a strong acid with a strong base and (2) a weak acid with a strong base. How do the two curves differ with respect to the following?
(a) The initial pH
(b) The pH in the region between the start of the titration and the equivalence point
(c) The pH at the equivalence point
(d) The pH beyond the equivalence point
(e) The volume of base required to reach the equivalence point
16.122 Consider the titration of 50.0 mL of 0.010 M HA $\left(K_{\mathrm{a}}=1.0 \times 10^{-4}\right)$ with 0.010 M NaOH .
(a) Sketch the pH titration curve, and label the equivalence point.
(b) How many milliliters of 0.010 M NaOH are required to reach the equivalence point?
(c) Is the pH at the equivalence point greater than, equal to, or less than 7 ?
(d) What is the pH exactly halfway to the equivalence point?
16.123 Consider saturated solutions of the slightly soluble salts AgBr and $\mathrm{BaCO}_{3}$.
(a) Is the solubility of AgBr increased, decreased, or unaffected by addition of each of the following substances?
(i) HBr
(ii) $\mathrm{HNO}_{3}$
(iii) $\mathrm{AgNO}_{3}$
(iv) $\mathrm{NH}_{3}$
(b) Is the solubility of $\mathrm{BaCO}_{3}$ increased, decreased, or unaffected by addition of each of the following substances?
(i) $\mathrm{HNO}_{3}$
(ii) $\mathrm{Ba}\left(\mathrm{NO}_{3}\right)_{2}$
(iii) $\mathrm{Na}_{2} \mathrm{CO}_{3}$
(iv) $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$
16.124 How many milliliters of $3.0 \mathrm{M} \mathrm{NH}_{4} \mathrm{Cl}$ must be added to 250 mL of $0.20 \mathrm{M} \mathrm{NH}_{3}$ to obtain a buffer solution having $\mathrm{pH}=9.40$ ?
16.125 Consider a buffer solution that contains equal concentrations of $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$and $\mathrm{HPO}_{4}{ }^{2-}$. Will the pH increase, decrease, or remain the same when each of the following substances is added?
(a) $\mathrm{Na}_{2} \mathrm{HPO}_{4}$
(b) HBr
(c) KOH
(d) KI
(e) $\mathrm{H}_{3} \mathrm{PO}_{4}$
(f) $\mathrm{Na}_{3} \mathrm{PO}_{4}$
16.126 A saturated solution of $\mathrm{Mg}(\mathrm{OH})_{2}$ in water has $\mathrm{pH}=10.35$. Calculate $K_{\text {sp }}$ for $\mathrm{Mg}(\mathrm{OH})_{2}$.
16.127 The mercurous ion, $\mathrm{Hg}_{2}{ }^{2+}$, reacts with $\mathrm{Cl}^{-}$to give a white precipitate of $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$. How much $\mathrm{Hg}_{2}{ }^{2+}$ remains in solution after addition of 1 drop (about 0.05 mL ) of 6 M HCl to 1.0 mL of $0.010 \mathrm{M} \mathrm{Hg}_{2}\left(\mathrm{NO}_{3}\right)_{2}$ ? Express your answer in:
(a) $\mathrm{mol} / \mathrm{L}$
(b) $\mathrm{g} / \mathrm{L}$
16.128 Calculate the concentrations of $\mathrm{NH}_{4}{ }^{+}$and $\mathrm{NH}_{3}$ and the pH in a solution prepared by mixing 20.0 g of NaOH and 0.500 L of $1.5 \mathrm{M} \mathrm{NH}_{4} \mathrm{Cl}$. Assume that the volume remains constant.
16.129 In qualitative analysis, $\mathrm{Ag}^{+}, \mathrm{Hg}_{2}{ }^{2+}$, and $\mathrm{Pb}^{2+}$ are separated from other cations by addition of HCl . Calculate the concentration of $\mathrm{Cl}^{-}$required to just begin precipitation of (a) AgCl , (b) $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$, and (c) $\mathrm{PbCl}_{2}$ in a solution having metal-ion concentrations of 0.030 M . What fraction of the $\mathrm{Pb}^{2+}$ remains in solution when the $\mathrm{Ag}^{+}$just begins to precipitate?
16.130 Calculate the molar solubility of MnS in a 0.30 M $\mathrm{NH}_{4} \mathrm{Cl}-0.50 \mathrm{M} \mathrm{NH}_{3}$ buffer solution that is saturated with $\mathrm{H}_{2} \mathrm{~S}\left(\left[\mathrm{H}_{2} \mathrm{~S}\right] \approx 0.10 \mathrm{M}\right)$. What is the solubility of MnS (in $\mathrm{g} / \mathrm{L}$ )? $\mathrm{K}_{\text {spa }}$ for MnS is $3 \times 10^{10}$.
16.131 What is the molar solubility of $\mathrm{Mg}(\mathrm{OH})_{2}$ in a buffer solution that has a pH of 9.00 ?
16.132 What is the pH of a solution prepared by mixing 60.0 mL of $1.00 \mathrm{M} \mathrm{H}_{3} \mathrm{PO}_{4}$ and 1.00 L of 0.100 M LiOH ?
16.133 A student dilutes a solution of 0.100 mol of $\mathrm{H}_{3} \mathrm{PO}_{4}$ and 0.150 mol of NaOH with water to a volume of 1.00 L but then realizes that the "distilled water" used was in fact dilute hydrochloric acid.
(a) If the pH of the final solution is 6.73 , what are the concentrations of $\mathrm{H}_{3} \mathrm{PO}_{4}, \mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$, and $\mathrm{HPO}_{4}{ }^{2-}$.
(b) How many moles of HCl were inadvertently added to the original solution?
16.134 Given a buret filled with 0.10 M acetic acid and a second buret filled with 0.15 M sodium acetate, how many milliliters of each solution should be mixed together to produce 20.0 mL of a solution with a pH of 4.85 ?
16.135 The acidity of lemon juice is derived primarily from citric acid ( $\mathrm{H}_{3} \mathrm{Cit}$ ), a triprotic acid. What are the concentrations of $\mathrm{H}_{3} \mathrm{Cit}, \mathrm{H}_{2} \mathrm{Cit}^{-}, \mathrm{HCit}^{2-}$, and $\mathrm{Cit}^{3-}$ in a sample of lemon juice that has a pH of 2.37 and a total concentration of the four citrate-containing species of 0.350 M ?
16.136 A 100.0 mL sample of a solution that is 0.100 M in HCl and 0.100 M in HCN is titrated with 0.100 M NaOH . Calculate the pH after addition of the following volumes of NaOH :
(a) 0.0 mL
(b) 75.0 mL
(c) 100.0 mL
(d) 125.0 mL
16.137 A 0.0100 mol sample of solid $\mathrm{Cd}(\mathrm{OH})_{2}\left(K_{\text {sp }}=\right.$ $5.3 \times 10^{-15}$ ) in 100.0 mL of water is titrated with $0.100 \mathrm{M} \mathrm{HNO}_{3}$.
(a) What is the molar solubility of $\mathrm{Cd}(\mathrm{OH})_{2}$ in pure water, and what is the pH of the solution before addition of any $\mathrm{HNO}_{3}$ ?
(b) What is the pH of the solution after addition of 90.0 mL of $0.100 \mathrm{M} \mathrm{HNO}_{3}$ ?
(c) How many milliliters of $0.100 \mathrm{M} \mathrm{HNO}_{3}$ must be added to completely neutralize the $\mathrm{Cd}(\mathrm{OH})_{2}$ ?
16.138 Zinc hydroxide, $\mathrm{Zn}(\mathrm{OH})_{2}\left(K_{\text {sp }}=4.1 \times 10^{-17}\right)$, is nearly insoluble in water, but is more soluble in strong base because $\mathrm{Zn}^{2+}$ forms the soluble complex ion $\mathrm{Zn}(\mathrm{OH})_{4}{ }^{2-}\left(K_{\mathrm{f}}=3 \times 10^{15}\right)$.
(a) What is the molar solubility of $\mathrm{Zn}(\mathrm{OH})_{2}$ in pure water? (You may ignore $\mathrm{OH}^{-}$from the selfdissociation of water.)
(b) What is the pH of the solution in part (a)?
(c) What is the molar solubility of $\mathrm{Zn}(\mathrm{OH})_{2}$ in 0.10 M NaOH ?
16.139 Citric acid $\left(\mathrm{H}_{3} \mathrm{Cit}\right)$ can be used as a household cleaning agent to dissolve rust stains. The rust, represented as $\mathrm{Fe}(\mathrm{OH})_{3}$, dissolves because the citrate ion forms a soluble complex with $\mathrm{Fe}^{3+}$ :
$\mathrm{Fe}(\mathrm{OH})_{3}(s)+\mathrm{H}_{3} \mathrm{Cit}(a q) \rightleftharpoons \mathrm{Fe}(\mathrm{Cit})(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)$
(a) Using the equilibrium constants in Appendix C and $K_{f}=6.3 \times 10^{11}$ for $\mathrm{Fe}(\mathrm{Cit})$, calculate the equilibrium constant $K$ for the above reaction.
(b) Calculate the molar solubility of $\mathrm{Fe}(\mathrm{OH})_{3}$ in a 0.500 M solution of $\mathrm{H}_{3} \mathrm{Cit}$.

## Multi-Concept Problems

16.140 When a typical diprotic acid $\mathrm{H}_{2} \mathrm{~A}\left(K_{\mathrm{a} 1}=10^{-4}\right.$; $K_{\mathrm{a} 2}=10^{-10}$ ) is titrated with NaOH , the principal Acontaining species at the first equivalence point is $\mathrm{HA}^{-}$.
(a) By considering all four proton-transfer reactions that can occur in an aqueous solution of $\mathrm{HA}^{-}$, show that the principal reaction is $2 \mathrm{HA}^{-} \rightleftharpoons$ $\mathrm{H}_{2} \mathrm{~A}+\mathrm{A}^{2-}$.
(b) Assuming that this is the principal reaction, show that the pH at the first equivalence point equals the average of $\mathrm{p} K_{\mathrm{a} 1}$ and $\mathrm{p} K_{\mathrm{a} 2}$.
(c) How many $\mathrm{A}^{2-}$ ions are present in 50.0 mL of 1.0 M NaHA ?
16.141 Ethylenediamine $\left(\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}\right.$, abbreviated en) is an organic base that can accept two protons:

$$
\begin{array}{r}
\mathrm{en}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{enH}^{+}(a q)+\mathrm{OH}^{-}(a q) \\
K_{\mathrm{b} 1}=5.2 \times 10^{-4} \\
\mathrm{enH}^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{enH}_{2}^{2+}(a q)+\mathrm{OH}^{-}(a q) \\
K_{\mathrm{b} 2}=3.7 \times 10^{-7}
\end{array}
$$

(a) Consider the titration of 30.0 mL of 0.100 M ethylenediamine with 0.100 M HCl . Calculate the pH after addition of the following volumes of acid, and construct a qualitative plot of pH versus milliliters of HCl added:
(i) 0.0 mL
(ii) 15.0 mL
(iii) 30.0 mL
(iv) 45.0 mL
(v) 60.0 mL
(vi) 75.0 mL
(b) Draw the structure of ethylenediamine, and explain why it can accept two protons.
(c) What hybrid orbitals do the N atoms use for bonding?
16.142 A 40.0 mL sample of a mixture of HCl and $\mathrm{H}_{3} \mathrm{PO}_{4}$ was titrated with 0.100 M NaOH . The first equivalence point was reached after 88.0 mL of base, and the second equivalence point was reached after 126.4 mL of base.
(a) What is the concentration of $\mathrm{H}_{3} \mathrm{O}^{+}$at the first equivalence point?
(b) What are the initial concentrations of HCl and $\mathrm{H}_{3} \mathrm{PO}_{4}$ in the mixture?
(c) What percent of the HCl is neutralized at the first equivalence point?
(d) What is the pH of the mixture before addition of any base?
(e) Sketch the pH titration curve, and label the buffer regions and equivalence points.
(f) What indicators would you select to signal the equivalence points?
16.143 A 1.000 L sample of HCl gas at $25^{\circ} \mathrm{C}$ and 732.0 mm Hg was absorbed completely in an aqueous solution that contained 6.954 g of $\mathrm{Na}_{2} \mathrm{CO}_{3}$ and 250.0 g of water.
(a) What is the pH of the solution?
(b) What is the freezing point of the solution?
(c) What is the vapor pressure of the solution? (The vapor pressure of pure water at $25^{\circ} \mathrm{C}$ is 23.76 mm Hg.)
16.144 A saturated solution of an ionic salt MX exhibits an osmotic pressure of 74.4 mm Hg at $25^{\circ} \mathrm{C}$. Assuming that MX is completely dissociated in solution, what is the value of its $K_{\text {sp }}$ ?
16.145 Consider the reaction that occurs on mixing 50.0 mL of $0.560 \mathrm{M} \mathrm{NaHCO}_{3}$ and 50.0 mL of 0.400 M NaOH at $25^{\circ} \mathrm{C}$.
(a) Write a balanced net ionic equation for the reaction.
(b) What is the pH of the resulting solution?
(c) How much heat (in joules) is liberated by the reaction? (Standard heats of formation are given in Appendix B.)
(d) What is the final temperature of the solution to the nearest $0.1^{\circ} \mathrm{C}$ ? You may assume that all the heat liberated is absorbed by the solution, the mass of the solution is 100.0 g , and its specific heat is $4.18 \mathrm{~J} /\left(\mathrm{g} \cdot{ }^{\circ} \mathrm{C}\right)$.
16.146 In qualitative analysis, $\mathrm{Ca}^{2+}$ and $\mathrm{Ba}^{2+}$ are separated from $\mathrm{Na}^{+}, \mathrm{K}^{+}$, and $\mathrm{Mg}^{2+}$ by adding aqueous $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ to a solution that also contains aqueous $\mathrm{NH}_{3}$ (Figure 16.17). Assume that the concentrations after mixing are $0.080 \mathrm{M}\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ and $0.16 \mathrm{M} \mathrm{NH}_{3}$.
(a) List all the Brønsted-Lowry acids and bases present initially, and identify the principal reaction.
(b) Calculate the pH and the concentrations of all species present in the solution.
(c) In order for the human eye to detect the appearance of a precipitate, a very large number of ions must come together to form solid particles. For this and other reasons, the ion product must often exceed $K_{\text {sp }}$ by a factor of about $10^{3}$ before a precipitate can be detected in a typical qualitative analysis experiment. Taking this fact into account, show quantitatively that the $\mathrm{CO}_{3}{ }^{2-}$ concentration is large enough to give observable precipitation of $\mathrm{CaCO}_{3}$ and $\mathrm{BaCO}_{3}$, but not $\mathrm{MgCO}_{3}$. Assume that the metal-ion concentrations are 0.010 M .
(d) Show quantitatively which of the $\mathrm{Mg}^{2+}, \mathrm{Ca}^{2+}$, and $\mathrm{Ba}^{2+}$ ions, if any, should give an observable precipitate of the metal hydroxide.
(e) Could the separation of $\mathrm{Ca}^{2+}$ and $\mathrm{Ba}^{2+}$ from $\mathrm{Mg}^{2+}$ be accomplished using $0.08 \mathrm{M} \mathrm{Na}_{2} \mathrm{CO}_{3}$ in place of $0.080 \mathrm{M}\left(\mathrm{NH}_{4}\right)_{2} \mathrm{CO}_{3}$ ? Show quantitatively why or why not.
16.147 A railroad tank car derails and spills 36 tons of concentrated sulfuric acid. The acid is 98.0 mass $\% \mathrm{H}_{2} \mathrm{SO}_{4}$ and has a density of $1.836 \mathrm{~g} / \mathrm{mL}$.
(a) What is the molarity of the acid?
(b) How many kilograms of sodium carbonate are needed to completely neutralize the acid?
(c) How many liters of carbon dioxide at $18^{\circ} \mathrm{C}$ and 745 mm Hg are produced as a by-product?
16.148 Some progressive hair dyes marketed to men, such as Grecian Formula 16, contain lead acetate, $\mathrm{Pb}\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)_{2}$. As the dye solution is rubbed on the hair, the $\mathrm{Pb}^{2+}$ ions react with the sulfur atoms in hair proteins to give lead(II) sulfide ( PbS ), which is black. A typical dye solution contains 0.3 mass $\% \mathrm{~Pb}\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)_{2}$, and about 2 mL of dye solution is used per application.
(a) Assuming that $30 \%$ of the $\mathrm{Pb}\left(\mathrm{CH}_{3} \mathrm{CO}_{2}\right)_{2}$ is converted to PbS , how many milligrams of PbS are formed per application of the dye?
(b) Suppose the hair is washed with shampoo and water that has $\mathrm{pH}=5.50$. How many washings would be required to remove $50 \%$ of the black color? Assume that 3 gal of water is used per washing and that the water becomes saturated with PbS .
(c) Does the calculated number of washings look reasonable, given that frequent application of the dye is recommended? What process(es) in addition to dissolution might contribute to the loss of color?

## eMedia Problems

16.149 Look at the Strong Acid-Strong Base Neutralization and Weak Acid-Strong Base Neutralization activities in eChapter 16.1 and answer the following questions:
(a) Why are strong acid molecules represented as $\mathrm{H}^{+}$ but weak acid molecules as HA?
(b) Write the net ionic equation for each reaction.
(c) If the acid in each reaction is HA and the base is MOH , what are the spectator ions in each?
(d) How are the reactions similar? How are they different?
16.150 Use the Buffer Solutions activity (eChapter 16.3) to identify the reaction responsible for maintaining pH upon the addition of a strong base and the addition of a strong acid.
16.151 The Buffer pH activity (eChapter 16.3) allows you determine the pH of a buffer system as the concentrations of an acid and its conjugate base are changed.
(a) Choose a buffer system, and identify the acid and its conjugate base.
(b) What quantity determines the pH of the buffer if the acid and the base have the same concentration?
(c) Which concentration must be increased to raise the pH of the buffer system?
16.152 In the Calculating pH Using the Henderson-Hasselbalch Equation activity (eChapter 16.4), a buffer is prepared by combining an acid (HA) and its sodium salt ( NaA ).
(a) Use the activity to determine the $\mathrm{p} K_{\mathrm{a}}$ and the $K_{\mathrm{a}}$ for formic acid $\mathrm{HCO}_{2} \mathrm{H}$.
(b) Why does changing the volume of water not affect the pH of the solution?
(c) Which acid would be the best choice for buffering a neutral solution? Why?
16.153 The Acid-Base Titration simulation in eChapter 16.6 allows you to simulate titrating unknown acids with various concentrations of NaOH .
(a) Which NaOH concentration would give the most accurate results? Why?
(b) For which acids would you be required to use the 0.40 M NaOH ? Why?
(c) Run the titration for Acid B using only the 1.00 mL button and determine the concentration. Repeat using both the 1.00 mL and 0.10 mL buttons. Repeat using all three buttons. Explain how knowing an approximate concentration for your unknown acid would speed up an actual titration you might perform in the lab.
16.154 The Qualitative Analysis activity in eChapter 16.15 shows the procedure for separating a mixture of metal ions into groups that may be further analyzed to determine the specific ions present.
(a) If a student used this procedure but mistakenly added $\mathrm{H}_{2} \mathrm{~S}$ prior to adding HCl , how might the results be affected?
(b) How does adding $\mathrm{NH}_{3}$ yield possible precipitates even though it does not actually form a salt with the metals?
(c) How might the Group V ions be identified once the analysis is complete?

## Chapter

## Thermodynamics: Entropy, Free Energy, and Equilibrium

## What factors determine the direction and extent of a

 chemical reaction? Some reactions, such as the combustion of hydrocarbon fuels, go almost to completion. Others, such as the combination of gold and oxygen, occur hardly at all. Still others-for example, the industrial synthesis of ammonia from $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ at $400-500^{\circ} \mathrm{C}$ - result in an equilibrium mixture that contains appreciable amounts of both reactants and products.

## CONTENTS

If the second law of thermodynamics states that all spontaneous processes lead to increased disorder, how can living things grow and evolve, creating ever more complex and highly ordered structures? The answer is in this chapter.
17.1 Spontaneous Processes
17.2 Enthalpy, Entropy, and Spontaneous Processes: A Brief Review
17.3 Entropy and Probability
17.4 Entropy and Temperature
17.5 Standard Molar Entropies and Standard Entropies of Reaction
17.6 Entropy and the Second Law of Thermodynamics
17.7 Free Energy

### 17.8 Standard Free-Energy Changes for Reactions

17.9 Standard Free Energies of Formation
17.10 Free-Energy Changes and Composition of the Reaction Mixture
17.11 Free Energy and Chemical Equilibrium

- Interlude-Some Random Thoughts About Entropy


Ruth Ben-Zvi, Judith Silberstein, and Rachel Mamiok, "A Model of Thermal Equilibrium: A Tool for the Introduction of Thermodynamics," J. Chem. Educ., Vol. 70, 1993, 31-34.

As we saw in Section 13.5, the extent of any particular reaction is described by the value of its equilibrium constant $K$ : A value of $K$ much larger than 1 indicates that the reaction goes far toward completion, and a value of $K$ much smaller than 1 means that the reaction does not proceed very far before reaching an equilibrium state. But what determines the value of the equilibrium constant, and can we predict its value without measuring it? Put another way, what fundamental properties of nature determine the direction and extent of a particular chemical reaction? For answers to these questions, we turn to thermodynamics, the area of science that deals with the interconversion of heat and other forms of energy.

## 17.1 | Spontaneous Processes

We have defined a spontaneous process as one that proceeds on its own without any external influence (Section 8.13). The reverse of a spontaneous process is always nonspontaneous and takes place only in the presence of some continuous external influence. Consider, for example, the expansion of a gas into a vacuum. When the stopcock in the apparatus shown in Figure 17.1 is opened, the gas in bulb A expands spontaneously into the evacuated bulb B until the gas pressure in the two bulbs is the same. The reverse process, migration of all the gas molecules into one bulb, does not occur spontaneously. To compress a gas from a larger to a smaller volume, we would have to push on the gas with a piston.


A FIGURE 17.1 When the stopcock is opened, the gas in bulb A expands spontaneously into evacuated bulb B to fill all the available volume. The reverse process, compression of the gas, is nonspontaneous.

James N. Spencer, Richard S. Moog, and Ronald J. Gillespie, "Demystifying Introductory Chemistry. Part 4: An Approach to Reaction Thermodynamics Through Enthalpies, Entropies, and Free Energies of Atomization," J. Chem. Educ., Vol. 73, 1996, 631-636.

[].]Raymond S. Ochs, "Thermodynamics and Spontaneity," J. Chem. Educ., Vol. 73, 1996, 952-954.


As a second example, consider the combination of hydrogen and oxygen in the presence of a platinum catalyst:

$$
2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \xrightarrow{\text { Catalyst }} 2 \mathrm{H}_{2} \mathrm{O}(l)
$$

The forward reaction occurs spontaneously, but the reverse reaction, decomposition of water into its elements, does not occur no matter how long we wait. We'll see in Chapter 18 that we can force the reverse reaction to occur by electrolysis, but that reverse process is nonspontaneous and requires a continuous input of electrical energy.

In general, whether the forward or reverse reaction is spontaneous depends on the temperature, pressure, and composition of the reaction mixture. Consider the Haber synthesis of ammonia:

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \xrightarrow{\text { Catalyst }} 2 \mathrm{NH}_{3}(g)
$$

A mixture of gaseous $\mathrm{N}_{2}, \mathrm{H}_{2}$, and $\mathrm{NH}_{3}$, each at a partial pressure of 1 atm , reacts spontaneously at 300 K to convert some of the $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ to $\mathrm{NH}_{3}$. We can predict the direction of spontaneous reaction from the relative values of the equilibrium constant $K$ and the reaction quotient $Q$ (Section 13.5). Since $K_{p}=4.4 \times 10^{5}$ at 300 K and $Q_{p}=1$ for partial pressures of 1 atm , the reaction will proceed in the forward direction because $Q_{p}$ is less than $K_{p}$. Under these conditions, the reverse reaction is nonspontaneous. At 700 K , however, $K_{\mathrm{p}}=8.8 \times 10^{-5}$, and the reverse reaction is spontaneous because $Q_{p}$ is greater than $K_{p}$.

A spontaneous reaction always moves a reaction mixture toward equilibrium. By contrast, a nonspontaneous reaction moves the composition of a mixture away
from the equilibrium composition. Remember, though, that the word "spontaneous" doesn't mean the same thing as "fast." A spontaneous reaction can be either fast or slow-for example, the gradual rusting of iron metal is a slow spontaneous reaction. Thermodynamics tells us where a reaction is headed, but it says nothing about how long it takes to get there. As discussed in Section 12.10, the rate at which equilibrium is achieved depends on kinetics, especially on the height of the activation energy barrier between the reactants and products (Figure 17.2).

V FIGURE 17.2 (a) The rusting of this car is a spontaneous reaction, but it occurs slowly. (b) A spontaneous reaction occurs slowly if it has a high activation energy $E_{a}$.

(a)

(b)

- PROBLEM 17.1 Which of the following processes are spontaneous, and which are nonspontaneous?
(a) Diffusion of perfume molecules from one side of a room to the other
(b) Heat flow from a cold object to a hot object
(c) Decomposition of rust $\left(\mathrm{Fe}_{2} \mathrm{O}_{3} \cdot \mathrm{H}_{2} \mathrm{O}\right)$ to iron metal, oxygen, and water
(d) Decomposition of solid $\mathrm{CaCO}_{3}$ to solid CaO and gaseous $\mathrm{CO}_{2}$ at $25^{\circ} \mathrm{C}$ and 1 atm pressure ( $K_{\mathrm{p}}=1.4 \times 10^{-23}$ )


### 17.2 Enthalpy, Entropy, and Spontaneous Processes: A Brief Review

Let's look more closely at spontaneous processes and at the thermodynamic driving forces that cause them to occur. We saw in Chapter 8 that most spontaneous chemical reactions are accompanied by the conversion of potential energy to heat. For example, when methane burns in air, the potential energy stored in the chemical bonds of $\mathrm{CH}_{4}$ and $\mathrm{O}_{2}$ is partly converted to heat, which flows from the system (reactants plus products) to the surroundings:

$$
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H^{\circ}=-890.3 \mathrm{~kJ}
$$

Because heat is lost by the system, the reaction is exothermic and the standard enthalpy of reaction is negative ( $\Delta H^{\circ}=-890.3 \mathrm{~kJ}$ ). The total energy is conserved, so all the energy lost by the system shows up as heat gained by the surroundings.

Because spontaneous reactions so often give off heat, the nineteenth-century French scientist Marcellin Berthelot proposed that spontaneous chemical or physical changes are always exothermic. But Berthelot's proposal can't be correct. Ice, for example, spontaneously absorbs heat and melts at temperatures above $0^{\circ} \mathrm{C}$. Similarly, liquid water absorbs heat and spontaneously boils at temperatures above $100^{\circ} \mathrm{C}$. As further examples, gaseous $\mathrm{N}_{2} \mathrm{O}_{4}$ absorbs heat when it


A The combustion of natural gas (mainly $\mathrm{CH}_{4}$ ) in air is a spontaneous, exothermic reaction.


A Why aren't these leaves ever blown into a neat pile?

John J. Fortman, "Pictorial Analogies of Heat Flow, Thermodynamics, and Entropy," J. Chem. Educ., Vol. 70, 1993, 102-103.


FIGURE 17.3 Molecular randomness-and thus entropy-increases when a solid melts and when a liquid vaporizes. Conversely, randomness and entropy decrease when a vapor condenses and when a liquid freezes. Note the sign of $\Delta S$ for each process.

[D]Joseph H. Lechner, "Visualizing Entropy," J. Chem. Educ., Vol. 76, 1999, 1382-1387.
decomposes to $\mathrm{NO}_{2}$ at 400 K , and table salt absorbs heat when it dissolves in water at room temperature:

$$
\begin{array}{ll}
\mathrm{H}_{2} \mathrm{O}(s) \longrightarrow \mathrm{H}_{2} \mathrm{O}(l) & \Delta H_{\text {fusion }}=+6.01 \mathrm{~kJ} \\
\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{H}_{2} \mathrm{O}(g) & \Delta H_{\text {vap }}=+40.7 \mathrm{~kJ} \\
\mathrm{~N}_{2} \mathrm{O}_{4}(g) \longrightarrow 2 \mathrm{NO}_{2}(g) & \Delta H^{\circ}=+57.1 \mathrm{~kJ} \\
\mathrm{NaCl}(s) \longrightarrow \mathrm{Na}^{+}(a q)+\mathrm{Cl}^{-}(a q) & \Delta H^{\circ}=+3.88 \mathrm{~kJ}
\end{array}
$$

All these processes are endothermic, yet all are spontaneous. In all cases, the system moves spontaneously to a state of higher potential energy by absorbing heat from the surroundings.

Since some spontaneous reactions are exothermic and others are endothermic, enthalpy alone can't account for the direction of spontaneous change; a second factor must be involved. This second thermodynamic driving force is nature's tendency to move to a condition of maximum randomness or disorder (Section 8.13).

The tendency of things to get "messed up" is common in everyday life. You may rake the leaves on your lawn into an orderly pile, but after a few windy days the leaves are again scattered randomly. The reverse process is nonspontaneous; the wind never blows the randomly disordered leaves into a neatly arranged pile. Molecular systems behave similarly: Molecular systems tend to move spontaneously to a state of maximum randomness or disorder.

Molecular randomness, or disorder, is called entropy and is denoted by the symbol $S$. Entropy is a state function (Section 8.3), and the entropy change $\Delta S$ for a process thus depends only on the initial and final states of the system:

$$
\Delta S=S_{\text {final }}-S_{\text {initial }}
$$

When the randomness or disorder of a system increases, $\Delta S$ has a positive value; when randomness decreases, $\Delta S$ is negative.

If you analyze the four spontaneous endothermic processes mentioned previously, you'll see that each involves an increase in the randomness of the system. When ice melts, for example, randomness increases because the highly ordered crystalline arrangement of tightly held water molecules collapses and the molecules become free to move about in the liquid. When liquid water vaporizes, randomness further increase because the molecules can now move independently in the much larger volume of the gas. In general, processes that convert a solid to a liquid or a liquid to a gas involve an increase in randomness and thus an increase in entropy (Figure 17.3).


The decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}\left(\mathrm{O}_{2} \mathrm{~N}-\mathrm{NO}_{2}\right)$ is accompanied by an increase in randomness because breaking the $\mathrm{N}-\mathrm{N}$ bond allows the two gaseous $\mathrm{NO}_{2}$ fragments
to move independently. Whenever a molecule breaks into two or more pieces, the amount of molecular randomness increases. More specifically, randomness-and thus entropy-increases whenever a reaction results in an increase in the number of gaseous molecules (Figure 17.4).

Less randomness
(less entropy)


More randomness
(more entropy)


The entropy change on dissolving sodium chloride in water occurs because the crystal structure of solid NaCl is disrupted and the $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions are hydrated (Section 11.2). Disruption of the crystal increases randomness because the $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions are tightly held in the solid but are free to move about in the liquid. The hydration process, however, decreases randomness because it puts the polar, hydrating water molecules into an orderly arrangement about the $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions. It turns out that the overall dissolution process results in a net increase in randomness, and $\Delta S$ is thus positive (Figure 17.5). This is usually the case for the dissolution of molecular solids, such as $\mathrm{HgCl}_{2}$, and salts that contain +1 cations and -1 anions. For salts such as $\mathrm{CaSO}_{4}$, which contain more highly charged ions, the hydrating water molecules are more strongly ordered about the ions, and the dissolution process often results in a net decrease in entropy. The following dissolution reactions illustrate the point:

$$
\begin{array}{ll}
\mathrm{HgCl}_{2}(s) \longrightarrow \mathrm{HgCl}_{2}(a q) & \Delta S=+9 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol}) \\
\mathrm{NaCl}(s) \longrightarrow \mathrm{Na}^{+}(a q)+\mathrm{Cl}^{-}(a q) & \Delta S=+43 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol}) \\
\mathrm{CaSO}_{4}(s) \longrightarrow \mathrm{Ca}^{2+}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q) & \Delta S=-140 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})
\end{array}
$$

< FIGURE 17.4 Molecular randomness-and thus entropy-increases when a reaction results in an increase in the number of gaseous particles. For example, $\Delta S$ is positive for the decomposition of $\mathrm{N}_{2} \mathrm{O}_{4}$ to $\mathrm{NO}_{2}$ and is negative for the formation of $\mathrm{N}_{2} \mathrm{O}_{4}$ from $\mathrm{NO}_{2}$.


Peter Weiss, "Another Face of Entropy," Science News, Vol. 154, 1998, 108-109.


4 FIGURE 17.5 When NaCl dissolves in water, the crystal breaks up, and the $\mathrm{Na}^{+}$and $\mathrm{Cl}^{-}$ions are surrounded by hydrating water molecules. The polar $\mathrm{H}_{2} \mathrm{O}$ molecules are oriented such that the partially negative O atoms are near the cations and the partially positive H atoms are near the anions. Disruption of the crystal increases the entropy, but the hydration process decreases the entropy. For dissolution of NaCl , the net effect is an entropy increase.
L. Glasser, "Order, Chaos, and All That!" J. Chem. Educ., Vol. 66, 1989, 997-1001.

John P. Lowe, "Entropy: Conceptual Disorder," J. Chem. Educ., Vol. 65, 1988, 403-406.

## Worked Example 17.1

Predict the sign of $\Delta S$ in the system for each of the following processes:
(a) $\mathrm{CO}_{2}(s) \rightarrow \mathrm{CO}_{2}(g)$ (sublimation of dry ice)
(b) $\mathrm{CaSO}_{4}(s) \rightarrow \mathrm{CaO}(s)+\mathrm{SO}_{3}(g)$
(c) $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightarrow 2 \mathrm{NH}_{3}(g)$
(d) $\mathrm{I}_{2}(s) \rightarrow \mathrm{I}_{2}(a q)$ (dissolution of iodine in water)

## Strategy

To predict the sign of $\Delta S$, look to see if the process involves a phase change, a change in the number of gaseous molecules, or the dissolution (or precipitation) of a solid. Entropy generally increases for phase transitions that convert a solid to a liquid or a liquid to a gas, reactions that increase the number of gaseous molecules, and dissolution of molecular solids or salts with +1 cations and -1 anions.

## SOlUTION

(a) A gas is much more disordered than a solid. Therefore, $\Delta S$ is positive.
(b) One mole of gaseous molecules appears on the product side of the equation and none on the reactant side. Since the reaction increases the number of gaseous molecules, the entropy change is positive.
(c) The entropy change is negative because the reaction decreases the number of gaseous molecules from four moles to two moles. Fewer particles can move independently after reaction than before.
(d) Iodine molecules are electrically neutral and form a molecular solid. The dissolution process destroys the order of the crystal and enables the iodine molecules to move about randomly in the liquid. Therefore, $\Delta S$ is positive.

- PROBLEM 17.2 Predict the sign of $\Delta S$ in the system for each of the following processes:
(a) $\mathrm{H}_{2} \mathrm{O}(g) \rightarrow \mathrm{H}_{2} \mathrm{O}(l)$ (formation of rain droplets)
(b) $\mathrm{I}_{2}(g) \rightarrow 2 \mathrm{I}(g)$
(c) $\mathrm{CaCO}_{3}(s) \rightarrow \mathrm{CaO}(s)+\mathrm{CO}_{2}(g)$
(d) $\mathrm{Ag}^{+}(a q)+\mathrm{Br}^{-}(a q) \rightarrow \mathrm{AgBr}(s)$


## Worked Key Concept Example 17.2

Consider the gas-phase reaction of $\mathrm{A}_{2}$ molecules (red) with B atoms (blue):

(a) Write a balanced equation for the reaction.
(b) Predict the sign of $\Delta S$ for the reaction.

## Strategy

To determine the stoichiometry of the reaction, count the number of reactant $\mathrm{A}_{2}$ molecules and $B$ atoms and the number of product $A B$ molecules. To predict the sign of the entropy change, see if the reaction increases or decreases the number of gaseous particles.

## Solution

In this reaction, $3 \mathrm{~A}_{2}$ molecules and 6 B atoms are consumed and 6 AB molecules are formed ( $3 \mathrm{~A}_{2}+6 \mathrm{~B} \rightarrow 6 \mathrm{AB}$ ). Dividing by 3 to reduce the coefficients to their smallest whole number values gives the balanced equation $\mathrm{A}_{2}(g)+2 \mathrm{~B}(g) \rightarrow 2 \mathrm{AB}(g)$. Because the reaction decreases the number of gaseous particles from 3 mol to 2 mol , the entropy change is negative.
$\mapsto$ KEY CONCEPT PROBLEM 17.3 Consider the gas-phase reaction of $\mathrm{AB}_{3}$ and $\mathrm{A}_{2}$ molecules:

(a) Write a balanced equation for the reaction.
(b) What is the sign of the entropy change for the reaction?

## 17.3 | Entropy and Probability

Why do systems tend to move spontaneously to a state of maximum randomness or disorder? The answer is that a disordered state is more probable than an ordered state because the disordered state can be achieved in more ways. Suppose, for example, that you shake a box containing 20 identical coins and then count the number of heads $(\mathrm{H})$ and tails (T). It's very unlikely that all 20 coins will come up heads; that is, a perfectly ordered arrangement is much less probable than the totally disordered state in which heads and tails come up randomly.

The probabilities of the ordered and disordered states are proportional to the number of ways that the states can be achieved. The perfectly ordered state ( 20 H ) can be achieved in only one way because it consists of a single configuration. In how many ways, though, can the totally disordered state be achieved? The totally disordered state of a collection of coins includes all possible configurations in which heads and tails are arranged at random. Thus, if there were just two coins in the box, each of them could come up in two ways ( H or T ), and the two together could come up in $2 \times 2=2^{2}=4$ ways (HH, HT, TH, or TT). Three coins could come up in $2 \times 2 \times 2=2^{3}=8$ ways (HHH, HTH, THH, TTH, HHT, HTT, THT, or TTT), and so on. For the case of 20 coins, the number of possible arrangements is $2^{20}=1,048,576$.

Because the perfectly ordered state of 20 heads can be achieved in only one way and the totally disordered state can be achieved in $2^{20}$ ways, the totally disordered state is $2^{20}$ times more probable than the perfectly ordered state. If you begin with the ordered state of 20 heads and shake the box, the system will almost always move to the disordered state of higher probability.

An analogous chemical example is a crystal containing diatomic molecules such as carbon monoxide in which the two distinct ends of the CO molecule correspond to the heads and tails of a coin. Let's suppose that the long dimensions of the molecules are oriented vertically (Figure 17.6) and that the temperature is 0 K , so that the molecules are locked into a fixed arrangement. The state in which the molecules pack together in a perfectly ordered "heads-up" arrangement (Figure 17.6a) can be achieved in only one way, whereas the state in which the molecules are arranged randomly with respect to the vertical direction can be achieved in
-


A Shaking a box that contains 20 quarters gives a random arrangement of heads and tails.


A FIGURE 17.6 A hypothetical crystal containing 20 CO molecules. In (a), the molecules are arranged in a perfectly ordered "heads-up" structure. In (b), the molecules are arranged randomly in one of the $2^{20}$ ways in which the disordered structure can be obtained.

Douglas K. Russell, "The Boltzmann Distribution," J. Chem. Educ., Vol. 73, 1996, 299-300.
P. G. Nelson, "Derivation of the Second Law of Thermodynamics from Boltzmann's Distribution Law," J. Chem. Educ., Vol. 65, 1989, 390-393.

Entropy and Probability activity

The value of $R$ used in energy-related calculations is $8.314 \mathrm{~J} / \mathrm{K}$, not
$0.08206(\mathrm{~L} \cdot \mathrm{~atm}) /(\mathrm{mol} \cdot \mathrm{K})$.
many ways- $2^{20}$ ways for a hypothetical crystal containing 20 CO molecules (Figure 17.6b). Therefore, the disordered state of the crystal is $2^{20}$ times more probable than the perfectly ordered "heads-up" structure.

The Austrian physicist Ludwig Boltzmann proposed in 1896 that the entropy of a particular state is related to the number of ways that the state can be achieved, according to the formula

$$
S=k \ln W
$$

where $S$ is the entropy of the state, $\ln W$ is the natural logarithm of the number of ways that the state can be achieved, and $k$, now known as Boltzmann's constant, is a universal constant equal to the gas constant $R$ divided by Avogadro's number $\left(k=R / N_{\mathrm{A}}=1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}\right)$. Because a logarithm is dimensionless, you can see from the Boltzmann equation that entropy has the same units as the constant $k$, namely, joules per kelvin.

Now let's apply Boltzmann's formula to our hypothetical crystal containing 20 CO molecules. Because the perfectly ordered state can be achieved in only one way ( $W=1$ in the Boltzmann equation) and because $\ln 1=0$, the entropy of the perfectly ordered state is zero:

$$
\begin{aligned}
S & =k \ln W=k \ln 1 \\
& =0
\end{aligned}
$$

The more probable totally disordered state, however, can be achieved in $2^{20}$ ways and thus has a higher entropy:

$$
\begin{aligned}
S & =k \ln W=k \ln 2^{20} \\
& =\left(1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}\right)(20)(\ln 2) \\
& =1.91 \times 10^{-22} \mathrm{~J} / \mathrm{K}
\end{aligned}
$$

where we have made use of the relation $\ln x^{a}=a \ln x$ (Appendix A.2).
If our crystal contained 1 mol of CO molecules, the entropy of the perfectly ordered state ( $6.02 \times 10^{23} \mathrm{C}$ atoms up) would still be zero, but the entropy of the totally disordered state would be much higher because Avogadro's number of molecules can be arranged randomly in a huge number of ways ( $W=$ $2^{N_{\mathrm{A}}}=2^{6.02 \times 10^{23}}$ ). According to Boltzmann's formula, the entropy of the disordered state is

$$
S=k \ln W=k \ln 2^{N_{\mathrm{A}}}=k N_{\mathrm{A}} \ln 2
$$

Because $k=R / N_{\mathrm{A}}$,

$$
\begin{aligned}
S & =R \ln 2=(8.314 \mathrm{~J} / \mathrm{K})(0.693) \\
& =5.76 \mathrm{~J} / \mathrm{K}
\end{aligned}
$$

Based on experimental measurements, the entropy of 1 mol of solid carbon monoxide near 0 K is about $5 \mathrm{~J} / \mathrm{K}$, indicating that the CO molecules adopt a nearly random arrangement.

The nearly random arrangement of CO molecules in crystalline carbon monoxide is unusual but can be understood in terms of molecular structure. Because CO molecules have a dipole moment of only 0.11 D, intermolecular dipole-dipole forces are unusually weak (Sections 10.1 and 10.2), and the molecules therefore have little preference for the slightly lower energy, completely ordered arrangement. By contrast, HCl , with a dipole moment of 1.03 D , forms an ordered crystalline solid, and so the entropy of 1 mol of solid HCl at 0 K is $0 \mathrm{~J} / \mathrm{K}$.

Boltzmann's formula also explains why a gas expands into a vacuum. If the two bulbs in Figure 17.1 have equal volumes, each molecule has one chance in two of being in bulb $A$ (heads, in our coin example) and one chance in two of being in bulb B (tails) when the stopcock is opened. It's exceedingly unlikely that all the
molecules in one mole of gas will be in bulb A, since that state can be achieved in only one way. The state in which Avogadro's number of molecules are randomly distributed between bulbs A and B can be achieved in $2^{6.02 \times 10^{23}}$ ways, and the entropy of the disordered state is therefore higher than the entropy of the ordered state by the now familiar amount, $R \ln 2=5.76 \mathrm{~J} / \mathrm{K}$. Thus, a gas expands spontaneously because the state of greater volume is more probable.

In general, when the volume of one mole of an ideal gas changes from $V_{\text {initial }}$ to $V_{\text {final }}$ at constant temperature, the entropy of the gas changes by an amount

$$
\Delta S=R \ln \frac{V_{\text {final }}}{V_{\text {initial }}}
$$

Because the pressure and volume of an ideal gas are related inversely $(P=$ $n R T / V)$, we can also write

$$
\Delta S=R \ln \frac{P_{\text {initial }}}{P_{\text {final }}}
$$

Thus, the entropy of a gas increases when its pressure decreases at constant temperature, and the entropy decreases when pressure increases. Common sense tells us that the more we squeeze the gas, the less space the gas molecules have and so the more ordered they will be.

- PROBLEM 17.4 Which state has the higher entropy? Explain in terms of probability.
(a) A perfectly ordered crystal of solid nitrous oxide $(\mathrm{N} \equiv \mathrm{N}-\mathrm{O})$ or a disordered crystal in which the molecules are oriented randomly
(b) Silica glass or a quartz crystal
(c) 1 mol of $\mathrm{N}_{2}$ gas at STP or 1 mol of $\mathrm{N}_{2}$ gas at 273 K in a volume of 11.2 L
(d) 1 mol of $\mathrm{N}_{2}$ gas at STP or 1 mol of $\mathrm{N}_{2}$ gas at 273 K and 0.25 atm


## 17.4 | Entropy and Temperature

Thus far we've seen that entropy is associated with the orientation and distribution of molecules in space. Disordered crystals have higher entropy than ordered crystals, and diffuse gases have higher entropy than compressed gases.

Entropy is also associated with molecular motion. As the temperature of a substance increases, random molecular motion increases and there is a corresponding increase in the average kinetic energy of the molecules. But not all the molecules have the same energy. As we saw in Section 9.6, there is a distribution of molecular speeds in a gas, a distribution that broadens and shifts to higher speeds with increasing temperature (Figure 9.12, page 360). In solids, liquids, and gases, the total energy of a substance can be distributed among the individual molecules in a number of ways that increases as the total energy increases. According to Boltzmann's formula, the more ways that the energy can be distributed, the greater the randomness of the state and the higher its entropy. Therefore, the entropy of a substance increases with increasing temperature (Figure 17.7).

A typical plot of entropy versus temperature is shown in Figure 17.8. At absolute zero, every substance is a solid whose particles are tightly held in a crystalline structure. If there is no residual orientational disorder, like that in carbon monoxide (Figure 17.6b), the entropy of the substance at 0 K will be zero, a general result summarized in the third law of thermodynamics:
third law of thermodynamics The entropy of a perfectly ordered crystalline substance at 0 K is zero.
(The first law of thermodynamics was discussed in Section 8.3. We'll review the first law and discuss the second law in Section 17.6.)

The greater the volume (and the lower the pressure) of a gas, the greater the entropy.

V
Entropy increases with an increase in the motion of atoms, ions, and molecules. The higher the temperature, the more rapid the motion and the greater the entropy.

FIGURE 17.7 (a) A substance at a higher temperature has greater molecular motion, more disorder, and greater entropy than (b) the same substance at a lower temperature.

FIGURE 17.8 The entropy of a pure substance, equal to zero at 0 K , shows a steady increase with rising temperature, punctuated by discontinuous jumps in entropy at the temperatures of the phase transitions.
s


Elic., Vol. 76, 199, 1388-1390.


As the temperature of a solid is raised, the added energy increases the vibrational motion of the molecules. The number of ways in which the vibrational energy can be distributed increases with rising temperature, and the entropy of the solid thus increases steadily as the temperature increases.

At the melting point, there is a discontinuous jump in entropy because there are many more ways of arranging the molecules in the liquid than in the solid. Furthermore, the molecules in the liquid can undergo translational and rotational as well as vibrational motion, and so there are many more ways of distributing the total energy in the liquid. An even greater jump in entropy is observed at the boiling point because molecules in the gas are free to occupy a much larger volume. Between the melting point and the boiling point, the entropy of a liquid increases steadily as molecular motion increases and the number of ways of distributing the total energy among the individual molecules increases. For the same reason, the entropy of a gas rises steadily as its temperature increases.

### 17.5 Standard Molar Entropies and Standard Entropies of Reaction

We won't describe how the entropy of a substance is determined, except to note that two approaches are available: (1) calculations based on Boltzmann's formula and (2) experimental measurements of heat capacities (Section 8.8) down to very low temperatures. Suffice it to say that standard molar entropies, denoted by $S^{\circ}$, are known for many substances.
standard molar entropy, $S^{\circ}$ The entropy of one mole of the pure substance at 1 atm pressure and a specified temperature, usually $25^{\circ} \mathrm{C}$.
Values of $S^{\circ}$ for some common substances at $25^{\circ} \mathrm{C}$ are listed in Table 17.1, and additional values are given in Appendix B. Note that the units of $S^{\circ}$ are joules (not kilojoules) per kelvin mole [J/ $(\mathrm{K} \cdot \mathrm{mol})]$ Standard molar entropies are often called absolute entropies because they are measured with respect to an absolute reference point-the entropy of the perfectly ordered crystalline substance at $0 \mathrm{~K}\left[S^{\circ}=\right.$ $0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ at $T=0 \mathrm{~K}$.

TABLE 17.1 Standard Molar Entropies for Some Common Substances at $25^{\circ} \mathrm{C}$

| Substance | Formula | $S^{\circ}[\mathbf{J} /(\mathbf{K} \cdot \mathrm{mol})]$ | Substance | Formula | $S^{\circ}[\mathbf{J} /(\mathrm{K} \cdot \mathrm{mol})]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Gases |  |  | Liquids |  |  |
| Acetylene | $\mathrm{C}_{2} \mathrm{H}_{2}$ | 200.8 | Acetic acid | $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ | 160 |
| Ammonia | $\mathrm{NH}_{3}$ | 192.3 | Ethanol | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}$ | 161 |
| Carbon dioxide | $\mathrm{CO}_{2}$ | 213.6 | Methanol | $\mathrm{CH}_{3} \mathrm{OH}$ | 127 |
| Carbon monoxide | CO | 197.6 | Water | $\mathrm{H}_{2} \mathrm{O}$ | 69.9 |
| Ethylene | $\mathrm{C}_{2} \mathrm{H}_{4}$ | 219.5 | Solids |  |  |
| Hydrogen | $\mathrm{H}_{2}$ | 130.6 | Calcium carbonate | $\mathrm{CaCO}_{3}$ | 92.9 |
| Methane | $\mathrm{CH}_{4}$ | 186.2 | Calcium oxide | CaO | 39.7 |
| Nitrogen | $\mathrm{N}_{2}$ | 191.5 | Diamond | C | 2.4 |
| Nitrogen dioxide | $\mathrm{NO}_{2}$ | 240.0 | Graphite | C | 5.7 |
| Dinitrogen tetroxide | $\mathrm{N}_{2} \mathrm{O}_{4}$ | 304.2 | Iron | Fe | 27.3 |
| Oxygen | $\mathrm{O}_{2}$ | 205.0 | Iron(III) oxide | $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | 87.4 |

Standard molar entropies make it possible to compare the entropies of different substances under the same conditions of temperature and pressure. It's apparent from Table 17.1, for example, that the entropies of gaseous substances tend to be larger than those of liquids, which, in turn, tend to be larger than those of solids. Table 17.1 also shows that $S^{\circ}$ values increase with increasing molecular complexity. Compare, for example, $\mathrm{CH}_{3} \mathrm{OH}$, which has $S^{\circ}=127 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$, to $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}$, which has $S^{\circ}=161 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$.

Once we have values for standard molar entropies, it's easy to calculate the entropy change for a chemical reaction. The standard entropy of reaction, $\Delta S^{\circ}$, can be obtained simply by subtracting the standard molar entropies of all the reactants from the standard molar entropies of all the products:

$$
\Delta S^{\circ}=S^{\circ}(\text { products })-S^{\circ}(\text { reactants })
$$

Because $S^{\circ}$ values are quoted on a per-mole basis, the $S^{\circ}$ value for each substance must be multiplied by the stoichiometric coefficient of that substance in the balanced chemical equation. Thus, for the general reaction

$$
a \mathrm{~A}+b \mathrm{~B} \longrightarrow c \mathrm{C}+d \mathrm{D}
$$

manmp In general, $S^{\circ}$ (gas) >
$\checkmark \mathrm{S}^{\circ}$ (liquid) $>\mathrm{S}^{\circ}$ (solid), and $S^{\circ}$ (large molecule) $>$ $S^{\circ}$ (small molecule).

$\square$Travis Thoms, "Periodic Trends for the Entropy of Elements," J. Chem. Educ., Vol. 72, 1995, 16.

0Remind students to multiply the standard molar entropy of each reactant and product by the appropriate coefficient from the balanced chemical equation when calculating the standard entropy of a reaction.
the standard entropy of reaction is

$$
\Delta S^{\circ}=\left[c S^{\circ}(\mathrm{C})+d S^{\circ}(\mathrm{D})\right]-\left[a S^{\circ}(\mathrm{A})+b S^{\circ}(\mathrm{B})\right]
$$

where the units of the coefficients are moles, the units of $S^{\circ}$ are $\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})$, and the units of $\Delta S^{\circ}$ are $\mathrm{J} / \mathrm{K}$.

As an example, let's calculate the standard entropy change for the reaction

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \longrightarrow 2 \mathrm{NO}_{2}(g)
$$

Using the appropriate $S^{\circ}$ values obtained from Table 17.1, we find that $\Delta S^{\circ}=$ 175.8 J/K:

$$
\begin{aligned}
\Delta S^{\circ} & =2 S^{\circ}\left(\mathrm{NO}_{2}\right)-S^{\circ}\left(\mathrm{N}_{2} \mathrm{O}_{4}\right) \\
& =(2 \mathrm{~mol})\left(240.0 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)-(1 \mathrm{~mol})\left(304.2 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right) \\
& =175.8 \mathrm{~J} / \mathrm{K}
\end{aligned}
$$

Although the standard molar entropy of $\mathrm{N}_{2} \mathrm{O}_{4}$ is larger than that of $\mathrm{NO}_{2}$, as expected for a more complex molecule, $\Delta S^{\circ}$ for the reaction is positive because 1 mol of $\mathrm{N}_{2} \mathrm{O}_{4}$ is converted to 2 mol of $\mathrm{NO}_{2}$. As noted earlier, we expect an increase in entropy whenever a molecule breaks into two or more pieces.

## Worked Example 17.3

Calculate the standard entropy of reaction at $25^{\circ} \mathrm{C}$ for the synthesis of ammonia:

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g)
$$

## Strategy

To calculate $\Delta S^{\circ}$ for the reaction, subtract the standard molar entropies of all the reactants from the standard molar entropies of all the products. Look up the $S^{\circ}$ values in Table 17.1 or Appendix B and remember to multiply the $S^{\circ}$ value for each substance by its coefficient in the balanced chemical equation.

## Solution

$$
\begin{aligned}
\Delta S^{\circ} & =2 S^{\circ}\left(\mathrm{NH}_{3}\right)-\left[S^{\circ}\left(\mathrm{N}_{2}\right)+3 S^{\circ}\left(\mathrm{H}_{2}\right)\right] \\
& =(2 \mathrm{~mol})\left(192.3 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)-\left[(1 \mathrm{~mol})\left(191.5 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)+(3 \mathrm{~mol})\left(130.6 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)\right] \\
& =-198.7 \mathrm{~J} / \mathrm{K}
\end{aligned}
$$

$\checkmark$ Ballpark Check As predicted in Worked Example 17.1c, $\Delta S^{\circ}$ should be negative because the reaction decrease the number of gaseous molecules from four moles to two moles.

- PROBLEM 17.5 Calculate the standard entropy of reaction at $25^{\circ} \mathrm{C}$ for the decomposition of calcium carbonate:

$$
\mathrm{CaCO}_{3}(s) \longrightarrow \mathrm{CaO}(s)+\mathrm{CO}_{2}(g)
$$

### 17.6 Entropy and the Second Law of Thermodynamics

We've seen thus far that molecular systems tend to move spontaneously toward a state of minimum enthalpy and maximum entropy. In any particular reaction, however, the enthalpy of the system can either increase or decrease. Similarly, the entropy of the system can either increase or decrease. How, then, can we decide
whether a reaction will occur spontaneously? In Section 8.14, we said that it is the value of the free-energy change, $\Delta G$, that is the criterion for spontaneity, where $\Delta G=\Delta H-T \Delta S$. If $\Delta G<0$, the reaction is spontaneous; if $\Delta G>0$, the reaction is nonspontaneous; and if $\Delta G=0$, the reaction is at equilibrium. In this section and the next, we'll see how that conclusion was reached. Let's begin by looking at the first and second laws of thermodynamics:
FIRST LAW OF
THERMODYNAMICS
SECOND LAW OF
THERMODYNAMICS

In any process, spontaneous or nonspontaneous, the total energy of a system and its surroundings is constant.
In any spontaneous process, the total entropy of a system and its surroundings always increases.

The first law (Section 8.3) is simply a statement of the conservation of energy. It says that energy (or enthalpy) can flow between a system and its surroundings but the total energy of the system plus the surroundings always remains constant. In an exothermic reaction, the system loses enthalpy to the surroundings; in an endothermic reaction, the system gains enthalpy from the surroundings. Since energy is conserved in all chemical processes, spontaneous and nonspontaneous, the first law helps us keep track of energy flow between the system and the surroundings, but it doesn't tell us whether a particular reaction will be spontaneous or nonspontaneous.

The second law, however, provides a clear-cut criterion of spontaneity. It says that the direction of spontaneous change is always determined by the sign of the total entropy change:

$$
\Delta S_{\text {total }}=\Delta S_{\text {system }}+\Delta S_{\text {surroundings }}
$$

Specifically,
If $\Delta S_{\text {total }}>0$, the reaction is spontaneous.
If $\Delta S_{\text {total }}<0$, the reaction is nonspontaneous.
If $\Delta S_{\text {total }}=0$, the reaction mixture is at equilibrium.
All reactions proceed spontaneously in the direction that increases the entropy of the system plus surroundings. A reaction that is nonspontaneous in the forward direction is spontaneous in the reverse direction because $\Delta S_{\text {total }}$ for the reverse reaction equals $-\Delta S_{\text {total }}$ for the forward reaction. If $\Delta S_{\text {total }}$ is zero, the reaction doesn't go spontaneously in either direction, and the reaction mixture is at equilibrium.

To determine the value of $\Delta S_{\text {total }}$, we need values for the entropy changes in the system and the surroundings. The entropy change in the system, $\Delta S_{\text {sys, }}$, is just the entropy of reaction, which can be calculated from standard molar entropies (Table 17.1), as described in Section 17.5. For a reaction that occurs at constant pressure, the entropy change in the surroundings is directly proportional to the enthalpy change for the reaction $(\Delta H)$ and inversely proportional to the kelvin temperature $(T)$ of the surroundings, according to the equation

$$
\Delta S_{\mathrm{surr}}=\frac{-\Delta H}{T}
$$

Although we won't derive this equation to calculate $\Delta S_{\text {surr }}$, we can nevertheless justify its form. To see why $\Delta S_{\text {surr }}$ is proportional to $-\Delta H$, recall that for an exothermic reaction $(\Delta H<0)$, the system loses heat to the surroundings

vA reaction is spontaneous only if $\Delta S_{\text {system }}+\Delta S_{\text {surroundings }}=$ $\Delta S_{\text {total }}>0 . \Delta S_{\text {system }}$ is calculated from standard molar entropies. $\Delta S_{\text {surr }}=-\Delta H / T$, where $-\Delta H$ is calculated from standard enthalpies of formation.

FIGURE 17.9 (a) When an exothermic reaction occurs in the system $(\Delta H<0)$, the surroundings gain heat and their entropy increases ( $\left.\Delta S_{\text {surr }}>0\right)$. (b) When an endothermic reaction occurs in the system ( $\Delta H>0$ ), the surroundings lose heat and their entropy decreases $\left(\Delta S_{\text {surr }}<0\right)$.
(Figure 17.9a). As a result, the random, chaotic motion of the molecules in the surroundings increases, and the entropy of the surroundings also increases $\left(\Delta S_{\text {surr }}>0\right)$. Conversely, for an endothermic reaction $(\Delta H>0)$, the system gains heat from the surroundings (Figure 17.9b) and the entropy of the surroundings therefore decreases $\left(\Delta S_{\text {surr }}<0\right)$. Because $\Delta S_{\text {surr }}$ is positive when $\Delta H$ is negative, and vice versa, $\Delta S_{\text {surr }}$ is proportional to $-\Delta H$ :

$$
\Delta S_{\text {surr }} \propto-\Delta H
$$



The reason why $\Delta S_{\text {surr }}$ is inversely proportional to the absolute temperature $T$ is more subtle. We can think of the surroundings as an infinitely large constanttemperature bath to which heat can be added without changing its temperature. If the surroundings have a low temperature, they have only a small amount of disorder, in which case addition of a given quantity of heat results in a substantial increase in the amount of disorder (a relatively large value of $\Delta S_{\text {surr }}$ ). If the surroundings have a high temperature, they already have a large amount of disorder, and addition of the same quantity of heat produces only a marginal increase in the amount of disorder (a relatively small value of $\Delta S_{\text {surr }}$ ). Thus, $\Delta S_{\text {surr }}$ varies inversely with temperature:

$$
\Delta S_{\text {surr }} \propto \frac{1}{T}
$$

Adding heat to the surroundings is somewhat analogous to tossing a rock into a lake. If the lake has little disorder (calm, smooth surface), the rock's impact produces considerable disorder, evident in a circular pattern of waves. If the lake is already appreciably disordered (rough, choppy surface), the additional disorder produced when the rock hits the water is hardly noticeable.


A Adding heat to cold surroundings is analogous to tossing a rock into calm waters. Both processes produce a considerable increase in disorder and thus a relatively large increase in entropy.


A Adding heat to hot surroundings is analogous to tossing a rock into rough waters. Both processes produce a relatively small increase in disorder and thus a relatively small increase in entropy.

## Worked Example 17.4

Consider the oxidation of iron metal:

$$
4 \mathrm{Fe}(s)+3 \mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{Fe}_{2} \mathrm{O}_{3}(s)
$$

By determining the sign of $\Delta S_{\text {total }}$, show that the reaction is spontaneous at $25^{\circ} \mathrm{C}$.

## Strategy

To determine the sign of $\Delta S_{\text {total }}=\Delta S_{\text {sys }}+\Delta S_{\text {surr }}$, we need to calculate the values of $\Delta S_{\text {sys }}$ and $\Delta S_{\text {surr }}$. The entropy change in the system equals the standard entropy of reaction and can be calculated using the standard molar entropies in Table 17.1. To obtain $\Delta S_{\text {surr }}=-\Delta H^{\circ} / T$, first calculate $\Delta H^{\circ}$ for the reaction from standard enthalpies of formation (Section 8.10).

## Solution

$$
\begin{aligned}
\Delta S_{\mathrm{sys}} & =\Delta S^{\circ}=2 S^{\circ}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)-\left[4 S^{\circ}(\mathrm{Fe})+3 S^{\circ}\left(\mathrm{O}_{2}\right)\right] \\
& =(2 \mathrm{~mol})\left(87.4 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)-\left[(4 \mathrm{~mol})\left(27.3 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)+(3 \mathrm{~mol})\left(205.0 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)\right] \\
& =-549.5 \mathrm{~J} / \mathrm{K} \\
\Delta H^{\circ} & =2 \Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)-\left[4 \Delta H^{\circ}(\mathrm{Fe})+3 \Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{O}_{2}\right)\right]
\end{aligned}
$$



Because $\Delta H^{\circ}{ }_{\mathrm{f}}=0$ for elements and $\Delta H^{\circ}{ }_{\mathrm{f}}=-824.2 \mathrm{~kJ} / \mathrm{mol}$ for $\mathrm{Fe}_{2} \mathrm{O}_{3}$ (Appendix B), $\Delta H^{\circ}$ for the reaction is

$$
\Delta H^{\circ}=2 \Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)=(2 \mathrm{~mol})(-824.2 \mathrm{~kJ} / \mathrm{mol})=-1648.4 \mathrm{~kJ}
$$

Therefore,

$$
\begin{aligned}
& \Delta S_{\text {surr }}=\frac{-\Delta H^{\circ}}{T}=\frac{-(-1,648,400 \mathrm{~J})}{298.15 \mathrm{~K}}=5529 \mathrm{~J} / \mathrm{K} \\
& \Delta S_{\text {total }}=\Delta S_{\text {sys }}+\Delta S_{\text {surr }}=-549.5 \mathrm{~J} / \mathrm{K}+5529 \mathrm{~J} / \mathrm{K}=4980 \mathrm{~J} / \mathrm{K}
\end{aligned}
$$

Because the total entropy change is positive, the reaction is spontaneous under standardstate conditions at $25^{\circ} \mathrm{C}$.
$\checkmark$ BALLPARK CHECK Since the reaction consumes three moles of gas, $\Delta S_{\text {sys }}$ is negative. Because the oxidation (burning) of iron metal is highly exothermic, $\Delta S_{\text {surr }}=-\Delta H^{\circ} / T$ is positive and very large. The value of $\Delta S_{\text {surr }}$ is greater than the absolute value of $\Delta S_{\text {sys }}$, and so $\Delta S_{\text {total }}$ is positive, in agreement with the solution.

PROBLEM 17.6 By determining the sign of $\Delta S_{\text {total }}$, show whether the decomposition of calcium carbonate is spontaneous under standard-state conditions at $25^{\circ} \mathrm{C}$.

$$
\mathrm{CaCO}_{3}(s) \longrightarrow \mathrm{CaO}(s)+\mathrm{CO}_{2}(g)
$$

## 17.7 | Free Energy

Chemists are generally more interested in the system (the reaction mixture) than the surroundings, and it's therefore convenient to restate the second law in terms of the thermodynamic properties of the system, without regard to the surroundings. For this purpose, we use the thermodynamic property called free energy, denoted by $G$ in honor of J. Willard Gibbs (1839-1903), the American mathematical physicist who laid the foundations of chemical thermodynamics. As discussed in Section 8.14, the free energy $G$ of a system is defined as
free energy $\quad G=H-T S$

Sidney Rosen, "J. Willard Gibbs (1839-1903): A Modern Genius," J. Chem. Educ., Vol. 60, 1983, 593-594.

Robert J. Deltete and David L. Thorsell, "Josiah Willard Gibbs and Wilhelm Ostwald: A Contrast in Scientific Style," J. Chem. Educ., Vol. 73, 1996, 289-295.
where $H$ is the enthalpy, $T$ is the temperature in kelvins, and $S$ is the entropy. As you might expect from its name, free energy has units of energy ( J or kJ ).

Why is $G$ called the free energy? If you think of $T S$ as the part of the system's energy that is already disordered, then $H-T S(=G)$ is the part of the system's energy that is still ordered and therefore free (available) to cause spontaneous change by becoming disordered.

Free energy, like enthalpy and entropy, is a state function, and the change in free energy $(\Delta G)$ for a process is therefore independent of path. For a reaction at constant temperature, $\Delta G$ equals the change in enthalpy minus the product of temperature times the change in entropy:

$$
\Delta G=\Delta H-T \Delta S
$$

To see what this equation for free-energy change has to do with spontaneity, let's return to the relationship

$$
\Delta S_{\text {total }}=\Delta S_{\text {sys }}+\Delta S_{\text {surr }}=\Delta S+\Delta S_{\text {surr }}
$$

where we have now dropped the subscript "sys." (It's generally understood that symbols without a subscript refer to the system, not the surroundings.) Since $\Delta S_{\text {surr }}=-\Delta H / T$, where $\Delta H$ is the heat gained by the system at constant pressure, we can also write

$$
\Delta S_{\text {total }}=\Delta S-\frac{\Delta H}{T}
$$

Multiplying both sides by $-T$ gives

$$
-T \Delta S_{\text {total }}=\Delta H-T \Delta S
$$

The right side of this equation is just $\Delta G$, the change in the free energy of the system at constant temperature and pressure. Therefore,

$$
-T \Delta S_{\text {total }}=\Delta G
$$

Note that $\Delta G$ and $\Delta S_{\text {total }}$ have opposite signs because the absolute temperature $T$ is always positive.

According to the second law of thermodynamics, a reaction is spontaneous if $\Delta S_{\text {total }}$ is positive, nonspontaneous if $\Delta S_{\text {total }}$ is negative, and at equilibrium if $\Delta S_{\text {total }}$ is zero. Since $-T \Delta S_{\text {total }}=\Delta G$ and since $\Delta G$ and $\Delta S_{\text {total }}$ have opposite signs, we can restate the thermodynamic criterion for the spontaneity of a reaction carried out at constant temperature and pressure in the following way:

If $\Delta G<0$, the reaction is spontaneous.
If $\Delta G>0$, the reaction is nonspontaneous.
If $\Delta G=0$, the reaction mixture is at equilibrium.
In other words, in any spontaneous process at constant temperature and pressure, the free energy of the system always decreases.

As discussed in Section 8.14, the temperature $T$ acts as a weighting factor that determines the relative importance of the enthalpy and entropy contributions to $\Delta G$ in the free-energy equation $\Delta G=\Delta H-T \Delta S$. If $\Delta H$ and $\Delta S$ are either both negative or both positive, the sign of $\Delta G$ (and therefore the spontaneity of the reaction) depends on the temperature (Table 17.2). If $\Delta H$ and $\Delta S$ are both negative, the reaction will be spontaneous only if the absolute value of $\Delta H$ is larger than the absolute value of $T \Delta S$. This is most likely at low temperatures, where the weighting factor $T$ in $T \Delta S$ is small. If $\Delta H$ and $\Delta S$ are both positive, the reaction will be spontaneous only if $T \Delta S$ is larger than $\Delta H$, which is most likely at high temperatures. We've already seen how these considerations apply to phase changes (Section 10.4).

TABLE 17.2 Signs of Enthalpy, Entropy, and Free-Energy Changes and Reaction Spontaneity for a Reaction at Constant Temperature and Pressure

| $\Delta \boldsymbol{H}$ | $\Delta S$ | $\Delta G=\Delta H-T \Delta S$ | Reaction Spontaneity | Example |
| :---: | :---: | :---: | :---: | :---: |
| - | + | - | Spontaneous at all temperatures | $2 \mathrm{NO}_{2}(g) \rightarrow \mathrm{N}_{2}(g)+2 \mathrm{O}_{2}(g)$ |
| - | - | - or + | Spontaneous at low temperatures where $\Delta H$ outweighs $T \Delta S$ | $\mathrm{N}_{2}(\mathrm{~g})+3 \mathrm{H}_{2}(g) \rightarrow 2 \mathrm{NH}_{3}(g)$ |
|  |  |  | Nonspontaneous at high temperatures where $T \Delta S$ outweighs $\Delta H$ |  |
| + | - | + | Nonspontaneous at all temperatures | $3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{O}_{3}(\mathrm{~g})$ |
| $+$ | + | - or + | Spontaneous at high temperatures where $T \Delta S$ outweighs $\Delta H$ | $2 \mathrm{HgO}(s) \rightarrow 2 \mathrm{Hg}(l)+\mathrm{O}_{2}(g)$ |
|  |  |  | Nonspontaneous at low temperatures where $\Delta H$ outweighs $T \Delta S$ |  |

## Worked Example 17.5

Iron metal can be produced by reducing iron(III) oxide with hydrogen:

$$
\begin{aligned}
\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{Fe}(s)+3 \mathrm{H}_{2} \mathrm{O}(g) \\
\Delta H^{\circ}=+98.8 \mathrm{~kJ} ; \Delta S^{\circ}=+141.5 \mathrm{~J} / \mathrm{K}
\end{aligned}
$$

(a) Is this reaction spontaneous under standard-state conditions at $25^{\circ} \mathrm{C}$ ?
(b) At what temperature will the reaction become spontaneous?

## Strategy and Solution

(a) To determine whether the reaction is spontaneous at $25^{\circ} \mathrm{C}$, we need to determine the sign of $\Delta G=\Delta H-T \Delta S$. At $25^{\circ} \mathrm{C}(298 \mathrm{~K}), \Delta G$ for the reaction is

$$
\begin{aligned}
\Delta G=\Delta H-T \Delta S & =(98.8 \mathrm{~kJ})-(298 \mathrm{~K})(0.1415 \mathrm{~kJ} / \mathrm{K}) \\
& =(98.8 \mathrm{~kJ})-(42.2 \mathrm{~kJ}) \\
& =56.6 \mathrm{~kJ}
\end{aligned}
$$

Because the positive $\Delta H$ term is larger than the positive $T \Delta S$ term, $\Delta G$ is positive and the reaction is nonspontaneous at 298 K .
(b) At sufficiently high temperatures, $T \Delta S$ becomes larger than $\Delta H, \Delta G$ becomes negative, and the reaction becomes spontaneous. We can estimate the temperature at which $\Delta G$ changes from positive to negative by setting $\Delta G=\Delta H-T \Delta S=0$. Solving for $T$, we find that the reaction becomes spontaneous at 698 K :

$$
T=\frac{\Delta H}{\Delta S}=\frac{98.8 \mathrm{~kJ}}{0.1415 \mathrm{~kJ} / \mathrm{K}}=698 \mathrm{~K}
$$

This calculation assumes the values of $\Delta H$ and $\Delta S$ are unchanged on going from 298 K to 698 K . In general, the enthalpies and entropies of both reactants and products increase with increasing temperature, but the increases for the products tend to cancel the increases for the reactants. As a result, values of $\Delta H$ and $\Delta S$ for a reaction are relatively independent of temperature, at least over a relatively small temperature range. In this example, the temperature range is quite large ( 400 K ), and so the calculated value of $T$ is only an estimate.

$\square$Two types of reactions have a spontaneity that cannot be reversed by changing the temperature (those with opposite signs for $\Delta H$ and $\Delta S$ ), and two have a spontaneity that can be reversed by changing the temperature (those with $\Delta H$ and $\Delta S$ both negative or both positive).

$\square$According to $\Delta G=$ $\Delta H-T \Delta S$, a spontaneous reaction is favored by a decrease in enthalpy and an increase in entropy. At lower temperatures the enthalpy term usually dominates; at higher temperatures the entropy term can become dominant.

## $\checkmark$ Ballpark Check

(a) Let's use rounded values of $\Delta H(100 \mathrm{~kJ}), T(300 \mathrm{~K})$, and $\Delta S(0.14 \mathrm{~kJ} / \mathrm{K})$ to estimate the relative values of $\Delta H$ and $T \Delta S$. Because $T \Delta S=300 \mathrm{~K} \times$ $0.14 \mathrm{~kJ} / \mathrm{K}=42 \mathrm{~kJ}$ is smaller than $\Delta H(100 \mathrm{~kJ}), \Delta G=\Delta H-T \Delta S$ is positive and the reaction is nonspontaneous at 300 K . The ballpark check agrees with the solution.
(b) The temperature at which the reaction becomes spontaneous is approximately $(100 \mathrm{~kJ}) /(0.14 \mathrm{~kJ} / \mathrm{K}) \approx 700 \mathrm{~K}$, in agreement with the solution.

- PROBLEM 17.7 Consider the decomposition of gaseous $\mathrm{N}_{2} \mathrm{O}_{4}$ :

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \longrightarrow 2 \mathrm{NO}_{2}(g) \quad \Delta H^{\circ}=+57.1 \mathrm{~kJ} ; \Delta S^{\circ}=+175.8 \mathrm{~J} / \mathrm{K}
$$

(a) Is this reaction spontaneous under standard-state conditions at $25^{\circ} \mathrm{C}$ ?
(b) Estimate the temperature at which the reaction becomes spontaneous.

PROBLEM 17.8 The following data apply to the vaporization of mercury: $\Delta H_{\text {vap }}=$ $58.5 \mathrm{~kJ} / \mathrm{mol} ; \Delta S_{\text {vap }}=92.9 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$.
(a) Does mercury boil at $325^{\circ} \mathrm{C}$ and 1 atm pressure?
(b) What is the normal boiling point of mercury?

- KEY CONCEPT PROBLEM 17.9 What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ for the following spontaneous reaction of $A$ atoms (red) and B atoms (blue)?



## 17.8 | Standard Free-Energy Changes for Reactions

The free energy of a substance, like its enthalpy and entropy, depends on temperature, pressure, the physical state of the substance (solid, liquid, or gas), and its concentration (in the case of solutions). As a result, free-energy changes for chemical reactions must be compared under a well-defined set of standard-state conditions:
$-\underset{\text { CONDITIONS }}{\text { STANDARD-State }}\left\{\begin{array}{l}\text { Solids, liquids, and gases in pure form at } 1 \mathrm{~atm} \text { pressure } \\ \text { Solutes at } 1 \mathrm{M} \text { concentration } \\ \text { A specified temperature, usually } 25^{\circ} \mathrm{C}\end{array}\right.$

The standard free-energy change, $\Delta G^{\circ}$, for a reaction is the change in free energy that occurs when reactants in their standard states are converted to products in their standard states. As with $\Delta H^{\circ}$ (Section 8.10), the value of $\Delta G^{\circ}$ is an extensive property that refers to the number of moles indicated in the chemical equation. For example, $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$ for the reaction

$$
\mathrm{Na}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 1 / 2 \mathrm{H}_{2}(g)+\mathrm{Na}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

is the change in free energy that occurs when 1 mol of solid sodium reacts completely with 1 mol of liquid water to give 0.5 mol of hydrogen gas at 1 atm pressure, along with an aqueous solution that contains 1 mol of $\mathrm{Na}^{+}$ions and 1 mol of $\mathrm{OH}^{-}$ions at concentrations of 1 M , with all reactants and products at a temperature of $25^{\circ} \mathrm{C}$. For this reaction, $\Delta G^{\circ}=-182 \mathrm{~kJ}$.

Because the free-energy change for any process at constant temperature and pressure is $\Delta G=\Delta H-T \Delta S$, we can calculate the standard free-energy change $\Delta G^{\circ}$ for a reaction from the standard enthalpy change $\Delta H^{\circ}$ and the standard entropy change $\Delta S^{\circ}$. Consider again the Haber synthesis of ammonia:

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g) \quad \Delta H^{\circ}=-92.2 \mathrm{~kJ} ; \Delta S^{\circ}=-198.7 \mathrm{~J} / \mathrm{K}
$$

The standard free-energy change at $25^{\circ} \mathrm{C}(298 \mathrm{~K})$ is

$$
\begin{aligned}
\Delta G^{\circ}=\Delta H^{\circ}-T \Delta S^{\circ} & =\left(-92.2 \times 10^{3} \mathrm{~J}\right)-(298 \mathrm{~K})(-198.7 \mathrm{~J} / \mathrm{K}) \\
& =\left(-92.2 \times 10^{3} \mathrm{~J}\right)-\left(-59.2 \times 10^{3} \mathrm{~J}\right) \\
& =-33.0 \mathrm{~kJ}
\end{aligned}
$$

Because the negative $\Delta H^{\circ}$ term is larger than the negative $T \Delta S^{\circ}$ term at $25^{\circ} \mathrm{C}, \Delta G^{\circ}$ is negative and the reaction is spontaneous under standard-state conditions.

A standard free-energy change applies to a hypothetical process rather than an actual process. In a hypothetical process, separate reactants in their standard states are completely converted to separate products in their standard states. In an actual process, however, reactants and products are mixed together, and the reaction may not go to completion.

Take the Haber synthesis, for example. The hypothetical process is

where $\Delta G^{\circ}=-33.0 \mathrm{~kJ}$ is the change in the free energy of the system on going from state 1 to state 2 . In an actual synthesis of ammonia, however, the reactants $\mathrm{N}_{2}$ and $\mathrm{H}_{2}$ are not separate but are mixed together. Moreover, the reaction doesn't go to completion; it reaches an equilibrium state in which both reactants and products are present together.

How, then, should we think about the meaning of $\Delta G^{\circ}$ in the context of an actual reaction? One way would be to suppose that we have a mixture of $\mathrm{N}_{2}, \mathrm{H}_{2}$, and $\mathrm{NH}_{3}$, with each substance present at a partial pressure of 1 atm . Suppose further that the mixture behaves as an ideal gas so that the free energy of each component in the mixture is the same as the free energy of the pure substance. Finally, suppose that the number of moles of each component-say $x, y$, and $z$-is very large so that the partial pressures don't change appreciably when 1 mol of $\mathrm{N}_{2}$ and 3 mol of $\mathrm{H}_{2}$ are converted to 2 mol of $\mathrm{NH}_{3}$. In other words, we are imagining the following real process:


State 2

The free-energy change for this process is the standard free-energy change $\Delta G^{\circ}$, since each reactant and product is present at 1 atm pressure. If $\Delta G^{\circ}$ is negative, the reaction will proceed spontaneously to give more products. If $\Delta G^{\circ}$ is positive, the reaction will proceed in the reverse direction to give more reactants. As always, the value of $\Delta G^{\circ}$ provides no information concerning the rate of the reaction.

## Worked Example 17.6

Gibb's Free Energy activity

Iron metal is produced commercially by reducing iron(III) oxide in iron ore with carbon monoxide:

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \longrightarrow 2 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(g)
$$

(a) Calculate the standard free-energy change for this reaction at $25^{\circ} \mathrm{C}$.
(b) Is the reaction spontaneous under standard-state conditions at $25^{\circ} \mathrm{C}$ ?
(c) Does the reverse reaction become spontaneous at higher temperatures? Explain.

## Strategy

(a) We can calculate the standard free-energy change from the relation $\Delta G^{\circ}=$ $\Delta H^{\circ}-T \Delta S^{\circ}$, but first we must find $\Delta H^{\circ}$ and $\Delta S^{\circ}$ from standard enthalpies of formation ( $\Delta H^{\circ}{ }_{\mathrm{f}}$ ) and standard molar entropies ( $S^{\circ}$ ).
(b) The reaction is spontaneous under standard-state conditions if $\Delta G^{\circ}$ is negative.
(c) The spontaneity of the reaction at higher temperatures depends on the signs and magnitudes of $\Delta H^{\circ}$ and $\Delta S^{\circ}$.

## Solution

(a) The following values of $\Delta H^{\circ}$ fand $S^{\circ}$ are found in Appendix B:

|  | $\mathbf{F e}_{\mathbf{2}} \mathbf{O}_{\mathbf{3}}(\mathbf{s})$ | $\mathbf{C O}(\boldsymbol{g})$ | $\mathbf{F e}(\boldsymbol{s})$ | $\mathbf{C O}_{\mathbf{2}}(\boldsymbol{g})$ |
| :--- | :---: | :---: | :---: | :---: |
| $\Delta H_{\mathrm{f}}^{\circ}(\mathrm{kJ} / \mathrm{mol})$ | -824.2 | -110.5 | 0 | -393.5 |
| $S^{\circ}[\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})]$ | 87.4 | 197.6 | 27.3 | 213.6 |

So we have

$$
\begin{aligned}
\Delta H^{\circ}= & {\left[2 \Delta H^{\circ}{ }_{\mathrm{f}}(\mathrm{Fe})+3 \Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{CO}_{2}\right)\right]-\left[\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)+3 \Delta H^{\circ}{ }_{\mathrm{f}}(\mathrm{CO})\right] } \\
= & {[(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(-393.5 \mathrm{~kJ} / \mathrm{mol})] } \\
& -[(1 \mathrm{~mol})(-824.2 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(-110.5 \mathrm{~kJ} / \mathrm{mol})] \\
\Delta H^{\circ}= & -24.8 \mathrm{~kJ}
\end{aligned}
$$

and

$$
\begin{aligned}
\Delta S^{\circ}= & {\left[2 S^{\circ}(\mathrm{Fe})+3 S^{\circ}\left(\mathrm{CO}_{2}\right)\right]-\left[S^{\circ}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)+3 S^{\circ}(\mathrm{CO})\right] } \\
= & {\left[(2 \mathrm{~mol})\left(27.3 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)+(3 \mathrm{~mol})\left(213.6 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)\right] } \\
& -\left[(1 \mathrm{~mol})\left(87.4 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)+(3 \mathrm{~mol})\left(197.6 \frac{\mathrm{~J}}{\mathrm{~K} \cdot \mathrm{~mol}}\right)\right] \\
\Delta S^{\circ}= & +15.0 \mathrm{~J} / \mathrm{K} \text { or } \quad 0.0150 \mathrm{~kJ} / \mathrm{K}
\end{aligned}
$$

Therefore,

$$
\begin{aligned}
\Delta G^{\circ} & =\Delta H^{\circ}-T \Delta S^{\circ} \\
& =(-24.8 \mathrm{~kJ})-(298 \mathrm{~K})(0.0150 \mathrm{~kJ} / \mathrm{K}) \\
\Delta G^{\circ} & =-29.3 \mathrm{~kJ}
\end{aligned}
$$

(b) Because $\Delta G^{\circ}$ is negative, the reaction is spontaneous at $25^{\circ} \mathrm{C}$. This means that a mixture of $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s}), \mathrm{CO}(\mathrm{g})$, $\mathrm{Fe}(\mathrm{s})$, and $\mathrm{CO}_{2}(g)$, with each gas at a partial pressure of 1 atm , will react at $25^{\circ} \mathrm{C}$ to produce more iron metal.
(c) Because $\Delta H^{\circ}$ is negative and $\Delta S^{\circ}$ is positive, $\Delta G^{\circ}$ will be negative at all temperatures. The forward reaction is therefore spontaneous at all temperatures, and the reverse reaction does not become spontaneous at higher temperatures.

PROBLEM 17.10 Consider the thermal decomposition of calcium carbonate:

$$
\mathrm{CaCO}_{3}(s) \longrightarrow \mathrm{CaO}(s)+\mathrm{CO}_{2}(g)
$$

(a) Use the data in Appendix B to calculate the standard free-energy change for this reaction at $25^{\circ} \mathrm{C}$.
(b) Will a mixture of solid $\mathrm{CaCO}_{3}$, solid CaO , and gaseous $\mathrm{CO}_{2}$ at 1 atm pressure react spontaneously at $25^{\circ} \mathrm{C}$ to produce more CaO and $\mathrm{CO}_{2}$ ?
(c) Assuming that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature, estimate the temperature at which the reaction becomes spontaneous.
-KEY CONCEPT PROBLEM 17.11 Consider the following endothermic decomposition of $A B_{2}$ molecules:

(a) What is the $\operatorname{sign}(+,-$, or 0$)$ of $\Delta S^{\circ}$ for the reaction?
(b) Is the reaction more likely to be spontaneous at high temperatures or at low temperatures? Explain.

### 17.9 Standard Free Energies of Formation

The standard free energy of formation, $\Delta G^{\circ}{ }_{f}$, of a substance is the free-energy change for formation of one mole of the substance in its standard state from the most stable form of its constituent elements in their standard states. For example, we found in Section 17.8 that the standard free-energy change $\Delta G^{\circ}$ for the synthesis of 2 mol of $\mathrm{NH}_{3}$ from its constituent elements is -33.0 kJ :

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g) \quad \Delta G^{\circ}=-33.0 \mathrm{~kJ}
$$

Therefore, $\Delta G^{\circ}{ }_{\mathrm{f}}$ for ammonia is $-33.0 \mathrm{~kJ} / 2 \mathrm{~mol}$, or $-16.5 \mathrm{~kJ} / \mathrm{mol}$.
Values of $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$ for some common substances are listed in Table 17.3, and additional values are given in Appendix B. Note that $\Delta G^{\circ}$ for an element in its most stable form at $25^{\circ} \mathrm{C}$ is defined to be zero. Thus, solid graphite has $\Delta G^{\circ}=0 \mathrm{~kJ} / \mathrm{mol}$, but diamond, a less stable form of solid carbon at $25^{\circ} \mathrm{C}$, has $\Delta G^{\circ}{ }_{\mathrm{f}}=2.9 \mathrm{~kJ} / \mathrm{mol}$. As with standard enthalpies of formation, $\Delta H_{\mathrm{f}}^{\circ}$, a zero value of $\Delta G^{\circ}$ for elements in their most stable form establishes a thermochemical "sea level," or reference point, with respect to which the standard free energies of other substances are measured. We can't measure the absolute value of a substance's free energy (as we can the entropy), but that's not a problem because we are interested only in free-energy differences between reactants and products.

The standard free energy of formation of a substance measures its thermodynamic stability with respect to its constituent elements. Substances that have a negative value of $\Delta G^{\circ}{ }_{f}$, such as carbon dioxide and water, are stable and do not decompose to their constituent elements under standard-state conditions. Substances that have a positive value of $\Delta G^{\circ}{ }_{f}$, such as ethylene and nitrogen dioxide, are thermodynamically unstable with respect to their constituent elements. Once prepared, though, such substances can exist for long periods of time if the rate of their decomposition is slow.

$\nabla$
For an element in its most stable form at $25^{\circ} \mathrm{C}$, both the standard free-energy of formation and the standard enthalpy of formation are equal to zero.

$\sqrt{ }$A substance with a negative standard free energy of formation with respect to decomposition to its constituent elements is stable. However, the substance may be unstable with respect to some other reaction under the same set of conditions.

TABLE 17.3 Standard Free Energies of Formation for Some Common Substances at $25^{\circ} \mathrm{C}$

| Substance | Formula | $\Delta G^{\circ}{ }_{\mathbf{f}}(\mathbf{k J} / \mathrm{mol})$ | Substance | Formula | $\Delta G^{\circ}{ }_{f}(\mathbf{k J} / \mathrm{mol})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Gases |  |  | Liquids |  |  |
| Acetylene | $\mathrm{C}_{2} \mathrm{H}_{2}$ | 209.2 | Acetic acid | $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}$ | -390 |
| Ammonia | $\mathrm{NH}_{3}$ | -16.5 | Ethanol | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$ | -174.9 |
| Carbon dioxide | $\mathrm{CO}_{2}$ | -394.4 | Methanol | $\mathrm{CH}_{3} \mathrm{OH}$ | -166.4 |
| Carbon monoxide | CO | -137.2 | Water | $\mathrm{H}_{2} \mathrm{O}$ | -237.2 |
| Ethylene | $\mathrm{C}_{2} \mathrm{H}_{4}$ | 68.1 | Solids |  |  |
| Hydrogen | $\mathrm{H}_{2}$ | 0 | Calcium carbonate | $\mathrm{CaCO}_{3}$ | -1128.8 |
| Methane | $\mathrm{CH}_{4}$ | -50.8 | Calcium oxide | CaO | -604.0 |
| Nitrogen | $\mathrm{N}_{2}$ | 0 | Diamond | C | 2.9 |
| Nitrogen dioxide | $\mathrm{NO}_{2}$ | 51.3 | Graphite | C | 0 |
| Dinitrogen tetroxide | $\mathrm{N}_{2} \mathrm{O}_{4}$ | 97.8 | Iron(III) oxide | $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | -742.2 |

There's no point in trying to synthesize a substance from its elements under standard-state conditions if the substance has a positive value of $\Delta G^{\circ}{ }_{f}$. Such a substance would have to be prepared at other temperatures and/or pressures, or it would have to be made from alternative starting materials using a reaction that has a negative free-energy change. Thus, a knowledge of thermodynamics can save considerable time in chemical synthesis.

In Section 17.8, we calculated standard free-energy changes for reactions from the equation $\Delta G^{\circ}=\Delta H^{\circ}-T \Delta S^{\circ}$, using tabulated values of $\Delta H^{\circ}{ }_{\mathrm{f}}$ and $S^{\circ}$ to find $\Delta H^{\circ}$ and $\Delta S^{\circ}$. Alternatively, we can calculate $\Delta G^{\circ}$ more directly by subtracting the standard free energies of formation of all the reactants from the standard free energies of formation of all the products:

$$
\Delta G^{\circ}=\Delta G_{\mathrm{f}}^{\circ}(\text { products })-\Delta G_{\mathrm{f}}^{\circ}(\text { reactants })
$$

For the general reaction

$$
a \mathrm{~A}+b \mathrm{~B} \longrightarrow c \mathrm{C}+d \mathrm{D}
$$

the standard free-energy change is

$$
\Delta G^{\circ}=\left[c \Delta G^{\circ}{ }_{\mathrm{f}}(\mathrm{C})+d \Delta G^{\circ}{ }_{\mathrm{f}}(\mathrm{D})\right]-\left[a \Delta G_{\mathrm{f}}^{\circ}(\mathrm{A})+b \Delta G^{\circ}{ }_{\mathrm{f}}(\mathrm{~B})\right]
$$

To illustrate, let's calculate the standard free-energy change for the reaction in Worked Example 17.6-the reduction of iron(III) oxide with carbon monoxide:

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \longrightarrow 2 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(g)
$$

Using the $\Delta G^{\circ}{ }_{f}$ values in Table 17.3, we obtain

$$
\begin{aligned}
\Delta G^{\circ}= & {\left[2 \Delta G^{\circ}(\mathrm{Fe})+3 \Delta G_{\mathrm{f}}^{\circ}\left(\mathrm{CO}_{2}\right)\right]-\left[\Delta G_{\mathrm{f}}^{\circ}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)+3 \Delta G_{\mathrm{f}}^{\circ}(\mathrm{CO})\right] } \\
= & {[(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(-394.4 \mathrm{~kJ} / \mathrm{mol})] } \\
& -[(1 \mathrm{~mol})(-742.2 \mathrm{~kJ} / \mathrm{mol})+(3 \mathrm{~mol})(-137.2 \mathrm{~kJ} / \mathrm{mol})] \\
\Delta G^{\circ}= & -29.4 \mathrm{~kJ}
\end{aligned}
$$

This result agrees well with the value of -29.3 kJ calculated from $\Delta G^{\circ}=$ $\Delta H^{\circ}-T \Delta S^{\circ}$ in Worked Example 17.6.

## Worked Example 17.7

(a) Calculate the standard free-energy change for the oxidation of ammonia to give nitric oxide ( NO ) and water. Is it worth trying to find a catalyst for this reaction?

$$
4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \longrightarrow 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(l)
$$

(b) Is it worth trying to find a catalyst for the synthesis of NO from gaseous $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$ under standard-state conditions at $25^{\circ} \mathrm{C}$ ?

## Strategy

We can calculate $\Delta G^{\circ}$ most easily from tabulated standard free energies of formation (Appendix B). It's worth trying to find a catalyst for a reaction only if the reaction has a negative free-energy change.

## Solution

(a) $\Delta G^{\circ}=\left[4 \Delta G^{\circ}{ }_{\mathrm{f}}(\mathrm{NO})+6 \Delta G^{\circ}{ }_{\mathrm{f}}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]-\left[4 \Delta G^{\circ}{ }_{\mathrm{f}}\left(\mathrm{NH}_{3}\right)+5 \Delta G^{\circ}{ }_{\mathrm{f}}\left(\mathrm{O}_{2}\right)\right]$
$=[(4 \mathrm{~mol})(86.6 \mathrm{~kJ} / \mathrm{mol})+(6 \mathrm{~mol})(-237.2 \mathrm{~kJ} / \mathrm{mol})]$
$-[(4 \mathrm{~mol})(-16.5 \mathrm{~kJ} / \mathrm{mol})+(5 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})]$
$\Delta G^{\circ}=-1010.8 \mathrm{~kJ}$
It is worth looking for a catalyst because the negative value of $\Delta G^{\circ}$ indicates that the reaction is spontaneous under standard-state conditions. (This reaction is the first step in the Ostwald process for production of nitric acid. In industry, the reaction is carried out using a platinum-rhodium catalyst.)
(b) It's not worth looking for a catalyst for the reaction $\mathrm{N}_{2}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{NO}(g)$ because the standard free energy of formation of NO is positive $\left(\Delta G^{\circ}{ }_{f}=\right.$ $86.6 \mathrm{~kJ} / \mathrm{mol}$ ). This means that NO is unstable with respect to decomposition to $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$ under standard-state conditions at $25^{\circ} \mathrm{C}$. A catalyst could only increase the rate of decomposition. It can't affect the composition of the equilibrium mixture (Section 13.10), and so it can't affect the direction of the reaction.

## - PROBLEM 17.12

(a) Using values of $\Delta G^{\circ}{ }_{f}$ in Appendix B, calculate the standard free-energy change for the reaction of calcium carbide $\left(\mathrm{CaC}_{2}\right)$ with water. Might this reaction be used for synthesis of acetylene $\left(\mathrm{C}_{2} \mathrm{H}_{2}\right)$ ?

$$
\mathrm{CaC}_{2}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{2}(g)+\mathrm{Ca}(\mathrm{OH})_{2}(s)
$$

(b) Is it possible to synthesize acetylene from solid graphite and gaseous $\mathrm{H}_{2}$ at $25^{\circ} \mathrm{C}$ and 1 atm pressure?

### 17.10 Free-Energy Changes and Composition of the Reaction Mixture

The sign of the standard free-energy change $\Delta G^{\circ}$ tells the direction of spontaneous reaction when both reactants and products are present at standard-state conditions. In actual reactions, however, the composition of the reaction mixture seldom corresponds to standard-state pressures and concentrations. Moreover, the partial pressures and concentrations change as a reaction proceeds. How, then, do we calculate the free-energy change $\Delta G$ for a reaction when the reactants and products are present at nonstandard-state pressures and concentrations?

The answer is given by the relation

$$
\Delta G=\Delta G^{\circ}+R T \ln Q
$$

where $\Delta G$ is the free-energy change under nonstandard-state conditions, $\Delta G^{\circ}$ is the free-energy change under standard-state conditions, $R$ is the gas constant, $T$ is the absolute temperature in kelvins, and $Q$ is the reaction quotient ( $Q_{p}$ for reactions involving gases because the standard state for gases is 1 atm pressure, or $Q_{c}$ for reactions involving solutes in solution because the standard state for solutes is 1 M concentration). Recall from Section 13.5 that the reaction quotient $Q_{\mathrm{c}}$ is an expression having the same form as the equilibrium constant expression $K_{c}$ except that the concentrations do not necessarily have equilibrium values. Similarly, $Q_{p}$ has the same form as $K_{p}$ except that the partial pressures have arbitrary values. For example, for the Haber synthesis of ammonia:

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g) \quad Q_{\mathrm{p}}=\frac{\left(P_{\mathrm{NH}_{3}}\right)^{2}}{\left(P_{\mathrm{N}_{2}}\right)\left(P_{\mathrm{H}_{2}}\right)^{3}}
$$

(For reactions that involve both gases and solutes in solution, the reaction quotient $Q$ contains partial pressures of gases and molar concentrations of solutes.)

We won't derive the equation for $\Delta G$ under nonstandard-state conditions. It's hardly surprising, however, that $\Delta G$ and $Q$ should turn out to be related because both predict the direction of a reaction. Worked Example 17.8 shows how to use this equation.

## Worked Example 17.8

Calculate the free-energy change for ammonia synthesis at $25^{\circ} \mathrm{C}(298 \mathrm{~K})$ given the following sets of partial pressures:
(a) $1.0 \mathrm{~atm} \mathrm{~N}_{2}, 3.0 \mathrm{~atm} \mathrm{H}_{2}, 0.020 \mathrm{~atm} \mathrm{NH}_{3}$
(b) $0.010 \mathrm{~atm} \mathrm{~N}_{2}, 0.030 \mathrm{~atm} \mathrm{H}_{2}, 2.0 \mathrm{~atm} \mathrm{NH}_{3}$

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g) \quad \Delta G^{\circ}=-33.0 \mathrm{~kJ}
$$

## Strategy

We can calculate $\Delta G$ from the relation $\Delta G=\Delta G^{\circ}+R T \ln Q$, where $Q$ is $Q_{p}$ for the reaction $\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)$.

## SOlUTION

(a) The value of $Q_{\mathrm{p}}$ is

$$
Q_{\mathrm{p}}=\frac{\left(P_{\mathrm{NH}_{3}}\right)^{2}}{\left(P_{\mathrm{N}_{2}}\right)\left(P_{\mathrm{H}_{2}}\right)^{3}}=\frac{(0.020)^{2}}{(1.0)(3.0)^{3}}=1.5 \times 10^{-5}
$$

Substituting this value of $Q_{\mathrm{p}}$ into the equation for $\Delta G$ gives

$$
\begin{aligned}
\Delta G & =\Delta G^{\circ}+R T \ln Q \\
& =\left(-33.0 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right)+[8.314 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})](298 \mathrm{~K})\left(\ln 1.5 \times 10^{-5}\right) \\
& =\left(-33.0 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right)+\left(-27.5 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right) \\
\Delta G & =-60.5 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

To maintain consistent units in this calculation, we have expressed $\Delta G$ and $\Delta G^{\circ}$ in units of $\mathrm{kJ} / \mathrm{mol}$ because $R$ has units of $\mathrm{J} /(\mathrm{K} \cdot \mathrm{mol})$. The "per mole" in this context means per molar amounts of reactants and products indicated by the coefficients in the balanced equation. Thus, the free-energy change is -60.5 kJ when 1 mol of $\mathrm{N}_{2}$ and 3 mol of $\mathrm{H}_{2}$ are converted to 2 mol of $\mathrm{NH}_{3}$ under the specified conditions.
$\Delta G$ is more negative than $\Delta G^{\circ}$ because $Q_{\mathrm{p}}$ is less than 1 and $\ln Q_{\mathrm{p}}$ is therefore a negative number. Thus, the reaction has a greater thermodynamic driving force under the cited conditions than it does under standard-state conditions. When each reactant and product is present at a partial pressure of $1 \mathrm{~atm}, Q_{\mathrm{p}}=1, \ln Q_{\mathrm{p}}=0$, and $\Delta G=\Delta G^{\circ}$.
(b) The value of $Q_{p}$ is

$$
Q_{\mathrm{p}}=\frac{\left(P_{\mathrm{NH}_{3}}\right)^{2}}{\left(P_{\mathrm{N}_{2}}\right)\left(P_{\mathrm{H}_{2}}\right)^{3}}=\frac{(2.0)^{2}}{(0.010)(0.030)^{3}}=1.5 \times 10^{7}
$$

The corresponding value of $\Delta G$ is

$$
\begin{aligned}
\Delta G & =\Delta G^{\circ}+R T \ln Q_{\mathrm{p}} \\
& =\left(-33.0 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right)+[8.314 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})](298 \mathrm{~K})\left(\ln 1.5 \times 10^{7}\right) \\
& =\left(-33.0 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right)+\left(40.9 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right)
\end{aligned}
$$

$$
\Delta G=7.9 \mathrm{~kJ} / \mathrm{mol}
$$

Because $Q_{p}$ is large enough to give a positive value for $\Delta G$, the reaction is nonspontaneous in the forward direction but spontaneous in the reverse direction. Thus, as we saw already in Section 13.7, the direction in which a reaction proceeds spontaneously depends on the composition of the reaction mixture.

## $\checkmark$ Ballpark Check

(a) Based on Le Châtelier's principle (Section 13.6), we expect that the reaction will have a greater tendency to occur under the cited conditions than under standard-state conditions because one of the reactant partial pressures is greater than 1 atm and the product partial pressure is less than 1 atm . We therefore predict that $\Delta G$ will be more negative than $\Delta G^{\circ}$, in agreement with the solution.
(b) In this case, the reaction mixture is rich in the product and poor in the reactants. Therefore, $Q_{\mathrm{p}}$ is expected to be greater than 1, and $\Delta G$ should be more positive than $\Delta G^{\circ}$, in agreement with the solution.

PROBLEM 17.13 Calculate $\Delta G$ for the formation of ethylene $\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)$ from carbon and hydrogen at $25^{\circ} \mathrm{C}$ when the partial pressures are $100 \mathrm{~atm} \mathrm{H}_{2}$ and $0.10 \mathrm{~atm} \mathrm{C}_{2} \mathrm{H}_{4}$.

$$
2 \mathrm{C}(s)+2 \mathrm{H}_{2}(g) \longrightarrow \mathrm{C}_{2} \mathrm{H}_{4}(g) \quad \Delta G^{\circ}=68.1 \mathrm{~kJ}
$$

Is the reaction spontaneous in the forward or the reverse direction?

- KEY CONCEPT PROBLEM 17.14 Consider the following gas-phase reaction of $\mathrm{A}_{2}$ (red) and $\mathrm{B}_{2}$ (blue) molecules:

$$
\mathrm{A}_{2}+\mathrm{B}_{2} \rightleftharpoons 2 \mathrm{AB} \quad \Delta G^{\circ}=15 \mathrm{~kJ}
$$

(a) Which of the following reaction mixtures has the largest $\Delta G$ of reaction, and which has the smallest?

(b) If the partial pressure of each reactant and product in reaction mixture (1) is equal to 1 atm , what is the value of $\Delta G$ for the reaction in mixture (1)?

Zheng Xianmin, "The Free Energy Prediction and the Principle of Le Châtelier," J. Chem. Educ., Vol. 66, 1989, 401-402.

$\square$
When all reactants and products are under standard conditions, $Q=1$ and $\Delta G=\Delta G^{\circ}$.

FIGURE 17.10 The total free energy of a reaction mixture as a function of the progress of the reaction. Beginning with either pure reactants or pure products, the free energy decreases ( $\Delta G$ is negative) as the system moves toward equilibrium. The graph is drawn assuming that the pure reactants and pure products are in their standard states and that $\Delta G^{\circ}$ for the reaction is negative so the equilibrium composition is rich in products.

### 17.11 Free Energy and Chemical Equilibrium

Now that we've seen how $\Delta G$ for a reaction depends on composition, we can understand how the total free energy of a reaction mixture changes as the reaction progresses toward equilibrium. Look again at the expression for calculating $\Delta G$ :

$$
\Delta G=\Delta G^{\circ}+R T \ln Q
$$

If the reaction mixture contains mainly reactants and almost no products, $Q$ will be much less than 1 and $R T \ln Q$ will be a very large negative number (minus infinity when $Q=0$ ). Consequently, no matter what the value of $\Delta G^{\circ}$ (positive or negative), the negative $R T \ln Q$ term will dominate the $\Delta G^{\circ}$ term, and $\Delta G$ will be negative. This means that the forward reaction is always spontaneous when the concentration of products is very small. Conversely, if the reaction mixture contains mainly products and almost no reactants, $Q$ will be much greater than 1, and $R T \ln Q$ will be a very large positive number (plus infinity when no reactants are present). Consequently, the positive $R T \ln Q$ term will dominate the $\Delta G^{\circ}$ term, and $\Delta G$ will be positive. Thus, the reverse reaction is always spontaneous when the concentration of reactants is very small. These conditions are summarized as follows:

- When the reaction mixture is mostly reactants:

$$
Q \ll 1 \quad R T \ln Q \ll 0 \quad \Delta G<0
$$

The total free energy decreases as the reaction proceeds spontaneously in the forward direction.

- When the reaction mixture is mostly products:

$$
Q \gg 1 \quad R T \ln Q \gg 0 \quad \Delta G>0
$$

The total free energy decreases as the reaction proceeds spontaneously in the reverse direction.

Figure 17.10 shows how the total free energy of a reaction mixture changes as the reaction progresses. Because the free energy decreases as pure reactants form

products and also decreases as pure products form reactants, the free-energy curve must go through a minimum somewhere between pure reactants and pure products. At that minimum free-energy composition, the system is at equilibrium because conversion of either reactants to products or products to reactants would involve an increase in free energy. The equilibrium composition persists indefinitely unless the system is disturbed by an external influence.

The sign of $\Delta G$ for the reaction is the same as the sign of the slope of the freeenergy curve (Figure 17.10). To the left of the equilibrium composition, $\Delta G$ and the slope of the curve are negative and the free energy decreases as reactants are converted to products. To the right of the equilibrium composition, $\Delta G$ and the slope of the curve are positive. Exactly at the equilibrium composition, $\Delta G$ and the slope of the curve are zero, and no reaction occurs.

We can now derive a relationship between free energy and the equilibrium constant. At equilibrium, $\Delta G$ for a reaction is zero and the reaction quotient $Q$ equals the equilibrium constant $K$. Substituting $\Delta G=0$ and $Q=K$ into the equation

$$
\Delta G=\Delta G^{\circ}+R T \ln Q
$$

gives

$$
0=\Delta G^{\circ}+R T \ln K
$$

> At equilibrium $\Delta G\left(\right.$ but not $\left.\Delta G^{\circ}\right)=0$.


TABLE 17.4 Relationship Between the Standard Free-Energy Change and the Equilibrium Constant for a Reaction: $\Delta G^{\circ}=-R T \ln K$

| TABLE 17.4 | Relationship Between the Standard Free-Energy Change and the <br> Equilibrium Constant for a Reaction: $\Delta G^{\circ}=-R T \ln K$ |  |  |
| :--- | :--- | :--- | :--- |
| $\Delta \mathbf{G}^{\circ}$ | $\ln \boldsymbol{K}$ | $\boldsymbol{K}$ | Comment |
| $\Delta G^{\circ}<0$ | $\ln K>0$ | $K>1$ | The equilibrium mixture is mainly products. <br> $\Delta G^{\circ}>0$ |
| $\ln K<0$ | $K<1$ | The equilibrium mixture is mainly reactants. |  |
| $\Delta G^{\circ}=0$ | $\ln K=0$ | $K=1$ | The equilibrium mixture contains <br> comparable amounts of reactants and <br> products $(K=1$ for 1 M concentrations <br> and 1 atm partial pressures). | constant greater than 1 , which corresponds to a minimum in the free-energy curve of Figure 17.10 at a composition rich in products. Conversely, a reaction that has a positive value of $\Delta G^{\circ}$ has an equilibrium constant less than 1 and a minimum in the free-energy curve at a composition rich in reactants. Try redrawing Figure 17.10 for the case where $\Delta G^{\circ}>0$.

(Here, $K$ is $K_{\mathrm{p}}$ for reactions involving gases and $K_{\mathrm{c}}$ for reactions involving solutes in solution. For reactions involving both gases and solutes in solution, the equilibrium constant expression contains partial pressures of gases and molar concentrations of solutes.)

The equation $\Delta G^{\circ}=-R T \ln K$ is one of the most important relationships in chemical thermodynamics because it allows us to calculate the equilibrium constant for a reaction from the standard free-energy change, or vice versa. This relationship is especially useful when $K$ is difficult to measure. Consider a reaction so slow that it takes more than an experimenter's lifetime to reach equilibrium or a reaction that goes essentially to completion, so that the equilibrium concentrations of the reactants are extremely small and hard to measure. We can't measure $K$ directly in such cases, but we can calculate its value from $\Delta G^{\circ}$.

The relationship between $\Delta G^{\circ}$ and the equilibrium constant $K$ is summarized in Table 17.4. A reaction with a negative value of $\Delta G^{\circ}$ has an equilibrium

We have now answered the fundamental question posed at the beginning of this chapter: What determines the value of the equilibrium constant-that is, what properties of nature determine the direction and extent of a particular chemical reaction? The answer is that the value of the equilibrium constant is determined by the standard free-energy change, $\Delta G^{\circ}$, for the reaction, which depends, in turn, on the standard heats of formation and the standard molar entropies of the reactants and products.

## Worked Example 17.9

Methanol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$, an important alcohol used in the manufacture of adhesives, fibers, and plastics, is synthesized industrially by the reaction

$$
\mathrm{CO}(g)+2 \mathrm{H}_{2}(g) \rightleftharpoons \mathrm{CH}_{3} \mathrm{OH}(g)
$$

Use the thermodynamic data in Appendix B to calculate the equilibrium constant for this reaction at $25^{\circ} \mathrm{C}$.

## Strategy

First calculate $\Delta G^{\circ}$ for the reaction from the tabulated values of $\Delta G^{\circ}{ }_{f}$ for reactants and products. Then use the equation $\Delta G^{\circ}=-R T \ln K$ to find the value of the equilibrium constant.

## Solution

$$
\begin{aligned}
\Delta G^{\circ} & =\Delta G^{\circ}\left(\mathrm{CH}_{3} \mathrm{OH}\right)-\left[\Delta G_{\mathrm{f}}^{\circ}(\mathrm{CO})+2 \Delta G^{\circ}{ }_{\mathrm{f}}\left(\mathrm{H}_{2}\right)\right] \\
& =(1 \mathrm{~mol})(-161.9 \mathrm{~kJ} / \mathrm{mol})-[(1 \mathrm{~mol})(-137.2 \mathrm{~kJ} / \mathrm{mol})+(2 \mathrm{~mol})(0 \mathrm{~kJ} / \mathrm{mol})] \\
\Delta G^{\circ} & =-24.7 \mathrm{~kJ}
\end{aligned}
$$

Solving the equation

$$
\Delta G^{\circ}=-R T \ln K
$$


for $\ln K$ gives


$$
\ln K=\frac{-\Delta G^{\circ}}{R T}=\frac{-\left(-24.7 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right)}{[8.314 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})](298 \mathrm{~K})}=9.97
$$

Therefore,

$$
K=K_{\mathrm{p}}=\operatorname{antiln} 9.97=e^{9.97}=2.1 \times 10^{4}
$$

The equilibrium constant obtained by this procedure is $K_{p}$ because the reactants and products are gases and their standard states are defined in terms of pressure. If we want the value of $K_{c}$, we must calculate it from the relation $K_{p}=K_{c}(R T)^{\Delta n}$ (Section 13.3), where $R$ must be expressed in the proper units $[R=0.08206(\mathrm{~L} \cdot \mathrm{~atm}) /(\mathrm{K} \cdot \mathrm{mol})]$.
$\checkmark$ BALLPARK CHECK $\Delta G^{\circ}$ is negative, so the equilibrium mixture should be mainly products ( $K>1$ ), in agreement with the solution.

## Worked Example 17.10

The value of $\Delta G^{\circ}{ }_{\mathrm{f}}$ at $25^{\circ} \mathrm{C}$ for gaseous mercury is $31.85 \mathrm{~kJ} / \mathrm{mol}$. What is the vapor pressure of mercury at $25^{\circ} \mathrm{C}$ ?

## Strategy

The vapor pressure (in atm) equals $K_{p}$ for the reaction

$$
\mathrm{Hg}(l) \rightleftharpoons \mathrm{Hg}(g) \quad K_{\mathrm{p}}=P_{\mathrm{Hg}}
$$

$\mathrm{Hg}(l)$ is omitted from the equilibrium constant expression because it is a pure liquid. Because the standard state for elemental mercury is the pure liquid, $\Delta G^{\circ}{ }_{\mathrm{f}}=0$ for $\operatorname{Hg}(l)$, and $\Delta G^{\circ}$ for the vaporization reaction simply equals $\Delta G^{\circ}{ }_{f}$ for $\operatorname{Hg}(g)$ (31.85 $\mathrm{kJ} / \mathrm{mol}$ ). We can calculate $K_{\mathrm{p}}$ from the equation $\Delta G^{\circ}=-R T \ln K_{\mathrm{p}}$, as in Worked Example 17.9.

## Solution

$$
\begin{aligned}
& \ln K_{\mathrm{p}}=\frac{-\Delta G^{\circ}}{R T}=\frac{-\left(31.85 \times 10^{3} \mathrm{~J} / \mathrm{mol}\right)}{[8.314 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})](298 \mathrm{~K})}=-12.86 \\
& K_{\mathrm{p}}=\operatorname{antiln}(-12.86)=e^{-12.86}=2.6 \times 10^{-6}
\end{aligned}
$$

Since $K_{\mathrm{p}}$ is defined in units of atmospheres, the vapor pressure of mercury at $25^{\circ} \mathrm{C}$ is $2.6 \times 10^{-6} \mathrm{~atm}(0.0020 \mathrm{~mm} \mathrm{Hg})$. Because the vapor pressure is appreciable and mercury is toxic in the lungs, mercury should not be handled without adequate ventilation.

BALLPARK CHECK $\Delta G^{\circ}$ is positive, so the vaporization reaction should not proceed very far before reaching equilibrium. Thus, $K_{\mathrm{p}}$ should be less than 1 , in agreement with the solution.


- Mercury has an appreciable vapor pressure at room temperature, and its handling requires adequate ventilation.


## Worked Example 17.11

At $25^{\circ} \mathrm{C}, K_{\text {sp }}$ for $\mathrm{PbCrO}_{4}$ is $2.8 \times 10^{-13}$. Calculate the standard free-energy change at $25^{\circ} \mathrm{C}$ for the reaction $\mathrm{PbCrO}_{4}(s) \rightleftharpoons \mathrm{Pb}^{2+}(a q)+\mathrm{CrO}_{4}{ }^{2-}(a q)$.

## Strategy and Solution

We can calculate $\Delta G^{\circ}$ directly from the equilibrium constant $K_{\text {sp }}$ :

$$
\begin{aligned}
\Delta G^{\circ} & =-R T \ln K_{\mathrm{sp}}=-[8.314 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{~mol})](298 \mathrm{~K})\left(\ln 2.8 \times 10^{-13}\right) \\
& =71.6 \times 10^{3} \mathrm{~J} / \mathrm{mol}=71.6 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

$\checkmark$ BALLPARK CHECK The $K_{\text {sp }}$ value is much less than 1 , so $\Delta G^{\circ}$ should be a large positive number, in agreement with the solution.

- PROBLEM 17.15 Given the data in Appendix B, calculate $K_{\mathrm{p}}$ at $25^{\circ} \mathrm{C}$ for the reaction $\mathrm{CaCO}_{3}(s) \rightleftharpoons \mathrm{CaO}(s)+\mathrm{CO}_{2}(g)$.
- PROBLEM 17.16 Use the data in Appendix B to calculate the vapor pressure of water at $25^{\circ} \mathrm{C}$.
- PROBLEM 17.17 At $25^{\circ} \mathrm{C}, \mathrm{K}_{\mathrm{w}}$ for the dissociation of water is $1.0 \times 10^{-14}$. Calculate $\Delta G^{\circ}$ for the reaction $2 \mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q)$.


## Interlude Some Random Thoughts About Entropy

 by other physical quantities.

Biologists, too, have been intrigued by entropy and its consequences. Their problem is that if the disorder of the universe is always increasing, how is it possible for enormously complex and increasingly sophisticated life forms to evolve? After all, the more complex the organism, the greater the amount of order required and the lower the entropy. The answer to the biologists' question again arises from the second law of thermodynamics: All spontaneous processes increase the disorder of the universe-that is, the total disorder of both system and surroundings. It's perfectly possible, however, for the disorder of any system to decrease spontaneously as long as the disorder of the surroundings increases by an even greater amount.

The energy used to power all living organisms on Earth comes from sunlight, caused ultimately by nuclear reactions in the sun. Photosynthetic cells in plants use the sun's energy to make glucose, which is then used by animals as their primary source of energy. The energy an animal obtains from glucose is then used to build and organize complex molecules, resulting in a decrease in entropy for the animal. At the same time, however, the entropy of the surroundings increases as the animal releases small, simple waste products such as $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$. Furthermore, heat is released by the animal, further increasing the entropy of the surroundings. Thus, an organism pays for its decrease in entropy by increasing the entropy of the rest of the universe.


A Plants capture solar energy and convert it to chemical potential energy by using it to make energy-rich molecules such as glucose. Animals tap this energy by eating plants (or other animals that have eaten plants) and use it to build even more complex molecular structures. These processes decrease entropy locally, but produce a net increase in the entropy of the universe as a whole.

- PROBLEM 17.18 Consider the growth of a human adult from a single cell. Does this process violate the second law of thermodynamics? Explain.
- PROBLEM 17.19 If you watched a movie run backwards, would you expect to see violations of the second law? Explain.

Summary

Thermodynamics deals with the interconversion of heat and other forms of energy and allows us to predict the direction and extent of chemical reactions and other spontaneous processes. A spontaneous process proceeds on its own without any external influence. All spontaneous reactions move toward equilibrium.

Entropy, denoted by $S$, is a state function that measures molecular disorder, or randomness. The entropy of a system (reactants plus products) increases ( $\Delta S$ is positive) for the following processes: phase transitions that convert a solid to a liquid or a liquid to a gas; reactions that increase the number of gaseous molecules; dissolution of molecular solids and certain salts in water; raising the temperature of a substance; expansion of a gas at constant temperature.

A disordered state of a system (state of high entropy) can be achieved in more ways ( $W$ ) than an ordered state and is therefore more probable. The entropy of a state can be calculated from Boltzmann's formula, $S=k \ln W$. According to the third law of thermodynamics, the entropy of a pure, perfectly ordered crystalline substance at 0 K is zero.

The standard molar entropy, $S^{\circ}$, of a substance is the absolute entropy of 1 mol of the pure substance at 1 atm pressure and a specified temperature, usually $25^{\circ} \mathrm{C}$. The standard entropy of reaction, $\Delta S^{\circ}$, can be calculated from the relation $\Delta S^{\circ}=S^{\circ}$ (products) $-S^{\circ}$ (reactants) .

The first law of thermodynamics states that in any process, the total energy of a system and its surroundings remains constant. The second law of thermodynamics says that in any spontaneous process, the total entropy of a system and its surroundings $\left(\Delta S_{\text {total }}=\Delta S_{\text {sys }}+\Delta S_{\text {surr }}\right)$ always
increases. A chemical reaction is spontaneous if $\Delta S_{\text {total }}>0$, nonspontaneous if $\Delta S_{\text {total }}<0$, and at equilibrium if $\Delta S_{\text {total }}=0$. Reactions that are nonspontaneous in the forward direction are spontaneous in the reverse direction. For a reaction at constant pressure, $\Delta S_{\text {surr }}=-\Delta H / T$, and $\Delta S_{\text {sys }}$ is $\Delta S^{\circ}$ for the reaction.

Free energy, $G=H-T S$, is a state function that indicates whether a reaction is spontaneous or nonspontaneous. A reaction at constant temperature and pressure is spontaneous if $\Delta G<0$, nonspontaneous if $\Delta G>0$, and at equilibrium if $\Delta G=0$. In the equation $\Delta G=\Delta H-T \Delta S$, temperature is a weighting factor that determines the relative importance of the enthalpy and entropy contributions to $\Delta G$.

The standard free-energy change, $\Delta G^{\circ}$, for a reaction is the change in free energy that occurs when reactants in their standard states are converted to products in their standard states. The standard free energy of formation, $\Delta G^{\circ}{ }_{f}$, of a substance is the free-energy change for formation of one mole of the substance in its standard state from the most stable form of the constituent elements in their standard states. Substances with a negative value of $\Delta G^{\circ}{ }_{f}$ are thermodynamically stable with respect to the constituent elements. We can calculate $\Delta G^{\circ}$ for a reaction in either of two ways: (1) $\Delta G^{\circ}=\Delta G^{\circ}{ }_{\mathrm{f}}$ (products) $-\Delta G^{\circ}{ }_{\mathrm{f}}($ reactants $)$ or (2) $\Delta G^{\circ}=\Delta H^{\circ}-T \Delta S^{\circ}$.

The free-energy change, $\Delta G$, for a reaction under non-standard-state conditions is given by $\Delta G=\Delta G^{\circ}+R T \ln Q$, where $Q$ is the reaction quotient. At equilibrium, $\Delta G=0$ and $Q=K$. As a result, $\Delta G^{\circ}=-R T \ln K$, which allows us to calculate the equilibrium constant from $\Delta G^{\circ}$ and vice versa.

## Key Words

| entropy $(S)$ | 724 |
| :---: | :---: |
| first law of | spontaneous process |
| thermodynamics | 733 | | 722 |
| :---: |
| standard entropy of |
| free energy $(G) \quad 735$ |
| second law of |
| thermodynamics |$\quad 733 \quad$| reaction $\left(\Delta S^{\circ}\right) \quad 731$ |
| :---: |
| standard free-energy |
| change $\left(\Delta G^{\circ}\right) \quad 738$ |

entropy (S) 724
thermodynamics 733
free energy ( $G$ ) 735
second law of
thermodynamics 733
spontaneous process
standard entropy of reaction ( $\Delta \boldsymbol{S}^{\circ}$ ) 731 change ( $\Delta G^{\circ}$ ) 738
standard free energy of
formation ( $\Delta G^{\circ}{ }_{f}$ ) 741
standard molar entropy
( $S^{\circ}$ ) 731
standard-state
conditions 738
thermodynamics 722
third law of thermodynamics 729

## Key Concept Summary



## Understanding Key Concepts

Problems 17.1-17.19 appear within the chapter.
17.20 Ideal gases A (red spheres) and B (blue spheres) occupy two separate bulbs. The contents of both bulbs constitute the initial state of an isolated system. Consider the process that occurs when the stopcock is opened.

(a) Sketch the final (equilibrium) state of the system.
(b) What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ for this process? Explain.
(c) How does this process illustrate the second law of thermodynamics?
(d) Is the reverse process spontaneous or nonspontaneous? Explain.
17.21 What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ for the spontaneous sublimation of a crystalline solid? Explain.

17.22 What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ for the spontaneous condensation of a vapor to a liquid? Explain.

17.23 An ideal gas is compressed at constant temperature. What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ for the process? Explain.

17.24 Consider the following spontaneous reaction of $\mathrm{A}_{2}$ molecules (red) and $\mathrm{B}_{2}$ molecules (blue):

(a) Write a balanced equation for the reaction.
(b) What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ for the reaction? Explain.
17.25 Consider the dissociation reaction $\mathrm{A}_{2}(g) \rightleftharpoons 2 \mathrm{~A}(g)$. The following pictures represent two possible initial states and the equilibrium state of the system:


Equilibrium state
(a) Is the reaction quotient $Q_{p}$ for initial state 1 greater than, less than, or equal to the equilibrium constant $K_{\mathrm{p}}$ ? Is $Q_{\mathrm{p}}$ for initial state 2 greater than, less than, or equal to $K_{p}$ ?
(b) What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ when the system goes from initial state 1 to the equilibrium state? Explain. Is this a spontaneous process?
(c) What are the signs $(+,-$, or 0$)$ of $\Delta H, \Delta S$, and $\Delta G$ when the system goes from initial state 2 to the equilibrium state? Explain. Is this a spontaneous process?
(d) Relate each of the pictures to the graph in Figure 17.10.
17.26 Consider again the dissociation reaction $\mathrm{A}_{2}(g) \rightleftharpoons$ $2 \mathrm{~A}(g)$ (Problem 17.25).
(a) What are the signs $(+,-$, or 0$)$ of the standard enthalpy change, $\Delta H^{\circ}$, and the standard entropy change, $\Delta S^{\circ}$, for the forward reaction?
(b) Distinguish between the meaning of $\Delta S^{\circ}$ for the dissociation reaction and $\Delta S$ for the process in which the system goes from initial state 1 to the equilibrium state (pictured in Problem 17.25).
(c) Can you say anything about the sign of $\Delta G^{\circ}$ for the dissociation reaction? How does $\Delta G^{\circ}$ depend on temperature? Will $\Delta G^{\circ}$ increase, decrease, or remain the same if the temperature increases?
(d) Will the equilibrium constant $K_{\mathrm{p}}$ increase, decrease, or remain the same if the temperature increases? How will the picture for the equilibrium state (Problem 17.25) change if the temperature increases?
(e) What is the value of $\Delta G$ for the dissociation reaction when the system is at equilibrium?
17.27 Consider the following graph of the total free energy of reactants and products versus reaction progress for a general reaction, Reactants $\rightarrow$ Products:

(a) Account for the shape of the curve, and identify the point at which $\Delta G=0$. What is the significance of that point?
(b) Why is the minimum in the plot on the left side of the graph?
17.28 The following pictures represent equilibrium mixtures for the interconversion of A molecules (red) and X, Y, or Z molecules (blue):


What is the sign of $\Delta G^{\circ}$ for each of the three reactions?
17.29 The following pictures represent the composition of the equilibrium mixture at $25^{\circ} \mathrm{C}$ and $45^{\circ} \mathrm{C}$ for the reaction $A \rightleftharpoons B$, where $A$ molecules are represented by red spheres, and B molecules, by blue spheres.

$T=25^{\circ} \mathrm{C}$


$$
T=45^{\circ} \mathrm{C}
$$

What are the signs of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for the forward reaction $\mathrm{A} \rightarrow \mathrm{B}$ ? Explain. (You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.)

## Additional Problems

## Spontaneous Processes

17.30 Distinguish between a spontaneous process and a nonspontaneous process and give an example of each.
17.31 The decomposition of hydrogen peroxide to gaseous $\mathrm{O}_{2}$ and water is a spontaneous process, yet $\mathrm{H}_{2} \mathrm{O}_{2}$ is stable for long periods of time. Explain.
17.32 Which of the following processes are spontaneous, and which are nonspontaneous?
(a) Freezing of water at $2^{\circ} \mathrm{C}$
(b) Corrosion of iron metal
(c) Expansion of a gas to fill the available volume
(d) Separation of an unsaturated aqueous solution of potassium chloride into solid KCl and liquid water
17.33 Tell whether the following processes are spontaneous or nonspontaneous:
(a) Dissolving sugar in hot coffee
(b) Decomposition of NaCl to solid sodium and gaseous chlorine at $25^{\circ} \mathrm{C}$ and 1 atm pressure
(c) Uniform mixing of bromine vapor and nitrogen gas
(d) Boiling of gasoline at $25^{\circ} \mathrm{C}$ and 1 atm pressure
17.34 Assuming that gaseous reactants and products are present at 1 atm partial pressure, which of the following reactions are spontaneous in the forward direction?
(a) $\mathrm{N}_{2}(g)+2 \mathrm{H}_{2}(g) \rightarrow \mathrm{N}_{2} \mathrm{H}_{4}(l) ; K_{\mathrm{p}}=7 \times 10^{-27}$
(b) $2 \mathrm{Mg}(s)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{MgO}(s) ; K_{\mathrm{p}}=2 \times 10^{198}$
(c) $\mathrm{MgCO}_{3}(s) \rightarrow \mathrm{MgO}(s)+\mathrm{CO}_{2}(g) ; K_{\mathrm{p}}=9 \times 10^{-10}$
(d) $2 \mathrm{CO}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{CO}_{2}(g) ; K_{\mathrm{p}}=1 \times 10^{90}$
17.35 Assuming that dissolved reactants and products are present at 1 M concentrations, which of the following reactions are nonspontaneous in the forward direction?
(a) $\mathrm{HCN}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CN}^{-}(a q)$;

$$
K=4.9 \times 10^{-10}
$$

(b) $\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)$;

$$
K=1.0 \times 10^{14}
$$

(c) $\mathrm{Ba}^{2+}(a q)+\mathrm{CO}_{3}{ }^{2-}(a q) \rightarrow \mathrm{BaCO}_{3}(s)$;

$$
K=3.8 \times 10^{8}
$$

(d) $\mathrm{AgCl}(s) \rightarrow \mathrm{Ag}^{+}(a q)+\mathrm{Cl}^{-}(a q) ; K=1.8 \times 10^{-10}$

## Entropy

17.36 Define entropy and give an example of a process in which the entropy of a system increases.
17.37 Comment on the following statement: Exothermic reactions are spontaneous, but endothermic reactions are nonspontaneous.
17.38 Predict the sign of the entropy change in the system for each of the following processes:
(a) A solid sublimes
(b) A liquid freezes
(c) AgI precipitates from a solution containing $\mathrm{Ag}^{+}$ and $\mathrm{I}^{-}$ions
(d) Gaseous $\mathrm{CO}_{2}$ bubbles out of a carbonated beverage
17.39 Predict the sign of $\Delta S$ in the system for each of the following reactions:
(a) $\mathrm{PCl}_{5}(s) \rightarrow \mathrm{PCl}_{3}(l)+\mathrm{Cl}_{2}(g)$
(b) $\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \rightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)$
(c) $2 \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CO}_{3}{ }^{2-}(a q) \rightarrow \mathrm{CO}_{2}(g)+3 \mathrm{H}_{2} \mathrm{O}(l)$
(d) $\mathrm{Mg}(\mathrm{s})+\mathrm{Cl}_{2}(g) \rightarrow \mathrm{MgCl}_{2}(s)$
17.40 Predict the sign of $\Delta S$ for each process in Problem 17.32.
17.41 Predict the sign of $\Delta S$ for each process in Problem 17.33.
17.42 Consider a disordered crystal of monodeuteriomethane in which each tetrahedral $\mathrm{CH}_{3} \mathrm{D}$ molecule is oriented randomly in one of four possible ways. Use Boltzmann's formula to calculate the entropy of the disordered state of the crystal if the crystal contains:
(a) 12 molecules
(b) 120 molecules
(c) 1 mol of molecules

What is the entropy of the crystal if the $\mathrm{C}-\mathrm{D}$ bond of each of the $\mathrm{CH}_{3} \mathrm{D}$ molecules points in the same direction?
17.43 Consider the distribution of ideal gas molecules among three bulbs (A, B, and C) of equal volume. For each of the following states, determine the number of ways ( $W$ ) that the state can be achieved, and use Boltzmann's formula to calculate the entropy of the state:
(a) 2 molecules in bulb A
(b) 2 molecules randomly distributed among bulbs A , $B$, and C
(c) 3 molecules in bulb A
(d) 3 molecules randomly distributed among bulbs A , $B$, and C
(e) 1 mol of molecules in bulb A
(f) 1 mol of molecules randomly distributed among bulbs A, B, and C
What is $\Delta S$ on going from state (e) to state (f)? Compare your result with $\Delta S$ calculated from the equation $\Delta S=R \ln \left(V_{\text {final }} / V_{\text {initial }}\right)$.
17.44 Which state in each of the following pairs has the higher entropy per mole of substance?
(a) $\mathrm{H}_{2}$ at $25^{\circ} \mathrm{C}$ in a volume of 10 L or $\mathrm{H}_{2}$ at $25^{\circ} \mathrm{C}$ in a volume of 50 L
(b) $\mathrm{O}_{2}$ at $25^{\circ} \mathrm{C}$ and 1 atm or $\mathrm{O}_{2}$ at $25^{\circ} \mathrm{C}$ and 10 atm
(c) $\mathrm{H}_{2}$ at $25^{\circ} \mathrm{C}$ and 1 atm or $\mathrm{H}_{2}$ at $100^{\circ} \mathrm{C}$ and 1 atm
(d) $\mathrm{CO}_{2}$ at STP or $\mathrm{CO}_{2}$ at $100^{\circ} \mathrm{C}$ and 0.1 atm
17.45 Which state in each of the following pairs has the higher entropy per mole of substance?
(a) Ice at $-40^{\circ} \mathrm{C}$ or ice at $0^{\circ} \mathrm{C}$
(b) $\mathrm{N}_{2}$ at STP or $\mathrm{N}_{2}$ at $0^{\circ} \mathrm{C}$ and 10 atm
(c) $\mathrm{N}_{2}$ at STP or $\mathrm{N}_{2}$ at $0^{\circ} \mathrm{C}$ in a volume of 50 L
(d) Water vapor at $150^{\circ} \mathrm{C}$ and 1 atm or water vapor at $100^{\circ} \mathrm{C}$ and 2 atm

## Standard Molar Entropies and Standard Entropies of Reaction

17.46 What is meant by the standard molar entropy of a substance? How are standard molar entropies used to calculate standard entropies of reaction?
17.47 What are the units of (a)standard molar entropies and (b) standard entropies of reaction? Why are standard molar entropies sometimes called absolute entropies?
17.48 Which substance in each of the following pairs would you expect to have the higher standard molar entropy? Explain.
(a) $\mathrm{C}_{2} \mathrm{H}_{2}(g)$ or $\mathrm{C}_{2} \mathrm{H}_{6}(g)$
(b) $\mathrm{CO}_{2}(g)$ or $\mathrm{CO}(g)$
(c) $\mathrm{I}_{2}(\mathrm{~s})$ or $\mathrm{I}_{2}(g)$
(d) $\mathrm{CH}_{3} \mathrm{OH}(g)$ or $\mathrm{CH}_{3} \mathrm{OH}(l)$
17.49 Which substance in each of the following pairs would you expect to have the higher standard molar entropy? Explain.
(a) $\mathrm{NO}(g)$ or $\mathrm{NO}_{2}(g)$
(b) $\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(l)$ or $\mathrm{HCO}_{2} \mathrm{H}(l)$
(c) $\mathrm{Br}_{2}(l)$ or $\mathrm{Br}_{2}(\mathrm{~s})$
(d) $\mathrm{S}(\mathrm{s})$ or $\mathrm{SO}_{3}(g)$
17.50 Use the standard molar entropies in Appendix B to calculate $\Delta S^{\circ}$ at $25^{\circ} \mathrm{C}$ for each of the following reactions. Account for the sign of the entropy change in each case.
(a) $2 \mathrm{H}_{2} \mathrm{O}_{2}(l) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g)$
(b) $2 \mathrm{Na}(s)+\mathrm{Cl}_{2}(g) \rightarrow 2 \mathrm{NaCl}(s)$
(c) $2 \mathrm{O}_{3}(\mathrm{~g}) \rightarrow 3 \mathrm{O}_{2}(\mathrm{~g})$
(d) $4 \mathrm{Al}(s)+3 \mathrm{O}_{2}(g) \rightarrow 2 \mathrm{Al}_{2} \mathrm{O}_{3}(s)$
17.51 Use the $S^{\circ}$ values in Appendix B to calculate $\Delta S^{\circ}$ at $25^{\circ} \mathrm{C}$ for each of the following reactions. Suggest a reason for the sign of $\Delta S^{\circ}$ in each case.
(a) $2 \mathrm{~S}(s)+3 \mathrm{O}_{2}(g) \rightarrow 2 \mathrm{SO}_{3}(g)$
(b) $\mathrm{SO}_{3}(g)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow \mathrm{H}_{2} \mathrm{SO}_{4}(a q)$
(c) $\mathrm{AgCl}(s) \rightarrow \mathrm{Ag}^{+}(a q)+\mathrm{Cl}^{-}(a q)$
(d) $\mathrm{NH}_{4} \mathrm{NO}_{3}(s) \rightarrow \mathrm{N}_{2} \mathrm{O}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)$

## Entropy and the Second Law of Thermodynamics

17.52 State the second law of thermodynamics.
17.53 An isolated system is one that exchanges neither matter nor energy with the surroundings. What is the entropy criterion for spontaneous change in an isolated system? Give an example of a spontaneous process in an isolated system.
17.54 Give an equation that relates the entropy change in the surroundings to the enthalpy change in the system. What is the sign of $\Delta S_{\text {surr }}$ for the following?
(a) An exothermic reaction
(b) An endothermic reaction
17.55 When heat is added to the surroundings, the entropy of the surroundings increases. How does $\Delta S_{\text {surr }}$ depend on the temperature of the surroundings? Explain.
17.56 Use the data in Appendix B to calculate $\Delta S_{\text {sys }}, \Delta S_{\text {surr }}$ and $\Delta S_{\text {total }}$ at $25^{\circ} \mathrm{C}$ for the reaction

$$
\mathrm{N}_{2}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{N}_{2} \mathrm{O}_{4}(g)
$$

Is this reaction spontaneous under standard-state conditions at $25^{\circ} \mathrm{C}$ ?
17.57 Copper metal is obtained by smelting copper(I) sulfide ores:

$$
\mathrm{Cu}_{2} \mathrm{~S}(s)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{Cu}(s)+\mathrm{SO}_{2}(g)
$$

Use the data in Appendix B to calculate $\Delta S_{\text {sys }}, \Delta S_{\text {surr }}$, and $\Delta S_{\text {total }}$ at $25^{\circ} \mathrm{C}$ for this reaction. Is the reaction spontaneous under standard-state conditions at $25^{\circ} \mathrm{C}$ ?
17.58 For the vaporization of benzene, $\Delta H_{\text {vap }}=30.7 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S_{\text {vap }}=87.0 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. Calculate $\Delta S_{\text {surr }}$ and $\Delta S_{\text {total }}$ at:
(a) $70^{\circ} \mathrm{C}$
(b) $80^{\circ} \mathrm{C}$
(c) $90^{\circ} \mathrm{C}$

Does benzene boil at $70^{\circ} \mathrm{C}$ and 1 atm pressure? Calculate the normal boiling point of benzene.
17.59 For the melting of sodium chloride, $\Delta H_{\text {fusion }}=$ $30.2 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S_{\text {fusion }}=28.1 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. Calculate $\Delta S_{\text {surr }}$ and $\Delta S_{\text {total }}$ at:
(a) 1050 K
(b) 1075 K
(c) 1100 K

Does NaCl melt at 1100 K ? Calculate the melting point of NaCl .

## Free Energy

17.60 Describe how the signs of $\Delta H$ and $\Delta S$ determine whether a reaction is spontaneous or nonspontaneous at constant temperature and pressure.
17.61 What determines the direction of spontaneous reaction when $\Delta H$ and $\Delta S$ are both positive or both negative? Explain.
17.62 The melting point of benzene is $5.5^{\circ} \mathrm{C}$. Predict the signs of $\Delta H, \Delta S$, and $\Delta G$ for melting of benzene at:
(a) $0^{\circ} \mathrm{C}$
(b) $15^{\circ} \mathrm{C}$
17.63 Consider a twofold expansion of an ideal gas at $25^{\circ} \mathrm{C}$ in the isolated system shown in Figure 17.1.
(a) What are the values of $\Delta H, \Delta S$, and $\Delta G$ for the process?
(b) How does this process illustrate the second law of thermodynamics?
17.64 Given the data in Problem 17.58, calculate $\Delta G$ for the vaporization of benzene at:
(a) $70^{\circ} \mathrm{C}$
(b) $80^{\circ} \mathrm{C}$
(c) $90^{\circ} \mathrm{C}$

Predict whether benzene will boil at each of these temperatures and 1 atm pressure.
17.65 Given the data in Problem 17.59, calculate $\Delta G$ for the melting of sodium chloride at:
(a) 1050 K
(b) 1075 K
(c) 1100 K

Predict whether NaCl will melt at each of these temperatures and 1 atm pressure.
17.66 Calculate the melting point of benzoic acid $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right)$, given the following data: $\Delta H_{\text {fusion }}=$ $17.3 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S_{\text {fusion }}=43.8 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$.
17.67 Calculate the enthalpy of fusion of naphthalene $\left(\mathrm{C}_{10} \mathrm{H}_{8}\right)$, given that its melting point is $128^{\circ} \mathrm{C}$ and its entropy of fusion is $47.7 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$.

## Standard Free-Energy Changes and Standard Free Energies of Formation

17.68 Define (a) the standard free-energy change, $\Delta G^{\circ}$, for a reaction and (b) the standard free energy of formation, $\Delta G^{\circ}{ }_{\mathrm{f}}$, of a substance.
17.69 What is meant by the standard state of a substance?
17.70 Use the data in Appendix B to calculate $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for each of the following reactions. From the values of $\Delta H^{\circ}$ and $\Delta S^{\circ}$, calculate $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$, and predict whether each reaction is spontaneous under standard-state conditions.
(a) $\mathrm{N}_{2}(g)+2 \mathrm{O}_{2}(g) \rightarrow 2 \mathrm{NO}_{2}(g)$
(b) $2 \mathrm{KClO}_{3}(s) \rightarrow 2 \mathrm{KCl}(s)+3 \mathrm{O}_{2}(g)$
(c) $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(l)+\mathrm{O}_{2}(g) \rightarrow$

$$
\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(l)+\mathrm{H}_{2} \mathrm{O}(l)
$$

17.71 Use the data in Appendix B to calculate $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for each of the following reactions. From the values of $\Delta H^{\circ}$ and $\Delta S^{\circ}$, calculate $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$ and predict whether each reaction is spontaneous under standardstate conditions.
(a) $2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{SO}_{3}(g)$
(b) $\mathrm{N}_{2}(g)+2 \mathrm{H}_{2}(g) \rightarrow \mathrm{N}_{2} \mathrm{H}_{4}(l)$
(c) $\mathrm{CH}_{3} \mathrm{OH}(l)+\mathrm{O}_{2}(g) \rightarrow \mathrm{HCO}_{2} \mathrm{H}(l)+\mathrm{H}_{2} \mathrm{O}(l)$
17.72 Use the standard free energies of formation in Appendix B to calculate $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$ for each reaction in Problem 17.70.
17.73 Use the standard free energies of formation in Appendix B to calculate $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$ for each reaction in Problem 17.71.
17.74 Use the data in Appendix B to tell which of the following compounds are thermodynamically stable with respect to their constituent elements at $25^{\circ} \mathrm{C}$ :
(a) $\mathrm{BaCO}_{3}(s)$
(b) $\mathrm{HBr}(g)$
(c) $\mathrm{N}_{2} \mathrm{O}(g)$
(d) $\mathrm{C}_{2} \mathrm{H}_{4}(g)$
17.75 Use the data in Appendix B to decide whether synthesis of the following compounds from their constituent elements is thermodynamically feasible at $25^{\circ} \mathrm{C}$ :
(a) $\mathrm{C}_{6} \mathrm{H}_{6}(l)$
(b) $\mathrm{NO}(g)$
(c) $\mathrm{PH}_{3}(g)$
(d) $\mathrm{FeO}(\mathrm{s})$
17.76 Ethanol is manufactured in industry by the hydration of ethylene:

$$
\mathrm{CH}_{2}=\mathrm{CH}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(l)
$$

Using the data in Appendix $B$, calculate $\Delta G^{\circ}$ and show that this reaction is spontaneous at $25^{\circ} \mathrm{C}$. Why does this reaction become nonspontaneous at higher temperatures? Estimate the temperature at which the reaction becomes nonspontaneous.
17.77 Sulfur dioxide in the effluent gases from coal-burning electric power plants is one of the principal causes of acid rain. One method for reducing $\mathrm{SO}_{2}$ emissions involves partial reduction of $\mathrm{SO}_{2}$ to $\mathrm{H}_{2} \mathrm{~S}$, followed by catalytic conversion of the $\mathrm{H}_{2} \mathrm{~S}$ and the remaining $\mathrm{SO}_{2}$ to elemental sulfur:

$$
2 \mathrm{H}_{2} \mathrm{~S}(g)+\mathrm{SO}_{2}(g) \longrightarrow 3 \mathrm{~S}(s)+2 \mathrm{H}_{2} \mathrm{O}(g)
$$

Using the data in Appendix B, calculate $\Delta G^{\circ}$ and show that this reaction is spontaneous at $25^{\circ} \mathrm{C}$. Why does this reaction become nonspontaneous at high temperatures? Estimate the temperature at which the reaction becomes nonspontaneous.
17.78 Consider the conversion of acetylene to benzene:

$$
3 \mathrm{C}_{2} \mathrm{H}_{2}(g) \longrightarrow \mathrm{C}_{6} \mathrm{H}_{6}(l)
$$

Is a catalyst for this reaction possible? Is it possible to synthesize benzene from graphite and gaseous $\mathrm{H}_{2}$ at $25^{\circ} \mathrm{C}$ and 1 atm pressure?
17.79 Consider the conversion of dichloroethane to vinyl chloride, the starting material for manufacturing poly(vinyl chloride) (PVC) plastics:

$$
\underset{\text { Dichloroethane }}{\mathrm{CH}_{2} \mathrm{ClCH}_{2} \mathrm{Cl}(l)} \longrightarrow \underset{\text { Vinyl chloride }}{\mathrm{CH}_{2}}=\mathrm{CHCl}(g)+\mathrm{HCl}(g)
$$

Is this reaction spontaneous under standard-state conditions? Would it help to carry out the reaction in the presence of base to remove HCl ? Explain. Is it possible to synthesize vinyl chloride from graphite, gaseous $\mathrm{H}_{2}$, and gaseous $\mathrm{Cl}_{2}$ at $25^{\circ} \mathrm{C}$ and 1 atm pressure?

## Free Energy, Composition, and Chemical Equilibrium

17.80 What is the relationship between the free-energy change under nonstandard-state conditions, $\Delta G$, the free-energy change under standard-state conditions, $\Delta G^{\circ}$, and the reaction quotient, $Q$ ?
17.81 Compare the values of $\Delta G$ and $\Delta G^{\circ}$ when:
(a) $Q<1$
(b) $Q=1$
(c) $Q>1$

Does the thermodynamic driving force increase or decrease as $Q$ increases?
17.82 Sulfuric acid is produced in larger amounts by weight than any other chemical. It is used in manufacturing fertilizers, oil refining, and hundreds of other processes. An intermediate step in the industrial process for the synthesis of $\mathrm{H}_{2} \mathrm{SO}_{4}$ is the catalytic oxidation of sulfur dioxide:
$2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{SO}_{3}(g) \quad \Delta G^{\circ}=-141.8 \mathrm{~kJ}$
Calculate $\Delta G$ at $25^{\circ} \mathrm{C}$ given the following sets of partial pressures:
(a) $100 \mathrm{~atm} \mathrm{SO}_{2}, 100 \mathrm{~atm} \mathrm{O}_{2}, 1.0 \mathrm{~atm} \mathrm{SO}_{3}$
(b) $2.0 \mathrm{~atm} \mathrm{SO}_{2}, 1.0 \mathrm{~atm} \mathrm{O}_{2}, 10 \mathrm{~atm} \mathrm{SO}_{3}$
(c) Each reactant and product at a partial pressure of 1.0 atm
17.83 Urea $\left(\mathrm{NH}_{2} \mathrm{CONH}_{2}\right)$, an important nitrogen fertilizer, is produced industrially by the reaction

$$
2 \mathrm{NH}_{3}(g)+\mathrm{CO}_{2}(g) \longrightarrow \mathrm{NH}_{2} \mathrm{CONH}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Given that $\Delta G^{\circ}=-13.6 \mathrm{~kJ}$, calculate $\Delta G$ at $25^{\circ} \mathrm{C}$ for the following sets of conditions:
(a) $10 \mathrm{~atm} \mathrm{NH}_{3}, 10 \mathrm{~atm} \mathrm{CO}_{2}, 1.0 \mathrm{M} \mathrm{NH}_{2} \mathrm{CONH}_{2}$
(b) $0.10 \mathrm{~atm} \mathrm{NH}_{3}, 0.10 \mathrm{~atm} \mathrm{CO}_{2}, 1.0 \mathrm{M} \mathrm{NH}_{2} \mathrm{CONH}_{2}$

Is the reaction spontaneous for the conditions in part (a) and/or part (b)?
17.84 What is the relationship between the standard freeenergy change, $\Delta G^{\circ}$, for a reaction and the equilibrium constant, $K$ ? What is the sign of $\Delta G^{\circ}$ when:
(a) $K>1$
(b) $K=1$
(c) $K<1$
17.85 Do you expect a large or small value of the equilibrium constant for a reaction with the following values of $\Delta G^{\circ}$ ?
(a) $\Delta G^{\circ}$ is positive.
(b) $\Delta G^{\circ}$ is negative.
17.86 Calculate the equilibrium constant $K_{\mathrm{p}}$ at $25^{\circ} \mathrm{C}$ for the reaction in Problem 17.82.
17.87 Calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for the reaction in Problem 17.83.
17.88 Given values of $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$ for liquid ethanol $(-174.9 \mathrm{~kJ} / \mathrm{mol})$ and gaseous ethanol ( $-168.6 \mathrm{~kJ} / \mathrm{mol}$ ), calculate the vapor pressure of ethanol at $25^{\circ} \mathrm{C}$.
17.89 At $25^{\circ} \mathrm{C}$, $\mathrm{K}_{\mathrm{a}}$ for acid dissociation of aspirin $\left(\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}_{4}\right)$ is $3.0 \times 10^{-4}$. Calculate $\Delta G^{\circ}$ for the reaction $\mathrm{C}_{9} \mathrm{H}_{8} \mathrm{O}_{4}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{C}_{9} \mathrm{H}_{7} \mathrm{O}_{4}{ }^{-}(a q)$
17.90 Ethylene oxide, $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}$, is used to make antifreeze (ethylene glycol, $\mathrm{HOCH}_{2} \mathrm{CH}_{2} \mathrm{OH}$ ). It is produced industrially by the catalyzed air oxidation of ethylene:


Use the data in Appendix B to calculate $\Delta G^{\circ}$ and $K_{p}$ for this reaction at $25^{\circ} \mathrm{C}$.
17.91 Use the data in Appendix B to calculate $K_{p}$ at $25^{\circ} \mathrm{C}$ for the reaction

$$
\mathrm{CO}(g)+2 \mathrm{H}_{2}(g) \rightleftharpoons \mathrm{CH}_{3} \mathrm{OH}(g)
$$

What is $\Delta G$ for this reaction at $25^{\circ} \mathrm{C}$ when each reactant and product is present at a partial pressure of 20 atm ?

## General Problems

17.92 Sorbitol $\left(\mathrm{C}_{6} \mathrm{H}_{14} \mathrm{O}_{6}\right)$, a substance used as a sweetener in foods, is prepared by the reaction of glucose with hydrogen in the presence of a catalyst:

$$
\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}(a q)+\mathrm{H}_{2}(g) \longrightarrow \mathrm{C}_{6} \mathrm{H}_{14} \mathrm{O}_{6}(a q)
$$

Which of the following quantities are affected by the catalyst?
(a) Rate of the forward reaction
(b) Rate of the reverse reaction
(c) Spontaneity of the reaction
(d) $\Delta H^{\circ}$
(e) $\Delta S^{\circ}$
(f) $\Delta G^{\circ}$
(g) The equilibrium constant
(h) Time required to reach equilibrium
17.93 Indicate whether the following processes are spontaneous or nonspontaneous:
(a) Heat transfer from a block of ice to a room maintained at $25^{\circ} \mathrm{C}$
(b) Evaporation of water from an open beaker
(c) Conversion of iron(III) oxide to iron metal and oxygen
(d) Uphill motion of an automobile
17.94 Do you agree with the following statements? If not, explain.
(a) Spontaneous reactions are always fast.
(b) In any spontaneous process, the entropy of the system always increases.
(c) An endothermic reaction is always nonspontaneous.
(d) A reaction that is nonspontaneous in the forward direction is always spontaneous in the reverse direction.
17.95 When rolling a pair of dice, there are two ways to get a point total of $3(1+2 ; 2+1)$ but only one way to get a point total of $2(1+1)$. How many ways are there of getting point totals of $4-12$ ? What is the most probable point total?
17.96 Make a rough, qualitative plot of the standard molar entropy versus temperature for methane from 0 K to 298 K . Incorporate the following data into your plot: $\mathrm{mp}=-182^{\circ} \mathrm{C} ; \mathrm{bp}=-164^{\circ} \mathrm{C} ; \mathrm{S}^{\circ}=186.2 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$ at $25^{\circ} \mathrm{C}$.
17.97 The standard free-energy change at $25^{\circ} \mathrm{C}$ for the dissociation of water is 79.9 kJ :
$2 \mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{OH}^{-}(a q) \quad \Delta G^{\circ}=79.9 \mathrm{~kJ}$
For each of the following sets of concentrations, calculate $\Delta G$ at $25^{\circ} \mathrm{C}$ and indicate whether the reaction is spontaneous in the forward or reverse direction.
(a) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \mathrm{M}$
(b) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$
(c) $\left[\mathrm{H}_{3} \mathrm{O}^{+}\right]=1.0 \times 10^{-7} \mathrm{M},\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-10} \mathrm{M}$

Are your results consistent with Le Châtelier's principle? Use the thermodynamic data to calculate the equilibrium constant for the reaction.
17.98 Calculate the normal boiling point of ethanol $\left(\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}\right)$, given that its enthalpy of vaporization is $38.6 \mathrm{~kJ} / \mathrm{mol}$ and its entropy of vaporization is $110 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$.
17.99 Chloroform $\left(\mathrm{CHCl}_{3}\right)$ has a normal boiling point of $61^{\circ} \mathrm{C}$ and an enthalpy of vaporization of $29.24 \mathrm{~kJ} / \mathrm{mol}$. What are its values of $\Delta G_{\text {vap }}$ and $\Delta S_{\text {vap }}$ at $61^{\circ} \mathrm{C}$ ?
17.100 The entropy change for a certain nonspontaneous reaction at $50^{\circ} \mathrm{C}$ is $104 \mathrm{~J} / \mathrm{K}$.
(a) Is the reaction endothermic or exothermic?
(b) What is the minimum value of $\Delta H$ (in kJ ) for the reaction?
17.101 Ammonium nitrate is dangerous because it decomposes (sometimes explosively) when heated:

$$
\mathrm{NH}_{4} \mathrm{NO}_{3}(s) \longrightarrow \mathrm{N}_{2} \mathrm{O}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)
$$

(a) Using the data in Appendix B, show that this reaction is spontaneous at $25^{\circ} \mathrm{C}$.
(b) How does $\Delta G^{\circ}$ for the reaction change when the temperature is raised?
(c) Calculate the equilibrium constant $K_{\mathrm{p}}$ at $25^{\circ} \mathrm{C}$.
(d) Calculate $\Delta G$ for the reaction when the partial pressure of each gas is 30 atm .
17.102 Use the data in Appendix B to calculate $\Delta H^{\circ}, \Delta S^{\circ}$, and $\Delta G^{\circ}$ at $25^{\circ} \mathrm{C}$ for each of the following reactions:
(a) $2 \mathrm{Mg}(s)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{MgO}(s)$
(b) $\mathrm{MgCO}_{3}(s) \rightarrow \mathrm{MgO}(s)+\mathrm{CO}_{2}(g)$
(c) $\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+2 \mathrm{Al}(s) \rightarrow \mathrm{Al}_{2} \mathrm{O}_{3}(s)+2 \mathrm{Fe}(s)$
(d) $2 \mathrm{NaHCO}_{3}(s) \rightarrow \mathrm{Na}_{2} \mathrm{CO}_{3}(s)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(g)$

Are these reactions spontaneous or nonspontaneous at $25^{\circ} \mathrm{C}$ and 1 atm pressure? How does $\Delta G^{\circ}$ change when the temperature is raised?
17.103 Trouton's rule says that the ratio of the molar heat of vaporization of a liquid to its normal boiling point (in kelvins) is approximately the same for all liquids: $\Delta H_{\text {vap }} / T_{\mathrm{bp}} \approx 88 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$.
(a) Check the reliability of Trouton's rule for the liquids listed in the following table.
(b) Explain why liquids tend to have the same value of $\Delta H_{\mathrm{vap}} / T_{\mathrm{bp}}$.
(c) Which of the liquids in the table deviate(s) from Trouton's rule? Explain.

| Liquid | $\mathbf{b p}$ <br> $\left({ }^{\circ} \mathbf{C}\right)$ | $\Delta \boldsymbol{H}_{\text {vap }}$ <br> $(\mathbf{k J} / \mathbf{m o l})$ |
| :--- | ---: | :--- |
| Ammonia | -77.7 | 23.4 |
| Benzene | 80.1 | 30.8 |
| Carbon tetrachloride | 76.8 | 29.8 |
| Chloroform | 61.1 | 29.2 |
| Mercury | 356.6 | 56.9 |

17.104 Just as we can define a standard enthalpy of formation $\left(\Delta H^{\circ}{ }_{\mathrm{f}}\right)$ and a standard free energy of formation $\left(\Delta G^{\circ}\right)$, we can define an analogous standard entropy of formation $\left(\Delta S_{\mathrm{f}}^{\circ}\right)$ as being the entropy change for formation of a substance in its standard state from its constituent elements in their standard states. Use the standard molar entropies given in Appendix B to calculate $\Delta S^{\circ}$ for the following substances:
(a) Benzene, $\mathrm{C}_{6} \mathrm{H}_{6}(l)$
(b) $\mathrm{CaSO}_{4}(s)$
(c) Ethanol, $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}(l)$

Check your answers by calculating $\Delta S^{\circ}{ }_{\mathrm{f}}$ from the values given in Appendix B for $\Delta H^{\circ}{ }_{f}$ and $\Delta G^{\circ}$.
17.105 Use the data in Appendix $B$ to calculate the equilibrium pressure of $\mathrm{CO}_{2}$ in a closed 1 L vessel that contains each of the following samples:
(a) 15 g of $\mathrm{MgCO}_{3}$ and 1.0 g of MgO at $25^{\circ} \mathrm{C}$
(b) 15 g of $\mathrm{MgCO}_{3}$ and 1.0 g of MgO at $280^{\circ} \mathrm{C}$
(c) 30 g of $\mathrm{MgCO}_{3}$ and 1.0 g of MgO at $280^{\circ} \mathrm{C}$

You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
17.106 The equilibrium constant $K_{\mathrm{b}}$ for dissociation of aqueous ammonia is $1.710 \times 10^{-5}$ at $20^{\circ} \mathrm{C}$ and $1.892 \times 10^{-5}$ at $50^{\circ} \mathrm{C}$. What are the values of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for the reaction?

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q)
$$

17.107 Consider the Haber synthesis of gaseous $\mathrm{NH}_{3}\left(\Delta H^{\circ}{ }_{\mathrm{f}}=\right.$ $\left.-46.1 \mathrm{~kJ} / \mathrm{mol} ; \Delta G^{\circ}{ }_{\mathrm{f}}=-16.5 \mathrm{~kJ} / \mathrm{mol}\right):$

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g)
$$

(a) Use only these data to calculate $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for the reaction at $25^{\circ} \mathrm{C}$.
(b) Account for the sign of $\Delta S^{\circ}$.
(c) Is the reaction spontaneous under standard-state conditions at $25^{\circ} \mathrm{C}$ ? Explain.
(d) What are the equilibrium constants $K_{\mathrm{p}}$ and $K_{\mathrm{c}}$ for the reaction at 350 K ? You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
17.108 Consider the dissolution of AgBr in water at $25^{\circ} \mathrm{C}$ :

$$
\operatorname{AgBr}(s) \rightleftharpoons \mathrm{Ag}^{+}(a q)+\mathrm{Br}^{-}(a q)
$$

(a) Use the standard heats of formation and standard molar entropies in Appendix B to calculate $\Delta G^{\circ}$ for the reaction at $25^{\circ} \mathrm{C}$.
(b) Calculate $K_{\text {sp }}$ for AgBr at $25^{\circ} \mathrm{C}$.
(c) Calculate $\Delta G$ for dissolution of AgBr at $25^{\circ} \mathrm{C}$ when $\left[\mathrm{Ag}^{+}\right]=\left[\mathrm{Br}^{-}\right]=1.00 \times 10^{-5} \mathrm{M}$. Is your result consistent with the relative values of $Q$ and $K_{\text {sp }}$ ?
17.109 The temperature dependence of the equilibrium constant is given by the equation

$$
\ln K=\frac{-\Delta H^{\circ}}{R}\left(\frac{1}{T}\right)+\frac{\Delta S^{\circ}}{R}
$$

where $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are assumed to be independent of temperature.
(a) Derive this equation from equations given in this chapter.
(b) Explain how this equation can be used to determine experimental values of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ from values of $K$ at several different temperatures.
(c) Use this equation to predict the sign of $\Delta H^{\circ}$ for a reaction whose equilibrium constant increases with increasing temperature. Is the reaction endothermic or exothermic? Is your prediction in accord with Le Châtelier's principle?
17.110 The normal boiling point of bromine is $58.8^{\circ} \mathrm{C}$, and the standard entropies of the liquid and vapor are $S^{\circ}\left[\mathrm{Br}_{2}(l)\right]=152.2 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol}) ; S^{\circ}\left[\mathrm{Br}_{2}(g)\right]=$ $245.4 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. At what temperature does bromine have a vapor pressure of 227 mm Hg ?
17.111 The molar solubility of lead iodide is $1.45 \times 10^{-3} \mathrm{M}$ at $20^{\circ} \mathrm{C}$ and $6.85 \times 10^{-3} \mathrm{M}$ at $80^{\circ} \mathrm{C}$. What are the values of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ for dissolution of $\mathrm{PbI}_{2}$ ?

$$
\mathrm{PbI}_{2}(s) \longrightarrow \mathrm{Pb}^{2+}(a q)+2 \mathrm{I}^{-}(a q)
$$

You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
17.112 Use the data in Appendix B to calculate the equilibrium constant $K$ for the following reaction at $80^{\circ} \mathrm{C}$ :

$$
2 \mathrm{Br}^{-}(a q)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{Br}_{2}(l)+2 \mathrm{Cl}^{-}(a q)
$$

You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
17.113 Use the data from Appendix B to determine the normal boiling point of carbon disulfide $\left(\mathrm{CS}_{2}\right)$.
17.114 A "humidity sensor" consists of a cardboard square that is colored blue in dry weather and red in humid weather. The color change is due to the reaction:


For this reaction at $25^{\circ} \mathrm{C}, \Delta H^{\circ}=-352 \mathrm{~kJ} / \mathrm{mol}$ and $\Delta S^{\circ}=-899 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$. Assuming that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature, what is the vapor pressure of water (in mm Hg ) at equilibrium for the above reaction at $35^{\circ} \mathrm{C}$ on a hot summer day?
17.115 The following reaction, sometimes used in the laboratory to generate small quantities of oxygen gas, has $\Delta G^{\circ}=-225.8 \mathrm{~kJ} / \mathrm{mol}$ at $25^{\circ} \mathrm{C}$ :

$$
2 \mathrm{KClO}_{3}(s) \longrightarrow 2 \mathrm{KCl}(s)+3 \mathrm{O}_{2}(g)
$$

Use the following additional data at $25^{\circ} \mathrm{C}$ to calculate the standard molar entropy $S^{\circ}$ of $\mathrm{O}_{2}$ at $25^{\circ} \mathrm{C}$ :
$\Delta H^{\circ}{ }_{\mathrm{f}}\left(\mathrm{KClO}_{3}\right)=-397.7 \mathrm{~kJ} / \mathrm{mol}$
$\Delta H^{\circ}{ }_{\mathrm{f}}(\mathrm{KCl})=-436.7 \mathrm{~kJ} / \mathrm{mol}$
$S^{\circ}\left(\mathrm{KClO}_{3}\right)=143 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$
$S^{\circ}(\mathrm{KCl})=82.6 \mathrm{~J} /(\mathrm{K} \cdot \mathrm{mol})$
17.116 Consider for the equilibrium $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)$.
(a) Use the thermodynamic data in Appendix B to determine the temperature at which an equilibrium mixture with a total pressure of 1.00 atm will contain twice as much $\mathrm{NO}_{2}$ as $\mathrm{N}_{2} \mathrm{O}_{4}$. You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
(b) At what temperature will an equilibrium mixture with a total pressure of 1.00 atm contain equal amounts of $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ ?

## Multi-Concept Problems

17.117 A mixture of $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$, each at an initial partial pressure of 1.00 atm and a temperature of $100^{\circ} \mathrm{C}$, is allowed to react. Use the data in Appendix B to calculate the partial pressure of each gas at equilibrium. You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.

$$
\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons 2 \mathrm{NO}_{2}(g)
$$

17.118 A mixture of 14.0 g of $\mathrm{N}_{2}$ and 3.024 g of $\mathrm{H}_{2}$ in a 5.00 L container is heated to $400^{\circ} \mathrm{C}$. Use the data in Appendix $B$ to calculate the molar concentrations of $\mathrm{N}_{2}, \mathrm{H}_{2}$, and $\mathrm{NH}_{3}$ at equilibrium. Assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature, and remember that the standard state of a gas is defined in terms of pressure.

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \rightleftharpoons 2 \mathrm{NH}_{3}(g)
$$

17.119 One step in the commercial synthesis of sulfuric acid is the catalytic oxidation of sulfur dioxide:

$$
2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{SO}_{3}(g)
$$

(a) A mixture of 192 g of $\mathrm{SO}_{2}, 48.0 \mathrm{~g}$ of $\mathrm{O}_{2}$, and a $\mathrm{V}_{2} \mathrm{O}_{5}$ catalyst is heated to 800 K in a 15.0 L vessel. Use the data in Appendix B to calculate the partial pressures of $\mathrm{SO}_{3}, \mathrm{SO}_{2}$, and $\mathrm{O}_{2}$ at equilibrium. You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
(b) Does the percent yield of $\mathrm{SO}_{3}$ increase or decrease on raising the temperature from 800 K to 1000 K ? Explain.
(c) Does the total pressure increase or decrease on raising the temperature from 800 K to 1000 K ? Calculate the total pressure (in atm) at 1000 K .
17.120 The lead storage battery uses the reaction

$$
\begin{array}{r}
\mathrm{Pb}(s)+\mathrm{PbO}_{2}(s)+2 \mathrm{H}^{+}(a q)+2 \mathrm{HSO}_{4}^{-}(a q) \longrightarrow \\
2 \mathrm{PbSO}_{4}(s)+2 \mathrm{H}_{2} \mathrm{O}(l)
\end{array}
$$

(a) Use the data in Appendix B to calculate $\Delta G^{\circ}$ for this reaction.
(b) Calculate $\Delta G$ for this reaction on a cold winter's day $\left(10^{\circ} \mathrm{F}\right)$ in a battery that has "run down" to the point where the sulfuric acid concentration is only 0.100 M .
17.121 What is the molar solubility of $\mathrm{CaCO}_{3}$ at $50^{\circ} \mathrm{C}$ in a solution prepared by dissolving 1.000 L of $\mathrm{CO}_{2}$ gas (at $20^{\circ} \mathrm{C}$ and 731 mm Hg ) and 3.335 g of solid $\mathrm{Ca}(\mathrm{OH})_{2}$ in enough water to make 500.0 mL of solution at $50^{\circ} \mathrm{C}$ ? Is the solubility of $\mathrm{CaCO}_{3}$ at $50^{\circ} \mathrm{C}$ larger or smaller than at $25^{\circ} \mathrm{C}$ ? Explain. You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
17.122 A 1.00 L volume of gaseous ammonia at $25.0^{\circ} \mathrm{C}$ and 744 mm Hg was dissolved in enough water to make 500.0 mL of aqueous ammonia at $2.0^{\circ} \mathrm{C}$. What is $K_{\mathrm{b}}$ for $\mathrm{NH}_{3}$ at $2.0^{\circ} \mathrm{C}$, and what is the pH of the solution. You may assume that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
17.123 Consider the unbalanced equation: $\mathrm{I}_{2}(s) \rightarrow \mathrm{I}^{-}(a q)+$ $\mathrm{IO}_{3}^{-}(a q)$.
(a) Balance the equation for this reaction in basic solution.
(b) Use the data in Appendix $B$ and $\Delta G_{f}^{\circ}$ for $\mathrm{IO}_{3}{ }^{-}(a q)=-128.0 \mathrm{~kJ} / \mathrm{mol}$ to calculate $\Delta G^{\circ}$ for the reaction at $25^{\circ} \mathrm{C}$.
(c) Is the reaction spontaneous or nonspontaneous under standard-state conditions?
(d) What pH is required for the reaction to be at equilibrium at $25^{\circ} \mathrm{C}$ when $\left[\mathrm{I}^{-}\right]=0.10 \mathrm{M}$ and $\left[\mathrm{IO}_{3}{ }^{-}\right]=0.50 \mathrm{M}$ ?

## eMedia Problems

17.124 The Spontaneous Process activity (eChapter 17.1) shows a vessel filled with gas connected to an evacuated vessel. What happens when the stopcock is opened? Is this a spontaneous process? Why? Is it possible to open and close the stopcock so that all of the gas returns to the original vessel? Why or why not?
17.125 Is it possible for a spontaneous process to absorb heat? Use the Enthalpy of Solution activity (eChapter 17.2) to find a solution process that confirms your answer. What entropy change must accompany this process?
17.126 The Entropy and Temperature activity (eChapter 17.4) has 5 distinct regions where entropy is changing as temperature is increasing. Explain the changes that are occurring at the molecular level that would account for the increase in entropy.
17.127 In the graphs generated by the Gibbs Free Energy activity (eChapter 17.8),
(a) What conditions give rise to the greatest temperature dependence of $\Delta G$ ?
(b) Which reactions have a negative $\Delta G$ at low temperatures? What do these reactions have in common?
(c) Which reactions have a negative $\Delta G$ at high temperatures? What do these reactions have in common?
17.128 The spontaneous decomposition of sodium azide is shown in the Airbags movie (eChapter 17.8).
(a) What are the signs of $\Delta G^{\circ}, \Delta H^{\circ}$, and $\Delta S^{\circ}$ for this decomposition reaction?
(b) Is there any temperature at which this reaction is not spontaneous? Explain.
17.129 According to the Reaction Mixture and Free Energy activity in eChapter 17.10,
(a) Which reaction component has the greatest effect on the value of the Gibbs free energy? Why?
(b) Addition of which reaction component will cause the reaction to become nonspontaneous? Explain in terms of equilibrium and in terms of the value of $\Delta G$.

## Chapter

## Electrochemistry

## Batteries are everywhere in modern

 societies. They provide the electric current to start our automobiles and to power a host of products such as pocket calculators, digital watches, heart pacemakers, radios, and tape recorders. A battery is an electrochemical cell, a device for interconvert-
ing chemical and electrical energy. A battery takes the energy released by a spontaneous chemical reaction and uses it to produce electricity.

Electrochemistry, the area of chemistry concerned with the interconversion of chemical and electrical

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Silver-plated objects such as this teapot are made by electroplating pure silver metal onto steel.
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18.2 Shorthand Notation for Galvanic Cells
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- Interlude-Electrochemical Art

FIGURE 18.1 (a) A strip of zinc metal is immersed in an aqueous copper sulfate solution. The redox reaction takes place at the metal-solution interface and directly transfers two electrons from Zn atoms to $\mathrm{Cu}^{2+}$ ions. (b) As time passes, a dark colored deposit of copper metal appears on the zinc, and the blue color due to $\mathrm{Cu}^{2+}(a q)$ fades from the solution.


Oxidation-Reduction Reactions Part 2 movie
taic Cells I: The Copper-Zinc Cell movie
energy, is enormously important in modern science and technology not only because of batteries but also because it makes possible the manufacture of essential industrial chemicals and materials. Sodium hydroxide, for example, which is used in the manufacture of paper, textiles, soaps, and detergents, is produced by passing an electric current through an aqueous solution of sodium chloride. Chlorine, essential to the manufacture of plastics such as poly(vinyl chloride) (PVC), is obtained in the same process. Aluminum metal is also produced in an electrochemical process, as is pure copper for use in electrical wiring.

In this chapter, we'll look at the principles involved in the design and operation of electrochemical cells. In addition, we'll explore some important connections between electrochemistry and thermodynamics.

## 18.1 | Galvanic Cells

Electrochemical cells are of two basic types: galvanic cells (also called voltaic cells) and electrolytic cells. The names "galvanic" and "voltaic" honor the Italian scientists Luigi Galvani (1737-1798) and Alessandro Volta (1745-1827), who conducted pioneering work in the field of electrochemistry. In a galvanic cell, a spontaneous

chemical reaction generates an electric current. In an electrolytic cell, an electric current drives a nonspontaneous reaction. The two types are therefore the reverse of each other. We'll take up galvanic cells in this section and will examine electrolytic cells later. First, though, let's review some of the basics of oxidation-reduction, or redox, reactions (Section 4.6).

If you immerse a strip of zinc metal in an aqueous solution of copper sulfate, you find that a dark colored solid deposits on the surface of the zinc and that the blue color characteristic of the $\mathrm{Cu}^{2+}$ ion slowly disappears from the solution (Figure 18.1). Chemical analysis shows that the dark colored deposit is finely divided copper metal and that the solution now contains zinc ions. Therefore, the reaction is

$$
\mathrm{Zn}(s)+\mathrm{Cu}^{2+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{Cu}(s)
$$

This is a redox reaction in which Zn is oxidized to $\mathrm{Zn}^{2+}$ and $\mathrm{Cu}^{2+}$ is reduced to Cu . Recall that an oxidation is a loss of electrons (an increase in oxidation number) and a reduction is a gain of electrons (a decrease in oxidation number).

We can represent the oxidation and reduction aspects of the reaction by separating the overall process into half-reactions, one representing the oxidation reaction and the other representing the reduction:

$$
\begin{array}{ll}
\text { Oxidation half-reaction: } & \mathrm{Zn}(s) \longrightarrow \mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-} \\
\text {Reduction half-reaction: } & \mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} \xrightarrow{ } \mathrm{Cu}(s)
\end{array}
$$

We say that $\mathrm{Cu}^{2+}$ is the oxidizing agent because, in gaining electrons from Zn , it causes the oxidation of Zn to $\mathrm{Zn}^{2+}$. Similarly, we say that Zn is the reducing agent because, in losing electrons to $\mathrm{Cu}^{2+}$, it causes the reduction of $\mathrm{Cu}^{2+}$ to Cu .

If the reaction is carried out as shown in Figure 18.1, electrons are transferred directly from Zn to $\mathrm{Cu}^{2+}$, and the enthalpy of reaction is lost to the surroundings as heat. If, however, the reaction is carried out using the electrochemical cell depicted in Figure 18.2, then some of the chemical energy released by the reaction is converted to electrical energy, which can be used to light a lightbulb or run an electric motor.

(a)

Lee R. Summerlin, Christie L.
Borgford, and Julie B. Ealy,
"Visible Oxidation-Reduction in Electrochemical Cells," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 205-206.
$\nabla$ FIGURE 18.2 (a) A galvanic cell that uses the oxidation of zinc metal to $\mathrm{Zn}^{2+}$ ions and the reduction of $\mathrm{Cu}^{2+}$ ions to copper metal. Note that the negative particles (electrons in the wire and anions in solution) travel around the circuit in the same direction. The resulting electric current can be used to light a lightbulb. (b) An operating Daniell cell. The salt bridge in part (a) is replaced by a porous glass disk that allows ions to flow between the anode and cathode compartments but prevents bulk mixing, which would bring $\mathrm{Cu}^{2+}$ ions into direct contact with zinc and short-circuit the cell. The lightbulb in part (a) is replaced with a digital voltmeter (more about this in Section 18.3).

(b)

Penelope Ann Huddle, Margaret Dawn White, and Fiona Rogers, "Using a Teaching Model to Correct Known Misconceptions in Electrochemistry," J. Chem. Educ., Vol. 77, 2000, 104-110.

V
Anions flow through the salt bridge into the anode compartment while cations flow into the cathode compartment to maintain electroneutrality.

VThe anode of a galvanic cell is negative (like an anion), and the cathode is positive (like a cation). Electrons move from the negative anode through an external circuit to the positive cathode.

The apparatus shown in Figure 18.2 is a type of galvanic cell called a Daniell cell, after John Frederick Daniell, the English chemist who first constructed it in 1836. It consists of two half-cells, a beaker containing a strip of zinc that dips into an aqueous solution of zinc sulfate and a second beaker containing a strip of copper that dips into aqueous copper sulfate. The strips of zinc and copper are called electrodes and are connected by an electrically conducting wire. In addition, the two solutions are connected by a salt bridge, a U-shaped tube that contains a gel permeated with a solution of an inert electrolyte, such as $\mathrm{Na}_{2} \mathrm{SO}_{4}$. The ions of the inert electrolyte do not react with the other ions in the solutions, and they are not oxidized or reduced at the electrodes.

The reaction that occurs in the Daniell cell is the same one that occurs when Zn reacts directly with $\mathrm{Cu}^{2+}$, but now, because the Zn metal and $\mathrm{Cu}^{2+}$ ions are in separate compartments, the electrons are transferred from Zn to $\mathrm{Cu}^{2+}$ through the wire. Consequently, the oxidation and reduction half-reactions occur at separate electrodes and an electric current flows through the wire. Electrons are not transferred through the solution because the metal wire is a much better conductor of electrons than is water. In fact, free electrons react rapidly with water and are therefore unstable in aqueous solutions.

The electrode at which oxidation takes place is called the anode (the zinc strip in this example), and the electrode at which reduction takes place is called the cathode (the copper strip). The anode and cathode half-reactions must add to give the overall cell reaction:

Anode (oxidation) half-reaction:

$$
\begin{aligned}
\mathrm{Zn}(s) & \longrightarrow \mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-} \\
\mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} & \longrightarrow \mathrm{Cu}(s) \\
\mathrm{Zn}(s)+\mathrm{Cu}^{2+}(a q) & \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{Cu}(s)
\end{aligned}
$$

Cathode (reduction) half-reaction:
Overall cell reaction:
The salt bridge is necessary to complete the electrical circuit. Without it, the solution in the anode compartment would become positively charged as $\mathrm{Zn}^{2+}$ ions appeared in it, and the solution in the cathode compartment would become negatively charged as $\mathrm{Cu}^{2+}$ ions were removed from it. Because of the charge imbalance, the electrode reactions would quickly come to a halt, and electron flow through the wire would cease.

With the salt bridge in place, electrical neutrality is maintained in both compartments by a flow of ions. Anions (in this case $\mathrm{SO}_{4}{ }^{2-}$ ) flow through the salt bridge from the cathode compartment to the anode compartment, and cations migrate through the salt bridge from the anode compartment to the cathode compartment. For the cell shown in Figure $18.2, \mathrm{Na}^{+}$ions move out of the salt bridge into the cathode compartment and $\mathrm{Zn}^{2+}$ ions move into the salt bridge from the anode compartment. (The anode and cathode get their names from the direction of ion flow between the two compartments: Anions move toward the anode, and cations move toward the cathode.)

The electrodes of commercial galvanic cells (batteries) are generally labeled with plus $(+)$ and minus $(-)$ signs, although the magnitude of the actual charge on the electrodes is infinitesimally small and the sign of the charge associated with each electrode depends on the point of view. From the perspective of the wire, the anode looks negative because a stream of negatively charged electrons comes from it. From the perspective of the solution, the anode looks positive because positively charged $\mathrm{Zn}^{2+}$ ions move from it. Because galvanic cells are used to supply electric current to an external circuit, it makes sense to adopt the perspective of the wire. Consequently, we regard the anode as the negative $(-)$ electrode and the cathode as the positive $(+)$ electrode. Thus, electrons move through the external circuit from the negative electrode, where they are produced by the anode half-reaction, to the positive electrode, where they are consumed by the cathode half-reaction.

Anode: $\left\{\begin{array}{l}\text { Is where oxidation occurs } \\ \text { Is where electrons are produced } \\ \text { Is what anions migrate toward } \\ \text { Has a negative sign }\end{array}\right.$

$$
\text { Cathode: }\left\{\begin{array}{l}
\text { Is where reduction occurs } \\
\text { Is where electrons are consumed } \\
\text { Is what cations migrate toward } \\
\text { Has a positive sign }
\end{array}\right.
$$



Why do anions move toward the anode? Shouldn't the negative ions be repelled by the negative charge of the anode? The answer is that the anode's negative charge is shielded by the surrounding $\mathrm{Zn}^{2+}$ cations, which enter the solution from the surface of the electrode when zinc is oxidized. From the perspective of the anions, the solution around the anode "looks" positive, and so the anions move toward the anode to neutralize the positive charge of the $\mathrm{Zn}^{2+}$ cations (Figure 18.3).

## Worked Example 18.1

Design a galvanic cell that uses the redox reaction

$$
\mathrm{Fe}(s)+2 \mathrm{Fe}^{3+}(a q) \longrightarrow 3 \mathrm{Fe}^{2+}(a q)
$$

Identify the anode and cathode half-reactions, and sketch the experimental setup. Label the anode and cathode, indicate the direction of electron and ion flow, and identify the sign of each electrode.

## Strategy

First, separate the overall cell reaction into anode (oxidation) and cathode (reduction) half-reactions. Then, set up two half-cells that use these half-reactions, and connect the half-cells with a conducting wire and a salt bridge.

## Solution

In the overall cell reaction, iron metal is oxidized to iron(II) ions, and iron(III) ions are reduced to iron(II) ions. Therefore, the cell half-reactions are

$$
\begin{array}{lrl}
\text { Anode (oxidation): } & \mathrm{Fe}(s) \longrightarrow \mathrm{Fe}^{2+}(a q)+2 \mathrm{e}^{-} \\
\text {Cathode (reduction): } & 2 \times\left[\mathrm{Fe}^{3+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Fe}^{2+}(a q)\right] \\
\text { Overall cell reaction: } & \mathrm{Fe}(s)+2 \mathrm{Fe}^{3+}(a q) \longrightarrow 3 \mathrm{Fe}^{2+}(a q)
\end{array}
$$

The cathode half-reaction has been multiplied by a factor of 2 so that the two halfreactions will add to give the overall cell reaction. Whenever half-reactions are added, the electrons must cancel. No electrons can appear in the overall reaction because all of the electrons lost by the reducing agent are gained by the oxidizing agent.

A possible experimental setup is shown on the next page. The anode compartment consists of an iron metal electrode dipping into an aqueous solution of $\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{2}$. Note, though, that any inert electrolyte can be used to carry the current in the anode

© FIGURE 18.3 Anions move toward the anode to neutralize the positive charge of the cations produced in solution when zinc metal is oxidized.
compartment; $\mathrm{Fe}^{2+}$ does not need to be present initially because it's not a reactant in the anode half-reaction.

Since $\mathrm{Fe}^{3+}$ is a reactant in the cathode half-reaction, $\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}$ would be a good electrolyte for the cathode compartment. The cathode can be any electrical conductor that doesn't react with the ions in the solution. A platinum wire is a common inert electrode. (Iron metal can't be used because it would react directly with $\mathrm{Fe}^{3+}$, thus shortcircuiting the cell.) The salt bridge contains $\mathrm{NaNO}_{3}$, but any inert electrolyte would do. Electrons flow through the wire from the iron anode $(-)$ to the platinum cathode $(+)$. Anions move from the cathode compartment toward the anode while cations migrate from the anode compartment toward the cathode.


PROBLEM 18.1 Describe a galvanic cell that uses the reaction

$$
2 \mathrm{Ag}^{+}(a q)+\mathrm{Ni}(s) \longrightarrow 2 \mathrm{Ag}(s)+\mathrm{Ni}^{2+}(a q)
$$

Identify the anode and cathode half-reactions, and sketch the experimental setup. Label the anode and cathode, indicate the direction of electron and ion flow, and identify the sign of each electrode.

### 18.2 Shorthand Notation for Galvanic Cells

Rather than describing a galvanic cell in words, it's convenient to use a shorthand notation for representing the cell. For the Daniell cell in Figure 18.2, which uses the reaction

$$
\mathrm{Zn}(s)+\mathrm{Cu}^{2+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{Cu}(s)
$$

we can write the following expression:

$$
\mathrm{Zn}(s)\left|\mathrm{Zn}^{2+}(a q) \| \mathrm{Cu}^{2+}(a q)\right| \mathrm{Cu}(s)
$$

In this notation, a single vertical line (l) represents a phase boundary, such as that between a solid electrode and an aqueous solution, and the double vertical line ( $\|$ ) denotes a salt bridge. The shorthand for the anode half-cell is always written on the left of the salt-bridge symbol, followed on the right by the shorthand for the cathode half-cell. The electrodes are written on the extreme left (anode) and on the extreme right (cathode), and the reactants in each half-cell are always written first, followed by the products. With these arbitrary conventions, electrons move through the external circuit from left to right (from anode to cathode). Reading the shorthand thus suggests the overall cell reaction: Zn is oxidized to $\mathrm{Zn}^{2+}$, and $\mathrm{Cu}^{2+}$ is reduced to Cu .


For the galvanic cell in Worked Example 18.1, based on the reaction

$$
\mathrm{Fe}(s)+2 \mathrm{Fe}^{3+}(a q) \longrightarrow 3 \mathrm{Fe}^{2+}(a q)
$$

the shorthand notation is

$$
\mathrm{Fe}(s)\left|\mathrm{Fe}^{2+}(a q) \| \mathrm{Fe}^{3+}(a q), \mathrm{Fe}^{2+}(a q)\right| \operatorname{Pt}(s)
$$

The shorthand for the cathode half-cell includes both reactant $\left(\mathrm{Fe}^{3+}\right)$ and product $\left(\mathrm{Fe}^{2+}\right)$ as well as the electrode ( Pt ). The two ions $\mathrm{Fe}^{3+}(a q)$ and $\mathrm{Fe}^{2+}(a q)$ are separated by a comma rather than a vertical line because they are in the same phase.

The notation for a cell involving a gas has an additional vertical line because an additional phase is present. Thus, the notation

$$
\mathrm{Cu}(s)\left|\mathrm{Cu}^{2+}(a q) \| \mathrm{Cl}_{2}(g)\right| \mathrm{Cl}^{-}(a q) \mid \mathrm{C}(s)
$$

specifies a cell in which copper is oxidized to $\mathrm{Cu}^{2+}$ at a copper anode and $\mathrm{Cl}_{2}$ gas is reduced to $\mathrm{Cl}^{-}$at a graphite (carbon) cathode. The cell reaction is

$$
\mathrm{Cu}(s)+\mathrm{Cl}_{2}(g) \longrightarrow \mathrm{Cu}^{2+}(a q)+2 \mathrm{Cl}^{-}(a q)
$$

A more detailed notation would include ion concentrations and gas pressures, as in the following:

$$
\mathrm{Cu}(s)\left|\mathrm{Cu}^{2+}(1.0 \mathrm{M}) \| \mathrm{Cl}_{2}(1 \mathrm{~atm})\right| \mathrm{Cl}^{-}(1.0 \mathrm{M}) \mid \mathrm{C}(s)
$$

## Worked Example 18.2

Given the following shorthand notation

$$
\operatorname{Pt}(s)\left|\mathrm{Sn}^{2+}(a q), \mathrm{Sn}^{4+}(a q) \| \mathrm{Ag}^{+}(a q)\right| \mathrm{Ag}(s)
$$

write a balanced equation for the cell reaction, and give a brief description of the cell.

## Strategy

We can obtain the cell half-reactions simply by reading the shorthand notation. To find the balanced equation for the cell reaction, add the two half-reactions after multiplying each by an appropriate factor so that the electrons will cancel. The shorthand notation specifies the anode (on the extreme left), the cathode (on the extreme right), and the reactants in the half-cell compartments.

## Solution

Because the anode always appears at the left in the shorthand notation, the anode (oxidation) half-reaction is

$$
\mathrm{Sn}^{2+}(a q) \longrightarrow \mathrm{Sn}^{4+}(a q)+2 \mathrm{e}^{-}
$$

The cathode (reduction) half-reaction is

$$
2 \times\left[\mathrm{Ag}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Ag}(s)\right]
$$

We multiply the cathode half-reaction by a factor of 2 so that the electrons will cancel when we sum the two half-reactions to give the cell reaction:

$$
\mathrm{Sn}^{2+}(a q)+2 \mathrm{Ag}^{+}(a q) \longrightarrow \mathrm{Sn}^{4+}(a q)+2 \mathrm{Ag}(s)
$$

Shorthand Notation
for Galvanic Cells activity

The cell consists of a platinum wire anode dipping into an $\mathrm{Sn}^{2+}$ solution-say, $\mathrm{Sn}\left(\mathrm{NO}_{3}\right)_{2}(a q)$ —and a silver cathode dipping into an $\mathrm{Ag}^{+}$solution—say, $\mathrm{AgNO}_{3}(a q)$. As usual, the anode and cathode half-cells must be connected by a wire and a salt bridge containing inert ions.

Although the anode half-cell always appears on the left in the shorthand notation, its location in a cell drawing is arbitrary. This means that you can't infer which electrode is the anode and which is the cathode from the location of the electrodes in a cell drawing. You must identify the electrodes based on whether each electrode half-reaction is an oxidation or a reduction.

- PROBLEM 18.2 Write the shorthand notation for a galvanic cell that uses the reaction

$$
\mathrm{Fe}(s)+\mathrm{Sn}^{2+}(a q) \longrightarrow \mathrm{Fe}^{2+}(a q)+\mathrm{Sn}(s)
$$

- PROBLEM 18.3 Write a balanced equation for the overall cell reaction, and give a brief description of a galvanic cell represented by the following shorthand notation:

$$
\mathrm{Pb}(s)\left|\mathrm{Pb}^{2+}(a q) \| \mathrm{Br}_{2}(l)\right| \mathrm{Br}^{-}(a q) \mid \operatorname{Pt}(s)
$$

- KEY CONCEPT PROBLEM 18.4 Consider the following galvanic cell:

Galvanic Cells activity

$\sqrt{ }$The driving force of a cell reaction, measured in volts and called cell voltage, cell potential, or electromotive force, is a function of the natural tendency of one substance to lose electrons and of a second substance to gain electrons. The greater these tendencies, the higher the cell voltage.

(a) Complete the drawing by adding any components essential for a functioning cell.
(b) Label the anode and cathode, and indicate the direction of ion flow.
(c) Write a balanced equation for the cell reaction.
(d) Write the shorthand notation for the cell.

### 18.3 Cell Potentials and Free-Energy Changes for Cell Reactions

Let's return to the Daniell cell shown in Figure 18.2 to find an electrical measure of the driving force of a cell reaction. Electrons move through the external circuit from the zinc anode to the copper cathode because they have lower energy when on copper than on zinc. The driving force that pushes the negatively charged electrons away from the anode ( - electrode) and pulls them toward the cathode ( + electrode) is an electrical potential called the electromotive force (emf), also known as the cell potential $(E)$ or the cell voltage. The SI unit of electrical potential is the volt $(\mathrm{V})$, and the potential of a galvanic cell is defined as a positive quantity.

The relationship between the volt and the SI units of energy (joule, J) and electric charge (coulomb, C) is given by the equation

$$
1 \mathrm{~J}=1 \mathrm{C} \times 1 \mathrm{~V}
$$

where 1 C is the amount of charge transferred when a current of 1 ampere (A) flows for 1 second (s). [Since 1 watt (W) is $1 \mathrm{~J} / \mathrm{s}$, the current passing through a 100 W household lightbulb is about 1 A , which means that the electric charge of the electrons passing through the bulb in 1 s is 1 C .] When 1 C of charge moves between two electrodes that differ in electrical potential by $1 \mathrm{~V}, 1 \mathrm{~J}$ of energy is released by the cell and can be used to do electrical work.

A cell potential is measured with an electronic instrument called a voltmeter (Figure 18.2b), which is designed to give a positive reading when the + and - terminals of the voltmeter are connected to the + (cathode) and - (anode) electrodes of the cell, respectively. Thus, the voltmeter-cell connections required to get a positive reading on the voltmeter indicate which electrode is the anode and which is the cathode.

We've now seen two quantitative measures of the driving force of a chemical reaction: the cell potential $E$ (an electrochemical quantity) and the free-energy change $\Delta G$ (a thermochemical quantity, Section 17.7). The values of $\Delta G$ and $E$ are directly proportional and are related by the equation

$$
\Delta G=-n F E
$$

where $n$ is the number of moles of electrons transferred in the reaction and $F$ is the faraday (or Faraday constant), the electric charge on 1 mol of electrons $\left(96,485 \mathrm{C} / \mathrm{mol} \mathrm{e}^{-}\right)$. In our calculations, we'll round the value of $F$ to three significant figures:

$$
F=96,500 \mathrm{C} / \mathrm{mol} \mathrm{e}^{-}
$$

The faraday is named in honor of Michael Faraday (1791-1867), the nineteenthcentury English scientist who laid the foundations for our current understanding of electricity.

Two features of the equation $\Delta G=-n F E$ are worth noting: the units and the minus sign. When we multiply the charge transferred ( $n F$ ) in coulombs by the cell potential $(E)$ in volts, we obtain an energy $(\Delta G)$ in joules, in accord with the relationship $1 \mathrm{~J}=1 \mathrm{C} \times 1 \mathrm{~V}$. The minus sign is required because $E$ and $\Delta G$ have opposite signs: The spontaneous reaction in a galvanic cell has a positive cell potential but a negative free-energy change (Section 17.7).

Later in this chapter, we'll see that cell potentials, like free-energy changes, depend on the composition of the reaction mixture. The standard cell potential $E^{\circ}$ is the cell potential when both reactants and products are in their standard states-solutes at 1 M concentrations, gases at a partial pressure of 1 atm , solids and liquids in pure form, with all at a specified temperature, usually $25^{\circ} \mathrm{C}$. For example, $E^{\circ}$ for the reaction

$$
\mathrm{Zn}(s)+\mathrm{Cu}^{2+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{Cu}(s)
$$

is the cell potential measured at $25^{\circ} \mathrm{C}$ for a cell that has pure Zn and Cu metal electrodes and 1 M concentrations of $\mathrm{Zn}^{2+}$ and $\mathrm{Cu}^{2+}$.

The standard free-energy change and the standard cell potential are related by the equation

$$
\Delta G^{\circ}=-n F E^{\circ}
$$

Because $\Delta G^{\circ}$ and $E^{\circ}$ are directly proportional, a voltmeter can be regarded as a "freeenergy meter." When a voltmeter measures $E^{\circ}$, it also indirectly measures $\Delta G^{\circ}$.

## Worked Example 18.3

Calculate the standard free-energy change at $25^{\circ} \mathrm{C}$ for the following reaction. The standard cell potential is 1.10 V at $25^{\circ} \mathrm{C}$.

$$
\mathrm{Zn}(s)+\mathrm{Cu}^{2+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{Cu}(s)
$$

$\nabla$When a chemical equation is balanced by the half-reaction method, the number of electrons that occur on both sides of the balanced equation (before canceling) is equal to the value of $n$.

For a spontaneous reaction $\Delta G$ is negative but $E$ is positive.

Standard conditions for $E^{\circ}$, the standard cell potential, are identical with standard conditions for $\Delta G^{\circ}, \Delta H^{\circ}$, and $\Delta S^{\circ}$.

## Strategy

To calculate $\Delta G^{\circ}$, we use the equation $\Delta G^{\circ}=-n F E^{\circ}$, where $E^{\circ}$ is given and $n$ can be inferred from the balanced chemical equation.

## Solution

Two moles of electrons are transferred from Zn to $\mathrm{Cu}^{2+}$ in this reaction, and the standard free-energy change is therefore

$$
\begin{aligned}
\Delta G^{\circ} & =-n F E^{\circ}=-\left(2 \mathrm{~mol} \mathrm{e}^{-}\right)\left(\frac{96,500 \mathrm{C}}{\mathrm{~mol} \mathrm{e}^{-}}\right)(1.10 \mathrm{~V})\left(\frac{1 \mathrm{~J}}{1 \mathrm{C} \cdot \mathrm{~V}}\right) \\
& =-212,000 \mathrm{~J}=-212 \mathrm{~kJ}
\end{aligned}
$$

$\checkmark$ BALlPARK CHECK $F$ is about $10^{5} \mathrm{C} / \mathrm{mol} \mathrm{e}^{-}$and $E^{\circ}$ is about 1 V , so $\Delta G^{\circ}=$ $-n F E^{\circ}$ is approximately $-\left(2 \mathrm{~mol} \mathrm{e}{ }^{-}\right)\left(10^{5} \mathrm{C} / \mathrm{mol} \mathrm{e}^{-}\right)(1 \mathrm{~V})=-2 \times 10^{5} \mathrm{~J}$, or -200 kJ . The ballpark check and the solution agree.

- PROBLEM 18.5 The standard cell potential at $25^{\circ} \mathrm{C}$ is 0.92 V for the reaction

$$
\mathrm{Al}(s)+\mathrm{Cr}^{3+}(a q) \longrightarrow \mathrm{Al}^{3+}(a q)+\mathrm{Cr}(s)
$$

What is the standard free-energy change for this reaction at $25^{\circ} \mathrm{C}$ ?

## 18.4 | Standard Reduction Potentials

The standard potential of any galvanic cell is the sum of the standard half-cell potentials for oxidation at the anode and reduction at the cathode:

$$
E_{\text {cell }}^{\circ}=E_{\mathrm{ox}}^{\circ}+E_{\mathrm{red}}^{\circ}
$$

Consider, for example, a cell in which $\mathrm{H}_{2}$ gas is oxidized to $\mathrm{H}^{+}$ions at the anode and $\mathrm{Cu}^{2+}$ ions are reduced to copper metal at the cathode (Figure 18.4):

$$
\begin{array}{lr}
\text { Anode (oxidation): } & \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \\
\text {Cathode (reduction): } & \mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cu}(s) \\
\text { Overall cell reaction: } & \mathrm{H}_{2}(g)+\mathrm{Cu}^{2+}(a q) \longrightarrow 2 \mathrm{H}^{+}(a q)+\mathrm{Cu}(s)
\end{array}
$$



FIGURE 18.4 A galvanic cell consisting of a $\mathrm{Cu}^{2+}(1 \mathrm{M}) / \mathrm{Cu}$ half-cell and a standard hydrogen electrode (S.H.E.). The S.H.E. is a piece of platinum foil that is in contact with bubbles of $\mathrm{H}_{2}(g)$ at 1 atm pressure and with $\mathrm{H}^{+}(a q)$ at 1 M concentration. Electrons flow from the S.H.E. (anode) to the copper cathode. The measured standard cell potential at $25^{\circ} \mathrm{C}$ is 0.34 V .

Every reduction half-cell reaction has a corresponding standard reduction potential, $E^{\circ}$ red. If the reaction is reversed, it becomes an oxidation half-cell reaction with a corresponding standard oxidation half-cell potential, $E_{o x}^{\circ}$. For any given half-cell reaction, $E^{\circ}{ }_{o x}=-E^{\circ}{ }_{\text {red }}$.
[We represent the hydrated proton as $\mathrm{H}^{+}(a q)$ rather than $\mathrm{H}_{3} \mathrm{O}^{+}(a q)$ because we're interested here in electron transfer, not proton transfer as in Chapter 15.] The standard potential for this cell, 0.34 V at $25^{\circ} \mathrm{C}$, is a measure of the combined driving forces of the oxidation and reduction half-reactions:

$$
E_{\text {cell }}^{\circ}=E_{\mathrm{ox}}^{\circ}+E_{\text {red }}^{\circ}=E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}^{\circ}+E^{\circ} \mathrm{Cu}^{2+} \rightarrow \mathrm{Cu}=0.34 \mathrm{~V}
$$

If we could determine $E^{\circ}$ values for individual half-reactions, we could combine those values to obtain $E^{\circ}$ values for a host of cell reactions. Unfortunately, it's not possible to measure the potential of a single electrode; we can measure only a potential difference by placing a voltmeter between two electrodes. Nevertheless, we can develop a set of standard half-cell potentials by choosing an arbitrary standard half-cell as a reference point, assigning it an arbitrary potential, and then expressing the potential of all other half-cells relative to the reference half-cell. Recall that this same approach was used in Section 8.10 for determining standard enthalpies of formation, $\Delta H_{\mathrm{f}}{ }_{\mathrm{f}}$.

To define an electrochemical "sea level," chemists have chosen a reference halfcell called the standard hydrogen electrode (S.H.E., shown in Figure 18.4). It consists of a platinum electrode in contact with $\mathrm{H}_{2}$ gas and aqueous $\mathrm{H}^{+}$ions at standard-state conditions [ $1 \mathrm{~atm} \mathrm{H}_{2}(g), 1 \mathrm{M} \mathrm{H}^{+}(a q), 25^{\circ} \mathrm{C}$ ]. The corresponding half-reaction, written in either direction, is assigned an arbitrary potential of exactly 0 V :

$$
\begin{array}{ll}
2 \mathrm{H}^{+}(a q, 1 \mathrm{M})+2 \mathrm{e}^{-} \longrightarrow \mathrm{H}_{2}(g, 1 \mathrm{~atm}) & E^{\circ}=0 \mathrm{~V} \\
\mathrm{H}_{2}(g, 1 \mathrm{~atm}) \longrightarrow 2 \mathrm{H}^{+}(a q, 1 \mathrm{M})+2 \mathrm{e}^{-} & E^{\circ}=0 \mathrm{~V}
\end{array}
$$

With this choice of standard reference electrode, the entire potential of the cell

$$
\operatorname{Pt}(s)\left|\mathrm{H}_{2}(1 \mathrm{~atm})\right| \mathrm{H}^{+}(1 \mathrm{M}) \| \mathrm{Cu}^{2+}(1 \mathrm{M}) \mid \mathrm{Cu}(s)
$$

can be attributed to the $\mathrm{Cu}^{2+} / \mathrm{Cu}$ half-cell:

Because the $\mathrm{Cu}^{2+} / \mathrm{Cu}$ half-reaction is a reduction, the corresponding half-cell potential, $E^{\circ}=0.34 \mathrm{~V}$, is called a standard reduction potential:

$$
\mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cu}(s) \quad \text { Standard reduction potential: } E^{\circ}=0.34 \mathrm{~V}
$$

In a cell in which this half-reaction occurs in the opposite direction, the corresponding half-cell potential has the same magnitude but opposite sign:

$$
\mathrm{Cu}(s) \longrightarrow \mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} \quad E^{\circ}=-0.34 \mathrm{~V}
$$

Whenever the direction of a half-reaction is reversed, the sign of $E^{\circ}$ must also be reversed. Thus, the standard potential for an oxidation half-reaction is the negative of the standard reduction potential.

We can determine standard potentials for other half-cells simply by constructing galvanic cells in which each half-cell of interest is paired up with the S.H.E. For example, to find the potential of a half-cell consisting of a zinc electrode dipping into a $1 \mathrm{M} \mathrm{Zn}^{2+}$ solution, we would build the cell shown in Figure 18.5. The voltmeter-electrode connections required to get a positive reading on the voltmeter ( 0.76 V ) tell us that the zinc electrode is the anode and the S.H.E. is the cathode. Therefore, the half-cell reactions involve oxidation of Zn and reduction of $\mathrm{H}^{+}$. Alternatively, we could identify the direction of the half-reactions by noting that the $\mathrm{H}^{+}$concentration decreases as the reaction progresses.

$$
\begin{array}{lll}
\text { Anode (oxidation): } & \mathrm{Zn}(s) \longrightarrow \mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-} & E^{\circ}=? \\
\text { Cathode (reduction): } & 2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{H}_{2}(g) & E^{\circ}=0 \mathrm{~V} \\
\text { Overall cell reaction: } & \mathrm{Zn}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{H}_{2}(g) & E^{\circ}=0.76 \mathrm{~V}
\end{array}
$$



Voltaic Cells II: The Zinc-Hydrogen Cell movie

FIGURE 18.5 A galvanic cell consisting of a $\mathrm{Zn} / \mathrm{Zn}^{2+}$ (1 M) half-cell and a standard hydrogen electrode. Electrons flow from the zinc anode to the S.H.E. (cathode). The measured standard cell potential at $25^{\circ} \mathrm{C}$ is 0.76 V .
J. J. Fortman and R. Battino, "Determining the Metal Activity Series Using a Potato Porcupine," J. Chem. Educ., Vol. 70, 1993, 939. Pieces of metal are inserted into a potato. A voltmeter is attached to a given metal and a copper reference electrode. With the potato serving as a salt bridge and source of electrolytes, the observed cell potentials are used to rank the metals in an activity series.

The more positive the halfcell potential, the greater the tendency for the reaction to occur as written. The more negative the half-cell potential, the greater the tendency for the reverse reaction to occur.


Since the anode and cathode half-cell potentials must sum to give the overall cell potential, the $E^{\circ}$ value for oxidation of Zn to $\mathrm{Zn}^{2+}$ must be 0.76 V and the standard reduction potential for the $\mathrm{Zn}^{2+} / \mathrm{Zn}$ half-cell is therefore -0.76 V .

We could also have calculated the standard reduction potential for the $\mathrm{Zn}^{2+} / \mathrm{Zn}$ half-cell from the observed standard potential of the Daniell cell ( 1.10 V ) and the standard reduction potential for the $\mathrm{Cu}^{2+} / \mathrm{Cu}$ half-cell $(0.34 \mathrm{~V})$ :

| Anode (oxidation): | $\mathrm{Zn}(s) \longrightarrow \mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-}$ | $E^{\circ}=?$ <br> Cathode (reduction): <br> Overall cell reaction: |
| :--- | :---: | :--- |
| $\mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cu}(s)$ | $\mathrm{Zn}(s)+\mathrm{Cu}^{2+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{Cu}(s)$ | $E^{\circ}=0.34 \mathrm{~V}$ |
| $E^{\circ}=1.10 \mathrm{~V}$ |  |  |

Since $1.10 \mathrm{~V}=0.76 \mathrm{~V}+0.34 \mathrm{~V}$, we would again conclude that the $E^{\circ}$ value for oxidation of Zn to $\mathrm{Zn}^{2+}$ is 0.76 V and the standard reduction potential for the $\mathrm{Zn}^{2+} / \mathrm{Zn}$ half-cell is therefore -0.76 V .

From experiments of the sort just described, hundreds of half-cell potentials have been determined. A short list is presented in Table 18.1, and a more complete tabulation is given in Appendix D. The following conventions are observed when constructing a table of half-cell potentials:

- The half-reactions are written as reductions rather than as oxidations. This means that oxidizing agents and electrons are on the left side of each half-reaction and reducing agents are on the right side.
- The listed half-cell potentials are standard reduction potentials, also known as standard electrode potentials.
- The half-reactions are listed in order of decreasing standard reduction potential (decreasing tendency to occur in the forward direction; increasing tendency to occur in the reverse direction). Consequently, the strongest oxidizing agents are located in the upper left of the table ( $\mathrm{F}_{2}, \mathrm{H}_{2} \mathrm{O}_{2}, \mathrm{MnO}_{4}{ }^{-}$, and so forth), and the strongest reducing agents are found in the lower right of the table ( $\mathrm{Li}, \mathrm{Na}, \mathrm{Mg}$, and so forth).
By choosing $E^{\circ}=0 \mathrm{~V}$ for the standard hydrogen electrode, we obtain standard reduction potentials that range from about +3 V to -3 V .

Note how the ordering of the half-reactions in Table 18.1 corresponds to their ordering in the activity series in Table 4.3 (page 132). The more active metals at the top of the activity series have the more positive oxidation potentials and therefore the more negative standard reduction potentials.

TABLE 18.1 Standard Reduction Potentials at $25^{\circ} \mathrm{C}$

|  | Reduction Half-Reaction |  | $\mathbf{E}^{\circ}$ <br> (V) |  |
| :---: | :---: | :---: | :---: | :---: |
| Stronger oxidizing agent | $\mathrm{F}_{2}(\mathrm{~g})+2 \mathrm{e}^{-}$ | $\longrightarrow 2 \mathrm{~F}(\mathrm{aq})$ | 2.87 | Weaker reducing agent |
|  | $\mathrm{H}_{2} \mathrm{O}_{2}(a q)+2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)$ | 1.78 |  |
|  | $\mathrm{MnO}_{4}^{-(a q)}+8 \mathrm{H}^{+}(a q)+5 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Mn}^{2+}(a q)+4 \mathrm{H}_{2} \mathrm{O}(l)$ | 1.51 |  |
|  | $\mathrm{Cl}_{2}(\mathrm{~g})+2 \mathrm{e}^{-}$ | $\longrightarrow 2 \mathrm{Cl}^{-}(a q)$ | 1.36 |  |
|  | $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-}$ | $\longrightarrow 2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l)$ | 1.33 |  |
|  | $\mathrm{O}_{2}(\mathrm{~g})+4 \mathrm{H}^{+}(a q)+4 \mathrm{e}^{-}$ | $\longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)$ | 1.23 |  |
|  | $\mathrm{Br}_{2}(l)+2 \mathrm{e}^{-}$ | $\longrightarrow 2 \mathrm{Br}^{-}(a q)$ | 1.09 |  |
|  | $\mathrm{Ag}^{+}(a q)+\mathrm{e}^{-}$ | $\longrightarrow \mathrm{Ag}(\mathrm{s})$ | 0.80 |  |
|  | $\mathrm{Fe}^{3+}(a q)+\mathrm{e}^{-}$ | $\longrightarrow \mathrm{Fe}^{2+}(a q)$ | 0.77 |  |
|  | $\mathrm{O}_{2}(\mathrm{~g})+2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{H}_{2} \mathrm{O}_{2}(\mathrm{aq})$ | 0.70 |  |
|  | $\mathrm{I}_{2}(\mathrm{~s})+2 \mathrm{e}^{-}$ | $\longrightarrow 2 \mathrm{I}^{-}(\mathrm{aq})$ | 0.54 |  |
|  | $\mathrm{O}_{2}(\mathrm{~g})+2 \mathrm{H}_{2} \mathrm{O}(l)+4 \mathrm{e}^{-}$ | $\longrightarrow 4 \mathrm{OH}^{-}(a q)$ | 0.40 |  |
|  | $\mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Cu}(\mathrm{s})$ | 0.34 |  |
|  | $\mathrm{Sn}^{4+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Sn}^{2+}(a q)$ | 0.15 |  |
|  | $2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{H}_{2}(\mathrm{~g})$ | 0 |  |
|  | $\mathrm{Pb}^{2+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Pb}(\mathrm{s})$ | -0.13 |  |
|  | $\mathrm{Ni}^{2+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Ni}(\mathrm{s})$ | -0.26 |  |
|  | $\mathrm{Cd}^{2+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Cd}(\mathrm{s})$ | -0.40 |  |
|  | $\mathrm{Fe}^{2+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Fe}(\mathrm{s})$ | -0.45 |  |
|  | $\mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Zn}(\mathrm{s})$ | -0.76 |  |
|  | $2 \mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{H}_{2}(\mathrm{~g})+2 \mathrm{OH}^{-}(a q)$ | -0.83 |  |
|  | $\mathrm{Al}^{3+}(a q)+3 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Al}(\mathrm{s})$ | -1.66 |  |
|  | $\mathrm{Mg}^{2+}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{Mg}(\mathrm{s})$ | -2.37 |  |
| oxidizing | $\mathrm{Na}^{+}(a q)+\mathrm{e}^{-}$ | $\longrightarrow \mathrm{Na}(\mathrm{s})$ | -2.71 | reducing |
| agent | $\mathrm{Li}^{+}(a q)+\mathrm{e}^{-}$ | $\longrightarrow \mathrm{Li}(\mathrm{s})$ | -3.04 | agent |

PROBLEM 18.6 The standard potential for the following galvanic cell is 0.92 V :

$$
\operatorname{Al}(s)\left|\mathrm{Al}^{3+}(a q) \| \mathrm{Cr}^{3+}(a q)\right| \mathrm{Cr}(s)
$$

Look up the standard reduction potential for the $\mathrm{Al}^{3+} / \mathrm{Al}$ half-cell in Table 18.1, and calculate the standard reduction potential for the $\mathrm{Cr}^{3+} / \mathrm{Cr}$ half-cell.

## 18.5 | Using Standard Reduction Potentials

A table of standard reduction potentials summarizes an enormous amount of chemical information in a very small space. It enables us to arrange oxidizing or reducing agents in order of increasing strength, and it permits us to predict the spontaneity or nonspontaneity of thousands of redox reactions. Suppose, for example, that the table contains just 100 half-reactions. We can pair each reduction half-reaction with any one of the remaining 99 oxidation half-reactions to give a total of $100 \times 99=9900$ cell reactions. By calculating the $E^{\circ}$ values for these cell reactions, we would find that half of them are spontaneous and the other half are nonspontaneous. (Can you see why?)

To illustrate how to use the tabulated $E^{\circ}$ values, let's calculate $E^{\circ}$ for the oxidation of $\mathrm{Zn}(s)$ by $\mathrm{Ag}^{+}(a q)$ :

$$
2 \mathrm{Ag}^{+}(a q)+\mathrm{Zn}(s) \longrightarrow 2 \mathrm{Ag}(s)+\mathrm{Zn}^{2+}(a q)
$$

Richard S. Treptow, "Dental Filling Discomforts Illustrate Electrochemical Potentials of Metals," J. Chem. Educ., Vol. 55, 1978, 189.


Half-cell potentials are never multiplied by a coefficient when used in the equation $E^{\circ}{ }_{\text {cell }}=E^{\circ}{ }_{\text {ox }}+E^{\circ}{ }_{\text {red }}$.

TWhen predicting whether a reaction is spontaneous using Table 18.1, some students find it useful to circle the two potential reactants and connect them with a line. If the line has a negative slope, the reaction is spontaneous; if the line has a positive slope, the reaction is nonspontaneous. If both potential reactants are on the same side of the arrows, no reaction can occur because an oxidation requires a simultaneous reduction.

First, we find the relevant half-reactions in Table 18.1 and write them in the appropriate direction for reduction of $\mathrm{Ag}^{+}$and oxidation of Zn . Next, we add the halfreactions to get the overall reaction. Before adding, though, we must multiply the $\mathrm{Ag}^{+} / \mathrm{Ag}$ half-reaction by a factor of 2 so that the electrons will cancel:

Reduction:
Oxidation:
Overall reaction:

$$
\begin{aligned}
2 \times\left[\mathrm{Ag}^{+}(a q)+\mathrm{e}^{-}\right. & \longrightarrow \mathrm{Ag}(s)] \\
\mathrm{Zn}(s) \longrightarrow \mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-} &
\end{aligned} \begin{aligned}
& E^{\circ}=0.80 \mathrm{~V} \\
& 2 \mathrm{Ag}^{+}(a q)+\mathrm{Zn}(s) \longrightarrow 2 \mathrm{Ag}(s)+\mathrm{Zn}^{2+}(a q)
\end{aligned} \begin{aligned}
& E^{\circ}=-(-0.76 \mathrm{~V}) \\
& E^{\circ}=1.56 \mathrm{~V}
\end{aligned}
$$

Then, we tabulate the $E^{\circ}$ values for the half-reactions, remembering that $E^{\circ}$ for oxidation of zinc is the negative of the standard reduction potential ( -0.76 V ). We do not multiply the $E^{\circ}$ value for reduction of $\mathrm{Ag}^{+}(0.80 \mathrm{~V})$ by a factor of 2 , however, because an electrical potential does not depend on how much reaction occurs.

The reason why $E^{\circ}$ values are independent of the amount of reaction can be understood by looking at the equation $\Delta G^{\circ}=-n F E^{\circ}$. Free energy is an extensive property (Section 1.4) because it depends on the amount of substance. If we double the amount of $\mathrm{Ag}^{+}$reduced, the free-energy change, $\Delta G^{\circ}$, doubles. The number of electrons transferred, $n$, also doubles, however, so the ratio $E^{\circ}=-\Delta G^{\circ} / n F$ is constant. Electrical potential is therefore an intensive property, which does not depend on the amount of substance.

The $E^{\circ}$ value for the overall reaction of $\mathrm{Zn}(s)$ with $\mathrm{Ag}^{+}(a q)$ is the sum of the $E^{\circ}$ values for the two half-reactions: $0.80 \mathrm{~V}+0.76 \mathrm{~V}=1.56 \mathrm{~V}$. Because $E^{\circ}$ is positive (and $\Delta G^{\circ}$ is negative), oxidation of zinc by $\mathrm{Ag}^{+}$is a spontaneous reaction under standard-state conditions. Just as $\mathrm{Ag}^{+}$can oxidize Zn , it's evident from Table 18.1 that $\mathrm{Ag}^{+}$can oxidize any reducing agent that lies below it in the table ( $\mathrm{Fe}^{2+}, \mathrm{H}_{2} \mathrm{O}_{2}, \mathrm{I}^{-}$, and so forth). The sum of $E^{\circ}$ for the $\mathrm{Ag}^{+} / \mathrm{Ag}$ reduction $(0.80 \mathrm{~V}$ ) and $-E^{\circ}$ for any half-reaction that lies below the $\mathrm{Ag}^{+} / \mathrm{Ag}$ half-reaction always gives a positive $E^{\circ}$ for the overall reaction.

In general, an oxidizing agent can oxidize any reducing agent that lies below it in the table but can't oxidize a reducing agent that appears above it in the table. Thus, $\mathrm{Ag}^{+}$can't oxidize $\mathrm{Br}^{-}, \mathrm{H}_{2} \mathrm{O}, \mathrm{Cr}^{3+}$, and so forth because $E^{\circ}$ for the overall reaction is negative. Simply by glancing at the locations of the oxidizing and reducing agents in the table, we can predict whether a reaction is spontaneous or nonspontaneous.

## Worked Example 18.4

(a) Arrange the following oxidizing agents in order of increasing strength under standard-state conditions: $\mathrm{Br}_{2}(l), \mathrm{Fe}^{3+}(a q), \mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q)$.
(b) Arrange the following reducing agents in order of increasing strength under standard-state conditions: $\mathrm{Al}(\mathrm{s}), \mathrm{Na}(\mathrm{s}), \mathrm{Zn}(\mathrm{s})$.

## Strategy

Pick out the half-reactions in Table 18.1 that involve the given oxidizing or reducing agents, and list them, along with their $E^{\circ}$ values, in the order in which they occur in the table. The strength of an oxidizing agent increases as the $E^{\circ}$ value increases, and the strength of a reducing agent increases as the $E^{\circ}$ value decreases.

## Solution

(a) List the half-reactions that involve $\mathrm{Br}_{2}, \mathrm{Fe}^{3+}$, and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ in the order in which they occur in Table 18.1:

$$
\begin{array}{ll}
\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l) & E^{\circ}=1.33 \mathrm{~V} \\
\mathrm{Br}_{2}(l)+2 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Br}^{-}(a q) & E^{\circ}=1.09 \mathrm{~V} \\
\mathrm{Fe}^{3+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Fe}^{2+}(a q) & E^{\circ}=0.77 \mathrm{~V}
\end{array}
$$

We can see that $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ has the greatest tendency to be reduced (largest $E^{\circ}$ ), and $\mathrm{Fe}^{3+}$ has the least tendency to be reduced (smallest $E^{\circ}$ ). The species that has the greatest tendency to be reduced is the strongest oxidizing agent, so oxidizing strength increases in the order $\mathrm{Fe}^{3+}<\mathrm{Br}_{2}<\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$. As a shortcut, simply note that the strength of the oxidizing agents, listed on the left side of Table 18.1, increases on moving up in the table.
(b) List the half-reactions that involve $\mathrm{Al}(s), \mathrm{Na}(s)$, and $\mathrm{Zn}(s)$ in the order in which they occur in Table 18.1:

$$
\begin{array}{ll}
\mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Zn}(s) & E^{\circ}=-0.76 \mathrm{~V} \\
\mathrm{Al}^{3+}(a q)+3 \mathrm{e}^{-} \longrightarrow \mathrm{Al}(s) & E^{\circ}=-1.66 \mathrm{~V} \\
\mathrm{Na}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Na}(s) & E^{\circ}=-2.71 \mathrm{~V}
\end{array}
$$

The last half-reaction has the least tendency to occur in the forward direction (most negative $E^{\circ}$ ) and the greatest tendency to occur in the reverse direction. Therefore, Na is the strongest reducing agent, and reducing strength increases in the order $\mathrm{Zn}<\mathrm{Al}<\mathrm{Na}$. As a shortcut, note that the strength of the reducing agents, listed on the right side of Table 18.1, increases on moving down the table.

## Worked Example 18.5

Predict from Table 18.1 whether $\mathrm{Pb}^{2+}(a q)$ can oxidize $\mathrm{Al}(s)$ or $\mathrm{Cu}(s)$ under standardstate conditions. Calculate $E^{\circ}$ for each reaction at $25^{\circ} \mathrm{C}$.

## Strategy

To predict whether a redox reaction is spontaneous, remember that an oxidizing agent can oxidize any reducing agent that lies below it in the table but can't oxidize one that lies above it. To calculate $E^{\circ}$ for a redox reaction, sum the $E^{\circ}$ values for the reduction and oxidation half-reactions.

## Solution

$\mathrm{Pb}^{2+}(a q)$ is above $\mathrm{Al}(s)$ in the table but below $\mathrm{Cu}(s)$. Therefore, $\mathrm{Pb}^{2+}(a q)$ can oxidize $\mathrm{Al}(s)$ but can't oxidize $\mathrm{Cu}(s)$. To confirm these predictions, calculate $E^{\circ}$ values for the overall reactions.

For the oxidation of Al by $\mathrm{Pb}^{2+}, E^{\circ}$ is positive $(1.53 \mathrm{~V})$ and the reaction is therefore spontaneous:

$$
\begin{array}{cl}
3 \times\left[\mathrm{Pb}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Pb}(s)\right] & E^{\circ}=-0.13 \mathrm{~V} \\
2 \times\left[\mathrm{Al}(s) \longrightarrow \mathrm{Al}^{3+}(a q)+3 \mathrm{e}^{-}\right] & E^{\circ}=1.66 \mathrm{~V} \\
\hline 3 \mathrm{~Pb}^{2+}(a q)+2 \mathrm{Al}(s) \longrightarrow 3 \mathrm{~Pb}(s)+2 \mathrm{Al}^{3+}(a q) &
\end{array}
$$

Note that we have multiplied the $\mathrm{Pb}^{2+} / \mathrm{Pb}$ half-reaction by a factor of 3 and the $\mathrm{Al} / \mathrm{Al}^{3+}$ half-reaction by a factor of 2 so that the electrons will cancel, but we do not multiply the $E^{\circ}$ values by these factors because electrical potential is an intensive property.

For the oxidation of Cu by $\mathrm{Pb}^{2+}, E^{\circ}$ is negative $(-0.47 \mathrm{~V})$, and the reaction is therefore nonspontaneous:

$$
\begin{aligned}
\mathrm{Pb}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Pb}(s) & E^{\circ}=-0.13 \mathrm{~V} \\
\mathrm{Cu}(s) \longrightarrow \mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} & \underline{E^{\circ}=-0.34 \mathrm{~V}} \\
\hline \mathrm{~Pb}^{2+}(a q)+\mathrm{Cu}(s) \longrightarrow \mathrm{Pb}(s)+\mathrm{Cu}^{2+}(a q) & E^{\circ}=-0.47 \mathrm{~V}
\end{aligned}
$$

PROBLEM 18.7 Which is the stronger oxidizing agent, $\mathrm{Cl}_{2}(g)$ or $\mathrm{Ag}^{+}(a q)$ ? Which is the stronger reducing agent, $\mathrm{Fe}(s)$ or $\mathrm{Mg}(s)$ ?

PROBLEM 18.8 Predict from Table 18.1 whether each of the following reactions can occur under standard-state conditions:
(a) $2 \mathrm{Fe}^{3+}(a q)+2 \mathrm{I}^{-}(a q) \rightarrow 2 \mathrm{Fe}^{2+}(a q)+\mathrm{I}_{2}(s)$
(b) $3 \mathrm{Ni}(s)+2 \mathrm{Al}^{3+}(a q) \rightarrow 3 \mathrm{Ni}^{2+}(a q)+2 \mathrm{Al}(s)$

Confirm your predictions by calculating the value of $E^{\circ}$ for each reaction. Which reaction(s) can occur in the reverse direction under standard-state conditions?

KEY CONCEPT PROBLEM 18.9 Consider the following table of standard reduction potentials:

| Reduction Half-Reaction | $\boldsymbol{E}^{\circ}(\mathbf{V})$ |
| :--- | ---: |
| $\mathrm{A}^{3+}+2 \mathrm{e}^{-} \rightarrow \mathrm{A}^{+}$ | 1.47 |
| $\mathrm{~B}^{2+}+2 \mathrm{e}^{-} \rightarrow \mathrm{B}$ | 0.60 |
| $\mathrm{C}^{2+}+2 \mathrm{e}^{-} \rightarrow \mathrm{C}$ | -0.21 |
| $\mathrm{D}^{+}+\mathrm{e}^{-} \rightarrow \mathrm{D}$ | -1.38 |

(a) Which substance is the strongest reducing agent? Which is the strongest oxidizing agent?
(b) Which substances can be oxidized by $\mathrm{B}^{2+}$ ? Which can be reduced by C ?
(c) Write a balanced equation for the overall cell reaction that delivers the highest voltage, and calculate $E^{\circ}$ for the reaction.

### 18.6 Cell Potentials and Composition of the Reaction Mixture: The Nernst Equation

Cell potentials, like free-energy changes (Section 17.10), depend on temperature and on the composition of the reaction mixture-that is, on the concentrations of solutes and the partial pressures of gases. This dependence can be derived from the equation

$$
\Delta G=\Delta G^{\circ}+R T \ln Q
$$

Recall from Section 17.10 that $\Delta G$ is the free-energy change for a reaction under nonstandard-state conditions, $\Delta G^{\circ}$ is the free-energy change under standard-state conditions, and $Q$ is the reaction quotient. Since $\Delta G=-n F E$ and $\Delta G^{\circ}=-n F E^{\circ}$, we can rewrite the equation for $\Delta G$ in the form

$$
-n F E=-n F E^{\circ}+R T \ln Q
$$

Dividing by $-n F$, we obtain the Nernst equation, named after Walther Nernst (1864-1941), the German chemist who first derived it:

$$
\text { Nernst equation } \quad E=E^{\circ}-\frac{R T}{n F} \ln Q \quad \text { or } \quad E=E^{\circ}-\frac{2.303 R T}{n F} \log Q
$$

Because of an intimate connection between the cell voltage and pH (Section 18.7), we will write the Nernst equation in terms of base- 10 logarithms. At $25^{\circ} \mathrm{C}$, $2.303 R T / F$ has a value of 0.0592 V , and therefore

$$
E=E^{\circ}-\frac{0.0592 \mathrm{~V}}{n} \log Q \quad \text { in volts, at } 25^{\circ} \mathrm{C}
$$

In actual galvanic cells, the concentrations and partial pressures of reactants and products seldom have standard-state values, and the values change as the
cell reaction proceeds. The Nernst equation is useful because it enables us to calculate cell potentials under nonstandard-state conditions, as shown in Worked Example 18.6.

## Worked Example 18.6

Consider a galvanic cell that uses the reaction

$$
\mathrm{Zn}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{H}_{2}(g)
$$



Calculate the cell potential at $25^{\circ} \mathrm{C}$ when $\left[\mathrm{H}^{+}\right]=1.0 \mathrm{M},\left[\mathrm{Zn}^{2+}\right]=0.0010 \mathrm{M}$, and $P_{\mathrm{H}_{2}}=0.10 \mathrm{~atm}$.

## Strategy

We can calculate the standard cell potential $E^{\circ}$ from the standard reduction potentials in Table 18.1. Then we use the Nernst equation to find the cell potential $E$ under the cited conditions.

## Solution

The standard cell potential is

$$
E^{\circ}=E^{\circ} \mathrm{Zn} \rightarrow \mathrm{Zn}^{2+}+E^{\circ} \mathrm{H}^{+} \rightarrow \mathrm{H}_{2}=-(-0.76 \mathrm{~V})+0 \mathrm{~V}=0.76 \mathrm{~V}
$$

The cell potential at $25^{\circ} \mathrm{C}$ under nonstandard-state conditions is given by the Nernst equation:

$$
\begin{aligned}
E & =E^{\circ}-\frac{0.0592 \mathrm{~V}}{n} \log Q \\
& =E^{\circ}-\left(\frac{0.0592 \mathrm{~V}}{n}\right)\left(\log \frac{\left[\mathrm{Zn}^{2+}\right]\left(P_{\mathrm{H}_{2}}\right)}{\left[\mathrm{H}^{+}\right]^{2}}\right)
\end{aligned}
$$

where the reaction quotient contains both molar concentrations of solutes and the partial pressure of a gas (in atm). As usual, zinc has been omitted from the reaction quotient because it's a pure solid. For this reaction, 2 mol of electrons are transferred, so $n=2$. Substituting into the Nernst equation the appropriate values of $E^{\circ}, n$, $\left[\mathrm{H}^{+}\right],\left[\mathrm{Zn}^{2+}\right]$, and $P_{\mathrm{H}_{2}}$ gives

$$
\begin{aligned}
E & =(0.76 \mathrm{~V})-\left(\frac{0.0592 \mathrm{~V}}{2}\right)\left(\log \frac{(0.0010)(0.10)}{(1.0)^{2}}\right)=(0.76 \mathrm{~V})-\left(\frac{0.0592 \mathrm{~V}}{2}\right)(-4.0) \\
& =0.76 \mathrm{~V}+0.12 \mathrm{~V} \\
& =0.88 \mathrm{~V} \text { at } 25^{\circ} \mathrm{C}
\end{aligned}
$$

$\checkmark$ Ballpark Check Qualitatively, we expect that the reaction will have a greater tendency to occur under the cited conditions than under standard-state conditions because the product concentrations are lower than standard-state values. We therefore predict that the cell potential $E$ will be greater than the standard cell potential $E^{\circ}$, in agreement with the solution.

- PROBLEM 18.10 Consider a galvanic cell that uses the reaction

$$
\mathrm{Cu}(s)+2 \mathrm{Fe}^{3+}(a q) \longrightarrow \mathrm{Cu}^{2+}(a q)+2 \mathrm{Fe}^{2+}(a q)
$$

What is the potential of a cell at $25^{\circ} \mathrm{C}$ that has the following ion concentrations?

$$
\left[\mathrm{Fe}^{3+}\right]=1.0 \times 10^{-4} \mathrm{M} \quad\left[\mathrm{Cu}^{2+}\right]=0.25 \mathrm{M} \quad\left[\mathrm{Fe}^{2+}\right]=0.20 \mathrm{M}
$$

## Worked Example 18.7

Consider the following galvanic cell:

(a) What is the quantitative change in the cell voltage on increasing the ion concentrations in the anode compartment by a factor of 10 ?
(b) What is the quantitative change in the cell voltage on increasing the ion concentrations in the cathode compartment by a factor of 10 ?

## Strategy

The direction of electron flow in the picture tells us that lead is the anode and silver is the cathode. Therefore, the cell reaction is $\mathrm{Pb}(s)+2 \mathrm{Ag}^{+}(a q) \rightarrow \mathrm{Pb}^{2+}(a q)+2 \mathrm{Ag}(s)$. The cell potential at $25^{\circ} \mathrm{C}$ is given by the Nernst equation, where $n=2$ and $Q=$ $\left[\mathrm{Pb}^{2+}\right] /\left[\mathrm{Ag}^{+}\right]^{2}$ :

$$
\begin{aligned}
E & =E^{\circ}-\frac{0.0592 \mathrm{~V}}{n} \log Q \\
& =E^{\circ}-\left(\frac{0.0592 \mathrm{~V}}{2}\right)\left(\log \frac{\left[\mathrm{Pb}^{2+}\right]}{\left[\mathrm{Ag}^{+}\right]^{2}}\right)
\end{aligned}
$$

The change in $E$ on changing the ion concentrations will be determined by the change in the log term in the Nernst equation.

## Solution

(a) $\mathrm{Pb}^{2+}$ is in the anode compartment, and $\mathrm{Ag}^{+}$is in the cathode compartment. Suppose that the original concentrations of $\mathrm{Pb}^{2+}$ and $\mathrm{Ag}^{+}$are 1 M , so that $E=E^{\circ}$. Increasing $\left[\mathrm{Pb}^{2+}\right]$ to 10 M gives

$$
E=E^{\circ}-\left(\frac{0.0592 \mathrm{~V}}{2}\right)\left(\log \frac{(10)}{(1)^{2}}\right)
$$

Because $\log 10=1.0, E=E^{\circ}-0.03 \mathrm{~V}$. Thus, increasing the $\mathrm{Pb}^{2+}$ concentration by a factor of 10 decreases the cell voltage by 0.03 V .
(b) Increasing $\left[\mathrm{Ag}^{+}\right]$to 10 M gives

$$
E=E^{\circ}-\left(\frac{0.0592 \mathrm{~V}}{2}\right)\left(\log \frac{(1)}{(10)^{2}}\right)
$$

Because $\log (10)^{-2}=-2.0, E=E^{\circ}+0.06 \mathrm{~V}$. Thus, increasing the $\mathrm{Ag}^{+}$concentration by a factor of 10 increases the cell voltage by 0.06 V .
$\checkmark$ Ballpark Check Qualitatively, we expect that the reaction will have a lesser tendency to occur when the product ion concentration, $\left[\mathrm{Pb}^{2+}\right]$, is increased and a greater tendency to occur when the reactant ion concentration, $\left[\mathrm{Ag}^{+}\right]$, is increased. Therefore, the cell voltage $E$ will decrease when $\left[\mathrm{Pb}^{2+}\right.$ ] is increased and will increase when $\left[\mathrm{Ag}^{+}\right]$is increased. The ballpark check and the solution agree.

KEY CONCEPT PROBLEM 18.11 Consider the following galvanic cell:

(a) What is the quantitative change in the cell voltage on decreasing the ion concentrations in the anode compartment by a factor of $100 ?$
(b) What is the quantitative change in the cell voltage on decreasing the ion concentrations in the cathode compartment by a factor of $100 ?$

### 18.7 Electrochemical Determination of pH

The electrochemical determination of pH using a pH meter is a particularly important application of the Nernst equation. Consider, for example, a cell with a hydrogen electrode as the anode and a second reference electrode as the cathode:

$$
\mathrm{Pt}\left|\mathrm{H}_{2}(1 \mathrm{~atm})\right| \mathrm{H}^{+}(? \mathrm{M}) \| \text { Reference cathode }
$$

The hydrogen electrode consists of a platinum wire that is in contact with $\mathrm{H}_{2}$ at 1 atm and dips into a solution of unknown pH . The potential of this cell is

$$
E_{\text {cell }}=E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}+E_{\text {ref }}
$$

We can calculate the potential for the hydrogen electrode half-reaction

$$
\mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-}
$$

by applying the Nernst equation to this half-reaction:

$$
E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}=\left(E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}^{\circ}\right)-\left(\frac{0.0592 \mathrm{~V}}{n}\right)\left(\log \frac{\left[\mathrm{H}^{+}\right]^{2}}{P_{\mathrm{H}_{2}}}\right)
$$

Since $E^{\circ}=0 \mathrm{~V}$ for the standard hydrogen electrode, $n=2$, and $P_{\mathrm{H}_{2}}=1 \mathrm{~atm}$, we can rewrite this equation as

$$
E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}=-\left(\frac{0.0592 \mathrm{~V}}{2}\right)\left(\log \left[\mathrm{H}^{+}\right]^{2}\right)
$$

[^20]Further, because $\log \left[\mathrm{H}^{+}\right]^{2}=2 \log \left[\mathrm{H}^{+}\right]$and $-\log \left[\mathrm{H}^{+}\right]=\mathrm{pH}$, the half-cell potential for the hydrogen electrode is directly proportional to the pH :

$$
\begin{aligned}
E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}} & =-\left(\frac{0.0592 \mathrm{~V}}{2}\right)(2)\left(\log \left[\mathrm{H}^{+}\right]\right)=(0.0592 \mathrm{~V})\left(-\log \left[\mathrm{H}^{+}\right]\right) \\
& =(0.0592 \mathrm{~V})(\mathrm{pH})
\end{aligned}
$$

The overall cell potential is

$$
E_{\text {cell }}=(0.0592 \mathrm{~V})(\mathrm{pH})+E_{\mathrm{ref}}
$$

and the pH is therefore a linear function of the cell potential:

$$
\mathrm{pH}=\frac{E_{\mathrm{cell}}-E_{\mathrm{ref}}}{0.0592 \mathrm{~V}}
$$

A higher cell potential indicates a higher pH , meaning that we can measure the pH of a solution simply by measuring $E_{\text {cell }}$.

In actual pH measurements, a glass electrode replaces the cumbersome hydrogen electrode and a calomel electrode is used as the reference. A glass electrode consists of a silver wire coated with silver chloride that dips into a reference solution of dilute hydrochloric acid (Figure 18.6). The hydrochloric acid is separated from the test solution of unknown pH by a thin glass membrane. For rugged applications, the exterior of the electrode is made of an epoxy resin, which protects the glass tip. A calomel electrode consists of mercury(I) chloride ( $\mathrm{Hg}_{2} \mathrm{Cl}_{2}$, calomel) in contact with liquid mercury and aqueous KCl . The cell half-reactions are

$$
\begin{array}{cl}
2 \times\left[\mathrm{Ag}(s)+\mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{AgCl}(s)+\mathrm{e}^{-}\right] & E^{\circ}=-0.22 \mathrm{~V} \\
\mathrm{Hg}_{2} \mathrm{Cl}_{2}(s)+2 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Hg}(l)+2 \mathrm{Cl}^{-}(a q) & E^{\circ}=0.28 \mathrm{~V}
\end{array}
$$



The overall cell potential, $E_{\text {cell }}$, depends not only on the potentials of these two half-reactions but also on the boundary potential that develops across the thin glass membrane separating the reference HCl solution from the test solution. Because the boundary potential depends linearly on the difference in the pH of the solutions on the two sides of the membrane, the pH of the test solution can be determined by measuring $E_{\text {cell }}$. The cell potential is measured with a pH meter, a voltage-measuring device that electronically converts $E_{\text {cell }}$ to pH and displays the result in pH units.

## Worked Example 18.8

The following cell has a potential of 0.55 V at $25^{\circ} \mathrm{C}$ :

$$
\operatorname{Pt}(s)\left|\mathrm{H}_{2}(1 \mathrm{~atm})\right| \mathrm{H}^{+}(? \mathrm{M}) \| \mathrm{Cl}^{-}(1 \mathrm{M})\left|\mathrm{Hg}_{2} \mathrm{Cl}_{2}(s)\right| \mathrm{Hg}(l)
$$

What is the pH of the solution in the anode compartment?

## Strategy

First, read the shorthand notation to obtain the cell reaction. Then, calculate the halfcell potential for the hydrogen electrode from the observed cell potential and the halfcell potential for the calomel reference electrode. Finally, apply the Nernst equation to find the pH .

## SOlution

The cell reaction is

$$
\mathrm{H}_{2}(g)+\mathrm{Hg}_{2} \mathrm{Cl}_{2}(s) \longrightarrow 2 \mathrm{H}^{+}(a q)+2 \mathrm{Hg}(l)+2 \mathrm{Cl}^{-}(a q)
$$

and the cell potential is

$$
E_{\text {cell }}=E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}+E_{\mathrm{Hg}_{2} \mathrm{Cl}_{2} \rightarrow \mathrm{Hg}}=0.55 \mathrm{~V}
$$

Because the reference electrode is the standard calomel electrode, which has $E=$ $E^{\circ}=0.28 \mathrm{~V}$ (Appendix D ), the half-cell potential for the hydrogen electrode is 0.27 V :

$$
E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}=E_{\text {cell }}-E_{\mathrm{Hg}_{2} \mathrm{Cl}_{2} \rightarrow \mathrm{Hg}}=0.55 \mathrm{~V}-0.28 \mathrm{~V}=0.27 \mathrm{~V}
$$

We can then apply the Nernst equation to the half-reaction $\mathrm{H}_{2}(g) \rightarrow 2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-}$:

$$
E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}=\left(E_{\mathrm{H}_{2} \rightarrow \mathrm{H}^{+}}^{\circ}\right)-\left(\frac{0.0592 \mathrm{~V}}{n}\right)\left(\log \frac{\left[\mathrm{H}^{+}\right]^{2}}{P_{\mathrm{H}_{2}}}\right)
$$

Substituting in the values of $E, E^{\circ}, n$, and $P_{\mathrm{H}_{2}}$ gives

$$
0.27 \mathrm{~V}=(0 \mathrm{~V})-\left(\frac{0.0592 \mathrm{~V}}{2}\right)\left(\log \frac{\left[\mathrm{H}^{+}\right]^{2}}{1}\right)=(0.0592 \mathrm{~V})(\mathrm{pH})
$$

Therefore, the pH is

$$
\mathrm{pH}=\frac{0.27 \mathrm{~V}}{0.0592 \mathrm{~V}}=4.6
$$

- PROBLEM 18.12 What is the pH of the solution in the anode compartment of the following cell if the measured cell potential at $25^{\circ} \mathrm{C}$ is 0.28 V ?

$$
\operatorname{Pt}(s)\left|\mathrm{H}_{2}(1 \mathrm{~atm})\right| \mathrm{H}^{+}(? \mathrm{M}) \| \mathrm{Pb}^{2+}(1 \mathrm{M}) \mid \mathrm{Pb}(s)
$$

The more positive the standard cell potential, the larger the value of the equilibrium constant, and the farther the equilibrium lies to the right.

### 18.8 Standard Cell Potentials and Equilibrium Constants

We saw in Section 18.3 that the standard free-energy change for a reaction is related to the standard cell potential by the equation

$$
\Delta G^{\circ}=-n F E^{\circ}
$$

In addition, we showed in Section 17.11 that the standard free-energy change is also related to the equilibrium constant for the reaction:

$$
\Delta G^{\circ}=-R T \ln K
$$

Combining these two equations, we obtain

$$
-n F E^{\circ}=-R T \ln K
$$

or

$$
E^{\circ}=\frac{R T}{n F} \ln K=\frac{2.303 R T}{n F} \log K
$$

Since $2.303 R T / F$ has a value of 0.0592 V at $25^{\circ} \mathrm{C}$, we can rewrite this equation in the simplified form

$$
E^{\circ}=\frac{0.0592 \mathrm{~V}}{n} \log K \quad \text { in volts, at } 25^{\circ} \mathrm{C}
$$

Very small concentrations are difficult to measure, so the determination of an equilibrium constant from concentration measurements is not feasible when $K$ is either very large or very small. Standard cell potentials, however, are relatively easy to measure. Consequently, the most common use of this equation is in calculating equilibrium constants from standard cell potentials.

As an example, let's calculate the value of $K$ for the reaction in the Daniell cell:

$$
\mathrm{Zn}(s)+\mathrm{Cu}^{2+}(a q) \longrightarrow \mathrm{Zn}^{2+}(a q)+\mathrm{Cu}(s)
$$

Solving the equation for $\log K$ and substituting in the appropriate values of $E^{\circ}$ and $n$, we obtain

$$
\begin{aligned}
E^{\circ} & =\frac{0.0592 \mathrm{~V}}{n} \log K \\
\log K & =\frac{n E^{\circ}}{0.0592 \mathrm{~V}}=\frac{(2)(1.10 \mathrm{~V})}{0.0592 \mathrm{~V}}=37.2
\end{aligned}
$$

Therefore, $K$ is the antilog of 37.2 (Appendix A.2):

$$
K=\operatorname{antilog} 37.2=10^{37.2}=2 \times 10^{37} \quad \text { at } 25^{\circ} \mathrm{C}
$$

Because the equilibrium constant is a very large number, the reaction goes essentially to completion. When $\left[\mathrm{Zn}^{2+}\right]=1 \mathrm{M}$, for example, $\left[\mathrm{Cu}^{2+}\right]$ is less than $10^{-37} \mathrm{M}$.

The preceding calculation shows that even a relatively small value of $E^{\circ}$ $(+1.10 \mathrm{~V})$ corresponds to a huge value of $K\left(2 \times 10^{37}\right)$. A positive value of $E^{\circ}$ corresponds to a positive value of $\log K$ and therefore $K>1$, and a negative value of $E^{\circ}$ corresponds to a negative value of $\log K$ and therefore $K<1$. Because the standard reduction potentials in Table 18.1 span a range of about $6 \mathrm{~V}, E^{\circ}$ for a redox reaction can range from +6 V for reaction of the strongest oxidizing agent with the strongest reducing agent to -6 V for reaction of the weakest oxidizing agent with the weakest reducing agent. However, $E^{\circ}$ values outside the range +3 V to -3 V are uncommon. For the case of $n=2$, the correspondence between the values of $E^{\circ}$ and $K$ is indicated in Figure 18.7. Equilibrium constants for redox reactions tend to be either very large or very small compared to equilibrium constants for


4 FIGURE 18.7 The relationship between the equilibrium constant $K$ for a redox reaction with $n=2$ and the standard cell potential $E^{\circ}$. Note that $K$ is plotted on a logarithmic scale.
acid-base reactions, which are in the range of $10^{14}$ to $10^{-14}$. Redox reactions typically go either essentially to completion ( $K$ is very large) or almost not at all ( $K$ is very small).

In previous chapters, we discussed two different ways to determine the value of an equilibrium constant $K$ : from concentration data (Section 13.2) and from thermochemical data (Section 17.11). In this section, we've added a third way: from electrochemical data. The following are the key relationships needed for each approach:

1. $K$ from concentration data for solutes: $K=\frac{[\mathrm{C}]^{c}[\mathrm{D}]^{d}}{[\mathrm{~A}]^{a}[\mathrm{~B}]^{b}}$
2. $K$ from thermochemical data: $\Delta G^{\circ}=-R T \ln K ; \ln K=\frac{-\Delta G^{\circ}}{R T}$
3. $K$ from electrochemical data: $E^{\circ}=\frac{R T}{n F} \ln K ; \quad \ln K=\frac{n F E^{\circ}}{R T}$

## Worked EXample 18.9

Use the standard reduction potentials in Table 18.1 to calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for the reaction

$$
6 \mathrm{Br}^{-}(a q)+\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q) \longrightarrow 3 \mathrm{Br}_{2}(l)+2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l)
$$

## Strategy

Calculate $E^{\circ}$ for the reaction from standard reduction potentials, as in Worked Example 18.5. Then use the equation $\log K=n E^{\circ} / 0.0592 \mathrm{~V}$ to determine the equilibrium constant.

## Solution

Find the relevant half-reactions in Table 18.1, and write them in the proper direction for oxidation of $\mathrm{Br}^{-}$and reduction of $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}$. Before adding the half-reactions to get the overall reaction, multiply the $\mathrm{Br}^{-} / \mathrm{Br}_{2}$ half-reaction by a factor of 3 so that the electrons will cancel:

| $3 \times\left[2 \mathrm{Br}^{-}(a q)\right.$ | $\left.\longrightarrow \mathrm{Br}_{2}(l)+2 \mathrm{e}^{-}\right]$ |
| :---: | :--- |
| $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l)$ | $E^{\circ}=-1.09 \mathrm{~V}$ |
| $6 \mathrm{Br}^{-}(a q)+\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q)+14 \mathrm{H}^{+}(a q) \longrightarrow 3 \mathrm{Br}_{2}(l)+2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l)$ |  |$\quad$| $E^{\circ}=1.33 \mathrm{~V}$ |
| :--- |
| $E^{\circ}=0.24 \mathrm{~V}$ |

A multicell battery is comprised of galvanic cells wired in series, so the battery voltage equals the sum of the voltages of the individual cells.

Michael J. Smith and Colin A. Vincent, "Structure and Content of Some Primary Batteries," J. Chem. Educ., Vol. 78, 2001, 519-521.

Note that $E^{\circ}$ for the $\mathrm{Br}^{-} / \mathrm{Br}_{2}$ oxidation is the negative of the tabulated standard reduction potential ( 1.09 V ), and remember that we don't multiply this $E^{\circ}$ value by a factor of 3 because electrical potential is an intensive property. The $E^{\circ}$ value for the overall reaction is the sum of the $E^{\circ}$ values for the half-reactions: $-1.09 \mathrm{~V}+1.33 \mathrm{~V}=0.24 \mathrm{~V}$. To calculate the equilibrium constant, use the relation between $\log K$ and $n E^{\circ}$, with $n=6$ :

$$
\log K=\frac{n E^{\circ}}{0.0592 \mathrm{~V}}=\frac{(6)(0.24 \mathrm{~V})}{0.0592 \mathrm{~V}}=24 \quad K=1 \times 10^{24} \quad \text { at } 25^{\circ} \mathrm{C}
$$

$\checkmark$ BALLPARK CHECK $E^{\circ}$ is positive, so $K$ should be greater than 1 , in agreement with the solution.

- PROBLEM 18.13 Use the data in Table 18.1 to calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for the reaction

$$
4 \mathrm{Fe}^{2+}(a q)+\mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q) \longrightarrow 4 \mathrm{Fe}^{3+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

PROBLEM 18.14 What is the value of $E^{\circ}$ for a redox reaction involving the transfer of 2 mol of electrons if its equilibrium constant is $1.8 \times 10^{-5}$ (the value of the aciddissociation constant $K_{\mathrm{a}}$ for acetic acid)?

## 18.9 | Batteries

By far the most important practical application of galvanic cells is their use as batteries. In multicell batteries, such as those in automobiles, the individual galvanic cells are linked in series, with the anode of each cell connected to the cathode of the adjacent cell. The voltage provided by the battery is the sum of the individual cell voltages. The features required in a battery depend on the application. In general, however, a commercially successful battery should be compact, lightweight, physically rugged, and inexpensive, and it must provide a stable source of power for relatively long periods of time. Battery design is an active area of research that requires considerable ingenuity as well as a solid understanding of electrochemistry.

Let's look at several of the most common types of commercial batteries.

## Lead Storage Battery

The lead storage battery is perhaps the most familiar of all galvanic cells because it has been used as a reliable source of power for starting automobiles for more than three-quarters of a century. A typical 12 V battery consists of six cells connected in series, each cell providing a potential of about 2 V . The cell design is illustrated in Figure 18.8. The anode, a series of lead grids packed with spongy lead, and the cathode, a second series of grids packed with lead dioxide, dip into the electrolyte, an aqueous solution of sulfuric acid ( $38 \%$ by weight). When the cell is discharging (providing current), the electrode half-reactions and the overall cell reaction are:

| Anode: | $\mathrm{Pb}(s)+\mathrm{HSO}_{4}{ }^{-}(a q)$ | $\longrightarrow \mathrm{PbSO}_{4}(s)+\mathrm{H}^{+}(a q)+2 \mathrm{e}^{-}$ | $E^{\circ}=0.296 \mathrm{~V}$ |
| :---: | :---: | :---: | :---: |
| Cathode: | $\mathrm{PbO}_{2}(s)+3 \mathrm{H}^{+}(a q)+\mathrm{HSO}_{4}^{-}(a q)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{PbSO}_{4}(s)+2 \mathrm{H}_{2} \mathrm{O}(l)$ | $E^{\circ}=1.628 \mathrm{~V}$ |
| Overall: | (s) $+\mathrm{PbO}_{2}(s)+2 \mathrm{H}^{+}(a q)+2 \mathrm{HSO}_{4}^{-}(a q)$ | $\longrightarrow 2 \mathrm{PbSO}_{4}(s)+2 \mathrm{H}_{2} \mathrm{O}(l)$ | $E^{\circ}=1.924 \mathrm{~V}$ |

Gerald Ondrey, Charlene Crabb, and Takeshi Kamiya, "Batteries: Full Speed Ahead," Chem. Eng., Vol. 106 (2), 1999, 47-51.
(These equations contain $\mathrm{HSO}_{4}{ }^{-}$ions because $\mathrm{SO}_{4}{ }^{2-}$ is protonated in strongly acidic solutions.)

Lead is oxidized to lead sulfate at the anode, and lead dioxide is reduced to lead sulfate at the cathode. The cell doesn't need to have separate anode and cathode compartments because the oxidizing and reducing agents are both solids $\left(\mathrm{PbO}_{2}\right.$ and Pb$)$ that are kept from coming in contact by the presence of insulating spacers between the grids.


Because the reaction product (solid $\mathrm{PbSO}_{4}$ ) adheres to the surface of the electrodes, a "run-down" lead storage battery can be recharged by using an external source of direct current to drive the cell reaction in the reverse, nonspontaneous direction. In an automobile, the battery is continuously recharged by a device called an alternator, which is driven by the engine.

A lead storage battery typically provides good service for several years, but eventually mechanical shock from driving over rough roads dislodges the $\mathrm{PbSO}_{4}$ from the electrodes. Then it's no longer possible to recharge the battery, and it must be replaced.

## Dry-Cell Batteries

The common household batteries used as power sources for flashlights, portable radios, and tape recorders use the dry cell, or Leclanché cell, patented in 1866 by the Frenchman George Leclanché. A dry-cell battery has a zinc metal can, which serves as the anode, and an inert graphite rod surrounded by a paste of solid manganese dioxide and carbon black, which functions as the cathode (Figure 18.9). Surrounding the $\mathrm{MnO}_{2}$-containing paste is the electrolyte, a moist paste of ammonium chloride and zinc chloride in starch. The dry cell is not completely dry but gets its name because the electrolyte is a viscous, aqueous paste rather than a liquid solution. The electrode reactions,


4 FIGURE 18.9 Leclanché dry cell and a cutaway view.

FIGURE 18.8 A lead storage battery and a cutaway view of one cell. Each electrode consists of several grids with a large surface area so that the battery can deliver the high currents required to start an automobile engine. The electrolyte is aqueous sulfuric acid.

which are rather complicated, can be represented in simplified form by the following equations:
Anode: $\quad \mathrm{Zn}(s) \longrightarrow \mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-}$
Cathode: $\quad 2 \mathrm{MnO}_{2}(s)+2 \mathrm{NH}_{4}{ }^{+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Mn}_{2} \mathrm{O}_{3}(s)+2 \mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l)$


A FIGURE 18.10 A small mercury battery and a cutaway view.

This cell provides a potential of about 1.5 V , but the potential deteriorates to about 0.8 V as the cell is used.

The alkaline dry cell is a modified version of the Leclanché cell in which the acidic $\mathrm{NH}_{4} \mathrm{Cl}$ electrolyte of the Leclanché cell is replaced by a basic electrolyte, either NaOH or KOH . As in the Leclanché cell, the electrode reactions involve oxidation of zinc and reduction of manganese dioxide, but the oxidation product is zinc oxide, as is appropriate to the basic conditions:

$$
\begin{array}{ll}
\text { Anode: } & \mathrm{Zn}(s)+2 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{ZnO}(s)+\mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-} \\
\text {Cathode: } & 2 \mathrm{MnO}_{2}(s)+\mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Mn}_{2} \mathrm{O}_{3}(s)+2 \mathrm{OH}^{-}(a q)
\end{array}
$$

Corrosion of the zinc anode is a significant side reaction under acidic conditions because zinc reacts with $\mathrm{H}^{+}(a q)$ to give $\mathrm{Zn}^{2+}(a q)$ and $\mathrm{H}_{2}(g)$. Under basic conditions, however, the cell has a longer life because zinc corrodes more slowly. The alkaline cell also produces higher power and more stable current and voltage because of more efficient ion transport in the alkaline electrolyte.

Closely related to the alkaline dry cell is the mercury battery, often used in watches, heart pacemakers, and other devices where a battery of small size is required (Figure 18.10). The anode of the mercury battery is zinc, as in the alkaline dry cell, but the cathode is steel in contact with mercury(II) oxide ( HgO ) in an alkaline medium of KOH and $\mathrm{Zn}(\mathrm{OH})_{2}$. Zinc is oxidized at the anode, and HgO is reduced at the cathode:

$$
\begin{array}{ll}
\text { Anode: } & \mathrm{Zn}(s)+2 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{ZnO}(s)+\mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-} \\
\text {Cathode: } & \mathrm{HgO}(s)+\mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Hg}(l)+2 \mathrm{OH}^{-}(a q)
\end{array}
$$

Even though mercury batteries can be made very small, they still produce a stable potential (about 1.3 V ) for long periods of time. When possible, used mercury batteries should be recycled to recover the mercury because of its toxicity.

## Nickel-Cadmium Batteries

Nickel-cadmium, or "ni-cad," batteries are popular for use in calculators and portable power tools because, unlike most other dry-cell batteries, they are rechargeable (Figure 18.11). The anode of a ni-cad battery is cadmium metal, and the cathode is the nickel(III) compound $\mathrm{NiO}(\mathrm{OH})$ supported on nickel metal. The electrode reactions are

$$
\begin{array}{ll}
\text { Anode: } & \mathrm{Cd}(s)+2 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{Cd}(\mathrm{OH})_{2}(s)+2 \mathrm{e}^{-} \\
\text {Cathode: } & \mathrm{NiO}(\mathrm{OH})(s)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{e}^{-} \longrightarrow \mathrm{Ni}(\mathrm{OH})_{2}(s)+\mathrm{OH}^{-}(a q)
\end{array}
$$

FIGURE 18.11 Rechargeable nickel-cadmium, or ni-cad, storage batteries.

$\mathrm{Ni}-$ cad batteries can be recharged many times because the solid products of the electrode reactions adhere to the surface of the electrodes.

## Lithium Batteries

Rechargeable lithium batteries may prove to be the batteries of the future because of their light weight and high voltage (about 3.0 V). More than 900 million were sold in 2001, with production doubling annually. Lithium has a higher $E^{\circ}$ value for oxidation than any other metal, and only 6.94 g of lithium is needed to provide 1 mol of electrons. Lithium batteries consist of a lithium anode-either lithium metal itself or lithium atoms inserted into a graphite electrode-a metal oxide or metal sulfide cathode that can incorporate $\mathrm{Li}^{+}$ions, and an electrolyte that contains a lithium salt, such as $\mathrm{LiClO}_{4}$, in an organic solvent. Solid-state polymer electrolytes that can transport $\mathrm{Li}^{+}$ions have also been used. When the cathode material is $\mathrm{MnO}_{2}$, for example, the electrode reactions are

$$
\begin{array}{ll}
\text { Anode: } & \mathrm{Li}(s) \longrightarrow \mathrm{Li}^{+}+\mathrm{e}^{-} \\
\text {Cathode: } & \mathrm{MnO}_{2}(s)+\mathrm{Li}^{+}+\mathrm{e}^{-} \longrightarrow \mathrm{LiMnO}_{2}(s)
\end{array}
$$

Lithium batteries are now used in cell phones, laptop computers, and cameras.

## Fuel Cells

A fuel cell is a galvanic cell in which one of the reactants is a traditional fuel such as methane or hydrogen. A fuel cell differs from an ordinary battery in that the reactants are not contained within the cell but instead are continuously supplied from an external reservoir. Perhaps the best-known example is the hydrogen-oxygen fuel cell, which is used as a source of electric power in space vehicles (Figure 18.12). This cell contains porous carbon electrodes impregnated with metallic catalysts and an electrolyte consisting of hot, aqueous KOH . The fuel (gaseous $\mathrm{H}_{2}$ ) and the oxidizing agent (gaseous $\mathrm{O}_{2}$ ) don't react directly but instead flow into separate cell compartments where $\mathrm{H}_{2}$ is oxidized at the anode and $\mathrm{O}_{2}$ is reduced at the cathode. The overall cell reaction is simply the conversion of hydrogen and oxygen to water:

$$
\begin{array}{lc}
\text { Anode: } & 2 \mathrm{H}_{2}(g)+4 \mathrm{OH}^{-}(a q) \longrightarrow 4 \mathrm{H}_{2} \mathrm{O}(l)+4 \mathrm{e}^{-} \\
\text {Cathode: } & \mathrm{O}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)+4 \mathrm{e}^{-} \longrightarrow 4 \mathrm{OH}^{-}(a q) \\
\text { Overall: } & 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)
\end{array}
$$

To date, large-scale applications of fuel cells have been limited because of cost, although the Tokyo Electric Power Company in Japan is now operating an


4 FIGURE 18.12 A hydrogen-oxygen fuel cell. Gaseous $\mathrm{H}_{2}$ is oxidized to water at the anode, and gaseous $\mathrm{O}_{2}$ is reduced to hydroxide ion at the cathode. The net reaction is the conversion of $\mathrm{H}_{2}$ and $\mathrm{O}_{2}$ to water.

© This environmentally clean, fuel-cell powered electric bus runs on compressed hydrogen. Its only exhaust gas is water.


A The steel support column of this bridge has corroded because the iron has been oxidized by moist air, yielding $\mathrm{Fe}_{2} \mathrm{O}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$ (rust).

11 MW fuel-cell power plant capable of supplying power to about 4000 households. Future applications include use as the power source in environmentally clean electric vehicles. Several fuel-cell powered buses have been tested in Chicago, and by 2004 DaimlerChrysler and Ford expect to be selling passenger cars that are powered by hydrogen-oxygen fuel cells.

- PROBLEM 18.15 Write a balanced equation for the overall cell reaction in each of the following batteries:
(a) Leclanché dry cell
(b) Alkaline dry cell
(c) Mercury battery
(d) Nickel-cadmium battery


## $18.10 \mid$ Corrosion

Corrosion is the oxidative deterioration of a metal, such as the conversion of iron to rust, a hydrated iron(III) oxide of approximate composition $\mathrm{Fe}_{2} \mathrm{O}_{3} \cdot \mathrm{H}_{2} \mathrm{O}$. The rusting of iron has enormous economic consequences. It has been estimated that as much as one-fourth of the steel produced in the United States goes to replace steel structures and products that have been destroyed by corrosion.

To prevent corrosion, we first have to understand how it occurs. One important fact is that the rusting of iron requires both oxygen and water; it doesn't occur in oxygen-free water or in dry air. Another clue is the observation that rusting involves pitting of the metal surface, but the rust is deposited at a location physically separated from the pits. This suggests that rust does not form by direct reaction of iron and oxygen, but rather by an electrochemical process in which iron is oxidized in one region of the surface and oxygen is reduced in another region.

A possible mechanism for rusting, consistent with the known facts, is illustrated in Figure 18.13. The surface of the iron and a droplet of surface water constitute a tiny galvanic cell in which different regions of the surface act as anode and cathode while the aqueous phase serves as the electrolyte. Iron is oxidized more readily in some regions (anode regions) than in others (cathode regions) because the composition of the metal is somewhat inhomogeneous and the surface is irregular. Factors such as impurities, phase boundaries, and mechanical stress may influence the ease of oxidation in a particular region of the surface.


Corrosion activity

- FIGURE 18.13 An electrochemical mechanism for corrosion of iron. The metal and a surface water droplet constitute a tiny galvanic cell in which iron is oxidized to $\mathrm{Fe}^{2+}$ in a region of the surface (anode region) remote from atmospheric $\mathrm{O}_{2}$, and $\mathrm{O}_{2}$ is reduced near the edge of the droplet at another region of the surface (cathode region). Electrons flow from anode to cathode through the metal, while ions flow through the water droplet. Dissolved $\mathrm{O}_{2}$ oxidizes $\mathrm{Fe}^{2+}$ further to $\mathrm{Fe}^{3+}$ before it is deposited as rust $\left(\mathrm{Fe}_{2} \mathrm{O}_{3} \cdot \mathrm{H}_{2} \mathrm{O}\right)$.

At an anode region, iron is oxidized to $\mathrm{Fe}^{2+}$ ions,

$$
\mathrm{Fe}(s) \longrightarrow \mathrm{Fe}^{2+}(a q)+2 \mathrm{e}^{-} \quad E^{\circ}=0.45 \mathrm{~V}
$$

while at a cathode region, oxygen is reduced to water:

$$
\mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q)+4 \mathrm{e}^{-} \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l) \quad E^{\circ}=1.23 \mathrm{~V}
$$

The actual potential for the reduction half-reaction is less than the standard potential $(1.23 \mathrm{~V})$ because the water droplet is not 1 M in $\mathrm{H}^{+}$ions. (In fact, the water is only slightly acidic because the main source of $\mathrm{H}^{+}$ions is the reaction of water with dissolved atmospheric carbon dioxide.) Even at pH 7 , however, the potential for the reduction half-reaction is 0.81 V , which means that the cell potential is highly positive, indicative of a spontaneous reaction.

The electrons required for reduction of $\mathrm{O}_{2}$ at the cathode region are supplied by a current that flows through the metal from the more easily oxidized anode region (Figure 18.13). The electrical circuit is completed by migration of ions in the water droplet. When $\mathrm{Fe}^{2+}$ ions migrate away from the pitted anode region, they come in contact with $\mathrm{O}_{2}$ dissolved in the surface portion of the water droplet and are further oxidized to $\mathrm{Fe}^{3+}$ ions:

$$
4 \mathrm{Fe}^{2+}(a q)+\mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q) \longrightarrow 4 \mathrm{Fe}^{3+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

Iron(III) forms a very insoluble hydrated oxide even in moderately acidic solutions, and the iron(III) is deposited as the familiar red-brown material that we call rust:

$$
2 \mathrm{Fe}^{3+}(a q)+4 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Fe}_{2} \mathrm{O}_{3} \cdot \mathrm{H}_{2} \mathrm{O}(s)+6 \mathrm{H}^{+}(a q)
$$

An electrochemical mechanism for corrosion also explains nicely why automobiles rust more rapidly in parts of the country where road salt is used to melt snow and ice. Dissolved salts in the water droplet greatly increase the conductivity of the electrolyte, thus accelerating the pace of corrosion.

A glance at a table of standard reduction potentials indicates that the $\mathrm{O}_{2} / \mathrm{H}_{2} \mathrm{O}$ half-reaction lies above the $\mathrm{M}^{n+} / \mathrm{M}$ half-reaction for nearly all metals, so $\mathrm{O}_{2}$ can oxidize all metals except a few, such as gold and platinum. Aluminum, for example, has $E^{\circ}=-1.66 \mathrm{~V}$ for the $\mathrm{Al}^{3+} / \mathrm{Al}$ half-reaction and is oxidized more readily than iron. In other words, the corrosion of aluminum products such as aircraft and automobile parts, window frames, cooking utensils, and soda cans should be a serious problem. Fortunately, it isn't, because oxidation of aluminum gives a very hard, almost impenetrable film of $\mathrm{Al}_{2} \mathrm{O}_{3}$ that adheres to the surface of the metal and protects it from further attack. Other metals such as magnesium, chromium, titanium, and zinc form similar protective oxide coatings. In the case of iron, however, rust is too porous to shield the underlying metal from further oxidation.


This titanium bicycle doesn't corrode because of a hard, impenetrable layer of $\mathrm{TiO}_{2}$ that adheres to the surface and protects the metal from further oxidation. tion of Corrosion Susceptibility of a Metal: Student Corrosion Experiment II," J. Chem. Educ., Vol. 65, 1988, 934.

VAlthough many metals react more readily than iron to form oxides, their oxides provide a protective coating against further corrosion. The corrosion product of iron ("rust") flakes off and exposes a fresh surface to further corrosion.

FIGURE 18.14 A layer of zinc protects iron from oxidation, even when the zinc layer becomes scratched. The zinc (anode), iron (cathode), and water droplet (electrolyte) constitute a tiny galvanic cell. Oxygen is reduced at the cathode, and zinc is oxidized at the anode, thus protecting the iron from oxidation.

四In an electrolytic cell a constant input of energy from an external direct current (dc) source, such as a battery, is used to drive a nonspontaneous reaction. The voltage of the battery must be more positive than the absolute value of the voltage for the electrolysis reaction.

## Prevention of Corrosion

Corrosion of iron can be prevented, or at least minimized, by shielding the metal surface from oxygen and moisture. A coat of paint is effective for a while, but rust begins to form as soon as the paint is scratched or chipped. Metals such as chromium, tin, or zinc afford a more durable surface coating for iron. The steel used in making automobiles, for example, is coated by dipping into a bath of molten zinc, a process known as galvanizing. As the potentials indicate, zinc is oxidized more easily than iron, and therefore, when the metal is oxidized, zinc is oxidized instead of iron. Any incipient oxidation of iron would be reversed immediately because Zn can reduce $\mathrm{Fe}^{2+}$ to Fe . As long as the zinc and iron are in contact, the zinc protects the iron from oxidation even if the zinc layer becomes scratched (Figure 18.14).

$$
\begin{array}{ll}
\mathrm{Fe}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Fe}(s) & E^{\circ}=-0.45 \mathrm{~V} \\
\mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Zn}(s) & E^{\circ}=-0.76 \mathrm{~V}
\end{array}
$$



The technique of protecting a metal from corrosion by connecting it to a second metal that is more easily oxidized is called cathodic protection. It's unnecessary to cover the entire surface of the metal with a second metal, as in galvanizing iron. All that's required is electrical contact with the second metal. An underground steel pipeline, for example, can be protected by connecting it through an insulated wire to a stake of magnesium, which acts as a sacrificial anode and corrodes instead of the iron. In effect, the arrangement is a galvanic cell in which the easily oxidized magnesium acts as the anode, the pipeline behaves as the cathode, and moist soil is the electrolyte. The cell half-reactions are
Anode: $\quad \mathrm{Mg}(s) \longrightarrow \mathrm{Mg}^{2+}(a q)+2 \mathrm{e}^{-} \quad E^{\circ}=2.37 \mathrm{~V}$
Cathode: $\quad \mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q)+4 \mathrm{e}^{-} \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l) \quad E^{\circ}=1.23 \mathrm{~V}$
For large steel structures such as pipelines, storage tanks, bridges, and ships, cathodic protection is the best defense against premature rusting.

- PROBLEM 18.16 Magnesium is often attached to the steel hulls of ships to protect the steel from rusting. Write balanced equations for the corrosion reactions that occur (a) in the presence of Mg and (b) in the absence of Mg .


### 18.11 Electrolysis and Electrolytic Cells

Thus far, we've been concerned only with galvanic cells-electrochemical cells in which a spontaneous redox reaction produces an electric current. A second important kind of electrochemical cell is the electrolytic cell, in which an electric current is used to drive a nonspontaneous reaction. Thus, the processes occurring in galvanic and electrolytic cells are the reverse of each other: A galvanic cell converts
chemical energy to electrical energy when a reaction with a positive value of $E$ (and a negative value of $\Delta G$ ) proceeds toward equilibrium; an electrolytic cell converts electrical energy to chemical energy when an electric current drives a reaction with a negative value of $E$ (and a positive value of $\Delta G$ ) in a direction away from equilibrium.

The process of using an electric current to bring about chemical change is called electrolysis. The opposite signs of $E$ and $\Delta G=-n F E$ for the two kinds of cells are summarized in Table 18.2, along with the situation for a reaction that has reached equilibrium-a dead battery!

| TABLE 18.2 | Relationship Between Cell Potentials $E$ and <br> Free-Energy Changes $\Delta G$ |  |  |
| :--- | :---: | :---: | :--- |
| Reaction Type | $\boldsymbol{E}$ | $\Delta \boldsymbol{G}$ | Cell Type |
| Spontaneous | + | - | Galvanic |
| Nonspontaneous | - | + | Electrolytic |
| Equilibrium | 0 | 0 | Dead battery |

## Electrolysis of Molten Sodium Chloride

An electrolytic cell has two electrodes that dip into an electrolyte and are connected to a battery or some other source of direct electric current. A cell for electrolysis of molten sodium chloride, for example, is illustrated in Figure 18.15. The battery serves as an electron pump, pushing electrons into one electrode and pulling them out of the other. The negative electrode attracts $\mathrm{Na}^{+}$cations, which combine with the electrons supplied by the battery and are thereby reduced to liquid sodium metal. Similarly, the positive electrode attracts $\mathrm{Cl}^{-}$anions, which replenish the electrons removed by the battery and are thereby oxidized to chlorine gas. The electrode reactions and overall cell reaction are

$$
\begin{array}{lr}
\text { Anode (oxidation): } & \quad 2 \mathrm{Cl}^{-}(l) \longrightarrow \mathrm{Cl}_{2}(g)+2 \mathrm{e}^{-} \\
\text {Cathode (reduction): } & 2 \mathrm{Na}^{+}(l)+2 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Na}(l) \\
\text { Overall cell reaction: } & 2 \mathrm{Na}^{+}(l)+2 \mathrm{Cl}^{-}(l) \longrightarrow 2 \mathrm{Na}(l)+\mathrm{Cl}_{2}\left(\frac{l}{l}\right.
\end{array}
$$

As in a galvanic cell, the anode is the electrode where oxidation takes place, and the cathode is the electrode where reduction takes place. The signs of the


FIGURE 18.15 Electrolysis of molten sodium chloride. Chloride ions are oxidized to $\mathrm{Cl}_{2}$ gas at the anode, and $\mathrm{Na}^{+}$ ions are reduced to sodium metal at the cathode.

Bassam Z. Shakhashiri, "Electrolytic Cells in Series: A Red, White, and Blue Electrolysis," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 4 (The University of Wisconsin Press, Madison, 1992) pp.170-173.
electrodes, however, are opposite for the two kinds of cells. In a galvanic cell, the anode is considered negative because it supplies electrons to the external circuit, but in an electrolytic cell, the anode is considered positive because electrons are pulled out of it by the battery. The sign of each electrode in the electrolytic cell is the same as the sign of the battery electrode to which it is attached.

## Electrolysis of Aqueous Sodium Chloride

When an aqueous salt solution is electrolyzed, the electrode reactions may differ from those for electrolysis of the molten salt because water may be involved. In the electrolysis of aqueous sodium chloride, for example, the cathode half-reaction might be either the reduction of $\mathrm{Na}^{+}$to sodium metal, as in the case of molten sodium chloride, or the reduction of water to hydrogen gas:

$$
\begin{array}{rll}
\mathrm{Na}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Na}(s) & E^{\circ}=-2.71 \mathrm{~V} \\
2 \mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-} \longrightarrow \mathrm{H}_{2}(g)+2 \mathrm{OH}^{-}(a q) & E^{\circ}=-0.83 \mathrm{~V}
\end{array}
$$

Because the standard potential is much less negative for the reduction of water than for the reduction of $\mathrm{Na}^{+}$, water is reduced preferentially and bubbles of hydrogen gas are produced at the cathode.

The anode half-reaction might be either oxidation of $\mathrm{Cl}^{-}$to $\mathrm{Cl}_{2}$ gas, as in the case of molten sodium chloride, or oxidation of water to oxygen gas:

$$
\begin{aligned}
& 2 \mathrm{Cl}^{-}(a q) E^{\circ}=-1.36 \mathrm{~V} \\
& 2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Cl}_{2}(g)+2 \mathrm{e}^{-} \mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q)+4 \mathrm{e}^{-} \\
& E^{\circ}=-1.23 \mathrm{~V}
\end{aligned}
$$

Based on the $E^{\circ}$ values, we might expect a slight preference for oxidation of water in a solution having 1 M ion concentrations. For a neutral solution ( $\left[\mathrm{H}^{+}\right]=10^{-7} \mathrm{M}$ ), the preference for water oxidation will be even greater because its oxidation potential at pH 7 is -0.81 V . The observed product at the anode, however, is $\mathrm{Cl}_{2}$, $\operatorname{not} \mathrm{O}_{2}$, because of a phenomenon called overvoltage.

Experiments indicate that the applied voltage required for an electrolysis is always greater than the voltage calculated from standard oxidation and reduction potentials. The additional voltage required is the overvoltage. The overvoltage is needed because the magnitude of the current that passes through an electrolytic cell is often limited by the rate of electron transfer at the electrode-solution interface for one or both of the cell half-reactions. If a half-reaction has a substantial activation energy barrier for electron transfer and a correspondingly slow rate (Section 12.10), then an additional voltage, or overvoltage, must be applied to surmount the barrier and cause the reaction to proceed at a satisfactory rate. For electrode half-reactions involving solution or deposition of metals, the overvoltage is quite small, but for half-reactions involving formation of $\mathrm{O}_{2}\left(\right.$ or $\left.\mathrm{H}_{2}\right)$ gas, the overvoltage can be as large as 1 V . Present theory is unable to predict the magnitude of the overvoltage, but it's known that the overvoltage for the formation of $\mathrm{O}_{2}$ is much larger than that for the formation of $\mathrm{Cl}_{2}$. Because of overvoltage, it's sometimes difficult to predict which half-reaction will occur when $E^{\circ}$ values for the competing half-reactions are similar. In such cases, only experiment can tell what actually happens.

The observed electrode reactions and overall cell reaction for electrolysis of aqueous sodium chloride are

| Anode (oxidation): | $2 \mathrm{Cl}^{-}(a q)$ | $\longrightarrow \mathrm{Cl}_{2}(g)+2 \mathrm{e}^{-}$ | $E^{\circ}=-1.36 \mathrm{~V}$ |
| :---: | :---: | :---: | :---: |
| Cathode (reduction): | $2 \mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-}$ | $\longrightarrow \mathrm{H}_{2}(g)+2 \mathrm{OH}^{-}(a q)$ | $E^{\circ}=-0.83 \mathrm{~V}$ |
| Overall cell reaction: | $(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)$ | $\longrightarrow \mathrm{Cl}_{2}(g)+\mathrm{H}_{2}(g)+2 \mathrm{OH}^{-}(a q)$ | $E^{\circ}=-2.19 \mathrm{~V}$ |

Sodium ion acts as a spectator ion and is not involved in the electrode reactions. Thus, the sodium chloride solution is converted to a sodium hydroxide solution as the electrolysis proceeds. The minimum potential required to force this nonspontaneous reaction to occur under standard-state conditions is 2.19 V plus the overvoltage.

## Electrolysis of Water

The electrolysis of any aqueous solution requires the presence of an electrolyte to carry the current in solution. If the ions of the electrolyte are less easily oxidized and reduced than water, however, then water will react at both electrodes. Consider, for example, the electrolysis of an aqueous solution of the inert electrolyte $\mathrm{Na}_{2} \mathrm{SO}_{4}$. Water is oxidized at the anode in preference to $\mathrm{SO}_{4}{ }^{2-}$ ions and is reduced at the cathode in preference to $\mathrm{Na}^{+}$ions. The electrode and overall cell reactions are


Anode (oxidation):


If the anode and cathode solutions are mixed, the $\mathrm{H}^{+}$and $\mathrm{OH}^{-}$ions react to form water:

$$
4 \mathrm{H}^{+}(a q)+4 \mathrm{OH}^{-}(a q) \longrightarrow 4 \mathrm{H}_{2} \mathrm{O}(l)
$$

The net electrolysis reaction is therefore the decomposition of water, a process sometimes used in the laboratory to produce small amounts of pure $\mathrm{H}_{2}$ and $\mathrm{O}_{2}$ :

$$
2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g)
$$

KEY CONCEPT PROBLEM 18.17 Metallic potassium was first prepared by Humphrey Davy in 1807 by electrolysis of molten potassium hydroxide:
(a) Label the anode and cathode, and show the direction of ion flow.
(b) Write balanced equations for the anode, cathode, and overall cell reactions.

- PROBLEM 18.18 Predict the half-cell reactions that occur when aqueous solutions of the following salts are electrolyzed in a cell with inert electrodes. What is the overall cell reaction in each case?
(a) LiCl
(b) $\mathrm{CuSO}_{4}$

This procedure and the Hall-Heroult process discussed below are examples of commercial uses of a colligative property (freezing point depression) to enable electrolytic reactions to be carried out more economically.

FIGURE 18.16 Crosssectional view of a Downs cell for commercial production of sodium metal by electrolysis of molten sodium chloride. The cell design keeps the sodium and chlorine apart so that they can't react with each other.

V
Originally, chlorine was a useless byproduct of this process. The search for uses of chlorine resulted in many commercial chlorinated compounds, including plastic film used to wrap food.

### 18.12 Commercial Applications of Electrolysis

Electrolysis is used in the manufacture of many important chemicals and in numerous processes for purification and electroplating of metals. Let's look at some examples.

## Manufacture of Sodium

Sodium metal is produced commercially in a Downs cell by electrolysis of a molten mixture of sodium chloride and calcium chloride (Figure 18.16). The presence of $\mathrm{CaCl}_{2}$ allows the cell to be operated at a lower temperature because the melting point of the $\mathrm{NaCl}-\mathrm{CaCl}_{2}$ mixture (about $580^{\circ} \mathrm{C}$ ) is depressed well below that of pure $\mathrm{NaCl}\left(801^{\circ} \mathrm{C}\right)$. The liquid sodium produced at the cylindrical steel cathode is less dense than the molten salt and thus floats to the top part of the cell, where it is drawn off into a suitable container. Chlorine gas forms at the graphite anode, which is separated from the cathode by an iron screen. The cell design keeps the highly reactive sodium and chlorine away from each other and out of contact with air. Because the Downs process requires high currents (typically 25,000-40,000 A), plants for producing sodium are located near sources of inexpensive hydroelectric power, such as Niagara Falls, New York.


## Manufacture of Chlorine and Sodium Hydroxide

Production of chlorine and sodium hydroxide by electrolysis of aqueous sodium chloride is the basis of the chlor-alkali industry, a business that generates annual sales of approximately $\$ 4$ billion in the United States alone. Both chlorine and sodium hydroxide rank among the top 10 chemicals in terms of production: Annual output of each in the United States is $11-12$ million tons. Chlorine is used in water and sewage treatment and in the manufacture of plastics such as poly(vinyl chloride) (PVC). Sodium hydroxide is employed in making paper, textiles, soaps, and detergents.

Figure 18.17 shows the essential features of a membrane cell for commercial production of chlorine and sodium hydroxide. A saturated aqueous solution of

sodium chloride (brine) flows into the anode compartment, where $\mathrm{Cl}^{-}$is oxidized to $\mathrm{Cl}_{2}$ gas, and water enters the cathode compartment, where it is converted to $\mathrm{H}_{2}$ gas and $\mathrm{OH}^{-}$ions. Between the anode and cathode compartments is a special plastic membrane that is permeable to cations but not to anions or water. The membrane keeps the $\mathrm{Cl}_{2}$ and $\mathrm{OH}^{-}$ions apart but allows a current of $\mathrm{Na}^{+}$ions to flow into the cathode compartment, thus carrying the current in the solution and maintaining electrical neutrality in both compartments. The $\mathrm{Na}^{+}$and $\mathrm{OH}^{-}$ions flow out of the cathode compartment as an aqueous solution of NaOH .

## Manufacture of Aluminum

Although aluminum is the third most abundant element in the earth's crust (8.3\% by mass), it remained a rare and expensive metal until 1886 , when a 22 -year-old American, Charles Martin Hall, and a 23-year-old Frenchman, Paul Heroult, independently devised a practical process for the electrolytic production of aluminum. Still used today, the Hall-Heroult process involves electrolysis of a molten mixture of aluminum oxide $\left(\mathrm{Al}_{2} \mathrm{O}_{3}\right)$ and cryolite $\left(\mathrm{Na}_{3} \mathrm{AlF}_{6}\right)$ at about $1000^{\circ} \mathrm{C}$ in a cell with graphite electrodes (Figure 18.18). Electrolysis of pure $\mathrm{Al}_{2} \mathrm{O}_{3}$ is impractical because it melts at a very high temperature $\left(2045^{\circ} \mathrm{C}\right)$, and electrolysis of aqueous $\mathrm{Al}^{3+}$ solutions is not feasible because water is reduced in preference to $\mathrm{Al}^{3+}$ ions. Thus, the use of cryolite as a solvent for $\mathrm{Al}_{2} \mathrm{O}_{3}$ is the key to the success of the Hall-Heroult process.

The electrode reactions are still not fully understood, but they probably involve complex anions of the type $\mathrm{AlF}_{x} \mathrm{O}_{y}{ }^{+3-x-2 y}$, formed by the reaction of $\mathrm{Al}_{2} \mathrm{O}_{3}$ and $\mathrm{Na}_{3} \mathrm{AlF}_{6}$. The complex anions are reduced at the cathode to molten aluminum metal and are oxidized at the anode to $\mathrm{O}_{2}$ gas, which reacts with the graphite anodes to give $\mathrm{CO}_{2}$ gas. As a result, the anodes are chewed up rapidly and must be replaced frequently. The cell operates at a low voltage ( $5-6 \mathrm{~V}$ ) but with very high currents (up to $250,000 \mathrm{~A}$ ) because 1 mol of electrons produces only 9.0 g of aluminum. Electrolytic production of aluminum is the largest single consumer of electricity in the United States today, making recycling of aluminum products highly desirable.

FIGURE 18.17 A membrane cell for electrolytic production of $\mathrm{Cl}_{2}$ and NaOH . Chloride ion is oxidized to $\mathrm{Cl}_{2}$ gas at the anode, and water is converted to $\mathrm{H}_{2}$ gas and $\mathrm{OH}^{-}$ ions at the cathode. Sodium ions move from the anode compartment to the cathode compartment through a cationpermeable membrane. Reactants (brine and water) enter the cell, and products $\left(\mathrm{Cl}_{2}\right.$ gas, $\mathrm{H}_{2}$ gas, aqueous NaOH , and depleted brine) leave through appropriately placed pipes.

FIGURE 18.18 An electrolytic cell for production of aluminum by the Hall-Heroult process. Molten aluminum metal forms at the graphite cathode that lines the cell. Because molten aluminum is more dense than the $\mathrm{Al}_{2} \mathrm{O}_{3}-\mathrm{Na}_{3} \mathrm{AlF}_{6}$ mixture, it collects at the bottom of the cell and is drawn off periodically.



## Electrorefining and Electroplating

The purification of a metal by means of electrolysis is called electrorefining. For example, impure copper obtained from ores is converted to pure copper in an electrolytic cell that has impure copper as the anode and pure copper as the cathode (Figure 18.19). The electrolyte is an aqueous solution of copper sulfate.

© FIGURE 18.19 Electrorefining of copper metal. (a) Alternating slabs of impure copper and pure copper serve as the electrodes in electrolytic cells for the refining of copper. (b) Copper is transferred through the $\mathrm{CuSO}_{4}$ solution from the impure Cu anode to the pure Cu cathode. More easily oxidized impurities ( $\mathrm{Zn}, \mathrm{Fe} \mathrm{)} \mathrm{remain} \mathrm{in} \mathrm{solution} \mathrm{as} \mathrm{cations}$, noble metal impurities $(\mathrm{Ag}, \mathrm{Au}, \mathrm{Pt})$ are not oxidized and collect as anode mud.

At the impure Cu anode, copper is oxidized along with more easily oxidized metallic impurities such as zinc and iron. Less easily oxidized impurities such as silver, gold, and platinum fall to the bottom of the cell as anode mud, which is reprocessed to recover the precious metals. At the pure Cu cathode, $\mathrm{Cu}^{2+}$ ions are reduced to pure copper metal, but the less easily reduced metal ions $\left(\mathrm{Zn}^{2+}, \mathrm{Fe}^{2+}\right.$, and so forth) remain in the solution.

$$
\begin{array}{ll}
\text { Anode (oxidation): } & \mathrm{M}(s) \longrightarrow \mathrm{M}^{2+}(a q)+2 \mathrm{e}^{-} \\
\text {Cathode (reduction): } & \mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cu}(s)
\end{array}
$$

Thus, the net cell reaction simply involves transfer of copper metal from the impure anode to the pure cathode. The copper obtained by this process is 99.95\% pure.

Closely related to electrorefining is electroplating, the coating of one metal on the surface of another using electrolysis. For example, steel automobile bumpers are plated with chromium to protect them from corrosion, and silver-plating is commonly used to make items of fine table service. The object to be plated is carefully cleaned and then set up as the cathode of an electrolytic cell that contains a solution of ions of the metal to be deposited.

- PROBLEM 18.19 Sketch an electrolytic cell suitable for electroplating a silver spoon. Describe the electrodes and the electrolyte, label the anode and cathode, and indicate the direction of electron and ion flow. Write balanced equations for the anode and cathode half-reactions. What is the overall cell reaction?


### 18.13 Quantitative Aspects of Electrolysis

Michael Faraday showed in the 1830s that the amount of substance produced at an electrode by electrolysis depends on the quantity of charge passed through the cell. For example, passing 1 mol of electrons through a Downs cell yields 1 mol $(23.0 \mathrm{~g})$ of sodium at the cathode:

$$
\begin{aligned}
& \mathrm{Na}^{+}(l)+\mathrm{e}^{-} \longrightarrow \\
& 1 \mathrm{~mol} \\
& 1 \mathrm{~mol}
\end{aligned} \underset{1 \mathrm{~mol}(23.0 \mathrm{~g})}{ } \mathrm{Na}(l)
$$

Similarly, passing 1 mol of electrons in the Hall-Heroult process produces $1 / 3 \mathrm{~mol}$ $(9.0 \mathrm{~g})$ of aluminum, because 3 mol of electrons are required to reduce 1 mol of $\mathrm{Al}^{3+}$ to aluminum metal:

$$
\begin{aligned}
& \mathrm{Al}^{3+}(l)+3 \mathrm{e}^{-} \longrightarrow \mathrm{Al}(l) \\
& 1 / 3 \mathrm{~mol} \quad 1 \mathrm{~mol} \quad 1 / 3 \mathrm{~mol}(9.0 \mathrm{~g})
\end{aligned}
$$

In general, the amount of product formed in an electrode reaction follows directly from the stoichiometry of the reaction and the molar mass of the product.

To find out how many moles of electrons pass through a cell in a particular experiment, we need to measure the electric current and the time that the current flows. The number of coulombs of charge passed through the cell equals the product of the current in amperes (coulombs per second) and the time in seconds:

$$
\text { Charge }(\mathrm{C})=\text { Current }(\mathrm{A}) \times \text { Time }(\mathrm{s})
$$

Because the charge on 1 mol of electrons is $96,500 \mathrm{C}$ (Section 18.3), the number of moles of electrons passed through the cell is

$$
\text { Moles of } \mathrm{e}^{-}=\text {Charge }(\mathrm{C}) \times \frac{1 \mathrm{~mol} \mathrm{e}^{-}}{96,500 \mathrm{C}}
$$

The sequence of conversions in Figure 18.20 is used to calculate the mass or volume of product produced by passing a known current through a cell for a fixed period of time. The key is to think of the electrons as a "reactant" in a balanced chemical equation and then to proceed as with any other stoichiometry problem. Worked Example 18.10 illustrates the calculations. Alternatively, we can calculate the current (or time) required to produce a given amount of product by working through the sequence in Figure 18.20 in the reverse direction, as shown in Worked Example 18.11.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Electroplating Copper," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 199-200.
v
Stress the use of this flowchart along with the dimensional analysis method of problem solving.

© FIGURE 18.20 Sequence of conversions used to calculate the amount of product produced by passing a current through an electrolytic cell for a fixed period of time.

Worked Example 18.10
A constant current of 30.0 A is passed through an aqueous solution of NaCl for a time of 1.00 h. How many grams of NaOH and how many liters of $\mathrm{Cl}_{2}$ gas at STP are produced?

## Strategy

To convert the current and time to grams or liters of product, carry out the sequence of conversions in Figure 18.20.

## Solution

Because electrons can be thought of as a reactant in the electrolysis process, the first step is to calculate the charge and the number of moles of electrons passed through the cell:

$$
\begin{aligned}
& \text { Charge }=\left(30.0 \frac{\mathrm{C}}{\mathrm{~s}}\right)(1.00 \mathrm{~h})\left(\frac{60 \mathrm{~min}}{\mathrm{~h}}\right)\left(\frac{60 \mathrm{~s}}{\mathrm{~min}}\right)=1.08 \times 10^{5} \mathrm{C} \\
& \text { Moles of } \mathrm{e}^{-}=\left(1.08 \times 10^{5} \mathrm{C}\right)\left(\frac{1 \mathrm{~mol} \mathrm{e}}{96,500 \mathrm{C}}\right)=1.12 \mathrm{~mol} \mathrm{e}
\end{aligned}
$$

The cathode reaction yields 2 mol of $\mathrm{OH}^{-}$per 2 mol of electrons (Section 18.11), so 1.12 mol of NaOH will be obtained:

$$
\begin{aligned}
& 2 \mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{e}^{-} \longrightarrow \mathrm{H}_{2}(g)+2 \mathrm{OH}^{-}(a q) \\
& \text { Moles of } \mathrm{NaOH}=\left(1.12 \mathrm{~mol} \mathrm{e}^{-}\right)\left(\frac{2 \mathrm{~mol} \mathrm{NaOH}}{2 \mathrm{~mol} \mathrm{e}^{-}}\right)=1.12 \mathrm{~mol} \mathrm{NaOH}
\end{aligned}
$$

Converting the number of moles of NaOH to grams of NaOH gives

$$
\text { Grams of } \mathrm{NaOH}=(1.12 \mathrm{~mol} \mathrm{NaOH})\left(\frac{40.0 \mathrm{~g} \mathrm{NaOH}}{\mathrm{~mol} \mathrm{NaOH}}\right)=44.8 \mathrm{~g} \mathrm{NaOH}
$$

The anode reaction gives 1 mol of $\mathrm{Cl}_{2}$ per 2 mol of electrons, so 0.560 mol of $\mathrm{Cl}_{2}$ will be obtained:

$$
\begin{aligned}
& 2 \mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{Cl}_{2}(g)+2 \mathrm{e}^{-} \\
& \text {Moles of } \mathrm{Cl}_{2}=\left(1.12 \mathrm{~mol} \mathrm{e}^{-}\right)\left(\frac{1 \mathrm{~mol} \mathrm{Cl}_{2}}{2 \mathrm{~mol} \mathrm{e}^{-}}\right)=0.560 \mathrm{~mol} \mathrm{Cl}_{2}
\end{aligned}
$$

Since 1 mol of an ideal gas occupies 22.4 L at STP, the volume of $\mathrm{Cl}_{2}$ obtained is

$$
\text { Liters of } \mathrm{Cl}_{2}=\left(0.560 \mathrm{~mol} \mathrm{Cl}_{2}\right)\left(\frac{22.4 \mathrm{~L} \mathrm{Cl}_{2}}{\mathrm{~mol} \mathrm{Cl}_{2}}\right)=12.5 \mathrm{~L} \mathrm{Cl}_{2}
$$

As a shortcut, the entire sequence of conversions can be carried out in one step. For example, the volume of $\mathrm{Cl}_{2}$ produced at the anode is

$$
\left(30.0 \frac{\mathrm{C}}{\mathrm{~s}}\right)(1.00 \mathrm{~h})\left(\frac{3600 \mathrm{~s}}{\mathrm{~h}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{e}^{-}}{96,500 \mathrm{C}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{Cl}_{2}}{2 \mathrm{~mol} \mathrm{e}^{-}}\right)\left(\frac{22.4 \mathrm{~L} \mathrm{Cl}_{2}}{\mathrm{~mol} \mathrm{Cl}_{2}}\right)=12.5 \mathrm{~L} \mathrm{Cl}_{2}
$$

$\checkmark$ BALLPARK CHECK Since approximately 1 mol of electrons is passed through the cell and the electrode reactions yield 1 mol of NaOH and 0.5 mol of $\mathrm{Cl}_{2}$ per mol of electrons, 1 mol of $\mathrm{NaOH}(\sim 40 \mathrm{~g})$ and 0.5 mol of $\mathrm{Cl}_{2}(\sim 11 \mathrm{~L}$ at STP) will be formed. The ballpark check and the solution agree.

## Worked Example 18.11

How many amperes must be passed through a Downs cell to produce sodium metal at a rate of $30.0 \mathrm{~kg} / \mathrm{h}$ ?

## Strategy

Proceed through a sequence of conversions similar to that in Worked Example 18.10, but in reverse order.

## SOLUTION

Because the molar mass of sodium is $23.0 \mathrm{~g} / \mathrm{mol}$, the number of moles of sodium produced per hour is

$$
\text { Moles of } \mathrm{Na}=(30.0 \mathrm{~kg} \mathrm{Na})\left(\frac{1000 \mathrm{~g}}{1 \mathrm{~kg}}\right)\left(\frac{1 \mathrm{~mol} \mathrm{Na}}{23.0 \mathrm{~g} \mathrm{Na}}\right)=1.30 \times 10^{3} \mathrm{~mol} \mathrm{Na}
$$

To produce each mole of sodium, 1 mol of electrons must be passed through the cell:

$$
\mathrm{Na}^{+}(l)+\mathrm{e}^{-} \longrightarrow \mathrm{Na}(l)
$$

Therefore, the charge passed per hour is

$$
\text { Charge }=\left(1.30 \times 10^{3} \mathrm{~mol} \mathrm{Na}\right)\left(\frac{1 \mathrm{~mol} \mathrm{e}^{-}}{1 \mathrm{~mol} \mathrm{Na}}\right)\left(\frac{96,500 \mathrm{C}}{\mathrm{~mol} \mathrm{e}^{-}}\right)=1.25 \times 10^{8} \mathrm{C}
$$

Since there are 3600 s in 1 h , the current required is

$$
\text { Current }=\frac{1.25 \times 10^{8} \mathrm{C}}{3600 \mathrm{~s}}=3.47 \times 10^{4} \mathrm{C} / \mathrm{s}=34,700 \mathrm{~A}
$$

PROBLEM 18.20 How many kilograms of aluminum can be produced in 8.00 h by passing a constant current of $1.00 \times 10^{5} \mathrm{~A}$ through a molten mixture of aluminum oxide and cryolite?

- PROBLEM 18.21 A layer of silver is electroplated on a coffee server using a constant current of 0.100 A . How much time is required to deposit 3.00 g of silver?


## Interlude



A These colored containers are made by anodizing aluminum, a silvery metal.


A The iridescent colors on this piece of metal are produced by anodizing different parts of the surface at different voltages.

## Electrochemical Art

If aluminum is a silvery metal, then why are some aluminum objects brightly colored? Aluminum bicycle parts, for instance, come in a spectrum of colors including red, blue, purple, yellow, and black.
Aluminum, chromium, titanium, and several other metals can be colored by an electrochemical process called anodizing. Unlike electroplating, in which a metal ion in the electrolyte is reduced and the metal is coated onto the surface of the cathode, anodizing oxidizes a metal anode to yield a metal oxide coat. In the oxidation of aluminum, for instance, the electrode reactions are

Cathode (reduction):

$$
6 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 3 \mathrm{H}_{2}(g)
$$

Anode (oxidation): $\quad 2 \mathrm{Al}(s)+3 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Al}_{2} \mathrm{O}_{3}(s)+6 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-}$
Overall cell reaction: $\quad 2 \mathrm{Al}(s)+3 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{Al}_{2} \mathrm{O}_{3}(s)+3 \mathrm{H}_{2}(g)$
The thickness of the aluminum oxide coating that forms on the anode can be controlled by varying the current flow during electrolysis. Typically, the coating is about 0.01 mm thick, which corresponds to about $4 \times 10^{4}$ atomic layers of $\mathrm{Al}_{2} \mathrm{O}_{3}$ on top of the underlying aluminum metal. The porosity of the $\mathrm{Al}_{2} \mathrm{O}_{3}$ coating can also be controlled by varying the electrolysis conditions, and it's this porosity that makes coloring possible. When an organic dye is added to the electrolyte, dye molecules soak into the spongy surface coating as it forms and become trapped as the surface hardens.

Titanium anodizing proceeds much like that of aluminum, but the resultant coat of $\mathrm{TiO}_{2}$ is much thinner $\left(10^{-4} \mathrm{~mm}\right)$ than the corresponding coat of $\mathrm{Al}_{2} \mathrm{O}_{3}$ $\left(10^{-2} \mathrm{~mm}\right)$. Furthermore, the iridescent colors of anodized titanium result not from the absorption of organic dyes but from the interference of light as it is reflected by the anodized surface. When a beam of white light strikes the anodized surface, part of the light is reflected from the outer $\mathrm{TiO}_{2}$, while part penetrates through the semitransparent $\mathrm{TiO}_{2}$ and is reflected from the inner metal. If the two reflections of a particular wavelength are out of phase, they interfere destructively and that wavelength is canceled from the reflected light. As a result, the light that remains is colored. (Similar effects are responsible for the colors in oil slicks and peacock feathers.)

The exact color of anodized titanium depends on the thickness of the $\mathrm{TiO}_{2}$ layer, which in turn varies with the voltage used to produce the layer. A voltage of 5 V , for example, gives a $\mathrm{TiO}_{2}$ coating $3 \times 10^{-5} \mathrm{~mm}$ thick with a yellow appearance, and a voltage of 30 V gives a coating $6 \times 10^{-5} \mathrm{~mm}$ thick with a light blue appearance. Artists use these effects to produce striking metal sculptures whose vibrant colors appear to change depending on the viewing angle.

PROBLEM 18.22 The reflection of light from anodized titanium is somewhat similar to the diffraction of $X$ rays from a crystal (Section 10.7). Explain why the color of anodized titanium depends on the thickness of the $\mathrm{TiO}_{2}$ layer.

- PROBLEM 18.23 How many minutes are required to produce a 0.0100 mm thick coating of $\mathrm{Al}_{2} \mathrm{O}_{3}$ (density $3.97 \mathrm{~g} / \mathrm{cm}^{3}$ ) on a square piece of aluminum metal 10.0 cm on an edge if the current passed through the piece is 0.600 A ?

Electrochemistry is the area of chemistry concerned with the interconversion of chemical and electrical energy. Chemical energy is converted to electrical energy in a galvanic cell, a device in which a spontaneous redox reaction is used to produce an electric current. Electrical energy is converted to chemical energy in an electrolytic cell, a cell in which an electric current drives a nonspontaneous reaction. It's convenient to separate cell reactions into half-reactions because oxidation and reduction occur at separate electrodes. The electrode at which oxidation occurs is called the anode, and the electrode at which reduction occurs is called the cathode.

The cell potential $E$ (also called the cell voltage or electromotive force) is an electrical measure of the driving force of the cell reaction. Cell potentials depend on temperature, ion concentrations, and gas pressures. The standard cell potential $E^{\circ}$ is the cell potential when reactants and products are in their standard states. Cell potentials are related to freeenergy changes by the equations $\Delta G=-n F E$ and $\Delta G^{\circ}=$ $-n F E^{\circ}$, where $F=96,500 \mathrm{C} / \mathrm{mol} \mathrm{e}^{-}$is the faraday, the charge on 1 mol of electrons.

The standard reduction potential for the a half-reaction is defined relative to an arbitrary value of 0 V for the standard hydrogen electrode (S.H.E.):

$$
2 \mathrm{H}^{+}(a q, 1 \mathrm{M})+2 \mathrm{e}^{-} \longrightarrow \mathrm{H}_{2}(g, 1 \mathrm{~atm}) \quad E^{\circ}=0 \mathrm{~V}
$$

Tables of standard reduction potentials-also called standard electrode potentials-are used to arrange oxidizing and reducing agents in order of increasing strength, to calculate $E^{\circ}$ values for cell reactions, and to decide whether a particular redox reaction is spontaneous.

Cell potentials under nonstandard-state conditions can be calculated using the Nernst equation,

$$
E=E^{\circ}-\frac{0.0592 \mathrm{~V}}{n} \log Q \quad \text { in volts, at } 25^{\circ} \mathrm{C}
$$

where $Q$ is the reaction quotient. The equilibrium constant $K$ and the standard cell potential $E^{\circ}$ are related by the equation

$$
E^{\circ}=\frac{0.0592 \mathrm{~V}}{n} \log K \quad \text { in volts, at } 25^{\circ} \mathrm{C}
$$

A battery consists of one or more galvanic cells. A fuel cell differs from a battery in that the reactants are continuously supplied to the cell.

Corrosion of iron (rusting) is an electrochemical process in which iron is oxidized in an anode region of the metal surface and oxygen is reduced in a cathode region. Corrosion can be prevented by covering iron with another metal, such as zinc, in the process called galvanizing, or simply by putting the iron in electrical contact with a second metal that is more easily oxidized, a process called cathodic protection.

Electrolysis, the process of using an electric current to bring about chemical change, is employed to produce sodium, chlorine, sodium hydroxide, and aluminum (Hall-Heroult process) and is used in electrorefining and electroplating.

The product obtained at an electrode depends on the reduction potentials and overvoltage. The amount of product obtained is related to the number of moles of electrons passed through the cell, which depends on the current and the time that the current flows.

## Key Words

anode 766
cathode 766
cathodic protection 792
cell potential (E) 770
cell voltage 770
corrosion 790
electrochemical cell 763
electrochemistry 763
electrode 766
electrolysis 793
electrolytic cell 792
electromotive force (emf) 770
electroplating 799
electrorefining 798
faraday (Faraday
constant) 771
fuel cell 789
galvanic cell (voltaic cell) 764
galvanizing 792
half-reaction 765
Hall-Heroult process 797
Nernst equation 778
overvoltage 794
sacrificial anode 792
salt bridge 766
standard cell potential
( $E^{\circ}$ ) 771
standard electrode potential 774 standard hydrogen electrode (S.H.E.) 773 standard reduction potential 773

## Key Concept Summary

- 



## Understanding Key Concepts

Problems 18.1-18.23 appear within the chapter.
18.24 The following picture of a galvanic cell has lead and zinc electrodes:

(a) Label the electrodes, and identify the ions present in the solutions.
(b) Label the anode and cathode.
(c) Indicate the direction of electron flow in the wire and ion flow in the solutions.
(d) Tell what electrolyte could be used in the salt bridge, and indicate the direction of ion flow.
(e) Write balanced equations for the electrode and overall cell reactions.
18.25 Consider the following galvanic cell:
-

(a) Identify the anode and cathode.
(b) Write a balanced equation for the cell reaction.
(c) Write the shorthand notation for the cell.
18.26 Consider the following galvanic cells:
(1) $\mathrm{Cu}(s)\left|\mathrm{Cu}^{2+}(1 \mathrm{M}) \| \mathrm{Fe}^{3+}(1 \mathrm{M}), \mathrm{Fe}^{2+}(1 \mathrm{M})\right| \mathrm{Pt}(\mathrm{s})$
(2) $\mathrm{Cu}(s)\left|\mathrm{Cu}^{2+}(1 \mathrm{M}) \| \mathrm{Fe}^{3+}(1 \mathrm{M}), \mathrm{Fe}^{2+}(5 \mathrm{M})\right| \mathrm{Pt}(\mathrm{s})$
(3) $\mathrm{Cu}(s)\left|\mathrm{Cu}^{2+}(0.1 \mathrm{M}) \| \mathrm{Fe}^{3+}(0.1 \mathrm{M}), \mathrm{Fe}^{2+}(0.1 \mathrm{M})\right| \mathrm{Pt}(s)$
(a) Write a balanced equation for each cell reaction.
(b) Sketch each cell. Label the anode and cathode, and indicate the direction of electron and ion flow.
(c) Which of the three cells has the largest cell potential? Which has the smallest cell potential? Explain.
18.27 Sketch a cell with inert electrodes suitable for electrolysis of aqueous $\mathrm{CuBr}_{2}$.
(a) Label the anode and cathode.
(b) Indicate the direction of electron and ion flow.
(c) Write balanced equations for the anode, cathode, and overall cell reactions.
18.28 Consider the following electrochemical cell:

(a) Is the cell a galvanic or an electrolytic cell? Explain.
(b) Label the anode and cathode, and show the direction of ion flow.
(c) Write balanced equations for the anode, cathode, and overall cell reactions.
18.29 It has recently been reported that porous pellets of $\mathrm{TiO}_{2}$ can be reduced to titanium metal at the cathode of an electrochemical cell containing molten $\mathrm{CaCl}_{2}$ as the electrolyte. When the $\mathrm{TiO}_{2}$ is reduced, the $\mathrm{O}^{2-}$ ions dissolve in the $\mathrm{CaCl}_{2}$ and are subsequently oxidized to $\mathrm{O}_{2}$ gas at the anode. This approach may be the basis for a less expensive process than the one currently used for producing titanium (see the Chapter 20 Interlude, page 903).

(a) Label the anode and cathode, and indicate the signs of the electrodes.
(b) Indicate the direction of electron and ion flow.
(c) Write balanced equations for the anode, cathode, and overall cell reactions.
18.30 Consider a Daniell cell with 1.0 M ion concentrations:
-


Does the cell voltage increase, decrease, or remain the same when each of the following changes is made? Explain.
(a) $5.0 \mathrm{M} \mathrm{CuSO}_{4}$ is added to the cathode compartment.
(b) $5.0 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ is added to the cathode compartment.
(c) $5.0 \mathrm{M} \mathrm{Zn}\left(\mathrm{NO}_{3}\right)_{2}$ is added to the anode compartment.
(d) $1.0 \mathrm{M} \mathrm{Zn}\left(\mathrm{NO}_{3}\right)_{2}$ is added to the anode compartment.
18.31 Consider the following galvanic cell with 0.10 M concentrations:


Does the cell voltage increase, decrease, or remain the same when each of the following changes is made? Explain.
(a) 0.10 M NaCl is added to the cathode compartment.
(b) 0.10 M NaCl is added to the anode compartment.
(c) $1.0 \mathrm{M} \mathrm{NH}_{3}$ is added to the cathode compartment.
(d) $1.0 \mathrm{M} \mathrm{NH}_{3}$ is added to the anode compartment.

## Additional Problems

## Galvanic Cells

18.32 Define anode and cathode with reference to a specific galvanic cell.
18.33 Does the oxidizing agent react at the anode or at the cathode in a galvanic cell? Explain.
18.34 Why is the cathode of a galvanic cell considered to be the positive electrode?
18.35 What is the function of a salt bridge in a galvanic cell?
18.36 Describe galvanic cells that use the following reactions. In each case, write the anode and cathode halfreactions, and sketch the experimental setup. Label the anode and cathode, identify the sign of each electrode, and indicate the direction of electron and ion flow.
(a) $\mathrm{Cd}(s)+\mathrm{Sn}^{2+}(a q) \rightarrow \mathrm{Cd}^{2+}(a q)+\mathrm{Sn}(s)$
(b) $2 \mathrm{Al}(s)+3 \mathrm{Cd}^{2+}(a q) \rightarrow 2 \mathrm{Al}^{3+}(a q)+3 \mathrm{Cd}(s)$
(c) $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+6 \mathrm{Fe}^{2+}(a q)+14 \mathrm{H}^{+}(a q) \rightarrow$

$$
2 \mathrm{Cr}^{3+}(a q)+6 \mathrm{Fe}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l)
$$

18.37 Describe galvanic cells that use the following reactions. In each case, write the anode and cathode halfreactions, and sketch the experimental setup. Label the anode and cathode, identify the sign of each electrode, and indicate the direction of electron and ion flow.
(a) $3 \mathrm{Cu}^{2+}(a q)+2 \mathrm{Cr}(s) \rightarrow 3 \mathrm{Cu}(s)+2 \mathrm{Cr}^{3+}(a q)$
(b) $\mathrm{Pb}(s)+2 \mathrm{H}^{+}(a q) \rightarrow \mathrm{Pb}^{2+}(a q)+\mathrm{H}_{2}(g)$
(c) $\mathrm{Cl}_{2}(g)+\mathrm{Sn}^{2+}(a q) \rightarrow \mathrm{Sn}^{4+}(a q)+2 \mathrm{Cl}^{-}(a q)$
18.38 Write the standard shorthand notation for each cell in Problem 18.36.
18.39 Write the standard shorthand notation for each cell in Problem 18.37.
18.40 $\mathrm{An} \mathrm{H}_{2} / \mathrm{H}^{+}$half-cell (anode) and an $\mathrm{Ag}^{+} / \mathrm{Ag}$ half-cell (cathode) are connected by a wire and a salt bridge.
(a) Sketch the cell, indicating the direction of electron and ion flow.
(b) Write balanced equations for the electrode and overall cell reactions.
(c) Give the shorthand notation for the cell.
18.41 A galvanic cell is constructed from a $\mathrm{Zn} / \mathrm{Zn}^{2+}$ half-cell (anode) and a $\mathrm{Cl}_{2} / \mathrm{Cl}^{-}$half-cell (cathode).
(a) Sketch the cell, indicating the direction of electron and ion flow.
(b) Write balanced equations for the electrode and overall cell reactions.
(c) Give the shorthand notation for the cell.
18.42 Write balanced equations for the electrode and overall cell reactions in the following galvanic cells. Sketch each cell, labeling the anode and cathode and showing the direction of electron and ion flow.
(a) $\mathrm{Co}(s)\left|\mathrm{Co}^{2+}(a q) \| \mathrm{Cu}^{2+}(a q)\right| \mathrm{Cu}(s)$
(b) $\mathrm{Fe}(s)\left|\mathrm{Fe}^{2+}(a q) \| \mathrm{O}_{2}(g)\right| \mathrm{H}^{+}(a q), \mathrm{H}_{2} \mathrm{O}(l) \mid \mathrm{Pt}(s)$
18.43 Write balanced equations for the electrode and overall cell reactions in the following galvanic cells. Sketch each cell, labeling the anode and cathode and showing the direction of electron and ion flow.
(a) $\operatorname{Mn}(s)\left|\mathrm{Mn}^{2+}(a q) \| \mathrm{Pb}^{2+}(a q)\right| \mathrm{Pb}(s)$
(b) $\mathrm{Pt}(s)\left|\mathrm{H}_{2}(g)\right| \mathrm{H}^{+}(a q) \| \mathrm{Cl}^{-}(a q)|\mathrm{AgCl}(s)| \mathrm{Ag}(s)$

## Cell Potentials and Free-Energy Changes; Standard Reduction Potentials

18.44 What are the SI units of electrical potential, electric charge, and energy? How are they related?
18.45 Define all terms in the equation $\Delta G=-n F E$.
18.46 What conditions must be met for a cell potential $E$ to qualify as a standard cell potential $E^{\circ}$ ?
18.47 How are standard reduction potentials defined?
18.48 The silver oxide-zinc battery used in hearing aids delivers a voltage of 1.60 V . Calculate the free-energy change (in kilojoules) for the cell reaction

$$
\mathrm{Zn}(s)+\mathrm{Ag}_{2} \mathrm{O}(s) \longrightarrow \mathrm{ZnO}(s)+2 \mathrm{Ag}(s)
$$

18.49 The standard cell potential for a lead storage battery is 1.924 V . Calculate $\Delta G^{\circ}$ (in kilojoules) for the cell reaction

$$
\begin{aligned}
& \mathrm{Pb}(s)+\mathrm{PbO}_{2}(s)+2 \mathrm{H}^{+}(a q)+ 2 \mathrm{HSO}_{4}^{-}(a q) \longrightarrow \\
& 2 \mathrm{PbSO}_{4}(s)+2 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

18.50 Using the standard free energies of formation in Appendix B, calculate the standard cell potential for the reaction in the hydrogen-oxygen fuel cell:

$$
2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)
$$

18.51 Consider a fuel cell that uses the reaction

$$
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

Given the standard free energies of formation in Appen$\operatorname{dix} \mathrm{B}$, what is the value of $E^{\circ}$ for the cell reaction?
18.52 The standard potential for the following galvanic cell is 0.40 V :

$$
\mathrm{Zn}(s)\left|\mathrm{Zn}^{2+}(a q) \| \mathrm{Eu}^{3+}(a q), \mathrm{Eu}^{2+}(a q)\right| \mathrm{Pt}(s)
$$

(Europium, Eu, is one of the lanthanide elements.) Use the data in Table 18.1 to calculate the standard reduction potential for the $\mathrm{Eu}^{3+} / \mathrm{Eu}^{2+}$ half-cell.
18.53 The following reaction has an $E^{\circ}$ value of 0.27 V :

$$
\mathrm{Cu}^{2+}(a q)+2 \mathrm{Ag}(s)+2 \mathrm{Br}^{-}(a q) \longrightarrow \underset{\mathrm{Cu}(s)+2 \operatorname{AgBr}(s)}{\longrightarrow}
$$

Use the data in Table 18.1 to calculate the standard reduction potential for the half-reaction

$$
\operatorname{AgBr}(s)+\mathrm{e}^{-} \longrightarrow \operatorname{Ag}(s)+\mathrm{Br}^{-}(a q)
$$

18.54 Arrange the following oxidizing agents in order of increasing strength under standard-state conditions: $\mathrm{Br}_{2}(l), \mathrm{MnO}_{4}^{-}(a q), \mathrm{Sn}^{4+}(a q)$.
18.55 List the following reducing agents in order of increasing strength under standard-state conditions: $\mathrm{Al}(s)$, $\mathrm{Pb}(\mathrm{s}), \mathrm{Fe}(\mathrm{s})$.
18.56 Consider the following substances: $\mathrm{I}_{2}(s), \mathrm{Fe}^{2+}(a q)$, $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(\mathrm{aq})$. Which is the strongest oxidizing agent? Which is the weakest oxidizing agent?
18.57 Consider the following substances: $\mathrm{Fe}^{2+}(a q)$, $\mathrm{Sn}^{2+}(a q), \mathrm{I}^{-}(a q)$. Identify the strongest reducing agent and the weakest reducing agent.
18.58 Calculate the standard cell potential and the standard free-energy change (in kilojoules) for each reaction in Problem 18.36. (See Appendix D for standard reduction potentials.)
18.59 Calculate $E^{\circ}$ and $\Delta G^{\circ}$ (in kilojoules) for the cell reactions in Problem 18.37. (See Appendix D for standard reduction potentials.)
18.60 Calculate $E^{\circ}$ for each of the following reactions, and tell which are spontaneous under standard-state conditions:
(a) $2 \mathrm{Fe}^{2+}(a q)+\mathrm{Pb}^{2+}(a q) \rightarrow 2 \mathrm{Fe}^{3+}(a q)+\mathrm{Pb}(s)$
(b) $\mathrm{Mg}(s)+\mathrm{Ni}^{2+}(a q) \rightarrow \mathrm{Mg}^{2+}(a q)+\mathrm{Ni}(s)$
18.61 Calculate $E^{\circ}$ for each of the following reactions, and tell which are spontaneous under standard-state conditions:

$$
\begin{aligned}
& \text { (a) } 5 \mathrm{Ag}^{+}(a q)+\mathrm{Mn}^{2+}(a q)+4 \mathrm{H}_{2} \mathrm{O}(l) \rightarrow \\
& \\
& \quad 5 \mathrm{Ag}(s)+\mathrm{MnO}_{4}^{-}(a q)+8 \mathrm{H}^{+}(a q) \\
& \text { (b) } 2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \rightarrow \mathrm{O}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

18.62 Use the data in Appendix D to predict whether the following reactions can occur under standard-state conditions:
(a) Oxidation of $\mathrm{Sn}^{2+}(a q)$ by $\mathrm{Br}_{2}(l)$
(b) Reduction of $\mathrm{Ni}^{2+}(a q)$ by $\mathrm{Sn}^{2+}(a q)$
(c) Oxidation of $\mathrm{Ag}(s)$ by $\mathrm{Pb}^{2+}(a q)$
(d) Reduction of $\mathrm{I}_{2}(s)$ by $\mathrm{H}_{2} \mathrm{SO}_{3}(a q)$
18.63 What reaction can occur, if any, when the following experiments are carried out under standard-state conditions?
(a) A strip of zinc is dipped into an aqueous solution of $\mathrm{Pb}\left(\mathrm{NO}_{3}\right)_{2}$.
(b) An acidic solution of $\mathrm{FeSO}_{4}$ is exposed to oxygen.
(c) A silver wire is immersed in an aqueous solution of $\mathrm{NiCl}_{2}$.
(d) Hydrogen gas is bubbled through aqueous $\mathrm{Cd}\left(\mathrm{NO}_{3}\right)_{2}$.

## The Nernst Equation

18.64 Consider a galvanic cell that uses the reaction

$$
2 \mathrm{Ag}^{+}(a q)+\mathrm{Sn}(s) \longrightarrow 2 \mathrm{Ag}(s)+\mathrm{Sn}^{2+}(a q)
$$

Calculate the potential at $25^{\circ} \mathrm{C}$ for a cell that has the following ion concentrations: $\left[\mathrm{Ag}^{+}\right]=0.010 \mathrm{M},\left[\mathrm{Sn}^{2+}\right]=$ 0.020 M .
18.65 Consider a galvanic cell based on the reaction
$2 \mathrm{Fe}^{2+}(a q)+\mathrm{Cl}_{2}(g) \longrightarrow 2 \mathrm{Fe}^{3+}(a q)+2 \mathrm{Cl}^{-}(a q)$
Calculate the cell potential at $25^{\circ} \mathrm{C}$ when $\left[\mathrm{Fe}^{2+}\right]=$ $1.0 \mathrm{M},\left[\mathrm{Fe}^{3+}\right]=1.0 \times 10^{-3} \mathrm{M},\left[\mathrm{Cl}^{-}\right]=3.0 \times 10^{-3} \mathrm{M}$, and $P_{\mathrm{Cl}_{2}}=0.50 \mathrm{~atm}$.
18.66 What is the cell potential at $25^{\circ} \mathrm{C}$ for the following galvanic cell?
$\mathrm{Pb}(s)\left|\mathrm{Pb}^{2+}(1.0 \mathrm{M}) \| \mathrm{Cu}^{2+}\left(1.0 \times 10^{-4} \mathrm{M}\right)\right| \mathrm{Cu}(s)$
If the $\mathrm{Pb}^{2+}$ concentration is maintained at 1.0 M , what is the $\mathrm{Cu}^{2+}$ concentration when the cell potential drops to zero?
18.67 A galvanic cell has an iron electrode in contact with $0.10 \mathrm{M} \mathrm{FeSO}_{4}$ and a copper electrode in contact with a $\mathrm{CuSO}_{4}$ solution. If the measured cell potential at $25^{\circ} \mathrm{C}$ is 0.67 V , what is the concentration of $\mathrm{Cu}^{2+}$ in the $\mathrm{CuSO}_{4}$ solution?
18.68 The Nernst equation applies to both cell reactions and half-reactions. For the conditions specified, calculate the potential for the following half-reactions at $25^{\circ} \mathrm{C}$ :
(a) $\mathrm{I}_{2}(s)+2 \mathrm{e}^{-} \rightarrow 2 \mathrm{I}^{-}(a q) ;\left[\mathrm{I}^{-}\right]=0.020 \mathrm{M}$
(b) $\mathrm{Fe}^{3+}(a q)+\mathrm{e}^{-} \rightarrow \mathrm{Fe}^{2+}(a q)$;

$$
\left[\mathrm{Fe}^{3+}\right]=\left[\mathrm{Fe}^{2+}\right]=0.10 \mathrm{M}
$$

(c) $\mathrm{Sn}^{2+}(a q) \rightarrow \mathrm{Sn}^{4+}(a q)+2 \mathrm{e}^{-}$;

$$
\left[\mathrm{Sn}^{2+}\right]=1.0 \times 10^{-3} \mathrm{M},\left[\mathrm{Sn}^{4+}\right]=0.40 \mathrm{M}
$$

(d) $2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l) \rightarrow$

$$
\begin{array}{r}
\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} ; \\
{\left[\mathrm{Cr}^{3+}\right]=\left[\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}\right]=1.0 \mathrm{M},\left[\mathrm{H}^{+}\right]=0.010 \mathrm{M}}
\end{array}
$$

18.69 What is the reduction potential at $25^{\circ} \mathrm{C}$ for the hydrogen electrode in each of the following solutions? The half-reaction is

$$
2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{H}_{2}(g, 1 \mathrm{~atm})
$$

(a) 1.0 M HCl
(b) A solution having pH 4.00
(c) Pure water
(d) 1.0 M NaOH
18.70 The following cell has a potential of 0.27 V at $25^{\circ} \mathrm{C}$ :

$$
\mathrm{Pt}(s)\left|\mathrm{H}_{2}(1 \mathrm{~atm})\right| \mathrm{H}^{+}(? \mathrm{M}) \| \mathrm{Ni}^{2+}(1 \mathrm{M}) \mid \mathrm{Ni}(\mathrm{~s})
$$

What is the pH of the solution in the anode compartment?
18.71 What is the pH of the solution in the cathode compartment of the following cell if the measured cell potential at $25^{\circ} \mathrm{C}$ is 0.58 V ?

$$
\mathrm{Zn}(s)\left|\mathrm{Zn}^{2+}(1 \mathrm{M}) \| \mathrm{H}^{+}(? \mathrm{M})\right| \mathrm{H}_{2}(1 \mathrm{~atm}) \mid \operatorname{Pt}(s)
$$

## Standard Cell Potentials and Equilibrium Constants

18.72 Beginning with the equations that relate $E^{\circ}, \Delta G^{\circ}$, and $K$, show that $\Delta G^{\circ}$ is negative and $K>1$ for a reaction that has a positive value of $E^{\circ}$.
18.73 If a reaction has an equilibrium constant $K<1$, is $E^{\circ}$ positive or negative? What is the value of $K$ when $E^{\circ}=0 \mathrm{~V}$ ?
18.74 Use the data in Table 18.1 to calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for the reaction

$$
\mathrm{Ni}(s)+2 \mathrm{Ag}^{+}(a q) \longrightarrow \mathrm{Ni}^{2+}(a q)+2 \mathrm{Ag}(s)
$$

18.75 From standard reduction potentials, calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for the reaction

$$
\begin{aligned}
2 \mathrm{MnO}_{4}^{-}(a q)+10 \mathrm{Cl}^{-}(a q)+16 \mathrm{H}^{+}(a q) \longrightarrow \\
2 \mathrm{Mn}^{2+}(a q)+5 \mathrm{Cl}_{2}(g)+8 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

18.76 Calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for each reaction in Problem 18.36.
18.77 Calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for each reaction in Problem 18.37.
18.78 Calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for disproportionation of $\mathrm{Hg}_{2}{ }^{2+}$ :

$$
\mathrm{Hg}_{2}{ }^{2+}(a q) \longrightarrow \mathrm{Hg}(l)+\mathrm{Hg}^{2+}(a q)
$$

See Appendix D for standard reduction potentials.
18.79 Use standard reduction potentials to calculate the equilibrium constant at $25^{\circ} \mathrm{C}$ for disproportionation of hydrogen peroxide:

$$
2 \mathrm{H}_{2} \mathrm{O}_{2}(l) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)+\mathrm{O}_{2}(g)
$$

## Batteries; Corrosion

18.80 What is rust? What causes it to form? What can be done to prevent its formation?
18.81 The standard oxidation potential for the reaction $\mathrm{Cr}(s) \rightarrow \mathrm{Cr}^{3+}(a q)+3 \mathrm{e}^{-}$is 0.74 V . Despite the large, positive oxidation potential, chromium is used as a protective coating on steel automobile bumpers. Why doesn't the chromium corrode?
18.82 What is meant by cathodic protection? Which of the following metals can offer cathodic protection to iron?

$$
\mathrm{Zn}, \mathrm{Ni}, \mathrm{Al}, \mathrm{Sn}
$$

18.83 What is a sacrificial anode? Give an example.
18.84 For a lead storage battery:
(a) Sketch one cell that shows the anode, cathode, electrolyte, direction of electron and ion flow, and sign of the electrodes.
(b) Write the anode, cathode, and overall cell reactions.
(c) Calculate the equilibrium constant for the cell reaction ( $E^{\circ}=1.924 \mathrm{~V}$ ).
(d) What is the cell voltage when the cell reaction reaches equilibrium?
18.85 Calculate the values of $E^{\circ}, \Delta G^{\circ}$ (in kilojoules), and $K$ at $25^{\circ} \mathrm{C}$ for the cell reaction in a hydrogen-oxygen fuel cell: $2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)$. What is the cell voltage at $25^{\circ} \mathrm{C}$ if the partial pressure of each gas is 25 atm ?
18.86 How many grams of HgO react at the cathode of a mercury battery when 2.00 g of zinc is consumed at the anode?
18.87 Write a balanced equation for the reaction that occurs when a nickel-cadmium battery is recharged. If 10.0 g of $\mathrm{Ni}(\mathrm{OH})_{2}$ is oxidized in the charging process, how many grams of cadmium are formed?

## Electrolysis

18.88 Magnesium metal is produced by the electrolysis of molten magnesium chloride using inert electrodes.
(a) Sketch the cell, label the anode and cathode, indicate the sign of the electrodes, and show the direction of electron and ion flow.
(b) Write balanced equations for the anode, cathode, and overall cell reactions.
18.89 (a) Sketch a cell with inert electrodes suitable for the electrolysis of an aqueous solution of sulfuric acid. Label the anode and cathode, and indicate the direction of electron and ion flow. Identify the positive and negative electrodes.
(b) Write balanced equations for the anode, cathode, and overall cell reactions.
18.90 List the anode and cathode half-reactions that might occur when an aqueous solution of $\mathrm{MgCl}_{2}$ is electrolyzed in a cell having inert electrodes. Predict which half-reactions will occur, and justify your answers.
18.91 What products should be formed when the following reactants are electrolyzed in a cell having inert electrodes? Account for any differences.
(a) Molten KCl
(b) Aqueous KCl
18.92 Predict the anode, cathode, and overall cell reactions when an aqueous solution of each of the following salts is electrolyzed in a cell having inert electrodes:
(a) NaBr
(b) $\mathrm{CuCl}_{2}$
(c) LiOH
18.93 Predict the anode, cathode, and overall cell reactions when an aqueous solution of each of the following salts is electrolyzed in a cell having inert electrodes:
(a) $\mathrm{Ag}_{2} \mathrm{SO}_{4}$
(b) $\mathrm{Ca}(\mathrm{OH})_{2}$
(c) KI
18.94 How many grams of silver will be obtained when an aqueous silver nitrate solution is electrolyzed for 20.0 min with a constant current of 2.40 A ?
18.95 A constant current of 100.0 A is passed through an electrolytic cell having an impure copper anode, a pure copper cathode, and an aqueous $\mathrm{CuSO}_{4}$ electrolyte. How many kilograms of copper are refined by transfer from the anode to the cathode in a 24.0 h period?
18.96 How many hours are required to produce $1.00 \times 10^{3} \mathrm{~kg}$ of sodium by the electrolysis of molten NaCl with a constant current of $3.00 \times 10^{4} \mathrm{~A}$ ? How many liters of $\mathrm{Cl}_{2}$ at STP will be obtained as a by-product?
18.97 What constant current (in amperes) is required to produce aluminum by the Hall-Heroult process at a rate of $40.0 \mathrm{~kg} / \mathrm{h}$ ?
18.98 How many grams of $\mathrm{PbSO}_{4}$ are reduced at the cathode if you charge a lead storage battery for 1.50 h with a constant current of 10.0 A ?
18.99 A layer of chromium is electroplated on an automobile bumper by passing a constant current of 200.0 A through a cell that contains $\mathrm{Cr}^{3+}(a q)$. How many minutes are required to deposit 125 g of chromium?

## General Problems

18.100 Consider a galvanic cell that uses the following halfreactions:

$$
\begin{aligned}
& \mathrm{MnO}_{4}^{-}(a q)+8 \mathrm{H}^{+}(a q)+5 \mathrm{e}^{-} \longrightarrow \\
& \mathrm{Sn}^{4+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Sn}^{2+}(a q)
\end{aligned}
$$

(a) Write a balanced equation for the overall cell reaction.
(b) What is the oxidizing agent, and what is the reducing agent?
(c) Calculate the standard cell potential.
18.101 Given the following half-reactions and $E^{\circ}$ values,

$$
\begin{array}{r}
\mathrm{Mn}^{3+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Mn}^{2+}(a q) \quad E^{\circ}=1.54 \mathrm{~V} \\
\mathrm{MnO}_{2}(s)+4 \mathrm{H}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Mn}^{3+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l) \\
E^{\circ}=0.95 \mathrm{~V}
\end{array}
$$

write a balanced equation for disproportionation of $\mathrm{Mn}^{3+}(a q)$, and calculate the value of $E^{\circ}$ for this reaction. Is the reaction spontaneous under standard-state conditions?
18.102 Consider the following half-reactions and $E^{\circ}$ values:

$$
\begin{array}{ll}
\mathrm{Ag}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Ag}(s) & E^{\circ}=0.80 \mathrm{~V} \\
\mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Cu}(s) & E^{\circ}=0.34 \mathrm{~V} \\
\mathrm{~Pb}^{2+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Pb}(s) & E^{\circ}=-0.13 \mathrm{~V}
\end{array}
$$

(a) Which of these metals or ions is the strongest oxidizing agent? Which is the strongest reducing agent?
(b) The half-reactions can be used to construct three different galvanic cells. Tell which cell delivers the highest voltage, identify the anode and cathode, and tell the direction of electron and ion flow.
(c) Write the cell reaction for part (b), and calculate the values of $E^{\circ}, \Delta G^{\circ}$ (in kilojoules), and $K$ for this reaction.
(d) Calculate the voltage for the cell in part (b) if both ion concentrations are 0.010 M .
18.103 Standard reduction potentials for the $\mathrm{Pb}^{2+} / \mathrm{Pb}$ and $\mathrm{Cd}^{2+} / \mathrm{Cd}$ half-reactions are -0.13 V and -0.40 V , respectively. At what relative concentrations of $\mathrm{Pb}^{2+}$ and $\mathrm{Cd}^{2+}$ will these half-reactions have the same reduction potential?
18.104 Consider a galvanic cell that uses the following halfreactions:

$$
\begin{aligned}
& 2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{H}_{2}(g) \\
& \mathrm{Al}^{3+}(a q)+3 \mathrm{e}^{-} \longrightarrow \mathrm{Al}(s)
\end{aligned}
$$

(a) What materials are used for the electrodes? Identify the anode and cathode, and indicate the direction of electron and ion flow.
(b) Write a balanced equation for the cell reaction, and calculate the standard cell potential.
(c) Calculate the cell potential at $25^{\circ} \mathrm{C}$ if the ion concentrations are 0.10 M and the partial pressure of $\mathrm{H}_{2}$ is 10.0 atm .
(d) Calculate $\Delta G^{\circ}$ (in kilojoules) and $K$ for the cell reaction at $25^{\circ} \mathrm{C}$.
(e) Calculate the mass change (in grams) of the aluminum electrode after the cell has supplied a constant current of 10.0 A for 25.0 min .
18.105 A Daniell cell delivers a constant current of 0.100 A for 200.0 h . How many grams of zinc are oxidized at the anode?
18.106 Approximately 13 million tons of $\mathrm{Cl}_{2}$ are produced annually in the United States by the electrolysis of brine. How many kilowatt-hours ( kWh ) of energy are required for the electrolysis if the cells operate at a potential of 4.5 V ? ( $\left.1 \mathrm{ton}=2000 \mathrm{lb} ; 1 \mathrm{kWh}=3.6 \times 10^{6} \mathrm{~J}.\right)$
18.107 The following cell reactions occur spontaneously:

$$
\begin{aligned}
& \mathrm{B}+\mathrm{A}^{+} \longrightarrow \mathrm{B}^{+}+\mathrm{A} \\
& \mathrm{C}+\mathrm{A}^{+} \longrightarrow \mathrm{C}^{+}+\mathrm{A} \\
& \mathrm{~B}+\mathrm{C}^{+} \longrightarrow \mathrm{B}^{+}+\mathrm{C}
\end{aligned}
$$

(a) Arrange the following reduction half-reactions in order of decreasing tendency to occur: $\mathrm{A}^{+}+$ $\mathrm{e}^{-} \rightarrow \mathrm{A}, \mathrm{B}^{+}+\mathrm{e}^{-} \rightarrow \mathrm{B}$, and $\mathrm{C}^{+}+\mathrm{e}^{-} \rightarrow \mathrm{C}$.
(b) Which of these substances $\left(\mathrm{A}, \mathrm{A}^{+}, \mathrm{B}, \mathrm{B}^{+}, \mathrm{C}, \mathrm{C}^{+}\right)$is the strongest oxidizing agent? Which is the strongest reducing agent?
(c) Which of the three cell reactions delivers the highest voltage?
18.108 Consider the following substances: $\mathrm{Fe}(s), \mathrm{PbO}_{2}(s)$, $\mathrm{H}^{+}(a q), \mathrm{Al}(s), \mathrm{Ag}(s), \mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q)$.
(a) Look at the $E^{\circ}$ values in Appendix D, and classify each substance as an oxidizing agent or reducing agent.
(b) Which is the strongest oxidizing agent? Which is the weakest oxidizing agent?
(c) Which is the strongest reducing agent? Which is the weakest reducing agent?
(d) Which substances can be oxidized by $\mathrm{Cu}^{2+}(a q)$ ? Which can be reduced by $\mathrm{H}_{2} \mathrm{O}_{2}(a q)$ ?
18.109 The standard half-cell potential for reduction of quinone to hydroquinone is 0.699 V :



When a photographic film is developed, silver bromide is reduced by hydroquinone (the developer) in a basic aqueous solution to give quinone and tiny black particles of silver metal:

$$
\begin{aligned}
& 2 \mathrm{AgBr}(s)+\mathrm{C}_{6} \mathrm{H}_{4}(\mathrm{OH})_{2}(a q)+2 \mathrm{OH}^{-}(a q) \longrightarrow \\
& 2 \mathrm{Ag}(s)+2 \mathrm{Br}^{-}(a q)+\mathrm{C}_{6} \mathrm{H}_{4} \mathrm{O}_{2}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

(a) What is the value of $E^{\circ}$ for this reaction under acidic conditions $\left(\left[\mathrm{H}^{+}\right]=1.0 \mathrm{M}\right)$ ? Is the reaction spontaneous in 1.0 M acid?
(b) What is the value of $E^{\circ}$ for the reaction under basic conditions $\left(\left[\mathrm{OH}^{-}\right]=1.0 \mathrm{M}\right)$ ?
18.110 When suspected drunk drivers are tested with a Breathalyzer, the alcohol (ethanol) in the exhaled breath is oxidized to acetic acid with an acidic solution of potassium dichromate:
$3 \mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}(a q)+2 \mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+16 \mathrm{H}^{+}(a q) \longrightarrow$
Ethanol

$$
3 \mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}(a q)+4 \mathrm{Cr}^{3+}(a q)+11 \mathrm{H}_{2} \mathrm{O}(l)
$$

Acetic acid
The color of the solution changes because some of the orange $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ is converted to the green $\mathrm{Cr}^{3+}$. The Breathalyzer measures the color change and produces a meter reading calibrated in terms of blood alcohol content.
(a) What is $E^{\circ}$ for the reaction if the standard half-cell potential for the reduction of acetic acid to ethanol is 0.058 V ?
(b) What is the value of $E$ for the reaction when the concentrations of ethanol, acetic acid, $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$, and $\mathrm{Cr}^{3+}$ are 1.0 M and the pH is 4.00 ?
18.111 Consider the addition of the following half-reactions:
(1) $\mathrm{Fe}^{3+}(a q)+3 \mathrm{e}^{-} \longrightarrow \mathrm{Fe}(s)$
$E^{\circ}{ }_{1}=-0.04 \mathrm{~V}$
(2) $\mathrm{Fe}(s) \longrightarrow \mathrm{Fe}^{2+}(a q)+2 \mathrm{e}^{-}$
$E^{\circ}{ }_{2}=0.45 \mathrm{~V}$
(3) $\mathrm{Fe}^{3+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Fe}^{2+}(a q)$

$$
E_{3}^{\circ}=?
$$

Because half-reactions (1) and (2) contain a different number of electrons, the net reaction (3) is another half-reaction, and $E^{\circ}{ }_{3}$ can't be obtained simply by adding $E^{\circ}{ }_{1}$ and $E^{\circ}{ }_{2}$. The free-energy changes, however, are additive because $G$ is a state function:

$$
\Delta G_{3}^{\circ}=\Delta G_{1}^{\circ}+\Delta G^{\circ}{ }_{2}
$$

(a) Starting with the relationship between $\Delta G^{\circ}$ and $E^{\circ}$, derive a general equation that relates the $E^{\circ}$ values for half-reactions (1), (2), and (3).
(b) Calculate the value of $E_{3}^{\circ}$ for the $\mathrm{Fe}^{3+} / \mathrm{Fe}^{2+}$ halfreaction.
(c) Explain why the $E^{\circ}$ values would be additive $\left(E^{\circ}{ }_{3}=E^{\circ}{ }_{1}+E^{\circ}{ }_{2}\right)$ if reaction (3) were an overall cell reaction rather than a half-reaction.
18.112 The following galvanic cell has a potential of 0.578 V at $25^{\circ} \mathrm{C}$ :

$$
\mathrm{Ag}(s)|\mathrm{AgCl}(s)| \mathrm{Cl}^{-}(1.0 \mathrm{M}) \| \mathrm{Ag}^{+}(1.0 \mathrm{M}) \mid \mathrm{Ag}(s)
$$

Use this information to calculate $K_{\text {sp }}$ for AgCl at $25^{\circ} \mathrm{C}$.
18.113 A galvanic cell has a silver electrode in contact with $0.050 \mathrm{M} \mathrm{AgNO}_{3}$ and a copper electrode in contact with $1.0 \mathrm{M} \mathrm{Cu}\left(\mathrm{NO}_{3}\right)_{2}$.
(a) Write a balanced equation for the cell reaction, and calculate the cell potential at $25^{\circ} \mathrm{C}$.
(b) Excess $\mathrm{NaBr}(a q)$ is added to the $\mathrm{AgNO}_{3}$ solution to precipitate AgBr . What is the cell potential at $25^{\circ} \mathrm{C}$ after the precipitation of AgBr if the concentration of excess $\mathrm{Br}^{-}$is 1.0 M ? Write a balanced equation for the cell reaction under these conditions. ( $K_{\text {sp }}$ for AgBr at $25^{\circ} \mathrm{C}$ is $5.4 \times 10^{-13}$.)
(c) Use the result in part (b) to calculate the standard reduction potential $E^{\circ}$ for the half-reaction $\mathrm{AgBr}(s)+\mathrm{e}^{-} \rightarrow \mathrm{Ag}(s)+\mathrm{Br}^{-}(a q)$.
18.114 At one time on Earth, iron was present mostly as iron(II). Later, once plants had produced a significant quantity of oxygen in the atmosphere, the iron became oxidized to iron(III). Show that $\mathrm{Fe}^{2+}(a q)$ can be spontaneously oxidized to $\mathrm{Fe}^{3+}(a q)$ by $\mathrm{O}_{2}(g)$ at $25^{\circ} \mathrm{C}$ assuming the following reasonable environmental conditions: $\left[\mathrm{Fe}^{2+}\right]=\left[\mathrm{Fe}^{3+}\right]=1 \times 10^{-7} \mathrm{M}$; $\mathrm{pH}=7.0 ; P_{\mathrm{O}_{2}}=160 \mathrm{~mm} \mathrm{Hg}$.
18.115 Given the following standard reduction potentials at $25^{\circ} \mathrm{C}$, (a) balance the equation for the reaction of $\mathrm{H}_{2} \mathrm{MoO}_{4}$ with elemental arsenic in acidic solution to give $\mathrm{Mo}^{3+}$ and $\mathrm{H}_{3} \mathrm{AsO}_{4}$, and (b) calculate $E^{\circ}$ for this reaction.

| Half-Reaction | $\boldsymbol{E}^{\circ}(\mathbf{V})$ |
| :--- | :---: |
| $\mathrm{H}_{3} \mathrm{AsO}_{4}(a q)+2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \rightarrow$ | +0.560 |
| $\mathrm{H}_{3} \mathrm{AsO}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l)$ |  |
| $\mathrm{H}_{3} \mathrm{AsO}_{3}(a q)+3 \mathrm{H}^{+}(a q)+3 \mathrm{e}^{-} \rightarrow$ | +0.240 |
| $\mathrm{As}(s)+3 \mathrm{H}_{2} \mathrm{O}(l)$ |  |
| $\mathrm{H}_{2} \mathrm{MoO}_{4}(a q)+2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} \rightarrow$ | +0.646 |
| $\mathrm{MoO}_{2}(s)+2 \mathrm{H}_{2} \mathrm{O}(l)$ |  |
| $\mathrm{MoO}_{2}(s)+4 \mathrm{H}^{+}(a q)+\mathrm{e}^{-} \rightarrow$ |  |
| $\mathrm{Mo}^{3+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)$ | -0.008 |

18.116 The following galvanic cell has a potential of 1.214 V at $25^{\circ} \mathrm{C}$ :
$\mathrm{Hg}(l)\left|\mathrm{Hg}_{2} \mathrm{Br}_{2}(s)\right| \mathrm{Br}^{-}(0.10 \mathrm{M}) \| \mathrm{MnO}_{4}{ }^{-}(0.10 \mathrm{M})$,

$$
\mathrm{Mn}^{2+}(0.10 \mathrm{M}), \mathrm{H}^{+}(0.10 \mathrm{M}) \mid \operatorname{Pt}(s)
$$

Calculate the value of $K_{\text {sp }}$ for $\mathrm{Hg}_{2} \mathrm{Br}_{2}$ at $25^{\circ} \mathrm{C}$.
18.117 For the following half-reaction, $E^{\circ}=1.103 \mathrm{~V}$ :

$$
\mathrm{Cu}^{2+}(a q)+2 \mathrm{CN}^{-}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Cu}(\mathrm{CN})_{2}^{-}(a q)
$$

Calculate the formation constant $K_{\mathrm{f}}$ for $\mathrm{Cu}(\mathrm{CN})_{2}{ }^{-}$.
18.118 Accidentally chewing on a stray fragment of aluminum foil can cause a sharp tooth pain if the aluminum comes in contact with an amalgam filling. The filling, an alloy of silver, tin, and mercury, acts as the cathode of a tiny galvanic cell, the aluminum behaves
as the anode, and saliva serves as the electrolyte. When the aluminum and the filling come in contact, an electric current passes from the aluminum to the filling, which is sensed by a nerve in the tooth. Aluminum is oxidized at the anode, and $\mathrm{O}_{2}$ gas is reduced to water at the cathode.
(a) Write balanced equations for the anode, cathode, and overall cell reactions.
(b) Write the Nernst equation in a form that applies at body temperature $\left(37^{\circ} \mathrm{C}\right)$.
(c) Calculate the cell voltage at $37^{\circ} \mathrm{C}$. You may assume that $\left[\mathrm{Al}^{3+}\right]=1.0 \times 10^{-9} \mathrm{M}, P_{\mathrm{O}_{2}}=0.20 \mathrm{~atm}$, and that saliva has a pH of 7.0 . Also assume that the $E^{\circ}$ values in Appendix D apply at $37^{\circ} \mathrm{C}$.
18.119 Copper reduces dilute nitric acid to nitric oxide (NO) but reduces concentrated nitric acid to nitrogen dioxide $\left(\mathrm{NO}_{2}\right)$ :
(1) $3 \mathrm{Cu}(s)+2 \mathrm{NO}_{3}{ }^{-}(a q)+8 \mathrm{H}^{+}(a q) \rightarrow$ $3 \mathrm{Cu}^{2+}(a q)+2 \mathrm{NO}(g)+4 \mathrm{H}_{2} \mathrm{O}(l) \quad \mathrm{E}^{\circ}=0.62 \mathrm{~V}$
(2) $\mathrm{Cu}(s)+2 \mathrm{NO}_{3}^{-}(a q)+4 \mathrm{H}^{+}(a q) \rightarrow$ $\mathrm{Cu}^{2+}(a q)+2 \mathrm{NO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l) \quad \mathrm{E}^{\circ}=0.45 \mathrm{~V}$
Assuming that $\left[\mathrm{Cu}^{2+}\right]=0.10 \mathrm{M}$ and that the partial pressures of NO and $\mathrm{NO}_{2}$ are $1.0 \times 10^{-3} \mathrm{~atm}$, calculate the potential ( $E$ ) for reactions (1) and (2) at $25^{\circ} \mathrm{C}$ and show which reaction has the greater thermodynamic tendency to occur when the concentration of $\mathrm{HNO}_{3}$ is
(a) 1.0 M
(b) 10.0 M
(c) At what $\mathrm{HNO}_{3}$ concentration do reactions (1) and (2) have the same value of $E$ ?

## Multi-Concept Problems

18.120 Adiponitrile, a key intermediate in the manufacture of nylon, is made industrially by an electrolytic process that reduces acrylonitrile:

Anode (oxidation): $\quad 2 \mathrm{H}_{2} \mathrm{O} \longrightarrow \mathrm{O}_{2}+4 \mathrm{H}^{+}+4 \mathrm{e}^{-}$
Cathode (reduction):

$$
\underset{\text { Acrylonitrile }}{2 \mathrm{CH}_{2}=\mathrm{CHCN}}+2 \mathrm{H}^{+}+2 \mathrm{e}^{-} \longrightarrow \underset{\text { Adiponitrile }}{\mathrm{NC}\left(\mathrm{CH}_{2}\right)_{4} \mathrm{CN}}
$$

(a) Write a balanced equation for the overall cell reaction.
(b) How many kilograms of adiponitrile are produced in 10.0 h in a cell that has a constant current of $3.00 \times 10^{3} \mathrm{~A}$ ?
(c) How many liters of $\mathrm{O}_{2}$ at 740 mm Hg and $25^{\circ} \mathrm{C}$ are produced as a by-product?
18.121 The reaction of $\mathrm{MnO}_{4}{ }^{-}$with oxalic acid $\left(\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$ in acidic solution is widely used to determine the concentration of permanganate solutions:
(a) Write a balanced net ionic equation for the reaction.
(b) Use the data in Appendix D to calculate $E^{\circ}$ for the reaction.
(c) Show that the reaction goes to completion by calculating the values of $\Delta G^{\circ}$ and $K$ at $25^{\circ} \mathrm{C}$.
(d) A 1.200 g sample of sodium oxalate $\left(\mathrm{Na}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$ is dissolved in dilute $\mathrm{H}_{2} \mathrm{SO}_{4}$ and then titrated with a $\mathrm{KMnO}_{4}$ solution. If 32.50 mL of the $\mathrm{KMnO}_{4}$ solution is required to reach the equivalence point, what is the molarity of the $\mathrm{KMnO}_{4}$ solution?
18.122 Consider the redox titration of 120.0 mL of 0.100 M $\mathrm{FeSO}_{4}$ with $0.120 \mathrm{M} \mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ at $25^{\circ} \mathrm{C}$, assuming that the pH of the solution is maintained at 2.00 with a suitable buffer. The solution is in contact with a platinum electrode and constitutes one half-cell of an electrochemical cell. The other half-cell is a standard hydrogen electrode. The two half-cells are connected with a wire and a salt bridge, and the progress of the titration is monitored by measuring the cell potential with a voltmeter.
(a) Write a balanced net ionic equation for the titration reaction.
(b) What is the cell potential at the equivalence point?
18.123 Consider the reaction that occurs in the hydrogenoxygen fuel cell:

$$
2 \mathrm{H}_{2}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l)
$$

(a) Use the thermodynamic data in Appendix B to calculate the values of $\Delta G^{\circ}$ and $E^{\circ}$ at $95^{\circ} \mathrm{C}$, assuming that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
(b) Calculate the cell voltage at $95^{\circ} \mathrm{C}$ when the partial pressures of $\mathrm{H}_{2}$ and $\mathrm{O}_{2}$ are 25 atm .
18.124 Consider a galvanic cell that utilizes the following half-reactions:

Anode: $\quad \mathrm{Zn}(s)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow$

$$
\mathrm{ZnO}(s)+2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-}
$$

Cathode: $\mathrm{Ag}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Ag}(s)$
(a) Write a balanced equation for the cell reaction, and use the thermodynamic data in Appendix B to calculate the values of $\Delta H^{\circ}, \Delta S^{\circ}$, and $\Delta G^{\circ}$ for the reaction.
(b) What are the values of $E^{\circ}$ and the equilibrium constant $K$ for the cell reaction?
(c) What happens to the cell voltage if aqueous ammonia is added to the cathode compartment? Calculate the cell voltage assuming that the solution in the cathode compartment was prepared by mixing 50.0 mL of $0.100 \mathrm{M} \mathrm{AgNO}_{3}$ and 50.0 mL of $4.00 \mathrm{M} \mathrm{NH}_{3}$.
(d) Will AgCl precipitate if 10.0 mL of 0.200 M NaCl is added to the solution in part (c)? Will AgBr precipitate if 10.0 mL of 0.200 M KBr is added to the resulting solution?
18.125 The nickel-iron battery has an iron anode, an $\mathrm{NiO}(\mathrm{OH})$ cathode, and a KOH electrolyte. This battery uses the following half-reactions and has an $E^{\circ}$ value of 1.37 V at $25^{\circ} \mathrm{C}$ :

$$
\mathrm{Fe}(s)+2 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{Fe}(\mathrm{OH})_{2}(s)+2 \mathrm{e}^{-}
$$

$\mathrm{NiO}(\mathrm{OH})(s)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{e}^{-} \longrightarrow \mathrm{Ni}(\mathrm{OH})_{2}(s)+\mathrm{OH}^{-}(a q)$
(a) Write a balanced equation for the cell reaction.
(b) Calculate $\Delta G^{\circ}$ (in kilojoules) and the equilibrium constant $K$ for the cell reaction at $25^{\circ} \mathrm{C}$.
(c) What is the cell voltage at $25^{\circ} \mathrm{C}$ when the concentration of KOH in the electrolyte is 5.0 M ?
(d) How many grams of $\mathrm{Fe}(\mathrm{OH})_{2}$ are formed at the anode when the battery produces a constant current of 0.250 A for 40.0 min ? How many water molecules are consumed in the process?
18.126 Experimental solid-oxide fuel cells that use butane $\left(\mathrm{C}_{4} \mathrm{H}_{10}\right)$ as the fuel have been reported recently. These cells contain composite metal/metal oxide electrodes and a solid metal oxide electrolyte. The cell half-reactions are

Anode:

$$
\mathrm{C}_{4} \mathrm{H}_{10}(g)+13 \mathrm{O}^{2-}(s) \longrightarrow
$$

$$
4 \mathrm{CO}_{2}(g)+5 \mathrm{H}_{2} \mathrm{O}(l)+26 \mathrm{e}^{-}
$$

Cathode:

$$
\mathrm{O}_{2}(g)+4 \mathrm{e}^{-} \longrightarrow 2 \mathrm{O}^{2-}(s)
$$

(a) Write a balanced equation for the cell reaction.
(b) Use the thermodynamic data in Appendix B to calculate the values of $E^{\circ}$ and the equilibrium constant $K$ for the cell reaction at $25^{\circ} \mathrm{C}$. Will $E^{\circ}$ and $K$ increase, decrease, or remain the same on raising the temperature.
(c) How many grams of butane are required to produce a constant current of 10.5 A for 8.00 h ? How many liters of butane at $20^{\circ} \mathrm{C}$ and 815 mm Hg pressure are required?
18.127 The half-reactions that occur in ordinary alkaline batteries can be written as

Cathode: $\mathrm{MnO}_{2}(s)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{e}^{-} \longrightarrow$

$$
\mathrm{MnO}(\mathrm{OH})(s)+\mathrm{OH}^{-}(a q)
$$

Anode: $\quad \mathrm{Zn}(s)+2 \mathrm{OH}^{-}(a q) \longrightarrow$

$$
\mathrm{Zn}(\mathrm{OH})_{2}(s)+2 \mathrm{e}^{-}
$$

In 1999, researchers in Israel reported a new type of alkaline battery, called a "super-iron" battery. This battery uses the same anode reaction as an ordinary alkaline battery but involves the reduction of $\mathrm{FeO}_{4}{ }^{2-}$ ion (from $\mathrm{K}_{2} \mathrm{FeO}_{4}$ ) to solid $\mathrm{Fe}(\mathrm{OH})_{3}$ at the cathode.
(a) Use the following standard reduction potential and any data from Appendixes C and D to calculate the standard cell potential expected for an ordinary alkaline battery:

$$
\begin{aligned}
& \mathrm{MnO}(\mathrm{OH})(s)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{e}^{-} \longrightarrow \\
& \quad \mathrm{Mn}(\mathrm{OH})_{2}(s)+\mathrm{OH}^{-}(a q) \quad E^{\circ}=-0.380 \mathrm{~V}
\end{aligned}
$$

(b) Write a balanced equation for the cathode halfreaction in a "super-iron" battery. The halfreaction occurs in a basic environment.
(c) A "super-iron" battery should last longer than an ordinary alkaline battery of the same size and weight because its cathode can provide more charge per unit mass. Quantitatively compare the number of coulombs of charge released by the reduction of 10.0 g of $\mathrm{K}_{2} \mathrm{FeO}_{4}$ to $\mathrm{Fe}(\mathrm{OH})_{3}$ with the number of coulombs of charge released by the reduction of 10.0 g of $\mathrm{MnO}_{2}$ to $\mathrm{MnO}(\mathrm{OH})$.
18.128 Gold metal is extracted from its ore by treating the crushed rock with an aerated cyanide solution. The unbalanced equation for the reaction is

$$
\mathrm{Au}(s)+\mathrm{CN}^{-}(a q)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{Au}(\mathrm{CN})_{2}^{-}(a q)
$$

(a) Balance the equation for this reaction in basic solution.
(b) Use any of the following data at $25^{\circ} \mathrm{C}$ to calculate $\Delta G^{\circ}$ for this reaction at $25^{\circ} \mathrm{C}: K_{\mathrm{f}}$ for $\mathrm{Au}(\mathrm{CN})_{2}{ }^{-}=$ $6.2 \times 10^{38}, K_{\mathrm{a}}$ for $\mathrm{HCN}=4.9 \times 10^{-10}$, and standard reduction potentials are

$$
\begin{aligned}
\mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q)+4 \mathrm{e}^{-} \longrightarrow 2 \mathrm{H}_{2} \mathrm{O}(l) & E^{\circ}=1.229 \mathrm{~V} \\
\mathrm{Au}^{3+}(a q)+3 \mathrm{e}^{-} \longrightarrow \mathrm{Au}(s) & E^{\circ}=1.498 \mathrm{~V} \\
\mathrm{Au}^{3+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Au}^{+}(a q) & E^{\circ}=1.401 \mathrm{~V}
\end{aligned}
$$

18.129 Consider the redox titration of 100.0 mL of a solution of $0.010 \mathrm{M} \mathrm{Fe}^{2+}$ in $1.50 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ with a 0.010 M solution of $\mathrm{KMnO}_{4}$. The titration is carried out in an electrochemical cell equipped with a platinum electrode and a calomel reference electrode consisting of an $\mathrm{Hg}_{2} \mathrm{Cl}_{2} / \mathrm{Hg}$ electrode in contact with a saturated KCl solution having $\left[\mathrm{Cl}^{-}\right]=2.9 \mathrm{M}$. Using any data in Appendixes C and D, calculate the cell potential after addition of (a) 5.0 mL , (b) 10.0 mL , (c) 19.0 mL , and (d) 21.0 mL of the $\mathrm{KMnO}_{4}$ solution.

## eMedia Problems

18.130 The Oxidation-Reduction Reactions Part 2 movie (eChapter 18.1) and the Galvanic Cells I movie (eChapter 18.1) both illustrate the same reaction, oxidation of zinc metal by copper(II) ions. Explain why this reaction as it is shown in the Oxidation-Reduction Reactions Part 2 movie cannot be used to generate a voltage.
18.131 The Redox Chemistry of Iron and Copper movie (eChapter 18.3) shows an iron nail in a solution of copper sulfate.
(a) Write the half-reaction for the formation of the copper metal on the surface of the nail.
(b) What species is being oxidized? Write the halfreaction for the oxidation.
(c) Write the equation for the oxidation-reduction reaction taking place in the movie.
(d) What is the sign of $\Delta G^{\circ}$ for the overall process?
18.132 The Nernst Equation activity in eChapter 18.6 allows you to determine the cell potential of the copper-zinc cell as the concentrations of the solutions are changed.
(a) Identify the reactant and product ions of this cell.
(b) According to Le Châtlelier's Principle, what do you expect to happen if you add more copper ion to the solution? How would this affect the cell potential? Use the activity to confirm your answer.
(c) According to Le Châtelier's Principle, what do you expect to happen if you add more zinc ion to the solution? How would this affect the cell potential? Use the activity to confirm your answer.
18.133 Choose a concentration for $\mathrm{Cu}^{2+}$ ion and $\mathrm{Zn}^{2+}$ ion in the Nernst Equation activity (eChapter 18.6), and show how the Nernst Equation can be used to calculate the observed cell potential. What combination of concentrations gives the highest cell potential? Explain this in terms of the Nernst Equation and in terms of equilibrium principles.
18.134 Identify the ion being converted to metal in each of the examples in the Electrolysis activity in eChapter 18.11. Write the reduction half reaction for the conversion of each ion to metal. Which do you expect to deposit the greatest number of moles per second? Why? Does the activity confirm your conclusion? What determines the number of moles of metal deposited?
18.135 The Quantitative Aspects of Electrolysis activity in eChapter 18.13 walks you through the steps for calculating the mass of metal that can be produced by an electrolytic cell for a given time at a certain current. Write down each of the steps required for the problem given; then use a similar procedure to determine the mass of copper that can be produced by passing a current of 18.0 A through a solution of copper(II) ions for 1.0 hour.

## Chapter

## The Main-Group Elements

The main-group elements are the 46 elements that occupy groups 1A-8A of the periodic table.

They are subdivided into the $s$-block elements of groups 1A and 2A, with valence electron configuration $n s^{1}$ or $n s^{2}$,

$\square$and the $p$-block elements of groups $3 \mathrm{~A}-8 \mathrm{~A}$, with valence configurations $n s^{2} n p^{1-6}$. Main-group elements are important because of their high natural abundance and their presence in commercially valuable chemicals. Eight of the 10 most abundant elements in the

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Lightning is a major source of fixed nitrogen. It provides the energy needed to convert $\mathrm{N}_{2}$ to nitrogen oxides.
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- Interlude—Photocopiers

George Gorin, "Mendeleev and Moseley: The Principal Discoverers of the Periodic Law," J. Chem. Educ., Vol. 73, 1996, 490-493.

Eric R. Scerri, "The Evolution of the Periodic System," Scientific American., September 1998, 78-83.
N. K. Goh and L. S. Chia,
"Using the Learning Cycle to Introduce Periodicity," J. Chem. Educ., Vol. 66, 1989, 747. Table
earth's crust and all 10 of the most abundant elements in the human body are main-group elements (Figure 19.1). In addition, the 10 most widely used industrial chemicals contain only main-group elements (Table 19.1).


A FIGURE 19.1 The 10 most abundant elements by mass (a) in the earth's crust and (b) in the human body. All are main-group elements except iron and titanium.

TABLE 19.1 The Top 10 Chemicals (2001 U.S. Production)

| Chemical | Millions <br> of Tons | Principal Uses |
| :--- | :--- | :--- |
| Sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$ | 40.1 | Fertilizers, chemicals, oil refining |
| Nitrogen $\left(\mathrm{N}_{2}\right)$ | 35.5 | Inert atmospheres, low temperatures |
| Oxygen $\left(\mathrm{O}_{2}\right)$ | 26.0 | Steelmaking, welding, medical uses |
| Ethylene $\left(\mathrm{CH}_{2}=\mathrm{CH}_{2}\right)$ | 24.8 | Plastics, antifreeze |
| Lime $(\mathrm{CaO})$ | 20.6 | Steelmaking, chemicals, water treatment |
| Propylene $\left(\mathrm{CH}_{3} \mathrm{CH}=\mathrm{CH}_{2}\right)$ | 14.5 | Plastics, fibers, solvents |
| Ammonia $\left(\mathrm{NH}_{3}\right)$ | 13.0 | Fertilizers, nitric acid |
| Chlorine $\left(\mathrm{Cl}_{2}\right)$ | 12.0 | Chemicals, plastics, water treatment |
| Phosphoric acid $\left(\mathrm{H}_{3} \mathrm{PO}_{4}\right)$ | 11.6 | Fertilizers, detergents |
| Sodium hydroxide $(\mathrm{NaOH})$ | 10.7 | Chemicals, textiles, soaps |

In Sections 6.7-6.11, we surveyed the alkali and alkaline earth metals (groups 1 A and 2A), aluminum (group 3A), the halogens (group 7A), and the noble gases (group 8A). In Chapter 14, we looked in detail at the chemistry of hydrogen and oxygen. Now we'll examine the remaining main-group elements, paying special attention to boron (group 3A), carbon and silicon (group 4A), nitrogen and phosphorus (group 5A), and sulfur (group 6A).

### 19.1 A Review of General Properties and Periodic Trends

Let's begin our survey of the main-group elements by reviewing the periodic trends that make it possible to classify these elements as metals, nonmetals, or semimetals. Figure 19.2 shows the main-group regions of the periodic table, with metals to the left of the heavy stairstep line, nonmetals to the right of the line, and semimetals-elements with intermediate properties-along the line. The elements usually classified as semimetals are boron (group 3A), silicon and germanium (group 4A), arsenic and antimony (group 5A), tellurium (group 6A), and astatine (group 7A).

Atomic radius and metallic character decrease

|  | 1 1 A |  |  |  |  |  |  |  |  | $\begin{array}{r} 18 \\ 8 \mathrm{~A} \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | H | $\begin{gathered} 2 \\ 2 \mathrm{~A} \end{gathered}$ |  |  | $\begin{array}{r} 13 \\ 3 \mathrm{~A} \end{array}$ | $\begin{array}{r} 14 \\ 4 \mathrm{~A} \end{array}$ | $\begin{array}{r} 15 \\ 5 \mathrm{~A} \end{array}$ | $\begin{aligned} & 16 \\ & 6 \mathrm{~A} \end{aligned}$ | $\begin{array}{r} 17 \\ 7 \mathrm{~A} \end{array}$ | Нe |
|  | Li | Be |  |  | B | C | N | O | F | Ne |
|  | Na | Mg |  |  | Al | Si | P | S | Cl | Ar |
|  | K | Ca |  |  | Ga | Ge | As | Se | Br | Kr |
|  | Rb | Sr |  |  | In | Sn | Sb | Te | I | Xe |
|  | Cs | Ba |  |  | Tl | Pb | Bi | Po | At | Rn |
|  | Fr | Ra |  |  |  | 114 |  | 116 |  |  |

From left to right across the periodic table, the effective nuclear charge $Z_{\text {eff }}$ increases because each additional valence electron does not completely shield the additional nuclear charge (Section 5.11). As a result, the atom's electrons are more strongly attracted to the nucleus, ionization energy generally increases, atomic radius decreases, and electronegativity increases. The elements on the left side of the table tend to form cations by losing electrons, and those on the right tend to form anions by gaining electrons. Thus, metallic character decreases and nonmetallic character increases across the table from left to right. In the third row, for example, sodium, magnesium, and aluminum are metals, silicon is a semimetal, and phosphorus, sulfur, and chlorine are nonmetals.

From the top to the bottom of a group in the periodic table, additional shells of electrons are occupied, and atomic radius therefore increases. Because the valence electrons are farther from the nucleus, though, ionization energy and electronegativity generally decrease. As a result, metallic character increases and nonmetallic character decreases down a group from top to bottom. In group 4A, for example, carbon is a nonmetal, silicon and germanium are semimetals, and tin and lead are metals. The horizontal and vertical periodic trends combine to locate the element with the most metallic character (francium) in the lower left of the periodic table, the element with the most nonmetallic character (fluorine) in the upper right, and the semimetals along the diagonal stairstep that stretches across the middle.

In earlier chapters, we saw examples of how the metallic or nonmetallic character of an element affects its chemistry. Metals tend to form ionic compounds with nonmetals, whereas nonmetals tend to form covalent, molecular compounds with one another. Thus, binary metallic hydrides, such as NaH and $\mathrm{CaH}_{2}$, are ionic solids with high melting points, and binary nonmetallic hydrides, such as $\mathrm{CH}_{4}, \mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{O}$, and HF , are covalent, molecular compounds that exist at room temperature as gases or volatile liquids (Section 14.5).

Oxides exhibit similar trends. In the third row, for example, $\mathrm{Na}_{2} \mathrm{O}$ and MgO are typical high-melting, ionic solids, and $\mathrm{P}_{4} \mathrm{O}_{10}, \mathrm{SO}_{3}$, and $\mathrm{Cl}_{2} \mathrm{O}_{7}$ are volatile, covalent, molecular compounds (Section 14.9). The metallic or nonmetallic character of an oxide also affects its acid-base properties. $\mathrm{Na}_{2} \mathrm{O}$ and MgO are basic, for example,

FIGURE 19.2 Periodic trends in the properties of the main-group elements. The metallic elements (green) and the nonmetallic elements (lavender) are separated by the heavy stairstep line. The semimetals, shown in blue, lie along the line.

Kimberley A. Waldron, Eric M. Fehringer, Amy E. Streeb, Jennifer E. Trotsky, and Joshua J. Pearson, "Screen Percentages Based on Slater Effective Nuclear Charge as a Versatile Tool for Teaching Periodic Trends," J. Chem. Educ., Vol. 78, 2001, 635-639.

$\square$Joan Mason, "Periodic Contractions Among the Elements; Or, on Being the Right Size," J. Chem. Educ., Vol. 65, 1988, 17-20.
7. Gabriel Pinto, "Using Balls from Different Sports to Model the Variation of Atomic Sizes," J. Chem. Educ., Vol. 75, 1998, 725-726.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Halogens Compete for Electrons," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 60-61.


Periodic Trends:
Acid-Base Behavior of Oxides movie

Ronald L. Rich, "Periodicity in the Acid-Base Behavior of Oxides and Hydroxides," J. Chem. Educ., Vol. 62, 1985, 44.

Bassam Z. Shakhashiri, "Acidic and Basic Properties of
Oxides," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989), pp. 109-113.
whereas $\mathrm{P}_{4} \mathrm{O}_{10}, \mathrm{SO}_{3}$, and $\mathrm{Cl}_{2} \mathrm{O}_{7}$ are acidic. Table 19.2 summarizes some of the properties that distinguish metallic and nonmetallic elements.

TABLE 19.2 Properties of Metallic and Nonmetallic Elements

| Metals | Nonmetals |
| :--- | :--- |
| All are solids at $25^{\circ} \mathrm{C}$ except Hg, | Eleven are gases at $25^{\circ} \mathrm{C}$, one is a liquid $(\mathrm{Br})$, <br> and five are solids $(\mathrm{C}, \mathrm{P}, \mathrm{S}, \mathrm{Se}$, and I$)$ |
| $\quad$ which is a liquid | Most lack a metallic luster |
| Most have a silvery shine | Nonmalleable and brittle |
| Malleable and ductile | Poor conductors of heat and electricity, |
| Good conductors of heat and | except graphite |
| electricity | Relatively high ionization energies |
| Relatively low ionization energies | Relatively high electronegativities |
| Relatively low electronegativities | Gain electrons to form anions; share electrons |
| Lose electrons to form cations | to form oxoanions |
| Hydrides are ionic (or interstitial) | Hydrides are covalent and molecular |
| Oxides are ionic and basic | Oxides are covalent, molecular, and acidic |

## Worked Example 19.1

Use the periodic table to predict which element in each of the following pairs has more metallic character:
(a) Ga or As
(b) P or Bi
(c) Sb or S
(d) Sn or Ba

## Strategy

Since metallic character increases from right to left and from top to bottom in the periodic table, we look to see which of the pair of elements lies farther toward the lower left of the table.

## Solution

(a) Ga and As are in the same row of the periodic table, but Ga (group 3A) lies to the left of As (group 5A). Therefore, Ga is more metallic.
(b) Bi lies below P in group 5A and is therefore more metallic.
(c) Sb (group 5A) has more metallic character because it lies below and to the left of S (group 6A).
(d) Ba (group 2A) is more metallic because it lies below and to the left of Sn (group 4A).

PROBLEM 19.1 Predict which element in each of the following pairs has more nonmetallic character:
(a) B or Al
(b) Ge or Br
(c) In or Se
(d) Cl or Te

### 19.2 Distinctive Properties of the Second-Row Elements

The properties of elements in the second row of the periodic table differ markedly from those of heavier elements in the same periodic group. The second-row atoms have especially small sizes and especially high electronegativities. In group 5A, for example, the electronegativity of N is 3.0 , whereas the electronegativities of P , $\mathrm{As}, \mathrm{Sb}$, and Bi are all in the range 2.1-1.9. Figure 7.4 (page 248) shows graphically
the discontinuity in electronegativity that distinguishes the second-row elements from other elements of the same periodic group.

The small sizes and high electronegativities of the second-row elements accentuate their nonmetallic behavior. Thus, BeO is amphoteric, but the oxides of the other group 2A elements are basic. Boron differs from the metallic elements of group 3A because it forms mainly covalent, molecular compounds. For example, $\mathrm{BF}_{3}\left(\mathrm{bp}-100^{\circ} \mathrm{C}\right.$ ) is a gaseous, molecular halide, but $\mathrm{AlF}_{3}\left(\mathrm{mp} 1290^{\circ} \mathrm{C}\right)$ is a typical high-melting, ionic solid. Furthermore, hydrogen bonding interactions are generally restricted to compounds of the highly electronegative second-row elements $\mathrm{N}, \mathrm{O}$, and F (Section 10.2). Recall also that HF contrasts with $\mathrm{HCl}, \mathrm{HBr}$, and HI in being the only weak hydrohalic acid (Section 15.2).

Another factor that distinguishes the second-row elements from the heavier elements is their lack of valence $d$ orbitals. Because the second-row elements have only four valence orbitals ( $2 s, 2 p_{x}, 2 p_{y}$, and $2 p_{z}$ ), they generally form a maximum of four covalent bonds. By contrast, the larger atoms of the third-row elements can accommodate more than four nearest neighbors and can use $d$ orbitals to form more than four bonds. Thus, nitrogen forms only $\mathrm{NCl}_{3}$, but phosphorus forms both $\mathrm{PCl}_{3}$ and $\mathrm{PCl}_{5}$ :




A further consequence of the small size of the second-row atoms $\mathrm{C}, \mathrm{N}$, and O is their ability to form multiple bonds by $\pi$ overlap of the $2 p$ orbitals. By contrast, the $3 p$ orbitals of the corresponding third-row atoms $\mathrm{Si}, \mathrm{P}$, and S are more diffuse, and the longer bond distances for these larger atoms result in poor $\pi$ overlap.


As a result of this poor overlap, $\pi$ bonds involving $p$ orbitals are rare for elements of the third and higher rows. Although compounds with $\mathrm{C}=\mathrm{C}$ double bonds are common, molecules with $\mathrm{Si}=\mathrm{Si}$ double bonds are uncommon and have been synthesized only recently. In group 5A, elemental nitrogen contains triply bonded $\mathrm{N}_{2}$ molecules, whereas white phosphorus contains tetrahedral $\mathrm{P}_{4}$ molecules, in which each P atom forms three single bonds rather than one triple bond. Similarly, $\mathrm{O}_{2}$ contains an $\mathrm{O}=\mathrm{O}$ double bond, whereas elemental sulfur contains crown-shaped $\mathrm{S}_{8}$ rings, in which each S atom forms two single bonds rather than one double bond.



Interactive Periodic Table

0
Due to small size, high electronegativity, ability to form $\pi$ bonds, and unavailability of $d$ orbitals, the first member of each $s$ - and $p$-block group differs substantially in its chemistry from the other members of the group.

$\sigma$Compounds of period 2 elements have a maximum of four covalent bonds and an octet of valence electrons; elements beyond period 2 may have more than four bonds and more than eight valence electrons.


$\nabla$Molecules of period $2 p$-block elements contain single, double, or triple bonds; molecules of higher period elements generally contain only single bonds.

## Worked Example 19.2

Account for the following observations:
(a) $\mathrm{CO}_{2}$ is a gaseous molecular substance, whereas $\mathrm{SiO}_{2}$ is a covalent network solid in which $\mathrm{SiO}_{4}$ tetrahedra are linked to four neighboring $\mathrm{SiO}_{4}$ tetrahedra by shared oxygen atoms.

(b) Glass made of $\mathrm{SiO}_{2}$ is attacked by hydrofluoric acid with the formation of $\mathrm{SiF}_{6}{ }^{2-}$ anions. The analogous $\mathrm{CF}_{6}{ }^{2-}$ anion does not exist.

## Strategy

To account for these differences, remember that (a) second-row atoms are smaller and form stronger multiple bonds than third-row atoms and (b) third-row atoms can form more than four bonds because of their larger size and the availability of $d$ orbitals.

## Solution

(a) Because of its small size and good $\pi$ overlap with other small atoms, carbon forms strong double bonds with two oxygens to give discrete $\mathrm{CO}_{2}$ molecules. Because the larger Si atom does not have good $\pi$ overlap with other atoms, it uses its four valence electrons to form four single bonds rather than two double bonds.
(b) The larger silicon atom has $3 d$ orbitals and can use octahedral $s p^{3} d^{2}$ hybrid orbitals to bond to six $\mathrm{F}^{-}$ions. With just $2 s$ and $2 p$ valence orbitals, the smaller carbon atom can form a maximum of only four bonds.


- PROBLEM 19.2
(a) Draw electron-dot structures for $\mathrm{HNO}_{3}$ and $\mathrm{H}_{3} \mathrm{PO}_{4}$, and suggest a reason for the difference in the formulas of these acids.
(b) Sulfur forms $\mathrm{SF}_{6}$, but oxygen bonds to a maximum of two F atoms, yielding $\mathrm{OF}_{2}$. Explain.
- KEY CONCEPT PROBLEM 19.3 The organic solvent acetone has the molecular formula $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CO}$. The silicon analogue, a thermally stable lubricant, is a polymer, $\left[\left(\mathrm{CH}_{3}\right)_{2} \mathrm{SiO}\right]_{n}$. Account for the difference in structure:


Acetone


## 19.3 | The Group 3A Elements

The group 3A elements are boron, aluminum, gallium, indium, and thallium. We discussed aluminum, the most important of these elements, in Section 6.9, and we'll take up boron in the next section. Gallium is remarkable for its unusually low melting point $\left(29.7^{\circ} \mathrm{C}\right)$ and unusually large liquid range $\left(29.7-2204^{\circ} \mathrm{C}\right)$. Its most important use is in making gallium arsenide (GaAs), a semiconductor
material employed in the manufacture of diode lasers for laser printers, compactdisc players, and fiber-optic communication devices. (We'll say more about semiconductors in Section 21.5.) Indium is also used in making semiconductor devices, such as transistors and electrical resistance thermometers called thermistors. Thallium is extremely toxic and has no commercial uses.


The valence electron configuration of the group 3A elements is $n s^{2} n p^{1}$, and their primary oxidation state is +3 . In addition, the heavier elements exhibit a +1 state, which is uncommon for gallium and indium but is the most stable oxidation state for thallium.

Despite some irregularities, the properties of the group 3A elements are generally consistent with increasing metallic character down the group (Tables 6.6 and 19.3). All the group 3A elements are metals except boron. Boron has a much smaller atomic radius and a higher electronegativity than the other elements of the group; it therefore shares its valence electrons in covalent bonds rather than transferring them to another element. Accordingly, boron has nonmetallic properties.

TABLE 19.3 Properties of the Group 3A Elements

| Property | Boron | Aluminum | Gallium | Indium | Thallium |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Valence electron configuration | $2 s^{2} 2 p^{1}$ | $3 s^{2} 3 p^{1}$ | $4 s^{2} 4 p^{1}$ | $5 s^{2} 5 p^{1}$ | $6 s^{2} 6 p^{1}$ |
| Common oxidation states | +3 | +3 | +3 | +3 | $+3,+1$ |
| Atomic radius (pm) | 83 | 143 | 135 | 167 | 170 |
| $\mathrm{M}^{3+}$ ionic radius (pm) |  | 51 | 62 | 81 | 95 |
| First ionization energy (kJ/mol) | 801 | 578 | 579 | 558 | 589 |
| Electronegativity | 2.0 | 1.5 | 1.6 | 1.7 | 1.8 |
| ${\operatorname{Redox~potential,~} E^{\circ}(\mathrm{V}) \text { for }}^{\mathrm{M}^{3+}(a q)+3 \mathrm{e}^{-} \rightarrow \mathrm{M}(s)}$ | $-0.87^{*}$ | -1.66 | -0.56 | -0.34 | $-0.34^{\dagger}$ | $\mathrm{M}^{3+}(a q)+3 \mathrm{e}^{-} \rightarrow \mathrm{M}(s)$

${ }^{*} E^{\circ}$ for the reaction $\mathrm{B}(\mathrm{OH})_{3}(a q)+3 \mathrm{H}^{+}(a q)+3 \mathrm{e}^{-} \rightarrow \mathrm{B}(s)+3 \mathrm{H}_{2} \mathrm{O}(l)$
${ }^{\dagger} E^{\circ}$ for the reaction $\mathrm{Tl}^{+}(a q)+\mathrm{e}^{-} \rightarrow \mathrm{Tl}(s)$

## 19.4 | Boron

Boron is a relatively rare element, accounting for only about $0.001 \%$ of the earth's crust by mass. Nevertheless, boron is readily available because it occurs in concentrated deposits of borate minerals such as borax, $\mathrm{Na}_{2} \mathrm{~B}_{4} \mathrm{O}_{7} \cdot 10 \mathrm{H}_{2} \mathrm{O}$.

Elemental boron can be prepared by the high-temperature reduction of $\mathrm{B}_{2} \mathrm{O}_{3}$ with magnesium, but the product is impure and amorphous:

$$
\mathrm{B}_{2} \mathrm{O}_{3}(l)+3 \mathrm{Mg}(s) \longrightarrow 2 \mathrm{~B}(s)+3 \mathrm{MgO}(s)
$$

(a) A sample of gallium metal. (b) The semiconductor material gallium arsenide is prepared by heating gallium and arsenic in a furnace. The tube contains bars of gallium metal (left) and pieces of arsenic (right).

0
Heavier $p$-block elements tend to exhibit a stable oxidation state equal to the group number minus 2 .


High-purity, crystalline boron is best obtained by the reaction of boron tribromide and hydrogen on a heated tantalum filament at high temperatures:

$$
2 \mathrm{BBr}_{3}(g)+3 \mathrm{H}_{2}(g) \xrightarrow[1200^{\circ} \mathrm{C}]{\text { Ta wire }} 2 \mathrm{~B}(s)+6 \mathrm{HBr}(g)
$$

Crystalline boron is a strong, hard, high-melting substance $\left(\mathrm{mp} 2075^{\circ} \mathrm{C}\right)$ that is chemically inert at room temperature, except for reaction with fluorine. These properties make boron fibers a desirable component in high-strength composite materials used in making sports equipment and military aircraft (see Section 21.8). Unlike $\mathrm{Al}, \mathrm{Ga}$, In, and Tl , which are metallic conductors, boron is a semiconductor.

> The borate minerals in this open-pit borax mine near Boron, California, are believed to have been formed by the evaporation of water from hot springs that were once present.


## Boron Compounds



- The boron halides are Lewis acids because they have a vacant $2 p$ orbital.


Boron Halides The boron halides are highly reactive, volatile, covalent compounds that consist of trigonal planar $\mathrm{BX}_{3}$ molecules. At room temperature, $\mathrm{BF}_{3}$ and $\mathrm{BCl}_{3}$ are gases, $\mathrm{BBr}_{3}$ is a liquid, and $\mathrm{BI}_{3}$ is a low-melting solid ( $\mathrm{mp} 43^{\circ} \mathrm{C}$ ). In their most important reactions, the boron halides behave as Lewis acids. For example, $\mathrm{BF}_{3}$ reacts with ammonia to give the Lewis acid-base adduct $\mathrm{F}_{3} \mathrm{~B}-\mathrm{NH}_{3}$ (Section 15.16); it reacts with metal fluorides, yielding salts that contain the tetrahedral $\mathrm{BF}_{4}{ }^{-}$anion; and it acts as a catalyst in many industrially important organic reactions. In all these reactions, the boron atom uses its vacant $2 p$ orbital to accept a share in a pair of electrons from a Lewis base.

Boron Hydrides The boron hydrides, or boranes, are volatile, molecular compounds with formulas $\mathrm{B}_{n} \mathrm{H}_{m}$. The simplest is diborane $\left(\mathrm{B}_{2} \mathrm{H}_{6}\right)$, the dimer of the unstable $\mathrm{BH}_{3}$. Diborane can be prepared by the reaction of sodium borohydride $\left(\mathrm{NaBH}_{4}\right)$ and iodine in an appropriate organic solvent:

$$
2 \mathrm{NaBH}_{4}+\mathrm{I}_{2} \longrightarrow \mathrm{~B}_{2} \mathrm{H}_{6}+\mathrm{H}_{2}+2 \mathrm{NaI}
$$

Because boranes have high heats of combustion, they were once considered as potential lightweight, high-energy rocket fuels, but they proved to be too expensive to prepare. Nevertheless, boranes continue to be of interest to chemists because of their unusual structures and bonding.

The diborane molecule has a structure in which two $\mathrm{BH}_{2}$ groups are connected by two bridging H atoms. The geometry about the B atoms is roughly tetrahedral, and the bridging $\mathrm{B}-\mathrm{H}$ bonds are significantly longer than the terminal $\mathrm{B}-\mathrm{H}$ bonds, 133 pm versus 119 pm . The structure differs from that of ethane $\left(\mathrm{C}_{2} \mathrm{H}_{6}\right)$ and is unusual because hydrogen normally forms only one bond.


Diborane


Ethane

If each line in the structural formula of diborane represented an ordinary 2-electron covalent bond between 2 atoms (a two-center, two-electron, or $2 \mathrm{c}-2 \mathrm{e}$ bond), there would be 8 pairs, or 16 valence electrons. Diborane, however, has a total of only 12 valence electrons- 3 electrons from each boron and 1 from each hydrogen. Thus, diborane is said to be electron-deficient: It doesn't have enough electrons to form a $2 \mathrm{c}-2 \mathrm{e}$ bond between each pair of bonded atoms.

Because the geometry about the B atoms is roughly tetrahedral, we can assume that each boron uses $s p^{3}$ hybrid orbitals to bond to the four neighboring H atoms. The four terminal $\mathrm{B}-\mathrm{H}$ bonds are assumed to be ordinary $2 \mathrm{c}-2 \mathrm{e}$ bonds, formed by the overlap of a boron $s p^{3}$ hybrid orbital and a hydrogen $1 s$ orbital, thereby using 4 of the 6 pairs of electrons. Each of the 2 remaining pairs of electrons forms a three-center, two-electron bond (3c-2e bond), which joins each bridging H atom to both B atoms. Each electron pair occupies a three-center molecular orbital formed by the interaction of three atomic orbitals-one $s p^{3}$ hybrid orbital from each $B$ atom and the $1 s$ orbital on one bridging H atom (Figure 19.3). Because the 2 electrons in the $\mathrm{B}-\mathrm{H}-\mathrm{B}$ bridge are spread out over 3 atoms, the electron density between adjacent atoms is less than in an ordinary $2 \mathrm{c}-2 \mathrm{e}$ bond. The bridging $\mathrm{B}-\mathrm{H}$ bonds are therefore weaker and correspondingly longer than the terminal $\mathrm{B}-\mathrm{H}$ bonds.

- PROBLEM 19.4 Why is an ethane-like structure unlikely for diborane?


## 19.5 | The Group 4A Elements

The group 4A elements-carbon, silicon, germanium, tin, and lead-are especially important, both in industry and in living organisms. Carbon is present in all plants and animals, accounts for $23 \%$ of the mass of the human body, and is an essential constituent of the molecules on which life is based. Silicon is equally important in the mineral world: It is present in numerous silicate minerals and is the second most abundant element in the earth's crust. Both silicon and germanium are used in making modern solid-state electronic devices. Tin and lead have been known and used since ancient times.

The group 4A elements exemplify the increase in metallic character down a group in the periodic table: Carbon is a nonmetal; silicon and germanium are semimetals; and tin and lead are metals. The usual periodic trends in atomic size, ionization energy, and electronegativity are evident in the data of Table 19.4.


A FIGURE 19.3 Three-center bonding molecular orbitals in diborane. Each of the two MOs (one shown darker than the other) is formed by the interaction of an $s p^{3}$ hybrid orbital on each B atom and the 1 s orbital on one bridging H atom. Each MO contains one pair of electrons and accounts for the bonding in one $\mathrm{B}-\mathrm{H}-\mathrm{B}$ bridge.

$\nabla$2c-2e terminal B-H bonds are stronger and shorter than bridging $3 c-2 e$ bonds in $\mathrm{B}_{2} \mathrm{H}_{6}$.


TABLE 19.4 Properties of the Group 4A Elements

| Property | Carbon | Silicon | Germanium | Tin | Lead |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Valence electron configuration | $2 s^{2} 2 p^{2}$ | $3 s^{2} 3 p^{2}$ | $4 s^{2} 4 p^{2}$ | $5 s^{2} 5 p^{2}$ | $6 s^{2} 6 p^{2}$ |
| Melting point $\left({ }^{\circ} \mathrm{C}\right)$ | $>3550^{*}$ | 1414 | 938 | $232^{\dagger}$ | 327 |
| Boiling point $\left({ }^{\circ} \mathrm{C}\right)$ |  | 3265 | 2833 | 2602 | 1749 |
| Density $\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ | $3.51^{*}$ | 2.33 | 5.32 | $7.26^{\dagger}$ | 11.3 |
| Abundance in Earth's crust (mass \%) | 0.020 | 28.2 | 0.0005 | 0.0002 | 0.0013 |
| Common oxidation states | $+2,+4$ | +4 | +4 | $+2,+4$ | $+2,+4$ |
| Atomic radius $(\mathrm{pm})$ | 77 | 117 | 122 | 140 | 175 |
| First ionization energy $(\mathrm{kJ} / \mathrm{mol})$ | 1086 | 786 | 762 | 709 | 716 |
| Electronegativity | 2.5 | 1.8 | 1.8 | 1.8 | 1.9 |
| Redox potential, $\mathrm{E}^{\circ}(\mathrm{V})$ for |  |  | -0.14 | -0.13 |  |
| $\mathrm{M}^{2+}(a q)+2 \mathrm{e}^{-\rightarrow \mathrm{M}(s)}$ |  |  |  |  |  |

[^21]VStudents tend to equate ionic character with high oxidation state. On the contrary, the higher the oxidation state, the more covalent the bonds formed by an element. Bonds in $\mathrm{SnCl}_{4}$ are more covalent than those in $\mathrm{SnCl}_{2}$.


Diamond is an electrical insulator, but graphite is an electrical conductor.


Because the group 4A elements have the valence electron configuration $n s^{2} n p^{2}$, their most common oxidation state is +4 , as in $\mathrm{CCl}_{4}, \mathrm{SiCl}_{4}, \mathrm{GeCl}_{4}, \mathrm{SnCl}_{4}$, and $\mathrm{PbCl}_{4}$. These compounds are volatile, molecular liquids in which the group 4A atom uses tetrahedral $s p^{3}$ hybrid orbitals to form covalent bonds to the Cl atoms. The +2 oxidation state occurs for tin and lead and is the most stable oxidation state for lead. Both $\mathrm{Sn}^{2+}(a q)$ and $\mathrm{Pb}^{2+}(a q)$ are common solution species, but there are no simple $\mathrm{M}^{4+}(a q)$ ions for any of the group 4A elements. Instead, $\mathrm{M}(\mathrm{IV})$ species exist in solution as covalently bonded complex ions-for example, $\mathrm{SiF}_{6}{ }^{2-}, \mathrm{GeCl}_{6}{ }^{2-}, \mathrm{Sn}(\mathrm{OH})_{6}{ }^{2-}$, and $\mathrm{Pb}(\mathrm{OH})_{6}{ }^{2-}$. In general, the +4 oxidation-state compounds are covalent, and the compounds with tin and lead in the +2 oxidation state are largely ionic.

## 19.6 | Carbon

Carbon, although the second most abundant element in living organisms, accounts for only $0.02 \%$ of the mass of the earth's crust. It is present in carbonate minerals, such as limestone $\left(\mathrm{CaCO}_{3}\right)$, and in fossil fuels, such as coal, petroleum, and natural gas. In uncombined form, carbon is found as diamond and graphite.

Recall from Section 10.10 that diamond has a covalent network structure in which each C atom uses $s p^{3}$ hybrid orbitals to form a tetrahedral array of $\sigma$ bonds, with bond lengths of 154 pm . (See Figure 10.26b, page 412.) The interlocking, threedimensional network of strong bonds makes diamond the hardest known substance and gives it the highest melting point for an element $\left(>3550^{\circ} \mathrm{C}\right)$. Because the valence electrons are localized in the $\sigma$ bonds, they are not free to move when an electrical potential is applied and diamond is therefore an electrical insulator.

Graphite has a two-dimensional sheetlike structure (Figure 10.26a, page 412) in which each C atom uses $s p^{2}$ hybrid orbitals to form trigonal planar $\sigma$ bonds to three neighboring C atoms. In addition, each C atom uses its remaining $p$ orbital, which is perpendicular to the plane of the sheet, to form a $\pi$ bond. Because each C atom must share its $\pi$ bond with its three neighbors, the $\pi$ electrons are delocalized and are free to move in the plane of the sheet. As a result, the electrical conductivity of graphite in a direction parallel to the sheets is about $10^{20}$ times greater than the conductivity of diamond, which makes graphite useful as an electrode material.

The carbon sheets in graphite are separated by a distance of 335 pm and are held together by only London dispersion forces. Atmospheric gases can be absorbed between the sheets, thus enabling the sheets to easily slide over one another. As a result, graphite has a slippery feel and can be used as a lubricant. Because the sheets are so far apart, it's relatively difficult for an electron to hop from one sheet to the next and the electrical conductivity in the direction perpendicular to the sheets is therefore about $10^{4}$ times smaller than the conductivity parallel to the sheets.

A third crystalline allotrope of carbon, called fullerene, was discovered in 1985 by Robert F. Curl, Jr., Harold Kroto, and Richard E. Smalley, who were awarded the 1996 Nobel Prize in chemistry for their pioneering work. This allotrope consists of nearly spherical $\mathrm{C}_{60}$ molecules with the shape of a soccer ball (Figure 10.27a, page 412). Fullerene can be prepared in relatively large amounts by electrically heating a graphite rod in an atmosphere of helium. Unlike diamond and graphite, $\mathrm{C}_{60}$ is a molecular substance, and it is therefore soluble in nonpolar organic solvents. Numerous derivatives of fullerene have been prepared, including compounds such as $\mathrm{C}_{60} \mathrm{~F}_{36}$, in which other atoms are attached to the outside of the $\mathrm{C}_{60}$ cage, and compounds such as $\mathrm{La@} \mathrm{C}_{60}$, in which a metal atom is trapped within the cage. (The symbol @ means that the lanthanum atom is located inside the $\mathrm{C}_{60}$ cage.) Closely related to $\mathrm{C}_{60}$ are other carbon clusters, such as the eggshaped molecule $\mathrm{C}_{70}$ and the recently discovered tube-shaped molecules called carbon nanotubes. These ultrasmall tubes are stronger than steel. Some are metallic and conduct electricity 10 times better than copper. Others are semiconductors and look to be a top candidate to eventually replace silicon in electronic devices.


Carbon also exists in more than 40 amorphous (noncrystalline) forms that resemble graphite; coke, charcoal, and carbon black are a few. Coke is made by heating coal in the absence of air and is used as a reducing agent in the manufacture of steel (Section 21.3). Charcoal is formed when wood is heated in the absence of air. Because charcoal has a porous, spongelike structure with an immense surface area ( $\sim 25 \mathrm{~m}^{2} / \mathrm{g}$ ), it has strong adsorbent properties and is widely used in filters for removing foul-smelling molecules from air and water. Carbon black, used in the manufacture of printing inks and automobile tires, is made by heating hydrocarbons such as natural gas $\left(\mathrm{CH}_{4}\right)$ in a limited supply of oxygen:

$$
\mathrm{CH}_{4}(g)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{C}(s)+2 \mathrm{H}_{2} \mathrm{O}(g)
$$

## Carbon Compounds

Carbon forms many millions of compounds, most of which are classified as organic; only $\mathrm{CO}, \mathrm{CO}_{2}, \mathrm{CaCO}_{3}, \mathrm{HCN}, \mathrm{CaC}_{2}$, and a handful of others are considered to be inorganic. The distinction is a historical one rather than a scientific one, though, as discussed in more detail in Chapter 23. For the present, we'll look only at some simple inorganic compounds of carbon.
Oxides of Carbon The most important oxides of carbon are carbon monoxide (CO) and carbon dioxide ( $\mathrm{CO}_{2}$ ). Carbon monoxide is a colorless, odorless, toxic gas that forms when carbon or hydrocarbon fuels are burned in a limited supply of oxygen. In an excess of oxygen, CO burns to give $\mathrm{CO}_{2}$ :

$$
\begin{aligned}
2 \mathrm{C}(s)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{CO}(g) & \Delta H^{\circ}=-221 \mathrm{~kJ} \\
2 \mathrm{CO}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{CO}_{2}(g) & \Delta H^{\circ}=-566 \mathrm{~kJ}
\end{aligned}
$$

Carbon monoxide is synthesized industrially, along with $\mathrm{H}_{2}$, by heating hydrocarbons or coke with steam (Section 14.3). One of its main uses is in the industrial synthesis of methanol, $\mathrm{CH}_{3} \mathrm{OH}$ :

$$
\mathrm{CO}(\mathrm{~g})+2 \mathrm{H}_{2}(\mathrm{~g}) \frac{400^{\circ} \mathrm{C}}{\mathrm{ZnO} / \mathrm{Cr}_{2} \mathrm{O}_{3} \text { catalyst }} \mathrm{CH}_{3} \mathrm{OH}(\mathrm{~g})
$$

The high toxicity of CO results from its ability to bond strongly to the iron(II) atom of hemoglobin, the oxygen-carrying protein in red blood cells. Because hemoglobin has a greater affinity for CO than for $\mathrm{O}_{2}$ by a factor of 200, even small concentrations of CO in the blood can convert a substantial fraction of the $\mathrm{O}_{2}$-bonded hemoglobin, called oxyhemoglobin, to the CO-bonded form, called carboxyhemoglobin, thus impairing the ability of hemoglobin to carry $\mathrm{O}_{2}$ to the tissues:


A A carbon nanotube has walls made of graphite sheets rolled into a cylinder and hemispherical tips made of a portion of a fullerene molecule.

A CO concentration in air of only 200 ppm can produce symptoms such as headache, dizziness, and nausea, and a concentration of 1000 ppm can cause death within 4 hours. One hazard of cigarette smoking is chronic exposure to low levels of CO. Because CO reduces the blood's ability to carry $\mathrm{O}_{2}$, the heart must work harder to supply $\mathrm{O}_{2}$ to the tissues, thus increasing the risk of heart attack.

Carbon dioxide is a colorless, odorless, nonpoisonous gas. It is produced when fuels are burned in an excess of oxygen and is an end product of food metabolism in humans and animals. Commercially, carbon dioxide is obtained as a by-product of the yeast-catalyzed fermentation of sugar in the manufacture of alcoholic beverages:


Carbon dioxide can also be obtained by heating metal carbonates, and it is produced in the laboratory when metal carbonates are treated with strong acids:

$$
\begin{aligned}
& \mathrm{CaCO}_{3}(s) \xrightarrow{\text { Heat }} \mathrm{CaO}(s)+\mathrm{CO}_{2}(g) \\
& \mathrm{Na}_{2} \mathrm{CO}_{3}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow 2 \mathrm{Na}^{+}(a q)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

Carbon dioxide is used in beverages and in fire extinguishers. The "bite" of carbonated beverages is due to the mild acidity of $\mathrm{CO}_{2}$ solutions ( $\mathrm{pH} \approx 4$ ), which results when approximately $0.3 \%$ of the dissolved $\mathrm{CO}_{2}$ is converted to carbonic acid $\left(\mathrm{H}_{2} \mathrm{CO}_{3}\right)$, a weak diprotic acid (Section 15.11):

$$
\mathrm{CO}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{2} \mathrm{CO}_{3}(a q) \rightleftharpoons \mathrm{H}^{+}(a q)+\mathrm{HCO}_{3}^{-}(a q)
$$

$\mathrm{CO}_{2}$ is useful in fighting fires because it is nonflammable and is about 1.5 times more dense than air. It therefore settles over a small fire like a blanket, separating the fire from its source of oxygen. Solid $\mathrm{CO}_{2}$ (dry ice), which sublimes at $-78^{\circ} \mathrm{C}$, is used primarily as a refrigerant.
These cattle were asphyxiated by an enormous bubble of carbon dioxide that welled up from the depths of Lake Nyos, Cameroon, in 1986. The gas, although not toxic in itself, is heavier than air. Released suddenly from solution, possibly as a result of volcanic activity, it blanketed the shores and overflowed into lower-lying surrounding regions, displacing oxygen and suffocating some 1700 people.


Carbonates Carbonic acid, $\mathrm{H}_{2} \mathrm{CO}_{3}$, has never been isolated as a pure substance, but it forms two series of salts: carbonates, which contain the trigonal planar $\mathrm{CO}_{3}{ }^{2-}$ ion, and hydrogen carbonates (bicarbonates), which contain the $\mathrm{HCO}_{3}{ }^{-}$ ion. Several million tons of soda ash, $\mathrm{Na}_{2} \mathrm{CO}_{3}$, are used annually to make glass, and $\mathrm{Na}_{2} \mathrm{CO}_{3} \cdot 10 \mathrm{H}_{2} \mathrm{O}$, known as washing soda, is used to launder textiles. The carbonate ion removes cations such as $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$ from hard water, and it acts as a base to give $\mathrm{OH}^{-}$ions, which help remove grease from fabrics:

$$
\begin{aligned}
& \mathrm{Ca}^{2+}(a q)+\mathrm{CO}_{3}^{2-}(a q) \longrightarrow \mathrm{CaCO}_{3}(s) \\
& \mathrm{CO}_{3}^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HCO}_{3}^{-}(a q)+\mathrm{OH}^{-}(a q)
\end{aligned}
$$

Sodium hydrogen carbonate, $\mathrm{NaHCO}_{3}$, is called baking soda because it reacts with acidic substances in food to yield bubbles of $\mathrm{CO}_{2}$ gas that cause dough to rise:

$$
\mathrm{NaHCO}_{3}(s)+\mathrm{H}^{+}(a q) \longrightarrow \mathrm{Na}^{+}(a q)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Hydrogen Cyanide and Cyanides Hydrogen cyanide is a highly toxic, volatile substance (bp $26^{\circ} \mathrm{C}$ ) produced when metal cyanide solutions are acidified:

$$
\mathrm{CN}^{-}(a q)+\mathrm{H}^{+}(a q) \longrightarrow \mathrm{HCN}(a q)
$$

Aqueous solutions of HCN , known as hydrocyanic acid, are very weakly acidic $\left(K_{\mathrm{a}}=4.9 \times 10^{-10}\right)$.

The cyanide ion is called a pseudohalide ion because it behaves like $\mathrm{Cl}^{-}$in forming an insoluble, white silver salt, AgCN. In complex ions such as $\mathrm{Fe}(\mathrm{CN})_{6}{ }^{3-}, \mathrm{CN}^{-}$acts as a Lewis base (Section 15.16), bonding to transition metals through the lone pair of electrons on carbon. In fact, the toxicity of HCN and other cyanides is due to the strong bonding of $\mathrm{CN}^{-}$to iron(III) in cytochrome oxidase, an important enzyme involved in the oxidation of food molecules. With $\mathrm{CN}^{-}$ attached to the iron, the enzyme is unable to function. Cellular energy production thus comes to a halt, and rapid death follows.

The bonding of $\mathrm{CN}^{-}$to gold and silver is exploited in the extraction of these metals from their ores. The crushed rock containing small amounts of the precious metals is treated with an aerated cyanide solution, and the metals are then recovered from their $\mathrm{M}(\mathrm{CN})_{2}{ }^{-}$complex ions by reduction with zinc. For gold, the reactions are

$$
\begin{aligned}
4 \mathrm{Au}(s)+8 \mathrm{CN}^{-}(a q)+\mathrm{O}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l) & \longrightarrow 4 \mathrm{Au}(\mathrm{CN})_{2}^{-}(a q)+4 \mathrm{OH}^{-}(a q) \\
2 \mathrm{Au}(\mathrm{CN})_{2}^{-}(a q)+\mathrm{Zn}(s) & \longrightarrow 2 \mathrm{Au}(s)+\mathrm{Zn}(\mathrm{CN})_{4}{ }^{2-}(a q)
\end{aligned}
$$

Carbides Carbon forms a number of binary compounds called carbides, in which the carbon atom has a negative oxidation state. Examples include ionic carbides of active metals such as $\mathrm{CaC}_{2}$ and $\mathrm{Al}_{4} \mathrm{C}_{3}$, interstitial carbides of transition metals such as $\mathrm{Fe}_{3} \mathrm{C}$, and covalent network carbides such as SiC . Calcium carbide is a high-melting, colorless solid that has an NaCl type of structure with $\mathrm{Ca}^{2+}$ ions in place of $\mathrm{Na}^{+}$and $\mathrm{C}_{2}{ }^{2-}$ ions in place of $\mathrm{Cl}^{-}$. It is prepared by heating lime ( CaO ) and coke $(\mathrm{C})$ at high temperatures and is used to prepare acetylene $\left(\mathrm{C}_{2} \mathrm{H}_{2}\right)$ for oxyacetylene welding:

$$
\begin{gathered}
\mathrm{CaO}(s)+3 \mathrm{C}(s) \xrightarrow{2200^{\circ} \mathrm{C}} \mathrm{CaC}_{2}(s)+\mathrm{CO}(g) \\
\mathrm{CaC}_{2}(s)+2 \mathrm{H}_{2} \mathrm{O}(l) \xrightarrow{ } \mathrm{C}_{2} \mathrm{H}_{2}(g)+\mathrm{Ca}(\mathrm{OH})_{2}(s)
\end{gathered}
$$

Iron carbide $\left(\mathrm{Fe}_{3} \mathrm{C}\right)$ is an important constituent of steel, and silicon carbide ( SiC ) is the industrial abrasive called carborundum. Almost as hard as diamond, SiC has a diamondlike structure with alternating Si and C atoms.

- PROBLEM 19.5 Hydrogen cyanide, HCN, is a linear triatomic molecule. Draw its electron-dot structure, and indicate which hybrid orbitals are used by the carbon atom.

PROBLEM 19.6 The equilibrium between oxyhemoglobin and carboxyhemoglobin suggests an approach to treating mild cases of carbon monoxide poisoning. Explain.

## 19.7 | Silicon

Silicon is a hard, gray, semiconducting solid that melts at $1410^{\circ} \mathrm{C}$. It crystallizes in a diamondlike structure but does not form a graphitelike allotrope because of the relatively poor overlap of silicon $\pi$ orbitals. In nature, silicon is generally found combined with oxygen in $\mathrm{SiO}_{2}$ and in various silicate minerals. It is obtained in

$\sqrt{ }$$\mathrm{CN}^{-}$and CO have the same number of electrons and the same Lewis electron-dot structure (: $\mathrm{C} \equiv \mathrm{N}^{:^{-}}$and $: \mathrm{C} \equiv \mathrm{O}$ : ).


A A cyanide leaching pool for extracting gold at the Picacho Gold Mine in the Mohave Desert.



FIGURE 19.4 (a) Purification of silicon by zone refining. The heater coil sweeps the molten zone and the impurities to the lower end of the rod. After the rod has cooled, the impurities are removed by cutting off the rod's lower end. (b) A rod of ultrapure silicon and silicon wafers cut from the rod. Silicon wafers are used to produce the integrated-circuit chips found in solid-state electronic devices.


- The mineral zircon $\left(\mathrm{ZrSiO}_{4}\right)$ is a relatively inexpensive gemstone.
elemental form by the reduction of silica sand $\left(\mathrm{SiO}_{2}\right)$ with coke $(\mathrm{C})$ in an electric furnace:

$$
\mathrm{SiO}_{2}(l)+2 \mathrm{C}(s) \xrightarrow{\text { Heat }} \mathrm{Si}(l)+2 \mathrm{CO}(g)
$$

The silicon used for making solid-state semiconductor devices such as transistors, computer chips, and solar cells must be ultrapure, with impurities at a level of less than $10^{-7} \%$ ( 1 ppb ). For electronic applications, silicon is purified by converting it to $\mathrm{SiCl}_{4}$, a volatile liquid ( $\mathrm{bp} 58^{\circ} \mathrm{C}$ ) that can be separated from impurities by fractional distillation and then converted back to elemental silicon by reduction with hydrogen:

$$
\begin{aligned}
& \mathrm{Si}(s)+2 \mathrm{Cl}_{2}(g) \longrightarrow \mathrm{SiCl}_{4}(l) \\
& \mathrm{SiCl}_{4}(g)+2 \mathrm{H}_{2}(g) \xrightarrow{\text { Heat }} \mathrm{Si}(s)+4 \mathrm{HCl}(g)
\end{aligned}
$$

The silicon is purified further by a process called zone refining (Figure 19.4a), in which a heater melts a narrow zone of a silicon rod. Because the impurities are more soluble in the liquid phase than in the solid, they concentrate in the molten zone. As the heater sweeps slowly down the rod, ultrapure silicon crystallizes at the trailing edge of the molten zone, and the impurities are dragged to the rod's lower end. Figure 19.4 b shows some samples of ultrapure silicon.


Silicates Approximately $90 \%$ of the earth's crust consists of silicates, ionic compounds that contain silicon oxoanions along with cations such as $\mathrm{Na}^{+}, \mathrm{K}^{+}, \mathrm{Mg}^{2+}$, or $\mathrm{Ca}^{2+}$ to balance the negative charge of the anions. As shown in Figure 19.5, the basic structural building block in silicates is the $\mathrm{SiO}_{4}$ tetrahedron, a unit that occurs as the simple orthosilicate ion $\left(\mathrm{SiO}_{4}{ }^{4-}\right)$ in the mineral zircon, $\mathrm{ZrSiO}_{4}$. If two $\mathrm{SiO}_{4}$ tetrahedra share a common O atom, the disilicate anion $\mathrm{Si}_{2} \mathrm{O}_{7}{ }^{6-}$, found in $\mathrm{Sc}_{2} \mathrm{Si}_{2} \mathrm{O}_{7}$, results.

Simple anions such as $\mathrm{SiO}_{4}{ }^{4-}$ and $\mathrm{Si}_{2} \mathrm{O}_{7}{ }^{6-}$ are relatively rare in silicate minerals. More common are larger anions in which two or more O atoms bridge between Si atoms to give rings, chains, layers, and extended three-dimensional structures. The sharing of two O atoms per $\mathrm{SiO}_{4}$ tetrahedron gives either cyclic anions, such as $\mathrm{Si}_{6} \mathrm{O}_{18}{ }^{12-}$, or infinitely extended chain anions with repeating $\mathrm{Si}_{2} \mathrm{O}_{6}{ }^{4-}$ units (Figure 19.6). The $\mathrm{Si}_{6} \mathrm{O}_{18}{ }^{12-}$ cyclic anion is present in the mineral


4 FIGURE 19.5 (a) A view of the $\mathrm{SiO}_{4}{ }^{4-}$ anion showing the tetrahedral $\mathrm{SiO}_{4}$ structural unit. (b) A tetrahedron is used as a shorthand representation of the $\mathrm{SiO}_{4}{ }^{4-}$ anion. An O atom is located at each corner of the tetrahedron, and the Si atom is at the center. (c) A view of the $\mathrm{Si}_{2} \mathrm{O}_{7}{ }^{6-}$ anion. (d) A shorthand representation of the $\mathrm{Si}_{2} \mathrm{O}_{7}{ }^{6-}$ anion. The corner shared by the two tetrahedra represents a shared O atom.
beryl $\left(\mathrm{Be}_{3} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{18}\right)$ and in the gemstone emerald, a beryl in which about $2 \%$ of the $\mathrm{Al}^{3+}$ is replaced by green $\mathrm{Cr}^{3+}$ cations. Chain anions are found in minerals such as diopside, $\mathrm{CaMgSi}_{2} \mathrm{O}_{6}$.

As shown in Figure 19.7, additional sharing of O atoms gives the doublestranded chain anions $\left(\mathrm{Si}_{4} \mathrm{O}_{11}{ }^{6-}\right)_{n}$ found in asbestos minerals such as tremolite, $\mathrm{Ca}_{2} \mathrm{Mg}_{5}\left(\mathrm{Si}_{4} \mathrm{O}_{11}\right)_{2}(\mathrm{OH})_{2}$, and the infinitely extended two-dimensional layer anions $\left(\mathrm{Si}_{4} \mathrm{O}_{10}{ }^{4-}\right)_{n}$ found in clay minerals, micas, and talc, $\mathrm{Mg}_{3}(\mathrm{OH})_{2}\left(\mathrm{Si}_{4} \mathrm{O}_{10}\right)$. Asbestos is fibrous, as shown in the figure, because the ionic bonds between the

© FIGURE 19.6 Samples of the silicate minerals: (a) emerald, a green beryl $\left(\mathrm{Be}_{3} \mathrm{Al}_{2} \mathrm{Si}_{6} \mathrm{O}_{18}\right)$ with about $2 \% \mathrm{Cr}^{3+}$ ions substituting for $\mathrm{Al}^{3+}$, and (b) diopside $\left(\mathrm{CaMgSi}_{2} \mathrm{O}_{6}\right)$. A shorthand representation of the structure of (c) the cyclic anion $\mathrm{Si}_{6} \mathrm{O}_{18}{ }^{12-}$ in beryl and (d) the infinitely extended chain anion $\left(\mathrm{Si}_{2} \mathrm{O}_{6}{ }^{4-}\right)_{n}$ in diopside. Note that the number of negative charges on the $\mathrm{Si}_{2} \mathrm{O}_{6}{ }^{4-}$ repeating unit equals the number of terminal (unshared) O atoms in that unit (four).


A FIGURE 19.7 (a) Asbestos is a fibrous material because of its chain structure. (b) Mica cleaves into thin sheets because of its two-dimensional layer structure. (c) A shorthand representation of the double-stranded chain anion $\left(\mathrm{Si}_{4} \mathrm{O}_{11}{ }^{6-}\right)_{n}$ in asbestos minerals. Two of the single-stranded chains of Figure 19.6d are laid side by side, and half of the $\mathrm{SiO}_{4}$ tetrahedra share an additional O atom. (d) The layer anion $\left(\mathrm{Si}_{4} \mathrm{O}_{10}{ }^{4-}\right)_{n}$ in mica is formed by the sharing of three O atoms per $\mathrm{SiO}_{4}$ tetrahedron. Note again that the number of negative charges on each repeating unit equals the number of terminal O atoms in that unit.
silicate chain anions and the $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$ cations that lie between the chains and hold them together are relatively weak and easily broken. Similarly, mica is sheetlike because the ionic bonds between the two-dimensional layer anions and the interposed metal cations are much weaker than the $\mathrm{Si}-\mathrm{O}$ covalent bonds within the layer anions.

If the layer anions of Figure 19.7d are stacked on top of one another and the terminal O atoms are shared, an infinitely extended three-dimensional structure is obtained in which all four O atoms of each $\mathrm{SiO}_{4}$ tetrahedron are shared between two Si atoms, resulting in silica $\left(\mathrm{SiO}_{2}\right)$. The mineral quartz is one of many crystalline forms of $\mathrm{SiO}_{2}$.

Partial substitution of the $\mathrm{Si}^{4+}$ of $\mathrm{SiO}_{2}$ with $\mathrm{Al}^{3+}$ gives aluminosilicates called feldspars, the most abundant of all minerals. An example is orthoclase, $\mathrm{KAlSi}_{3} \mathrm{O}_{8}$, which has a three-dimensional structure like that of $\mathrm{SiO}_{2}$. The $\left(\mathrm{AlSi}_{3} \mathrm{O}_{8}{ }^{-}\right)_{n}$ framework consists of $\mathrm{SiO}_{4}$ and $\mathrm{AlO}_{4}$ tetrahedra that share all four of their corners with neighboring tetrahedra. The $\mathrm{K}^{+}$cation balances the negative charge. In the aluminosilicates known as zeolites, the $\mathrm{SiO}_{4}$ and $\mathrm{AlO}_{4}$ tetrahedra are joined together in an open structure that has a three-dimensional network of cavities linked by channels. Because only small molecules can enter these channels, zeolites act as molecular sieves for separating small molecules from larger ones. They are also used as catalysts in the manufacture of gasoline.


## Worked Key Concept Example 19.3

The following pictures represent silicate anions. What is the formula and charge of each anion?


## Strategy

Each tetrahedron represents an $\mathrm{SiO}_{4}$ structural unit, with an Si atom at the center of the tetrahedron and an O atom at each corner. Each terminal (unshared) O atom needs one electron to complete its octet and therefore has a charge of -1 . Each bridging (shared) O atom completes its octet by forming bonds to two Si atoms and is therefore electrically neutral. To find the number of Si atoms in the formula, count the number of tetrahedra. To find the number of $O$ atoms, count the number of corners (shared and unshared). To find the charge on the anion, count the number of unshared corners.

## Solution

(a) The picture contains three tetrahedra, with three shared corners and six unshared corners (nine in all). Therefore, the anion is $\mathrm{Si}_{3} \mathrm{O}_{9}{ }^{6-}$.
(b) The picture contains four tetrahedra, with three shared corners and 10 unshared corners ( 13 in all). Therefore, the anion is $\mathrm{Si}_{4} \mathrm{O}_{13}{ }^{10-}$.

4 (a) Pure crystalline quartz, one form of $\mathrm{SiO}_{2}$, is colorless. (b) Orthoclase, $\mathrm{KAlSi}_{3} \mathrm{O}_{8}$, has a structure similar to that of $\mathrm{SiO}_{2}$.

CHECK We can check the charge on a silicate anion by assigning the usual oxidation states of +4 to silicon and -2 to oxygen. Thus, the charge on anion (a) must be $(3)(4)+(9)(-2)=-6$, and the charge on anion (b) must be $(4)(4)+(13)$ $(-2)=-10$.

- KEY CONCEPT PROBLEM 19.7 The following pictures represent silicate anions. What are the formula and charge of the anion in (a) and the repeating unit of the chain anion in (b)?

(a)

(b)


## 19.8 | Germanium, Tin, and Lead

Germanium, tin, and lead have relatively low abundances in the earth's crust (Table 19.4, page 823), but tin and lead are concentrated in workable deposits and are readily extracted from their ores. Tin is obtained from the mineral cassiterite $\left(\mathrm{SnO}_{2}\right)$ by reducing the purified oxide with carbon:

$$
\mathrm{SnO}_{2}(s)+2 \mathrm{C}(s) \xrightarrow{\text { Heat }} \mathrm{Sn}(l)+2 \mathrm{CO}(g)
$$

Tin is used as a protective coating over steel to make tin cans, and is an important component of alloys such as bronze $(10 \% \mathrm{Sn}, 90 \% \mathrm{Cu})$, pewter $(90 \% \mathrm{Sn}$, with Cu and Sb ), and lead solder ( $33 \% \mathrm{Sn}, 67 \% \mathrm{~Pb}$ ).

Lead is obtained from its ore, galena ( PbS ), by roasting the sulfide in air and reducing the resulting PbO with carbon monoxide in a blast furnace:

$$
\begin{aligned}
2 \mathrm{PbS}(s)+3 \mathrm{O}_{2}(g) & \longrightarrow \mathrm{PbO}(s)+2 \mathrm{SO}_{2}(g) \\
\mathrm{PbO}(s)+\mathrm{CO}(g) & \mathrm{Pb}(l)+\mathrm{CO}_{2}(g)
\end{aligned}
$$

Lead is used to make pipes, cables, pigments, and, most important, electrodes for storage batteries (Section 18.9).

Although tin and lead have been known for over 5000 years, germanium was not discovered until 1886, by C. A. Winkler in Germany. In fact, germanium was one of the "holes" in Mendeleev's periodic table (Figure 5.2, page 160). Germanium is used to make transistors and special glasses for infrared devices.

The physical properties of the heavier group 4A elements nicely illustrate the gradual transition from semimetal to metallic character. Germanium is a relatively high-melting, brittle semiconductor that has the same crystal structure as diamond and silicon. Tin exists in two allotropic forms: the usual silvery white metallic form called white tin and a brittle, semiconducting form with the diamond structure called gray tin. White tin is the stable form at room temperature, but when kept for long periods of time below the transition temperature of $13^{\circ} \mathrm{C}$, it slowly crumbles to gray tin, a phenomenon known as "tin disease":

$$
\text { White tin } \stackrel{13^{\circ} \mathrm{C}}{\rightleftharpoons} \text { Gray tin }
$$

Only the metallic form occurs for lead. Both white tin and lead are soft, malleable, low-melting metals.


## 19.9 | The Group 5A Elements

The group 5A elements are nitrogen, phosphorus, arsenic, antimony, and bismuth. As shown in Table 19.5, these elements exhibit the expected trends of increasing atomic size, decreasing ionization energy, and decreasing electronegativity down the periodic group from N to Bi . Accordingly, metallic character increases in the same order: N and P are typical nonmetals, As and Sb are semimetals, and Bi is a metal. Thus, nitrogen is a gaseous substance made up of $\mathrm{N}_{2}$ molecules, but bismuth is a silvery solid having an extended three-dimensional structure. The increasing metallic character of the heavier elements is also evident in the acid-base properties of their oxides: Most nitrogen and phosphorus oxides are acidic, arsenic and antimony oxides are amphoteric, and $\mathrm{Bi}_{2} \mathrm{O}_{3}$ is basic.

- Samples of (a) germanium, (b) tin, and (c) lead.


TABLE 19.5 Properties of the Group 5A Elements

| Property | Nitrogen | Phosphorus | Arsenic | Antimony | Bismuth |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Valence electron configuration | $2 s^{2} 2 p^{3}$ | $3 s^{2} 3 p^{3}$ | $4 s^{2} 4 p^{3}$ | $5 s^{2} 5 p^{3}$ | $6 s^{2} 6 p^{3}$ |
| Melting point $\left({ }^{\circ} \mathrm{C}\right)$ | -210 | $44^{*}$ | $614^{\dagger}$ | 631 | 271 |
| Boiling point $\left({ }^{\circ} \mathrm{C}\right)$ | -196 | 280 |  | 1587 | 1564 |
| Atomic radius (pm) | 75 | 110 | 120 | 140 | 150 |
| First ionization energy (kJ/mol) | 1402 | 1012 | 947 | 834 | 703 |
| Electronegativity | 3.0 | 2.1 | 2.0 | 1.9 | 1.9 |

*White phosphorus
${ }^{\dagger}$ 'Sublimes



v
Due to the high strength of the nitrogen-nitrogen bond, $\mathrm{N}_{2}$, the most common molecule in the earth's atmosphere is practically unreactive under ordinary conditions. An exception is its use by plants in nitrogen fixation, a process yet to be duplicated in the laboratory.

The valence electron configuration of the group 5A elements is $n s^{2} n p^{3}$. They exhibit a maximum oxidation state of +5 in compounds such as $\mathrm{HNO}_{3}$ and $\mathrm{PF}_{5}$, in which they share all five valence electrons with a more electronegative element. They show a minimum oxidation state of -3 in compounds such as $\mathrm{NH}_{3}$ and $\mathrm{PH}_{3}$, where they share three valence electrons with a less electronegative element. The -3 state also occurs in ionic compounds such as $\mathrm{Li}_{3} \mathrm{~N}$ and $\mathrm{Mg}_{3} \mathrm{~N}_{2}$, which contain the $\mathrm{N}^{3-}$ anion.

Nitrogen and phosphorus are unusual in that they exhibit all oxidation states between -3 and +5 . For arsenic and antimony, the most important oxidation states are +3 , as in $\mathrm{AsCl}_{3}, \mathrm{As}_{2} \mathrm{O}_{3}$, and $\mathrm{H}_{3} \mathrm{AsO}_{3}$, and +5 , as in $\mathrm{AsF}_{5}, \mathrm{As}_{2} \mathrm{O}_{5}$, and $\mathrm{H}_{3} \mathrm{AsO}_{4}$. The +5 state becomes increasingly less stable from As to Sb to Bi . Another indication of increasing metallic character down the group is the existence of $\mathrm{Sb}^{3+}$ and $\mathrm{Bi}^{3+}$ cations in salts such as $\mathrm{Sb}_{2}\left(\mathrm{SO}_{4}\right)_{3}$ and $\mathrm{Bi}\left(\mathrm{NO}_{3}\right)_{3}$. By contrast, no simple cations are found in compounds of N or P .

The natural abundances of $\mathrm{As}, \mathrm{Sb}$, and Bi in the earth's crust are relatively low—about $0.0002 \%$ for As and about $0.00002 \%$ for Sb and Bi. All three elements are found in sulfide ores and are used to make various metal alloys. Arsenic is also used to make pesticides and semiconductors, such as GaAs. Bismuth compounds are present in some pharmaceuticals, such as Pepto-Bismol.

## $19.10 \mid$ Nitrogen

Elemental nitrogen is a colorless, odorless, tasteless gas that makes up 78\% of the earth's atmosphere by volume. Because nitrogen ( $\mathrm{bp}-196^{\circ} \mathrm{C}$ ) is the most volatile component of liquid air, it is readily separated from the less volatile oxygen (bp $-183^{\circ} \mathrm{C}$ ) and argon (bp $-186^{\circ} \mathrm{C}$ ) by fractional distillation. As shown in Table 19.1 on page 816 , the annual U.S. production of nitrogen is 35.5 million tons, greater than that of any other industrial chemical except sulfuric acid. Nitrogen gas is used as a protective inert atmosphere in manufacturing processes, and the liquid is used as a refrigerant. By far the most important use of nitrogen, however, is in the Haber process for the manufacture of ammonia, used in nitrogen fertilizers.

Under most conditions, the $\mathrm{N}_{2}$ molecule is unreactive because a large amount of energy is required to break its strong nitrogen-nitrogen triple bond:

$$
: \mathrm{N} \equiv \mathrm{~N}: \longrightarrow 2: \dot{\mathrm{N}} \cdot \quad \Delta H^{\circ}=945 \mathrm{~kJ}
$$

As a result, reactions involving $\mathrm{N}_{2}$ often have a high activation energy and/or an unfavorable equilibrium constant. For example, $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$ do not combine to form nitric oxide at $25^{\circ} \mathrm{C}$ because the equilibrium constant for the reaction is $4.5 \times 10^{-31}$ :

$$
\mathrm{N}_{2}(g)+\mathrm{O}_{2}(g) \rightleftharpoons 2 \mathrm{NO}(g) \quad \Delta H^{\circ}=180.5 \mathrm{~kJ} ; K_{\mathrm{c}}=4.5 \times 10^{-31} \text { at } 25^{\circ} \mathrm{C}
$$

At higher temperatures, however, the reaction does occur because it is endothermic and the equilibrium shifts to the right with increasing temperature (Section 13.9). Indeed, the high-temperature formation of NO from air in automobile engines is a major source of air pollution. Atmospheric $\mathrm{N}_{2}$ and $\mathrm{O}_{2}$ also react to form NO during electrical storms, where lightning discharges provide the energy required for the highly endothermic reaction.

Nitrogen reacts with $\mathrm{H}_{2}$ in the Haber process for the synthesis of $\mathrm{NH}_{3}$, but the reaction requires high temperatures, high pressures, and a catalyst (Sections 13.8-13.10):

$$
\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \xrightarrow[\mathrm{Fe} / \mathrm{K}_{2} \mathrm{O} / \mathrm{Al}_{2} \mathrm{O}_{3} \text { catalyst }]{400-50{ }^{\circ} \mathrm{atm}, 130-300 \mathrm{~atm}} 2 \mathrm{NH}_{3}(g)
$$

It's convenient to classify nitrogen compounds by oxidation state, as shown in Table 19.6.

TABLE 19.6 Oxidation States of Nitrogen and Representative Compounds

| Oxidation <br> State | Compound | Formula | Electron-Dot Structure |
| :---: | :---: | :---: | :---: |
| -3 | Ammonia | $\mathrm{NH}_{3}$ |  |
| -2 | Hydrazine | $\mathrm{N}_{2} \mathrm{H}_{4}$ |  |
| -1 | Hydroxylamine | $\mathrm{NH}_{2} \mathrm{OH}$ |  |
| +1 | Nitrous oxide | $\mathrm{N}_{2} \mathrm{O}$ | $: N \equiv N-\ddot{\mathrm{O}}:$ |
| +2 | Nitric oxide | NO | $: \dot{\mathrm{N}}=\ddot{\mathrm{O}}:$ |
| +3 | Nitrous acid | $\mathrm{HNO}_{2}$ | $\mathrm{H}-\ddot{\mathrm{O}}-\ddot{\mathrm{N}}=\ddot{\mathrm{O}}:$ |
| +4 | Nitrogen dioxide | $\mathrm{NO}_{2}$ | $: \ddot{\mathrm{O}}-\dot{\mathrm{N}}=\ddot{\mathrm{O}}$ : |
| +5 | Nitric acid | $\mathrm{HNO}_{3}$ |  |

Bassam Z. Shakhashiri, "Preparation and Properties of Ammonia," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 2 (The University of Wisconsin Press, Madison, 1985), pp. 202-204. Ammonia gas is produced from the reaction of ammonium chloride with calcium hydroxide and is collected in an Erlenmeyer flask by the displacement of air. The ammonia gas turns moistened litmus paper blue, demonstrating the basic properties of ammonia dissolved in water. When the mouth of an ammonia-filled Erlenmeyer flask is placed below the surface of a pool of water, water rapidly enters the flask to replace ammonia that dissolves in the water. White smoke forms when ammonia vapor is passed over the top of a beaker of concentrated hydrochloric acid forming solid ammonium chloride.

## Nitrogen Compounds

Ammonia Ammonia and its synthesis by the Haber process serve as the gateway to nitrogen chemistry because ammonia is the starting material for the industrial synthesis of other important nitrogen compounds, such as nitric acid. Used in agriculture as a fertilizer, ammonia is the most commercially important compound of nitrogen.

Ammonia is a colorless, pungent-smelling gas, consisting of polar, trigonal pyramidal $\mathrm{NH}_{3}$ molecules that have a lone pair of electrons on the N atom. Because of hydrogen bonding (Section 10.2), gaseous $\mathrm{NH}_{3}$ is extremely soluble in water and is easily condensed to liquid $\mathrm{NH}_{3}$, which boils at $-33^{\circ} \mathrm{C}$. Like water, liquid ammonia is an excellent solvent for ionic compounds. It also dissolves alkali metals, as mentioned in Section 6.7.

Because ammonia is a Brønsted-Lowry base (Section 15.1), its aqueous solutions are weakly alkaline:

$$
\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}^{+}(a q)+\mathrm{OH}^{-}(a q) \quad K_{\mathrm{b}}=1.8 \times 10^{-5}
$$

Neutralization of aqueous ammonia with acids yields ammonium salts, which resemble alkali metal salts in their solubility.

Hydrazine Hydrazine $\left(\mathrm{H}_{2} \mathrm{NNH}_{2}\right)$ can be regarded as a derivative of $\mathrm{NH}_{3}$ in which one H atom is replaced by an amino $\left(\mathrm{NH}_{2}\right)$ group. It can be prepared by the reaction of ammonia with a basic solution of sodium hypochlorite $(\mathrm{NaOCl})$ :

$$
2 \mathrm{NH}_{3}(a q)+\mathrm{OCl}^{-}(a q) \longrightarrow \mathrm{N}_{2} \mathrm{H}_{4}(a q)+\mathrm{H}_{2} \mathrm{O}(l)+\mathrm{Cl}^{-}(a q)
$$

You have perhaps heard that household cleaners should never be mixed because exothermic reactions may occur or dangerous products may form. The formation of hydrazine on mixing household ammonia and hypochlorite-containing chlorine bleaches is a case in point.

Pure hydrazine is a poisonous, colorless liquid that smells like ammonia, freezes at $2^{\circ} \mathrm{C}$, and boils at $114^{\circ} \mathrm{C}$. It is violently explosive in the presence of air or


Ammonia


Hydrazine


Any highly exothermic reaction that generates gaseous products has the potential to occur with explosive force.


Nitrous oxide
3D models of $\mathrm{N}_{2} \mathrm{O}$ and NO


Nitric oxide
When an element occurs in two extremely different oxidation states in a compound, as does nitrogen in $\mathrm{NH}_{4} \mathrm{NO}_{3}$, the compound may decompose violently.


Nitrogen dioxide $\mathrm{NO}_{2}$ 3D model

FIGURE 19.8 (a) Nitric oxide is a colorless gas. (b) It turns brown on contact with air because NO is rapidly oxidized to $\mathrm{NO}_{2}$. (c) Copper reacts with concentrated $\mathrm{HNO}_{3}$, yielding noxious, red-brown fumes of $\mathrm{NO}_{2}$. The blue color of the solution is due to $\mathrm{Cu}^{2+}$ ions.
other oxidizing agents and is used as a rocket fuel. For example, the Apollo lunarlanding module used a fuel composed of hydrazine and a derivative of hydrazine, along with dinitrogen tetroxide $\left(\mathrm{N}_{2} \mathrm{O}_{4}\right)$ as the oxidizer. The highly exothermic reaction is

$$
2 \mathrm{~N}_{2} \mathrm{H}_{4}(l)+\mathrm{N}_{2} \mathrm{O}_{4}(l) \longrightarrow 3 \mathrm{~N}_{2}(g)+4 \mathrm{H}_{2} \mathrm{O}(g) \quad \Delta H^{\circ}=-1049 \mathrm{~kJ}
$$

Hydrazine can be handled safely in aqueous solutions, where it behaves as a weak base $\left(K_{\mathrm{b}}=8.9 \times 10^{-7}\right)$ and a versatile reducing agent. It reduces $\mathrm{Fe}^{3+}$ to $\mathrm{Fe}^{2+}, \mathrm{I}_{2}$ to $\mathrm{I}^{-}$, and $\mathrm{Ag}^{+}$to metallic Ag , for example.
Oxides of Nitrogen Nitrogen forms a large number of oxides, but here we'll discuss only three: nitrous oxide (dinitrogen monoxide, $\mathrm{N}_{2} \mathrm{O}$ ), nitric oxide (nitrogen monoxide, NO ), and nitrogen dioxide $\left(\mathrm{NO}_{2}\right)$. We discussed $\mathrm{N}_{2} \mathrm{O}_{5}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ in Chapters 12 and 13.

Nitrous oxide $\left(\mathrm{N}_{2} \mathrm{O}\right)$ is a colorless, sweet-smelling gas obtained when molten ammonium nitrate is heated gently at about $270^{\circ} \mathrm{C}$ :

$$
\mathrm{NH}_{4} \mathrm{NO}_{3}(l) \longrightarrow \mathrm{N}_{2} \mathrm{O}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)
$$

(Strong heating can cause an explosion.) Known as "laughing gas" because small doses are mildly intoxicating, nitrous oxide is used as a dental anesthetic and as a propellant for dispensing whipped cream.

Nitric oxide ( NO ) is a colorless gas, produced in the laboratory when copper metal is treated with dilute nitric acid:

$$
3 \mathrm{Cu}(s)+2 \mathrm{NO}_{3}^{-}(a q)+8 \mathrm{H}^{+}(a q) \longrightarrow 3 \mathrm{Cu}^{2+}(a q)+2 \mathrm{NO}(g)+4 \mathrm{H}_{2} \mathrm{O}(l)
$$

As we'll discuss later, NO is prepared in large quantities by catalytic oxidation of ammonia, the first step in the industrial synthesis of nitric acid. Recently, it has been found that nitric oxide is important in biological processes: It helps transmit messages between nerve cells and kills harmful microorganisms. It also helps to protect the heart from insufficient oxygen levels by dilating blood vessels. Very recently, it has been learned that the drug nitroglycerin, long used to relieve of the pain of angina, is a source of nitric oxide, which in turn dilates clogged arteries.

Nitrogen dioxide $\left(\mathrm{NO}_{2}\right)$ is the highly toxic, reddish brown gas that forms rapidly when nitric oxide is exposed to air (Figure 19.8):

$$
2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{NO}_{2}(g)
$$

$\mathrm{NO}_{2}$ is also produced when copper reacts with concentrated nitric acid:

$$
\mathrm{Cu}(s)+2 \mathrm{NO}_{3}^{-}(a q)+4 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Cu}^{2+}(a q)+2 \mathrm{NO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$


(a)

(b)

(c)

Because $\mathrm{NO}_{2}$ has an odd number of electrons (23), it is paramagnetic. It tends to dimerize, forming colorless, diamagnetic $\mathrm{N}_{2} \mathrm{O}_{4}$, in which the unpaired electrons of two $\mathrm{NO}_{2}$ molecules pair up to give an $\mathrm{N}-\mathrm{N}$ bond:

$$
\underset{\text { Brown }}{\mathrm{O}_{2} \mathrm{~N} \cdot+\cdot \mathrm{NO}_{2}} \rightleftharpoons \underset{\text { Colorless }}{\mathrm{O}_{2} \mathrm{~N}-\mathrm{NO}_{2}} \quad \Delta H^{\circ}=-57.2 \mathrm{~kJ}
$$

In the gas phase, $\mathrm{NO}_{2}$ and $\mathrm{N}_{2} \mathrm{O}_{4}$ are present in equilibrium. Because dimer formation is exothermic, $\mathrm{N}_{2} \mathrm{O}_{4}$ predominates at lower temperatures, and $\mathrm{NO}_{2}$ predominates at higher temperatures. Thus, the color of the mixture fades on cooling and darkens on warming, as was illustrated in Figure 13.13 (page 555). By contrast, gaseous NO, which also has an odd number of electrons, has little tendency to dimerize.

Nitrous Acid Nitrogen dioxide reacts with water to yield a mixture of nitrous acid $\left(\mathrm{HNO}_{2}\right)$ and nitric acid $\left(\mathrm{HNO}_{3}\right)$ :

$$
2 \mathrm{NO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{HNO}_{2}(a q)+\mathrm{H}^{+}(a q)+\mathrm{NO}_{3}^{-}(a q)
$$

This is a disproportionation reaction in which nitrogen goes from the +4 oxidation state in $\mathrm{NO}_{2}$ to the +3 state in $\mathrm{HNO}_{2}$ and the +5 state in $\mathrm{HNO}_{3}$. Nitrous acid is a weak acid $\left(K_{\mathrm{a}}=4.5 \times 10^{-4}\right)$ that tends to disproportionate to nitric oxide and nitric acid. It has not been isolated as a pure compound:

$$
3 \mathrm{HNO}_{2}(a q) \rightleftharpoons 2 \mathrm{NO}(g)+\mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NO}_{3}^{-}(a q)
$$

Nitric Acid Nitric acid, one of the most important inorganic acids, is used mainly to make ammonium nitrate for fertilizers, but it is also used to manufacture explosives, plastics, and dyes. Annual U.S. production of $\mathrm{HNO}_{3}$ is approximately 8 million tons.

Nitric acid is produced industrially by the multistep Ostwald process, which involves (1) air oxidation of ammonia to nitric oxide at about $850^{\circ} \mathrm{C}$ over a platinum-rhodium catalyst, (2) rapid oxidation of the nitric oxide to nitrogen dioxide, and (3) disproportionation of $\mathrm{NO}_{2}$ in water:

$$
\begin{aligned}
& \text { (1) } 4 \mathrm{NH}_{3}(g)+5 \mathrm{O}_{2}(g) \frac{850^{\circ} \mathrm{C}}{\text { Pt } / \text { Rh catalyst }} 4 \mathrm{NO}(g)+6 \mathrm{H}_{2} \mathrm{O}(g) \\
& (2) \\
& 2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{NO}_{2}(g) \\
& (3) \\
& 3 \mathrm{NO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{HNO}_{3}(a q)+\mathrm{NO}(g)
\end{aligned}
$$

Distillation of the resulting aqueous $\mathrm{HNO}_{3}$ removes some of the water and gives concentrated ( 15 M ) nitric acid, an $\mathrm{HNO}_{3}-\mathrm{H}_{2} \mathrm{O}$ mixture that is $68.5 \% \mathrm{HNO}_{3}$ by mass.

Further removal of water is required to obtain pure nitric acid, a colorless liquid that boils at $83^{\circ} \mathrm{C}$. In the laboratory, concentrated nitric acid often has a yellow-brown color. The color is due to $\mathrm{NO}_{2}$, produced by a slight amount of decomposition:

$$
4 \mathrm{HNO}_{3}(a q) \longrightarrow 4 \mathrm{NO}_{2}(a q)+\mathrm{O}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

Nitric acid is a strong acid, essentially $100 \%$ dissociated in water. It's also a strong oxidizing agent, as indicated by large, positive $E^{\circ}$ values for reduction to lower oxidation states:

$$
\begin{array}{ll}
\mathrm{NO}_{3}^{-}(a q)+2 \mathrm{H}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{NO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l) & E^{\circ}=0.79 \mathrm{~V} \\
\mathrm{NO}_{3}^{-}(a q)+4 \mathrm{H}^{+}(a q)+3 \mathrm{e}^{-} \longrightarrow \mathrm{NO}(g)+2 \mathrm{H}_{2} \mathrm{O}(l) & E^{\circ}=0.96 \mathrm{~V}
\end{array}
$$

Thus, nitric acid is a stronger oxidizing agent than $\mathrm{H}^{+}(a q)$ and can oxidize relatively inactive metals like copper and silver that are not oxidized by aqueous HCl . The reduction product of $\mathrm{HNO}_{3}$ in a particular reaction depends on the nature of the reducing agent and the reaction conditions. We've already seen, for example,

0
The equilibrium for an exothermic reaction shifts to the left as the temperature is raised.


Nitrous acid


Nitric acid


- Why does freshly prepared concentrated nitric acid (left) turn yellow-brown on standing (right)?
that copper reduces dilute $\mathrm{HNO}_{3}$ to NO , but it reduces concentrated $\mathrm{HNO}_{3}$ to $\mathrm{NO}_{2}$.

An even more potent oxidizing agent than $\mathrm{HNO}_{3}$ is aqua regia, a mixture of concentrated HCl and concentrated $\mathrm{HNO}_{3}$ in a $3: 1$ ratio by volume. Aqua regia can oxidize even inactive metals like gold, which do not react with either HCl or $\mathrm{HNO}_{3}$ separately:

$$
\mathrm{Au}(s)+3 \mathrm{NO}_{3}^{-}(a q)+6 \mathrm{H}^{+}(a q)+4 \mathrm{Cl}^{-}(a q) \longrightarrow \mathrm{AuCl}_{4}^{-}(a q)+3 \mathrm{NO}_{2}(g)+3 \mathrm{H}_{2} \mathrm{O}(l)
$$

In this reaction, $\mathrm{NO}_{3}{ }^{-}$serves as the oxidizing agent, and $\mathrm{Cl}^{-}$provides an additional driving force by converting the $\mathrm{Au}(\mathrm{III})$ oxidation product to the $\mathrm{AuCl}_{4}{ }^{-}$ complex ion.

- PROBLEM 19.8 For those molecules in Table 19.6 that must be described as resonance hybrids, draw electron-dot resonance structures, assign formal charges, and indicate which resonance structure(s) is (are) most important. In addition, indicate which of the molecules in Table 19.6 are paramagnetic.



3D models of white phosphorus and red phosphorus

$\square$Note that both allotropes of period 3 phosphorus have only single bonds, whereas period 2 nitrogen has a triple bond in $\mathrm{N}_{2}$.

### 19.11 Phosphorus

Phosphorus is the most abundant element of group 5A, accounting for $0.10 \%$ of the mass of the earth's crust. It is found in phosphate rock, which is mostly calcium phosphate, $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$, and in fluorapatite, $\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{~F}$. The apatites are phosphate minerals with the formula $3 \mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2} \cdot \mathrm{CaX}_{2}$, where $\mathrm{X}^{-}$is usually $\mathrm{F}^{-}$ or $\mathrm{OH}^{-}$. Phosphorus is also important in living systems and is the sixth most abundant element in the human body (Figure 19.1). Our bones are mostly $\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}$, and tooth enamel is almost pure $\mathrm{Ca}_{5}\left(\mathrm{PO}_{4}\right)_{3} \mathrm{OH}$. Phosphate groups are an integral part of the nucleic acids DNA and RNA, the molecules that pass genetic information from generation to generation (see Section 24.12).

Elemental phosphorus is produced industrially by heating phosphate rock, coke, and silica sand at about $1500^{\circ} \mathrm{C}$ in an electric furnace. The reaction can be represented by the simplified equation

$$
2 \mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}(s)+10 \mathrm{C}(s)+6 \mathrm{SiO}_{2}(s) \longrightarrow \mathrm{P}_{4}(g)+10 \mathrm{CO}(g)+6 \mathrm{CaSiO}_{3}(l)
$$

To condense the phosphorus, the gaseous reaction products are passed through water. Phosphorus is used to make phosphoric acid, one of the top 10 industrial chemicals (Table 19.1).

Phosphorus exists in two common allotropic forms: white phosphorus and red phosphorus (Figure 19.9). White phosphorus, the form produced in the industrial synthesis, is a toxic, waxy, white solid that contains discrete tetrahedral $\mathrm{P}_{4}$ molecules. Red phosphorus, by contrast, is essentially nontoxic and has a polymeric structure.

Finely divided white phosphorus, deposited on a piece of filter paper by evaporation of a carbon disulfide solution of $\mathrm{P}_{4}$, bursts into flame in air.



Red phosphorus
As expected for a molecular solid that contains small, nonpolar molecules, white phosphorus has a low melting point $\left(44^{\circ} \mathrm{C}\right)$ and is soluble in nonpolar solvents such as carbon disulfide, $\mathrm{CS}_{2}$. It is highly reactive, bursting into flames when exposed to air, and is thus stored underwater. When white phosphorus is heated in the absence of air at about $300^{\circ} \mathrm{C}$, it is converted to the more stable red form. Consistent with its polymeric structure, red phosphorus is higher melting ( $\mathrm{mp} \sim 600^{\circ} \mathrm{C}$ ), less soluble, and less reactive than white phosphorus, and it does not ignite on contact with air (Figure 19.9).

The high reactivity of white phosphorus is due to an unusual bonding that produces considerable strain in the $\mathrm{P}_{4}$ molecules. If each P atom uses three $3 p$ orbitals to form three $\mathrm{P}-\mathrm{P}$ bonds, all the bond angles should be $90^{\circ}$. The geometry of $\mathrm{P}_{4}$, however, requires that all the bonds have $60^{\circ}$ angles, which means that the $p$ orbitals can't overlap in a head-on fashion. As a result, the P-P bonds are "bent," relatively weak, and highly reactive (Figure 19.10).

## Phosphorus Compounds

Like nitrogen, phosphorus forms compounds in all oxidation states between -3 and +5 , but the +3 state, as in $\mathrm{PCl}_{3}, \mathrm{P}_{4} \mathrm{O}_{6}$, and $\mathrm{H}_{3} \mathrm{PO}_{3}$, and the +5 state, as in
© FIGURE 19.9 Red phosphorus (left), and white phosphorus stored underwater (right).


4 FIGURE 19.10 One equilateral triangular face of a tetrahedral $\mathrm{P}_{4}$ molecule showing the $60^{\circ}$ bond angles and the $90^{\circ}$ angles between the $p$ orbitals. The relatively poor orbital overlap in the bent bonds accounts for the high reactivity of white phosphorus.


Phosphine


Phosphorus trichloride


Phosphorus pentachloride


is more likely to be found in a positive oxidation state because of its lower electronegativity (Table 19.5, page 833).
Phosphine Phosphine $\left(\mathrm{PH}_{3}\right)$, a colorless, extremely poisonous gas, is the most important hydride of phosphorus. Like $\mathrm{NH}_{3}$, phosphine has a trigonal pyramidal structure and has the group 5A atom in the -3 oxidation state. Unlike $\mathrm{NH}_{3}$, however, its aqueous solutions are neutral, indicating that $\mathrm{PH}_{3}$ is a poor proton acceptor. In accord with the low electronegativity of phosphorus, phosphine is easily oxidized, burning in air to form phosphoric acid:

$$
\mathrm{PH}_{3}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{H}_{3} \mathrm{PO}_{4}(l)
$$

Phosphorus Halides Phosphorus reacts with all the halogens, forming phosphorus(III) halides, $\mathrm{PX}_{3}$, or phosphorus(V) halides, $\mathrm{PX}_{5}(\mathrm{X}=\mathrm{F}, \mathrm{Cl}, \mathrm{Br}$, or I$)$, depending on the relative amounts of the reactants:

$$
\begin{aligned}
& \text { Limited amount of } \mathrm{X}_{2}: \mathrm{P}_{4}+6 \mathrm{X}_{2} \longrightarrow 4 \mathrm{PX}_{3} \\
& \text { Excess amount of } \mathrm{X}_{2}: \\
& \mathrm{P}_{4}+10 \mathrm{X}_{2} \longrightarrow 4 \mathrm{PX}_{5}
\end{aligned}
$$

All these halides are gases, volatile liquids, or low-melting solids. For example, phosphorus trichloride is a colorless liquid that boils at $76^{\circ} \mathrm{C}$, and phosphorus pentachloride is an off-white solid that melts at $167^{\circ} \mathrm{C}$. Both fume on contact with moist air because of a reaction with water that breaks the $\mathrm{P}-\mathrm{Cl}$ bonds, converting $\mathrm{PCl}_{3}$ to phosphorous acid $\left(\mathrm{H}_{3} \mathrm{PO}_{3}\right)$, and $\mathrm{PCl}_{5}$ to phosphoric acid $\left(\mathrm{H}_{3} \mathrm{PO}_{4}\right)$ :

$$
\begin{aligned}
& \mathrm{PCl}_{3}(l)+3 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{H}_{3} \mathrm{PO}_{3}(a q)+3 \mathrm{HCl}(a q) \\
& \mathrm{PCl}_{5}(s)+4 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \mathrm{H}_{3} \mathrm{PO}_{4}(a q)+5 \mathrm{HCl}(a q)
\end{aligned}
$$


$\triangle$ Samples of $\mathrm{PCl}_{3}$ (left) and $\mathrm{PCl}_{5}$ (right).

Oxides and Oxoacids of Phosphorus When phosphorus burns in air or oxygen, it yields tetraphosphorus hexoxide $\left(\mathrm{P}_{4} \mathrm{O}_{6}, \mathrm{mp} 24^{\circ} \mathrm{C}\right)$ or tetraphosphorus decoxide ( $\mathrm{P}_{4} \mathrm{O}_{10}, \mathrm{mp} 420^{\circ} \mathrm{C}$ ), depending on the amount of oxygen present:

$$
\begin{aligned}
& \text { Limited amount of } \mathrm{O}_{2}: \mathrm{P}_{4}(s)+3 \mathrm{O}_{2}(g) \longrightarrow \mathrm{P}_{4} \mathrm{O}_{6}(s) \\
& \text { Excess amount of } \mathrm{O}_{2}: \quad \mathrm{P}_{4}(s)+5 \mathrm{O}_{2}(g) \longrightarrow \mathrm{P}_{4} \mathrm{O}_{10}(s)
\end{aligned}
$$

Both oxides are molecular compounds and have structures with a tetrahedral array of P atoms, as in white phosphorus. One O atom bridges each of the six edges of the $\mathrm{P}_{4}$ tetrahedron, and an additional, terminal O atom is bonded to each P atom in $\mathrm{P}_{4} \mathrm{O}_{10}$.

$\mathrm{P}_{4} \mathrm{O}_{6}$


Both $\mathrm{P}_{4} \mathrm{O}_{6}$ and $\mathrm{P}_{4} \mathrm{O}_{10}$ are acidic oxides, and they react with water to form aqueous solutions of phosphorous acid and phosphoric acid, respectively:

$$
\begin{aligned}
& \mathrm{P}_{4} \mathrm{O}_{6}(s)+6 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 4 \mathrm{H}_{3} \mathrm{PO}_{3}(a q) \\
& \mathrm{P}_{4} \mathrm{O}_{10}(s)+6 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 4 \mathrm{H}_{3} \mathrm{PO}_{4}(a q)
\end{aligned}
$$

Because $\mathrm{P}_{4} \mathrm{O}_{10}$ has a great affinity for water, it is widely used as a drying agent for gases and organic solvents.

Phosphorous acid $\left(\mathrm{H}_{3} \mathrm{PO}_{3}\right)$ is a weak diprotic acid because only two of its three H atoms are bonded to oxygen. The H atom bonded directly to phosphorus is not acidic because phosphorus and hydrogen have the same electronegativity and the $\mathrm{P}-\mathrm{H}$ bond is nonpolar. In phosphoric acid, however, all three hydrogens are attached to oxygen, and thus phosphoric acid is a weak triprotic acid. The geometry about the P atom in both molecules is tetrahedral, as expected. Note that the successive dissociation constants decrease by a factor of about $10^{5}$ (Section 15.11).


Phosphorous acid, $\mathrm{H}_{3} \mathrm{PO}_{3}$

$$
\begin{aligned}
& K_{\mathrm{a} 1}=1.0 \times 10^{-2} \\
& K_{\mathrm{a} 2}=2.6 \times 10^{-7}
\end{aligned}
$$



Phosphoric acid, $\mathrm{H}_{3} \mathrm{PO}_{4}$

$$
\begin{aligned}
& K_{\mathrm{a} 1}=7.5 \times 10^{-3} \\
& K_{\mathrm{a} 2}=6.2 \times 10^{-8} \\
& K_{\mathrm{a} 3}=4.8 \times 10^{-13}
\end{aligned}
$$

Pure phosphoric acid is a low-melting, colorless, crystalline solid ( $\mathrm{mp} 42^{\circ} \mathrm{C}$ ), but the commercially available phosphoric acid used in the laboratory is a syrupy, aqueous solution containing about $82 \% \mathrm{H}_{3} \mathrm{PO}_{4}$ by mass. The method used to manufacture phosphoric acid depends on its intended application. For use as a food additive-for example, as the tart ingredient in various soft drinks-pure phosphoric acid is made by burning molten phosphorus in a mixture of air and steam:

$$
\mathrm{P}_{4}(\mathrm{l}) \xrightarrow{\mathrm{O}_{2}} \mathrm{P}_{4} \mathrm{O}_{10}(\mathrm{~s}) \xrightarrow{\mathrm{H}_{2} \mathrm{O}} \mathrm{H}_{3} \mathrm{PO}_{4}(a q)
$$

For use in making fertilizers, an impure form of phosphoric acid is produced by treating phosphate rock with sulfuric acid:

$$
\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}(s)+3 \mathrm{H}_{2} \mathrm{SO}_{4}(a q) \longrightarrow 2 \mathrm{H}_{3} \mathrm{PO}_{4}(a q)+3 \mathrm{CaSO}_{4}(a q)
$$

Phosphoric acid is sometimes called orthophosphoric acid to distinguish it from polyphosphoric acids that are obtained when $\mathrm{H}_{3} \mathrm{PO}_{4}$ is heated. For example, diphosphoric acid, $\mathrm{H}_{4} \mathrm{P}_{2} \mathrm{O}_{7}$, also called pyrophosphoric acid, is obtained when two molecules of $\mathrm{H}_{3} \mathrm{PO}_{4}$ combine, with elimination of one water molecule:
-



Reaction of the phosphoric acid with more phosphate rock gives $\mathrm{Ca}\left(\mathrm{H}_{2} \mathrm{PO}_{4}\right)_{2}$, a water-soluble fertilizer known as triple superphosphate:

$$
\mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}(s)+4 \mathrm{H}_{3} \mathrm{PO}_{4}(a q) \longrightarrow 3 \mathrm{Ca}^{2+}(a q)+6 \mathrm{H}_{2} \mathrm{PO}_{4}^{-}(a q)
$$

The next in the series is triphosphoric acid, $\mathrm{H}_{5} \mathrm{P}_{3} \mathrm{O}_{10}$, and the one with an indefinitely long chain of phosphate groups is called polymetaphosphoric acid,


- Sodium triphosphate, $\mathrm{Na}_{5} \mathrm{P}_{3} \mathrm{O}_{10}$, in synthetic detergents can contribute to the eutrophication of rivers and lakes.

- 



Repeating unit, $\mathrm{HPO}_{3}$
Polymetaphosphoric acid, $\left(\mathrm{HPO}_{3}\right)_{n}$

All these acids have phosphorus in the +5 oxidation state, and all have structures in which $\mathrm{PO}_{4}$ tetrahedra share bridging O atoms.

The sodium salt of triphosphoric acid, $\mathrm{Na}_{5} \mathrm{P}_{3} \mathrm{O}_{10}$, is a component of some synthetic detergents. It is made by heating a stoichiometric mixture of the powdered orthophosphate salts $\mathrm{Na}_{2} \mathrm{HPO}_{4}$ and $\mathrm{NaH}_{2} \mathrm{PO}_{4}$ :

$$
2 \mathrm{Na}_{2} \mathrm{HPO}_{4}(s)+\mathrm{NaH}_{2} \mathrm{PO}_{4}(s) \longrightarrow \mathrm{Na}_{5} \mathrm{P}_{3} \mathrm{O}_{10}(s)+2 \mathrm{H}_{2} \mathrm{O}(g)
$$

The triphosphate ion $\mathrm{P}_{3} \mathrm{O}_{10}{ }^{5-}$ acts as a water softener, bonding to ions such as $\mathrm{Ca}^{2+}$ and $\mathrm{Mg}^{2+}$ that are responsible for the formation of soap scum in hard water. Unfortunately, $\mathrm{P}_{3} \mathrm{O}_{10}{ }^{5-}$ can also contribute to excessive fertilization and rampant growth of algae, a process called eutrophication, when phosphate-rich waste water is discharged into lakes. Subsequent decomposition of the algae can deplete a lake of oxygen and cause fish to die off.

## Worked Example 19.4

Write balanced equations for conversion of orthophosphoric acid to:
(a) Triphosphoric acid
(b) Polymetaphosphoric acid

## Strategy

Both reactions combine $\mathrm{H}_{3} \mathrm{PO}_{4}$ molecules, with elimination of water. For a phosphate chain of any length, the number of water molecules eliminated is one less than the number of P atoms in the chain. For a very long chain, as in $\left(\mathrm{HPO}_{3}\right)_{n}$, the number of water molecules eliminated is essentially the same as the number of P atoms in the chain.

## Solution

(a) $3 \mathrm{H}_{3} \mathrm{PO}_{4}(a q) \rightarrow \mathrm{H}_{5} \mathrm{P}_{3} \mathrm{O}_{10}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l)$
(b) $n \mathrm{H}_{3} \mathrm{PO}_{4}(a q) \rightarrow\left(\mathrm{HPO}_{3}\right)_{n}(a q)+n \mathrm{H}_{2} \mathrm{O}(l)$

PROBLEM 19.9 Elimination of water from $\mathrm{H}_{3} \mathrm{PO}_{4}$ leads to the formation of tetraphosphoric acid, $\mathrm{H}_{6} \mathrm{P}_{4} \mathrm{O}_{13}$. Write a balanced equation for the reaction. Draw structural formulas for $\mathrm{H}_{3} \mathrm{PO}_{4}$ and $\mathrm{H}_{6} \mathrm{P}_{4} \mathrm{O}_{13}$, and show how elimination of water gives $\mathrm{H}_{6} \mathrm{P}_{4} \mathrm{O}_{13}$.

### 19.12 The Group 6A Elements

The group 6A elements are oxygen, sulfur, selenium, tellurium, and polonium. As shown in Table 19.7, their properties exhibit the usual periodic trends. Both oxygen and sulfur are typical nonmetals. Selenium and tellurium are primarily nonmetallic in character, though the most stable allotrope of selenium, gray selenium, is a lustrous semiconducting solid. Tellurium is also a semiconductor and is usually classified as a semimetal. Polonium, a radioactive element that occurs in trace amounts in uranium ores, is a silvery white metal.


TABLE 19.7 Properties of the Group 6A Elements

| Property | Oxygen | Sulfur | Selenium | Tellurium | Polonium |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Valence electron configuration | $2 s^{2} 2 p^{4}$ | $3 s^{2} 3 p^{4}$ | $4 s^{2} 4 p^{4}$ | $5 s^{2} 5 p^{4}$ | $6 s^{2} 6 p^{4}$ |
| Melting point $\left({ }^{\circ} \mathrm{C}\right)$ | -219 | $113^{*}$ | $221^{\dagger}$ | 450 | 254 |
| Boiling point $\left({ }^{\circ} \mathrm{C}\right)$ | -183 | 445 | 685 | 988 | 962 |
| Atomic radius $(\mathrm{pm})$ | 66 | 104 | 116 | 143 | 167 |
| $\mathrm{X}^{2-}$ ionic radius $(\mathrm{pm})$ | 132 | 184 | 191 | 211 |  |
| First ionization energy (kJ/mol) | 1314 | 1000 | 941 | 869 | 812 |
| Electron affinity $(\mathrm{kJ} / \mathrm{mol})$ | -141 | -200 | -195 | -190 | -183 |
| Electronegativity | 3.5 | 2.5 | 2.4 | 2.1 | 2.0 |
| Redox potential, $E^{\circ}(\mathrm{V})$ for | 1.23 | 0.14 | -0.40 | -0.79 | - |
| $\mathrm{X}+2 \mathrm{H}^{+}+2 \mathrm{e}^{-} \rightarrow \mathrm{H}_{2} \mathrm{X}$ |  |  |  |  |  |

*Rhombic S
${ }^{\dagger}$ Gray Se
With valence electron configuration $n s^{2} n p^{4}$, the group 6A elements are just two electrons short of an octet configuration, and the -2 oxidation state is therefore common. The stability of the -2 state decreases, however, with increasing metallic character, as indicated by the $E^{\circ}$ values in Table 19.7. Thus, oxygen is a powerful oxidizing agent, but $E^{\circ}$ values for reduction of Se and Te are negative, which means that $\mathrm{H}_{2} \mathrm{Se}$ and $\mathrm{H}_{2} \mathrm{Te}$ are reducing agents. Because $\mathrm{S}, \mathrm{Se}$, and Te are much less electronegative


A The color of the red glass in these traffic signals is due to cadmium selenide, CdSe.


(1)Miriam C. Nagel, "Herman Frasch, Sulfur King," J. Chem. Educ., Vol. 58, 1981, 60-61.

3D models of $\mathrm{H}_{2} \mathrm{~S}$ and $\mathrm{SO}_{2}$

than oxygen, they are commonly found in positive oxidation states, especially +4 , as in $\mathrm{SF}_{4}, \mathrm{SO}_{2}$, and $\mathrm{H}_{2} \mathrm{SO}_{3}$, and +6 , as in $\mathrm{SF}_{6}, \mathrm{SO}_{3}$, and $\mathrm{H}_{2} \mathrm{SO}_{4}$.

Commercial uses of $\mathrm{Se}, \mathrm{Te}$, and Po are limited, though selenium is used to make red colored glass and in photocopiers (see the Interlude at the end of this chapter). Tellurium is used in alloys to improve their machinability, and polonium ( ${ }^{210} \mathrm{Po}$ ) has been used as a heat source in space equipment and as a source of alpha particles in scientific research.

### 19.13 Sulfur

Sulfur is the sixteenth most abundant element in the earth's crust- $0.026 \%$ by mass. It occurs in elemental form in large underground deposits and is present in numerous minerals such as pyrite ( $\mathrm{FeS}_{2}$, which contains the $\mathrm{S}_{2}{ }^{2-}$ ion), galena ( PbS , page 832 ), cinnabar ( HgS ), and gypsum $\left(\mathrm{CaSO}_{4} \cdot 2 \mathrm{H}_{2} \mathrm{O}\right)$. Sulfur is also present in natural gas as $\mathrm{H}_{2} \mathrm{~S}$ and in crude oil as organic sulfur compounds. In plants and animals, sulfur occurs in various proteins, and it is one of the 10 most abundant elements in the human body (Figure 19.1).

> Pyrite $\left(\mathrm{FeS}_{2}\right)$ is often called fool's gold because of its golden yellow color. It contains the disulfide ion ( $\mathrm{S}_{2}{ }^{2-}$ ), the sulfur analogue of the peroxide ion $\left(\mathrm{O}_{2}{ }^{2-}\right)$.


Elemental sulfur is obtained from underground deposits and recovered from natural gas and crude oil. Sulfur is removed from these fuels prior to burning in order to prevent pollution of the air with $\mathrm{SO}_{2}$ and subsequent formation of acid rain (see the Interlude in Chapter 15). The sulfur compounds in gas and oil are first converted to $\mathrm{H}_{2} \mathrm{~S}$, one-third of which is then burned to give $\mathrm{SO}_{2}$. Subsequent reaction of the $\mathrm{SO}_{2}$ with the remaining $\mathrm{H}_{2} \mathrm{~S}$ yields elemental sulfur:

$$
\begin{aligned}
& 2 \mathrm{H}_{2} \mathrm{~S}(g)+3 \mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{SO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(g) \\
& \mathrm{SO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{~S}(g) \xrightarrow[\mathrm{Fe}_{2} \mathrm{O}_{3} \text { catalyst }]{30{ }^{\circ} \mathrm{C}} 3 \mathrm{~S}(g)+2 \mathrm{H}_{2} \mathrm{O}(g)
\end{aligned}
$$

In the United States, $88 \%$ of the sulfur produced is used to manufacture sulfuric acid.
Sulfur exists in many allotropic forms, but the most stable at $25^{\circ} \mathrm{C}$ is rhombic sulfur, a yellow crystalline solid ( $\mathrm{mp} 113^{\circ} \mathrm{C}$ ) that contains crown-shaped $\mathrm{S}_{8}$ rings:



A A sample of rhombic sulfur, the most stable allotrope of sulfur.


可Note that all allotropes of period 3 sulfur have only single bonds, whereas period 2 oxygen has a double bond in $\mathrm{O}_{2}$. brown, and its viscosity increases by a factor of more than 10,000. At still-higher temperatures, the liquid becomes more fluid again and then boils at $445^{\circ} \mathrm{C}$ to give a vapor that contains mostly $\mathrm{S}_{8}$ molecules along with smaller amounts of other $\mathrm{S}_{n}$ molecules $(2 \leq n \leq 10)$. If the liquid is cooled rapidly by pouring it into water, the sulfur forms an amorphous, rubbery material called plastic sulfur.

(a)

(b)

(c)

The dramatic increase in the viscosity of molten sulfur at $160-195^{\circ} \mathrm{C}$ is due to the opening of the $\mathrm{S}_{8}$ rings, yielding $\mathrm{S}_{8}$ chains that form long polymers with more than $200,000 \mathrm{~S}$ atoms in the chain:
$\mathrm{S}_{8}$ rings $\xrightarrow{\text { Heat }} \cdot \mathrm{S}-\mathrm{S}_{6}-\mathrm{S} \cdot$ chains

$$
\cdot \mathrm{S}-\mathrm{S}_{6}-\mathrm{S} \cdot \text { chains }+\mathrm{S}_{8} \text { rings } \longrightarrow \cdot \mathrm{S}-\mathrm{S}_{14}-\mathrm{S} \cdot \text { chains } \mathrm{L}
$$

- FIGURE 19.11 Effect of temperature on the properties of sulfur. (a) Fluid, strawcolored liquid sulfur at about $120^{\circ} \mathrm{C}$. (b) Viscous, reddish brown liquid sulfur at about $180^{\circ} \mathrm{C}$. (c) Plastic sulfur, obtained by pouring liquid sulfur into water. Plastic sulfur is unstable and reverts to rhombic sulfur on standing at room temperature.


Hydrogen sulfide $\mathrm{H}_{2} \mathrm{~S} 3 \mathrm{D}$ model

$\square$
Expecting to see a yellow solid, students frequently do not recognize finely divided sulfur, which appears white.


Sulfur dioxide


Sulfur trioxide

3D models of $\mathrm{SO}_{2}$ and $\mathrm{SO}_{3}$

Whereas the small $\mathrm{S}_{8}$ rings easily slide over one another in the liquid, the long polymer chains become entangled, thus accounting for the increase in viscosity. Above $200^{\circ} \mathrm{C}$, the polymer chains begin to fragment into smaller pieces, and the viscosity therefore decreases. On rapid cooling, the chains are temporarily frozen in a disordered, tangled arrangement, which accounts for the elastic properties of plastic sulfur.

## Sulfur Compounds

Hydrogen Sulfide Hydrogen sulfide is a colorless gas (bp $-61^{\circ} \mathrm{C}$ ) with the strong, foul odor we associate with rotten eggs, in which it occurs because of the bacterial decomposition of sulfur-containing proteins. Hydrogen sulfide is extremely toxic, causing headaches and nausea at concentrations of 10 ppm and sudden paralysis and death at 100 ppm . On initial exposure, the odor of $\mathrm{H}_{2} \mathrm{~S}$ can be detected at about 0.02 ppm , but unfortunately the gas tends to dull the sense of smell. It is thus an extremely insidious poison, even more dangerous than HCN.

In the laboratory, $\mathrm{H}_{2} \mathrm{~S}$ can be prepared by treating iron(II) sulfide with dilute sulfuric acid:

$$
\mathrm{FeS}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{H}_{2} \mathrm{~S}(g)+\mathrm{Fe}^{2+}(a q)
$$

For use in qualitative analysis (Section 16.15), $\mathrm{H}_{2} \mathrm{~S}$ is usually generated in solution by the hydrolysis of thioacetamide:


Hydrogen sulfide is a very weak diprotic acid ( $K_{\mathrm{a} 1}=1.0 \times 10^{-7} ; K_{\mathrm{a} 2} \approx 10^{-19}$ ) and a mild reducing agent. In reactions with mild oxidizing agents, it is oxidized to a milky white suspension of elemental sulfur:

$$
\mathrm{H}_{2} \mathrm{~S}(a q)+2 \mathrm{Fe}^{3+}(a q) \longrightarrow \mathrm{S}(s)+2 \mathrm{Fe}^{2+}(a q)+2 \mathrm{H}^{+}(a q)
$$

Oxides and Oxoacids of Sulfur Sulfur dioxide $\left(\mathrm{SO}_{2}\right)$ and sulfur trioxide $\left(\mathrm{SO}_{3}\right)$ are the most important of the various oxides of sulfur. Sulfur dioxide, a colorless,

Sulfur burns in air with a blue flame, yielding $\mathrm{SO}_{2}$ gas.

toxic gas ( $\mathrm{bp}-10^{\circ} \mathrm{C}$ ) with a pungent, choking odor, is formed when sulfur burns in air:

$$
\mathrm{S}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{SO}_{2}(g)
$$

Sulfur dioxide is slowly oxidized in the atmosphere to $\mathrm{SO}_{3}$, which dissolves in rainwater to give sulfuric acid. The burning of sulfur-containing fuels is thus a major cause of acid rain (Section 9.9). In the laboratory, $\mathrm{SO}_{2}$ is conveniently prepared by treating sodium sulfite with dilute acid:

$$
\mathrm{Na}_{2} \mathrm{SO}_{3}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{SO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)+2 \mathrm{Na}^{+}(a q)
$$

Because $\mathrm{SO}_{2}$ is toxic to microorganisms, it is used for sterilizing wine and dried fruit.
Both $\mathrm{SO}_{2}$ and $\mathrm{SO}_{3}$ are acidic, though aqueous solutions of $\mathrm{SO}_{2}$ contain mainly dissolved $\mathrm{SO}_{2}$ and little, if any, sulfurous acid $\left(\mathrm{H}_{2} \mathrm{SO}_{3}\right)$ :

$$
\mathrm{SO}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{2} \mathrm{SO}_{3}(a q)
$$

Nevertheless, it's convenient to write the acidic species as $\mathrm{H}_{2} \mathrm{SO}_{3}$, a weak diprotic acid:

$$
\begin{array}{ll}
\mathrm{H}_{2} \mathrm{SO}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{HSO}_{3}^{-}(a q) & K_{\mathrm{a} 1}=1.5 \times 10^{-2} \\
\mathrm{HSO}_{3}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{SO}_{3}^{2-}(a q) & K_{\mathrm{a} 2}=6.3 \times 10^{-8}
\end{array}
$$

Like carbonic acid, sulfurous acid has never been isolated in pure form.
Sulfuric acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$, the world's most important industrial chemical, is manufactured by the contact process, a three-step reaction sequence in which (1) sulfur burns in air to give $\mathrm{SO}_{2}$, (2) $\mathrm{SO}_{2}$ is oxidized to $\mathrm{SO}_{3}$ in the presence of a vanadium $(V)$ oxide catalyst, and (3) $\mathrm{SO}_{3}$ reacts with water to give $\mathrm{H}_{2} \mathrm{SO}_{4}$ :
(2) $2 \mathrm{SO}_{2}(g)+\mathrm{O}_{2}(g) \xrightarrow[\mathrm{V}_{2} \mathrm{O}_{5} \text { catalyst }]{\text { Heat }} 2 \mathrm{SO}_{3}(g)$
(3) $\mathrm{SO}_{3}(g)+\mathrm{H}_{2} \mathrm{O}\left(\right.$ in conc $\left.\mathrm{H}_{2} \mathrm{SO}_{4}\right) \longrightarrow \mathrm{H}_{2} \mathrm{SO}_{4}$ (in conc $\mathrm{H}_{2} \mathrm{SO}_{4}$ )

In the third step, the $\mathrm{SO}_{3}$ is absorbed in concentrated sulfuric acid rather than in water because the dissolution of $\mathrm{SO}_{3}$ in water is slow. Water is then added to achieve the desired concentration. Commercial concentrated sulfuric acid is $98 \%$ $\mathrm{H}_{2} \mathrm{SO}_{4}$ by mass $\left(18 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}\right)$. Anhydrous ( $100 \%$ ) $\mathrm{H}_{2} \mathrm{SO}_{4}$ is a viscous, colorless liquid that freezes at $10.4^{\circ} \mathrm{C}$ and boils above $300^{\circ} \mathrm{C}$. The $\mathrm{H}_{2} \mathrm{SO}_{4}$ molecule is tetrahedral, as predicted by the VSEPR model (Section 7.9)

Sulfuric acid is a strong acid in the dissociation of its first proton and has $K_{\mathrm{a} 2}=1.2 \times 10^{-2}$ for the dissociation of its second proton. As a diprotic acid, it forms two series of salts: hydrogen sulfates (bisulfates), such as $\mathrm{NaHSO}_{4}$, and sulfates, such as $\mathrm{Na}_{2} \mathrm{SO}_{4}$.

The oxidizing properties of sulfuric acid depend on its concentration and temperature. In dilute solutions at room temperature, $\mathrm{H}_{2} \mathrm{SO}_{4}$ behaves like HCl , oxidizing metals that stand above hydrogen in the activity series (Table 4.3, page 132):

$$
\mathrm{Fe}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Fe}^{2+}(a q)+\mathrm{H}_{2}(g)
$$

Hot, concentrated $\mathrm{H}_{2} \mathrm{SO}_{4}$ is a better oxidizing agent than the dilute, cold acid and can oxidize metals like copper, which are not oxidized by $\mathrm{H}^{+}(a q)$. In the process, $\mathrm{H}_{2} \mathrm{SO}_{4}$ is reduced to $\mathrm{SO}_{2}$ :

$$
\mathrm{Cu}(s)+2 \mathrm{H}_{2} \mathrm{SO}_{4}(l) \longrightarrow \mathrm{Cu}^{2+}(a q)+\mathrm{SO}_{4}^{2-}(a q)+\mathrm{SO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)
$$

U.S. production of sulfuric acid in 2001 was 40.1 million tons, far exceeding that of any other chemical (Table 19.1). It is used mostly to manufacture soluble phosphate and ammonium sulfate fertilizers, but it is essential to many other industries (Figure 19.12). So widespread is the use of sulfuric acid in industrial countries that the amount produced is sometimes regarded as an indicator of economic activity.


$\checkmark$
A small segment of the population experiences a severe allergic reaction to foods treated with sulfites, the presence of which is noted on wine-bottle labels but not always on labels of dried fruits and nuts.




Sulfuric acid

FIGURE 19.12 Uses of sulfuric acid in the United States.


KEY CONCEPT PROBLEM 19.10 Consider the following sulfur-containing oxoanions:


Physical Properties of the Halogens movie

Only four of the acids listed in Table 19.8 have been isolated in pure form: perchloric acid $\left(\mathrm{HClO}_{4}\right)$, iodic acid $\left(\mathrm{HIO}_{3}\right)$, and the two periodic acids, metaperiodic acid $\left(\mathrm{HIO}_{4}\right)$ and paraperiodic acid $\left(\mathrm{H}_{5} \mathrm{IO}_{6}\right)$. The others are stable only in aqueous solution or in the form of their salts. Chlorous acid $\left(\mathrm{HClO}_{2}\right)$ is the only known halous acid.

The acid strength of the halogen oxoacids increases with the increasing oxidation state of the halogen (Section 15.15). For example, acid strength increases from HClO , a weak acid $\left(K_{\mathrm{a}}=3.5 \times 10^{-8}\right)$, to $\mathrm{HClO}_{4}$, a very strong acid $\left(K_{\mathrm{a}} \gg 1\right)$. The acidic proton is bonded to oxygen, not to the halogen, even though we usually write the molecular formula of these acids as $\mathrm{HXO}_{n}$. All the halogen oxoacids and their salts are strong oxidizing agents.

A hypohalous acid is formed when $\mathrm{Cl}_{2}, \mathrm{Br}_{2}$, or $\mathrm{I}_{2}$ dissolves in cold water:

$$
\mathrm{X}_{2}(g, l, \text { or } s)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HOX}(a q)+\mathrm{H}^{+}(a q)+\mathrm{X}^{-}(a q)
$$

In this reaction, the halogen disproportionates, going to the +1 oxidation state in HOX and the -1 state in $X^{-}$. The equilibrium lies to the left but is shifted to the right in basic solution:

$$
\mathrm{X}_{2}(g, l, \text { or } s)+2 \mathrm{OH}^{-}(a q) \rightleftharpoons \mathrm{OX}^{-}(a q)+\mathrm{X}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l)
$$

Large amounts of aqueous sodium hypochlorite $(\mathrm{NaOCl})$ are produced in the chlor-alkali industry (Section 18.12) when the $\mathrm{Cl}_{2}$ gas and aqueous NaOH from the electrolysis of aqueous NaCl are allowed to mix. Aqueous NaOCl is a strong oxidizing agent and is sold in a $5 \%$ solution as chlorine bleach.

Further disproportionation of $\mathrm{OCl}^{-}$to $\mathrm{ClO}_{3}^{-}$and $\mathrm{Cl}^{-}$is slow at room temperature but becomes fast at higher temperatures. Thus, when $\mathrm{Cl}_{2}$ gas reacts with hot aqueous NaOH , it gives a solution that contains sodium chlorate $\left(\mathrm{NaClO}_{3}\right)$ rather than NaOCl :

$$
3 \mathrm{Cl}_{2}(g)+6 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{ClO}_{3}^{-}(a q)+5 \mathrm{Cl}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l)
$$

Chlorate salts are used as weed-killers and as strong oxidizing agents. Potassium chlorate, for example, is an oxidizer in matches, fireworks, and explosives. It also reacts vigorously with organic matter.

Sodium perchlorate $\left(\mathrm{NaClO}_{4}\right)$ is produced commercially by the electrolytic oxidation of aqueous sodium chlorate and is converted to perchloric acid by reaction with concentrated HCl :

$$
\begin{aligned}
& \mathrm{ClO}_{3}^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \xrightarrow{\text { Electrolysis }} \mathrm{ClO}_{4}^{-}(a q)+\mathrm{H}_{2}(g) \\
& \mathrm{NaClO}_{4}(s)+\mathrm{HCl}(a q) \longrightarrow \mathrm{HClO}_{4}(a q)+\mathrm{NaCl}(s)
\end{aligned}
$$

The $\mathrm{HClO}_{4}$ is then concentrated by distillation at reduced pressure.
Pure, anhydrous perchloric acid is a colorless, shock-sensitive liquid that decomposes explosively on heating. It is a powerful and dangerous oxidizing agent, violently oxidizing organic matter and rapidly oxidizing even silver and gold. Perchlorate salts are also strong oxidants, and they too must be handled with caution. Ammonium perchlorate $\left(\mathrm{NH}_{4} \mathrm{ClO}_{4}\right)$, in fact, is the oxidizer in the solid booster rockets used to propel the space shuttle.

Iodine differs from the other halogens because it forms more than one perhalic acid. Paraperiodic acid $\left(\mathrm{H}_{5} \mathrm{IO}_{6}\right)$ is obtained as white crystals (mp $128^{\circ} \mathrm{C}$ ) when periodic acid solutions are evaporated. When heated to $100^{\circ} \mathrm{C}$ at reduced pressure, these crystals lose water and are converted to metaperiodic acid ( $\mathrm{HIO}_{4}$ ):

$$
\mathrm{H}_{5} \mathrm{IO}_{6}(\mathrm{~s}) \xrightarrow[12 \mathrm{~mm} \mathrm{Hg}]{100^{\circ} \mathrm{C}} \mathrm{HIO}_{4}(\mathrm{~s})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{~g})
$$

C. E. Ophardt, "Redox Demonstrations and Descriptive Chemistry: Part 2. Halogens," J. Chem. Educ., Vol. 64, 1987, 807. Using an abbreviated table of reduction potentials as a predictive tool, reactions of bromine and iodine in various oxidation states are demonstrated.

## Robert C. Hansen, "An Over-

head Demonstration of Some Descriptive Chemistry of the Halogens and Le Châtelier's Principle," J. Chem. Educ., Vol. 65, 1988, 264-265.

Metaperiodic acid is a strong monoprotic acid, whereas paraperiodic acid is a weak polyprotic acid $\left(K_{\mathrm{a} 1}=5.1 \times 10^{-4} ; K_{\mathrm{a} 2}=4.9 \times 10^{-9}\right)$. It has an octahedral structure in which a central iodine atom is bonded to one O atom and five OH groups:



Paraperiodic acid, $\mathrm{H}_{5} \mathrm{IO}_{6}$


Metaperiodic acid, $\mathrm{HIO}_{4}$

Chlorine and bromine do not form perhalic acids of the type $\mathrm{H}_{5} \mathrm{XO}_{6}$ because their smaller sizes favor a tetrahedral structure over an octahedral one.

FIGURE 19.13 The photocopying process. A seleniumcoated rotating drum is given a uniform positive charge (step 1) and is then exposed to an image (step 2). Negatively charged toner particles are attracted to the charged areas of the drum (step 3), and the image is transferred from the drum to a sheet of paper (step 4). Heating then fixes the image, and the drum is flooded with light and cleaned to ready the machine for another cycle (step 5).

## Photocopiers

Not too many years ago, copies of documents were made either by using various wet photographic methods or by typing the original using "carbon paper." The introduction of the plain-paper photocopy machine in the mid-1950s revolutionized the way offices handle paper. Now, the most widely used method of document copying is based on xerography, a term derived from the Greek words for "dry writing."

Dry photocopiers use an unusual property of selenium, the group 6A element below sulfur in the periodic table. Selenium is a photoconductor, a substance that is a poor electrical conductor when dark but whose conductivity increases (by a factor of 1000) when exposed to light. When the light is removed, the conductivity again drops.

As illustrated in Figure 19.13, the xerographic process begins when a seleniumcoated drum is given a uniform positive charge and is then exposed through a lens to a brightly illuminated document. Those areas on the drum that correspond to a light part of the document become conducting when exposed and lose their charge, while those areas on the drum that correspond to a dark part of the document remain nonconducting and retain their charge. Thus, an image of the document is formed on the drum as an array of positive electrical charges.


Following its formation, the image is developed by exposing the drum to negatively charged dry ink particles (toner), which are attracted to the positively charged areas of the drum. The developed image is then transferred to paper by passing a sheet of paper between the drum and a positively charged development electrode, which induces the negatively charged toner particles to jump from the drum to the paper.

The toner particles, in addition to serving as pigment, are made of a resinous plastic material that fuses to the paper when heated, thereby fixing the image. The final copy then rolls out of the machine, and the drum is restored to its original condition by flooding it with light to remove all remaining charges and gently scraping off any bits of excess toner.

- PROBLEM 19.12 What would be the effect of coating the photocopier drum with copper instead of selenium? Explain.


## Summary

The main-group elements are the $s$-block elements of groups 1 A and 2A and the $p$-block elements of groups 3A-8A. From left to right across the periodic table, ionization energy, electronegativity, and nonmetallic character generally increase, while atomic radius and metallic character decrease. From top to bottom of a group in the periodic table, ionization energy, electronegativity, and nonmetallic character generally decrease, while atomic radius and metallic character increase. The second-row elements form strong multiple bonds but are unable to form more than four bonds because they lack valence $d$ orbitals.

The group 3A elements-B, Al, Ga, In, and Tl -are metals except for boron, which is a semimetal. Boron is a semiconductor and forms molecular compounds. Boranes, such as diborane ( $\mathrm{B}_{2} \mathrm{H}_{6}$ ), are electron-deficient molecules that contain three-center, two-electron bonds ( $\mathrm{B}-\mathrm{H}-\mathrm{B}$ ).

The group 4A elements- $\mathrm{C}, \mathrm{Si}, \mathrm{Ge}, \mathrm{Sn}$, and Pb -exhibit the usual increase in metallic character down the group. Their most common oxidation state is +4 , but the +2 state becomes increasingly more stable from Ge to Sn to Pb . In elemental form, carbon exists as diamond, graphite, fullerene, coke, charcoal, and carbon black.

Silicon, the second most abundant element in the earth's crust, is obtained by reducing silica sand $\left(\mathrm{SiO}_{2}\right)$ with coke. It is purified for use in the semiconductor industry by zone refining. In the silicates, $\mathrm{SiO}_{4}$ tetrahedra share common O atoms to give silicon oxoanions with ring, chain, layer, and extended three-dimensional structures. In aluminosilicates, such as $\mathrm{KAlSi}_{3} \mathrm{O}_{8}, \mathrm{Al}^{3+}$ replaces some of the $\mathrm{Si}^{4+}$.

Molecular nitrogen $\left(\mathrm{N}_{2}\right)$ is unreactive because of its strong $\mathrm{N} \equiv \mathrm{N}$ triple bond. Nitrogen exhibits all oxidation states between -3 and +5 . Nitric acid is manufactured by the Ostwald process.

Phosphorus, the most abundant group 5A element, exists in two common allotropic forms-white phosphorus, which contains highly reactive tetrahedral $\mathrm{P}_{4}$ molecules, and red phosphorus, which is polymeric. The most common oxidation states of P are -3 , as in phosphine $\left(\mathrm{PH}_{3}\right) ;+3$, as in $\mathrm{PCl}_{3}, \mathrm{P}_{4} \mathrm{O}_{6}$, and $\mathrm{H}_{3} \mathrm{PO}_{3}$; and +5 , as in $\mathrm{PCl}_{5}, \mathrm{P}_{4} \mathrm{O}_{10}$, and $\mathrm{H}_{3} \mathrm{PO}_{4}$. On heating, $\mathrm{H}_{3} \mathrm{PO}_{4}$ molecules combine, with elimination of water molecules, yielding polyphosphoric acids (for example, $\mathrm{H}_{5} \mathrm{P}_{3} \mathrm{O}_{10}$ ) or polymetaphosphoric acid $\left(\mathrm{HPO}_{3}\right)_{n}$.

Sulfur is obtained from underground deposits and is recovered from natural gas and crude oil. The properties of sulfur change dramatically on heating as the $\mathrm{S}_{8}$ rings of rhombic sulfur open and polymerize to give long chains, which then fragment at higher temperatures. The most common oxidation states of S are -2 , as in $\mathrm{H}_{2} \mathrm{~S} ;+4$, as in $\mathrm{SO}_{2}$ and $\mathrm{H}_{2} \mathrm{SO}_{3}$; and +6 , as in $\mathrm{SO}_{3}$ and $\mathrm{H}_{2} \mathrm{SO}_{4}$. Sulfuric acid, the world's most important industrial chemical, is manufactured by the contact process.

Chlorine, bromine, and iodine form a series of oxoacids: hypohalous acid ( HXO ), halous acid $\left(\mathrm{HXO}_{2}\right.$ for $\left.\mathrm{X}=\mathrm{Cl}\right)$, halic acid $\left(\mathrm{HXO}_{3}\right)$, and perhalic acid $\left(\mathrm{HXO}_{4}\right)$. Acid strength increases as the oxidation state of the halogen increases from +1 to +7 . Iodine forms two perhalic acids, $\mathrm{HIO}_{4}$ and $\mathrm{H}_{5} \mathrm{IO}_{6}$. Halogen oxoacids and their salts are strong oxidizing agents.
aluminosilicate 830
boranes 822
carbide 827
contact process 847

Ostwald process 837 polyphosphoric acids 842 pseudohalide 827
silicate 828
three-center two-
electron bond 823

## Key Concept Summary



## Understanding Key Concepts

Problems 19.1-19.12 appear within the chapter.
19.13 Locate each of the following groups of elements on the periodic table.

(a) Main-group elements
(b) $s$-Block elements
(c) $p$-Block elements
(d) Main-group metals
(e) Nonmetals
(f) Semimetals
19.14 Locate each of the following elements on the periodic table.

(a) Element with the lowest ionization energy
(b) Most electronegative element
(c) Group 4A element with the largest atomic radius
(d) Group 6A element with the smallest atomic radius
(e) Group 3A element that is a semiconductor
(f) Group 5A element that forms the strongest $\pi$ bonds
19.15 Locate the following elements on the periodic table.

(a) Elements that are gases at room temperature $\left(25^{\circ} \mathrm{C}\right)$
(b) An element that is a liquid at $25^{\circ} \mathrm{C}$
(c) Nonmetals that are solids at $25^{\circ} \mathrm{C}$
(d) Elements that exist as diatomic molecules at $25^{\circ} \mathrm{C}$
19.16 Consider the six second- and third-row elements in groups 5A-7A of the periodic table:


Possible molecular structures for common allotropes of these elements are shown below:

(a) What is the molecular structure of each of the six elements?
(b) Using electron-dot structures, explain why each element has its particular molecular structure.
(c) Explain why nitrogen and phosphorus have different molecular structures and why oxygen and sulfur have different molecular structures, but fluorine and chlorine have the same molecular structure.
19.17 The following models represent the structures of binary oxides of second- and third-row elements in their highest oxidation states:

(a) Identify the nonoxygen atom in each case, and write the molecular formula for each oxide.
(b) Draw an electron-dot structure for each oxide. For which oxides are resonance structures needed?
19.18 The following models represent the structures of binary hydrides of second-row elements:

(a) Identify the nonhydrogen atom in each case, and write the molecular formula for each hydride.
(b) Draw an electron-dot structure for each hydride. For which hydride is there a problem in drawing the structure? Explain.
19.19 The following pictures represent various silicate anions. Give the formula and charge of each anion.


(c)

## Additional Problems

## General Properties and Periodic Trends

19.20 Which element in each of the following pairs has the higher ionization energy?
(a) S or Cl
(b) Si or Ge
(c) In or O
19.21 Arrange the following elements in order of increasing ionization energy:
(a) P
(b) K
(c) Al
(d) F
19.22 Which element in each of the following pairs has the larger atomic radius?
(a) B or Al
(b) PorS
(c) Pb or Br
19.23 Arrange the following elements in order of increasing atomic radius:
(a) As
(b) O
(c) Sn
(d) S
19.24 Which element in each of the following pairs has the higher electronegativity?
(a) Te or I
(b) N or P
(c) In or F
19.25 Arrange the following elements in order of increasing electronegativity:
(a) N
(b) Ge
(c) O
(d) P
19.26 Which element in each of the following pairs has more metallic character?
(a) Si or Sn
(b) Ge or Se
(c) Bi or I
19.27 Which element in each of the following pairs has more nonmetallic character?
(a) S or Te
(b) Cl or P
(c) Bi or Br
19.28 Which compound in each of the following pairs is more ionic?
(a) $\mathrm{CaH}_{2}$ or $\mathrm{NH}_{3}$
(b) $\mathrm{P}_{4} \mathrm{O}_{6}$ or $\mathrm{Ga}_{2} \mathrm{O}_{3}$
(c) $\mathrm{SiCl}_{4}$ or KCl
(d) $\mathrm{BCl}_{3}$ or $\mathrm{AlCl}_{3}$
19.29 Which compound in each of the following pairs is more covalent?
(a) $\mathrm{PCl}_{3}$ or $\mathrm{AlF}_{3}$
(b) CaO or NO
(c) $\mathrm{NH}_{3}$ or KH
(d) $\mathrm{SnO}_{2}$ or $\mathrm{SiO}_{2}$
19.30 Which of the following compounds are molecular, and which have an extended three-dimensional structure?
(a) $\mathrm{B}_{2} \mathrm{H}_{6}$
(b) $\mathrm{KAlSi}_{3} \mathrm{O}_{8}$
(c) $\mathrm{SO}_{3}$
(d) $\mathrm{GeCl}_{4}$
19.31 Which of the following compounds are molecular, and which have an extended three-dimensional structure?
(a) KF
(b) $\mathrm{P}_{4} \mathrm{O}_{10}$
(c) $\mathrm{SiCl}_{4}$
(d) $\mathrm{CaMgSi} 2_{2} \mathrm{O}_{6}$
19.32 Which oxide in each of the following pairs is more acidic?
(a) $\mathrm{Al}_{2} \mathrm{O}_{3}$ or $\mathrm{P}_{4} \mathrm{O}_{10}$
(b) $\mathrm{B}_{2} \mathrm{O}_{3}$ or $\mathrm{Ga}_{2} \mathrm{O}_{3}$
(c) $\mathrm{SO}_{2}$ or $\mathrm{SnO}_{2}$
(d) $\mathrm{As}_{2} \mathrm{O}_{3}$ or $\mathrm{N}_{2} \mathrm{O}_{3}$
19.33 Which oxide in each of the following pairs is more basic?
(a) $\mathrm{SO}_{2}$ or $\mathrm{SnO}_{2}$
(b) $\mathrm{In}_{2} \mathrm{O}_{3}$ or $\mathrm{Ga}_{2} \mathrm{O}_{3}$
(c) $\mathrm{Al}_{2} \mathrm{O}_{3}$ or $\mathrm{N}_{2} \mathrm{O}_{5}$
(d) BaO or MgO
19.34 Consider the elements $\mathrm{C}, \mathrm{Se}, \mathrm{B}, \mathrm{Sn}, \mathrm{Cl}$. Identify the element on this list that:
(a) Has the largest atomic radius
(b) Is the most electronegative
(c) Is the best electrical conductor
(d) Has a maximum oxidation state of +6
(e) Forms a hydride with the empirical formula $\mathrm{XH}_{3}$
19.35 Consider the elements $\mathrm{N}, \mathrm{Si}, \mathrm{Al}, \mathrm{S}, \mathrm{F}$. Identify the element on this list that:
(a) Has the highest ionization energy
(b) Has the most metallic character
(c) Forms the strongest $\pi$ bonds
(d) Is a semiconductor
(e) Forms a 2- anion
19.36 $\mathrm{BF}_{3}$ reacts with $\mathrm{F}^{-}$to give $\mathrm{BF}_{4}{ }^{-}$, but $\mathrm{AlF}_{3}$ reacts with $\mathrm{F}^{-}$ to give $\mathrm{AlF}_{6}{ }^{3-}$. Explain.
$19.37 \mathrm{GeCl}_{4}$ reacts with $\mathrm{Cl}^{-}$to give $\mathrm{GeCl}_{6}{ }^{2-}$, but $\mathrm{CCl}_{4}$ does not react with excess $\mathrm{Cl}^{-}$. Explain.
19.38 At ordinary temperatures, sulfur exists as $\mathrm{S}_{8}$, but oxygen exists as $\mathrm{O}_{2}$. Explain.
19.39 Elemental nitrogen exists as $\mathrm{N}_{2}$, but white phosphorus exists as $\mathrm{P}_{4}$. Explain.

## The Group 3A Elements

19.40 What is the most common oxidation state for each of the group 3A elements?
19.41 What is the oxidation state of the group 3A element in each of the following compounds?
(a) $\mathrm{NaBF}_{4}$
(b) $\mathrm{GaCl}_{3}$
(c) TlCl
(d) $\mathrm{B}_{2} \mathrm{H}_{6}$
19.42 List three ways in which the properties of boron differ from those of the other group 3A elements.
19.43 Explain why the properties of boron differ so markedly from the properties of the other group 3A elements.
19.44 How is crystalline boron prepared? Write a balanced equation for the reaction.
19.45 Write a balanced equation for the reduction of boron oxide by magnesium.
19.46 Tell what is meant by:
(a) An electron-deficient molecule
(b) A three-center, two-electron bond

Illustrate each definition with an example.
19.47 Describe the structure of diborane $\left(\mathrm{B}_{2} \mathrm{H}_{6}\right)$, and explain why the bridging $\mathrm{B}-\mathrm{H}$ bonds are longer than the terminal B-H bonds.
19.48 Identify the group 3A element that best fits each of the following descriptions:
(a) Is the most abundant element of the group
(b) Is stable in the +1 oxidation state
(c) Is a semiconductor
(d) Forms a molecular fluoride
19.49 Identify the group 3 A element that best fits each of the following descriptions:
(a) Has an unusually low melting point
(b) Is the most electronegative
(c) Is extremely toxic
(d) Forms an acidic oxide

## The Group 4A Elements

19.50 Identify the group 4A element that best fits each of the following descriptions:
(a) Prefers the +2 oxidation state
(b) Forms the strongest $\pi$ bonds
(c) Is the second most abundant element in the earth's crust
(d) Forms the most acidic oxide
19.51 Select the group 4A element that best fits each of the following descriptions:
(a) Forms the most basic oxide
(b) Is the least dense semimetal
(c) Is the second most abundant element in the human body
(d) Is the most electronegative
19.52 Describe the geometry of each of the following molecules or ions, and tell which hybrid orbitals are used by the central atom:
(a) $\mathrm{GeBr}_{4}$
(b) $\mathrm{CO}_{2}$
(c) $\mathrm{CO}_{3}{ }^{2-}$
(d) $\mathrm{Sn}(\mathrm{OH})_{6}{ }^{2-}$
19.53 What is the geometry of each of the following molecules or ions, and which hybrid orbitals are used by the central atom?
(a) $\mathrm{SiO}_{4}{ }^{4-}$
(b) $\mathrm{PF}_{6}{ }^{-}$
(c) $\mathrm{SnCl}_{2}$
(d) $\mathrm{N}_{2} \mathrm{O}$
19.54 List three properties of diamond, and account for them in terms of structure and bonding.
19.55 Describe the structure and bonding in graphite, and explain why graphite is a good lubricant and a good electrical conductor.
19.56 Give the name and formula of a compound in which carbon exhibits an oxidation state of:
(a) +4
(b) +2
(c) -4
19.57 Give an example of an ionic carbide. What is the oxidation state of carbon in this substance?
19.58 List three commercial uses for carbon dioxide, and relate each use to one of carbon dioxide's properties.
19.59 Why are CO and $\mathrm{CN}^{-}$so toxic to humans?
19.60 Describe the preparation of silicon from silica sand, and tell how silicon is purified for use in semiconductor devices. Write balanced equations for all reactions.
19.61 What minerals are the starting materials for preparation of the following?
(a) Silicon
(b) Tin
(c) Lead

Give the name and chemical formula for each mineral, and write a balanced equation for the preparation of each element.
19.62 Using the shorthand notation of Figure 19.5 (page 829), draw the structure of the silicate anion in:
(a) $\mathrm{K}_{4} \mathrm{SiO}_{4}$
(b) $\mathrm{Ag}_{10} \mathrm{Si}_{4} \mathrm{O}_{13}$

What is the relationship between the charge on the anion and the number of terminal O atoms?
19.63 Using the shorthand notation of Figure 19.5 (page 829), draw the structure of the cyclic silicate anion in which four $\mathrm{SiO}_{4}$ tetrahedra share O atoms to form an eightmembered ring of alternating Si and O atoms. Give the formula and charge of the anion.
19.64 The silicate anion in the mineral kinoite is a chain of three $\mathrm{SiO}_{4}$ tetrahedra that share corners with adjacent tetrahedra. The mineral also contains $\mathrm{Ca}^{2+}$ ions, $\mathrm{Cu}^{2+}$ ions, and water molecules in a 1:1:1 ratio.
(a) Give the formula and charge of the silicate anion.
(b) Give the complete formula for the mineral.
19.65 Suggest a plausible structure for the silicate anion in each of the following minerals:
(a) Spodumene, $\mathrm{LiAlSi}_{2} \mathrm{O}_{6}$
(b) Wollastonite, $\mathrm{Ca}_{3} \mathrm{Si}_{3} \mathrm{O}_{9}$
(c) Thortveitite, $\mathrm{Sc}_{2} \mathrm{Si}_{2} \mathrm{O}_{7}$
(d) Albite, $\mathrm{NaAlSi}_{3} \mathrm{O}_{8}$

## The Group 5A Elements

19.66 Identify the group 5A element(s) that best fits each of the following descriptions:
(a) Makes up part of bones and teeth
(b) Forms stable salts containing $\mathrm{M}^{3+}$ ions
(c) Is the most abundant element in the atmosphere
(d) Forms a basic oxide
19.67 Identify the group 5A element that best fits each of the following descriptions:
(a) Forms strong $\pi$ bonds
(b) Is a metal
(c) Is the most abundant group 5A element in the earth's crust
(d) Forms oxides with the group 5A element in the $+1,+2$, and +4 oxidation states
19.68 Give the chemical formula for each of the following compounds, and indicate the oxidation state of the group 5A element:
(a) Nitrous oxide
(b) Hydrazine
(c) Calcium phosphide
(d) Phosphorous acid
(e) Arsenic acid
19.69 Give the chemical formula for each of the following compounds, and indicate the oxidation state of the group 5A element:
(a) Nitric oxide
(b) Nitrous acid
(c) Phosphine
(d) Tetraphosphorus decoxide
(e) Triphosphoric acid
19.70 Draw an electron-dot structure for $\mathrm{N}_{2}$, and explain why this molecule is so unreactive.
19.71 Draw electron-dot structures for:
(a) Nitrous oxide
(b) Nitric oxide
(c) Nitrogen dioxide

Predict the molecular geometry of each, and indicate which are expected to be paramagnetic.
19.72 Predict the geometry of each of the following molecules or ions, and tell which hybrid orbitals are used by the central atom:
(a) $\mathrm{NO}_{2}^{-}$
(b) $\mathrm{PH}_{3}$
(c) $\mathrm{PF}_{5}$
(d) $\mathrm{PCl}_{4}{ }^{+}$
19.73 Predict the geometry of each of the following molecules or ions, and tell which hybrid orbitals are used by the central atom:
(a) $\mathrm{PCl}_{6}{ }^{-}$
(b) $\mathrm{N}_{2} \mathrm{O}$
(c) $\mathrm{H}_{3} \mathrm{PO}_{3}$
(d) $\mathrm{NO}_{3}{ }^{-}$
19.74 Describe the structures of the white and red allotropes of phosphorus, and explain why white phosphorus is so reactive.
19.75 Draw the structure of each of the following molecules:
(a) Tetraphosphorus hexoxide
(b) Tetraphosphorus decoxide
(c) Phosphorous acid
(d) Orthophosphoric acid
(e) Polymetaphosphoric acid
19.76 Account for each of the following observations:
(a) Phosphorous acid is a diprotic acid.
(b) Nitrogen doesn't exist as a four-atom molecule like $\mathrm{P}_{4}$.
19.77 Account for each of the following observations:
(a) Nitric acid is a strong oxidizing agent, but phosphoric acid is not.
(b) Phosphorus, arsenic, and antimony form trichlorides and pentachlorides, but nitrogen forms only $\mathrm{NCl}_{3}$.
19.78 Write a balanced equation to account for each of the following observations:
(a) Nitric oxide turns brown when exposed to air.
(b) Nitric acid turns yellow-brown on standing.
(c) Silver dissolves in dilute $\mathrm{HNO}_{3}$, yielding a colorless gas.
(d) Hydrazine reduces iodine to $\mathrm{I}^{-}$and in the process is oxidized to $\mathrm{N}_{2}$ gas.
19.79 Describe the process used for the industrial production of the following chemicals:
(a) Nitrogen
(b) Ammonia
(c) Nitric acid
(d) Phosphoric acid

Write balanced equations for all chemical reactions.

## The Group 6A Elements

19.80 Identify the group 6A element that best fits each of the following descriptions:
(a) Is the most electronegative
(b) Is a semimetal
(c) Is radioactive
(d) Is the most abundant element in the earth's crust
19.81 Identify the group 6A element that best fits each of the following descriptions:
(a) Is a metal
(b) Is the most abundant element in the human body
(c) Is the strongest oxidizing agent
(d) Has the most negative electron affinity
19.82 Describe the structure of the sulfur molecules in:
(a) Rhombic sulfur
(b) Monoclinic sulfur
(c) Plastic sulfur
(d) Liquid sulfur above $160^{\circ} \mathrm{C}$
19.83 The viscosity of liquid sulfur increases sharply at about $160^{\circ} \mathrm{C}$ and then decreases again above $200^{\circ} \mathrm{C}$. Explain.
19.84 Give the name and formula of two compounds in which sulfur exhibits an oxidation state of:
(a) -2
(b) +4
(c) +6
19.85 What is the oxidation state of sulfur in each of the following compounds?
(a) HgS
(b) $\mathrm{Ca}\left(\mathrm{HSO}_{4}\right)_{2}$
(c) $\mathrm{H}_{2} \mathrm{SO}_{3}$
(d) $\mathrm{FeS}_{2}$
(e) $\mathrm{SF}_{4}$
19.86 Describe the contact process for the manufacture of sulfuric acid, and write balanced equations for all reactions.
19.87 Describe a convenient laboratory method for preparing each of the following compounds, and write balanced equations for all reactions:
(a) Sulfur dioxide
(b) Hydrogen sulfide
(c) Sodium hydrogen sulfate
19.88 Write a balanced net ionic equation for each of the following reactions:
(a) $\mathrm{Zn}(s)+$ dilute $\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \rightarrow$
(b) $\mathrm{BaSO}_{3}(s)+\mathrm{HCl}(a q) \rightarrow$
(c) $\mathrm{Cu}(s)+$ hot, conc $\mathrm{H}_{2} \mathrm{SO}_{4}(l) \rightarrow$
(d) $\mathrm{H}_{2} \mathrm{~S}(a q)+\mathrm{I}_{2}(a q) \rightarrow$
19.89 Write a balanced net ionic equation for each of the following reactions:
(a) $\mathrm{ZnS}(s)+\mathrm{HCl}(a q) \rightarrow$
(b) $\mathrm{H}_{2} \mathrm{~S}(a q)+\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}(a q) \rightarrow$
(c) $\mathrm{Fe}(s)+$ dilute $\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \rightarrow$
(d) $\mathrm{BaO}(s)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \rightarrow$
19.90 Account for each of the following observations:
(a) $\mathrm{H}_{2} \mathrm{SO}_{4}$ is a stronger acid than $\mathrm{H}_{2} \mathrm{SO}_{3}$.
(b) $\mathrm{SF}_{4}$ exists, but $\mathrm{OF}_{4}$ does not.
(c) $\mathrm{The}_{8}$ ring is nonplanar.
19.91 Account for each of the following observations:
(a) Oxygen is more electronegative than sulfur.
(b) Sulfur forms long $\mathrm{S}_{n}$ chains, but oxygen does not.
(c) The $\mathrm{SO}_{3}$ molecule is trigonal planar, but the $\mathrm{SO}_{3}{ }^{2-}$ ion is trigonal pyramidal.

## Halogen Oxoacids and Oxoacid Salts

19.92 Write the formula for each of the following compounds, and indicate the oxidation state of the halogen:
(a) Bromic acid
(b) Hypoiodous acid
(c) Sodium chlorite
(d) Potassium metaperiodate
19.93 Write the formula for each of the following compounds, and indicate the oxidation state of the halogen:
(a) Potassium hypobromite
(b) Paraperiodic acid
(c) Sodium bromate
(d) Chlorous acid
19.94 Name each of the following compounds:
(a) $\mathrm{HIO}_{3}$
(b) $\mathrm{HClO}_{2}$
(c) NaOBr
(d) $\mathrm{LiClO}_{4}$
19.95 Name each of the following compounds:
(a) $\mathrm{KClO}_{2}$
(b) $\mathrm{HIO}_{4}$
(c) HOBr
(d) $\mathrm{NaBrO}_{3}$
19.96 Write an electron-dot structure for each of the following molecules or ions, and predict the molecular geometry:
(a) $\mathrm{HIO}_{3}$
(b) $\mathrm{ClO}_{2}{ }^{-}$
(c) HOCl
(d) $\mathrm{IO}_{6}{ }^{5-}$
19.97 Write an electron-dot structure for each of the following molecules or ions, and predict the molecular geometry:
(a) $\mathrm{BrO}_{4}^{-}$
(b) $\mathrm{ClO}_{3}{ }^{-}$
(c) $\mathrm{HIO}_{4}$
(d) HOBr
19.98 Explain why acid strength increases in the order $\mathrm{HClO}<\mathrm{HClO}_{2}<\mathrm{HClO}_{3}<\mathrm{HClO}_{4}$.
19.99 Explain why acid strength increases in the order $\mathrm{HIO}<\mathrm{HBrO}<\mathrm{HClO}$.
19.100 Write a balanced net ionic equation for each of the following reactions:
(a) $\mathrm{Br}_{2}(l)+$ cold $\mathrm{NaOH}(a q) \rightarrow$
(b) $\mathrm{Cl}_{2}(g)+$ cold $\mathrm{H}_{2} \mathrm{O}(l) \rightarrow$
(c) $\mathrm{Cl}_{2}(g)+\operatorname{hot} \mathrm{NaOH}(a q) \rightarrow$
19.101 Write a balanced equation for the reaction of potassium chlorate and sucrose. The products are $\mathrm{KCl}(s)$, $\mathrm{CO}_{2}(g)$, and $\mathrm{H}_{2} \mathrm{O}(g)$.

## General Problems

19.102 What is the chemical formula for the most important mineral sources of each of the following elements?
(a) B
(b) P
(c) S
19.103 What are the principal uses of the following industrial chemicals?
(a) $\mathrm{H}_{2} \mathrm{SO}_{4}$
(b) $\mathrm{N}_{2}$
(c) $\mathrm{NH}_{3}$
(d) $\mathrm{HNO}_{3}$
(e) $\mathrm{H}_{3} \mathrm{PO}_{4}$
19.104 Which compound in each of the following pairs has the higher melting point?
(a) LiCl or $\mathrm{PCl}_{3}$
(b) $\mathrm{CO}_{2}$ or $\mathrm{SiO}_{2}$
(c) $\mathrm{P}_{4} \mathrm{O}_{10}$ or $\mathrm{NO}_{2}$
19.105 Which element in each of the following pairs is the better electrical conductor?
(a) B or Ga
(b) In or S
(c) Pb or P
19.106 The structures of the various phosphate and silicate anions have many similarities. List some.
19.107 Compare and contrast the properties of ammonia and phosphine.
19.108 How many of the four most abundant elements in the earth's crust and in the human body can you identify without consulting Figure 19.1?
19.109 Identify as many of the 10 most important industrial chemicals as you can without consulting Table 19.1.
19.110 Which of the group 4A elements have allotropes with the diamond structure? Which have metallic allotropes? How does the variation in the structure of the group 4A elements illustrate how metallic character varies down a periodic group?
19.111 Write a balanced chemical equation for a laboratory preparation of each of the following compounds:
(a) $\mathrm{NH}_{3}$
(b) $\mathrm{CO}_{2}$
(c) $\mathrm{B}_{2} \mathrm{H}_{6}$ (diborane)
(d) $\mathrm{C}_{2} \mathrm{H}_{2}$ (acetylene)
(e) $\mathrm{N}_{2} \mathrm{O}$
(f) $\mathrm{NO}_{2}$
19.112 Write balanced equations for the reactions of (a) $\mathrm{H}_{3} \mathrm{PO}_{4}$ and (b) $\mathrm{B}(\mathrm{OH})_{3}$ with water. Classify each acid as a Brønsted-Lowry acid or a Lewis acid.
19.113 What sulfur-containing compound is present in acid rain, and how is it formed by the burning of sulfurcontaining fossil fuels?
19.114 Account for each of the following observations:
(a) Diamond is extremely hard and high melting, whereas graphite is very soft and high melting.
(b) Chlorine does not form a perhalic acid, $\mathrm{H}_{5} \mathrm{ClO}_{6}$.
19.115 Give one example from main-group chemistry that illustrates each of the following descriptions:
(a) Covalent network solid
(b) Disproportionation reaction
(c) Paramagnetic oxide
(d) Polar molecule that violates the octet rule
(e) Lewis acid
(f) Amphoteric oxide
(g) Semiconductor
(h) Strong oxidizing agent
(i) Allotropes
19.116 Could the strain in the $\mathrm{P}_{4}$ molecule be reduced by using $s p^{3}$ hybrid orbitals in bonding instead of pure $p$ orbitals? Explain.
19.117 Carbon is an essential element in the molecules on which life is based. Would silicon be equally satisfactory? Explain.

## Multi-Concept Problems

19.118 An important physiological reaction of nitric oxide $(\mathrm{NO})$ is its interaction with the superoxide ion $\left(\mathrm{O}_{2}{ }^{-}\right)$ to form the peroxynitrite ion $\left(\mathrm{ONOO}^{-}\right)$.
(a) Write electron-dot structures for $\mathrm{NO}, \mathrm{O}_{2}{ }^{-}$, and $\mathrm{ONOO}^{-}$, and predict the $\mathrm{O}-\mathrm{N}-\mathrm{O}$ bond angle in $\mathrm{ONOO}^{-}$.
(b) The bond length in NO ( 115 pm ) is intermediate between the length of an NO triple bond and an NO double bond. Account for the bond length and the paramagnetism of NO using molecular orbital theory.
19.119 Consider phosphorous acid, a polyprotic acid with formula $\mathrm{H}_{3} \mathrm{PO}_{3}$.
(a) Draw two plausible structures for $\mathrm{H}_{3} \mathrm{PO}_{3}$. For each one, predict the shape of the pH titration curve for the titration of the $\mathrm{H}_{3} \mathrm{PO}_{3}\left(K_{\mathrm{a} 1}=\right.$ $1.0 \times 10^{-2}$ ) with aqueous NaOH .
(b) For the structure with the H atoms in two different environments, calculate the pH at the first and second equivalence points assuming that 30.00 mL of $0.1240 \mathrm{M} \mathrm{H}_{3} \mathrm{PO}_{3}\left(K_{\mathrm{a} 2}=2.6 \times 10^{-7}\right)$ is titrated with 0.1000 M NaOH .
19.120 We've said that the +1 oxidation state is uncommon for indium but is the most stable state for thallium. Verify this statement by calculating $E^{\circ}$ and $\Delta G^{\circ}$ (in kilojoules) for the disproportionation reaction
$3 \mathrm{M}^{+}(a q) \longrightarrow \mathrm{M}^{3+}(a q)+2 \mathrm{M}(s) \quad \mathrm{M}=\mathrm{In}$ or Tl
Is disproportionation a spontaneous reaction for $\mathrm{In}^{+}$ and/or $\mathrm{Tl}^{+}$? Standard reduction potentials for the relevant half-reactions are

$$
\begin{array}{ll}
\mathrm{In}^{3+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{In}^{+}(a q) & E^{\circ}=-0.44 \mathrm{~V} \\
\mathrm{In}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \operatorname{In}(s) & E^{\circ}=-0.14 \mathrm{~V} \\
\mathrm{Tl}^{3+}(a q)+2 \mathrm{e}^{-} \longrightarrow \mathrm{Tl}^{+}(a q) & E^{\circ}=+1.25 \mathrm{~V} \\
\mathrm{Tl}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Tl}(s) & E^{\circ}=-0.34 \mathrm{~V}
\end{array}
$$

19.121 Terrorists often use ammonium nitrate fertilizer as an ingredient in car bombs. When ammonium nitrate explodes, it decomposes to gaseous nitrogen, oxygen, and water vapor. The force of the explosion results from the sudden production of a huge volume of hot gas.
(a) Write a balanced equation for the reaction.
(b) What volume of gas (in liters) is produced from the explosion of $1.80 \mathrm{~m}^{3}$ of solid $\mathrm{NH}_{4} \mathrm{NO}_{3}$ ? Assume that the gas has a temperature of $500^{\circ} \mathrm{C}$ and a pressure of 1.00 atm . The density of $\mathrm{NH}_{4} \mathrm{NO}_{3}$ is $1.725 \mathrm{~g} / \mathrm{cm}^{3}$.
(c) Use the thermodynamic data in Appendix B to calculate the amount of heat (in kilojoules) released in the reaction.
19.122 It has been claimed that $\mathrm{NH}_{4} \mathrm{NO}_{3}$ fertilizer can be rendered unexplodable (see Problem 19.121) by adding compounds such as diammonium hydrogen phosphate, $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}$. Analysis of such a "desensitized" sample of $\mathrm{NH}_{4} \mathrm{NO}_{3}$ showed the mass \% nitrogen to be $33.81 \%$.
(a) Assuming that the mixture contains only $\mathrm{NH}_{4} \mathrm{NO}_{3}$ and $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}$, what is the mass percent of each of these two components?
(b) A 0.965 g sample of the mixture was dissolved in enough water to make 50.0 mL of solution. What is the pH of the solution? (Hint: The strongest base present is $\mathrm{HPO}_{4}{ }^{2-}$.)
19.123 A 5.00 g quantity of white phosphorus was burned in an excess of oxygen, and the product was dissolved in enough water to make 250.0 mL of solution.
(a) Write balanced equations for the reactions.
(b) What is the pH of the solution?
(c) When the solution was treated with an excess of aqueous $\mathrm{Ca}\left(\mathrm{NO}_{3}\right)_{2}$, a white precipitate was obtained. Write a balanced equation for the reaction, and calculate the mass of the precipitate in grams.
(d) The precipitate in part (c) was removed, and the solution that remained was treated with an excess of zinc, yielding a colorless gas that was collected at $20^{\circ} \mathrm{C}$ and 742 mm Hg . Identify the gas, and determine its volume.
19.124 A 500.0 mL sample of an equilibrium mixture of gaseous $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ at $25^{\circ} \mathrm{C}$ and 753 mm Hg pressure was allowed to react with enough water to make 250.0 mL of solution at $25^{\circ} \mathrm{C}$. You may assume that all the dissolved $\mathrm{N}_{2} \mathrm{O}_{4}$ is converted to $\mathrm{NO}_{2}$, which disproportionates in water, yielding a solution of nitrous acid and nitric acid. Assume further that the disproportionation reaction goes to completion and that none of the nitrous acid disproportionates. The equilibrium constant $K_{\mathrm{p}}$ for the reaction $\mathrm{N}_{2} \mathrm{O}_{4}(g) \rightleftharpoons$ $2 \mathrm{NO}_{2}(g)$ is 0.113 at $25^{\circ} \mathrm{C}$. $K_{\mathrm{a}}$ for $\mathrm{HNO}_{2}$ is $4.5 \times 10^{-4}$ at $25^{\circ} \mathrm{C}$.
(a) Write a balanced equation for the disproportionation reaction.
(b) What is the molar concentration of $\mathrm{NO}_{2}{ }^{-}$and the pH of the solution?
(c) What is the osmotic pressure of the solution in atmospheres?
(d) How many grams of lime ( CaO ) would be needed to neutralize the solution?

## eMedia Problems

19.125 Use the Interactive Periodic Table in eChapter 19.2 to answer the following questions:
(a) What are the trends in electronegativity and atomic radius as you move across the second row of the periodic table? To what do you attribute this trend?
(b) How does the atomic radius of the second-row elements compare to the heavier elements in the same groups? How does the electronegativity compare?
19.126 Look at the 3D models of $\mathrm{BF}_{3}$ and $\mathrm{B}_{2} \mathrm{H}_{6}$ in eChapter 19.4.
(a) Draw the electron-dot structure of $\mathrm{BF}_{3}$. How is this molecule an exception to the octet rule? How would you expect this to affect the reactivity of $\mathrm{BF}_{3}$ ?
(b) Draw the electron-dot structure of $\mathrm{B}_{2} \mathrm{H}_{6}$. Identify the number of electrons being shared in each of the bonds in the $\mathrm{B}_{2} \mathrm{H}_{6}$ molecule.
19.127 Diamond, graphite, and fullerene are elemental forms of carbon which have very different properties but which are all solids at room temperature. Looking at the 3D models of diamond, graphite, and fullerene in eChapter 19.6, what intermolecular forces do you expect to find in each?
19.128 Watch the Nitrogen Dioxide and Dinitrogen Tetroxide movie (eChapter 19.10).
(a) What is the equation corresponding to the equilibrium between the two species?
(b) Based on the information in the movie, which species would predominate at a high temperature? Which species would predominate at a low temperature?
19.129 The Physical Properties of the Halogens movie (eChapter 19.14) shows three of the halogens and indicates the physical state of each at room temperature. Given that all of the halogens are nonpolar, diatomic molecules, explain in terms of intermolecular forces how the halogens can exist in three different states at room temperature.

## Chapter

## Transition Elements and Coordination <br> Chemistry

The transition elements occupy the central part of the periodic table, bridging the gap between the active $s$-block metals of groups 1 A and 2 A on the left and the $p$-block metals, semimetals, and nonmetals of groups 3A-8A on the right (Figure 20.1). Because the $d$ subshells are being filled in this region of the periodic table, the transition elements are also called the $d$-block elements.

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The color of stained glass is due to transition metal oxides.
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■ Interlude—Titanium: A High-Tech Metal

FIGURE 20.1 The transition elements ( $d$-block elements, shown in yellow) are located in the central region of the periodic table between the $s$-block and $p$-block maingroup elements. The two series of inner transition elements (f-block elements, shown in green) follow lanthanum and actinium.

Electron Configurations activity

| Main | roup |  |  |  |  |  |  |  |  |  |  |  |  | in | oup |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 18 |
| 1A |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 8A |
| 1 | 2 |  |  |  |  |  |  |  |  |  |  | 13 | 14 | 15 | 16 | 17 | 2 |
| H | 2A |  |  |  |  |  |  |  |  |  |  | 3A | 4A | 5A | 6A | 7A | He |
| 3 | 4 |  |  |  |  |  |  |  |  |  |  | 5 | 6 | 7 | 8 | 9 | 10 |
| Li | Be | $\Gamma$ |  |  | rans | ion- | etal | roup |  |  |  | B | C | N | O | F | Ne |
| 11 | 12 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| Na | Mg | 3B | 4B | 5B | 6B | 7B | $\Gamma$ | 8B | $\checkmark$ | 1B | 2B | Al | Si | P | S | Cl | Ar |
| 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 | 31 | 32 | 33 | 34 | 35 | 36 |
| K | Ca | Sc | Ti | V | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | Kr |
| 37 | 38 | 39 | 40 | 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 | 51 | 52 | 53 | 54 |
| Rb | Sr | Y | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I | Xe |
| 55 | 56 | 57 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 | 81 | 82 | 83 | 84 | 85 | 86 |
| Cs | Ba | La | Hf | Ta | W | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | Rn |
| 87 | 88 | 89 | 104 | 105 | 106 | 107 | 108 | 109 | 110 | 111 | 112 |  | 114 |  | 116 |  |  |
| Fr | Ra | Ac | Rf | Db | Sg | Bh | Hs | Mt |  |  |  |  |  |  |  |  |  |


| Lanthanides | 58 | 59 | 60 | 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ce | Pr | Nd | Pm | Sm | Eu | Gd | Tb | Dy | Но | Er | Tm | Yb | Lu |
| Actinides | 90 | 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 | 101 | 102 | 103 |
|  | Th | Pa | U | Np | Pu | Am | Cm | Bk | Cf | Es | Fm | Md | No | Lr |

Each $d$ subshell consists of five orbitals and can accommodate 10 electrons, so each transition series consists of 10 elements. The first series extends from scandium through zinc and includes many familiar metals, such as chromium, iron, and copper. The second series runs from yttrium through cadmium, and the third series runs from lanthanum through mercury. In addition, there is a fourth transition series made up of actinium through the recently discovered and as yet unnamed element 112 .

Tucked into the periodic table between lanthanum (atomic number 57) and hafnium (atomic number 72) are the lanthanides. In this series of 14 metallic elements, the seven $4 f$ orbitals are progressively filled, as shown in Figure 5.17 (page 185). Following actinium (atomic number 89) is a second series of 14 elements, the actinides, in which the $5 f$ subshell is progressively filled. The lanthanides and actinides together comprise the $f$-block elements, or inner transition elements.

The transition metals iron and copper have been known since antiquity and have played an important role in the development of civilization. Iron, the main constituent of steel, is still important as a structural material. Worldwide production of steel amounts to some 800 million tons per year. In newer technologies, other transition elements are useful. For example, the strong, lightweight metal titanium is a major component in modern jet aircraft. Transition metals are also used as heterogeneous catalysts in automobile catalytic converters and in the industrial synthesis of essential chemicals such as sulfuric acid, nitric acid, and ammonia.

The role of the transition elements in living systems is equally important. Iron is present in biomolecules such as hemoglobin, which transports oxygen from our lungs to other parts of the body. Cobalt is an essential component of vitamin $\mathrm{B}_{12}$. Nickel, copper, and zinc are vital constituents of many enzymes, the large protein molecules that catalyze biochemical reactions.

In this chapter, we'll look at the properties and chemical behavior of transition metal compounds, paying special attention to coordination compounds, in which a central metal ion (or atom) -usually a transition metal-is attached to a group of surrounding molecules or ions by coordinate covalent bonds (Section 7.5).

### 20.1 Electron Configurations

Look at the electron configurations of potassium and calcium, the s-block elements immediately preceding the first transition series. These atoms have $4 s$ valence electrons, but no $d$ electrons:

$$
\mathrm{K}(Z=19):[\mathrm{Ar}] 3 d^{0} 4 s^{1} \quad \mathrm{Ca}(Z=20):[\mathrm{Ar}] 3 d^{0} 4 s^{2}
$$

The filling of the $3 d$ subshell begins at atomic number 21 (scandium) and continues until the subshell is completely filled at atomic number 30 (zinc):

$$
\text { Sc }(Z=21):[\mathrm{Ar}] 3 d^{1} 4 s^{2} \longrightarrow \mathrm{Zn}(Z=30):[\mathrm{Ar}] 3 d^{10} 4 s^{2}
$$

(It's convenient to list the valence electrons in order of principal quantum number because the $4 s$ electrons are lost first in forming ions.)

The valence electrons are generally considered to be those in the outermost shell (Section 5.12) because they are the ones that are involved in chemical bonding. For transition elements, however, both the $(n-1) d$ and the $n s$ electrons are involved in bonding and are considered valence electrons.

The filling of the $3 d$ subshell generally proceeds according to Hund's rule (Section 5.12) with one electron adding to each of the five $3 d$ orbitals before a second electron adds to any one of them. There are just two exceptions to the expected regular filling pattern, chromium and copper:


V
Anomalous electron configurations frequently occur if the atom can attain half-filled or completely filled subshells.

Electron configurations depend on both orbital energies and electron-electron repulsions. Consequently, it's not always possible to predict configurations when two valence subshells have similar energies. It's often found, however, that exceptions from the expected orbital filling pattern result in either half-filled or completely filled subshells. In the case of chromium, for example, the $3 d$ and $4 s$ subshells have similar energies. It's evidently advantageous to shift one electron from the $4 s$ to the $3 d$ subshell, which decreases electron-electron repulsions and gives two halffilled subshells. Because each valence electron is in a separate orbital, the electron-electron repulsion that would otherwise occur between the two $4 s$ electrons in the expected configuration is eliminated. A similar shift of one electron from $4 s$ to $3 d$ in copper gives a completely filled $3 d$ subshell and a half-filled $4 s$ subshell.

For transition metal cations, the valence $s$ orbital is vacant, and all the valence electrons occupy the $d$ orbitals. Iron, for example, which forms $2+$ and $3+$ cations, has the following valence electron configurations:

VThere are no anomalous electron configurations for common transition metal cations. The $n s$ orbital is vacant, and the remaining valence electrons occupy $(n-1) d$ orbitals, where $n$ is the period.

When a neutral atom loses one or more electrons, the remaining electrons are less shielded, and the effective nuclear charge ( $Z_{\text {eff }}$ ) increases. Consequently, the remaining electrons are more strongly attracted to the nucleus, and their orbital energies decrease. It turns out that the $3 d$ orbitals experience a steeper drop in energy with increasing $Z_{\text {eff }}$ than does the $4 s$ orbital, making the $3 d$ orbitals in cations lower in energy than the $4 s$ orbital. As a result, all the valence electrons occupy the $3 d$ orbitals, and the $4 s$ orbital is vacant.

In neutral molecules and complex anions, the metal atom usually has a positive oxidation state. It therefore has a partial positive charge and a higher $Z_{\text {eff }}$ than that of the neutral atom. As a result, the $3 d$ orbitals are again lower in energy than the $4 s$ orbital, and so all the metal's valence electrons occupy the $d$ orbitals. The metal atom in both $\mathrm{VCl}_{4}$ and $\mathrm{MnO}_{4}{ }^{2-}$, for example, has the valence configuration $3 d^{1}$. Electron configurations and other properties for atoms and common ions of first-series transition elements are summarized in Table 20.1.

TABLE 20.1 Selected Properties of First-Series Transition Elements

| Group: | $\mathbf{3 B}$ | $\mathbf{4 B}$ | $\mathbf{5 B}$ | $\mathbf{6 B}$ | $\mathbf{7 B}$ |  | $\mathbf{8 B}$ |  | $\mathbf{1 B}$ | $\mathbf{2 B}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Element: | $\mathbf{S c}$ | $\mathbf{T i}$ | $\mathbf{V}$ | $\mathbf{C r}$ | $\mathbf{M n}$ | $\mathbf{F e}$ | $\mathbf{C o}$ | $\mathbf{N i}$ | $\mathbf{C u}$ | $\mathbf{Z n}$ |
| Valence electron <br> configuration |  |  |  |  |  |  |  |  |  |  |
| $\quad$ M atom |  |  |  |  |  |  |  |  |  |  |
| $\mathrm{M}^{2+}$ ion | $3 d^{1} 4 s^{2}$ | $3 d^{2} 4 s^{2}$ | $3 d^{3} 4 s^{2}$ | $3 d^{5} 4 s^{1}$ | $3 d^{5} 4 s^{2}$ | $3 d^{6} 4 s^{2}$ | $3 d^{7} 4 s^{2}$ | $3 d^{8} 4 s^{2}$ | $3 d^{10} 4 s^{1}$ | $3 d^{10} 4 s^{2}$ |
| $\mathrm{M}^{3+}$ ion |  | $3 d^{2}$ | $3 d^{3}$ | $3 d^{4}$ | $3 d^{5}$ | $3 d^{6}$ | $3 d^{7}$ | $3 d^{8}$ | $3 d^{9}$ | $3 d^{10}$ |
| Elec. conductivity ${ }^{*}$ | $3 d^{0}$ | $3 d^{1}$ | $3 d^{2}$ | $3 d^{3}$ | $3 d^{4}$ | $3 d^{5}$ | $3 d^{6}$ |  |  |  |
| Melting point $\left({ }^{\circ} \mathrm{C}\right)$ | 3 | 4 | 8 | 11 | 1 | 17 | 24 | 24 | 96 | 27 |
| Boiling point $\left({ }^{\circ} \mathrm{C}\right)$ | 1541 | 1668 | 1910 | 1907 | 1246 | 1538 | 1495 | 1455 | 1085 | 420 |
| Density $\left(\mathrm{g} / \mathrm{cm}^{3}\right)$ | 2836 | 3287 | 3407 | 2671 | 2061 | 2861 | 2927 | 2913 | 2562 | 907 |
| Atomic radius $(\mathrm{pm})$ | 2.99 | 4.51 | 6.0 | 7.15 | 7.3 | 7.87 | 8.86 | 8.90 | 8.96 | 7.14 |
| $E_{\mathrm{i}}(\mathrm{kJ} / \mathrm{mol})^{\dagger}$ | 162 | 147 | 134 | 128 | 127 | 126 | 125 | 124 | 128 | 134 |
| First |  |  |  |  |  |  |  |  |  |  |
| Second | 631 | 658 | 650 | 653 | 717 | 759 | 758 | 737 | 745 | 906 |
| Third | 1235 | 1310 | 1414 | 1592 | 1509 | 1561 | 1646 | 1753 | 1958 | 1733 |

[^22]Transition elements are placed in groups of the periodic table designated 1B-8B because their valence electron configurations are similar to those of analogous elements in the main groups 1A-8A. Thus, copper in group 1B ([Ar] $\left.3 d^{10} 4 s^{1}\right)$ and zinc in group 2B $\left([\operatorname{Ar}] 3 d^{10} 4 s^{2}\right)$ have valence electron configurations similar to those of potassium in group $1 \mathrm{~A}\left([\mathrm{Ar}] 4 s^{1}\right)$ and calcium in group $2 \mathrm{~A}\left([\mathrm{Ar}] 4 s^{2}\right)$. Similarly, scandium in group 3B $\left([\operatorname{Ar}] 3 d^{1} 4 s^{2}\right)$ through iron in group $8 \mathrm{~B}\left([\mathrm{Ar}] 3 d^{6} 4 s^{2}\right)$ have the same number of valence electrons as the $p$-block elements aluminum in group 3A ( $[\mathrm{Ne}] 3 s^{2} 3 p^{1}$ ) through argon in group $8 \mathrm{~A}\left([\mathrm{Ne}] 3 s^{2} 3 p^{6}\right)$. Cobalt ([Ar] $3 d^{7} 4 s^{2}$ ) and nickel ([Ar] $3 d^{8} 4 s^{2}$ ) are also assigned to group 8B although there are no main-group elements with 9 or 10 valence electrons.

## Worked Example 20.1

Give the electron configuration of the metal in each of the following atoms or ions:
(a) Ni
(b) $\mathrm{Cr}^{3+}$
(c) $\mathrm{FeO}_{4}{ }^{2-}$ (ferrate ion)

## Strategy

In neutral atoms of the first transition series, the $4 s$ orbital is usually filled with 2 electrons, and the remaining electrons occupy the $3 d$ orbitals. In transition metal ions, all the valence electrons occupy the $d$ orbitals. For polyatomic ions, first determine the oxidation number of the transition metal, and then assign the valence electrons to the $d$ orbitals as you would if the metal were a simple ion.

## Solution

(a) Nickel $(Z=28)$ has a total of 28 electrons, including the argon core of 18 . Two of the valence electrons occupy the $4 s$ orbital, and the remaining eight are assigned to the $3 d$ orbitals. The electron configuration is therefore [Ar] $3 d^{8} 4 s^{2}$.
(b) A neutral Cr atom $(Z=24)$ has a total of 24 electrons; $\mathrm{Cr}^{3+}$ ion has $24-3=21$ electrons. Because all the valence electrons occupy the $3 d$ orbitals, the electron configuration of $\mathrm{Cr}^{3+}$ is [Ar] $3 d^{3}$.
(c) The oxidation number of each of the four oxygens in $\mathrm{FeO}_{4}{ }^{2-}$ is -2 , and the overall charge on the oxoanion is -2 , so the oxidation number of the iron must be +6 . An iron(VI) atom has a total of 20 electrons, 6 less than a neutral iron atom ( $Z=26$ ). Because the valence electrons occupy the $3 d$ orbitals, the electron configuration of $\mathrm{Fe}(\mathrm{VI})$ is $[\mathrm{Ar}] 3 d^{2}$.

PROBLEM 20.1 Give the electron configuration of the metal in each of the following:
(a) V
(b) $\mathrm{Co}^{2+}$
(c) $\mathrm{MnO}_{2}$
(d) $\mathrm{CuCl}_{4}{ }^{2-}$

KEY CONCEPT PROBLEM 20.2 On the periodic table below, locate the transition metal atom or ion with the following electron configurations. Identify each atom or ion.
(a) An atom: $[\mathrm{Ar}] 3 \mathrm{~d}^{5} 4 \mathrm{~s}^{2}$
(b) A $2+$ ion: $[\mathrm{Ar}] 3 \mathrm{~d}^{8}$
(c) An atom: $[\mathrm{Kr}] 4 \mathrm{~d}^{10} 5 \mathrm{~s}^{1}$
(d) A 3+ ion: $[\mathrm{Kr}] 4 \mathrm{~d}^{3}$


## 20.2 | Properties of Transition Elements

Let's look at some trends in the properties of the transition elements shown in Table 20.1 and try to understand them in terms of electron configurations.

## Metallic Properties

All the transition elements are metals. Like the metals of groups 1A and 2A, the transition metals are malleable, ductile, lustrous, and good conductors of heat and electricity. Silver has the highest electrical conductivity of any element at room temperature, with copper a close second. The transition metals are harder, have higher melting and boiling points, and are more dense than the group 1 A and 2 A metals, largely because the sharing of $d$, as well as $s$, electrons results in stronger bonding.

From left to right across the first transition series, melting points increase from $1541^{\circ} \mathrm{C}$ for Sc to a maximum of $1910^{\circ} \mathrm{C}$ for V in group 5 B , then decrease to $420^{\circ} \mathrm{C}$ for Zn (Table 20.1, Figure 20.2). The second- and third-series elements exhibit a


A Native copper.
Interactive Periodic
Table

$\nabla$
Within any transition series, the melting points increase for the first three or four elements, then show a general decrease.


A FIGURE 20.2 Relative melting points of the transition elements. Melting points reach a maximum value in the middle of each series.

Peter P. Edwards and M. J. Sienko, "On the Occurrence of Metallic Character in the Periodic Table of the Elements," J. Chem. Educ., Vol. 60, 1983, 691-696.

Frank Rioux, "An Ionic Model for Metallic Bonding," J. Chem. Educ., Vol. 62, 1985, 383-384.

FIGURE 20.3 Atomic radii (in pm ) of the transition elements. The radii decrease with increasing atomic number and then increase again toward the end of each transition series. Note that the second- and third-series transition elements have nearly identical radii.
similar maximum in melting point, but at group $6 \mathrm{~B}: 2623^{\circ} \mathrm{C}$ for Mo and $3422^{\circ} \mathrm{C}$ for W , the metal with the highest melting point. The melting points increase as the number of unpaired $d$ electrons available for bonding increases and then decrease as the $d$ electrons pair up and become less available for bonding. Zinc $\left(3 d^{10} 4 s^{2}\right)$, in which all the $d$ and $s$ electrons are paired, has a relatively low melting point $\left(420^{\circ} \mathrm{C}\right)$ and mercury $\left(4 f^{14} 5 d^{10} 6 s^{2}\right)$ is a liquid at room temperature $\left(\mathrm{mp}-39^{\circ} \mathrm{C}\right)$. We'll look at bonding in metals in more detail in Section 21.4.

## Atomic Radii and Densities

Atomic radii are given in Figure 20.3. From left to right across a transition series, the atomic radii decrease, at first markedly and then more gradually after group $6 B$. Toward the end of each series, the radii increase again. The decrease in radii with increasing atomic number occurs because the added $d$ electrons only partially shield the added nuclear charge (Section 5.15). As a result, the effective nuclear charge $Z_{\text {eff }}$ increases. With increasing $Z_{\text {eff }}$, the electrons are more strongly attracted to the nucleus, and atomic size decreases. The upturn in radii toward the end of each series is probably due to more effective shielding and to increasing electron-electron repulsion as double occupation of the $d$ orbitals is completed. In contrast to the large variation in radii for main-group elements, all transition metal atoms have quite similar radii, which accounts for their ability to blend together in forming alloys such as brass (mostly copper and zinc).


The atomic radii of the second- and third-series transition elements from group 4 B on are nearly identical, though we would expect an increase in size on adding an entire principal quantum shell of electrons. The small sizes of the thirdseries atoms are associated with what is called the lanthanide contraction, the general decrease in atomic radii of the $f$-block lanthanide elements between the second and third transition series (Figure 20.4).

The lanthanide contraction is due to the increase in effective nuclear charge with increasing atomic number as the $4 f$ subshell is filled. By the end of the lanthanides, the size decrease due to a larger $Z_{\text {eff }}$ almost exactly compensates for the expected size increase due to an added quantum shell of electrons. Consequently, atoms of the third transition series have radii very similar to those of the second transition series.

FIGURE 20.4 Atomic radii (in pm ) of the lanthanide elements. The radii generally decrease with increasing atomic number.


The densities of the transition metals are inversely related to their atomic radii (Figure 20.5). The densities initially increase from left to right across each transition series and then decrease toward the end of each series. Because the secondand third-series elements have nearly the same atomic volume, the much heavier third-series elements have unusually high densities: $22.6 \mathrm{~g} / \mathrm{cm}^{3}$ for osmium and $22.5 \mathrm{~g} / \mathrm{cm}^{3}$ for iridium, the most dense elements.

0
Due to the lanthanide contraction, second- and third-series transition elements have similar atomic radii, so the heavier third-series elements are much denser than the lighter secondseries elements.


## Ionization Energies and Oxidation Potentials

Ionization energies generally increase from left to right across a transition series, though there are some irregularities, as indicated in Table 20.1 for the atoms of the first transition series. The general trend correlates with an increase in effective nuclear charge and a decrease in atomic radius.

Table 20.2 lists standard potentials $E^{\circ}$ for oxidation of first-series transition metals. Note that these potentials are the negative of the corresponding standard reduction potentials (Table 18.1, page 775). Except for copper, all the $E^{\circ}$ values are positive, which means that the solid metal is oxidized to its aqueous cation more readily than $\mathrm{H}_{2}$ gas is oxidized to $\mathrm{H}^{+}(a q)$.

$$
\begin{array}{lll}
\mathrm{M}(s) \longrightarrow \mathrm{M}^{2+}(a q)+2 \mathrm{e}^{-} & E^{\circ}>0 \mathrm{~V} \\
\mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{H}^{+}(a q)+2 \mathrm{e}^{-} & E^{\circ}=0 \mathrm{~V} &
\end{array}
$$

TABLE 20.2 Standard Potentials for Oxidation of First-Series Transition Metals

| Oxidation Half-Reaction | $\boldsymbol{E}^{\circ}(\mathbf{V})$ | Oxidation Half-Reaction | $\boldsymbol{E}^{\circ}(\mathbf{V})$ |
| :--- | :--- | :--- | ---: |
| $\mathrm{Sc}(s) \rightarrow \mathrm{Sc}^{3+}(a q)+3 \mathrm{e}^{-}$ | 2.08 | $\mathrm{Fe}(s) \rightarrow \mathrm{Fe}^{2+}(a q)+2 \mathrm{e}^{-}$ | 0.45 |
| $\mathrm{Ti}(s) \rightarrow \mathrm{Ti}^{2+}(a q)+2 \mathrm{e}^{-}$ | 1.63 | $\mathrm{Co}(s) \rightarrow \mathrm{Co}^{2+}(a q)+2 \mathrm{e}^{-}$ | 0.28 |
| $\mathrm{~V}(s) \rightarrow \mathrm{V}^{2+}(a q)+2 \mathrm{e}^{-}$ | 1.18 | $\mathrm{Ni}(s) \rightarrow \mathrm{Ni}^{2+}(a q)+2 \mathrm{e}^{-}$ | 0.26 |
| $\mathrm{Cr}(s) \rightarrow \mathrm{Cr}^{2+}(a q)+2 \mathrm{e}^{-}$ | 0.91 | $\mathrm{Cu}(s) \rightarrow \mathrm{Cu}^{2+}(a q)+2 \mathrm{e}^{-}$ | -0.34 |
| $\mathrm{Mn}(s) \rightarrow \mathrm{Mn}^{2+}(a q)+2 \mathrm{e}^{-}$ | 1.18 | $\mathrm{Zn}(s) \rightarrow \mathrm{Zn}^{2+}(a q)+2 \mathrm{e}^{-}$ | 0.76 |

In other words, the first-series metals, except for copper, are stronger reducing agents than $\mathrm{H}_{2}$ gas and can therefore be oxidized by the $\mathrm{H}^{+}$ion in acids like HCl that lack an oxidizing anion:

$$
\mathrm{M}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{M}^{2+}(a q)+\mathrm{H}_{2}(g) \quad E^{\circ}>0 \mathrm{~V}(\text { except for } \mathrm{M}=\mathrm{Cu})
$$

Oxidation of copper requires a stronger oxidizing agent, such as $\mathrm{HNO}_{3}$.
The standard potential for the oxidation of a metal is a composite property that depends on $\Delta G^{\circ}$ for the sublimation of the metal, the ionization energies of the metal atom, and $\Delta G^{\circ}$ for the hydration of the metal ion:

$$
\mathrm{M}(s) \xrightarrow{\Delta G_{\mathrm{subl}}^{\circ}} \mathrm{M}(g) \xrightarrow{E_{\mathrm{i}}\left(-2 \mathrm{e}^{-}\right)} \mathrm{M}^{2+}(g) \xrightarrow{\Delta G_{\mathrm{hydr}}^{\circ}} \mathrm{M}^{2+}(a q)
$$

A FIGURE 20.5 Relative densities of the transition metals. Density initially increases across each series and then decreases.

Of the first-series metals, only copper cannot be oxidized by hydrochloric acid.

Nevertheless, the general trend in the $E^{\circ}$ values shown in Table 20.2 correlates with the general trend in the ionization energies in Table 20.1. The ease of oxidation of the metal decreases as the ionization energies increase across the transition series from Sc to Zn . (Only Mn and Zn deviate from the trend of decreasing $E^{\circ}$ values.) Thus, the so-called early transition metals, those on the left side of the $d$ block (Sc through Mn), are oxidized most easily and are the strongest reducing agents.

### 20.3 Oxidation States of Transition Elements

The transition elements differ from most main-group metals in that they exhibit a variety of oxidation states. Sodium, magnesium, and aluminum, for example, have a single oxidation state equal to their periodic group number $\left(\mathrm{Na}^{+}, \mathrm{Mg}^{2+}\right.$, and $\mathrm{Al}^{3+}$ ), but the transition elements frequently have oxidation states less than their group number. For example, manganese in group 7B shows oxidation states of +2 in $\mathrm{Mn}^{2+}(a q),+3$ in $\mathrm{Mn}(\mathrm{OH})_{3}(s),+4$ in $\mathrm{MnO}_{2}(s),+6$ in $\mathrm{MnO}_{4}{ }^{2-}(a q)$ (manganate ion), and +7 in $\mathrm{MnO}_{4}{ }^{-}(a q)$ (permanganate ion). Figure 20.6 summarizes the common oxidation states for elements of the first transition series, with the most frequently encountered ones indicated in red.

Manganese has different oxidation states and different colors in $\mathrm{Mn}^{2+}(a q), \mathrm{Mn}(\mathrm{OH})_{3}(s)$, $\mathrm{MnO}_{2}(s), \mathrm{MnO}_{4}{ }^{2-}(a q)$, and $\mathrm{MnO}_{4}^{-}(a q)$ (from left to right).

## \%



FIGURE 20.6 Common oxidation states for first-series transition elements. The states encountered most frequently are shown in red. The highest oxidation state for the group 3B-7B metals is their periodic group number, but the group 8B transition metals have a maximum oxidation state less than their group number. Most transition elements have more than one common oxidation state.


$\square$All first-series transition metals except scandium form $2+$ ions.

All the first-series transition elements except scandium form a $2+$ cation, corresponding to loss of the two $4 s$ valence electrons. Because the $3 d$ and $4 s$ orbitals have similar energies, loss of a $3 d$ electron is also possible, yielding $3+$ cations such as $\mathrm{V}^{3+}(a q), \mathrm{Cr}^{3+}(a q)$, and $\mathrm{Fe}^{3+}(a q)$. Additional energy is required to remove the third electron, but this is more than compensated for by the larger (more negative) $\Delta G^{\circ}$ of hydration of the more highly charged $3+$ cation. Still higher oxidation states result from loss or sharing of additional $d$ electrons. In their highest oxidation states, the transition elements are combined with the most electronegative elements ( F and O ): for example, $\mathrm{VF}_{5}(l)$ and $\mathrm{V}_{2} \mathrm{O}_{5}(s)$ for vanadium in group 5B; $\mathrm{CrO}_{4}{ }^{2-}$ (chromate ion) and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ (dichromate ion) for chromium in group 6B; $\mathrm{MnO}_{4}{ }^{-}$for manganese in group 7B.

Note in Figure 20.6 that the highest oxidation state for the group 3B-7B metals is the group number, corresponding to loss or sharing of all the valence $s$ and $d$ electrons. For the group 8 B transition metals, though, loss or sharing of all the valence electrons is energetically prohibitive because of the increasing value of $Z_{\text {eff. }}$ Consequently, only lower oxidation states are accessible for these transition metals-for example, +6 in $\mathrm{FeO}_{4}{ }^{2-}$ and +3 in $\mathrm{Co}^{3+}$. Even these species have a great tendency to be reduced to still lower oxidation states. For example, the aqueous $\mathrm{Co}^{3+}$ ion oxidizes water to $\mathrm{O}_{2}$ gas and is thereby reduced to $\mathrm{Co}^{2+}$ :

$$
4 \mathrm{Co}^{3+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 4 \mathrm{Co}^{2+}(a q)+\mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q) \quad E^{\circ}=+0.58 \mathrm{~V}
$$

In general, ions that have the transition metal in a high oxidation state tend to be good oxidizing agents-for example, $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}, \mathrm{MnO}_{4}{ }^{-}$, and $\mathrm{FeO}_{4}{ }^{2-}$. Conversely, early transition metal ions with the metal in a low oxidation state are good reducing agents-for example, $\mathrm{V}^{2+}$ and $\mathrm{Cr}^{2+}$. Divalent ions of the later transition metals on the right side of the $d$ block, such as $\mathrm{Co}^{2+}, \mathrm{Ni}^{2+}, \mathrm{Cu}^{2+}$, and $\mathrm{Zn}^{2+}$, are poor reducing agents because of the larger value of $Z_{\text {eff }}$. In fact, zinc has only one oxidation state ( +2 ).

The elements of the second and third transition series also exhibit a variety of oxidation states. In general, the stability of the higher oxidation states increases down a periodic group. In group 8 B , for example, the oxide of iron with the highest oxidation state is iron(III) oxide, $\mathrm{Fe}_{2} \mathrm{O}_{3}$. Ruthenium and osmium, though, form volatile tetroxides, $\mathrm{RuO}_{4}$ and $\mathrm{OsO}_{4}$, in which the metals have an oxidation state of +8 .

KEY CONCEPT PROBLEM 20.3 How does the effective nuclear charge, $Z_{\text {eff }}$, vary from left to right across the first transition series?

| Sc | Ti | V | Cr | Mn | Fe | Co | Ni | Cu | Zn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

Based on the variation in $Z_{\text {eff }}$,
(a) Which $\mathrm{M}^{2+}$ ion $(\mathrm{M}=\mathrm{Ti}-\mathrm{Zn})$ should be the strongest reducing agent? Which should be the weakest?
(b) Which oxoanion $\left(\mathrm{VO}_{4}{ }^{3-}, \mathrm{CrO}_{4}{ }^{2-}, \mathrm{MnO}_{4}{ }^{2-}\right.$, or $\left.\mathrm{FeO}_{4}{ }^{2-}\right)$ should be the strongest oxidizing agent? Which should be the weakest?

### 20.4 Chemistry of Selected Transition Elements

Experimental work in transition metal chemistry is particularly enjoyable because most transition metal compounds have brilliant colors. In this section, we'll look at the chemistry of some representative elements commonly encountered in the laboratory.

## Chromium

Chromium, which gets its name from the Greek word for color (chroma), is obtained from the ore chromite, a mixed metal oxide with the formula $\mathrm{FeO} \cdot \mathrm{Cr}_{2} \mathrm{O}_{3}$, or $\mathrm{FeCr}_{2} \mathrm{O}_{4}$. Reduction of chromite with carbon gives the alloy ferrochrome, which is used to make stainless steel, a hard, corrosion-resistant steel that contains up to $30 \%$ chromium.

$$
\mathrm{FeCr}_{2} \mathrm{O}_{4}(\mathrm{~s})+4 \mathrm{C}(\mathrm{~s}) \longrightarrow \underbrace{\mathrm{Fe}(\mathrm{~s})+2 \mathrm{Cr}(\mathrm{~s})}_{\text {Ferrochrome }}+4 \mathrm{CO}(\mathrm{~g})
$$

Pure chromium is obtained by reducing chromium(III) oxide with aluminum:

$$
\mathrm{Cr}_{2} \mathrm{O}_{3}(s)+2 \mathrm{Al}(s) \longrightarrow 2 \mathrm{Cr}(s)+\mathrm{Al}_{2} \mathrm{O}_{3}(s)
$$

$v$Electrons generally become more difficult to remove from left to right across a transition series. The first elements in a transition series tend to occur in relatively high oxidation states, and later elements tend to occur in low oxidation states.


0
Simple transition-metal ions and complex ions are soluble in water, but uncharged transition-metal compounds are often insoluble in water.

In addition to its use in making steels, chromium is widely used to electroplate metallic objects with an attractive, protective coating (Section 18.12). Chromium is hard and lustrous, takes a high polish, and resists corrosion because an invisible, microscopic film of chromium(III) oxide shields the surface from further oxidation.

The aqueous solution chemistry of chromium can be systematized according to its oxidation states and the species that exist under acidic and basic conditions (Table 20.3). The common oxidation states are $+2,+3$, and +6 , with the +3 state the most stable.

TABLE 20.3 Chromium Species in Common Oxidation States



A This sculpture, Herakles in Ithaka by Jason Seley, was made from chromium-plated automobile bumpers. Jason Seley (1919-1983), Herakles in Ithaka I, 1980-81. Sculpture, welded steel, 342.9 cm . Gift of the Artist, the Herbert F. Johnson Museum of Art, Cornell University. Photo by Robert Barker, Director, Cornell University Photography

Chromium metal reacts with aqueous acids in the absence of oxygen to give $\mathrm{Cr}^{2+}(a q)$, the beautiful blue chromium(II) (chromous) ion, in which $\mathrm{Cr}^{2+}$ is bound to six water molecules, $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}$ (Figure 20.7a):

$$
\mathrm{Cr}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Cr}^{2+}(a q)+\mathrm{H}_{2}(g) \quad E^{\circ}=+0.91 \mathrm{~V}
$$

In air, the reaction of chromium metal with acids yields chromium(III) because chromium(II) is rapidly oxidized by atmospheric oxygen:

$$
4 \mathrm{Cr}^{2+}(a q)+\mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q) \longrightarrow 4 \mathrm{Cr}^{3+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l) \quad E^{\circ}=+1.64 \mathrm{~V}
$$

Although the $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ ion is violet, chromium(III) solutions are often green because anions replace some of the bound water molecules to give green complex ions such as $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{5} \mathrm{Cl}^{2+}$ and $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{4} \mathrm{Cl}_{2}{ }^{+}$(Figure 20.7b).

FIGURE 20.7 (a) Reaction of chromium metal with $6 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ in the absence of air gives bubbles of $\mathrm{H}_{2}$ gas and a solution containing the blue chromium(II) ion. (b) Reaction of chromium metal with 6 M HCl in the presence of air yields a green solution containing chromium(III) species.


(a)

In basic solution, chromium(III) precipitates as chromium(III) hydroxide, a pale green solid that dissolves both in acid and in excess base (Figure 20.8):

In acid: $\quad \mathrm{Cr}(\mathrm{OH})_{3}(s)+3 \mathrm{H}_{3} \mathrm{O}^{+}(a q) \rightleftharpoons \mathrm{Cr}^{3+}(a q)+6 \mathrm{H}_{2} \mathrm{O}(l)$
In excess base: $\mathrm{Cr}(\mathrm{OH})_{3}(s)+\mathrm{OH}^{-}(a q) \rightleftharpoons \mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}(a q)$
Recall from Section 16.12 that this behavior is typical of amphoteric metal hydroxides.


In contrast to the amphoteric $\mathrm{Cr}(\mathrm{OH})_{3}$, chromium(II) hydroxide is a typical basic hydroxide. It dissolves in acid, but not in excess base. Conversely, the chromium(VI) compound, $\mathrm{CrO}_{2}(\mathrm{OH})_{2}$, is a strong acid (chromic acid, $\mathrm{H}_{2} \mathrm{CrO}_{4}$ ). Recall from Section 15.15 that acid strength increases with increasing polarity of the $\mathrm{O}-\mathrm{H}$ bonds, which increases, in turn, with increasing oxidation number of the chromium atom.

| $\substack{+2 \\ \mathrm{Cr}(\mathrm{OH})_{2} \\ \text { Basic }}$ | +3 <br>  Increasing strength as a proton donor |
| :---: | :---: | :---: |

In the +6 oxidation state, the most important solution species are the yellow chromate ion $\left(\mathrm{CrO}_{4}{ }^{2-}\right)$ and the orange dichromate ion $\left(\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}\right)$. These ions are interconverted by the rapid equilibrium reaction

$$
2 \mathrm{CrO}_{4}{ }^{2-}(a q)+2 \mathrm{H}^{+}(a q) \rightleftharpoons \mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \quad K \approx 10^{14}
$$

Because the equilibrium constant is about $10^{14}, \mathrm{CrO}_{4}{ }^{2-}$ ions predominate in basic solutions and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ ions predominate in acidic solutions (Figure 20.9).

The $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ ion is a powerful oxidizing agent in acidic solution and is widely used as an oxidant in analytical chemistry.

$$
\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+14 \mathrm{H}^{+}(a q)+6 \mathrm{e}^{-} \longrightarrow 2 \mathrm{Cr}^{3+}(a q)+7 \mathrm{H}_{2} \mathrm{O}(l) \quad E^{\circ}=+1.33 \mathrm{~V}
$$

In basic solution, where $\mathrm{CrO}_{4}{ }^{2-}$ is the predominant species, chromium $(\mathrm{VI})$ is a much weaker oxidizing agent:
$\mathrm{CrO}_{4}{ }^{2-}(a q)+4 \mathrm{H}_{2} \mathrm{O}(l)+3 \mathrm{e}^{-} \longrightarrow \mathrm{Cr}(\mathrm{OH})_{3}(s)+5 \mathrm{OH}^{-}(a q) \quad E^{\circ}=-0.13 \mathrm{~V}$
Chromium(VI) compounds must be handled with care because they are highly toxic and are known to cause cancer.

4 FIGURE 20.8 (a) Slow addition of aqueous NaOH to a solution of the violet $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ ion gives a pale green precipitate of chromium(III) hydroxide, $\mathrm{Cr}(\mathrm{OH})_{3}$. (b) The $\mathrm{Cr}(\mathrm{OH})_{3}$ dissolves on addition of $\mathrm{H}_{2} \mathrm{SO}_{4}$, re-forming the $\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ ion. (c) $\mathrm{Cr}(\mathrm{OH})_{3}$ also dissolves on addition of excess NaOH , yielding the deep green chromite ion, $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}$.

$\sigma$
The higher the oxidation state of the central atom, the more acidic the hydroxo species.

d.J. M. Anderson, "Oxidation-Reduction in Blood Analysis: Demonstrating the Reaction in a Breathalyzer," J. Chem. Educ., Vol. 67, 1990, 263. The oxidation of a primary alcohol by the orange dichromate ion is shown to first form an aldehyde, then a carboxylic acid, and green chromium(III) ion. The use of this reaction, principles of spectrometry, and gas laws in a commercial device for measuring blood-alcohol content are discussed.


Chromate ion, $\mathrm{CrO}_{4}{ }^{2-}$


Dichromate ion, $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$

FIGURE 20.9 (a) An aqueous solution of sodium chromate $\left(\mathrm{Na}_{2} \mathrm{CrO}_{4}\right)$. (b) On addition of dilute sulfuric acid to the solution in (a), the yellow $\mathrm{CrO}_{4}{ }^{2-}$ ion is converted to the orange $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}$ ion.


A FIGURE 20.10 When dilute NaOH is added to a solution of iron(III) sulfate, $\mathrm{Fe}_{2}\left(\mathrm{SO}_{4}\right)_{3}$, a gelatinous, red-brown precipitate of $\mathrm{Fe}(\mathrm{OH})_{3}$ forms.

(a)

(b)

## Iron

Iron, the fourth most abundant element in the earth's crust ( $5.6 \%$ by mass), is immensely important both in human civilization and in living systems. Because iron is relatively soft and easily corroded, it is combined with carbon and other metals, such as vanadium, chromium, and manganese, to make alloys (steels) that are harder and less reactive than pure iron. Iron is obtained from its most important ores, hematite $\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)$ and magnetite $\left(\mathrm{Fe}_{3} \mathrm{O}_{4}\right)$, by reduction with coke in a blast furnace (see Section 21.3). In living systems, iron is an essential constituent of numerous biomolecules. The body of a healthy human adult contains about 4 g of iron, $65 \%$ of which is present in the oxygen-carrying protein hemoglobin (Chapter 13 Interlude).

The most common oxidation states of iron are +2 (ferrous) and +3 (ferric). When iron metal reacts in the absence of air with an acid such as HCl , which lacks an oxidizing anion, the product is the light green iron(II) ion, $\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}$ :

$$
\mathrm{Fe}(s)+2 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Fe}^{2+}(a q)+\mathrm{H}_{2}(g) \quad E^{\circ}=+0.45 \mathrm{~V}
$$

The oxidation stops at the iron(II) stage because the standard potential for oxidation of the iron(II) ion is negative:

$$
\mathrm{Fe}^{2+}(a q) \longrightarrow \mathrm{Fe}^{3+}(a q)+\mathrm{e}^{-} \quad E^{\circ}=-0.77 \mathrm{~V}
$$

In air, the iron(II) ion is slowly oxidized by atmospheric oxygen to the iron(III) ion, $\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{3+}$ :

$$
4 \mathrm{Fe}^{2+}(a q)+\mathrm{O}_{2}(g)+4 \mathrm{H}^{+}(a q) \longrightarrow 4 \mathrm{Fe}^{3+}(a q)+2 \mathrm{H}_{2} \mathrm{O}(l) \quad E^{\circ}=+0.46 \mathrm{~V}
$$

When iron is treated with an acid that has an oxidizing anion-for example, dilute nitric acid-the metal is oxidized directly to iron(III):
$\mathrm{Fe}(s)+\mathrm{NO}_{3}{ }^{-}(a q)+4 \mathrm{H}^{+}(a q) \longrightarrow \mathrm{Fe}^{3+}(a q)+\mathrm{NO}(g)+2 \mathrm{H}_{2} \mathrm{O}(l)$

$$
E^{\circ}=+1.00 \mathrm{~V}
$$

Addition of base to iron(III) solutions precipitates the gelatinous, red-brown hydrous oxide, $\mathrm{Fe}_{2} \mathrm{O}_{3} \cdot x \mathrm{H}_{2} \mathrm{O}$, usually written as $\mathrm{Fe}(\mathrm{OH})_{3}$ (Figure 20.10):

$$
\mathrm{Fe}^{3+}(a q)+3 \mathrm{OH}^{-}(a q) \longrightarrow \mathrm{Fe}(\mathrm{OH})_{3}(s)
$$

Because $\mathrm{Fe}(\mathrm{OH})_{3}$ is very insoluble $\left(K_{\mathrm{sp}}=2.6 \times 10^{-39}\right)$, it forms as soon as the pH rises above pH 2 . The red-brown rust stains that you've seen in sinks and bathtubs are due to air oxidation of $\mathrm{Fe}^{2+}(a q)$ followed by deposition of hydrous iron(III)
oxide. Unlike $\mathrm{Cr}(\mathrm{OH})_{3}, \mathrm{Fe}(\mathrm{OH})_{3}$ is not appreciably amphoteric. It dissolves in acid, but not in excess base.

## Copper

Copper, a reddish colored metal, is a relatively rare element, accounting for only $0.0068 \%$ of the earth's crust by mass. Like the other group 1B elements silver and gold, copper is found in nature in the elemental state. Its most important ores are sulfides, such as chalcopyrite, $\mathrm{CuFeS}_{2}$. In a multistep process, copper sulfides are concentrated, separated from iron, and converted to molten copper(I) sulfide, which is then reduced to elemental copper by blowing air through the hot liquid:

$$
\mathrm{Cu}_{2} \mathrm{~S}(l)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{Cu}(l)+\mathrm{SO}_{2}(g)
$$

The product, containing about 99\% copper, is purified by electrolysis (Section 18.12).
Because of its high electrical conductivity and negative oxidation potential, copper is widely used to make electrical wiring and corrosion-resistant water pipes. Copper is also used in coins and is combined with other metals to make alloys such as brass (mostly copper and zinc) and bronze (mostly copper and tin). Though less reactive than other first-series transition metals, copper is oxidized on prolonged exposure to $\mathrm{O}_{2}, \mathrm{CO}_{2}$, and water in moist air, forming basic copper(II) carbonate, $\mathrm{Cu}_{2}(\mathrm{OH})_{2} \mathrm{CO}_{3}$. Subsequent reaction with dilute $\mathrm{H}_{2} \mathrm{SO}_{4}$ in acid rain then forms $\mathrm{Cu}_{2}(\mathrm{OH})_{2} \mathrm{SO}_{4}$, the green patina seen on bronze monuments.

$$
\begin{aligned}
& 2 \mathrm{Cu}(s)+\mathrm{O}_{2}(g)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(g) \longrightarrow \mathrm{Cu}_{2}(\mathrm{OH})_{2} \mathrm{CO}_{3}(s) \\
& \mathrm{Cu}_{2}(\mathrm{OH})_{2} \mathrm{CO}_{3}(s)+\mathrm{H}_{2} \mathrm{SO}_{4}(a q) \longrightarrow \mathrm{Cu}_{2}(\mathrm{OH})_{2} \mathrm{SO}_{4}(s)+\mathrm{CO}_{2}(g)+\mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

In its compounds, copper exists in two common oxidation states, +1 (cuprous) and +2 (cupric). Because $E^{\circ}$ for the $\mathrm{Cu}^{+} / \mathrm{Cu}^{2+}$ half-reaction is less negative than that for the $\mathrm{Cu} / \mathrm{Cu}^{+}$half-reaction, any oxidizing agent strong enough to oxidize copper to the copper(I) ion is also able to oxidize the copper(I) ion to the copper(II) ion.

$$
\begin{array}{ll}
\mathrm{Cu}(s) \longrightarrow \mathrm{Cu}^{+}(a q)+\mathrm{e}^{-} & E^{\circ}=-0.52 \mathrm{~V} \\
\mathrm{Cu}^{+}(a q) \longrightarrow \mathrm{Cu}^{2+}(a q)+\mathrm{e}^{-} & E^{\circ}=-0.15 \mathrm{~V}
\end{array}
$$

Dilute nitric acid, for example, oxidizes copper to the +2 oxidation state:

$$
\begin{aligned}
& 3 \mathrm{Cu}(s)+2 \mathrm{NO}_{3}^{-}(a q)+8 \mathrm{H}^{+}(a q) \longrightarrow \\
& 3 \mathrm{Cu}^{2+}(a q)+2 \mathrm{NO}(g)+4 \mathrm{H}_{2} \mathrm{O}(l) \quad E^{\circ}=+0.62 \mathrm{~V}
\end{aligned}
$$

It follows from the $E^{\circ}$ values that $\mathrm{Cu}^{+}(a q)$ can disproportionate, oxidizing and reducing itself:

$$
\begin{aligned}
\mathrm{Cu}^{+}(a q)+\mathrm{e}^{-} \longrightarrow \mathrm{Cu}(s) & E^{\circ}=+0.52 \mathrm{~V} \\
\mathrm{Cu}^{+}(a q) \longrightarrow \mathrm{Cu}^{2+}(a q)+\mathrm{e}^{-} & E^{\circ}=-0.15 \mathrm{~V} \\
\hline 2 \mathrm{Cu}^{+}(a q) \longrightarrow \mathrm{Cu}(s)+\mathrm{Cu}^{2+}(a q) & E^{\circ}=+0.37 \mathrm{~V}
\end{aligned}
$$

The positive $E^{\circ}$ value for the disproportionation corresponds to a large equilibrium constant, indicating that the reaction proceeds far toward completion:

$$
2 \mathrm{Cu}^{+}(a q) \rightleftharpoons \mathrm{Cu}(s)+\mathrm{Cu}^{2+}(a q) \quad K_{\mathrm{c}}=1.8 \times 10^{6}
$$

Thus, the copper(I) ion is not an important species in aqueous solution, though copper(I) does exist in solid compounds such as CuCl . In the presence of $\mathrm{Cl}^{-}$ions, the disproportionation equilibrium is reversed because precipitation of the insoluble, white copper(I) chloride drives the following reaction to the right:

$$
\mathrm{Cu}(s)+\mathrm{Cu}^{2+}(a q)+2 \mathrm{Cl}^{-}(a q) \longrightarrow 2 \mathrm{CuCl}(s)
$$

The more common +2 oxidation state is found in the blue aqueous ion, $\mathrm{Cu}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}$, and in numerous solid compounds and complex ions. The addition


- Why do monuments made of copper or bronze turn green with age?

Bassam Z. Shakhashiri, "Precipitates and Complexes of Copper(II)," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 1 (The University of Wisconsin Press, Madison, 1983), pp. 318-323.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Green and Blue Copper Complexes," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 71-72.

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Copper Sulfate: Blue to White," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 69-70.

VStudents should review Lewis acid-base theory in preparation for the sections in this chapter on coordination chemistry.
of base (aqueous ammonia) to a solution of a copper(II) salt gives a blue precipitate of copper(II) hydroxide, which dissolves in excess aqueous ammonia, yielding the dark blue complex ion $\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$ (Figure 20.11):

$$
\begin{aligned}
\mathrm{Cu}^{2+}(a q)+2 \mathrm{OH}^{-}(a q) & \longrightarrow \mathrm{Cu}(\mathrm{OH})_{2}(s) \\
\mathrm{Cu}(\mathrm{OH})_{2}(s)+4 \mathrm{NH}_{3}(a q) & \longrightarrow \mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}(a q)+2 \mathrm{OH}^{-}(a q)
\end{aligned}
$$


© FIGURE 20.11 When an aqueous solution of $\mathrm{CuSO}_{4}$ (left) is treated with aqueous ammonia, a blue precipitate of $\mathrm{Cu}(\mathrm{OH})_{2}$ forms (center). On the addition of excess ammonia, the precipitate dissolves, yielding the deep blue $\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}{ }^{2+}$ ion (right).

Perhaps the most common of all copper compounds is the blue colored cop$\operatorname{per}(\mathrm{II})$ sulfate pentahydrate, $\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}$. Four of the five water molecules are bound to the copper(II) ion, and the fifth is hydrogen bonded to the sulfate ion. When heated, $\mathrm{CuSO}_{4} \cdot 5 \mathrm{H}_{2} \mathrm{O}$ loses its water and its color (Figure 14.13, page 599), suggesting that the blue color of the pentahydrate is due to bonding of $\mathrm{Cu}^{2+}$ to the water molecules.

## 20.5 | Coordination Compounds

A coordination compound is a compound in which a central metal ion (or atom) is attached to a group of surrounding molecules or ions by coordinate covalent bonds. A good example is the anticancer drug cisplatin, $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$, in which two $\mathrm{NH}_{3}$ molecules and two $\mathrm{Cl}^{-}$ions use lone pairs of electrons to bond to the platinum(II) ion:

$$
\begin{aligned}
&: \ddot{\mathrm{Cl}}: \\
&: \ddot{\mathrm{Cl}}: \ddot{\mathrm{P}}: \mathrm{NH}_{3} \quad \text { Cisplatin } \\
& \ddot{\mathrm{N}} \mathrm{~N}_{3}
\end{aligned}
$$

The molecules or ions that surround the central metal ion in a coordination compound are called ligands, and the atoms that are attached directly to the metal are called ligand donor atoms. In cisplatin, for example, the ligands are $\mathrm{NH}_{3}$ and $\mathrm{Cl}^{-}$, and the ligand donor atoms are N and Cl . The formation of a coordination compound is a Lewis acid-base interaction (Section 15.16) in which the ligands act as Lewis bases (electron-pair donors) and the central metal ion behaves as a Lewis acid (an electron-pair acceptor).

Not all coordination compounds are neutral molecules like $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$. Many are salts, such as $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right] \mathrm{Cl}_{2}$ and $\mathrm{K}_{3}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]$, which contain a complex cation or anion along with enough ions of opposite charge to give a compound that is electrically neutral overall. To emphasize that the complex ion is a discrete structural unit, it is always enclosed in brackets in the formula of the salt. Thus, $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right] \mathrm{Cl}_{2}$ contains $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right]^{2+}$ cations and $\mathrm{Cl}^{-}$anions. The term metal complex (or simply complex) refers both to neutral molecules, such as $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$, and to complex ions, such as $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right]^{2+}$ and $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$.

The number of ligand donor atoms that surround a central metal ion in a complex is called the coordination number of the metal. Thus, platinum(II) has a coordination number of 4 in $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$, and iron(III) has a coordination number of 6 in $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$. The most common coordination numbers are 4 and 6 , but others are well known (Table 20.4). The coordination number of a metal ion in a particular complex depends on the metal ion's size, charge, and electron configuration, and on the size and shape of the ligands.

| TABLE 20.4 | Examples of Complexes with <br> Various Coordination Numbers |
| :--- | :--- |
| Coordination <br> Number | Complex |
| 2 | $\left.\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}\right]^{+},[\mathrm{CuCl}]_{2}\right]^{-}$ |
| 3 | $[\mathrm{HgI}]^{-}$ |
| 4 | $\left[\mathrm{Zn}\left(\mathrm{NH}_{3}\right)_{4}\right]^{2+},\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$ |
| 5 | $\left[\mathrm{Ni}(\mathrm{CN})_{5}\right]^{3-}, \mathrm{Fe}(\mathrm{CO})_{5}$ |
| 6 | $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+},\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ |
| 7 | $[\mathrm{ZrF} 7]^{3-}$ |
| 8 | $\left[\mathrm{Mo}(\mathrm{CN})_{8}\right]^{4-}$ |

Metal complexes have characteristic shapes, depending on the metal ion's coordination number. Two-coordinate complexes, such as $\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}\right]^{+}$, are linear. Four-coordinate complexes are either tetrahedral or square planar; for example, $\left[\mathrm{Zn}\left(\mathrm{NH}_{3}\right)_{4}\right]^{2+}$ is tetrahedral, and $\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$ is square planar. Nearly all six-coordinate complexes are octahedral. The more common coordination geometries are illustrated in Figure 20.12. Coordination geometries were first deduced by the Swiss chemist Alfred Werner, who was awarded the 1913 Nobel Prize in chemistry for his pioneering studies.


$$
L-M-L
$$

Linear


Tetrahedral


Square planar


Octahedral
© FIGURE 20.12 The arrangement of ligand donor atoms (L) in $\mathrm{ML}_{n}$ complexes with coordination numbers 2,4 , and 6 . In the octahedral arrangement, four ligands are at the corners of a square, with one more above and one below the plane of the square.
R. Bruce Martin, "A Stability Ruler for Metal Ion Complexes," J. Chem. Educ., Vol. 64, 1987, 402.

ज
Ions present in a coordination compound to balance the charge of a complex ion are sometimes called counterions.

## -

Lee R. Summerlin and James L. Ealy, Jr., "Cobalt Complexes: Changing Coordination Numbers," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 1 (American Chemical Society, Washington, DC, 1988), pp. 41-42.

1D. Venkataraman, Yahua Du, Scott R. Wilson, A. Hirsch, Peng Zhang, and Jeffrey S. Moore, "A Coordination Geometry Table of the $d$-Block Elements and Their Ions," J. Chem. Educ., Vol. 74, 1997, 915-918.


V
Most transition metal complexes with a coordination number 4 are tetrahedral. Metal ions with eight $d$ electrons usually form complexes that are square planar.

The charge on a metal complex equals the charge on the metal ion (its oxidation state) plus the sum of the charges on the ligands. Thus, if we know the charge on each ligand and the charge on the complex, we can easily find the oxidation state of the metal.

## Worked Example 20.2

A cobalt(III) ion forms a complex with four ammonia molecules and two chloride ions. What is the formula of the complex?

## Strategy

The charge on the complex is the sum of the charges on the $\mathrm{Co}^{3+}$ ion, the four $\mathrm{NH}_{3}$ ligands, and the two $\mathrm{Cl}^{-}$ligands:

$$
\begin{gathered}
\mathrm{Co}^{3+} \\
+3
\end{gathered}{4 \mathrm{NH}_{3} \quad 2 \mathrm{Cl}^{-}}_{(4 \times 0)+[2 \times(-1)]=+1}
$$

## Solution

The formula of the complex is $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}\right]^{+}$.

## Worked Example 20.3

What is the oxidation state of platinum in the coordination compound $\mathrm{K}\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right) \mathrm{Cl}_{5}\right]$ ?

## Strategy

Because the compound is electrically neutral overall and contains one $\mathrm{K}^{+}$cation per complex anion, the anion must be $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right) \mathrm{Cl}_{5}\right]^{-}$. Since ammonia is neutral, and chloride has a charge of -1 , the sum of the oxidation numbers is $+1+n+0+$ $(5)(-1)=0$, where $n$ is the oxidation number of Pt :

$$
\begin{aligned}
& \mathrm{K}^{+} \mathrm{Pt}^{n+} \mathrm{NH}_{3} \quad 5 \mathrm{Cl}^{-} \\
& +1+n+0 \quad+[5 \times(-1)]=0 ; \quad n=+4
\end{aligned}
$$


$\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right) \mathrm{Cl}_{5}\right]^{-}$

## Solution

The oxidation state of platinum is +4 .

Daniel T. Haworth, "Some Linguistic Detail on Chelation," J. Chem. Educ., Vol. 75, 1998, 47.

Mark Conway, Smallwood Holoman, Ladell Jones, Ray Leenhouts, and Gerald Williamson, "Selecting and Using Chelating Agents," Chem. Eng., Vol. 106(3), 1999, 86-90.

PROBLEM 20.4 What is the formula of the chromium(III) complex that contains two ammonia and four thiocyanate $\left(\mathrm{SCN}^{-}\right)$ligands?

- PROBLEM 20.5 What is the oxidation state of iron in $\mathrm{Na}_{4}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]$ ?


## 20.6 | Ligands

Structures of some typical ligands are shown in Figure 20.13. Because all ligands are Lewis bases, they have at least one lone pair of electrons that can be used to form a coordinate covalent bond to a metal ion. They can be classified as monodentate or polydentate, depending on the number of ligand donor atoms that bond to the metal. Ligands such as $\mathrm{H}_{2} \mathrm{O}, \mathrm{NH}_{3}$, or $\mathrm{Cl}^{-}$that bond using the electron pair of a single donor atom are called monodentate ligands (literally, "onetoothed" ligands). Those that bond through electron pairs on more than one donor atom are termed polydentate ligands ("many-toothed" ligands). For example, ethylenediamine $\left(\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}\right.$, abbreviated en) is a bidentate ligand because it


A FIGURE 20.13 Structures of some common ligands. Ligand donor atoms are in color. The thiocyanate ion can bond to a metal through either the S atom or the N atom.


3D models of Ethylenediamine, Glycinate Ion, Oxalate lon, and EDTA ${ }^{4-}$

v
Chelate ligands usually form five- or six-membered rings with a metal ion.
J. Roger Hart, "EDTA-Type Chelating Agents in Everyday Consumer Products," J. Chem. Educ., Vol. 61, 1984, 1060-1061.
bonds to a metal using an electron pair on each of its two nitrogen atoms. The hexadentate ligand ethylenediaminetetraacetate ion (EDTA ${ }^{4-}$ ) bonds to a metal ion through electron pairs on six donor atoms (two N atoms and four O atoms).

Polydentate ligands are known as chelating agents (pronounced key-late-ing, from the Greek word chele, meaning "claw") because their multipoint attachment to a metal ion resembles the grasping of an object by the claws of a crab. For example, ethylenediamine holds a cobalt(III) ion with two claws, its two nitrogen donor atoms (Figure 20.14). The resulting five-membered ring consisting of the Co (III) ion, two N atoms, and two C atoms of the ligand is called a chelate ring. A complex such as $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ or $[\mathrm{Co}(\mathrm{EDTA})]^{-}$that contains one or more chelate rings is known as a metal chelate. Because EDTA ${ }^{4-}$ bonds to a metal ion through six donor atoms, it forms especially stable complexes and is often used to hold metal ions in solution. For example, in the treatment of lead poisoning, EDTA ${ }^{4-}$ bonds to $\mathrm{Pb}^{2+}$, which is then excreted by the kidneys as the soluble chelate $[\mathrm{Pb}(\text { EDTA })]^{2-}$. EDTA ${ }^{4-}$ is commonly added to food products such as commercial salad dressings to complex any metal cations that might be present in trace amounts. The free metal ions might otherwise catalyze the oxidation of oils, thus causing the dressing to become rancid.


N. M. Senozan and R. L. Hunt, "Hemoglobin: Its Occurrence, Structure, and Adaptation," J. Chem. Educ., Vol. 59, 1982, 173-178.

Colin J. Rix, "The Biochemistry of Some Iron Porphyrin Complexes," J. Chem. Educ., Vol. 59, 1982, 389-392.

Ei-Ichiro Ochiai, "Toxicity of Heavy Metals and Biological Defense: Principles and Applications in Bioinorganic Chemistry, Part VII," J. Chem. Educ., Vol. 72, 1995, 479-484.
$\triangle$ FIGURE 20.14 (a) Molecular model and (b) shorthand representation of the $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ ion. The complex contains three cobalt-ethylenediamine chelate rings. In (b), the symbol $\mathrm{N}^{-} \mathrm{N}$ represents a bidentate $\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}$ ligand, which spans adjacent corners of the octahedron. (c) Molecular model and (d) shorthand representation of the [Co(EDTA)] ion. The hexadentate EDTA ${ }^{4-}$ ligand uses its two N atoms and four O atoms to bond to the metal, thus forming five chelate rings.

Naturally occurring chelating ligands are essential constituents of many important biomolecules. For example, the heme group in hemoglobin contains a planar, tetradentate ligand that uses the lone pair of electrons on each of its four N atoms to bond to an iron(II) ion (Chapter 13 Interlude). The ligand in heme is a porphyrin, a derivative of the porphine molecule (Figure 20.15a) in which the porphine's peripheral H atoms are replaced by various substituent groups ( $-\mathrm{CH}_{3},-\mathrm{CH}=\mathrm{CH}_{2}$, and $-\mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CO}_{2}^{-}$in heme). Bonding of the porphyrin to the $\mathrm{Fe}(\mathrm{II})$ ion involves prior loss of the two NH protons, which makes room for the $\mathrm{Fe}(\mathrm{II})$ to occupy the cavity between the four N atoms.

In hemoglobin (and in the iron storage protein myoglobin), the heme is linked to a protein (the globin) through an additional $\mathrm{Fe}-\mathrm{N}$ bond, as shown in Figure 20.15b. In addition, the $\mathrm{Fe}(\mathrm{II})$ can bond to an $\mathrm{O}_{2}$ molecule to give the sixcoordinate, octahedral complex present in oxyhemoglobin and oxymyoglobin. The three-dimensional shape of the protein part of the molecule makes possible the reversible binding of $\mathrm{O}_{2}$. We'll have more to say about proteins in Sections 24.4 and 24.5.

(a)

(b)

## 20.7 | Naming Coordination Compounds

In the early days of coordination chemistry, coordination compounds were named after their discoverer or according to their color. Now, we use systematic names that specify the number of ligands of each particular type, the metal, and its oxidation state. Before listing the rules used to name coordination compounds, let's consider a few examples that will illustrate how to apply the rules:


The following list summarizes the nomenclature rules recommended by the International Union of Pure and Applied Chemistry:

1. If the compound is a salt, name the cation first and then the anion, just as in naming simple salts (Section 2.10). For example, $\mathrm{K}_{3}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]$ is potassium hexacyanoferrate(III).
2. In naming a complex ion or a neutral complex, name the ligands first and then the metal. The names of anionic ligands end in -o. As shown in Table 20.5, they are usually obtained by changing the anion endings -ide to -o and -ate to -ato. Neutral ligands are specified by their usual names, except for $\mathrm{H}_{2} \mathrm{O}, \mathrm{NH}_{3}$, and CO , which are called aqua, ammine (note spelling), and carbonyl, respectively. The name of a complex is one word, with no space between the various ligand names and no space between the names of the last ligand and the metal.

A FIGURE 20.15 (a) The structure of the porphine molecule. Loss of the two NH protons gives a planar, tetradentate 2- ligand that can bond to a metal cation. The porphyrins are derivatives of porphine in which the peripheral H atoms are replaced by various substituent groups. (b) Schematic of the planar heme group, the attached protein chain, and the bound $\mathrm{O}_{2}$ molecule in oxyhemoglobin and oxymyoglobin. The Fe (II) ion has a six-coordinate, octahedral environment, and the $\mathrm{O}_{2}$ acts as a monodentate ligand.

$\sqrt{ }$Older literature named ligand water aquo instead of aqua. The ending -o implies an anionic ligand.

VAmmonia as a ligand has the name ammine, with two $m$ 's. If one or more of the hydrogen atoms are replaced by groups of atoms bonded through carbon, the resulting ligand is an organic amine, with one $m$.

TABLE 20.5 Names of Some Common Ligands

| Anionic Ligand | Ligand Name | Neutral Ligand | Ligand Name |
| :--- | :--- | :--- | :--- |
| Bromide, $\mathrm{Br}^{-}$ | Bromo | Ammonia, $\mathrm{NH}_{3}$ | Ammine |
| Carbonate, $\mathrm{CO}_{3}{ }^{2-}$ | Carbonato | Water, $\mathrm{H}_{2} \mathrm{O}$ | Aqua |
| Chloride, $\mathrm{Cl}^{-}$ | Chloro | Carbon monoxide, CO | Carbonyl |
| Cyanide, $\mathrm{CN}^{-}$ | Cyano | Ethylenediamine, en | Ethylenediamine |
| Fluoride, $\mathrm{F}^{-}$ | Fluoro |  |  |
| Glycinate, $\mathrm{gly}^{-}$ | Glycinato |  |  |
| Hydroxide, $\mathrm{OH}^{-}$ | Hydroxo |  |  |
| Oxalate, $\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}$ | Oxalato |  |  |
| Thiocyanate, $\mathrm{SCN}^{-}$ | Thiocyanato |  |  |
|  | Isothiocyanato ${ }^{+}$ |  |  |

* Ligand donor atom is S
${ }^{\dagger}$ Ligand donor atom is N


A A sample of tris(ethylenediamine)cobalt(III) chloride, $\left[\mathrm{Co}(\mathrm{en})_{3}\right] \mathrm{Cl}_{3}$.
3. If the complex contains more than one ligand of a particular type, indicate the number with the appropriate Greek prefix: di-, tri-, tetra-, penta-, hexa-, and so forth. The ligands are listed in alphabetical order, and the prefixes are ignored in determining the order. Thus, tetraaqua precedes dichloro in the name for $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{4} \mathrm{Cl}_{2}\right] \mathrm{Cl}$ : tetraaquadichlorochromium(III) chloride.
4. If the name of a ligand itself contains a Greek prefix-for example, ethylenediamine-put the ligand name in parentheses and use one of the following alternative prefixes to specify the number of ligands: bis- (2), tris- (3), tetrakis- (4), and so forth. Thus, the name of $\left[\mathrm{Co}(\mathrm{en})_{3}\right] \mathrm{Cl}_{3}$ is tris(ethylenediamine)cobalt(III) chloride.
5. Use a Roman numeral in parentheses, immediately following the name of the metal, to indicate the metal's oxidation state. As shown by the preceding examples, there is no space between the name of the metal and the parenthesis.
6. In naming the metal, use the ending -ate if the metal is in an anionic complex. Thus, $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ is the hexacyanoferrate(III) anion. There are no simple rules for going from the name of the metal to the name of the metallate anion, partly because some of the anions have Latin names. Some common examples are given in Table 20.6.

TABLE 20.6 Names of Some Common Metallate Anions

| Metal | Anion Name | Metal | Anion Name |
| :--- | :--- | :--- | :--- |
| Aluminum | Aluminate | Iron | Ferrate |
| Chromium | Chromate | Manganese | Manganate |
| Cobalt | Cobaltate | Nickel | Nickelate |
| Copper | Cuprate | Platinum | Platinate |
| Gold | Aurate | Zinc | Zincate |

The rules for naming coordination compounds make it possible to go from a formula to the systematic name or from a systematic name to the appropriate formula. Worked Examples 20.4 and 20.5 provide some practice.

## Worked Example 20.4

## Name each of the following:

(a) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right] \mathrm{Cl}_{3}$, prepared in 1798 by B. M. Tassaert and generally considered to be the first coordination compound
(b) $\left[\mathrm{Rh}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{I}\right] \mathrm{I}_{2}$, a yellow compound obtained by heating $\left[\mathrm{Rh}\left(\mathrm{NH}_{3}\right)_{5}\left(\mathrm{H}_{2} \mathrm{O}\right)\right] \mathrm{I}_{3}$ at $100^{\circ} \mathrm{C}$
(c) $\mathrm{Fe}(\mathrm{CO})_{5}$, a highly toxic, volatile liquid
(d) $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$, the ion formed when $\mathrm{Fe}_{2} \mathrm{O}_{3}$ rust stains are dissolved in oxalic acid $\left(\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}\right)$

## Strategy

First determine the oxidation state of the metal, as in Worked Example 20.3. Then apply the six rules above to name the compound or ion.

## Solution

(a) Because the chloride ion has a charge of -1 and ammonia is neutral, the oxidation state of cobalt is +3 . Use the prefix hexa- to indicate that the cation contains six $\mathrm{NH}_{3}$ ligands, and use a Roman numeral III in parentheses to indicate the oxidation state of cobalt. The name of $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right] \mathrm{Cl}_{3}$ is hexaamminecobalt(III) chloride.
(b) Because the iodide ion has a charge of -1 , the complex cation is $\left[\mathrm{Rh}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{I}\right]^{2+}$ and the rhodium has an oxidation state of +3 . List the $a$ mmine ligands before the iodo ligand, and use the prefix penta- to indicate the presence of five $\mathrm{NH}_{3}$ ligands. The name of $\left[\mathrm{Rh}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{I}\right] I_{2}$ is pentaammineiodorhodium(III) iodide.
(c) Because the carbonyl ligand is neutral, the oxidation state of iron is zero. The systematic name of $\mathrm{Fe}(\mathrm{CO})_{5}$ is pentacarbonyliron(0), but the common name iron pentacarbonyl is often used.
(d) Because each oxalate ligand $\left(\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}\right)$ has a charge of -2 , and because $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$ has an overall charge of -3 , iron must have an oxidation state of +3 . Use the name ferrate(III) for the metal because the complex is an anion. The name of $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$ is the trioxalatoferrate(III) ion.


A The compound $\mathrm{K}_{3}\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right] \cdot 3 \mathrm{H}_{2} \mathrm{O}$ contains the trioxalatoferrate(III) ion.

## Worked Example 20.5

Write the formula for each of the following:
(a) Potassium tetracyanonickelate(II)
(b) Aquachlorobis(ethylenediamine)cobalt(III) chloride
(c) Sodium hexafluoroaluminate
(d) Diamminesilver(I) ion

## Strategy

To find the formula and charge of the complex cation or anion, note the number of ligands of each type, their charge, and the oxidation state of the metal in the name of the compound or ion. If the name refers to an electrically neutral compound, balance the charge of the complex cation or anion with the appropriate number of ions of opposite charge.

## Solution

(a) The bonding of four $\mathrm{CN}^{-}$ligands to $\mathrm{Ni}^{2+}$ gives an $\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$ anion, which must be balanced by two $\mathrm{K}^{+}$cations. The compound's formula is therefore $\mathrm{K}_{2}\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]$. This compound is obtained when excess KCN is added to a solution of a nickel(II) salt.

0Isomers have the same chemical formula but different physical and chemical properties.

FIGURE 20.16
Classification scheme for the kinds of isomers in coordination chemistry. See the text for examples.
(b) Because the complex cation contains one $\mathrm{H}_{2} \mathrm{O}$, one $\mathrm{Cl}^{-}$, and two neutral en ligands, and because the metal is $\mathrm{Co}^{3+}$, the cation is $\left[\mathrm{Co}(\mathrm{en})_{2}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Cl}\right]^{2+}$. The $2+$ charge of the cation must be balanced by two $\mathrm{Cl}^{-}$anions, so the formula of the compound is $\left[\mathrm{Co}(\mathrm{en})_{2}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Cl}^{2} \mathrm{Cl}_{2}\right.$. The cation is the first product formed when $\left[\mathrm{Co}(\mathrm{en})_{2} \mathrm{Cl}_{2}\right]^{+}$reacts with water.
(c) Sodium hexafluoroaluminate, also called cryolite, is used in the electrolytic production of aluminum metal (Section 18.12) and is a coordination compound of a maingroup element. The oxidation state of aluminum is omitted from the name because aluminum has only one oxidation state $(+3)$. Because $\mathrm{F}^{-}$has a charge of -1 , the anion is $\left[\mathrm{AlF}_{6}\right]^{3-}$. The charge of the anion must be balanced by three $\mathrm{Na}^{+}$cations; therefore, the formula for the compound is $\mathrm{Na}_{3}\left[\mathrm{AlF}_{6}\right]$.
(d) Diamminesilver(I) ion, formed when silver chloride dissolves in an excess of aqueous ammonia, has the formula $\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}\right]^{+}$.

- PROBLEM 20.6 Name each of the following:
(a) $\left[\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}\right] \mathrm{SO}_{4}$, a deep blue compound obtained when $\mathrm{CuSO}_{4}$ is treated with an excess of ammonia
(b) $\mathrm{Na}\left[\mathrm{Cr}(\mathrm{OH})_{4}\right]$, the compound formed when $\mathrm{Cr}(\mathrm{OH})_{3}$ is dissolved in an excess of aqueous NaOH
(c) $\mathrm{Co}(\text { gly })_{3}$, a complex that contains the anion of the amino acid glycine
(d) $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{5}(\mathrm{NCS})\right]^{2+}$, the red complex ion formed in a qualitative analysis test for iron

PROBLEM 20.7 Write the formula for each of the following:
(a) Tetraamminezinc(II) nitrate, the compound formed when zinc nitrate is treated with an excess of ammonia
(b) Tetracarbonylnickel(0), the first metal carbonyl (prepared in 1888) and an important compound in the industrial refining of nickel metal
(c) Potassium amminetrichloroplatinate(II), a compound that contains a square planar anion
(d) The dicyanoaurate(I) ion, an ion important in the extraction of gold from its ores

### 20.8 Isomers

One of the more interesting aspects of coordination chemistry is the existence of isomers, compounds that have the same formula but a different arrangement of their constituent atoms. Because their atoms are arranged differently, isomers are different compounds with different chemical reactivity and different physical properties (such as color, solubility, and melting point). Figure 20.16 shows a scheme for classifying

some of the kinds of isomers in coordination chemistry. As we'll see in Chapters 23 and 24 , isomers are also important in organic chemistry and biochemistry.

## Constitutional Isomers

Isomers that have different connections among their constituent atoms are called constitutional isomers. Of the various types of constitutional isomers, we'll discuss just two: linkage isomers and ionization isomers.

Linkage isomers arise when a ligand can bond to a metal through either of two different donor atoms. For example, the nitrite $\left(\mathrm{NO}_{2}{ }^{-}\right)$ion forms two different pentaamminecobalt(III) complexes: a yellow nitro complex that contains a $\mathrm{Co}-\mathrm{N}$ bond, $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5}\left(\mathrm{NO}_{2}\right)\right]^{2+}$, and a red nitrito complex that contains a $\mathrm{Co}-\mathrm{O}$ bond, $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5}(\mathrm{ONO})\right]^{2+}$ (Figure 20.17). The ligand in the nitrito complex is written as ONO to emphasize that it's linked to the cobalt through the oxygen atom. The thiocyanate $\left(\mathrm{SCN}^{-}\right)$ion is another ligand that gives linkage isomers because it can bond to a metal through either the sulfur atom to give a thiocyanato complex or the nitrogen atom to give an isothiocyanato complex.


V FIGURE 20.17 Samples and structures of (a) the nitro complex $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5}\left(\mathrm{NO}_{2}\right)\right]^{2+}$, which contains an N -bonded $\mathrm{NO}_{2}{ }^{-}$ligand, and (b) the nitrito complex $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5}(\mathrm{ONO})\right]^{2+}$, which contains an O-bonded $\mathrm{NO}_{2}{ }^{-}$ ligand.


Ionization isomers differ in the anion that is bonded to the metal ion. An example is the pair $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}\right] \mathrm{SO}_{4}$, a violet compound that has a $\mathrm{Co}-\mathrm{Br}$ bond and a free sulfate anion, and $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{SO}_{4}\right] \mathrm{Br}$, a red compound that has a Co-sulfate bond and a free bromide ion. Ionization isomers get their name because they yield different ions in solution.

## Stereoisomers

Isomers that have the same connections among atoms but a different arrangement of the atoms in space are called stereoisomers. In coordination chemistry, there are two kinds of stereoisomers: diastereoisomers and enantiomers (we'll discuss the latter in Section 20.9). -

DTiJ John J. Fortman, "Pictorial Analogies VIII: Types of Formulas and Structural Isomers," J. Chem. Educ., Vol. 70, 1993, 755. Hannia Lujan-Upton, "Introducing Stereochemistry to
Non-Science Majors," J. Chem.
Educ., Vol. 78, 2001, 475-477.

(a) cis

(b) trans

© FIGURE 20.18 Diastereoisomers of the square planar complex $\operatorname{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$. The two compounds have the same connections among atoms but different arrangements of the atoms in space.

Diastereoisomers, also called geometric isomers, have the same connections among atoms but different spatial orientations of their metal-ligand bonds. For example, in the square planar complex $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$ the two $\mathrm{Pt}-\mathrm{Cl}$ bonds can be oriented either adjacent at a $90^{\circ}$ angle or opposite at a $180^{\circ}$ angle, as shown in Figure 20.18. The isomer in which identical ligands occupy adjacent corners of the square is called the cis isomer, and that in which identical ligands are across from each other is called the trans isomer. (The Latin word cis means next to; trans means across.) Cis and trans isomers are different compounds with different properties. Thus, cis- $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$ is a polar molecule and is more soluble in water than trans $-\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$. The trans isomer is nonpolar because the two $\mathrm{Pt}-\mathrm{Cl}$ and the two $\mathrm{Pt}-\mathrm{NH}_{3}$ bond dipoles point in opposite directions and therefore cancel. It's also interesting that $c i s-\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$ (cisplatin) is an effective anticancer drug, whereas the trans isomer is physiologically inactive.

When counting diastereoisomers, students frequently arrive at too many because they draw the same isomer in different orientations.

In general, square planar complexes of the type $M A_{2} B_{2}$ and $M A_{2} B C$-where M is a metal ion and $\mathrm{A}, \mathrm{B}$, and C are ligands-can exist as cis-trans isomers. No cis-trans isomers are possible, however, for four-coordinate tetrahedral complexes because all four corners of a tetrahedron are adjacent to one another.

Octahedral complexes of the type $\mathrm{MA}_{4} \mathrm{~B}_{2}$ can also exist as diastereoisomers because the two B ligands can be on either adjacent or opposite corners of the octahedron. Examples are the violet compound cis-[Co( $\left.\left.\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}\right] \mathrm{Cl}$ and the green compound trans- $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}\right] \mathrm{Cl}$. As Figure 20.19 shows, there are several ways of drawing the cis and trans isomers because each complex can be rotated in space, changing the perspective but not the identity of the isomer.

How can we be sure that there are only two diastereoisomers of the $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}\right]^{+}$ion? The first $\mathrm{Cl}^{-}$ligand can be located at any one of the six corners of the octahedron. Once one $\mathrm{Cl}^{-}$is present, however, the five corners remaining are no longer equivalent. The second $\mathrm{Cl}^{-}$can be located either on one of the four corners adjacent to the first $\mathrm{Cl}^{-}$, which gives the cis isomer, or on the unique corner opposite the first $\mathrm{Cl}^{-}$, which gives the trans isomer. Thus, only two diastereoisomers are possible for complexes of the type $\mathrm{MA}_{4} \mathrm{~B}_{2}$ (and $\mathrm{MA}_{4} \mathrm{BC}$ ).

Worked Example 20.6

Platinum(II) forms square planar complexes, and platinum(IV) gives octahedral complexes. How many diastereoisomers are possible for each of the following complexes? Describe their structures.
(a) $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}\right]^{+}$
(b) $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right) \mathrm{Cl}_{5}\right]^{-}$
(c) $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}\left(\mathrm{NO}_{2}\right)$
(d) $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{ClBr}\right]^{2+}$

## Strategy

Recall that cis and trans isomers are possible for square planar complexes of the type $M A_{2} B_{2}$ and $M A_{2} B C$ and for octahedral complexes of the type $M A_{4} B_{2}$ and $M A_{4} B C$. Cis and trans isomers are not possible when only one ligand differs from the others, as in complexes of the type $\mathrm{MA}_{3} \mathrm{~B}$ and $\mathrm{MA}_{5} \mathrm{~B}$.

## Solution

(a) No isomers are possible for $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}\right]^{+}$, a square planar complex of the type $M A B 3 \mathrm{~B}$.

(b) No isomers are possible for $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right) \mathrm{Cl}_{5}\right]^{-}$, an octahedral complex of the type $\mathrm{MA}_{5} \mathrm{~B}$.

(c) Cis and trans isomers are possible for $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}\left(\mathrm{NO}_{2}\right)$, a square planar complex of the type $\mathrm{MA}_{2} \mathrm{BC}$. The $\mathrm{Cl}^{-}$and $\mathrm{NO}_{2}{ }^{-}$ligands can be on either adjacent or opposite corners of the square.

(d) Cis and trans isomers are possible for $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{ClBr}\right]^{2+}$, an octahedral complex of the type $\mathrm{MA}_{4} \mathrm{BC}$. The $\mathrm{Cl}^{-}$and $\mathrm{Br}^{-}$ligands can be on either adjacent or opposite corners of the octahedron.


## Worked EXample 20.7

Draw the structures of all possible diastereoisomers of triamminetrichlorocobalt(III), $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}_{3}$.

## Strategy and Solution

Two diastereoisomers are possible for an octahedral complex of the type $\mathrm{MA}_{3} \mathrm{~B}_{3}$. Isomer (a) shown below has the three $\mathrm{Cl}^{-}$ligands in adjacent positions on one triangular face of the octahedron; isomer (b) has all three $\mathrm{Cl}^{-}$ligands in a plane that contains the Co (III) ion. In isomer (a), all three $\mathrm{Cl}-\mathrm{Co}-\mathrm{Cl}$ bond angles are $90^{\circ}$, whereas in isomer (b) two $\mathrm{Cl}-\mathrm{Co}^{-} \mathrm{Cl}$ angles are $90^{\circ}$ and the third is $180^{\circ}$.


(a)

(b)

To convince yourself that only two diastereoisomers of $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}_{3}$ exist, look back at Figure 20.19 and consider the products obtained from cis- and trans- $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}\right]^{+}$ when one of the four $\mathrm{NH}_{3}$ ligands is replaced by a $\mathrm{Cl}^{-}$. There are two kinds of $\mathrm{NH}_{3}$ ligands in cis- $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}\right]^{+}$: two $\mathrm{NH}_{3}$ ligands that are trans to each other and two $\mathrm{NH}_{3}$ ligands that are trans to a $\mathrm{Cl}^{-}$. Replacing an $\mathrm{NH}_{3}$ trans to another $\mathrm{NH}_{3}$ with $\mathrm{Cl}^{-}$ gives $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}_{3}$ isomer (a), whereas replacing an $\mathrm{NH}_{3}$ trans to a $\mathrm{Cl}^{-}$with another $\mathrm{Cl}^{-}$gives isomer (b). All four $\mathrm{NH}_{3}$ ligands in trans- $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}\right]^{+}$are equivalent, and
replacing any one of them with a $\mathrm{Cl}^{-}$gives isomer (b). [If you rotate the resulting $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}_{3}$ complex, you can see that it is identical to the previous drawing of isomer
(b).] Thus, there are only two diastereoisomers for a complex of the type $M A_{3} B_{3}$.



PROBLEM 20.8 How many diastereoisomers are possible for the following complexes? Draw the structure of each diastereoisomer.


Isomers Classification activity
(a) $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2}(\mathrm{SCN})_{2}$
(b) $\left[\mathrm{CoCl}_{2} \mathrm{Br}_{2}\right]^{2-}$ (tetrahedral)
(c) $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3}\left(\mathrm{NO}_{2}\right)_{3}$
(d) $\mathrm{Pt}(\mathrm{en}) \mathrm{Cl}_{2}$
(e) $\left[\mathrm{Cr}(\mathrm{en})_{2} \mathrm{Br}_{2}\right]^{+}$
(f) $\left[\mathrm{Rh}(\mathrm{en})_{3}\right]^{3+}$

## Worked Key Concept Example 20.8

Consider the following isomers of the $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Cl}\right]^{2+}$ ion:

(1)
$\bigcirc=\mathrm{Co} \quad=\mathrm{NH}_{3}$


(2)

(3)

(4)
(a) Label the isomers as cis or trans.
(b) Which isomers are identical, and which are different?

## Strategy

Look at the location of the $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Cl}^{-}$ligands. Those isomers that have $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Cl}^{-}$on adjacent corners of the octahedron are cis, while those that have $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Cl}^{-}$ on opposite corners are trans. Because only two isomers are possible for complexes of the type $\mathrm{MA}_{4} \mathrm{BC}$, all the cis isomers are identical and all the trans isomers are identical.

## Solution

(a) Isomers (1) and (4) have $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Cl}^{-}$on opposite corners of the octahedron and are therefore trans isomers. Isomers (2) and (3) have $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{Cl}^{-}$on adjacent corners of the octahedron and are therefore cis isomers.
(b) Isomers (1) and (4) are identical, as can be seen by rotating (1) counterclockwise by $90^{\circ}$ about the vertical $(z)$ axis:



Chirality movie

Steven C. Stinson, "Chiral Drugs," Chem. Eng. News, September 19, 1994, 38-57.

Isomers (2) and (3) differ from (1) and (4) and are identical, as can be seen by rotating (2) clockwise by $90^{\circ}$ about the $x$ axis and then counterclockwise by $90^{\circ}$ about the $y$ axis:

$\curvearrowleft$ KEY CONCEPT PROBLEM 20.9 Which of the following $\left[\mathrm{Co}(\mathrm{en})\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}\right]^{2+}$ isomers are identical, and which are different?


### 20.9 Enantiomers and Molecular Handedness

Diastereoisomers are relatively easy to distinguish because the various bonds in the cis and trans isomers point in different directions. Enantiomers, however, are stereoisomers that differ in a more subtle way: Enantiomers are molecules or ions that are nonidentical mirror images of each other; they differ because of their handedness.

Handedness affects almost everything we do. Anyone who has played much softball knows that the last available glove always fits the wrong hand. Any lefthanded person sitting next to a right-handed person in a lecture knows that taking notes sometimes means bumping elbows. The reason for these difficulties is that our hands aren't identical-they're mirror images. When you hold your left hand up to a mirror, the image you see looks like your right hand. (Try it.)

Not all objects are handed. There's no such thing as a "right-handed" tennis ball or a "left-handed" coffee mug. When a tennis ball or a coffee mug is held up to a mirror, the image reflected is identical to the ball or mug itself. Objects that do have a handedness to them are said to be chiral (pronounced ky-ral, from the Greek cheir, meaning hand), and objects that lack handedness are said to be nonchiral, or achiral.


Why is it that some objects are chiral but others aren't? In general, an object is not chiral if, like the coffee mug, it has a symmetry plane cutting through its middle so that one half of the object is a mirror image of the other half. If you were to cut the mug in half, one half of the mug would be the mirror image of the other half. A hand, however, has no symmetry plane and is therefore chiral. If you were to cut a hand in two, one "half" of the hand would not be a mirror image of the other half (Figure 20.20).

Just as certain objects like a hand are chiral, certain molecules and ions are also chiral. Consider, for example, the tris(ethylenediamine)cobalt(III) ion, $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$, a molecule with the shape of a three-bladed propeller (Figure 20.21). The $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ cation has no symmetry plane because its two halves aren't mirror images, but it does have a threefold symmetry axis, which passes through the Co (III) ion and is nearly perpendicular to the plane of the figure. Like a hand, $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ is chiral and can exist in two nonidentical mirror-image forms-a "right-handed" enantiomer in which the three ethylenediamine ligands spiral to the right (clockwise) about the threefold axis and a "left-handed" enantiomer in which the ethylenediamine ligands spiral to the left (counterclockwise) about the threefold axis. The direction of spiral is indicated in the figure by the red arrows. By contrast, the analogous ammonia complex $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$ is achiral because, like a coffee mug, it has a symmetry plane. (Actually, $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$ has several symmetry planes, though only one is shown in Figure 20.21.) Thus, $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$ exists in a single form and does not have enantiomers.


Enantiomers have identical properties except for their reactions with other chiral substances and their effect on plane-polarized light. In ordinary light, the electric vibrations occur in all planes parallel to the direction in which the light wave is traveling, but in plane-polarized light, the electric vibrations of the light wave are restricted to a single plane, as shown in Figure 20.22. Plane-polarized light is


Karen F. Schmidt, "Mirror Image Molecules: New Techniques Promise More Potent Drugs and Pesticides," Science News, May 29, 1993, 348-350.

$\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$
Enantiomers 3D
models

- FIGURE 20.21 The structures of the $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ enantiomers and the achiral $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$ ion. $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ has a helical structure in which the three en ligands lie along the threads of a screw. As the red arrows show, one enantiomer is "right-handed" in the sense that the screw would advance into the page as you rotated it to the right. The other enantiomer is "left-handed" because it would advance into the page as you rotated it to the left. In contrast, $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$ has several symmetry planes and is achiral. (Only one of the symmetry planes is identified.)




FIGURE 20.22 The essential features of a polarimeter. The polarimeter measures the angle through which the plane of planepolarized light is rotated when the light is passed through a solution of a chiral substance.

obtained by passing ordinary light through a polarizing filter, like that found in certain kinds of sunglasses. If the plane-polarized light is then passed through a solution of one enantiomer, the plane of polarization is rotated, either to the right (clockwise) or to the left (counterclockwise). If the light is passed through a solution of the other enantiomer, its plane of polarization is rotated through an equal angle, but in the opposite direction. Enantiomers are sometimes called optical isomers because of their effect on plane-polarized light.

Enantiomers are labeled $(+)$ or $(-)$, depending on the direction of rotation of the plane of polarization. For example, the isomer of $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ that rotates the plane of polarization to the right is labeled $(+)-\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$, and the isomer that rotates the plane of polarization to the left is designated $(-)-\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$. $\mathrm{A} 1: 1$ mixture of the $(+)$ and $(-)$ isomers, called a racemic mixture, produces no net optical rotation because the rotations produced by the individual enantiomers exactly cancel.

## Worked Example 20.9

Draw the structures of all possible diastereoisomers and enantiomers of $\left[\mathrm{Co}(\mathrm{en})_{2} \mathrm{Cl}_{2}\right]^{+}$.

## Strategy

Ethylenediamine always spans adjacent corners of an octahedron, but the $\mathrm{Cl}^{-}$ligands can be on either adjacent or opposite corners. Therefore, there are two diastereoisomers, cis and trans. Because the trans isomer has several symmetry planes-one cuts through the Co and the en ligands-it is achiral and has no enantiomers. The cis isomer, however, is chiral and exists as a pair of enantiomers that are nonidentical mirror images.

## Solution



You can see that the cis enantiomer on the right is not the same as the one on the left if you rotate it by $180^{\circ}$ about the vertical $\mathrm{N}-\mathrm{Co}^{-} \mathrm{N}$ axis.

PROBLEM 20.10 Which of the following objects are chiral?
(a) A chair
(b) A foot
(c) A pencil
(d) A corkscrew
(e) A banana
(f) A football

KEY CONCEPT PROBLEM 20.11 Consider the following ethylenediamine complexes of rhodium:

(a) Which complexes are chiral, and which are achiral?
(b) Draw the enantiomer of each chiral complex.

- PROBLEM 20.12 Which of the following complexes can exist as enantiomers? Draw the structure of each enantiomer.
(a) $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$
(b) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4}(\mathrm{en})\right]^{3+}$
(c) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{2}(\mathrm{en})_{2}\right]^{3+}$
(d) $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{4} \mathrm{Cl}_{2}\right]^{+}$


### 20.10 Color of Transition Metal Complexes

Most transition metal complexes have beautiful colors that depend on the identity of the metal and the ligands. The color of an aqua complex, for example, depends on the metal: $\left[\mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ is pink, $\left[\mathrm{Ni}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ is green, $\left[\mathrm{Cu}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ is blue, but $\left[\mathrm{Zn}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ is colorless (Figure 20.23). If we keep the metal constant but vary the ligand, the color also changes. For example, $\left[\mathrm{Ni}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ is green, $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right]^{2+}$ is blue, and $\left[\mathrm{Ni}(\mathrm{en})_{3}\right]^{2+}$ is violet (Figure 20.24).


4 FIGURE 20.23 Aqueous solutions of the nitrate salts of cobalt(II), nickel(II), copper(II), and zinc(II) (from left to right).

How can we account for the color of transition metal complexes? Let's begin by recalling that white light consists of a continuous spectrum of wavelengths corresponding to different colors (Section 5.2). When white light strikes a colored substance, some wavelengths are transmitted while others are absorbed. Just as atoms can absorb light by undergoing electronic transitions between atomic energy levels, thereby giving rise to atomic spectra (Section 5.3), so a metal complex can absorb light by undergoing an electronic transition from its lowest (ground) energy state to a higher (excited) energy state.


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Laurence Poncini and Franz L. Wimmer, "Color Classification of Coordination Compounds," J. Chem. Educ., Vol. 64, 1987, 1001-1002.

© FIGURE 20.24 Aqueous solutions that contain $\left[\mathrm{Ni}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+},\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right]^{2+}$, and $\left[\mathrm{Ni}(\mathrm{en})_{3}\right]^{2+}$ (from left to right). The two solutions on the right were prepared by adding ammonia and ethylenediamine, respectively, to aqueous nickel(II) nitrate.

VThe color of a complex corresponds to wavelengths of light that are not absorbed by the complex. The observed color is usually the complement of the color absorbed. If all wavelengths of light are absorbed, a complex appears black. If no wavelengths of light are absorbed, a complex appears white (colorless).

FIGURE 20.25 (a) A solution that contains the $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ ion. (b) Visible absorption spectrum of the $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ ion.


The wavelength $\lambda$ of the light absorbed by a metal complex depends on the energy separation $\Delta E=E_{2}-E_{1}$ between the two states, as given by the Planck equation $\Delta E=h \nu=h c / \lambda$ (Section 5.4), where $h$ is Planck's constant, $\nu$ is the frequency of the light, and $c$ is the speed of light:

$$
\begin{aligned}
\Delta E & =E_{2}-E_{1}=h \nu=\frac{h c}{\lambda} \\
\text { or } \quad \lambda & =\frac{h c}{\Delta E}
\end{aligned}
$$

The measure of the amount of light absorbed by a substance is called the absorbance, and a plot of absorbance versus wavelength is called an absorption spectrum. For example, the absorption spectrum of the red-violet $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ ion has a broad absorption band at about 500 nm , a wavelength in the blue-green part of the visible spectrum (Figure 20.25). Because the absorbance is smaller in

the red and violet regions of the spectrum, these colors are largely transmitted, and we perceive the color of $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ to be red-violet. In general, the color that we see is complementary to the color absorbed (Figure 20.26).

FIGURE 20.26 Using an artist's color wheel, we can determine the observed color of a substance from the color of the light absorbed. Complementary colors are shown on opposite sides of the color wheel, and an approximate wavelength range for each color is indicated. Observed and absorbed colors are generally complementary. For example, if a complex absorbs only red light of 720 nm wavelength, it has a green color.


### 20.11 Bonding in Complexes: Valence Bond Theory

According to the valence bond theory (Section 7.10), the bonding in metal complexes arises when a filled ligand orbital containing a pair of electrons overlaps a vacant hybrid orbital on the metal ion to give a coordinate covalent bond:


Vacant metal hybrid atomic orbital
 atomic orbital

Coordinate covalent bond

The hybrid orbitals (Sections 7.11 and 7.12) that a metal ion uses to accept a share in the ligand electrons are those that point in the directions of the ligands.

Remember that geometry and hybridization go together. Once you know the geometry of a complex, you automatically know which hybrid orbitals the metal ion uses. The relationship between the geometry of a complex and the hybrid orbitals used by the metal ion is summarized in Table 20.7.

TABLE 20.7 Hybrid Orbitals for Common Coordination Geometries

| Coordination <br> Number Geometry Hybrid <br> Orbitals | Example |  |  |
| :--- | :--- | :--- | :--- |
| 2 | Linear | $s p$ | $\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}\right]^{+}$ |
| 4 | Tetrahedral | $s p^{3}$ | $\left.[\mathrm{CoCl}]_{4}\right]^{-}$ |
| 4 | Square planar | $d s p^{2}$ | $\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$ |
| 6 | Octahedral | $d^{2} s p^{3}$ or $s p^{3} d^{2}$ | $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+},\left[\mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ |

To illustrate the relationship between geometry and hybridization, let's consider the tetrahedral complex $\left[\mathrm{CoCl}_{4}\right]^{2-}$. A free $\mathrm{Co}^{2+}$ ion has the electron configuration $[\operatorname{Ar}] 3 d^{7}$, and its orbital diagram is

$$
\mathrm{Co}^{2+}:[\mathrm{Ar}] \frac{\uparrow \downarrow}{\uparrow \downarrow} \frac{\uparrow}{3 d} \xrightarrow{\uparrow} \frac{\uparrow}{4 s} \quad-\frac{}{4 p}-
$$

Because the geometry of $\left[\mathrm{CoCl}_{4}\right]^{2-}$ is tetrahedral, the hybrid orbitals that $\mathrm{Co}^{2+}$ uses to accept a share in the four pairs of ligand electrons must be $s p^{3}$ hybrids formed from the vacant $4 s$ and $4 p$ orbitals. The following orbital diagram represents the bonding in the complex, showing the hybridization of the metal orbitals and the four pairs of ligand electrons, now shared in the bonds between the metal and the ligands:

$$
\left[\mathrm{CoCl}_{4}\right]^{2-:}:[\mathrm{Ar}] \stackrel{\uparrow \downarrow}{ } \frac{\uparrow \downarrow}{3 d} \uparrow \uparrow \begin{array}{|ccc}
\frac{\uparrow \downarrow}{4 s} & \frac{\uparrow \downarrow}{} \frac{\uparrow \downarrow}{4 p} \frac{\uparrow \downarrow}{} \\
\text { Four } s p^{3} \text { bonds to the ligands }
\end{array}
$$

In accord with this description, $\left[\mathrm{CoCl}_{4}\right]^{2-}$ has three unpaired electrons and is paramagnetic. Recall from Section 7.14 that paramagnetic substances contain unpaired electrons and are attracted by magnetic fields, whereas diamagnetic substances contain only paired electrons and are weakly repelled by magnetic fields. The number of unpaired electrons in a transition metal complex can be determined by quantitatively measuring the force exerted on the complex by a magnetic field.

As an example of a square planar complex, consider $\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$. A free $\mathrm{Ni}^{2+}$ ion has eight $3 d$ electrons, two of which are unpaired in accord with Hund's rule (Section 5.12):

$$
\mathrm{Ni}^{2+}:[\mathrm{Ar}] \uparrow \downarrow \uparrow \downarrow \frac{\uparrow \downarrow}{3 d} \uparrow \xlongequal{\uparrow} \quad \overline{4 s} \quad-\frac{\overline{4 p}}{4 p}-
$$

In square planar complexes, the metal uses a set of four hybrid orbitals called $d s p^{2}$ hybrids, which point toward the four corners of a square. By pairing up the two unpaired $d$ electrons in one $d$ orbital, we obtain a vacant $3 d$ orbital that can be hybridized with the $4 s$ orbital and two of the $4 p$ orbitals to give the square planar $d s p^{2}$ hybrids. These hybrids form bonds to the ligands by accepting a share in the four pairs of ligand electrons:

$$
\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}:[\mathrm{Ar}] \frac{\uparrow \downarrow}{\square} \frac{\uparrow \downarrow}{3 d} \frac{\uparrow \downarrow}{\frac{\uparrow \downarrow}{\frac{\uparrow \downarrow}{4 s}} \frac{\uparrow \downarrow}{} \frac{\uparrow \downarrow}{} \frac{\uparrow \downarrow}{4 p}}-
$$

In agreement with this description, $\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$ is diamagnetic.
In octahedral complexes, the metal ion uses either $s p^{3} d^{2}$ or $d^{2} s p^{3}$ hybrid orbitals. To see the difference between these two kinds of hybrids, let's consider

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VThe number of hybrid orbitals used by a metal ion in a coordination complex equals the number of atomic orbitals from which the hybrid orbitals were formed and equals the number of ligand donor atoms.

$\square$
Although both have a coordination number of four, the metal ions in square planar and tetrahedral complexes require different hybrid orbitals because of the differences in the orientation of the ligands.
the cobalt(III) complexes $\left[\mathrm{CoF}_{6}\right]^{3-}$ and $\left[\mathrm{Co}(\mathrm{CN})_{6}\right]^{3-}$. A free $\mathrm{Co}^{3+}$ ion has six $3 d$ electrons, four of which are unpaired:

$$
\mathrm{Co}^{3+}:[\mathrm{Ar}] \underline{\downarrow} \uparrow \frac{\uparrow}{3 d} \uparrow \uparrow \quad \overline{4 s} \quad-\frac{1}{4 p}-\quad-\quad \frac{\overline{4 d}}{-}
$$

Magnetic measurements indicate that $\left[\mathrm{CoF}_{6}\right]^{3-}$ is paramagnetic and contains four unpaired electrons. Evidently, none of the $3 d$ orbitals is available to accept a share in the ligand electrons because each is already at least partially occupied. Consequently, the octahedral hybrids that $\mathrm{Co}^{3+}$ uses are formed from the vacant $4 s, 4 p$, and $4 d$ orbitals. These orbitals, called $s p^{3} d^{2}$ hybrids, share in the six pairs of ligand electrons, as shown in the following orbital diagram:
$\left[\mathrm{CoF}_{6}\right]^{3-}:[\mathrm{Ar}] \underline{\uparrow} \downarrow \frac{\uparrow}{3 d} \xlongequal{\uparrow}$


In contrast to $\left[\mathrm{CoF}_{6}\right]^{3-}$, magnetic measurements indicate that $\left[\mathrm{Co}(\mathrm{CN})_{6}\right]^{3-}$ is diamagnetic. All six $3 d$ electrons are therefore paired and occupy just three of the five $3 d$ orbitals. That leaves two vacant $3 d$ orbitals, which combine with the vacant $4 s$ and $4 p$ orbitals to give a set of six octahedral hybrid orbitals called $d^{2} s p^{3}$ hybrids. The $d^{2} s p^{3}$ hybrids form bonds to the ligands by accepting a share in the six pairs of ligand electrons:

The difference between $d^{2} s p^{3}$ and $s p^{3} d^{2}$ hybrids lies in the principal quantum number of the $d$ orbitals. In $d^{2} s p^{3}$ hybrids, the principal quantum number of the $d$ orbitals is one less than the principal quantum number of the $s$ and $p$ orbitals. In $s p^{3} d^{2}$ hybrids, the $s, p$, and $d$ orbitals have the same principal quantum number. To determine which set of hybrids is used in any given complex, we must know the magnetic properties of the complex.

Complexes of metals like $\mathrm{Co}^{3+}$ that exhibit more than one spin state are classified as high-spin or low-spin. A high-spin complex, such as $\left[\mathrm{CoF}_{6}\right]^{3-}$, is one in which the $d$ electrons are arranged according to Hund's rule to give the maximum number of unpaired electrons. A low-spin complex, such as $\left[\mathrm{Co}(\mathrm{CN})_{6}\right]^{3-}$, is one in which the $d$ electrons are paired up to give a maximum number of doubly occupied $d$ orbitals and a minimum number of unpaired electrons.

## Worked Example 20.10

Give a valence bond description of the bonding in $\left[\mathrm{V}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$. Include orbital diagrams for the free metal ion and the metal ion in the complex. Tell which hybrid orbitals the metal ion uses and the number of unpaired electrons present.

## Strategy and Solution

The free $\mathrm{V}^{3+}$ ion has the electron configuration $[\mathrm{Ar}] 3 d^{2}$ and the orbital diagram

$$
\mathrm{V}^{3+}:[\mathrm{Ar}] \uparrow \xlongequal{3 d}--\overline{4 s} \quad-\frac{}{4 p}-
$$

Because $\left[\mathrm{V}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$ is octahedral, the $\mathrm{V}^{3+}$ ion must use either $d^{2} s p^{3}$ or $s p^{3} d^{2}$ hybrid orbitals in accepting a share in six pairs of electrons from the six $\mathrm{NH}_{3}$ ligands. The preferred hybrids are $d^{2} s p^{3}$ because several $3 d$ orbitals are vacant and $d^{2} s p^{3}$ hybrids have

lower energy than $s p^{3} d^{2}$ hybrids (because the $3 d$ orbitals have lower energy than the $4 d$ orbitals). Thus, $\left[\mathrm{V}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$ has the following orbital diagram:

The complex has two unpaired electrons and is therefore paramagnetic.

- PROBLEM 20.13 Give a valence bond description of the bonding in each of the following complexes. Include orbital diagrams for the free metal ion and the metal ion in the complex. Tell which hybrid orbitals the metal ion uses and the number of unpaired electrons in each complex.
(a) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ (low-spin)
(b) $\left[\mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ (high-spin)
(c) $\left[\mathrm{VCl}_{4}\right]^{-}$(tetrahedral)
(d) $\left[\mathrm{PtCl}_{4}\right]^{2-}$ (square planar)


### 20.12 Crystal Field Theory

Valence bond theory helps us visualize the bonding in complexes, but it doesn't account for their color or explain why some complexes are high-spin whereas others are low-spin. To explain these properties, we turn to the crystal field theory, a model that views the bonding in complexes as arising from electrostatic interactions and considers the effect of the ligand charges on the energies of the metal ion $d$ orbitals. This model was first applied to transition metal ions in ionic crystals-hence the name crystal field theory-but it also applies to metal complexes where the "crystal field" is the electric field due to the charges or dipoles of the ligands.

## Octahedral Complexes

Let's first consider an octahedral complex such as $\left[\mathrm{TiF}_{6}\right]^{3-}$ (Figure 20.27). According to crystal field theory, the bonding is ionic and involves electrostatic attraction between the positively charged $\mathrm{Ti}^{3+}$ ion and the negatively charged $\mathrm{F}^{-}$ ligands. Of course, the $\mathrm{F}^{-}$ligands repel one another, which is why they adopt the geometry (octahedral) that locates them as far apart from one another as possible. Because the metal-ligand attractions are greater than the ligand-ligand repulsions, the complex is more stable than the separated ions, thus accounting for the bonding.

Note the differences between crystal field theory and valence bond theory. In crystal field theory, there are no covalent bonds, no shared electrons, and no hybrid orbitals-just electrostatic interactions within an array of ions. In complexes that contain neutral dipolar ligands, such as $\mathrm{H}_{2} \mathrm{O}$ or $\mathrm{NH}_{3}$, the electrostatic interactions are of the ion-dipole type (Section 10.2). For example, in $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$, the $\mathrm{Ti}^{3+}$ ion attracts the negative end of the water dipoles.

To explain why complexes are colored, we need to look at the effect of the ligand charges on the energies of the $d$ orbitals. Recall that four of the $d$ orbitals are shaped like a cloverleaf, and the fifth $\left(d_{z^{2}}\right)$ is shaped like a dumbbell inside a donut (Section 5.8). Figure 20.28 shows the spatial orientation of the $d$ orbitals with respect to an octahedral array of charged ligands located along the $x, y$, and $z$ coordinate axes.

Because the $d$ electrons are negatively charged, they are repelled by the negatively charged ligands. Thus, their orbital energies are higher in the complex than in the free metal ion. But not all the $d$ orbitals are raised in energy by the same

vCrystal field theory is an electrostatic model. Valence bond theory is an orbital overlap model.


A FIGURE 20.27 Crystal field model of the octahedral $\left[\mathrm{TiF}_{6}\right]^{3-}$ complex. The metal ion and ligands are regarded as charged particles held together by electrostatic attraction. The ligands lie along the $\pm x, \pm y$, and $\pm z$ directions.

A FIGURE 20.28 The shapes of the five $d$ orbitals and their orientation with respect to an octahedral array of charged ligands. The lobes of the orbitals indicate the regions of space where a $d$ electron is most likely to be found.

amount. As shown in Figure 20.29, the $d_{z^{2}}$ and $d_{x^{2}-y^{2}}$ orbitals, which point directly at the ligands, are raised in energy to a greater extent than the $d_{x y}, d_{x z}$, and $d_{y z}$ orbitals, which point between the ligands. This energy splitting between the two sets of $d$ orbitals is called the crystal field splitting and is represented by the Greek letter $\Delta$.


In general, the crystal field splitting energy $\Delta$ corresponds to wavelengths of light in the visible region of the spectrum, and the colors of complexes can therefore be attributed to electronic transitions between the lower- and higher-energy sets of $d$ orbitals. Consider, for example, $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$, a complex that contains a single $d$ electron ( $\mathrm{Ti}^{3+}$ has the electron configuration [Ar] $3 d^{1}$ ). In the groundenergy state, the $d$ electron occupies one of the lower-energy orbitals- $x y, x z$, or $y z$ (from now on we'll denote the $d$ orbitals by their subscripts). When
$\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ absorbs blue-green light with a wavelength of about 500 nm , the absorbed energy promotes the $d$ electron to one of the higher-energy orbitals, $z^{2}$ or $x^{2}-y^{2}$ :

We can calculate the value of $\Delta$ from the wavelength of the absorbed light, about 500 nm for $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ :

$$
\Delta=h \nu=\frac{h c}{\lambda}=\frac{\left(6.626 \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s}\right)\left(3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}\right)}{500 \times 10^{-9} \mathrm{~m}}=3.98 \times 10^{-19} \mathrm{~J}
$$

This is the energy needed to excite a single $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ ion. To express $\Delta$ on a per-mole basis, we multiply by Avogadro's number:

$$
\begin{aligned}
\Delta & =\left(3.98 \times 10^{-19} \frac{\mathrm{~J}}{\text { ion }}\right)\left(6.02 \times 10^{23} \frac{\text { ions }}{\mathrm{mol}}\right) \\
& =2.40 \times 10^{5} \mathrm{~J} / \mathrm{mol}=240 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

The absorption spectra of different complexes indicate that the size of the crystal field splitting depends on the nature of the ligands. For example, $\Delta$ for $\mathrm{Ni}^{2+}\left([\mathrm{Ar}] 3 d^{8}\right)$ complexes increases as the ligand varies from $\mathrm{H}_{2} \mathrm{O}$ to $\mathrm{NH}_{3}$ to ethylenediamine (en). Accordingly, the electronic transitions shift to higher energy (shorter wavelength) as the ligand varies from $\mathrm{H}_{2} \mathrm{O}$ to $\mathrm{NH}_{3}$ to en, thus accounting for the observed variation in color (Figure 20.24):


In general, the crystal field splitting increases as the ligand varies in the following order, known as the spectrochemical series:

$$
\text { Weak-field ligands } \mathrm{I}^{-}<\mathrm{Br}^{-}<\mathrm{Cl}^{-}<\mathrm{F}^{-}<\mathrm{H}_{2} \mathrm{O}<\mathrm{NH}_{3}<\mathrm{en}<\mathrm{CN}^{-} \text {Strong-field ligands }
$$

## Increasing $\Delta$

Ligands such as halides and $\mathrm{H}_{2} \mathrm{O}$, which give a relatively small value of $\Delta$, are called weak-field ligands. Ligands such as $\mathrm{NH}_{3}$, en, and $\mathrm{CN}^{-}$, which produce a relatively large value of $\Delta$, are known as strong-field ligands. Different metal ions have different values of $\Delta$, which explains why their complexes with the same ligand have different colors (Figure 20.23). Because $d^{0}$ ions such as $\mathrm{Ti}^{4+}, d^{10}$ ions such as $\mathrm{Zn}^{2+}$, and main-group ions don't have partially filled $d$ subshells, they can't undergo $d-d$ electronic transitions, and most of their compounds are therefore colorless.

Crystal field theory accounts for the magnetic properties of complexes as well as for their color. It explains, for example, why complexes with weak-field ligands,


Crystal Field Theory activity

0
The stronger the interaction between a ligand and a metal ion, the greater the crystal field splitting, $\Delta$, and the higher the energy (and the shorter the wavelength) of light absorbed by the complex.

vThe strong-field ligands $\mathrm{CN}^{-}$ and CO are toxic to humans because of their strong interactions with iron in cytochrome oxidase and hemoglobin, respectively.
such as $\left[\mathrm{CoF}_{6}\right]^{3-}$, are high-spin, whereas related complexes with strong-field ligands, such as $\left[\mathrm{Co}(\mathrm{CN})_{6}\right]^{3-}$, are low-spin. In $\left[\mathrm{CoF}_{6}\right]^{3-}$, the six $d$ electrons of $\mathrm{Co}^{3+}\left([\mathrm{Ar}] 3 d^{6}\right)$ occupy both the higher- and lower-energy $d$ orbitals, whereas in $\left[\mathrm{Co}(\mathrm{CN})_{6}\right]^{3-}$, all six $d$ electrons are spin-paired in the lower-energy orbitals:

What determines which of the two spin states has the lower energy? In general, when an electron moves from a $z^{2}$ or $x^{2}-y^{2}$ orbital to one of the lowerenergy orbitals, the orbital energy decreases by $\Delta$. But because of electron-electron repulsion, it costs energy to put the electron into an orbital that already contains another electron. The energy required is called the spin-pairing energy $P$. If $\Delta$ is greater than $P$, as it is for $\left[\mathrm{Co}(\mathrm{CN})_{6}\right]^{3-}$, then the low-spin arrangement has lower energy. If $\Delta$ is less than $P$, as it is for $\left[\mathrm{CoF}_{6}\right]^{3-}$, the high-spin arrangement has lower energy. Thus, the observed spin state depends on the relative values of $\Delta$ and $P$. In general, strong-field ligands give low-spin complexes, and weak-field ligands give high-spin complexes.

A choice between high-spin and low-spin electron configurations arises only for complexes of metal ions with four to seven $d$ electrons, so-called $d^{4}-d^{7}$ complexes. For $d^{1}-d^{3}$ and $d^{8}-d^{10}$ complexes, only one ground-state electron configuration is possible. In $d^{1}-d^{3}$ complexes, all the electrons occupy the lower-energy $d$ orbitals, independent of the value of $\Delta$. In $d^{8}-d^{10}$ complexes, the lower-energy set of $d$ orbitals is filled with three pairs of electrons, while the higher-energy set contains two, three, or four electrons, again independent of the value of $\Delta$.

## Worked Example 20.11

Draw a crystal field orbital energy-level diagram, and predict the number of unpaired electrons for each of the following complexes:
(a) $\left[\mathrm{Cr}(\mathrm{en})_{3}\right]^{3+}$
(b) $\left[\mathrm{Mn}(\mathrm{CN})_{6}\right]^{3-}$
(c) $\left[\mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$

## Strategy

All three complexes are octahedral, so the energy-level diagrams will show three lowerenergy and two higher-energy $d$ orbitals. For $d^{1}-d^{3}$ and $d^{8}-d^{10}$ complexes, the electrons occupy the orbitals in accord with Hund's rule so as to give the maximum number of unpaired electrons. For $d^{4}-d^{7}$ complexes, the orbital occupancy and number of unpaired electrons depend on the position of the ligand in the spectrochemical series.

## SOlUTION

(a) $\mathrm{Cr}^{3+}\left([\mathrm{Ar}] 3 d^{3}\right)$ has three unpaired electrons. In the complex, they occupy the lower-energy set of $d$ orbitals.
(b) $\mathrm{Mn}^{3+}\left([\mathrm{Ar}] 3 d^{4}\right)$ can have a high-spin or low-spin configuration. Because $\mathrm{CN}^{-}$is a strong-field ligand, all four $d$ electrons go into the lower-energy $d$ orbitals. The complex is low-spin, with two unpaired electrons.
(c) $\mathrm{Co}^{2+}\left([\mathrm{Ar}] 3 d^{7}\right)$ has a high-spin configuration with three unpaired electrons because $\mathrm{H}_{2} \mathrm{O}$ is a weak-field ligand.

In the following orbital energy-level diagrams, the relative values of the crystal field splitting $\Delta$ agree with the positions of the ligands in the spectrochemical series $\left(\mathrm{H}_{2} \mathrm{O}<\right.$ en $\left.<\mathrm{CN}^{-}\right)$:


- PROBLEM 20.14 Draw a crystal field $d$-orbital energy-level diagram, and predict the number of unpaired electrons for each of the following complexes:
(a) $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$
(b) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4-}$
(c) $\left[\mathrm{VF}_{6}\right]^{3-}$
(d) $\left[\mathrm{Ni}(\mathrm{en})_{3}\right]^{2+}$


## Tetrahedral and Square Planar Complexes

Different geometric arrangements of the ligands give different energy splittings for the $d$ orbitals. Figure 20.30 shows $d$-orbital energy-level diagrams for tetrahedral and square planar complexes.


The splitting pattern in tetrahedral complexes is just the opposite of that in octahedral complexes; that is, the $x y, x z$, and $y z$ orbitals have higher energy than the $x^{2}-y^{2}$ and $z^{2}$ orbitals. (As with octahedral complexes, the energy ordering follows from the relative orientation of the orbital lobes and the ligands, but we won't try to derive the result.) Because none of the orbitals points directly at the ligands in tetrahedral geometry, and because there are only four ligands instead of six, the crystal field splitting in tetrahedral complexes is only about half of that in octahedral complexes. Consequently, $\Delta$ is almost always smaller than the spinpairing energy $P$, and nearly all tetrahedral complexes are high-spin.

Square planar complexes look like octahedral ones (Figure 20.28) except that the two trans ligands along the $z$ axis are missing. In square planar complexes, the $x^{2}-y^{2}$ orbital is high in energy (Figure 20.30) because it points directly at all four ligands, which lie along the $x$ and $y$ axes. The splitting pattern is more complicated here than for the octahedral and tetrahedral cases, but the main point to remember is that a large energy gap exists between the $x^{2}-y^{2}$ orbital and the four lower-energy orbitals. Square planar geometry is most common for metal


4 FIGURE 20.30 Energies of the $d$ orbitals in tetrahedral and square planar complexes relative to their energy in the free metal ion. The crystal field splitting energy $\Delta$ is small in tetrahedral complexes but much larger in square planar complexes.


$\sqrt{ }$
Almost all tetrahedral complexes are high-spin, and square planar complexes are low-spin. Octahedral complexes can be either low-spin or high-spin.
ions with electron configuration $d^{8}$ because this configuration favors low-spin complexes in which all four lower-energy orbitals are filled and the higherenergy $x^{2}-y^{2}$ orbital is vacant. Common examples are $\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-},\left[\mathrm{PdCl}_{4}\right]^{2-}$, and $\operatorname{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$.

## Worked Example 20.12

Draw crystal field energy-level diagrams and predict the number of unpaired electrons for the following complexes:
(a) $\left[\mathrm{FeCl}_{4}\right]^{-}$(tetrahedral)
(b) $\left[\mathrm{PtCl}_{4}\right]^{2-}$ (square planar)

## Strategy

Begin with the energy-level diagrams in Figure 20.30, and remember that nearly all tetrahedral complexes are high-spin (small $\Delta$ ) while square planar complexes have a large energy gap (large $\Delta$ ) between the $x^{2}-y^{2}$ orbital and the four lower-energy orbitals.

## Solution

(a) The five $d$ electrons of $\mathrm{Fe}^{3+}\left([\mathrm{Ar}] 3 d^{5}\right)$ are distributed between the higher- and lower-energy orbitals as shown below. Because $\Delta$ is small in tetrahedral complexes, $\left[\mathrm{FeCl}_{4}\right]^{-}$is high-spin with five unpaired electrons.

(b) $\mathrm{Pt}^{2+}\left([\mathrm{Xe}] 4 f^{14} 5 d^{8}\right)$ has eight $d$ electrons. Because $\Delta$ is large in square planar complexes, all the electrons occupy the four lower-energy $d$ orbitals. There are no unpaired electrons, and the complex is diamagnetic.
-

$$
\left[\mathrm{FeCl}_{4}\right]^{-}
$$

$$
\left[\mathrm{PtCl}_{4}\right]^{2-}
$$

PROBLEM 20.15 Draw a crystal field energy-level diagram, and predict the number of unpaired electrons for the following complexes:
(a) $\left[\mathrm{NiCl}_{4}\right]^{2-}$ (tetrahedral)
(b) $\left[\mathrm{Ni}(\mathrm{CN})_{4}\right]^{2-}$ (square planar)

## Interlude <br> Titanium: A High-Tech Metal

 metal.

Named after the Titans, Greek mythological figures symbolic of power and strength, titanium is the ninth most abundant element in the earth's crust ( $0.57 \%$ by mass). It occurs in rutile $\left(\mathrm{TiO}_{2}\right)$ and in the mineral ilmenite $\left(\mathrm{FeTiO}_{3}\right)$, found in the United States, Australia, Canada, Malaysia, and elsewhere. Despite its abundance, titanium is difficult and expensive to produce in its pure form, and it remained a curiosity until about 1950, when its potential applications in aerospace technology were recognized.

Titanium is a superb structural material because of its hardness, strength, heat resistance ( $\mathrm{mp} 1668^{\circ} \mathrm{C}$ ), and relatively low density $\left(4.51 \mathrm{~g} / \mathrm{cm}^{3}\right)$. Titanium is just as strong as steel, but $45 \%$ lighter; titanium is twice as strong as aluminum but only $60 \%$ heavier. When alloyed with a few percent aluminum and vanadium, titanium has a higher strength-to-weight ratio than any other engineering metal.
These properties make titanium an ideal choice in aerospace applications, such as airframes and jet engines, as well as for recreational use. (Those who can afford one rave about the ride and feel of a titanium bike frame.)

Although titanium has a large positive $E^{\circ}$ for oxidation, and Ti dust will burn in air, the bulk metal is remarkably immune to corrosion because its surface becomes coated with a thin, protective oxide film. Titanium objects are inert to seawater, nitric acid, hot aqueous NaOH , and even to aqueous chlorine gas. Titanium is therefore used in chemical plants, in desalination equipment, and in numerous other industrial processes that demand inert, noncorrosive materials. Because it is nontoxic and inert to body fluids, titanium is even used for manufacturing artificial joints and dental implants.

Pure titanium is obtained commercially from rutile $\left(\mathrm{TiO}_{2}\right)$ by an indirect route in which $\mathrm{TiO}_{2}$ reacts with $\mathrm{Cl}_{2}$ gas and coke to yield liquid $\mathrm{TiCl}_{4}\left(\right.$ bp $136^{\circ} \mathrm{C}$ ), which is purified by fractional distillation. Subsequent reduction to Ti metal is then carried out by reaction with molten magnesium at $900^{\circ} \mathrm{C}$, and further purification is effected by melting the titanium in an electric arc under an atmosphere of argon.

$$
\begin{aligned}
& \mathrm{TiO}_{2}(s)+2 \mathrm{Cl}_{2}(g)+2 \mathrm{C}(s) \longrightarrow \mathrm{TiCl}_{4}(l)+2 \mathrm{CO}(g) \\
& \mathrm{TiCl}_{4}(g)+2 \mathrm{Mg}(l) \longrightarrow \mathrm{Ti}(s)+2 \mathrm{MgCl}_{2}(l)
\end{aligned}
$$

Although the process is extremely expensive and energy-intensive, the cost of producing titanium is justified because of its unique properties. Worldwide production of titanium now exceeds 100,000 tons per year.

- PROBLEM $20.16 E^{\circ}$ values for the oxidation of the metal to the $\mathrm{M}^{3+}(a q)$ ion are +1.37 V for $\mathrm{M}=\mathrm{Ti}$ and +0.04 V for $\mathrm{M}=\mathrm{Fe}$. Why, then, doesn't titanium corrode?

PROBLEM 20.17 How many liters of $\mathrm{Cl}_{2}$ at $20^{\circ} \mathrm{C}$ and 740 mm Hg pressure would be needed to produce $1.00 \times 10^{5}$ tons of titanium metal from $\mathrm{TiO}_{2}$ if the overall yield is $93.5 \%$ ?

Transition elements (d-block elements) are the metallic elements in the central part of the periodic table. Most of the neutral atoms have valence electron configuration $(n-1) d^{1-10} n s^{2}$, and the cations have configuration $(n-1) d^{1-10}$. Transition metals exhibit a variety of oxidation states. Ions with the metal in a high oxidation state tend to be good oxidizing agents $\left(\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}, \mathrm{MnO}_{4}^{-}\right)$, and ions with the metal in a low oxidation state are good reducing agents $\left(\mathrm{V}^{2+}, \mathrm{Cr}^{2+}\right)$.

Coordination compounds (metal complexes) are compounds in which a central metal ion is attached to a group of surrounding ligands by coordinate covalent bonds. Ligands can be monodentate or polydentate, depending on the number of donor atoms attached to the metal. Polydentate ligands are also called chelating agents. They form complexes (metal chelates) that contain rings of atoms known as chelate rings.

The number of ligand donor atoms bonded to a metal is called the coordination number of the metal. Common coordination numbers and geometries are 2 (linear), 4 (tetrahedral or square planar), and 6 (octahedral). Systematic names for complexes specify the number of ligands of each particular type, the metal, and its oxidation state.

Many complexes exist as isomers, compounds that have the same formula but a different arrangement of the constituent atoms. Constitutional isomers, such as linkage isomers and ionization isomers, have different connections between their constituent atoms. Stereoisomers (diastereoisomers and enantiomers) have the same connections but a different arrangement of the atoms in space. The most common diastereoisomers are cis and trans isomers of square planar $\mathrm{MA}_{2} \mathrm{~B}_{2}$ and octahe-
dral $\mathrm{MA}_{4} \mathrm{~B}_{2}$ complexes. Enantiomers, such as "right-handed" and "left-handed" $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$, are nonidentical mirror images. One isomer rotates the plane of plane-polarized light to the right, and the other rotates this plane through an equal angle but in the opposite direction. A 1:1 mixture of the two isomers is called a racemic mixture. Molecules that have handedness are said to be chiral. All other molecules are achiral.

Valence bond theory describes the bonding in complexes in terms of two-electron, coordinate covalent bonds resulting from the overlap of filled ligand orbitals with vacant metal hybrid orbitals that point in the direction of the ligands: $s p$ (linear), $s p^{3}$ (tetrahedral), $d s p^{2}$ (square planar), and $d^{2} s p^{3}$ or $s p^{3} d^{2}$ (octahedral).

Crystal field theory assumes that the metal-ligand bonding is entirely ionic. Because of electrostatic repulsions between the $d$ electrons and the ligands, the $d$ orbitals are raised in energy and are differentiated by an energy separation called the crystal field splitting, $\Delta$. In octahedral complexes, the $z^{2}$ and $x^{2}-y^{2}$ orbitals have higher energy than the $x y, x z$, and $y z$ orbitals. Tetrahedral and square planar complexes exhibit different splitting patterns. The colors of complexes are due to electronic transitions from one set of $d$ orbitals to another, and the transition energies depend on the position of the ligand in the spectrochemical series. Weak-field ligands give small $\Delta$ values, and strong-field ligands give large $\Delta$ values. Crystal field theory accounts for the magnetic properties of complexes in terms of the relative values of $\Delta$ and the spin-pairing energy $P$. Small $\Delta$ values favor high-spin complexes, and large $\Delta$ values favor low-spin complexes.

## Key Words

```
absorption spectrum 894
achiral 891
bidentate 878
chelate 880
chelate ring 880
chelating agent 880
chiral 890
cis isomer 886
constitutional isomer 885
coordination compound 876
```

coordination number 877
crystal field splitting ( $\Delta$ ) 898
crystal field theory 897
diastereoisomer 886
donor atom 876
enantiomer 890
geometric isomer 886
hexadentate 880
high-spin complex 896
ionization isomer 885
isomer 884
lanthanide contraction 868
ligand 876
linkage isomer 885
low-spin complex 896
metal complex 877
monodentate 878
polydentate 878
racemic mixture 892
spectrochemical series 899
stereoisomer 885 strong-field ligand 899
symmetry plane 891
trans isomer 886
transition element 863
valence bond theory 894
weak-field ligand 899

## Key Concept Summary



## Understanding Key Concepts

Problems 20.1-20.17 appear within the chapter.
20.18 Locate on the periodic table below the transition elements with the following electron configurations. Identify each element.
(a) $[\mathrm{Ar}] 3 d^{7} 4 s^{2}$
(b) $[\mathrm{Ar}] 3 d^{5} 4 s^{1}$
(c) $[\mathrm{Kr}] 4 d^{2} 5 s^{2}$
(d) $[\mathrm{Xe}] 4 f^{3} 6 s^{2}$

20.19 What is the general trend in the following properties from left to right across the first transition series (Sc to Zn )? Explain each trend.
(a) Atomic radius
(b) Density
(c) Ionization energy
(d) Standard oxidation potential

| Sc | Ti | V | Cr | Mn | Fe | Co | Ni | Cu | Zn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

20.21 Draw the structure of the following complexes. What are the oxidation state, coordination number, and coordination geometry of the metal in each?
(a) $\mathrm{Na}\left[\mathrm{Au}(\mathrm{CN})_{2}\right]$
(b) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}^{2} \mathrm{SO}_{4}\right.$
(c) $\mathrm{Pt}(\mathrm{en}) \mathrm{Cl}_{2}$
(d) $\left(\mathrm{NH}_{4}\right)_{2}\left[\mathrm{PtCl}_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right]$
20.22 Consider the following isomers of $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{4}\right]^{-}$:
T/
(1)
(1)

$=\mathrm{NH}_{3}$
$=\mathrm{Cl}$

(2)

(3)

(4)
(a) Label the isomers as cis or trans.
(b) Which isomers are identical, and which are different?
(c) Do any of these isomers exist as enantiomers? Explain.
20.20 Classify the following ligands as monodentate, biden-tate, or tridentate. Which can form chelate rings?

(a) $\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}$

(b) $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}$

(c) $\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NHCH}_{2} \mathrm{CO}_{2}^{-}$

(d) $\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{3}{ }^{+}$
20.23 Consider the following ethylenediamine complexes:
-
$O=\mathrm{Cr}$

(1)



(2)

(3)

(4)
(a) Which complexes are chiral, and which are achiral?
(b) Draw the enantiomer of each chiral complex.
(c) Which, if any, of the chiral complexes are enantiomers of one another?
20.24 Predict the crystal field energy-level diagram for a square pyramidal $\mathrm{ML}_{5}$ complex that has two ligands along the $\pm x$ and $\pm y$ axes but only one ligand along the $z$ axis. Your diagram should be intermediate between those for an octahedral $\mathrm{ML}_{6}$ complex and a square planar $\mathrm{ML}_{4}$ complex.


20.25 Imagine two complexes, one tetrahedral and one square planar, in which the central atom is bonded to four different ligands (shown here in four different colors). Is either complex chiral? Explain.


## Additional Problems

## Electron Configurations and Properties of Transition Elements

20.26 Use the periodic table to give the electron configuration for each of the following atoms and ions:
(a) Cr
(b) Zr
(c) $\mathrm{Co}^{2+}$
(d) $\mathrm{Fe}^{3+}$
(e) $\mathrm{Mo}^{3+}$
(f) $\mathrm{Cr}(\mathrm{VI})$ in $\mathrm{CrO}_{4}{ }^{2-}$
20.27 Specify the electron configuration for each of the following atoms and ions:
(a) Mn
(b) Cd
(c) $\mathrm{Cr}^{3+}$
(d) $\mathrm{Ag}^{+}$
(e) $\mathrm{Rh}^{3+}$
(f) $\mathrm{Mn}(\mathrm{VI})$ in $\mathrm{MnO}_{4}{ }^{2-}$
20.28 Predict the number of unpaired electrons for each of the following:
(a) $\mathrm{Cu}^{2+}$
(b) $\mathrm{Ti}^{2+}$
(c) $\mathrm{Zn}^{2+}$
(d) $\mathrm{Cr}^{3+}$
20.29 Predict the number of unpaired electrons for each of the following:
(a) $\mathrm{Sc}^{3+}$
(b) $\mathrm{Co}^{2+}$
(c) $\mathrm{Mn}^{3+}$
(d) $\mathrm{Cr}^{2+}$
20.30 Titanium, used to make jet aircraft engines, is much harder than potassium or calcium. Explain.
20.31 Molybdenum (mp $2623^{\circ} \mathrm{C}$ ) has a higher melting point than yttrium ( $\mathrm{mp} 1522^{\circ} \mathrm{C}$ ) or cadmium ( $321^{\circ} \mathrm{C}$ ). Explain.
20.32 Briefly account for each of the following observations:
(a) Atomic radii decrease in the order $\mathrm{Sc}>\mathrm{Ti}>\mathrm{V}$.
(b) Densities increase in the order $\mathrm{Ti}<\mathrm{V}<\mathrm{Cr}$.
20.33 Arrange the following atoms in order of decreasing atomic radii, and account for the trend:
(a) Cr
(b) Ti
(c) Mn
(d) V
20.34 What is the lanthanide contraction, and why does it occur?
20.35 The atomic radii of zirconium and hafnium are nearly identical. Explain.
20.36 Calculate the sum of the first two ionization energies for the first-series transition elements, and account for the general trend.
20.37 What is the general trend in standard potentials for the oxidation of first-series transition metals from Sc to Zn ? What is the reason for the trend?
20.38 Write a balanced net ionic equation for the reaction of each of the following metals with hydrochloric acid in the absence of air. If no reaction occurs, indicate N.R.
(a) Cr
(b) Zn
(c) Cu
(d) Fe
20.39 Write a balanced net ionic equation for the reaction of each of the following metals with dilute sulfuric acid in the absence of air. If no reaction occurs, indicate N.R.
(a) Mn
(b) Ag
(c) Sc
(d) Ni

## Oxidation States

20.40 Which of the following metals have more than one oxidation state?
(a) Zn
(b) Mn
(c) Sr
(d) Cu
20.41 Which of the following metals have only one oxidation state?
(a) V
(b) Al
(c) Co
(d) Sc
20.42 What is the highest oxidation state for each of the elements from Sc to Zn ?
20.43 The highest oxidation state for the early transition metals $\mathrm{Sc}, \mathrm{Ti}, \mathrm{V}, \mathrm{Cr}$, and Mn is the periodic group number. The highest oxidation state for the later transition elements $\mathrm{Fe}, \mathrm{Co}$, and Ni is less than the periodic group number. Explain.
20.44 Which is the stronger oxidizing agent, $\mathrm{Cr}^{2+}$ or $\mathrm{Cu}^{2+}$ ? Explain.
20.45 Which is the stronger reducing agent, $\mathrm{Ti}^{2+}$ or $\mathrm{Ni}^{2+}$ ? Explain.
20.46 Which is more easily oxidized, $\mathrm{Cr}^{2+}$ or $\mathrm{Ni}^{2+}$ ? Explain.
20.47 Which is more easily reduced, $\mathrm{V}^{3+}$ or $\mathrm{Fe}^{3+}$ ? Explain.
20.48 Arrange the following substances in order of increasing strength as an oxidizing agent, and account for the trend:
(a) $\mathrm{Mn}^{2+}$
(b) $\mathrm{MnO}_{2}$
(c) $\mathrm{MnO}_{4}^{-}$
20.49 Arrange the following ions in order of increasing strength as a reducing agent, and account for the trend:
(a) $\mathrm{Cr}^{2+}$
(b) $\mathrm{Cr}^{3+}$
(c) $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}$

## Chemistry of Selected Transition Elements

20.50 Write a balanced equation for the industrial production of:
(a) Chromium metal from chromium(III) oxide
(b) Copper metal from copper(I) sulfide
20.51 Write a balanced net ionic equation for the reaction of nitric acid with:
(a) Iron metal
(b) Copper metal
(c) Chromium metal
20.52 What product is formed when dilute $\mathrm{H}_{2} \mathrm{SO}_{4}$, a nonoxidizing acid, is added to each of the following ions or compounds?
(a) $\mathrm{CrO}_{4}{ }^{2-}$
(b) $\mathrm{Cr}(\mathrm{OH})_{3}$
(c) $\mathrm{Cr}(\mathrm{OH})_{2}$
(d) $\mathrm{Fe}(\mathrm{OH})_{2}$
(e) $\mathrm{Cu}(\mathrm{OH})_{2}$
20.53 What product is formed when excess aqueous NaOH is added to a solution of each of the following ions?
(a) $\mathrm{Cr}^{2+}$
(b) $\mathrm{Cr}^{3+}$
(c) $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}$
(d) $\mathrm{Fe}^{2+}$
(e) $\mathrm{Fe}^{3+}$
20.54 Arrange the following hydroxy compounds in order of increasing acid strength, and account for the trend:
(a) $\mathrm{CrO}_{2}(\mathrm{OH})_{2}$
(b) $\mathrm{Cr}(\mathrm{OH})_{2}$
(c) $\mathrm{Cr}(\mathrm{OH})_{3}$
20.55 Explain how $\mathrm{Cr}(\mathrm{OH})_{3}$ can act both as an acid and as a base.
20.56 Which of the following compounds is amphoteric?
(a) $\mathrm{Cr}(\mathrm{OH})_{2}$
(b) $\mathrm{Fe}(\mathrm{OH})_{2}$
(c) $\mathrm{Cr}(\mathrm{OH})_{3}$
(d) $\mathrm{Fe}(\mathrm{OH})_{3}$
20.57 Which of the following ions disproportionates in aqueous solution? Write a balanced net ionic equation for the reaction.
(a) $\mathrm{Cr}^{3+}$
(b) $\mathrm{Fe}^{3+}$
(c) $\mathrm{Cu}^{+}$
(d) $\mathrm{Cu}^{2+}$
20.58 How might you separate the following pairs of ions by the addition of a single reagent? Include formulas for the major products of the reactions.
(a) $\mathrm{Fe}^{3+}$ and $\mathrm{Na}^{+}$
(b) $\mathrm{Cr}^{3+}$ and $\mathrm{Fe}^{3+}$
(c) $\mathrm{Fe}^{3+}$ and $\mathrm{Cu}^{2+}$
20.59 Give a method for separating the following pairs of ions by the addition of a single reagent. Include formulas for the major products of the reactions.
(a) $\mathrm{K}^{+}$and $\mathrm{Cu}^{2+}$
(b) $\mathrm{Cu}^{2+}$ and $\mathrm{Cr}^{3+}$
(c) $\mathrm{Fe}^{3+}$ and $\mathrm{Al}^{3+}$
20.60 Complete and balance the net ionic equation for each of the following reactions in acidic solution:
(a) $\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q)+\mathrm{Fe}^{2+}(a q) \rightarrow$
(b) $\mathrm{Fe}^{2+}(a q)+\mathrm{O}_{2}(g) \rightarrow$
(c) $\mathrm{Cu}_{2} \mathrm{O}(s)+\mathrm{H}^{+}(a q) \rightarrow$
(d) $\mathrm{Fe}(s)+\mathrm{H}^{+}(a q) \rightarrow$
20.61 Complete and balance the net ionic equation for each of the following reactions in acidic solution:
(a) $\mathrm{Cr}^{2+}(a q)+\mathrm{Cr}_{2} \mathrm{O}_{7}^{2-}(a q) \rightarrow$
(b) $\mathrm{Cu}(s)+$ conc $\mathrm{HNO}_{3}(a q) \rightarrow$
(c) $\mathrm{Cu}^{2+}(a q)+$ excess $\mathrm{NH}_{3}(a q) \rightarrow$
(d) $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}(a q)+$ excess $\mathrm{H}^{+}(a q) \rightarrow$
20.62 Write a balanced net ionic equation for each of the following reactions:
(a) $\mathrm{A} \mathrm{CrO}_{4}{ }^{2-}$ solution turns from yellow to orange upon addition of acid.
(b) $\mathrm{Fe}^{3+}(a q)$ reacts with aqueous KSCN to give a deep red solution.
(c) Copper metal reacts with nitric acid to give NO gas and a blue solution.
(d) A deep green solution of $\mathrm{Cr}(\mathrm{OH})_{3}$ in excess base turns yellow on addition of hydrogen peroxide.
20.63 Write a balanced net ionic equation for each of the following reactions:
(a) $\mathrm{A} \mathrm{CuSO}_{4}$ solution becomes dark blue when excess ammonia is added.
(b) A solution of $\mathrm{Na}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ turns from orange to yellow on addition of base.
(c) When base is added to a solution of $\mathrm{Fe}\left(\mathrm{NO}_{3}\right)_{3}$, a red-brown precipitate forms.
(d) Dissolution of CuS in hot $\mathrm{HNO}_{3}$ gives NO gas, a blue solution, and a yellow solid.

## Coordination Compounds; Ligands

20.64 Forming $\left[\mathrm{Ni}(\mathrm{en})_{3}\right]^{2+}$ from $\mathrm{Ni}^{2+}$ and ethylenediamine is a Lewis acid-base reaction. Explain.
20.65 Identify the Lewis acid and the Lewis base in the reaction of oxalate ions $\left(\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}\right)$ with $\mathrm{Fe}^{3+}$ to give $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$.
20.66 Give an example of a coordination compound in which the metal exhibits a coordination number of:
(a) 2
(b) 4
(c) 6
20.67 What is the coordination number of the metal in each of the following complexes?
(a) $\mathrm{AgCl}_{2}{ }^{-}$
(b) $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{5} \mathrm{Cl}\right]^{2+}$
(c) $\left[\mathrm{Co}(\mathrm{NCS})_{4}\right]^{2-}$
(d) $\left[\mathrm{ZrF}_{8}\right]^{4-}$
(e) $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3}\left(\mathrm{NO}_{2}\right)_{3}$
(f) $\left[\mathrm{Fe}(\mathrm{EDTA})\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{-}$
20.68 What is the oxidation state of the metal in each of the complexes in Problem 20.67?
20.69 Identify the oxidation state of the metal in each of the following complexes:
(a) $\left[\mathrm{Ni}(\mathrm{CN})_{5}\right]^{3-}$
(b) $\mathrm{Ni}(\mathrm{CO})_{4}$
(c) $\left[\mathrm{Co}(\mathrm{en})_{2}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Br}\right]^{2+}$
(d) $\left[\mathrm{Cu}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right]^{2-}$
20.70 What is the formula of a complex that has each of the following geometries?
(a) Tetrahedral
(b) Linear
(c) Octahedral
(d) Square planar
20.71 What is the formula for each of the following complexes?
(a) An iridium(III) complex with three ammonia and three chloride ligands
(b) A chromium(III) complex with two water and two oxalate ligands
(c) A platinum(IV) complex with two ethylenediamine and two thiocyanate ligands
20.72 Draw the structure of the iron oxalate complex $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$. Describe the coordination geometry, and identify any chelate rings. What are the coordination number and the oxidation number of the iron?
20.73 Draw the structure of the platinum ethylenediamine complex $\left[\mathrm{Pt}(\mathrm{en})_{2}\right]^{2+}$. Describe the coordination geometry, and identify any chelate rings. What are the coordination number and the oxidation number of the platinum?
20.74 Identify the oxidation state of the metal in each of the following compounds:
(a) $\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3}\left(\mathrm{NO}_{2}\right)_{3}$
(b) $\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}\right] \mathrm{NO}_{3}$
(c) $\mathrm{K}_{3}\left[\mathrm{Cr}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2} \mathrm{Cl}_{2}\right]$
(d) $\mathrm{Cs}\left[\mathrm{CuCl}_{2}\right]$
20.75 What is the oxidation state of the metal in each of the following compounds?
(a) $\left(\mathrm{NH}_{4}\right)_{3}\left[\mathrm{RhCl}_{6}\right]$
(b) $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{4}(\mathrm{SCN})_{2}\right] \mathrm{Br}$
(c) $\left[\mathrm{Cu}(\mathrm{en})_{2}\right]_{4}$
(d) $\mathrm{Na}_{2}[\mathrm{Mn}(E D T A)]$

## Naming Coordination Compounds

20.76 What is the systematic name for each of the following ions?
(a) $\left[\mathrm{MnCl}_{4}\right]^{2-}$
(b) $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}\right]^{2+}$
(c) $\left[\mathrm{Co}\left(\mathrm{CO}_{3}\right)_{3}\right]^{3-}$
(d) $\left[\mathrm{Pt}(\mathrm{en})_{2}(\mathrm{SCN})_{2}\right]^{2+}$
20.77 Assign a systematic name to each of the following ions:
(a) $\left[\mathrm{AuCl}_{4}\right]^{-}$
(b) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4-}$
(c) $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{5} \mathrm{NCS}\right]^{2+}$
(d) $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{2}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right]^{-}$
20.78 What is the systematic name for each of the following coordination compounds?
(a) $\mathrm{Cs}\left[\mathrm{FeCl}_{4}\right]$
(b) $\left[\mathrm{V}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]\left(\mathrm{NO}_{3}\right)_{3}$
(c) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Br}_{2}\right] \mathrm{Br}$
(d) $\mathrm{Cu}(\text { gly })_{2}$
20.79 What is the systematic name for each of the following compounds?
(a) $\left[\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}\right] \mathrm{SO}_{4}$
(b) $\mathrm{Cr}(\mathrm{CO})_{6}$
(c) $\mathrm{K}_{3}\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]$
(d) $\left[\mathrm{Co}(\mathrm{en})_{2}\left(\mathrm{NH}_{3}\right) \mathrm{CN}\right] \mathrm{Cl}_{2}$
20.80 Write the formula for each of the following compounds:
(a) Tetraammineplatinum(II) chloride
(b) Sodium hexacyanoferrate(III)
(c) Tris(ethylenediamine)platinum(IV) sulfate
(d) Triamminetrithiocyanatorhodium(III)
20.81 Write the formula for each of the following compounds:
(a) Diamminesilver(I) nitrate
(b) Potassium diaquadioxalatocobaltate(III)
(c) Hexacarbonylmolybdenum(0)
(d) Diamminebis(ethylenediamine)chromium(III) chloride

## Isomers

20.82 Draw all possible constitutional isomers of $\left[\mathrm{Ru}\left(\mathrm{NH}_{3}\right)_{5-}\right.$ $\left.\left(\mathrm{NO}_{2}\right)\right] \mathrm{Cl}$. Label the isomers as linkage isomers or ionization isomers.
20.83 There are six possible isomers for a square planar palladium(II) complex that contains two $\mathrm{Cl}^{-}$and two $\mathrm{SCN}^{-}$ligands. Sketch the structures of all six, and label them according to the isomer classification scheme in Figure 20.16.
20.84 Which of the following complexes can exist as diastereoisomers?
(a) $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{4}\right]^{-}$
(b) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{5} \mathrm{Br}\right]^{2+}$
(c) $\left[\mathrm{FeCl}_{2}(\mathrm{NCS})_{2}\right]^{2-}$ (tetrahedral)
(d) $\left[\mathrm{PtCl}_{2} \mathrm{Br}_{2}\right]^{2-}$ (square planar)
20.85 Tell how many diastereoisomers are possible for each of the following complexes, and draw their structures:
(a) $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2}(\mathrm{CN})_{2}$
(b) $\left[\mathrm{Co}(\mathrm{en})(\mathrm{SCN})_{4}\right]^{-}$
(c) $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{4} \mathrm{Cl}_{2}\right]^{+}$
(d) $\mathrm{Ru}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{I}_{3}$
20.86 Which of the following complexes are chiral?
(a) $\left[\mathrm{Pt}(\mathrm{en}) \mathrm{Cl}_{2}\right]$
(b) cis- $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Br}_{2}\right]^{+}$
(c) $c i s-\left[\mathrm{Cr}(\mathrm{en})_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right]^{3+}$
(d) $\left[\mathrm{Cr}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$
20.87 Which of the following complexes can exist as enantiomers? Draw their structures.
(a) $\left[\mathrm{Cr}(\mathrm{en})_{3}\right]^{3+}$
(b) cis-[Co(en $\left.)_{2}\left(\mathrm{NH}_{3}\right) \mathrm{Cl}\right]^{2+}$
(c) trans- $\left[\mathrm{Co}(\mathrm{en})_{2}\left(\mathrm{NH}_{3}\right) \mathrm{Cl}\right]^{2+}$
(d) $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cl}_{3}\right]^{+}$
20.88 Draw all possible diastereoisomers and enantiomers of each of the following complexes:
(a) $\mathrm{Ru}\left(\mathrm{NH}_{3}\right)_{4} \mathrm{Cl}_{2}$
(b) $\left[\operatorname{Pt}(\mathrm{en})_{3}\right]^{4+}$
(c) $\left[\mathrm{Pt}(\mathrm{en})_{2} \mathrm{ClBr}\right]^{2+}$
20.89 Draw all possible diastereoisomers and enantiomers of each of the following complexes:
(a) $\left[\mathrm{Rh}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2} \mathrm{I}_{2}\right]^{3-}$
(b) $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{4}\right]^{-}$
(c) $[\mathrm{Co}(\mathrm{EDTA})]^{-}$
20.90 How does plane-polarized light differ from ordinary light? Draw the structure of a chromium complex that rotates the plane of plane-polarized light.
20.91 What is a racemic mixture? Does it affect planepolarized light? Explain.

## Color of Complexes; Valence Bond and Crystal Field Theories

20.92 What is an absorption spectrum? If the absorption spectrum of a complex has just one band at 455 nm , what is the color of the complex?
20.93 A red colored complex has just one absorption band in the visible region of the spectrum. Predict the approximate wavelength of this band.
20.94 Give a valence bond description of the bonding in each of the following complexes. Include orbital diagrams for the free metal ion and the metal ion in the complex. Indicate which hybrid orbitals the metal ion uses for bonding, and specify the number of unpaired electrons.
(a) $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$
(b) $\left[\mathrm{NiBr}_{4}\right]^{2-}$ (tetrahedral)
(c) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ (low-spin)
(d) $\left[\mathrm{MnCl}_{6}\right]^{3-}$ (high-spin)
20.95 For each of the following complexes, describe the bonding using valence bond theory. Include orbital diagrams for the free metal ion and the metal ion in the complex. Indicate which hybrid orbitals the metal ion uses for bonding, and specify the number of unpaired electrons.
(a) $\left[\mathrm{AuCl}_{4}\right]^{-}$(square planar)
(b) $\left[\mathrm{Ag}\left(\mathrm{NH}_{3}\right)_{2}\right]^{+}$
(c) $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ (high-spin)
(d) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4-}$ (low-spin)
20.96 Draw a crystal field energy-level diagram for the $3 d$ orbitals of titanium in $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$. Indicate what is meant by the crystal field splitting, and explain why $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ is colored.
20.97 Use a sketch to explain why the $d_{x y}$ and $d_{x^{2}-y^{2}}$ orbitals have different energies in an octahedral complex. Which of the two orbitals has higher energy?
20.98 The $\left[\mathrm{Ti}(\mathrm{NCS})_{6}\right]^{3-}$ ion exhibits a single absorption band at 544 nm . Calculate the crystal field splitting energy $\Delta$ (in $\mathrm{kJ} / \mathrm{mol}$ ). Is $\mathrm{NCS}^{-}$a stronger or weaker field ligand than water? Predict the color of $\left[\mathrm{Ti}(\mathrm{NCS})_{6}\right]^{3-}$.
20.99 The $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ ion is violet, and $\left[\mathrm{Cr}(\mathrm{CN})_{6}\right]^{3-}$ is yellow. Explain this difference using crystal field theory. Use the colors to order $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{CN}^{-}$in the spectrochemical series.
20.100 For each of the following complexes, draw a crystal field energy-level diagram, assign the electrons to orbitals, and predict the number of unpaired electrons:
(a) $\left[\mathrm{CrF}_{6}\right]^{3-}$
(b) $\left[\mathrm{V}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$
(c) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$
20.101 Draw a crystal field energy-level diagram, assign the electrons to orbitals, and predict the number of unpaired electrons for each of the following:
(a) $\left[\mathrm{Cu}(\mathrm{en})_{3}\right]^{2+}$
(b) $\left[\mathrm{FeF}_{6}\right]^{3-}$
(c) $\left[\mathrm{Co}(\mathrm{en})_{3}\right]^{3+}$ (low-spin)
20.102 The $\mathrm{Ni}^{2+}(a q)$ cation is green, but $\mathrm{Zn}^{2+}(a q)$ is colorless. Explain.
20.103 The $\mathrm{Cr}^{3+}(a q)$ cation is violet, but $\mathrm{Y}^{3+}(a q)$ is colorless. Explain.
20.104 Weak-field ligands tend to give high-spin complexes, but strong-field ligands tend to give low-spin complexes. Explain.
20.105 Explain why nearly all tetrahedral complexes are highspin.
20.106 Draw a crystal field energy-level diagram for a square planar complex, and explain why square planar geometry is especially common for $d^{8}$ complexes.
20.107 For each of the following complexes, draw a crystal field energy-level diagram, assign the electrons to orbitals, and predict the number of unpaired electrons:
(a) $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{4}\right]^{2+}$ (square planar)
(b) $\left[\mathrm{MnCl}_{4}\right]^{2-}$ (tetrahedral)
(c) $\left[\mathrm{Co}(\mathrm{NCS})_{4}\right]^{2-}$ (tetrahedral)
(d) $\left[\mathrm{Cu}(\mathrm{en})_{2}\right]^{2+}$ (square planar)

## General Problems

20.108 Which of the following complexes are paramagnetic?
(a) $\left[\mathrm{Mn}(\mathrm{CN})_{6}\right]^{3-}$
(b) $\left[\mathrm{Zn}\left(\mathrm{NH}_{3}\right)_{4}\right]^{2+}$
(c) $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{4-}$
(d) $\left[\mathrm{FeF}_{6}\right]^{4-}$
20.109 Which of the following complexes are diamagnetic?
(a) $\left[\mathrm{Ni}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$
(b) $\left[\mathrm{Co}(\mathrm{CN})_{6}\right]^{3-}$
(c) $\left[\mathrm{HgI}_{4}\right]^{2-}$
(d) $\left[\mathrm{Cu}\left(\mathrm{NH}_{3}\right)_{4}\right]^{2+}$
20.110 For each of the following reactions in acidic solution, predict the products and write a balanced net ionic equation:
(a) $\mathrm{Co}^{3+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightarrow$
(b) $\mathrm{Cr}^{2+}(a q)+\mathrm{O}_{2}(g) \rightarrow$
(c) $\mathrm{Cu}(s)+\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q) \rightarrow$
(d) $\mathrm{CrO}_{4}{ }^{2-}(a q)+\mathrm{H}^{+}(a q) \rightarrow$
20.111 Write a balanced net ionic equation for each of the following reactions in acidic, basic, or neutral solution:
(a) $\mathrm{MnO}_{4}{ }^{-}(a q)+\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}(a q) \xrightarrow{\text { Acidic }}$

$$
\mathrm{Mn}^{2+}(a q)+\mathrm{CO}_{2}(g)
$$

(b) $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}(a q)+\mathrm{Ti}^{3+}(a q) \xrightarrow{\text { Acidic }}$

$$
\mathrm{Cr}^{3+}(a q)+\mathrm{TiO}^{2+}(a q)
$$

(c) $\mathrm{MnO}_{4}^{-}(a q)+\mathrm{SO}_{3}{ }^{2-}(a q) \xrightarrow{\text { Basic }}$

$$
\mathrm{MnO}_{4}{ }^{2-}(a q)+\mathrm{SO}_{4}{ }^{2-}(a q)
$$

(d) $\mathrm{Fe}(\mathrm{OH})_{2}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g}) \xrightarrow{\text { Neutral }} \mathrm{Fe}(\mathrm{OH})_{3}(\mathrm{~s})$
20.112 Calculate the concentrations of $\mathrm{Fe}^{3+}, \mathrm{Cr}^{3+}$, and $\mathrm{Cr}_{2} \mathrm{O}_{7}{ }^{2-}$ in a solution prepared by mixing 100.0 mL of $0.100 \mathrm{M} \mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ and 100.0 mL of $0.400 \mathrm{M} \mathrm{FeSO}_{4}$. The initial solutions are strongly acidic.
20.113 In basic solution, $\mathrm{Cr}(\mathrm{OH})_{4}{ }^{-}$is oxidized to $\mathrm{CrO}_{4}{ }^{2-}$ by hydrogen peroxide. Calculate the concentration of $\mathrm{CrO}_{4}{ }^{2-}$ in a solution prepared by mixing 40.0 mL of $0.030 \mathrm{M} \mathrm{Cr}_{2}\left(\mathrm{SO}_{4}\right)_{3}, 10.0 \mathrm{~mL}$ of $0.20 \mathrm{M} \mathrm{H}_{2} \mathrm{O}_{2}$, and 50.0 mL of 1.0 M NaOH .
20.114 Name each of the following compounds:
(a) $\mathrm{Na}\left[\mathrm{Pt}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Br}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\right]$
(b) $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{6}\right]\left[\mathrm{Co}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]$
(c) $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{6}\right]\left[\mathrm{Cr}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]$
(d) $\left[\mathrm{Rh}(\mathrm{en})_{2}\left(\mathrm{NH}_{3}\right)_{2}\right]_{2}\left(\mathrm{SO}_{4}\right)_{3}$
20.115 Describe the bonding in $\left[\mathrm{Mn}(\mathrm{CN})_{6}\right]^{3-}$, using both crystal field theory and valence bond theory. Include the appropriate crystal field $d$ orbital energy-level diagram and the valence bond orbital diagram. Which model allows you to predict the number of unpaired electrons? How many do you expect?
20.116 The complex $\left[\mathrm{FeCl}_{6}\right]^{3-}$ is more paramagnetic than $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$. Explain.
20.117 Although $\mathrm{Cl}^{-}$is a weak-field ligand and $\mathrm{CN}^{-}$is a strong-field ligand, $\left[\mathrm{CrCl}_{6}\right]^{3-}$ and $\left[\mathrm{Cr}(\mathrm{CN})_{6}\right]^{3-}$ exhibit approximately the same amount of paramagnetism. Explain.
20.118 In octahedral complexes, the choice between high-spin and low-spin electron configurations arises only for $d^{4}-d^{7}$ complexes. Explain.
20.119 Draw a crystal field energy-level diagram, and predict the number of unpaired electrons for each of the following:
(a) $\left[\mathrm{Mn}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$
(b) $\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{2} \mathrm{Cl}_{2}$
(c) $\left[\mathrm{FeO}_{4}\right]^{2-}$
(d) $\left[\mathrm{Ru}\left(\mathrm{NH}_{3}\right)_{6}\right]^{2+}$ (low-spin)
20.120 Explain why $\left[\mathrm{CoCl}_{4}\right]^{2-}$ (blue) and $\left[\mathrm{Co}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$ (pink) have different colors. Which complex has its absorption bands at longer wavelengths?
20.121 The complex $\left[\mathrm{Rh}(\mathrm{en})_{2}\left(\mathrm{NO}_{2}\right)(\mathrm{SCN})\right]^{+}$can exist in 12 isomeric forms, including constitutional isomers and stereoisomers. Sketch the structures of all 12 isomers.
20.122 The glycinate anion, gly ${ }^{-}=\mathrm{NH}_{2} \mathrm{CH}_{2} \mathrm{CO}_{2}{ }^{-}$, bonds to metal ions through the N atom and one of the O atoms. Using $\mathrm{N}^{-} \mathrm{O}$ to represent $\mathrm{gly}^{-}$, sketch the structures of the four stereoisomers of $\mathrm{Co}(\mathrm{gly})_{3}$.
20.123 Sketch the five possible diastereoisomers of $\mathrm{Pt}(\mathrm{gly})_{2} \mathrm{Cl}_{2}$, where $\mathrm{gly}^{-}$is the bidentate ligand described in Problem 20.122. Which of the isomers has a dipole moment? Which can exist as a pair of enantiomers?
20.124 Draw the structures of all possible diastereoisomers of an octahedral complex with the formula $\mathrm{MA}_{2} \mathrm{~B}_{2} \mathrm{C}_{2}$. Which of the diastereoisomers, if any, can exist as enantiomers?
20.125 Look at the colors of the isomeric complexes in Figure 20.17, and predict which is the stronger field ligand, nitro $\left(-\mathrm{NO}_{2}\right)$ or nitrito (-ONO)? Explain your reasoning.
20.126 The amount of paramagnetism for a first-series transition metal complex is related approximately to its spin-only magnetic moment. The spin-only value of the magnetic moment in units of Bohr magnetons (BM) is given by $\sqrt{n(n+2)}$, where $n$ is the number of unpaired electrons. Calculate the spin-only value of the magnetic moment for the $2+$ ions of the first-series transition metals (except Sc) in octahedral complexes with (a) weak-field ligands and (b) strong-field ligands. For which electron configurations can the magnetic moment distinguish between high-spin and low-spin electron configurations?
20.127 Predict the crystal field energy-level diagram for a linear $\mathrm{ML}_{2}$ complex that has two ligands along the $\pm \mathrm{z}$ axis:

20.128 Reaction of the octahedral complex $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3}\left(\mathrm{NO}_{2}\right)_{3}\right]$ with HCl yields a complex $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Cl}_{2}\right]^{+}$in which the two chloride ligands are trans to one another.
(a) Draw the two possible stereoisomers of the starting material $\left[\mathrm{Co}\left(\mathrm{NH}_{3}\right)_{3}\left(\mathrm{NO}_{2}\right)_{3}\right]$. (All three $\mathrm{NO}_{2}{ }^{-}$ ligands are bonded to Co through the N atom.)
(b) Assuming that the $\mathrm{NH}_{3}$ groups remain in place, which of the two starting isomers could give rise to the observed product?
20.129 Consider the octahedral complex $[\mathrm{Co}(\mathrm{en})(\text { dien }) \mathrm{Cl}]^{2+}$, where dien $=\mathrm{H}_{2} \mathrm{NCH}_{2} \mathrm{CH}_{2} \mathrm{NHCH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}$, which can be abbreviated $\mathrm{N}^{\sim} \mathrm{N}^{\sim} \mathrm{N}$.
(a) The dien ligand is a tridentate ligand. Explain what is meant by "tridentate" and why dien can act as a tridentate ligand.
(b) Draw all possible stereoisomers of $[\mathrm{Co}(\mathrm{en})(\text { dien }) \mathrm{Cl}]^{2+}$ (dien is a flexible ligand). Which stereoisomers are chiral, and which are achiral?
20.130 For each of the following, (i) give the systematic name of the compound and specify the oxidation state of the transition metal, (ii) draw a crystal field energy-level diagram and assign the $d$ electrons to orbitals, (iii) indicate whether the complex is high-spin or low-spin (for $d^{4}-d^{7}$ complexes), and (iv) specify the number of unpaired electrons.
(a) $\left(\mathrm{NH}_{4}\right)\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]\left(\mathrm{SO}_{4}\right)_{2}$
(b) $\mathrm{Mo}(\mathrm{CO})_{6}(\mathrm{CO}$ is a strong-field ligand)
(c) $\left[\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{4}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right]\left(\mathrm{NO}_{3}\right)_{2}$
(d) $\mathrm{K}_{4}\left[\mathrm{Os}(\mathrm{CN})_{6}\right]$
(e) $\left[\mathrm{Pt}\left(\mathrm{NH}_{3}\right)_{4}\right]\left(\mathrm{ClO}_{4}\right)_{2}$
(f) $\mathrm{Na}_{2}\left[\mathrm{Fe}(\mathrm{CO})_{4}\right]$
20.131 The drug Nipride, $\mathrm{Na}_{2}\left[\mathrm{Fe}(\mathrm{CN})_{5} \mathrm{NO}\right]$, is an inorganic complex used as a source of NO to lower blood pressure during surgery.
(a) The nitrosyl ligand in this complex is believed to be $\mathrm{NO}^{+}$rather than neutral NO. What is the oxidation state of iron, and what is the systematic name for $\mathrm{Na}_{2}\left[\mathrm{Fe}(\mathrm{CN})_{5} \mathrm{NO}\right]$ ?
(b) Draw a crystal field energy-level diagram for $\left[\mathrm{Fe}(\mathrm{CN})_{5} \mathrm{NO}\right]^{2-}$, assign the electrons to orbitals, and predict the number of unpaired electrons.
20.132 Based on the colors of their Cr (III) complexes, arrange the following ligands in a spectrochemical series in order of increasing value of the crystal field splitting $\Delta: \mathrm{acac}^{-}$(a bidentate ligand), acetate ${ }^{-}, \mathrm{Cl}^{-}, \mathrm{H}_{2} \mathrm{O}, \mathrm{NH}_{3}$, and urea. The colors of the $\mathrm{Cr}(\mathrm{III})$ complexes are red for $\mathrm{Cr}(\mathrm{acac})_{3}$, violet for $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$, green for $\left[\mathrm{CrCl}_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{4}\right]^{+}$, green for $\left[\mathrm{Cr}(\text { urea })_{6}\right]^{3+}$, yellow for $\left[\mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{6}\right]^{3+}$, and blue-violet for $\mathrm{Cr}(\text { acetate })_{3}\left(\mathrm{H}_{2} \mathrm{O}\right)_{3}$.

## Multi-Concept Problems

20.133 Spinach contains a lot of iron but is not a good source of dietary iron because nearly all the iron is tied up in the oxalate complex $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$.
(a) The formation constant $K_{\mathrm{f}}$ for $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$ is $3.3 \times 10^{20}$. Calculate the equilibrium concentration of free $\mathrm{Fe}^{3+}$ in a 0.100 M solution of $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$. (Ignore any acid-base reactions.)
(b) Under the acidic conditions in the stomach, the $\mathrm{Fe}^{3+}$ concentration should be greater because of the reaction

$$
\begin{aligned}
& {\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}(a q)+6 \mathrm{H}_{3} \mathrm{O}^{+}(a q) \rightleftharpoons} \\
& \mathrm{Fe}^{3+}(a q)+3 \mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}(a q)+6 \mathrm{H}_{2} \mathrm{O}(l)
\end{aligned}
$$

Show, however, that this reaction is nonspontaneous under standard-state conditions. (For $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$, $K_{\mathrm{a} 1}=5.9 \times 10^{-2}$ and $K_{\mathrm{a} 2}=6.4 \times 10^{-5}$. )
(c) Draw a crystal field energy-level diagram for $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$, and predict the number of unpaired electrons. $\left(\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}\right.$ is a weak-field bidentate ligand.)
(d) Draw the structure of $\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]^{3-}$. Is the complex chiral or achiral?
20.134 Formation constants for the ammonia and ethylenediamine complexes of nickel(II) indicate that $\mathrm{Ni}(\mathrm{en})_{3}{ }^{2+}$ is much more stable than $\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}{ }^{2+}$ :
(1) $\mathrm{Ni}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}(a q)+6 \mathrm{NH}_{3}(a q) \rightleftharpoons$

$$
\mathrm{Ni}\left(\mathrm{NH}_{3}\right)_{6}{ }^{2+}(a q)+6 \mathrm{H}_{2} \mathrm{O}(l) \quad K_{\mathrm{f}}=2.0 \times 10^{8}
$$

(2) $\mathrm{Ni}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}{ }^{2+}(a q)+3 \mathrm{en}(a q) \rightleftharpoons$

$$
\mathrm{Ni}(\mathrm{en})_{3}{ }^{2+}(a q)+6 \mathrm{H}_{2} \mathrm{O}(l) \quad K_{\mathrm{f}}=4 \times 10^{17}
$$

The enthalpy changes for the two reactions, $\Delta H^{\circ}{ }_{1}$ and $\Delta H^{\circ}{ }_{2}$, should be about the same because both complexes have six $\mathrm{Ni}-\mathrm{N}$ bonds.
(a) Which of the two reactions should have the larger entropy change, $\Delta S^{\circ}$ ? Explain.
(b) Account for the greater stability of $\mathrm{Ni}(\mathrm{en})_{3}{ }^{2+}$ in terms of the relative values of $\Delta S^{\circ}$ for the two reactions.
(c) Assuming that $\Delta H^{\circ}{ }_{2}-\Delta H^{\circ}$ is zero, calculate the value of $\Delta S^{\circ}{ }_{2}-\Delta S^{\circ}{ }_{1}$.
20.135 The percent iron in iron ore can be determined by dissolving the ore in acid, then reducing the iron to $\mathrm{Fe}^{2+}$, and finally titrating the $\mathrm{Fe}^{2+}$ with aqueous $\mathrm{KMnO}_{4}$. The reaction products are $\mathrm{Fe}^{3+}$ and $\mathrm{Mn}^{2+}$.
(a) Write a balanced net ionic equation for the titration reaction.
(b) Use the $E^{\circ}$ values in Appendix D to calculate $\Delta G^{\circ}$ (in kilojoules) and the equilibrium constant for the reaction.
(c) Draw a crystal field energy-level diagram for the reactants and products, $\mathrm{MnO}_{4}{ }^{-},\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$, $\left[\mathrm{Fe}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$, and $\left[\mathrm{Mn}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{2+}$, and predict the number of unpaired electrons for each.
(d) Does the paramagnetism of the solution increase or decrease as the reaction proceeds? Explain.
(e) What is the mass \% Fe in the iron ore if titration of the $\mathrm{Fe}^{2+}$ from a 1.265 g sample of ore requires 34.83 mL of $0.05132 \mathrm{M} \mathrm{KMnO}_{4}$ to reach the equivalence point?
20.136 The complete reaction of 2.60 g of chromium metal with 50.00 mL of $1.200 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}$ in the absence of air gave a blue solution and a colorless gas that was collected at $25^{\circ} \mathrm{C}$ and a pressure of 735 mm Hg .
(a) Write a balanced net ionic equation for the reaction.
(b) How many liters of gas were produced?
(c) What is the pH of the solution?
(d) Describe the bonding in the blue colored ion, using both the crystal field theory and the valence bond theory. Include the appropriate crystal field $d$-orbital energy-level diagram and the valence bond orbital diagram. Identify the hybrid orbitals used in the valence bond description.
(e) When an excess of KCN is added to the solution, the color changes, and the paramagnetism of the solution decreases. Explain.
20.137 In acidic aqueous solution, the complex trans$\left[\mathrm{Co}(\mathrm{en})_{2} \mathrm{Cl}_{2}\right]^{+}$undergoes the following substitution reaction:

$$
\begin{aligned}
& \text { trans- }\left[\mathrm{Co}(\mathrm{en})_{2} \mathrm{Cl}_{2}\right]^{+}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \longrightarrow \\
& \text { trans- }\left[\mathrm{Co}(\mathrm{en})_{2}\left(\mathrm{H}_{2} \mathrm{O}\right) \mathrm{Cl}\right]^{2+}(a q)+\mathrm{Cl}^{-}(a q)
\end{aligned}
$$

The reaction is first order in trans- $\left[\mathrm{Co}(\mathrm{en})_{2} \mathrm{Cl}_{2}\right]^{+}$, and the rate constant at $25^{\circ} \mathrm{C}$ is $3.2 \times 10^{-5} \mathrm{~s}^{-1}$.
(a) What is the half-life of the reaction in hours?
(b) If the initial concentration of trans- $\left[\mathrm{Co}(\mathrm{en})_{2} \mathrm{Cl}_{2}\right]^{+}$ is 0.138 M , what is its molarity after a reaction time of 16.5 h ?
(c) Devise a possible reaction mechanism with a unimolecular rate-determining step.
(d) Is the reaction product chiral or achiral? Explain.
(e) Draw a crystal field energy-level diagram for trans- $\left[\mathrm{Co}(\mathrm{en})_{2} \mathrm{Cl}_{2}\right]^{+}$that takes account of the fact that $\mathrm{Cl}^{-}$is a weaker field ligand than ethylenediamine.
20.138 Chromium forms three isomeric compounds $\mathrm{A}, \mathrm{B}$, and C with percent composition $19.52 \% \mathrm{Cr}, 39.91 \% \mathrm{Cl}$, and $40.57 \% \mathrm{H}_{2} \mathrm{O}$. When a sample of each compound was dissolved in water and aqueous $\mathrm{AgNO}_{3}$ was added, a precipitate of AgCl formed immediately. A 0.225 g sample of compound A gave 0.363 g of $\mathrm{AgCl}, 0.263 \mathrm{~g}$ of B gave 0.283 g of AgCl , and 0.358 g of C gave 0.193 g of AgCl . One of the three compounds is violet, while the other two are green. In all three, chromium has coordination number six.
(a) What is the empirical formula of $\mathrm{A}, \mathrm{B}$, and C ?
(b) What are the probable structural formulas of $\mathrm{A}, \mathrm{B}$, and C? Draw the structure of the cation in each compound. Which cation can exist as diastereoisomers?
(c) Which of the three compounds is likely to be the violet one? Explain.
(d) What are the approximate freezing points of 0.25 m solutions of A, B, and C assuming complete dissociation?
20.139 Cobalt(III) trifluoroacetylacetonate, $\mathrm{Co}(\mathrm{tfac})_{3}$, is a sixcoordinate, octahedral metal chelate in which three planar, bidentate tfac ligands are attached to a central Co atom:

(a) Draw all possible diastereoisomers and enantiomers of $\mathrm{Co}(\mathrm{tfac})_{3}$.
(b) Diastereoisomers A and B have dipole moments of 6.5 D and 3.8 D , respectively. Which of your diastereoisomers is A and which is B ?
(c) The isomerization reaction $\mathrm{A} \rightarrow \mathrm{B}$ in chloroform solution has first-order rate constants of $0.0889 h^{-1}$ at $66.1^{\circ} \mathrm{C}$ and $0.0870 \mathrm{~min}^{-1}$ at $99.2^{\circ} \mathrm{C}$. What is the activation energy for the reaction?
(d) Draw a crystal field energy-level diagram for $\mathrm{Co}(\mathrm{tfac})_{3}$, and predict its magnetic properties. (In this complex, tfac is a strong-field ligand.)

## eMedia Problems

20.140 Examine the trends for boiling points, atomic radii, and ionization energies using the Interactive Periodic Table (eChapter 20.2). Explain the factors that account for each of these trends.
20.141 For each of the oxidation states of the elements in the Oxidation States of Transition Elements activity (eChapter 20.3), identify the subshell(s) of the electrons being lost or shared.
20.142 Enantiomers are designated either + or - , depending on whether they rotate the plane of plane-polarized light clockwise or counterclockwise, respectively. Watch the Optical Activity movie (eChapter 20.9), and draw both enantiomers for each of the following chiral complexes.
(a) cis-[Cr(en) $\left.2_{2} \mathrm{Cl}_{2}\right]^{+}$
(b) cis- $\left[\mathrm{Cr}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{2}\left(\mathrm{H}_{2} \mathrm{O}\right)_{2}\right]^{-}$
(c) $\left[\mathrm{Ni}(\mathrm{en})_{3}\right]^{2+}$
20.143 Use the Color Observation activity in eChapter 20.10 to predict the color a solution would appear if it absorbed blue, orange, red, or violet light. Does the Color Wheel activity in that same section confirm your predictions?
20.144 The $\mathrm{Cr}^{3+}$ ion has the same electron configuration in $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ and in $\left[\mathrm{Cr}(\mathrm{CN})_{6}\right]^{3-}$ but one absorbs yellow light to appear violet and one absorbs violet light to appear yellow. According to the Spin-Pairing Energy activity in eChapter 20.12, which complex is yellow and which is violet? Why do these ions absorb different wavelengths even though they have the same electron configuration?

## Chapter

## Metals and SolidState Materials

The materials available for making tools and weapons, houses and skyscrapers, computers and lasers have had a profound effect on the development of human civilization. Indeed, archaeologists organize early human history in terms of materials-the Stone Age, in which only natural materials such as wood and stone were available; the Bronze Age, in which implements were made of copper alloyed with tin; and the Iron Age, in which ornaments, weapons, and tools were made of iron. Copper and iron are still of enormous importance. Copper is used to make electrical wiring, and iron is the main constituent of steel.

Levitation of a magnet above a pellet of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ cooled to 77 K with liquid nitrogen. $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ becomes a superconductor at approximately 90 K .

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21.8 Composites
$\square$ Interlude-Diamonds and Diamond Films

The MRI instruments used in hospitals contain magnets made from superconductors.

- FIGURE 21.1 Samples of (a) hematite $\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)$, (b) starshaped needles of rutile $\left(\mathrm{TiO}_{2}\right)$ on a quartz matrix, and (c) cinnabar (HgS).

Today, metals unknown in ancient times, such as aluminum and titanium, play a leading role in modern technology. These metals are widely used, for instance, in the aircraft industry because of their low densities and high resistance to corrosion.

Modern technology is made possible by a host of solid-state materials such as semiconductors, superconductors, advanced ceramics, and composites. Semiconductors are used in the miniature solid-state electronic devices found in computers. Superconductors are used to make the powerful magnets found in the magnetic resonance imaging (MRI) instruments employed in medical diagnosis. Advanced ceramics and composites have numerous engineering, electronic, and biomedical applications and are likely to be among the more important materials in future technologies.


In this chapter, we'll look at both metals and solid-state materials. We'll examine the natural sources of the metallic elements, the methods used to obtain metals from their ores, and the models used to describe the bonding in metals. We'll also look at the structure, bonding, properties, and applications of semiconductors, superconductors, ceramics, and composites.

### 21.1 Sources of the Metallic Elements

Most metals occur in nature as minerals, the crystalline, inorganic constituents of the rocks that make up the earth's crust. Silicates and aluminosilicates (Section 19.7) are the most abundant minerals, but they are difficult to concentrate and reduce and are therefore generally unimportant as commercial sources of metals. More important are oxides and sulfides, such as hematite $\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)$, rutile $\left(\mathrm{TiO}_{2}\right)$, and cinnabar ( HgS ) (Figure 21.1), which yield iron, titanium, and

mercury, respectively. Mineral deposits from which metals can be produced economically are called ores (Table 21.1).

| TABLE 21.1 | Principal Ores of Some Important Metals |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| Metal | Ore | Formula | Location of Important Deposits |  |
| Aluminum | Bauxite | $\mathrm{Al}_{2} \mathrm{O}_{3} \cdot x \mathrm{H}_{2} \mathrm{O}$ | Australia, Brazil, Jamaica |  |
| Chromium | Chromite | $\mathrm{FeCr}_{2} \mathrm{O}_{4}$ | Russia, South Africa |  |
| Copper | Chalcopyrite | $\mathrm{CuFeS}_{2}$ | U.S., Chile, Canada |  |
| Iron | Hematite | $\mathrm{Fe}_{2} \mathrm{O}_{3}$ | Australia, Ukraine, U.S. |  |
| Lead | Galena | $\mathrm{PbS}^{\text {Manganese }}$ | Pyrolusite | $\mathrm{MnO}_{2}$ |

The chemical compositions of the most common ores correlate with the locations of the metals in the periodic table (Figure 21.2). The early transition metals on the left side of the $d$ block generally occur as oxides, and the more electronegative, late transition metals on the right side of the $d$ block occur as sulfides. This pattern makes sense because the less electronegative metals tend to form ionic compounds by losing electrons to highly electronegative nonmetals such as oxygen. By contrast, the more electronegative metals tend to form compounds with more covalent character by bonding to the less electronegative nonmetals such as sulfur.


We might also expect to find oxide ores for the s-block metals and sulfide ores for the more electronegative $p$-block metals. In fact, sulfide ores are common for the $p$-block metals, except for Al and Sn , but oxides of the $s$-block metals are strongly basic and far too reactive to exist in an environment that contains acidic oxides such as $\mathrm{CO}_{2}$ and $\mathrm{SiO}_{2}$. Consequently, s-block metals are found in nature as carbonates, as silicates, and, in the case of Na and K , as chlorides (Sections 6.7 and 6.8). Only gold and the platinum-group metals (Ru, Os, Rh, Ir, Pd , and Pt ) are sufficiently unreactive to occur commonly in uncombined form as the free metals. spective on Rutile," J. Chem. Educ., Vol. 75, 1998, 641.


FIGURE 21.2 Primary mineral sources of metals. The sblock metals occur as chlorides, silicates, and carbonates. The $d$ - and $p$-block metals are found as oxides and sulfides, except for the group 3B metals, which occur as phosphates, and the platinum-group metals and gold, which occur in uncombined form. There is no mineral source of technetium (Tc in group 7B), a radioactive element that is made in nuclear reactors.


(1)Daniel Bartet and Eugenia Aguilia, "Teaching the Concepts of Metallurgy Through the Use of Postage Stamps," J. Chem. Educ., Vol. 64, 1987, 526-528.


A In panning for gold, prospectors use density differences to separate gold from the gangue.

FIGURE 21.3 The flotation process for concentrating metal sulfide ores. Mineral particles float to the top of the tank along with the soapy air bubbles, while the gangue sinks to the bottom.

## 21.2 | Metallurgy

An ore is a complex mixture of a metal-containing mineral and economically worthless material called gangue (pronounced "gang"), consisting of sand, clay, and other impurities. The extraction of a metal from its ore requires several steps: (1) concentration of the ore and, if necessary, chemical treatment prior to reduction; (2) reduction of the mineral to the free metal; and (3) refining or purification of the metal. These processes are a part of metallurgy, the science and technology of extracting metals from their ores. Another aspect of metallurgy is the making of alloys, metallic solutions composed of two or more elements. Steels and bronze are alloys.

## Concentration and Chemical Treatment of Ores

Ores are concentrated by separating the mineral from the gangue. The mineral and the gangue have different properties, which are exploited in various separation methods. Density differences, for example, are important in panning for gold, a procedure in which prospectors flush water over gold-bearing earth in a pan. The less dense gangue is washed away, and the more dense gold particles remain at the bottom of the pan. Differences in magnetic properties are used to concentrate the iron ore magnetite $\left(\mathrm{Fe}_{3} \mathrm{O}_{4}\right)$. The $\mathrm{Fe}_{3} \mathrm{O}_{4}$ is strongly attracted by magnets, but the gangue is unaffected.

Metal sulfide ores are concentrated by flotation, a process that exploits differences in the ability of water and oil to wet the surfaces of the mineral and the gangue. A powdered ore such as chalcopyrite $\left(\mathrm{CuFe}_{2}\right)$ is mixed with water, oil, and a detergent, and the mixture is vigorously agitated in a tank by blowing air through the liquid (Figure 21.3). The gangue, which contains ionic silicates, is moistened by the polar water molecules and sinks to the bottom of the tank. The mineral particles, which contain the less polar metal sulfide, are coated by the nonpolar oil molecules and become attached to the soapy air bubbles created by the detergent. The metal sulfide particles are thus carried to the surface in the soapy froth, which is skimmed off at the top of the tank.


Sometimes, ores are concentrated by chemical treatment. In the Bayer process, for instance, the $\mathrm{Al}_{2} \mathrm{O}_{3}$ in bauxite $\left(\mathrm{Al}_{2} \mathrm{O}_{3} \cdot x \mathrm{H}_{2} \mathrm{O}\right)$ is separated from $\mathrm{Fe}_{2} \mathrm{O}_{3}$ impurities by treating the ore with hot aqueous NaOH . The amphoteric $\mathrm{Al}_{2} \mathrm{O}_{3}$ dissolves as the aluminate ion, $\mathrm{Al}(\mathrm{OH})_{4}{ }^{-}$, but the basic $\mathrm{Fe}_{2} \mathrm{O}_{3}$ does not:

$$
\mathrm{Al}_{2} \mathrm{O}_{3}(s)+2 \mathrm{OH}^{-}(a q)+3 \mathrm{H}_{2} \mathrm{O}(l) \longrightarrow 2 \mathrm{Al}(\mathrm{OH})_{4}^{-}(a q)
$$

The Bayer process is described in more detail in Section 16.12.

Chemical treatment is also used to convert minerals to compounds that are more easily reduced to the metal. For example, sulfide minerals, such as sphalerite $(\mathrm{ZnS})$, are converted to oxides by roasting, a process that involves heating the mineral in air:

$$
2 \mathrm{ZnS}(s)+3 \mathrm{O}_{2}(g) \xrightarrow{\text { Heat }} 2 \mathrm{ZnO}(s)+2 \mathrm{SO}_{2}(g)
$$

Formerly, the sulfur dioxide by-product was a source of acid rain because it is oxidized in the atmosphere to $\mathrm{SO}_{3}$, which reacts with water vapor to yield sulfuric acid. In modern roasting facilities, however, the $\mathrm{SO}_{2}$ is converted to sulfuric acid rather than being vented to the atmosphere.

## Reduction

Once an ore has been concentrated, it is reduced to the free metal, either by chemical reduction or by electrolysis. The method used (Table 21.2) depends on the activity of the metal as measured by its standard reduction potential (Table 18.1). The most active metals have the most negative standard reduction potentials and are the most difficult to reduce; the least active metals have the most positive standard reduction potentials and are the easiest to reduce.

| TABLE 21.2 | Reduction Methods for Producing Some Common Metals |  |
| :--- | :--- | :--- |
|  | Metal | Reduction Method |
| Least active | $\mathrm{Au}, \mathrm{Pt}$ | None; found in nature as the free metal |
|  | $\mathrm{Cu}, \mathrm{Ag}, \mathrm{Hg}$ | Roasting of the metal sulfide |
|  | $\mathrm{V}, \mathrm{Cr}, \mathrm{Mn}, \mathrm{Fe}$, | Reduction of the metal oxide with carbon, <br> hydrogen, or a more active metal |
|  | $\mathrm{Ni}, \mathrm{Zn}, \mathrm{W}, \mathrm{Pb}$ | Electrolysis of molten $\mathrm{Al}_{2} \mathrm{O}_{3}$ in cryolite |
|  | Al | Electrolysis of the molten metal chloride |

Gold and platinum are so inactive that they are usually found in nature in uncombined form, but copper and silver, which are slightly more active, are found in both combined and uncombined form. Copper, silver, and mercury commonly occur in sulfide ores that are easily reduced by roasting. Cinnabar $(\mathrm{HgS})$, for example, yields elemental mercury when the ore is heated at $600^{\circ} \mathrm{C}$ in a stream of air:

$$
\mathrm{HgS}(s)+\mathrm{O}_{2}(g) \xrightarrow{600^{\circ} \mathrm{C}} \mathrm{Hg}(g)+\mathrm{SO}_{2}(g)
$$

Although it may seem strange that heating a substance in oxygen reduces it to the metal, both oxidation and reduction of HgS occur in this reaction: Sulfide ions are oxidized and mercury(II) is reduced.

More active metals, such as chromium, zinc, and tungsten, are obtained by reducing their oxides with a chemical reducing agent such as carbon, hydrogen, or a more active metal ( $\mathrm{Na}, \mathrm{Mg}$, or Al ). Pure chromium, for example, is produced by reducing $\mathrm{Cr}_{2} \mathrm{O}_{3}$ with aluminum (Section 20.4). Zinc , used in the automobile industry for galvanizing steel (Section 18.10), is obtained by reducing ZnO with coke, a form of carbon produced by heating coal in the absence of air:

$$
\mathrm{ZnO}(s)+\mathrm{C}(s) \xrightarrow{\text { Heat }} \mathrm{Zn}(g)+\mathrm{CO}(g)
$$

Although carbon is the cheapest available reducing agent, it is unsatisfactory for reducing oxides of metals like tungsten that form very stable carbides.


$\sqrt{ }$
In general, the ease of reducing an ore to the free metal increases from left to right of the periodic table. s-Block and aluminum metal ores are reduced with difficulty. Heavy transition metal ores at the right of the $d$-block are easiest to reduce.


Formation of Silver Crystals movie

0A driving force in the reduction of an ore by roasting or chemical treatment with carbon or hydrogen is the formation of gaseous byproducts, which can be continuously removed from the system.

© FIGURE 21.4 The familiar incandescent lightbulb emits white light when an electric current passes through the tungsten wire filament, heating it to a high temperature. The glass bulb contains gases such as argon and nitrogen, which carry away heat from the filament. Although tungsten has the highest boiling point of any element $\left(5555^{\circ} \mathrm{C}\right)$, the tungsten slowly evaporates from the hot filament and condenses as the black spot of tungsten metal usually visible on the inside surface of a burned-out bulb.

VMetal carbonyls are nonpolar, easily purified, volatile liquids or solids. They are convenient sources of metals in the zero oxidation state and readily converted to the free metal.
(Tungsten carbide, WC, is an extremely hard material used to make high-speed cutting tools.) The preferred method for producing tungsten reduces tungsten(VI) oxide with hydrogen:

$$
\mathrm{WO}_{3}(\mathrm{~s})+3 \mathrm{H}_{2}(g) \xrightarrow{850^{\circ} \mathrm{C}} \mathrm{~W}(s)+3 \mathrm{H}_{2} \mathrm{O}(g)
$$

Because of its high strength, high melting point $\left(3422^{\circ} \mathrm{C}\right)$, low volatility, and high efficiency for converting electrical energy into light, tungsten is used to make filaments for electric lightbulbs (Figure 21.4).

There are no chemical reducing agents strong enough to reduce compounds of the most active metals, so these metals are produced by electrolytic reduction (Section 18.12). Lithium, sodium, and magnesium, for example, are obtained by the electrolysis of their molten chlorides. Aluminum is manufactured by the electrolysis of purified $\mathrm{Al}_{2} \mathrm{O}_{3}$ in molten cryolite $\left(\mathrm{Na}_{3} \mathrm{AlF}_{6}\right)$.

## Refining

For most applications, the metals obtained from processing and reducing ores need to be purified. The methods used include distillation, chemical purification, and electrorefining. Zinc (bp $907^{\circ} \mathrm{C}$ ), for example, is volatile enough to be separated from cadmium, lead, and other impurities by distillation. In this way, the purity of the zinc obtained from reduction of ZnO is increased from $99 \%$ to $99.99 \%$. Nickel, used as a catalyst and as a battery material, is purified by the Mond process, a chemical method in which the volatile compound nickel tetracarbonyl, $\mathrm{Ni}(\mathrm{CO})_{4}$ (bp $43^{\circ} \mathrm{C}$ ), is formed and subsequently decomposed. Carbon monoxide is passed over impure nickel at about $150^{\circ} \mathrm{C}$ and 20 atm pressure, forming $\mathrm{Ni}(\mathrm{CO})_{4}$ and leaving metal impurities behind. The $\mathrm{Ni}(\mathrm{CO})_{4}$ is then decomposed at higher temperatures (about $230^{\circ} \mathrm{C}$ ) on pellets of pure nickel. The process works because the equilibrium shifts to the left with increasing temperature:

$$
\mathrm{Ni}(s)+4 \mathrm{CO}(g) \underset{\text { Higher temp. }}{\stackrel{\text { Lower temp. }}{\rightleftharpoons} \mathrm{Ni}(\mathrm{CO})_{4}(g) \quad \Delta H^{\circ}=-160.8 \mathrm{~kJ} ; \Delta S^{\circ}=-410 \mathrm{~J} / \mathrm{K}, ~(g)}
$$

A similar strategy is employed to purify zirconium, which is used as cladding for fuel rods in nuclear reactors (Section 22.6). The crude metal is heated at about $200^{\circ} \mathrm{C}$ with a small amount of iodine in an evacuated container to form the volatile $\mathrm{ZrI}_{4}$. The $\mathrm{ZrI}_{4}$ is then decomposed to pure zirconium by letting the vapor come in contact with an electrically heated tungsten or zirconium filament at about $1300^{\circ} \mathrm{C}$ :

$$
\mathrm{Zr}(s)+2 \mathrm{I}_{2}(g) \stackrel{200^{\circ} \mathrm{C}}{\underset{1300^{\circ} \mathrm{C}}{\rightleftharpoons}} \mathrm{ZrI}_{4}(g)
$$

Copper from the reduction of ores must be purified for use in making electrical wiring because impurities increase its electrical resistance. The method used is electrorefining (Figure 18.19), an electrolytic process in which copper is oxidized to $\mathrm{Cu}^{2+}$ at an impure copper anode, and $\mathrm{Cu}^{2+}$ from an aqueous copper sulfate solution is reduced to copper at a pure copper cathode. The process is described in Section 18.12.

- PROBLEM 21.1 Write a balanced equation for the production of each of the following metals:
(a) Chromium by reducing $\mathrm{Cr}_{2} \mathrm{O}_{3}$ with aluminum
(b) Copper by roasting $\mathrm{Cu}_{2} \mathrm{~S}$
(c) Lead by reducing PbO with coke
(d) Potassium by the electrolysis of molten KCl


Zirconium is used as cladding for uranium dioxide fuel rods in nuclear reactors.

### 21.3 Iron and Steel

The metallurgy of iron is of special technological importance because iron is the major constituent of steel, the most widely used of all metals. Worldwide production of steel amounts to some 800 million tons per year. Iron is produced by carbon monoxide reduction of iron ore, usually hematite $\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)$, in a huge reactor called a blast furnace (Figure 21.5). A charge of iron ore, coke, and limestone $\left(\mathrm{CaCO}_{3}\right)$ is introduced at the top of the furnace, and a blast of hot air is sent in at the bottom, burning coke and yielding carbon monoxide at a temperature of about $2000^{\circ} \mathrm{C}$ :

$$
2 \mathrm{C}(s)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{CO}(g) \quad \Delta H^{\circ}=-221.0 \mathrm{~kJ}
$$

As the charge descends and the hot carbon monoxide rises, a complex series of high-temperature reactions occurs in the various regions of the furnace, as shown in Figure 21.5. The key overall reaction is the reduction of $\mathrm{Fe}_{2} \mathrm{O}_{3}$ to iron metal ( mp $1538^{\circ} \mathrm{C}$ ), which is obtained as an impure liquid at the bottom of the furnace:

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \longrightarrow 2 \mathrm{Fe}(l)+3 \mathrm{CO}_{2}(g)
$$

The purpose of the limestone is to remove the gangue from the iron ore. At the high temperatures of the furnace, the limestone decomposes yielding lime $(\mathrm{CaO})$, a basic oxide that reacts with $\mathrm{SiO}_{2}$ and other acidic oxides present in the gangue. The product, called slag, is a molten material consisting mainly of calcium silicate:

$$
\begin{gathered}
\mathrm{CaCO}_{3}(s) \longrightarrow \mathrm{CaO}(s)+\mathrm{CO}_{2}(g) \\
\mathrm{CaO}(s)+\mathrm{SiO}_{2}(s) \longrightarrow \underset{\text { Lime }}{\text { Land }} \mathrm{CaSiO}_{3}(l) \\
\text { Slag }
\end{gathered}
$$

The slag, which is less dense than the molten iron, floats on the surface of the iron, thus allowing the iron and the slag to be removed from the bottom of the furnace through separate taps.

The iron obtained from a blast furnace is a brittle material called cast iron, or pig iron. It contains about $4 \%$ elemental carbon and smaller amounts of other


VAccording to the Lux-Flood acid-base theory, an acid is an oxide ion acceptor, and a base is an oxide ion donor. This theory is useful in the steel and ceramic industries, where oxides are commonly employed.

FIGURE 21.5 A diagram of a blast furnace for the reduction of iron ore. Modern blast furnaces are as large as 60 m in height and 14 m in diameter. They are designed for continuous operation and produce up to 10,000 tons of iron per day. Note the approximate temperatures and the chemical reactions that occur in the various regions of the furnace.

impurities such as elemental silicon, phosphorus, sulfur, and manganese, which are formed from their compounds in the reducing atmosphere of the furnace. The most important of several methods for purifying the iron and converting it to steel is the basic oxygen process. Molten iron from the blast furnace is exposed to a jet of pure oxygen gas for about 20 min in a furnace that is lined with basic oxides such as CaO . The impurities in the iron are oxidized, and the acidic oxides that form react with the basic CaO to yield a molten slag that can be poured off. Phosphorus, for example, is oxidized to $\mathrm{P}_{4} \mathrm{O}_{10}$, which then reacts with CaO to give molten calcium phosphate:

$$
\begin{aligned}
\mathrm{P}_{4}(l)+5 \mathrm{O}_{2}(g) & \longrightarrow \mathrm{P}_{4} \mathrm{O}_{10}(l) \\
6 \mathrm{CaO}(s)+\mathrm{P}_{4} \mathrm{O}_{10}(l) & \longrightarrow \mathrm{Ca}_{3}\left(\mathrm{PO}_{4}\right)_{2}(l) \\
\text { Basic oxide } \quad \text { Acidic oxide } & \text { Slag }
\end{aligned}
$$

Manganese also passes into the slag because its oxide is basic and reacts with added $\mathrm{SiO}_{2}$, yielding molten manganese silicate:

$$
\begin{aligned}
2 \mathrm{Mn}(l)+\mathrm{O}_{2}(g) & \longrightarrow \\
\mathrm{MnO}(s)+\mathrm{SiO}_{2}(s) & 2 \mathrm{MnO}(s) \\
\text { Basic oxide Acidic oxide } & \mathrm{MnSiO}_{3}(l)
\end{aligned}
$$

The basic oxygen process produces steels that contain about $1 \%$ carbon but only very small amounts of phosphorus and sulfur. Usually, the composition of the liquid steel is monitored by chemical analysis, and the amounts of oxygen and impure iron used are adjusted to achieve the desired concentrations of carbon and other impurities. The hardness, strength, and malleability of the steel depend on its chemical composition, on the rate at which the liquid steel is cooled, and on subsequent heat treatment of the solid. The mechanical and chemical properties of a steel can also be altered by adding other metals. Stainless steel, for example, is a
corrosion-resistant iron alloy that contains up to $30 \%$ chromium along with smaller amounts of nickel.

## 21.4 | Bonding in Metals

Thus far, we've discussed the sources, production, and properties of some important metals. Some properties, such as hardness and melting point, vary considerably among metals, but other properties are characteristic of metals in general. For instance, all metals can be drawn into wires (ductility) or beaten into sheets (malleability) without breaking into pieces like glass or an ionic crystal. Furthermore, all metals have a high thermal and electrical conductivity. When you touch a metal, it feels cold because the metal efficiently conducts heat away from your hand, and when you connect a metal wire to the terminals of a battery, it conducts an electric current.

To understand those properties, we need to look at the bonding in metals. We'll consider two theoretical models that are commonly used: the electron-sea model and the molecular orbital theory.


## Electron-Sea Model of Metals

If you try to draw an electron-dot structure for a metal, you'll quickly realize that there aren't enough valence electrons available to form an electron-pair bond between every pair of adjacent atoms. Sodium, for example, which has just one valence electron per atom $\left(3 s^{1}\right)$, crystallizes in a body-centered cubic structure in which each Na atom is surrounded by eight nearest neighbors (Section 10.8). Consequently, the valence electrons can't be localized in a bond between any particular pair of atoms. Instead, they are delocalized and belong to the crystal as a whole.

In the electron-sea model, a metal crystal is viewed as a three-dimensional array of metal cations immersed in a sea of delocalized electrons that are free to move throughout the crystal (Figure 21.6). The continuum of delocalized, mobile valence electrons acts as an electrostatic glue that holds the metal cations together.

The electron-sea model affords a simple qualitative explanation for the electrical and thermal conductivity of metals. Because the electrons are mobile, they are free to move away from a negative electrode and toward a positive electrode when a metal is subjected to an electrical potential. The mobile electrons can also conduct heat by carrying kinetic energy from one part of the crystal to another. Metals are malleable and ductile because the delocalized bonding extends in all

$\square$Peter P. Edwards and M. J. Sienko, "On the Occurrence of Metallic Character in the Periodic Table of the Elements," J. Chem. Educ., Vol. 60, 1983, 691-696.

0
Joseph F. Lomax, "Conducting Midshipmen-A Classroom Activity Modeling Extended Bonding in Solids," J. Chem. Educ., Vol. 69, 1992, 794-795.

1
Frank Rioux, "An Ionic Model for Metallic Bonding," J. Chem. Educ., Vol. 62, 1985, 383-384.

4 Because of its ductility, aluminum can be drawn into the wires used in electric power lines.

V
In the electron-sea model, electrons are delocalized and free to move throughout the entire metal.

The number of molecular orbitals equals the number of atomic orbitals from which the molecular orbitals were formed.

FIGURE 21.7 Molecular orbital energy levels for $\mathrm{Na}_{n}$ molecules. A crystal of sodium metal can be regarded as a giant $\mathrm{Na}_{n}$ molecule, where $n$ has a value of about $10^{20}$. As the value of $n$ increases, the energy levels merge into an almost continuous band. Because each Na atom has one $3 s$ valence electron and each MO can hold two electrons, the $3 s$ band is half-filled. In this and subsequent figures, the deep red color denotes the filled portion of a band.

FIGURE 21.6 Twodimensional representation of the electron-sea model of a metal. An ordered array of cations is immersed in a continuous distribution of delocalized, mobile valence electrons. The valence electrons do not belong to any particular metal ion but to the crystal as a whole.

directions; that is, it is not confined to oriented bond directions, as in covalent network solids like $\mathrm{SiO}_{2}$. When a metallic crystal is deformed, no localized bonds are broken. Instead, the electron sea simply adjusts to the new distribution of cations, and the energy of the deformed structure is similar to that of the original. Thus, the energy required to deform a metal like sodium is relatively small. The energy required to deform a transition metal like iron is greater because iron has more valence electrons $\left(4 s^{2} 3 d^{6}\right)$, and the electrostatic glue is therefore more dense.

## Molecular Orbital Theory for Metals

A more detailed understanding of the bonding in metals is provided by the molecular orbital theory, a model that is a logical extension of the molecular orbital description of small molecules discussed in Sections 7.13-7.15. Recall that in the $\mathrm{H}_{2}$ molecule the $1 s$ orbitals of the two H atoms overlap to give a $\sigma$ bonding MO and a higher-energy $\sigma^{*}$ antibonding MO. The bonding in the gaseous $\mathrm{Na}_{2}$ molecule is similar: The $3 s$ orbitals of the two Na atoms combine to give a $\sigma$ and a $\sigma^{*}$ MO. Because each Na atom has just one $3 s$ valence electron, the lower-energy bonding orbital is filled and the higher-energy antibonding orbital is empty:


Now consider what happens if we bring together an increasingly larger number of Na atoms to build up a crystal of sodium metal. The key idea to remember from Section 7.13 is that the number of molecular orbitals formed is the same as the number of atomic orbitals combined. Thus, there will be three MOs for a triatomic $\mathrm{Na}_{3}$ molecule, four MOs for $\mathrm{Na}_{4}$, and so on. A cubic crystal of sodium metal, 1.5 mm on an edge, contains about $10^{20} \mathrm{Na}$ atoms and therefore has about $10^{20} \mathrm{MOs}$, each of which is delocalized over all the atoms in the crystal. As shown in Figure 21.7, the difference in energy between successive MOs in an $\mathrm{Na}_{n}$ molecule decreases as the

number of Na atoms increases, so that the MOs merge into an almost continuous band of energy levels. Consequently, MO theory for metals is often called band theory. The bottom half of the band consists of bonding MOs and is filled, whereas the top half of the band consists of antibonding MOs and is empty.

How does band theory account for the electrical conductivity of metals? Because each of the MOs in a metal has a definite energy (Figure 21.7), each electron in a metal has a specific kinetic energy and a specific velocity. These values depend on the particular MO energy level and increase from the bottom of a band to the top. For a onedimensional metal wire, electrons traveling in opposite directions at the same speed have the same kinetic energy. Thus, the energy levels within a band occur in degenerate pairs; one set of energy levels applies to electrons moving to the right, and the other set applies to electrons moving to the left. (Recall from Section 5.12 that degenerate energy levels are levels that have the same energy.)

In the absence of an electrical potential, the two sets of levels are equally populated. That is, for each electron moving to the right, another electron moves to the left with exactly the same speed (Figure 21.8). As a result, there is no net electric current in either direction. In the presence of an electrical potential, however, those electrons moving to the right (toward the positive terminal of a battery) are accelerated, those moving to the left (toward the negative terminal) are slowed down, and those moving to the left with very slow speeds undergo a change of direction. Thus, the number of electrons moving to the right is now greater than the number moving to the left, and so there is a net electric current.


4 FIGURE 21.8 Half-filled $3 s$ band of MO energy levels for sodium metal. The direction of electron motion for the two degenerate sets of energy levels is indicated by the horizontal arrows. (a) In the absence of an electrical potential, the two sets of levels are equally populated, and no electric current flows through the wire. (b) In the presence of an electrical potential (positive electrode on the right), some of the electrons shift from one set of energy levels to the other, and there is a net current of electrons from left to right.

Figure 21.8 shows that an electrical potential can shift electrons from one set of energy levels to the other only if the band is partially filled. If the band is completely filled, there are no available vacant energy levels to which electrons can be excited, and therefore the two sets of levels must remain equally populated, even in the presence of an electrical potential. This means that an electrical potential can't accelerate the electrons in a completely filled band. Materials that have only completely filled bands are therefore electrical insulators. By contrast, materials that have partially filled bands are metals.

Based on the preceding analysis, we would predict that magnesium should be an insulator because it has the electron configuration [Ar] $3 s^{2}$ and should therefore have a completely filled $3 s$ band. This prediction is wrong, however, because we have not yet considered the $3 p$ valence orbitals. Just as the $3 s$ orbitals combine to form a $3 s$ band, so the $3 p$ orbitals can combine to form a $3 p$ band. If the $3 s$ and $3 p$ bands were widely separated in energy, the $3 s$ band would be filled, the $3 p$ band would be empty, and magnesium would be an insulator. In fact, though, the $3 s$ and $3 p$ bands overlap in energy, and the resulting composite band is only partially filled (Figure 21.9). Thus, magnesium is a conductor.

v
Metals have electrons in a partially filled band or in a filled band that overlaps with a second, empty band to give a partially filled composite band. Insulators have electrons in completely filled bands that do not overlap with empty bands.

© FIGURE 21.9 In magnesium metal, the $3 s$ and $3 p$ bands have similar energies and overlap to give a composite band consisting of four MOs per Mg atom. The composite band can accommodate eight electrons per Mg atom but is only partially filled, since each Mg atom has just two valence electrons. (In this and subsequent figures, the separate sets of energy levels for the right- and leftmoving electrons aren't shown.)

v
Population of the lower (bonding) portions of a band by electrons strengthens metallic bonding, whereas population of the upper (antibonding) portion of a band weakens metallic bonding.

Metallic Bonding activity

Transition metals have a $d$ band that can overlap the $s$ band to give a composite band consisting of six MOs per metal atom. Half of these MOs are bonding and half are antibonding. We might therefore expect maximum bonding for metals that have six valence electrons per metal atom because six electrons will just fill the bonding MOs and leave the antibonding MOs empty. In accord with this picture, maximum bonding near group 6B causes the melting points of the transition metals to also be at a maximum near group 6B (Section 20.2).

## Worked Example 21.1

The melting points of chromium and zinc are $1907^{\circ} \mathrm{C}$ and $420^{\circ} \mathrm{C}$, respectively. Use band theory to account for the difference.

## Strategy

The electron configurations are [Ar] $3 d^{5} 4 s^{1}$ for Cr and [ Ar$] 3 d^{10} 4 s^{2}$ for Zn . Assume that the $3 d$ and $4 s$ bands overlap. The composite band, which can accommodate 12 valence electrons per metal atom, will be half-filled for Cr and completely filled for Zn . The melting points will depend on the occupancy of the bonding and antibonding MOs.

## Solution

Strong bonding and consequently a high melting point are expected for Cr because all the bonding MOs are occupied and all the antibonding MOs are empty. Weak bonding and a low melting point are expected for Zn because both the bonding and the antibonding MOs are occupied. (The fact that Zn is a metal suggests that the $4 p$ orbitals also contribute to the composite band.)


## Worked Key Concept Example 21.2

The following pictures represent the electron population of the composite $s-d$ band for three metals-Ag, Mo, and Y:

(1)

(2)

(3)
(a) Which picture corresponds to which metal? Explain.
(b) Which metal has the highest melting point, and which has the lowest? Explain.
(c) Molybdenum is very hard, whereas silver is relatively soft. Explain.

## Strategy

As second-series transition metals, $\mathrm{Ag}, \mathrm{Mo}$, and Y have $5 s$ and $4 d$ valence electrons. All the valence electrons will occupy a composite $s-d$ band, which can accommodate 12 electrons per metal atom. To identify each metal, count the number of $5 s$ and $4 d$ valence electrons and compare that number with the population of bands in pictures (1), (2), and (3) above. The melting point and hardness of a metal is expected to increase as the difference between the number of bonding and antibonding electrons increases.

## Solution

(a) Ag in group 1 B has 11 valence electrons. Thus, its $s-d$ band is eleven-twelfths filled, which corresponds to picture (3). Mo in group 6B has six valence electrons. Its $s-d$ band is exactly half-filled, which corresponds to picture (1). Y in group 3B has three valence electrons. Its $s-d$ band is one-fourth filled, which corresponds to picture (2).
(b) Mo has the highest melting point because its bonding MOs are completely filled and its antibonding MOs are completely vacant. Ag has the lowest melting point because it has six bonding electrons and five antibonding electrons per Ag atom, an excess of only one bonding electron per Ag atom.
(c) Mo is very hard because it has an excess of six bonding electrons per Mo atom, Ag is very soft because it has an excess of only one bonding electron per Ag atom. Both hardness and melting point increase as metal-metal bonding increases.

- PROBLEM 21.2 Mercury metal is a liquid at room temperature. Use band theory to suggest a reason for its low melting point $\left(-39^{\circ} \mathrm{C}\right)$.

KEY CONCEPT PROBLEM 21.3 The following pictures represent the electron population of the composite $s-d$ band for three metals- $\mathrm{Hf}, \mathrm{Pt}$, and Re :

(a) Which picture corresponds to which metal? Explain.
(b) Which metal has the highest melting point, and which is the hardest? Explain.
(c) Which metal has the lowest melting point, and which is the softest? Explain.

### 21.5 Semiconductors

A semiconductor, such as silicon or germanium, is a material that has an electrical conductivity intermediate between that of a metal and that of an insulator. To understand the electrical properties of semiconductors, let's look first at the bonding in insulators. Consider diamond, for example, a covalent network solid in which each $C$ atom is bonded tetrahedrally to four other $C$ atoms (Figure 10.26). In a localized description of the bonding, $\mathrm{C}-\mathrm{C}$ electron-pair bonds result from the overlap of $s p^{3}$ hybrid orbitals. In a delocalized description, the $2 s$ and $2 p$ valence orbitals of all the C atoms combine to give bands of bonding and antibonding MOs—a total of four MOs per C atom. As is generally the case for insulators, the bonding MOs, called the valence band, and the higher-energy antibonding MOs,


Silicon and germanium are the two most common semiconductors.

VA semiconductor has a band gap between its valence and conduction bands that is small enough to allow a small equilibrium thermal electron population in the conduction band, leaving holes in the valence band. These electrons and holes can then move when a potential is applied.

$\square$The electrical conductivity of a metal decreases with an increase in temperature, whereas the electrical conductivity of a semiconductor increases with an increase in temperature.
called the conduction band, are separated in energy by a large band gap. The band gap in diamond is about $520 \mathrm{~kJ} / \mathrm{mol}$.

Each of the two bands in diamond can accommodate four electrons per C atom. Because carbon has just four valence electrons $\left(2 s^{2} 2 p^{2}\right)$, the valence band is completely filled and the conduction band is completely empty. Diamond is therefore an insulator because there are no vacant MOs in the valence band to which electrons can be excited by an electrical potential, and because population of the vacant MOs of the conduction band is prevented by the large band gap. By contrast, metallic conductors have no energy gap between the highest occupied and lowest unoccupied MOs. This fundamental difference between the energy levels of metals and insulators is illustrated in Figure 21.10.


4 FIGURE 21.10 Bands of MO energy levels for (a) a metallic conductor, (b) an electrical insulator, and (c) a semiconductor. A metallic conductor has a partially filled band. An electrical insulator has a completely filled valence band and a completely empty conduction band, which are separated in energy by a large band gap. In a semiconductor, the band gap is smaller. As a result, the conduction band is partially occupied with a few electrons, and the valence band is partially empty. Electrical conductivity in metals and semiconductors results from the presence of partially filled bands.

The MOs of a semiconductor are similar to those of an insulator, but the band gap in a semiconductor is smaller (Figure 21.10). As a result, a few electrons have enough thermal energy to jump the gap and occupy the higher-energy conduction band. The conduction band is thus partially filled, and the valence band is partially empty because it now contains a few unoccupied MOs. When an electrical potential is applied to a semiconductor, it conducts a small amount of current because the potential can accelerate the electrons in the partially filled bands. Table 21.3 shows how the electrical properties of the group 4A elements vary with the size of the band gap.

| TABLE 21.3 | Band Gaps for the Group 4A Elements |  |
| :--- | :--- | :--- |
| Element $^{*}$ | Band Gap (kJ/mol) | Type of Material |
| C (diamond) | 520 | Insulator |
| Si | 107 | Semiconductor |
| Ge | 65 | Semiconductor |
| Sn (gray tin) | 8 | Semiconductor |
| Sn (white tin) | 0 | Metal |
| Pb | 0 | Metal |

* $\mathrm{Si}, \mathrm{Ge}$, and gray Sn have the same structure as diamond.

The electrical conductivity of a semiconductor increases with increasing temperature because the number of electrons with sufficient energy to occupy the
conduction band increases as the temperature rises. At higher temperatures, there are more charge carriers (electrons) in the conduction band and more vacancies in the valence band. By contrast, the electrical conductivity of a metal decreases with increasing temperature. At higher temperatures, the metal cations undergo increased vibrational motion about their lattice sites, and vibration of the cations disrupts the flow of electrons through the crystal.

The conductivity of a semiconductor can be greatly increased by adding certain impurities in small ( ppm ) amounts, a process called doping. Consider, for example, the addition of a group 5A element such as phosphorus to a group 4A semiconductor such as silicon. Like diamond, silicon has a structure in which each Si atom is surrounded tetrahedrally by four others. The added P atoms occupy normal Si positions in the structure, but each $P$ atom has five valence electrons and therefore introduces an extra electron not needed for bonding. In the MO picture, the extra electrons occupy the conduction band, as shown in Figure 21.11a. The number of electrons in the conduction band of the doped silicon is much greater than in pure silicon, and the conductivity of the doped semiconductor is therefore correspondingly higher. Because the charge carriers are negative electrons, the silicon doped with a group 5A element is called an $\boldsymbol{n}$-type semiconductor.


FIGURE 21.11 MO energy levels for doped semiconductors. (a) An $n$-type semiconductor, such as silicon doped with phosphorus, has more electrons than needed for bonding and thus has negative electrons in the partially filled conduction band. (b) A $p$-type semiconductor, such as silicon doped with boron, has fewer electrons than needed for bonding and thus has vacancies-positive holes-in the valence band.

Now let's consider a semiconductor in which silicon is doped with a group 3A element such as boron. Each B atom has just three valence electrons and therefore does not have enough electrons to form bonds to its four Si neighbors. In the MO picture, the bonding MOs of the valence band are only partially filled, as shown in Figure 21.11b. The vacancies in the valence band can be regarded as positive holes in a filled band, and the silicon doped with a group 3A element is therefore called a $p$-type semiconductor. In a localized picture, a positive hole is a missing electron in a B-Si electron-pair bond. When an electron from an adjacent $\mathrm{Si}-\mathrm{Si}$ bond moves into the hole, the hole moves in the opposite direction.

Doped semiconductors are essential components in the modern solid-state electronic devices found in radios, television sets, pocket calculators, and computers. Devices such as transistors, which control electrical signals in these products, are made from $n$-type and $p$-type semiconductors. In modern integrated circuits, an amazing number of extremely small devices can be packed into a small space, thus decreasing the size and increasing the speed of electrical equipment. For example, computer microprocessors now contain up to 42 million transistors on a silicon chip with a surface area of about $2 \mathrm{~cm}^{2}$ and are able to execute as many as 1.5 billion instructions per second.

## Worked Example 21.3

Consider a crystal of germanium that has been doped with a small amount of aluminum. Is the doped crystal an $n$-type or $p$-type semiconductor? Compare the conductivity of the doped crystal with that of pure germanium.


## Strategy

Consider the location of germanium and aluminum in the periodic table and the number of valence electrons in the doped crystal relative to the number in pure germanium. Doped semiconductors with more electrons than the pure semiconductor are $n$-type, and those with fewer electrons are $p$-type.

## Solution

Germanium, like silicon, is a group 4A semiconductor, and aluminum, like boron, is a group 3A element. The doped germanium is therefore a $p$-type semiconductor because each Al atom has one less valence electron than needed for bonding to the four neighboring Ge atoms. (Like silicon, germanium has the diamond structure.) The valence band is thus partially filled, which accounts for the electrical conductivity. The conductivity is greater than that of pure germanium because the doped germanium has many more positive holes in the valence band. That is, it has more vacant MOs available to which electrons can be excited by an electrical potential.

- PROBLEM 21.4 Is germanium doped with arsenic an $n$-type or $p$-type semiconductor? Why is its conductivity greater than that of pure germanium?
- KEY CONCEPT PROBLEM 21.5 The following pictures show the electron population of the bands of MO energy levels for four materials-diamond, silicon, silicon doped with aluminum, and white tin:

(a) Which picture corresponds to which material?
(b) Arrange the four materials in order of increasing electrical conductivity. Explain.


## 21.6 | Superconductors

The discovery of high-temperature superconductors is surely one of the most exciting scientific developments in the last 20 years. It has stimulated an enormous amount of research in chemistry, physics, and materials science that could some day lead to a world of superfast computers, magnetically levitated trains, and power lines that carry electric current without loss of energy.

A superconductor is a material that loses all electrical resistance below a characteristic temperature called the superconducting transition temperature, $T_{c}$. This phenomenon was discovered in 1911 by the Dutch physicist Heike Kamerlingh Onnes, who found that mercury abruptly loses its electrical resistance when it is cooled with liquid helium to 4.2 K (Figure 21.12 ). Below its $T_{\mathrm{c}}$, a superconductor becomes a perfect conductor, and an electric current, once started, flows indefinitely without loss of energy.

Since 1911, scientists have been searching for materials that superconduct at higher temperatures, and more than 6000 superconductors are now known. Until 1986, however, the record value of $T_{\mathrm{c}}$ was only 23.2 K (for the compound $\mathrm{Nb}_{3} \mathrm{Ge}$ ). The situation changed dramatically in 1986 when K. Alex Müller and J. Georg Bednorz of the IBM Zürich Research Laboratory reported a $T_{\mathrm{C}}$ of 35 K for the nonstoichiometric barium lanthanum copper oxide $\mathrm{Ba}_{x} \mathrm{La}_{2-x} \mathrm{CuO}_{4}$, where $x$ has a

value of about 0.1. Soon thereafter, scientists found even higher values of $T_{\mathrm{c}}$ for other copper-containing oxides: 90 K for $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}, 125 \mathrm{~K}$ for $\mathrm{Tl}_{2} \mathrm{Ca}_{2} \mathrm{Ba}_{2} \mathrm{Cu}_{3} \mathrm{O}_{10}$, and 133 K for $\mathrm{HgCa}_{2} \mathrm{Ba}_{2} \mathrm{Cu}_{3} \mathrm{O}_{8+x}$, the recordholder as of this writing. High values of $T_{\mathrm{c}}$ for these compounds were completely unexpected because most metal oxides-nonmetallic inorganic solids called ceramics-are electrical insulators. Within just one year of discovering the first ceramic superconductor, Müller and Bednorz were awarded the 1987 Nobel Prize in physics.

The crystal structure of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$, the so-called 1-2-3 compound ( 1 yttrium, 2 bariums, and 3 coppers), is illustrated in Figure 21.13, and one unit cell of the structure is shown in Figure 21.14. The crystal contains parallel planes of Y, Ba, and Cu atoms. Two-thirds of the Cu atoms are surrounded by a square pyramid of five O atoms, some of which are shared with neighboring $\mathrm{CuO}_{5}$ groups to give two-dimensional layers of square pyramids. The remaining Cu atoms are surrounded by a square of four O atoms, two of which are shared with neighboring $\mathrm{CuO}_{4}$ squares to give chains of $\mathrm{CuO}_{4}$ groups. It's interesting to note that the Cu atoms have a fractional oxidation number of +2.33 , based on the usual oxidation


Yttrium

Barium

Copper
Oxygen
FIGURE 21.14 One unit cell of the crystal structure of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ contains one Y atom, two Ba atoms, three Cu atoms, and seven O atoms. In counting the Cu and O atoms, recall that the unit cell contains one-eighth of each corner atom, one-fourth of each edge atom, and one-half of each face atom (Section 10.8). The figure includes eight O atoms from neighboring unit cells to show the square pyramidal $\mathrm{CuO}_{5}$ groups and the square planar $\mathrm{CuO}_{4}$ groups.
 cal resistance of mercury falls to zero at its superconducting transition temperature, $T_{\mathrm{c}}=4.2 \mathrm{~K}$. Above $T_{\mathrm{c}}$, mercury is a metallic conductor: Its resistance increases (conductivity decreases) with increasing temperature. Below $T_{c}$, mercury is a superconductor.


A FIGURE 21.13 A computer graphics representation of the crystal structure of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$. Layers of Y atoms (yellow) and Ba atoms (blue) are sandwiched between layers of $\mathrm{CuO}_{5}$ square pyramids (red) and chains of square planar $\mathrm{CuO}_{4}$ groups (green).


© FIGURE 21.15 An experimental magnetically levitated train (Maglev) in Japan is suspended above superconducting magnets that are cooled with liquid helium. This five-car train has attained a speed of $552 \mathrm{~km} / \mathrm{h}$ in a manned vehicle run.
numbers of +3 for $\mathrm{Y},+2$ for Ba , and -2 for O . Both the infinitely extended layers of Cu and O atoms and the fractional oxidation number of Cu appear to play a role in the current flow, but a generally accepted theory of superconductivity in ceramic superconductors is not yet available. This is a field where experiment is far ahead of theory.

One of the most dramatic properties of a superconductor is its ability to levitate a magnet (see photo, page 915). When a superconductor is cooled below its $T_{\mathrm{c}}$ and a magnet is lowered toward it, the superconductor and the magnet repel each other, and the magnet hovers above the superconductor as though suspended in midair.

The repulsive force arises in the following way: When the magnet moves toward the superconductor, it induces a supercurrent in the surface of the superconductor that continues to flow even after the magnet stops moving. The supercurrent, in turn, induces a magnetic field in the superconductor that exactly cancels the field from the magnet. Thus, the net magnetic field within the bulk of the superconductor is zero, a phenomenon called the Meissner effect. Outside the superconductor, however, the magnetic fields due to the magnet and the supercurrent repel each other, just as the north poles of two bar magnets do. The magnet therefore experiences an upward magnetic force as well as the usual downward gravitational force, and it remains suspended above the superconductor at the point where the two forces are equal. Potential applications of the Meissner effect include high-speed, magnetically levitated trains (Figure 21.15).

Some applications of superconductors already exist. For example, powerful superconducting magnets are essential components in the magnetic resonance imaging (MRI) instruments widely used in medical diagnosis (see Section 22.10). Superconductors are also used to make the magnets that bend the path of charged particles in high-energy particle accelerators. All present applications, however, use conventional superconductors ( $T_{\mathrm{c}} \leq 20 \mathrm{~K}$ ) that are cooled to 4.2 K with liquid helium, an expensive substance that requires sophisticated cryogenic (cooling) equipment. Much of the excitement surrounding the new, high-temperature superconductors arises because their $T_{\mathrm{c}}$ values are above the boiling point of liquid nitrogen (bp 77 K ), an abundant refrigerant that is cheaper than milk. Of course, the search goes on for materials with still-higher values of $T_{\mathrm{c}}$. For applications such as long-distance electric power transmission, the goal is a material that superconducts at room temperature.

Several serious problems must be surmounted before applications of hightemperature superconductors can become a reality. Presently known ceramic superconductors are brittle powders with high melting points, so they are not easily fabricated into the wires and coils needed for electrical equipment. Also, the currents that these materials are able to carry at 77 K are still too low for practical applications. Thus, applications are likely in the future but are not right around the corner.

In 1991, scientists at AT\&T Bell Laboratories discovered a new class of hightemperature superconductors based on fullerene, the allotrope of carbon that contains $\mathrm{C}_{60}$ molecules (Sections 10.10 and 19.6). Called "buckyballs," after the architect R. Buckminster Fuller, these soccer ball-shaped $C_{60}$ molecules react with potassium to give $K_{3} \mathrm{C}_{60}$. This stable crystalline solid contains a face-centered cubic array of buckyballs, with $\mathrm{K}^{+}$ions in the cavities between the $\mathrm{C}_{60}$ molecules (Figure 21.16). At room temperature, $\mathrm{K}_{3} \mathrm{C}_{60}$ is a metallic conductor, but it becomes a superconductor at 18 K . The rubidium fulleride, $\mathrm{Rb}_{3} \mathrm{C}_{60}$, and a rubidium-thallium- $\mathrm{C}_{60}$ compound of unknown stoichiometry have higher $T_{\mathrm{c}}$ values of 30 K and $45-48 \mathrm{~K}$, respectively.

The copper oxide ceramic superconductors are two-dimensional conductors: They can conduct a current parallel to the layers of Cu and O atoms but not between the layers. The fullerides, by contrast, are three-dimensional conductors that conduct equally in all directions. Because of this property, they may prove to be superior materials for making superconducting wires.


FIGURE 21.16 A portion of one unit cell of the face-centered cubic structure of $\mathrm{K}_{3} \mathrm{C}_{60}$ viewed perpendicular to a cube face. The $\mathrm{C}_{60}$ "buckyballs" are located at the cube corners and face centers, and the $\mathrm{K}^{+}$ ions (red and blue spheres) are in two kinds of holes between the $\mathrm{C}_{60}{ }^{3-}$ ions. The $\mathrm{K}^{+}$ions shown in red lie in the plane of the cube face (the plane of the paper) and are surrounded octahedrally by six $\mathrm{C}_{60}{ }^{3-}$ ions. Those shown in blue lie in a plane one-fourth of a cell edge length below the plane of the paper and are surrounded tetrahedrally by four $\mathrm{C}_{60}{ }^{3-}$ ions.

PROBLEM 21.6 Show that one unit cell of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ (Figure 21.14) contains three Cu atoms and seven O atoms.

### 21.7 Ceramics

Ceramics are inorganic, nonmetallic, nonmolecular solids, including both crystalline materials such as quartz $\left(\mathrm{SiO}_{2}\right)$ and amorphous materials such as glasses. Known since ancient times, traditional silicate ceramics, such as pottery and porcelain, are made by heating aluminosilicate clays to high temperatures. Modern, so-called advanced ceramics-materials that have high-tech engineering, electronic, and biomedical applications-include oxide ceramics, such as alumina $\left(\mathrm{Al}_{2} \mathrm{O}_{3}\right)$, and nonoxide ceramics, such as silicon carbide $(\mathrm{SiC})$ and silicon nitride $\left(\mathrm{Si}_{3} \mathrm{~N}_{4}\right)$. Additional examples are listed in Table 21.4, which compares the properties of ceramics with those of aluminum and steel. (Note that oxide ceramics are named by replacing the -um ending of the element name with an $-a$; thus, BeO is beryllia, $\mathrm{ZrO}_{2}$ is zirconia, and so forth.)

TABLE 21.4 Properties of Some Ceramic and Metallic Materials

| Material | Melting <br> Point <br> $\left({ }^{\circ} \mathrm{C}\right)$ | $\begin{aligned} & \text { Density } \\ & \left(\mathrm{g} / \mathrm{cm}^{3}\right) \end{aligned}$ | Elastic <br> Modulus <br> (GPa) | Hardness (mohs) |
| :---: | :---: | :---: | :---: | :---: |
| Oxide ceramics |  |  |  |  |
| Alumina, $\mathrm{Al}_{2} \mathrm{O}_{3}$ | 2054 | 3.97 | 380 | 9 |
| Beryllia, BeO | 2578 | 3.01 | 370 | 8 |
| Zirconia, $\mathrm{ZrO}_{2}$ | 2710 | 5.68 | 210 | 8 |
| Nonoxide ceramics |  |  |  |  |
| Boron carbide, $\mathrm{B}_{4} \mathrm{C}$ | 2350 | 2.50 | 280 | 9 |
| Silicon carbide, SiC | 2830 | 3.16 | 400 | 9 |
| Silicon nitride, $\mathrm{Si}_{3} \mathrm{~N}_{4}$ | 1900 | 3.17 | 310 | 9 |
| Metals |  |  |  |  |
| Aluminum | 660 | 2.70 | 70 | 3 |
| Plain carbon steel | 1515 | 7.86 | 205 | 5 |

[^23]

A A silicon nitride rotor for use in gas-turbine engines.


In many respects, the properties of ceramics are superior to those of metals: Ceramics have higher melting points, and they are stiffer, harder, and more resistant to wear and corrosion. Moreover, they maintain much of their strength at high temperatures, where metals either melt or corrode because of oxidation. Silicon nitride and silicon carbide, for example, are stable to oxidation in air up to $1400-1500^{\circ} \mathrm{C}$, and oxide ceramics don't react with oxygen because they are already fully oxidized. Because ceramics are less dense than steel, they are attractive lightweight, high-temperature materials for replacing metal components in aircraft, space vehicles, and automotive engines.

Unfortunately, ceramics are brittle, as anyone who has dropped a coffee cup well knows. The brittleness, hardness, stiffness, and high melting points of ceramics are due to strong chemical bonding. Take silicon carbide, for example, a covalent network solid that crystallizes in the diamond structure (Figure 21.17). Each Si atom is bonded tetrahedrally to four C atoms, and each C atom is bonded tetrahedrally to four Si atoms. The strong, highly directional covalent bonds ( $D_{\mathrm{Si}-\mathrm{C}}=435 \mathrm{~kJ} / \mathrm{mol}$ ) prevent the planes of atoms from sliding over one another when the solid is subjected to the stress of a load or an impact. As a result, the solid can't deform to relieve the stress. It maintains its shape up to a point, but then the bonds give way suddenly, and the material fails catastrophically when the stress exceeds a certain threshold value. Oxide ceramics, in which the bonding is largely ionic, behave similarly. By contrast, metals are able to deform under stress because their planes of metal cations can slide easily in the electron sea (Section 21.4). As a result, metals dent but ceramics shatter.

FIGURE 21.17 One unit cell of the cubic form of silicon carbide, SiC . The Si atoms are located at the corners and face centers of a face-centered cubic unit cell, while the C atoms occupy cavities (tetrahedral holes) between four Si atoms. Each C atom is bonded tetrahedrally to four Si atoms, and each Si atom is bonded tetrahedrally to four C atoms. The crystal can't deform under stress because the bonds are strong and highly directional.


Ceramic processing, the series of steps that leads from raw material to the finished ceramic object, is important in determining the strength and the resistance to fracture of the product. Processing often begins with a fine powder, which is combined with an organic binder, shaped, compacted, and finally sintered at temperatures of $1300-2000^{\circ} \mathrm{C}$. Sintering, which occurs below the melting point, is a process in which the particles of the powder are "welded" together without completely melting. During sintering, the crystal grains grow larger and the density of the material increases as the void spaces between particles disappear. Unfortunately, impurities and remaining voids can lead to microscopic cracks that cause the material to fail under stress. It is therefore important to minimize impurities and voids by beginning with high-purity, fine powders that can be tightly compacted prior to sintering.

One approach to making such powders is the sol-gel method, in which a metal oxide powder is synthesized from a metal alkoxide, a compound derived from a metal and an alcohol. In the synthesis of titania $\left(\mathrm{TiO}_{2}\right)$ from titanium ethoxide, $\mathrm{Ti}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{4}$, for example, the $\mathrm{Ti}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{4}$ starting material is made by the reaction of titanium(IV) chloride with ethanol and ammonia in a benzene solution:


Pure $\mathrm{Ti}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{4}$ is then dissolved in an appropriate organic solvent, and water is added to bring about a hydrolysis reaction:

$$
\mathrm{Ti}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{4}+4 \mathrm{H}_{2} \mathrm{O} \xrightarrow{\text { Solution }} \mathrm{Ti}(\mathrm{OH})_{4}(s)+4 \mathrm{HOCH}_{2} \mathrm{CH}_{3}
$$

In this reaction, $\mathrm{Ti}-\mathrm{OCH}_{2} \mathrm{CH}_{3}$ bonds are broken, $\mathrm{Ti}-\mathrm{OH}$ bonds are formed, and ethanol is regenerated. $\mathrm{The} \mathrm{Ti}(\mathrm{OH})_{4}$ forms in the solution as a colloidal dispersion called a sol, consisting of extremely fine particles having a diameter of only $0.001-0.1 \mu \mathrm{~m}$. Subsequent reactions eliminate water molecules and form oxygen bridges between Ti atoms:


Because all the OH groups can undergo this reaction, the particles of the sol link together through a three-dimensional network of oxygen bridges, and the sol is converted to a more rigid, gelatinlike material called a gel. The remaining water and solvent are then removed by heating the gel, and $\mathrm{TiO}_{2}$ is obtained as a fine powder consisting of high-purity particles with a diameter less than $1 \mu \mathrm{~m}$ (Figure 21.18).


Oxide ceramics have many important uses. Alumina, for example, is the material of choice for making spark-plug insulators because of its high electrical resistance, high strength, high thermal stability, and chemical inertness. Because alumina is nontoxic and essentially inert in biological systems, it is used in constructing dental crowns and the heads of artificial hips. Alumina is also used as a substrate material for electronic circuit boards.

## Worked Example 21.4

Alumina $\left(\mathrm{Al}_{2} \mathrm{O}_{3}\right)$ powders can be prepared from aluminum ethoxide by the sol-gel method. Write a balanced equation for the hydrolysis of aluminum ethoxide.

## Strategy

First, determine the chemical formula of aluminum ethoxide, and then write a balanced equation for the reaction of aluminum ethoxide with water.

## Solution

Because aluminum is a group 3A element, it has an oxidation number of +3 . The ethoxide ligand is the anion of ethanol, $\mathrm{HOCH}_{2} \mathrm{CH}_{3}$, and has a charge of -1 . Since aluminum ethoxide is a neutral compound, its formula must be $\mathrm{Al}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{3}$. The hydrolysis reaction, which breaks the $\mathrm{Al}-\mathrm{OCH}_{2} \mathrm{CH}_{3}$ bonds and forms $\mathrm{Al}-\mathrm{OH}$ bonds, requires one $\mathrm{H}_{2} \mathrm{O}$ molecule for each ethoxide ligand:

$$
\mathrm{Al}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{3}+3 \mathrm{H}_{2} \mathrm{O} \longrightarrow \mathrm{Al}(\mathrm{OH})_{3}+3 \mathrm{HOCH}_{2} \mathrm{CH}_{3}
$$

Subsequent heating converts the aluminum hydroxide to alumina.

4 FIGURE 21.18 Electron micrographs of a titania powder consisting of tightly packed particles of $\mathrm{TiO}_{2}$ with a diameter less than $1 \mu \mathrm{~m}$ (left) and the dense ceramic produced by sintering the powder (right). The powder was made by the sol-gel method.

## Worked Example 21.5

The 1-2-3 ceramic superconductor $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ has been synthesized by the sol-gel method from a stoichiometric mixture of yttrium ethoxide, barium ethoxide, and copper(II) ethoxide in an appropriate organic solvent. The oxide product, before being heated in oxygen, has the formula $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{6.5}$. Write a balanced equation for the hydrolysis of the stoichiometric mixture of metal ethoxides.

## Strategy

First, determine the chemical formulas of the metal ethoxides, and then write a balanced equation for the reaction of the mixture of metal ethoxides with water.

## Solution

Because yttrium is a group 3 B element and has an oxidation number of +3 , the formula of yttrium ethoxide must be $\mathrm{Y}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{3}$. Similarly, because both barium (in group 2 A ) and copper(II) have an oxidation number of +2 , the formulas of barium ethoxide and copper ethoxide must be $\mathrm{Ba}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{2}$ and $\mathrm{Cu}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{2}$, respectively. If the three metal ethoxides were present separately, hydrolysis would give $\mathrm{Y}(\mathrm{OH})_{3}, \mathrm{Ba}(\mathrm{OH})_{2}$, and $\mathrm{Cu}(\mathrm{OH})_{2}$. Because they are present together in a 1:2:3 ratio, we write the product as $\mathrm{Y}(\mathrm{OH})_{3} \cdot 2 \mathrm{Ba}(\mathrm{OH})_{2} \cdot 3 \mathrm{Cu}(\mathrm{OH})_{2}$, or $\mathrm{YBa}_{2} \mathrm{Cu}_{3}(\mathrm{OH})_{13}$. Thus, the hydrolysis reaction requires $13 \mathrm{H}_{2} \mathrm{O}$ molecules for $13 \mathrm{OCH}_{2} \mathrm{CH}_{3}$ ligands, and the balanced equation is

$$
\begin{array}{r}
\mathrm{Y}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{3}+2 \mathrm{Ba}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{2}+3 \mathrm{Cu}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{2}+13 \mathrm{H}_{2} \mathrm{O} \longrightarrow \\
\mathrm{YBa}_{2} \mathrm{Cu}_{3}(\mathrm{OH})_{13}+13 \mathrm{HOCH}_{2} \mathrm{CH}_{3}
\end{array}
$$

Subsequent heating removes water, converting the mixed-metal hydroxide to the oxide $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{6.5}$, which is then oxidized to $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ by heating in $\mathrm{O}_{2}$ gas.

- PROBLEM 21.7 Silica glasses used in lenses, laser mirrors, and other optical components can be made by the sol-gel method. One step in the process is the hydrolysis of $\mathrm{Si}\left(\mathrm{OCH}_{3}\right)_{4}$. Write a balanced equation for the reaction.
- PROBLEM 21.8 Crystals of the oxide ceramic barium titanate, $\mathrm{BaTiO}_{3}$, have an unsymmetrical arrangement of ions, which gives the crystals an electric dipole moment. Such materials are called ferroelectrics and are used to make various electronic devices. Barium titanate can be made by the sol-gel method, which involves hydrolysis of a mixture of metal alkoxides. Write a balanced equation for the hydrolysis of a 1:1 mixture of barium isopropoxide and titanium isopropoxide, and explain how the resulting sol is converted to $\mathrm{BaTiO}_{3}$. (The isopropoxide ligand is the anion of isopropyl alcohol, $\mathrm{HOCH}\left(\mathrm{CH}_{3}\right)_{2}$, also known as rubbing alcohol.)


## 21.8 | Composites

We saw in the previous section that ceramics are brittle and prone to fracture. They can be strengthened and toughened, though, by mixing the ceramic powder prior to sintering with fibers of a second ceramic material, such as carbon, boron, or silicon carbide. The resulting hybrid material, called a ceramic composite, combines the advantageous properties of both components. An example is the composite consisting of fine grains of alumina reinforced with whiskers of silicon carbide. Whiskers are tiny, fiber-shaped particles, about $0.5 \mu \mathrm{~m}$ in diameter and $50 \mu \mathrm{~m}$ long, that are very strong because they are single crystals. Silicon carbidereinforced alumina possesses high strength and high shock resistance, even at high temperatures, and has therefore been used to make high-speed cutting tools for machining very hard steels.

How do fibers and whiskers increase the strength and fracture toughness of a composite material? First, fibers have great strength along the fiber axis because most of the chemical bonds are aligned in that direction. Second, there are several
ways in which fibers can prevent microscopic cracks from propagating to the point that they lead to the fracture of the material. The fibers can deflect cracks, thus preventing them from moving cleanly in one direction, and they can bridge cracks, thus holding the two sides of a crack together.

Silicon carbide-reinforced alumina is a composite in which both the fibers and the surrounding matrix are ceramics. There are other composites, however, in which the two phases are different types of materials. Examples are ceramic-metal composites, or cermets, such as aluminum metal reinforced with boron fiber, and ceramic-polymer composites, such as boron/epoxy and carbon/epoxy. (Epoxy is a resin consisting of long-chain organic molecules.) These materials are popular for aerospace and military applications because of their high strength-to-weight ratios. Boron-reinforced aluminum, for example, is used as a lightweight structural material in the space shuttle, and boron/epoxy and carbon/epoxy skins are used on military aircraft. Increased use of composite materials in commercial aircraft could result in weight savings of $20-30 \%$ and corresponding savings in fuel (which accounts for $10-15 \%$ of the cost of operating an airline).


Ceramic fibers used in composites are usually made by high-temperature methods. Carbon (graphite) fiber, for example, can be made by the thermal decomposition of fibers of polyacrylonitrile, a long-chain organic molecule also used to make the textile Orlon:


Polyacrylonitrile

In the final step of the multistep process, the carbon in the fiber is converted to graphite by heating at $1400-2500^{\circ} \mathrm{C}$. Similarly, silicon carbide fiber can be made by heating fibers that contain long-chain molecules with alternating silicon and carbon atoms:

$$
-\mathrm{SiH}_{2}-\mathrm{CH}_{2} \underset{\text { Repeating unit }}{-\mathrm{SiH}_{2}-\mathrm{CH}_{2}-} \mathrm{SiH}_{2}-\mathrm{CH}_{2}-\xrightarrow[-\mathrm{H}_{2}]{\text { Heat }} \mathrm{SiC} \text { fiber }
$$

- PROBLEM 21.9 Classify each of these composites as ceramic-ceramic, ceramicmetal, or ceramic-polymer:
(a) Cobalt/tungsten carbide
(b) Silicon carbide/zirconia
(c) Boron nitride/epoxy
(d) Boron carbide/titanium

V
Composites are hybrid materials of two ceramics, a ceramic and a metal, or a ceramic and a polymer.

4 The skin of the B-2 advanced technology aircraft is a strong, lightweight composite material that contains carbon fibers.

## Interlude <br> Diamonds and Diamond Films



These diamonds, fine enough to be of gem
quality, were made from graphite at high temquality, were made from gra
heir sparkling beauty has made diamonds an object of fascination and desire for millennia. Far more important-at least industri-ally-is their hardness. Diamond powder is unsurpassed for polishing, diamond-tipped bits are unequalled for drilling, and diamond-tipped saw blades are unparalleled for cutting. In fact, the industrial demand for diamonds dwarfs that of the jewelry trade and far outstrips the supply of natural stones. As a result of this demand, an intensive effort to produce synthetic diamonds began in the 1940s and culminated in the mid-1950s with independent announcements by the General Electric company in the United States and the Allemanna Svenska Elektriska company in Sweden of a method for preparing diamond from graphite.

The original General Electric method for producing diamond from graphite used high temperature $\left(2500^{\circ} \mathrm{C}\right)$ and pressure (100,000 atm) and yielded a black gritty material suitable for use as an industrial abrasive. Subsequent technical improvements have made possible the synthesis of gem-quality stones of up to 2 carats in mass (about 0.4 g ) at a price competitive with that of natural diamond. So inexpensive (relatively speaking) have synthetic diamonds become that the electronics industry uses them as heat sinks to help cool heat-producing semiconductor components.
This application arises from another important property of diamond: its ability to conduct heat about four times better than either copper or silver.

The most exciting recent advance in diamond-producing technology was the development by several research groups in the 1980s of methods for depositing diamond films on a variety of surfaces at low pressure. When a dilute mixture (about $1 \%$ by volume) of $\mathrm{CH}_{4}$ in $\mathrm{H}_{2}$ gas at a pressure of about 40 mm Hg is heated in a microwave discharge to a temperature near $1000^{\circ} \mathrm{C}$, free carbon and hydrogen atoms are produced. The hydrogen atoms evidently impede the formation of graphite, and the carbon atoms therefore deposit on a nearby surface in the form of diamond. The thin, filmlike coating that results is made up of tiny diamond crystals about 10-20 nm in diameter.

Imagine the possibilities, some of which are just now becoming reality: Tools, knife blades, and scalpels coated with diamond remain forever sharp. Eyeglass lenses and wristwatches coated with diamond remain scratch-free. High-fidelity loudspeakers coated with diamond give a nearly perfect, undistorted sound at high frequencies. Hip joints and other biological implants coated with diamond are not rejected by the body's immune system.

Further improvements in deposition technology are still needed-only substrates stable at a temperature of $1000^{\circ} \mathrm{C}$ can be coated at present-but the time may not be too far off before diamond coatings on a variety of consumer products become commonplace.

- PROBLEM 21.10 Is diamond a ceramic? Explain.
- PROBLEM 21.11 Draw one unit cell of a diamond crystal, and explain why diamond is so hard.

Most metals occur in nature as minerals-the silicates, carbonates, oxides, sulfides, phosphates, and chlorides that make up the rocks of the earth's crust. The type of mineral in which a metal is found depends on the metal's location in the periodic table. Minerals from which metals can be produced economically are called ores.

Metallurgy, the science and technology of extracting metals from their ores, involves three steps: (1) concentration and chemical treatment to separate the mineral from impurities called gangue; (2) reduction of the mineral to the free metal; and (3) refining or purification of the metal. The first step uses processes such as flotation and roasting. The reduction method (roasting, chemical reduction, or electrolysis) depends on the activity of the metal. The refining step involves distillation, chemical purification (for example, the Mond process for nickel), or electrorefining.

Iron is produced in a blast furnace by reducing iron oxide ores with CO . Added limestone $\left(\mathrm{CaCO}_{3}\right)$ decomposes to CaO , which reacts with $\mathrm{SiO}_{2}$ and other acidic oxide impurities to yield a molten slag (mainly $\mathrm{CaSiO}_{3}$ ) that is separated from the molten iron at the bottom of the furnace. The iron is converted to steel by the basic oxygen process, which removes impurities such as elemental $\mathrm{Si}, \mathrm{P}, \mathrm{S}$, and most of the C .

Two bonding models are used for metals. The electronsea model pictures a metal as an array of metal cations immersed in a sea of delocalized, mobile valence electrons that act as an electrostatic glue. In the molecular orbital theory for metals, also called band theory, the delocalized valence electrons occupy a vast number of MO energy levels that are so closely spaced that they merge into an almost continuous band. Both theories account for properties such as malleability, ductility, and high thermal and electrical conductivity, but band theory better explains how the number of valence electrons affects properties such as melting point and hardness.

Band theory also accounts for the electrical properties of metals, insulators, and semiconductors. Because electrical conductivity involves excitation of valence electrons to readily accessible higher-energy MOs, materials with partially filled bands are metallic conductors, and materials with only completely filled bands are electrical insulators. In insulators, the bonding MOs, called the valence band, and the antibonding MOs, called the conduction band, are separated in energy by a large band gap. In semiconductors, the band gap is smaller, and a few electrons have enough energy to occupy the conduction band. The resulting partially filled valence and conduction bands give rise to a small conductivity. The conductivity can be increased by doping-adding a group 5A impurity to a group 4A element, which gives an $n$-type semiconductor, or adding a group 3A impurity to a group 4A element, which gives a $p$-type semiconductor.

A superconductor is a material that loses all electrical resistance below a characteristic temperature called the superconducting transition temperature, $T_{\mathbf{c}}$. An example is $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}\left(T_{\mathrm{c}}=90 \mathrm{~K}\right)$. Below $T_{\mathrm{c}}$, a superconductor can levitate a magnet, a consequence of the Meissner effect.

Ceramics are inorganic, nonmetallic, nonmolecular solids. Modern advanced ceramics include oxide ceramics such as $\mathrm{Al}_{2} \mathrm{O}_{3}$ and $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ and nonoxide ceramics such as SiC and $\mathrm{Si}_{3} \mathrm{~N}_{4}$. Ceramics are generally higher-melting, lighter, stiffer, harder, and more resistant to wear and corrosion than metals. One approach to ceramic processing is the sol-gel method, involving hydrolysis of a metal alkoxide. The strength and fracture toughness of ceramics can be increased by making ceramic composites, hybrid materials such as $\mathrm{Al}_{2} \mathrm{O}_{3} / \mathrm{SiC}$ in which fine grains of $\mathrm{Al}_{2} \mathrm{O}_{3}$ are reinforced by whiskers of SiC . Other types of composites include ceramic-metal composites and ceramic-polymer composites.

## advanced ceramic 933

alloy 918
band gap 928
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## Key Concept Summary

- 



## Understanding Key Concepts

Problems 21.1-21.11 appear within the chapter.
21.12 Look at the location of elements A, B, C, and D in the following periodic table:


Without looking at Figure 21.2, predict whether these elements are likely to be found in nature as carbonates, oxides, sulfides, or in uncombined form. Explain.
21.13 Among the methods for extracting metals from their ores are (i) roasting a metal sulfide, (ii) chemical reduc-
 tion of a metal oxide, and (iii) electrolysis. The preferred method depends on the $E^{\circ}$ value for the reduction half-reaction $\mathrm{M}^{n+}(a q)+n \mathrm{e}^{-} \rightarrow \mathrm{M}(s)$.
(a) Which method is appropriate for the metals with the most negative $E^{\circ}$ values?
(b) Which method is appropriate for the metals with the most positive $E^{\circ}$ values?
(c) Which method is appropriate for metals A, B, C, and D in the following periodic table?

21.14 The following pictures show the electron populations of the bands of MO energy levels for four different materials:

(1)

(2)

(3)

(4)
(a) Classify each material as an insulator, a semiconductor, or a metal.
(b) Arrange the four materials in order of increasing electrical conductivity. Explain.
(c) Tell whether the conductivity of each material increases or decreases when the temperature increases.
21.15 The following pictures show the electron populations of the composite $s-d$ bands for three different transition
 metals:

(a) Which metal has the highest melting point? Explain.
(b) Which metal has the lowest melting point? Explain.
(c) Arrange the metals in order of increasing hardness. Explain.
21.16 The following picture represents the electron population of the bands of MO energy levels for elemental silicon:

(a) Identify the valence band, conduction band, and band gap.
(b) In a drawing, show how the electron population changes when the silicon is doped with gallium.
(c) In a drawing, show how the electron population changes when the silicon is doped with arsenic.
(d) Compare the electrical conductivity of the doped silicon samples with that of pure silicon. Account for the differences.
21.17 Sketch the electron populations of the bands of MO energy levels for elemental carbon (diamond), silicon, germanium, gray tin, and white tin. (Band gap data are given in Table 21.3.) Your sketches should show how the populations of the different bands vary with a change in the group 4A element.

## Additional Problems

## Sources of the Metallic Elements

21.18 List three metals that are found in nature as oxide ores.
21.19 List three metals that are found in nature in uncombined form.
21.20 Locate the following metals in the periodic table, and predict whether they are likely to be found in nature as oxides, sulfides, or in uncombined form:
(a) Copper
(b) Zirconium
(c) Palladium
(d) Bismuth
21.21 Locate the following metals in the periodic table, and predict whether they are likely to be found in nature as oxides, sulfides, or in uncombined form:
(a) Vanadium
(b) Silver
(c) Rhodium
(d) Hafnium
21.22 Explain why early transition metals occur in nature as oxides but late transition metals occur as sulfides.
21.23 Explain why iron occurs in nature as an oxide but calcium occurs as a carbonate.
21.24 Name the following minerals:
(a) $\mathrm{Fe}_{2} \mathrm{O}_{3}$
(b) PbS
(c) $\mathrm{TiO}_{2}$
(d) $\mathrm{CuFeS}_{2}$
21.25 Write chemical formulas for the following minerals:
(a) Cinnabar
(b) Bauxite
(c) Sphalerite
(d) Chromite

## Metallurgy

21.26 Describe the flotation process for concentrating a metal sulfide ore, and explain why this process would not work well for concentrating a metal oxide ore.
21.27 Gallium is a minor constituent in bauxite, $\mathrm{Al}_{2} \mathrm{O}_{3} \cdot x \mathrm{H}_{2} \mathrm{O}$, and like aluminum, forms an amphoteric oxide, $\mathrm{Ga}_{2} \mathrm{O}_{3}$. Explain how the Bayer process makes it possible to separate $\mathrm{Ga}_{2} \mathrm{O}_{3}$ from $\mathrm{Fe}_{2} \mathrm{O}_{3}$, which is also present in bauxite. Write a balanced net ionic equation for the reaction.
21.28 Zinc, cadmium, and mercury are found in nature as sulfide ores. Values of $E^{\circ}$ for the reduction half-reaction $\mathrm{M}^{2+}(a q)+2 \mathrm{e}^{-} \rightarrow \mathrm{M}(s)$ are -0.76 V for $\mathrm{M}=\mathrm{Zn}$, -0.40 V for $\mathrm{M}=\mathrm{Cd}$, and +0.85 V for $\mathrm{M}=\mathrm{Hg}$. Explain why roasting sphalerite ( ZnS ) gives ZnO but roasting cinnabar (HgS) gives elemental mercury. What product would you expect from roasting CdS?
21.29 Zinc metal is produced by reducing ZnO with coke, and magnesium metal is produced by the electrolysis of molten $\mathrm{MgCl}_{2}$. Look at the standard reduction potentials in Appendix D, and explain why magnesium can't be prepared by the method used for zinc.
21.30 Complete and balance each of the following equations:
(a) $\mathrm{V}_{2} \mathrm{O}_{5}(s)+\mathrm{Ca}(s) \rightarrow$
(b) $\mathrm{PbS}(s)+\mathrm{O}_{2}(g) \rightarrow$
(c) $\mathrm{MoO}_{3}(\mathrm{~s})+\mathrm{H}_{2}(g) \rightarrow$
(d) $\mathrm{MnO}_{2}(s)+\mathrm{Al}(s) \rightarrow$
(e) $\mathrm{MgCl}_{2}(l) \xrightarrow{\text { Electrolysis }}$
21.31 Complete and balance each of the following equations:
(a) $\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+\mathrm{H}_{2}(g) \rightarrow$
(b) $\mathrm{Cr}_{2} \mathrm{O}_{3}(s)+\mathrm{Al}(s) \rightarrow$
(c) $\mathrm{Ag}_{2} \mathrm{~S}(s)+\mathrm{O}_{2}(g) \rightarrow$
(d) $\mathrm{TiCl}_{4}(g)+\mathrm{Mg}(l) \rightarrow$
(e) $\mathrm{LiCl}(l) \xrightarrow{\text { Electrolysis }}$
21.32 Use the data in Appendix B to calculate $\Delta H^{\circ}$ and $\Delta G^{\circ}$ for the roasting of sphalerite, ZnS :

$$
2 \mathrm{ZnS}(s)+3 \mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{ZnO}(s)+2 \mathrm{SO}_{2}(g)
$$

Explain why $\Delta H^{\circ}$ and $\Delta G^{\circ}$ have different values, and account for the sign of $\left(\Delta H^{\circ}-\Delta G^{\circ}\right)$.
21.33 Use the thermodynamic data in Appendix B to calculate $\Delta H^{\circ}$ and $\Delta G^{\circ}$ for the roasting of cinnabar, HgS :

$$
\mathrm{HgS}(s)+\mathrm{O}_{2}(g) \longrightarrow \mathrm{Hg}(l)+\mathrm{SO}_{2}(g)
$$

Explain why $\Delta H^{\circ}$ and $\Delta G^{\circ}$ have different values, and account for the sign of $\left(\Delta H^{\circ}-\Delta G^{\circ}\right)$.
21.34 Ferrochrome, an iron-chromium alloy used to make stainless steel, is produced by reducing chromite ( $\mathrm{FeCr}_{2} \mathrm{O}_{4}$ ) with coke:

$$
\mathrm{FeCr}_{2} \mathrm{O}_{4}(\mathrm{~s})+4 \mathrm{C}(\mathrm{~s}) \longrightarrow \underbrace{\mathrm{Fe}(\mathrm{~s})+2 \mathrm{Cr}(\mathrm{~s})}_{\text {Ferrochrome }}+4 \mathrm{CO}(\mathrm{~g})
$$

(a) How many kilograms of chromium can be obtained by the reaction of 236 kg of chromite with an excess of coke?
(b) How many liters of carbon monoxide at $25^{\circ} \mathrm{C}$ and 740 mm Hg are obtained as a by-product?
21.35 In one step of the industrial process for producing copper from chalcopyrite $\left(\mathrm{CuFeS}_{2}\right)$, molten copper(I) sulfide is reduced with a blast of hot air:

$$
\mathrm{Cu}_{2} \mathrm{~S}(l)+\mathrm{O}_{2}(g) \longrightarrow 2 \mathrm{Cu}(l)+\mathrm{SO}_{2}(g)
$$

(a) How many kilograms of $\mathrm{Cu}_{2} \mathrm{~S}$ must be reduced to account for the world's annual copper production of about $8 \times 10^{9} \mathrm{~kg}$ ?
(b) How many liters of $\mathrm{SO}_{2}$ at STP are produced as a by-product?
(c) If all the $\mathrm{SO}_{2}$ escaped into the atmosphere and was converted to sulfuric acid in acid rain, how many kilograms of $\mathrm{H}_{2} \mathrm{SO}_{4}$ would there be in the rain?
21.36 Nickel, used to make stainless steel, can be purified by electrorefining. The electrolysis cell has an impure nickel anode, a pure nickel cathode, and an aqueous solution of nickel sulfate as the electrolyte. How many kilograms of nickel can be refined in 8.00 h if the current passed through the cell is held constant at 52.5 A?
21.37 Pure copper for use in electrical wiring is obtained by electrorefining. How many hours are required to transfer 7.50 kg of copper from an impure copper anode to a pure copper cathode if the current passed through the electrolysis cell is held constant at 40.0 A ?

## Iron and Steel

21.38 Write a balanced equation for the overall reaction that occurs in a blast furnace when iron ore is reduced to iron metal. Identify the oxidizing agent and the reducing agent.
21.39 What is the role of coke in the commercial process for producing iron? Write balanced equations for the relevant chemical reactions.
21.40 What is slag, and what is its role in the commercial process for producing iron?
21.41 Why is limestone added to the blast furnace in the commercial process for producing iron? Write balanced equations for the relevant chemical reactions.
21.42 Briefly describe the basic oxygen process. Write balanced equations for the relevant reactions.
21.43 Why does slag form in the basic oxygen process? Write balanced equations for the relevant reactions.
21.44 When iron ore is reduced in a blast furnace, some of the $\mathrm{SiO}_{2}$ impurity is also reduced by reaction with carbon to give elemental silicon and carbon monoxide. The silicon is subsequently reoxidized in the basic oxygen process, and the resulting $\mathrm{SiO}_{2}$ reacts with CaO , yielding slag, which is then separated from the molten steel. Write balanced equations for the three reactions involving $\mathrm{SiO}_{2}$.
21.45 In a blast furnace, some of the $\mathrm{CaSO}_{4}$ impurity in iron ore is reduced by carbon, yielding elemental sulfur and carbon monoxide. The sulfur is subsequently oxidized in the basic oxygen process, and the product reacts with CaO to give a molten slag. Write balanced equations for the reactions.

## Bonding in Metals

21.46 Potassium metal crystallizes in a body-centered cubic structure. Draw one unit cell, and try to draw an electron-dot structure for bonding of the central K atom to its nearest-neighbor K atoms. What is the problem?
21.47 Describe the electron-sea model of the bonding in cesium metal. Cesium has a body-centered cubic structure.
21.48 How does the electron-sea model account for the malleability and ductility of metals?
21.49 How does the electron-sea model account for the electrical and thermal conductivity of metals?
21.50 Cesium metal is very soft, and tungsten metal is very hard. Explain the difference using the electron-sea model.
21.51 Sodium melts at $98^{\circ} \mathrm{C}$, and magnesium melts at $649^{\circ} \mathrm{C}$. Account for the higher melting point of magnesium using the electron-sea model.
21.52 Why is the molecular orbital theory for metals called band theory?
21.53 Draw an MO energy-level diagram that shows the population of the $4 s$ band for potassium metal.
21.54 How does band theory account for the electrical conductivity of metals?
21.55 Materials with partially filled bands are metallic conductors, and materials with only completely filled bands are electrical insulators. Explain why the population of the bands affects the conductivity.
21.56 Draw an MO energy-level diagram for beryllium metal, and show the population of the MOs for the following two cases:
(a) The $2 s$ and $2 p$ bands are well separated in energy.
(b) The $2 s$ and $2 p$ bands overlap in energy.

Which diagram agrees with the fact that beryllium has a high electrical conductivity? Explain.
21.57 Draw an MO energy-level diagram for calcium metal, and show the population of the MOs for the following two cases:
(a) The $4 s$ and $3 d$ bands are well separated in energy.
(b) The $4 s$ and $3 d$ bands overlap in energy.

Which diagram agrees with the fact that calcium has a high electrical conductivity? Explain.
21.58 The melting points for the second-series transition elements increase from $1522^{\circ} \mathrm{C}$ for yttrium to $2623^{\circ} \mathrm{C}$ for molybdenum and then decrease again to $321^{\circ} \mathrm{C}$ for cadmium. Account for the trend using band theory.
21.59 Copper has a Mohs hardness value of 3, and iron has a Mohs hardness value of 5 . Use band theory to explain why copper is softer than iron.

## Semiconductors

21.60 Define a semiconductor, and give three examples.
21.61 Explain each of the following terms:
(a) Valence band
(b) Conduction band
(c) Band gap
(d) Doping
21.62 Draw the bands of MO energy levels and the electron population for:
(a) A semiconductor
(b) An electrical insulator

Explain why a semiconductor has the higher electrical conductivity.
21.63 Draw the bands of MO energy levels and the electron population for:
(a) A semiconductor
(b) A metallic conductor

Explain why a semiconductor has the lower electrical conductivity.
21.64 How does the electrical conductivity of a semiconductor change as the size of the band gap increases? Explain.
21.65 How does the electrical conductivity of a semiconductor change as the temperature increases? Explain.
21.66 Explain what an $n$-type semiconductor is, and give an example. Draw an MO energy-level diagram, and show the population of the valence band and the conduction band for an $n$-type semiconductor.
21.67 Explain what a $p$-type semiconductor is, and give an example. Draw an MO energy-level diagram, and show the population of the valence band and the conduction band for a $p$-type semiconductor.
21.68 Explain why germanium doped with phosphorus has a higher electrical conductivity than pure germanium.
21.69 Explain why silicon doped with gallium has a higher electrical conductivity than pure silicon.
21.70 Classify the following semiconductors as $n$-type or $p$-type:
(a) Si doped with In
(b) Ge doped with Sb
(c) Gray Sn doped with As
21.71 Classify the following semiconductors as $n$-type or $p$-type:
(a) Ge doped with As
(b) Ge doped with B
(c) Si doped with Sb
21.72 Arrange the following materials in order of increasing electrical conductivity:
(a) Cu
(b) $\mathrm{Al}_{2} \mathrm{O}_{3}$
(c) Fe
(d) Pure Ge
(e) Ge doped with In
21.73 Arrange the following materials in order of increasing electrical conductivity:
(a) Pure gray Sn
(b) Gray Sn doped with Sb
(c) NaCl
(d) Ag
(e) Pure Si

## Superconductors

21.74 What are the two most characteristic properties of a superconductor?
21.75 $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ is a superconductor below its $T_{\mathrm{c}}$ of 90 K and a metallic conductor above 90 K . Make a rough plot of electrical resistance versus temperature for $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$.
21.76 Compare the structure and properties of ceramic superconductors such as $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ with those of fullerenebased superconductors such as $\mathrm{Rb}_{3} \mathrm{C}_{60}$.
21.77 Look at Figure 21.14, and identify the coordination numbers of the $\mathrm{Cu}, \mathrm{Y}$, and Ba atoms.

## Ceramics and Composites

21.78 What is a ceramic, and what properties distinguish a ceramic from a metal?
21.79 Contrast the bonding in ceramics with the bonding in metals.
21.80 Why are ceramics more wear-resistant than metals?
21.81 Why are oxide ceramics more corrosion-resistant than metals?
21.82 Silicon nitride $\left(\mathrm{Si}_{3} \mathrm{~N}_{4}\right)$, a high-temperature ceramic useful for making engine components, is a covalent network solid in which each Si atom is bonded to four N atoms and each N atom is bonded to three Si atoms. Explain why silicon nitride is more brittle than a metal like copper.
21.83 Magnesia (MgO), used as an insulator for electrical heating devices, has a face-centered cubic structure like that of NaCl . Draw one unit cell of the structure of MgO , and explain why MgO is more brittle than magnesium metal.
21.84 What is ceramic processing?
21.85 Describe what happens when a ceramic powder is sintered.
21.86 Describe the differences between a sol and a gel.
21.87 What is the difference between a hydrolysis reaction and the reaction that occurs when a sol is converted to a gel?
21.88 Zirconia $\left(\mathrm{ZrO}_{2}\right)$, an unusually tough oxide ceramic, has been used to make very sharp table knives. Write a balanced equation for the hydrolysis of zirconium isopropoxide in the sol-gel method for making zirconia powders. The isopropoxide ligand is the anion of isopropyl alcohol, $\mathrm{HOCH}\left(\mathrm{CH}_{3}\right)_{2}$.
21.89 Zinc oxide is a semiconducting ceramic used to make varistors (variable resistors). Write a balanced equation for the hydrolysis of zinc ethoxide in the sol-gel method for making ZnO powders.
21.90 Describe the reactions that occur when an $\mathrm{Si}(\mathrm{OH})_{4}$ sol becomes a gel. What is the formula of the ceramic obtained when the gel is dried and sintered?
21.91 Describe the reactions that occur when a $\mathrm{Y}(\mathrm{OH})_{3}$ sol becomes a gel. What is the chemical formula of the ceramic obtained when the gel is dried and sintered?
21.92 Silicon nitride powder can be made by the reaction of silicon tetrachloride vapor with gaseous ammonia. The by-product is gaseous hydrogen chloride. Write a balanced equation for the reaction.
21.93 Boron, which is used to make composites, is deposited on a tungsten wire when the wire is heated electrically in the presence of boron trichloride vapor and gaseous hydrogen. Write a balanced equation for the reaction.
21.94 Explain why graphite/epoxy composites are good materials for making tennis rackets and golf clubs.
21.95 Explain why silicon carbide-reinforced alumina is stronger and tougher than pure alumina.

## General Problems

21.96 Imagine a planet with an atmosphere that contains $\mathrm{O}_{2}$ and $\mathrm{SO}_{2}$ but no $\mathrm{CO}_{2}$. Give the chemical composition of the minerals you would expect to find for the alkaline earth metals on such a planet.
21.97 Superconductors with values of $T_{\mathrm{c}}$ above 77 K are of special interest. What's so special about 77 K ?
21.98 What properties of metals are better explained by band theory than by the electron-sea model?
21.99 Tungsten is hard and has a very high melting point $\left(3422^{\circ} \mathrm{C}\right)$, and gold is soft and has a relatively low melting point $\left(1064^{\circ} \mathrm{C}\right)$. Are these facts in better agreement with the electron-sea model or the MO model (band theory)? Explain.
21.100 Explain why the enthalpy of vaporization of vanadium ( $460 \mathrm{~kJ} / \mathrm{mol}$ ) is much larger than that of zinc ( $114 \mathrm{~kJ} / \mathrm{mol}$ ).
21.101 Classify each of the following materials as a metallic conductor, an $n$-type semiconductor, a $p$-type semiconductor, or an electrical insulator:
(a) MgO
(b) Si doped with Sb
(c) White tin
(d) Ge doped with Ga
(e) Stainless steel
21.102 Gallium arsenide, a material used to manufacture laser printers and compact-disc players, has a band gap of $130 \mathrm{~kJ} / \mathrm{mol}$. Is GaAs a metallic conductor, a semiconductor, or an electrical insulator? With what group 4A element is GaAs isoelectronic? (Isoelectronic substances have the same number of electrons.) Draw an MO energy-level diagram for GaAs, and show the population of the bands.
21.103 A $3.4 \times 10^{3} \mathrm{~kg}$ batch of cast iron contains $0.45 \%$ by mass of phosphorus as an impurity. In the conversion of cast iron to steel by the basic oxygen process, the phosphorus is oxidized to $\mathrm{P}_{4} \mathrm{O}_{10}$, which then reacts with CaO and is removed as slag.
(a) Write balanced equations for the oxidation of $\mathrm{P}_{4}$ and for the formation of slag.
(b) How many kilograms of CaO are required to react with all the $\mathrm{P}_{4} \mathrm{O}_{10}$ ?
21.104 The $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ superconductor can be synthesized by the sol-gel method from a stoichiometric mixture of metal ethoxides. How many grams of $\mathrm{Y}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{3}$ and how many grams of $\mathrm{Ba}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{2}$ are required to react with 75.4 g of $\mathrm{Cu}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{2}$ and an excess of water? Assuming a $100 \%$ yield, how many grams of $\mathrm{YBa}_{2} \mathrm{Cu}_{3} \mathrm{O}_{7}$ are obtained?
21.105 A 0.3249 g sample of stainless steel was analyzed for iron by dissolving the sample in sulfuric acid and titrating the $\mathrm{Fe}^{2+}$ in the resulting solution with 0.01854 M $\mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$. If 38.89 mL of the $\mathrm{K}_{2} \mathrm{Cr}_{2} \mathrm{O}_{7}$ solution was required to reach the equivalence point, what is the mass percentage of iron in the steel?
21.106 Mullite, $3 \mathrm{Al}_{2} \mathrm{O}_{3} \cdot 2 \mathrm{SiO}_{2}$, a high-temperature ceramic being considered for use in engines, can be made by the sol-gel method.
(a) Write a balanced equation for formation of the sol by hydrolysis of a stoichiometric mixture of aluminum ethoxide and tetraethoxysilane, $\mathrm{Si}\left(\mathrm{OCH}_{2} \mathrm{CH}_{3}\right)_{4}$.
(b) Describe the reactions that convert the sol to a gel.
(c) What additional steps are required to convert the gel to the ceramic product?
21.107 The glass in photochromic sunglasses is called a nanocomposite because it contains tiny silver halide particles with a diameter of less than 10 nm . This glass darkens and becomes less transparent outdoors in sunlight but returns to its original transparency indoors, where there is less light. How might these reversible changes occur?
21.108 Small molecules with $\mathrm{C}=\mathrm{C}$ double bonds, called monomers, can join with one another to form long chain molecules called polymers. Thus, acrylonitrile, $\mathrm{H}_{2} \mathrm{C}=\mathrm{CHCN}$, polymerizes under appropriate conditions to give polyacrylonitrile, a common starting material for producing the carbon fibers used in composites.

(a) Write electron-dot structures for acrylonitrile and polyacrylonitrile, and show how rearranging the electrons can lead to formation of the polymer.
(b) Use the bond dissociation energies in Table 7.1 to calculate $\Delta H$ per $\mathrm{CH}_{2}=\mathrm{CHCN}$ unit for the conversion of acrylonitrile to polyacrylonitrile. Is the reaction endothermic or exothermic?
21.109 Zinc selenide ( ZnSe ) doped with Ga has some Ga atoms in place of Zn atoms and is an $n$-type semiconductor. Draw an MO energy-level diagram for doped ZnSe , show the population of the bands, and explain why Ga substitution gives an $n$-type semiconductor.
21.110 Consider a hypothetical material consisting of an infinite one-dimensional array of hydride ions $\left(\mathrm{H}^{-}\right)$.
(a) Show how a band of MOs could be formed from individual atomic orbitals, and explain why this material should be an electrical insulator.
(b) If some of the hydride ions in the above material were replaced with neutral hydrogen atoms, the resulting "doped" material should be a better electrical conductor. Draw an MO energy-level diagram for the doped material, show the population of the band, and explain why the doped material can conduct electricity.
(c) Would you describe the doped material as $n$-type or $p$-type? Explain.
21.111 The small size of cellular telephones results from the use of sophisticated gallium arsenide (GaAs) semiconductors instead of ordinary silicon-based semiconductors.
(a) Draw an MO energy-level diagram for GaAs, and show the population of the bands.
(b) Explain why the conductivity of GaAs increases as the temperature increases.
(c) Should the conductivity of GaAs increase or decrease when pure GaAs is doped with (i) Zn or (ii) S? Explain.

## Multi-Concept Problems

21.112 The mineral wustite is a nonstoichiometric iron oxide with the empirical formula $\mathrm{Fe}_{x} \mathrm{O}$, where $x$ is a number slightly less than 1 . Wustite can be regarded as an FeO in which some of the Fe sites are vacant. It has a density of $5.75 \mathrm{~g} / \mathrm{cm}^{3}$, a cubic unit cell with an edge length of 431 pm , and a face-centered cubic arrangement of oxygen atoms.
(a) What is the value of $x$ in the formula $\mathrm{Fe}_{x} \mathrm{O}$ ?
(b) Based on the formula in part (a), what is the average oxidation state of Fe ?
(c) Each Fe atom in wustite is in either the +2 or the +3 oxidation state. What percent of the Fe atoms are in the +3 oxidation state?
(d) Using $X$ rays with a wavelength of 70.93 pm , at what angle would third-order diffraction be observed from the planes of atoms that coincide with the faces of the unit cells? Third-order diffraction means that the value of $n$ in the Bragg equation is equal to 3 .
(e) Wustite is a semiconducting iron(II) oxide in which some of the $\mathrm{Fe}^{2+}$ has been replaced by $\mathrm{Fe}^{3+}$. Should it be described as an $n$-type or a $p$-type semiconductor? Explain.
21.113 At high temperatures, coke reduces silica impurities in iron ore to elemental silicon:

$$
\mathrm{SiO}_{2}(s)+2 \mathrm{C}(s) \longrightarrow \mathrm{Si}(s)+2 \mathrm{CO}(g)
$$

(a) Use the data in Appendix B to calculate the values of $\Delta H^{\circ}, \Delta S^{\circ}$, and $\Delta G^{\circ}$ for this reaction at $25^{\circ} \mathrm{C}$.
(b) Is the reaction endothermic or exothermic?
(c) Account for the sign of the entropy change.
(d) Is the reaction spontaneous at $25^{\circ} \mathrm{C}$ and 1 atm pressure of CO ?
(e) Assuming that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ do not depend on temperature, estimate the temperature at which the reaction becomes spontaneous at 1 atm pressure of CO.
21.114 The Mond process for purifying nickel involves the reaction of impure nickel with carbon monoxide at about $150^{\circ} \mathrm{C}$ to give nickel tetracarbonyl. The nickel tetracarbonyl then decomposes to pure nickel at about $230^{\circ} \mathrm{C}$ :

$$
\begin{aligned}
& \mathrm{Ni}(s)+4 \mathrm{CO}(g) \rightleftharpoons \\
& \mathrm{Ni}(\mathrm{CO})_{4}(g) \\
& \Delta H^{\circ}=-160.8 \mathrm{~kJ} ; \Delta S^{\circ}=-410 \mathrm{~J} / \mathrm{K}
\end{aligned}
$$

The values of $\Delta H^{\circ}$ and $\Delta S^{\circ}$ apply at $25^{\circ} \mathrm{C}$, but they are relatively independent of temperature and can be used at $150^{\circ} \mathrm{C}$ and $230^{\circ} \mathrm{C}$.
(a) Calculate $\Delta G^{\circ}$ and the equilibrium constant $K_{\mathrm{p}}$ at $150^{\circ} \mathrm{C}$.
(b) Calculate $\Delta G^{\circ}$ and the equilibrium constant $K_{\mathrm{p}}$ at $230^{\circ} \mathrm{C}$.
(c) Why does the reaction have a large negative value for $\Delta S^{\circ}$ ? Show that the change in $\Delta G^{\circ}$ with increasing temperature is consistent with a negative value of $\Delta S^{\circ}$.
(d) Show that the change in $K_{\mathrm{p}}$ with increasing temperature is consistent with a negative value of $\Delta H^{\circ}$.
21.115 Figure 21.5 indicates that carbon reacts with carbon dioxide to form carbon monoxide at high temperatures:

$$
\mathrm{C}(s)+\mathrm{CO}_{2}(g) \longrightarrow 2 \mathrm{CO}(g)
$$

(a) Use the thermodynamic data in Appendix B to calculate the total pressure and the molar concentrations of CO and $\mathrm{CO}_{2}$ at $500^{\circ} \mathrm{C}$ in a 50.00 L vessel that initially contains 100.0 g of $\mathrm{CO}_{2}$ and an excess of solid carbon. Assume that the reaction mixture has reached equilibrium and that $\Delta H^{\circ}$ and $\Delta S^{\circ}$ are independent of temperature.
(b) Calculate the total pressure and the equilibrium concentrations at $1000^{\circ} \mathrm{C}$.
(c) Use $\Delta H^{\circ}$ and $\Delta S^{\circ}$ to explain why the concentrations increase or decrease on raising the temperature.
21.116 Zinc chromite $\left(\mathrm{ZnCr}_{2} \mathrm{O}_{4}\right)$, which is used to make magnetic tape for cassette recorders, can be prepared by the thermal decomposition of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{Zn}\left(\mathrm{CrO}_{4}\right)_{2}$. The other reaction products are $\mathrm{N}_{2}$ and water vapor.
(a) Write a balanced equation for the reaction.
(b) How many grams of $\mathrm{ZnCr}_{2} \mathrm{O}_{4}$ can be prepared from 10.36 g of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{Zn}\left(\mathrm{CrO}_{4}\right)_{2}$ ?
(c) How many liters of gaseous by-products are obtained at $292^{\circ} \mathrm{C}$ and 745 mm pressure?
(d) $\mathrm{ZnCr}_{2} \mathrm{O}_{4}$ has the cubic spinel structure consisting of a cubic closest-packed (face-centered cubic) array of $\mathrm{O}^{2-}$ ions with $\mathrm{Zn}^{2+}$ ions in the tetrahedral holes and $\mathrm{Cr}^{3+}$ ions in the octahedral holes. The tetrahedral and octahedral holes are like those in $\mathrm{K}_{3} \mathrm{C}_{60}$ (see Figure 21.16). What fraction of each of the two types of holes is occupied?
(e) Draw a crystal field $d$-orbital energy-level diagram for the $\mathrm{Cr}^{3+}$ ion in $\mathrm{ZnCr}_{2} \mathrm{O}_{4}$. Would you expect this compound to be colored? Explain. Does the $\mathrm{Zn}^{2+}$ ion contribute to the color? Explain.
21.117 The alkali metal fulleride superconductors $\mathrm{M}_{3} \mathrm{C}_{60}$ have a cubic closest-packed (face-centered cubic) arrangement of nearly spherical $\mathrm{C}_{60}{ }^{3-}$ anions with $\mathrm{M}^{+}$cations in the holes between the larger $\mathrm{C}_{60}{ }^{3-}$ ions. The holes are of two types: octahedral holes, which are surrounded octahedrally by six $\mathrm{C}_{60}{ }^{3-}$ ions, and tetrahedral holes, which are surrounded tetrahedrally by four $\mathrm{C}_{60}{ }^{3-}$ ions.
(a) Sketch the three-dimensional structure of one unit cell.
(b) How many $\mathrm{C}_{60}{ }^{3-}$ ions, octahedral holes, and tetrahedral holes are present per unit cell?
(c) Specify fractional coordinates for all the octahedral and tetrahedral holes. (Fractional coordinates are fractions of the unit cell edge lengths. For example, a hole at the center of the cell has fractional coordinates $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$.)
(d) The radius of a $\mathrm{C}_{60}{ }^{3-}$ ion is about 500 pm . Assuming that the $\mathrm{C}_{60}{ }^{3-}$ ions are in contact along the face diagonals of the unit cell, calculate the radii of the octahedral and tetrahedral holes.
(e) The ionic radii of $\mathrm{Na}^{+}, \mathrm{K}^{+}$, and $\mathrm{Rb}^{+}$are 97,133 , and 147 pm , respectively. Which of these ions will fit into the octahedral and tetrahedral holes? Which ions will fit only if the framework of $\mathrm{C}_{60}{ }^{3-}$ ions expands?
21.118 A single-walled carbon nanotube can be regarded as a single sheet of graphite rolled into a cylinder (Figure 10.27 b ). Calculate the number of $C$ atoms in a singlewalled nanotube having length of 1.0 mm and a diameter of 1.08 nm . The $\mathrm{C}-\mathrm{C}$ bond length in graphite is 141.5 pm .

## eMedia Problems

21.119 Using the Common Metal Ores activity in eChapter 21.1, choose a metal from each category and write the formula of its common ore. List the ores in order of increasing covalent character from the most ionic to the most covalent.
21.120 Write the equation for the reaction between iron(III) oxide and aluminum metal shown in the Thermite movie (eChapter 21.3). What is the purpose of adding potassium chlorate, sugar, and concentrated sulfuric acid?
21.121 Use the Metallic Bonding activity (eChapter 21.4) to determine the melting points of the transition elements in row 4,5 , or 6 of the periodic table.
(a) What is the relationship between the melting point of a transition metal and the relative numbers of electrons in bonding and antibonding molecular orbitals?
(b) Explain why the electron-sea model of bonding in metals does not accurately predict the trends in transition metal melting points.
21.122 Examine the four types of materials in the Conductivity Band Structure activity (eChapter 21.5). Describe the differences among the band structures in each type and explain how these account for the conductive nature of each.
21.123 The 1-2-3 Superconductor $\mathbf{Y B a}_{2} \mathbf{C u}_{3} \mathbf{O}_{\mathbf{7}}$ (eChapter 21.6) has one of the highest known $T_{c}$ values, 90 K . By rotating the structure, identify the $\mathrm{CuO}_{5}$ group and the $\mathrm{CuO}_{4}$ group. What are the geometries of these groups? What properties of this and other high temperature superconductors keep them from being widely used?
21.124 What advantages do ceramics such as Silicon Carbide (eChapter 21.7) have relative to metals? What are the disadvantages of ceramics? Rotate the 3D model, and see if you can find a special orientation where planes of atoms are separated by largely empty space, devoid of bonds. What does the result of this investigation say about the physical properties of ceramics?

## Chapter

## Nuclear Chemistry

## When methane $\left(\mathrm{CH}_{4}\right)$ burns in oxygen, the $\mathrm{C}, \mathrm{H}$, and O atoms recombine to yield $\mathrm{CO}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$, but they still remain $\mathrm{C}, \mathrm{H}$, and O . When aqueous

 NaCl reacts with aqueous $\mathrm{AgNO}_{3}$, solid AgCl precipitates from solution, but the $\mathrm{Ag}^{+}$and $\mathrm{Cl}^{-}$ions themselves remain the same. In fact, in all the reactions we've discussed up to this point, only the bonds between atoms have changed; the chemical identities of the atoms themselves have remained unchanged. But anyone who reads the paper or watches

## CONTENTS

More than 250 ships on the world's oceans are powered by nuclear reactors, including this Russian icebreaker.
22.1 Nuclear Reactions and Their Characteristics
22.2 Nuclear Reactions and Radioactivity
22.3 Radioactive Decay Rates
22.4 Nuclear Stability
22.5 Energy Changes During Nuclear Reactions
22.6 Nuclear Fission and Fusion
22.7 Nuclear Transmutation
22.8 Detecting and Measuring Radioactivity
22.9 Biological Effects of Radiation
22.10 Applications of Nuclear Chemistry

- Interlude—The Origin of Chemical Elements

Carbon Isotopes activity

Enrique A. Hughes and Anita Zalts, "Radioactivity in the Classroom," J. Chem. Educ., Vol. 77, 2000, 613-614.

$\square$
"Nuclear Chemistry: State of the Art for Teachers," a series of articles in the October 1994 issue of the Journal of Chemical Education.
D. S. Hutchinson and F. I. Hutchinson, "Radioactivity: in Everyday Life," J. Chem. Educ., Vol. 74, 1997, 501-505.

Dr Charles H. Atwood, "Teaching Aids for Nuclear Chemistry," J. Chem. Educ., Vol. 71, 1994, 845-847.

[^24]television knows that atoms can change, often resulting in the conversion of one element into another. Atomic weapons, nuclear energy, and radioactive radon gas in our homes are all topics of societal importance, and all involve nuclear chemistrythe study of the properties and reactions of atomic nuclei.

### 22.1 Nuclear Reactions and Their Characteristics

Recall from Section 2.5 that an atom is characterized by its atomic number, $Z$, and its mass number, $A$. The atomic number, written as a subscript to the left of the element symbol, gives the number of protons in the nucleus. The mass number, written as a superscript to the left of the element symbol, gives the total number of nucleons, a general term for both protons ( p ) and neutrons ( n ). The most common isotope of carbon, for example, has 12 nucleons: 6 protons and 6 neutrons.


Atoms with identical atomic numbers but different mass numbers are called isotopes, and the nucleus of a specific isotope is called a nuclide. There are 13 known isotopes of carbon, two of which occur commonly ( ${ }^{12} \mathrm{C}$ and ${ }^{13} \mathrm{C}$ ) and one of which $\left({ }^{14} \mathrm{C}\right)$ is produced in small amounts in the upper atmosphere by the action of neutrons from cosmic rays on ${ }^{14} \mathrm{~N}$. The remaining 10 carbon isotopes have been produced artificially. Only the two commonly occurring ones are indefinitely stable; the other 11 undergo spontaneous nuclear reactions, which change their nuclei. Carbon-14, for example, slowly decomposes to give nitrogen-14 plus an electron, a process we can write as

$$
{ }_{6}^{14} \mathrm{C} \longrightarrow{ }_{7}^{14} \mathrm{~N}+{ }_{-1}^{0} \mathrm{e}
$$

The electron is often written as ${ }_{-1}^{0} \mathrm{e}$, where the superscript 0 indicates that the mass of an electron is essentially zero when compared to that of a proton or neutron, and the subscript -1 indicates that the charge is -1 . (The subscript in this instance is not a true atomic number.)

Nuclear reactions, such as the spontaneous decay of ${ }^{14} \mathrm{C}$, are distinguished from chemical reactions in several ways:

- A nuclear reaction involves a change in an atom's nucleus, usually producing a different element. A chemical reaction, by contrast, involves only a change in distribution of the outer-shell electrons around the atom and never changes the nucleus itself or produces a different element.
- Different isotopes of an element have essentially the same behavior in chemical reactions but often have completely different behavior in nuclear reactions.
- The rate of a nuclear reaction is unaffected by a change in temperature or pressure or by the addition of a catalyst.
- The nuclear reaction of an atom is essentially the same, regardless of whether the atom is in a chemical compound or in uncombined elemental form.
- The energy change accompanying a nuclear reaction is far greater than that accompanying a chemical reaction. The nuclear transformation of 1.0 g of uranium- 235 releases $8.2 \times 10^{7} \mathrm{~kJ}$, for example, whereas the chemical combustion of 1.0 g of methane releases only 56 kJ .


## 22.2 | Nuclear Reactions and Radioactivity

Scientists have known since 1896 that many nuclides are radioactive-that is, they spontaneously emit radiation. Early studies of radioactive nuclei, or radionuclides, by the New Zealand physicist Ernest Rutherford in 1897 showed that there are three common types of radiation with markedly different properties: alpha $(\alpha)$, beta ( $\beta$ ), and $\operatorname{gamma}(\gamma)$ radiation, named after the first three letters of the Greek alphabet.

## Alpha ( $\alpha$ ) Radiation

Using the simple experiment shown in Figure 22.1, Rutherford found that $\boldsymbol{\alpha}$ radiation consists of a stream of particles that are repelled by a positively charged electrode, are attracted by a negatively charged electrode, and have a mass-tocharge ratio identifying them as helium nuclei, ${ }_{2}^{4} \mathrm{He}^{2+}$. Alpha particles thus consist of two protons and two neutrons.


Because the emission of an $\alpha$ particle from a nucleus results in a loss of two protons and two neutrons, it reduces the mass number of the nucleus by 4 and reduces the atomic number by 2 . Alpha emission is particularly common for heavy radioactive isotopes, or radioisotopes: Uranium-238, for example, spontaneously emits an $\alpha$ particle and forms thorium- 234 .


Note how the nuclear equation for the radioactive decay of uranium-238 is written. The equation is not balanced in the usual chemical sense because the kinds of nuclei are not the same on both sides of the arrow. Instead, a nuclear equation is balanced when the sums of the nucleons are the same on both sides of the equation and when the sums of the charges on the nuclei and any elementary particles (protons, neutrons, and electrons) are the same on both sides. In the decay of ${ }_{92}^{238} \mathrm{U}$ to give ${ }_{2}^{4} \mathrm{He}$ and ${ }_{90}^{234} \mathrm{Th}$, for example, there are 238 nucleons and 92 nuclear charges on both sides of the nuclear equation.

Note also that we are concerned only with charges on elementary particles and on nuclei when we write nuclear equations, not with ionic charges on atoms. The $\alpha$ particle is thus written as ${ }_{2}^{4} \mathrm{He}$ rather than as ${ }_{2}^{4} \mathrm{He}^{2+}$, and the thorium resulting from radioactive decay of ${ }_{92}^{238} \mathrm{U}$ is written as ${ }_{90}^{234} \mathrm{Th}$ rather than as ${ }_{90}^{234} \mathrm{Th}^{2-}$. We ignore the ionic charges both because they are irrelevant to nuclear disintegration and because they soon disappear. The ${ }_{2}^{4} \mathrm{He}^{2+}$ ion immediately picks up two electrons from whatever it strikes, yielding a neutral helium atom, and the ${ }_{90}^{234} \mathrm{Th}^{2-}$ ion immediately gives two electrons to whatever it is in electrical contact with, yielding a neutral thorium atom.
C. Ronneau, "Radioactivity: A Natural Phenomenon," J. Chem. Educ., Vol. 67, 1990, 736-737.


Separation of Alpha, Beta, and Gamma
Rays movie

## -

4 FIGURE 22.1 The effect of an electric field on $\alpha, \beta$, and $\gamma$ radiation. The radioactive source in the shielded box emits radiation, which passes between two electrodes. Alpha radiation is deflected toward the negative electrode, $\beta$ radiation is strongly deflected toward the positive electrode, and $\gamma$ radiation is undeflected.

$\square$
An alpha ( $\alpha$ ) particle $\left({ }_{2}^{4} \mathrm{He}^{2+}\right)$ is a helium nucleus, but the +2 charge is not used in writing nuclear equations.

$\square$For a nuclear equation to be balanced: sum of atomic numbers of reactants (subscripts) $=$ sum of atomic numbers of products, and sum of nucleons of reactants $($ superscripts $)=$ sum of nucleons of products. Ionic charges are ignored.

Robert Suder, "Beta Decay Diagram," J. Chem. Educ., Vol. 66, 1989, 231.

$\square$For the purpose of balancing nuclear equations, the mass of the electron is taken to be 0 and its "nuclear charge," is taken to be -1 .

## Beta ( $\beta$ ) Radiation

Further work by Rutherford in the late 1800s showed that $\boldsymbol{\beta}$ radiation consists of a stream of particles that are attracted to a positive electrode (Figure 22.1), are repelled by a negative electrode, and have a mass-to-charge ratio identifying them as electrons, ${ }_{-1}^{0} \mathrm{e}$ or $\beta^{-}$. Beta emission occurs when a neutron in the nucleus spontaneously decays into a proton plus an electron, which is then ejected. The product nucleus has the same mass number as the starting nucleus because a neutron has turned into a proton, but it has a higher atomic number because of the newly created proton. The reaction of ${ }^{131}$ I to give ${ }^{131} \mathrm{Xe}$ is an example:


Writing the emitted $\beta$ particle as ${ }_{-1}^{0} \mathrm{e}$ in the nuclear equation makes clear the charge balance of the nuclear reaction: The subscript in the ${ }_{53}^{131}$ I nucleus on the left (53) is balanced by the sum of the two subscripts on the right ( $54-1=53$ ).

## Gamma ( $\gamma$ ) Radiation

Gamma radiation is unaffected by electric fields (Figure 22.1), has no mass, and is simply electromagnetic radiation of very high energy and thus of very short wavelength $\left(\lambda=10^{-11}-10^{-14} \mathrm{~m}\right)$. In modern terms, we would say that $\gamma$ radiation consists of a stream of high-energy photons. Gamma radiation almost always accompanies $\alpha$ and $\beta$ emission as a mechanism for the release of energy, but it is often not shown when writing nuclear equations because it changes neither the mass number nor the atomic number of the product nucleus.

## Positron Emission and Electron Capture

In addition to $\alpha, \beta$, and $\gamma$ radiation, two other common types of radioactive decay processes also occur: positron emission and electron capture. Positron emission occurs with conversion of a proton in the nucleus into a neutron plus an ejected positron, ${ }_{1}^{0}$ e or $\beta^{+}$, a particle that can be thought of as a "positive electron." A positron has the same mass as an electron but an opposite charge. The result of positron emission is a decrease in the atomic number of the product nucleus but no change in the mass number. Potassium-40, for example, undergoes positron emission to yield argon-40, a nuclear reaction important in geology for dating rocks. Note once again that the sum of the two subscripts on the right of the nuclear equation $(18+1=19)$ is equal to the subscript in the ${ }_{19}^{40} \mathrm{~K}$ nucleus on the left.


Electron capture is a process in which the nucleus captures an inner-shell electron, thereby converting a proton into a neutron. The mass number of the product
nucleus is unchanged, but the atomic number decreases by 1 , just as in positron emission. The conversion of mercury-197 into gold-197 is an example:

|  | Inner-shell | 79 protons |
| :---: | :---: | :---: |
| 80 protons | electron | 118 neutrons |
| 117 neutrons |  | 197 nucleons |
| 197 nucleons |  |  |

Characteristics of the different kinds of radioactive decay processes are summarized in Table 22.1.

TABLE 22.1 A Summary of Radioactive Decay Processes

|  |  | Change in <br> Atomic <br> Number | Change in <br> Mass <br> Number | Change in <br> Neutron <br> Number |
| :--- | :--- | :--- | :--- | :--- |
| Process | Symbol | -2 | -4 | -2 |
| Alpha emission | ${ }_{2}^{4} \mathrm{He}$ or $\alpha$ | 0 | -1 |  |
| Beta emission | -1 e or $\beta^{-}$ | +1 | 0 | 0 |
| Gamma emission | ${ }_{0}^{0} \gamma$ or $\gamma$ | 0 | 0 | +1 |
| Positron emission | ${ }_{1} \mathrm{e}$ or $\beta^{+}$ | -1 | 0 | +1 |
| Electron capture | E. C. | -1 | 0 |  |

## Worked Example 22.1

Write balanced nuclear equations for each of the following processes:
(a) Alpha emission from curium-242: ${ }_{96}^{242} \mathrm{Cm} \rightarrow{ }_{2}^{4} \mathrm{He}+$ ?
(b) Beta emission from magnesium-28: ${ }_{12}^{28} \mathrm{Mg} \rightarrow{ }_{-1}^{0} \mathrm{e}+$ ?
(c) Positron emission from xenon-118: ${ }_{54}^{118} \mathrm{Xe} \rightarrow{ }_{1}^{0} \mathrm{e}+$ ?

## Strategy

The key to writing nuclear equations is to make sure that the number of nucleons is the same on both sides of the equation and that the number of elementary and nuclear charges is the same.

## Solution

(a) In $\alpha$ emission, the mass number decreases by 4 , and the atomic number decrease by 2, giving plutonium- $238:{ }_{96}^{242} \mathrm{Cm} \rightarrow{ }_{2}^{4} \mathrm{He}+{ }_{94}^{238} \mathrm{Pu}$
(b) In $\beta$ emission, the mass number is unchanged, and the atomic number increases by 1 , giving aluminum $-28:{ }_{12}^{28} \mathrm{Mg} \rightarrow{ }_{-1}^{0} \mathrm{e}+{ }_{13}^{28} \mathrm{Al}$
(c) In positron emission, the mass number is unchanged, and the atomic number decreases by 1 , giving iodine-118: ${ }_{54}^{118} \mathrm{Xe} \rightarrow{ }_{1}^{0} \mathrm{e}+{ }_{53}^{118} \mathrm{I}$

- PROBLEM 22.1 Write balanced nuclear equations for each of the following processes:
(a) Beta emission from ruthenium-106: ${ }_{44}^{106} \mathrm{Ru} \rightarrow{ }_{-1}^{0} \mathrm{e}+$ ?
(b) Alpha emission from bismuth-189: ${ }_{83}^{189} \mathrm{Bi} \rightarrow{ }_{2}^{4} \mathrm{He}+$ ?
(c) Electron capture by polonium-204: ${ }_{84}^{204} \mathrm{Po}+{ }_{-1}^{0} \mathrm{e} \rightarrow$ ?
- PROBLEM 22.2 What particle is produced by decay of thorium-214 to radium-210?

$$
{ }_{90}^{214} \mathrm{Th} \longrightarrow{ }_{88}^{210} \mathrm{Ra}+?
$$

Donald J. Olbris and Judith
Herzfeld, "Nucleogenesis! A Game with Natural Rules for Teaching Nuclear Synthesis and Decay," J. Chem. Educ., Vol. 76, 1999, 349-352.

First-Order Process movie

Cosmers
The use of the integrated first-order rate law for nuclear decay is identical with its use for chemical reactions, except that numbers of nuclei ( $N$ and $N_{0}$ ) replace molar concentrations of chemical species.


FIGURE 22.2 The decay of a radionuclide over time. No matter what the value of the half-life, $50 \%$ of the sample remains after one half-life, 25\% remains after two half-lives, $12.5 \%$ remains after three halflives, and so on.

## 22.3 | Radioactive Decay Rates

The rates of different radioactive decay processes vary enormously. Some radionuclides, such as uranium-238, decay at a barely perceptible rate over billions of years; others, such as carbon-17, decay within milliseconds.

Radioactive decay is kinetically a first-order process (Section 12.4), whose rate is proportional to the number of radioactive nuclei $N$ in a sample times the firstorder rate constant $k$, called the decay constant:

$$
\text { Decay rate }=k \times N
$$

As we saw in Section 12.4, a first-order rate law can be converted into an integrated rate law of the form

$$
\ln \left(\frac{N}{N_{0}}\right)=-k t
$$

where $N_{0}$ is the number of radioactive nuclei originally present in a sample and $N$ is the number remaining at time $t$. The decay constant $k$ has units of time ${ }^{-1}$ so that the quantity $k t$ is unitless.

Like all first-order processes, radioactive decay is characterized by a half-life, $t_{1 / 2}$, the time required for the number of radioactive nuclei in a sample to drop to half its initial value (Section 12.5). For example, the half-life of iodine-131, a radioisotope used in thyroid testing, is 8.02 days. If today you have 1.000 g of ${ }_{53}^{131} \mathrm{I}$, then 8.02 days from now you will have only 0.500 g of ${ }_{53}^{131}$ I remaining because onehalf of the sample will have decayed (by beta emission), yielding 0.500 g of ${ }_{54}^{131} \mathrm{Xe}$. After 8.02 more days ( 16.04 total), only 0.250 g of ${ }_{53}^{131} \mathrm{I}$ will remain; after a further 8.02 days ( 24.06 total), only 0.125 g will remain; and so on. Each passage of a halflife causes the decay of one-half of whatever sample remains, as shown graphically by the curve in Figure 22.2. The half-life is the same no matter what the size of the sample, the temperature, or any other external condition.

$$
{ }_{53}^{131} \mathrm{I} \longrightarrow{ }_{54}^{131} \mathrm{Xe}+{ }_{-1}^{0} \mathrm{e} \quad t_{1 / 2}=8.02 \text { days }
$$



Mathematically, the value of $t_{1 / 2}$ can be calculated from the integrated rate law by setting $N=1 / 2 N_{0}$ at time $t_{1 / 2}$ :

$$
\begin{aligned}
& \ln \left(\frac{\frac{1}{2} N_{0}}{N_{0}}\right)=-k t_{1 / 2} \text { and } \ln \frac{1}{2}=-\ln 2=-k t_{1 / 2} \\
& \text { so } \quad t_{1 / 2}=\frac{\ln 2}{k} \text { and } k=\frac{\ln 2}{t_{1 / 2}}
\end{aligned}
$$

These equations say that if we know the value of either the decay constant $k$ or the half-life $t_{1 / 2}$, we can calculate the value of the other. Furthermore, if we know the value of $t_{1 / 2}$, we can calculate the ratio of remaining and initial amounts of radioactive sample $N / N_{0}$ at any time $t$ by substituting the expression for $k$ into the integrated rate law:

Since

$$
\ln \left(\frac{N}{N_{0}}\right)=-k t \quad \text { and } \quad k=\frac{\ln 2}{t_{1 / 2}}
$$

then $\quad \ln \left(\frac{N}{N_{0}}\right)=(-\ln 2)\left(\frac{t}{t_{1 / 2}}\right)$
Worked Example 22.2 shows how to calculate a half-life from a decay constant, and Worked Example 22.4 shows how to determine the percentage of radioactive sample remaining at time $t$.

The half-lives of some useful radioisotopes are listed in Table 22.2. As you might expect, radioisotopes used internally in medical applications have fairly short half-lives so that they decay rapidly and don't cause long-term health hazards.

© Technetium-99m, a short-lived radioisotope used for brain scans, is obtained by neutron bombardment of molybdenum-99 and then stored in a "molybdenum cow" in the form of $\mathrm{MoO}_{4}{ }^{2-}$. Small amounts are removed by passing a saline solution through the cylinder.

TABLE 22.2 Half-Lives of Some Useful Radioisotopes

| Radioisotope | Symbol | Radiation | Half-Life | Use |
| :---: | :---: | :---: | :---: | :---: |
| Tritium | ${ }_{1}^{3} \mathrm{H}$ | $\beta^{-}$ | 12.33 years | Biochemical tracer |
| Carbon-14 | ${ }_{6}^{14} \mathrm{C}$ | $\beta^{-}$ | 5730 years | Archaeological dating |
| Phosphorus-32 | ${ }_{15}^{32} \mathrm{P}$ | $\beta^{-}$ | 14.26 days | Leukemia therapy |
| Potassium-40 | ${ }_{19}^{40} \mathrm{~K}$ | $\beta^{-}$ | $1.28 \times 10^{9}$ years | Geological dating |
| Cobalt-60 | ${ }_{27}^{60} \mathrm{Co}$ | $\beta^{-}, \gamma$ | 5.27 years | Cancer therapy |
| Technetium-99m* | ${ }_{43}^{99} \mathrm{~T}$ T | $\gamma$ | 6.01 hours | Brain scans |
| Iodine-123 | ${ }_{53}^{123}$ | $\gamma$ | 13.27 hours | Thyroid therapy |
| Uranium-235 | ${ }_{92}^{235} \mathrm{U}$ | $\alpha, \gamma$ | $7.04 \times 10^{8}$ years | Nuclear reactors |

*The $m$ in technetium- $99 m$ stands for metastable, meaning that it undergoes $\gamma$ emission but does not change its mass number or atomic number.

## Worked Example 22.2

The decay constant for sodium-24, a radioisotope used medically in blood studies, is $4.63 \times 10^{-2} \mathrm{~h}^{-1}$. What is the half-life of ${ }^{24} \mathrm{Na}$ ?


## Strategy

Half-life can be calculated from the decay constant by using the equation

$$
t_{1 / 2}=\frac{\ln 2}{k}
$$

## Solution

Substituting the values $k=4.63 \times 10^{-2} \mathrm{~h}^{-1}$ and $\ln 2=0.693$ into the equation gives

$$
t_{1 / 2}=\frac{0.693}{4.63 \times 10^{-2} \mathrm{~h}^{-1}}=15.0 \mathrm{~h}
$$

The half-life of sodium- 24 is 15.0 h .

## Worked Example 22.3

The half-life of radon-222, a radioactive gas of concern as a health hazard in some homes, is 3.823 days. What is the decay constant of ${ }^{222} \mathrm{Rn}$ ?

## Strategy

A decay constant can be calculated from the half-life by using the equation

$$
k=\frac{\ln 2}{t_{1 / 2}}
$$

## Solution

Substituting the values $t_{1 / 2}=3.823$ days and $\ln 2=0.693$ into the equation gives

$$
k=\frac{0.693}{3.823 \text { days }}=0.181 \mathrm{day}^{-1}
$$

## Worked Example 22.4

Phosphorus-32, a radioisotope used in leukemia therapy, has a half-life of 14.26 days. What percent of a sample remains after 35.0 days?

## Strategy

The ratio of remaining $(N)$ and initial $\left(N_{0}\right)$ amounts of a radioactive sample at time $t$ is given by the equations

$$
\ln \left(\frac{N}{N_{0}}\right)=(-\ln 2)\left(\frac{t}{t_{1 / 2}}\right) \quad \text { and } \quad \frac{N}{N_{0}}=\operatorname{antiln}\left[\ln \left(\frac{N}{N_{0}}\right)\right]
$$

Taking $N_{0}$ as $100 \%, N$ can then be obtained.

## Solution

Substituting values for $t$ and for $t_{1 / 2}$ into the equation gives

$$
\ln \left(\frac{N}{N_{0}}\right)=-0.693\left(\frac{35.0 \text { days }}{14.26 \text { days }}\right)=-1.70
$$

Taking the natural antilog of -1.70 then gives the ratio $N / N_{0}$ :

$$
\frac{N}{N_{0}}=\operatorname{antiln}(-1.70)=0.183
$$

Since the initial amount of ${ }^{32} \mathrm{P}$ was $100 \%$, we can set $N_{0}=100 \%$ and solve for $N$ :

$$
\frac{N}{100 \%}=0.183 \quad \text { so } \quad N=0.183 \times 100 \%=18.3 \%
$$

After 35.0 days, $18.3 \%$ of a ${ }^{32} \mathrm{P}$ sample remains, and $100 \%-18.3 \%=81.7 \%$ has decayed.

## Worked Example 22.5

A sample of ${ }^{41} \mathrm{Ar}$, a radioisotope used to measure the flow of gases from smokestacks, decays initially at a rate of 34,500 disintegrations $/ \mathrm{min}$, but the decay rate falls to 21,500 disintegrations $/ \mathrm{min}$ after 75.0 min . What is the half-life of ${ }^{41} \mathrm{Ar}$ ?

## Strategy

The half-life of a radioactive decay process is given by finding $t_{1 / 2}$ in the equation

$$
\ln \left(\frac{N}{N_{0}}\right)=(-\ln 2)\left(\frac{t}{t_{1 / 2}}\right)
$$

In the present instance, though, we are given decay rates at two different times rather than values of $N$ and $N_{0}$. Nevertheless, for a first-order process like radioactive decay, in which rate $=k N$, the ratio of the decay rate at any time $t$ to the decay rate at time $t=0$ is the same as the ratio of $N$ to $N_{0}$ :

$$
\frac{\text { Decay rate at time } t}{\text { Decay rate at time } t=0}=\frac{k N}{k N_{0}}=\frac{N}{N_{0}}
$$

## Solution

Substituting the proper values into the equation gives

$$
\begin{aligned}
& \ln \left(\frac{21,500}{34,500}\right)=-0.693\left(\frac{75.0 \mathrm{~min}}{t_{1 / 2}}\right) \quad \text { or } \quad-0.473=\frac{-52.0 \mathrm{~min}}{t_{1 / 2}} \\
& \text { so } \quad t_{1 / 2}=\frac{-52.0 \mathrm{~min}}{-0.473}=110 \mathrm{~min}
\end{aligned}
$$

The half-life of ${ }^{41} \mathrm{Ar}$ is 110 min .

PROBLEM 22.3 The decay constant for mercury-197, a radioisotope used medically in kidney scans, is $1.08 \times 10^{-2} \mathrm{~h}^{-1}$. What is the half-life of mercury-197?

- PROBLEM 22.4 The half-life of carbon-14 is 5730 years. What is its decay constant?
- PROBLEM 22.5 What percentage of ${ }_{6}^{14} \mathrm{C}\left(t_{1 / 2}=5730\right.$ years $)$ remains in a sample estimated to be 16,230 years old?
- PROBLEM 22.6 What is the half-life of iron-59, a radioisotope used medically in the diagnosis of anemia, if a sample with an initial decay rate of 16,800 disintegrations/min decays at a rate of 10,860 disintegrations/min after 28.0 days?

KEY CONCEPT PROBLEM 22.7 What is the half-life of the radionuclide that shows the following decay curve?


Darleane C. Hoffman and Diana M. Lee, "Chemistry of the Heaviest Elements-One Element at a Time," J. Chem. Educ., Vol. 76, 1999, 332-347.

Nuclear Stability activity

$\square$
Transuranium elements, those with atomic numbers higher than uranium, do not occur naturally but are produced by nuclear transmutation reactions, discussed in Section 22.7.

FIGURE 22.3 The band of nuclear stability indicating various neutron/proton combinations that give rise to observable nuclei with measurable half-lives. Combinations outside the band are not stable. The "island of stability" near 114 protons and 184 neutrons corresponds to a group of superheavy nuclei that are predicted to be stable. The first member of this group was reported in 1999.
-KEY CONCEPT PROBLEM 22.8 Copper-59 (red spheres) decays to ${ }^{59} \mathrm{Ni}$ (green spheres) with a half-life of 1.35 min . Write a balanced nuclear equation for the process, and tell how many half-lives have passed in the following sample:


## 22.4 | Nuclear Stability

Why do some nuclei undergo radioactive decay while others do not? Why, for instance, does a carbon-14 nucleus, with six protons and eight neutrons, spontaneously emit a $\beta$ particle, whereas a carbon-13 nucleus, with six protons and seven neutrons, is stable indefinitely? Before answering these questions, it's important to define what we mean by "stable." In the context of nuclear chemistry, we'll use the word stable to refer to isotopes whose half-lives can be measured, even if that half-life is only a fraction of a second. We'll call those isotopes that decay too rapidly for their half-lives to be measured unstable, and those isotopes that do not undergo radioactive decay nonradioactive, or stable indefinitely.

The answer to the question about why some nuclei are radioactive while others are not has to do with the neutron/proton ratio in the nucleus and the forces holding the nucleus together. To see the effect of the neutron/proton ratio on nuclear stability, look at the grid pictured in Figure 22.3. Along the side of the grid are divisions representing the number of neutrons in nuclei, a number arbitrarily cut off at 200 . Along the bottom of the grid are divisions representing the number of protons in nuclei-the first 92 divisions represent the naturally occurring elements, the next 17 represent the artificially produced transuranium elements, and the divisions beyond 109 represent elements about which little or nothing is known. (Actually, only 90 of the first 92 elements occur naturally. Technetium and promethium do not occur naturally because all their isotopes are radioactive and have very short half-lives. Francium and astatine occur on Earth only in very tiny amounts.)


When the more than 3600 known nuclides are plotted on the neutron/proton grid in Figure 22.3, they fall in a curved band sometimes called the "band of nuclear stability." Even within the band, only 264 of the nuclides are stable indefinitely. The remainder decay spontaneously, although their rates of decay vary enormously. On either side of the band is a "sea of instability" representing the large number of unstable neutron/proton combinations that have never been seen. Particularly interesting is the "island of stability" predicted to exist for a few superheavy nuclides near 114 protons and 184 neutrons. The first members of this group- ${ }^{287} 114,{ }^{288} 114,{ }^{289} 114$, and ${ }^{292} 116$-were prepared in 1999 and do indeed seem to be unusually stable. Isotope ${ }^{289} 114$, for example, has a half-life of 30.4 seconds.

Several generalizations can be made about the data in Figure 22.3:

- Every element in the periodic table has at least one radioactive isotope.
- Hydrogen is the only element whose most abundant stable isotope $\left({ }_{1}^{1} \mathrm{H}\right)$ contains more protons (1) than neutrons (0). The most abundant stable isotopes of other elements lighter than calcium $(Z=20)$ usually have either the same number of protons and neutrons $\left({ }_{2}^{4} \mathrm{He},{ }_{6}^{12} \mathrm{C},{ }_{8}^{16} \mathrm{O}\right.$, and ${ }_{14}^{28} \mathrm{Si}$, for example) or have only one more neutron than protons ( ${ }_{5}^{11} \mathrm{~B},{ }_{9}^{19} \mathrm{~F}$, and ${ }_{11}^{23} \mathrm{Na}$, for example).
- The ratio of neutrons to protons gradually increases for elements heavier than calcium, giving a curved appearance to the band of stability. The most abundant stable isotope of bismuth, for example, has 126 neutrons and 83 protons $\left({ }_{83}^{209} \mathrm{Bi}\right)$.
- All isotopes heavier than bismuth-209 are radioactive, even though they may occur naturally.
- Of the 264 nonradioactive isotopes, 207 have an even number of neutrons in their nuclei. Most nonradioactive isotopes (156) have even numbers of both protons and neutrons, 51 have an even number of neutrons but an odd number of protons, and only 4 have an odd number of both protons and neutrons (Figure 22.4).

Observations such as those in Figure 22.3 lead to the suggestion that neutrons function as a kind of nuclear "glue" that holds nuclei together by overcoming proton-proton repulsions. The more protons there are in the nucleus, the more glue is needed. Furthermore, there appear to be certain "magic numbers" of protons or neutrons- $2,8,20,28,50,82,126$-that give rise to particularly stable nuclei. For instance, there are ten naturally occurring isotopes of tin, which has a magic number of protons $(Z=50)$, but there are only two naturally occurring isotopes of its neighbors on either side, indium $(Z=49)$ and antimony $(Z=51)$. Lead-208 is especially stable because it has a double magic number of nucleons: 126 neutrons and 82 protons. We'll see in the next section how the relative stability of different nuclei can be measured quantitatively.

The correlation of nuclear stability with special numbers of nucleons is reminiscent of the correlation of chemical stability with special numbers of electronsthe octet rule discussed in Section 6.12. In fact, a shell model of nuclear structure has been proposed, analogous to the shell model of electronic structure. The magic numbers of nucleons correspond to filled nuclear-shell configurations, although the details are relatively complex.

A close-up look at a segment of the band of nuclear stability reveals some more interesting trends (Figure 22.5). One trend is that elements with an even atomic number have a larger number of nonradioactive isotopes than do elements with an odd atomic number. Tungsten $(Z=74)$ has 5 nonradioactive isotopes and osmium $(Z=76)$ has 7 , for example, while their neighbor rhenium $(Z=75)$ has only 1 .

v
Magic numbers for nuclei are analogous to noble-gas electron configurations for atoms. A nucleus with $2,8,20,28,50,82$, or 126 protons or neutrons is particularly stable, just as an atom having a noble-gas electron configuration with $2,10,18,36,54$, or 86 electrons tends to be stable.


Neutrons

A FIGURE 22.4 Numbers of nonradioactive isotopes with various even/odd combinations of neutrons and protons. The majority of nonradioactive isotopes have both an even number of protons and an even number of neutrons. Only 4 nonradioactive isotopes have both an odd number of protons and an odd number of neutrons.

FIGURE 22.5 A close-up look at the band of nuclear stability in the region from $Z=66$ (dysprosium) through $Z=79$ (gold) shows the types of radioactive processes undergone by various nuclides. Nuclides with lower neutron/proton ratios tend to undergo positron emission, electron capture, or $\alpha$ emission, whereas nuclides with higher neutron/proton ratios tend to undergo $\beta$ emission.


## Decay Series activity



Another trend is that radioactive nuclei with higher neutron/proton ratios (top side of the band) tend to emit $\beta$ particles, while nuclei with lower neutron/ proton ratios (bottom side of the band) tend to undergo nuclear decay by positron emission, electron capture, or $\alpha$ emission. This makes sense if you think about it: The nuclei on the top side of the band are neutron-rich and therefore undergo a process that decreases the neutron/proton ratio. The nuclei on the bottom side of the band, by contrast, are neutron-poor and therefore undergo processes that increase the neutron/proton ratio. (Take a minute to convince yourself that $\alpha$ emission does, in fact, increase the neutron/proton ratio for heavy nuclei in which $\mathrm{n}>\mathrm{p}$.)

| This process decreases the neutron/proton ratio: | $\{$ Beta emission: | Neutron $\longrightarrow$ Proton $+\beta^{-}$ |
| :---: | :---: | :---: |
| These processes increase the neutron/proton ratio: | $\left\{\begin{array}{l}\text { Positron emission: } \\ \text { Electron capture: } \\ \text { Alpha emmision: }\end{array}\right.$ | $\begin{aligned} & \text { Proton } \longrightarrow \text { Neutron }+\beta^{+} \\ & \text {Proton }+ \text { Electron } \longrightarrow \text { Neutron } \\ & { }_{Z}^{A} X \longrightarrow{ }_{Z-2} Y+{ }_{2}^{4} \mathrm{He} \end{aligned}$ |

One further point about nuclear decay is that some nuclides, particularly those of the heavy elements above bismuth, can't reach a nonradioactive decay product by a single emission. The product nucleus resulting from the first decay is itself radioactive and therefore undergoes a further disintegration. In fact, such nuclides must often undergo a whole series of nuclear disintegrations-a decay series-before they ultimately reach a nonradioactive product. Uranium-238, for example, undergoes a series of 14 sequential nuclear reactions, ultimately ending at lead-206 (Figure 22.6).


PROBLEM 22.9 Of the two isotopes ${ }^{173} \mathrm{Au}$ and ${ }^{199} \mathrm{Au}$, one decays by $\beta$ emission and one decays by $\alpha$ emission. Which is which?

KEY CONCEPT PROBLEM 22.10 The following series has two kinds of processes: one represented by the shorter arrows pointing right and the other represented by the longer arrows pointing left. Tell what kind of nuclear decay process each arrow corresponds to, and identify each nuclide A-E in the series:


### 22.5 Energy Changes During Nuclear Reactions

We said in the previous section that neutrons appear to act as a kind of nuclear glue by overcoming the proton-proton repulsions that would otherwise cause the nucleus to fly apart. In principle, it should be possible to measure the strength of the forces holding a nucleus together by measuring the amount of heat released on forming the nucleus from isolated protons and neutrons. For example, the energy change associated with combining two neutrons and two protons to yield a

4 FIGURE 22.6 The decay series from ${ }_{92}^{238} \mathrm{U}$ to ${ }_{82}^{206} \mathrm{~Pb}$. Each nuclide except for the last is radioactive and undergoes nuclear decay. The leftpointing, longer arrows (red) represent $\alpha$ emissions, and the right-pointing, shorter arrows (blue) represent $\beta$ emissions.
-
helium-4 nucleus should be a direct measure of nuclear stability, just as the energy change associated with formation of a chemical bond is a measure of the bond's stability.

$$
2{ }_{1}^{1} \mathrm{H}+2{ }_{0}^{1} \mathrm{n} \longrightarrow{ }_{2}^{4} \mathrm{He} \quad \Delta E=?
$$

Unfortunately, there is a problem with actually carrying out the measurement: Temperatures rivaling those in the interior of the sun $\left(10^{7} \mathrm{~K}\right)$ are necessary for the reaction to occur! That is, the activation energy (Section 12.10) required to force the elementary particles close enough for reaction is extremely high. Nevertheless, the energy change for the process can be calculated by using the Einstein equation $\Delta E=\Delta m c^{2}$, which relates the energy change $(\Delta E)$ of a nuclear process to a corresponding mass change $\Delta m$ (Section 5.5).

Take a helium-4 nucleus, for example. We know from Table 2.1 that the mass of two neutrons and two protons is 4.03188 amu :

$$
\begin{aligned}
& \text { Mass of } 2 \text { neutrons }=(2)(1.00866 \mathrm{amu})=2.01732 \mathrm{amu} \\
& \text { Mass of } 2 \text { protons }=(2)(1.00728 \mathrm{amu})=2.01456 \mathrm{amu} \\
& \hline \text { Total mass of } 2 \mathrm{n}+2 \mathrm{p}
\end{aligned}=4.03188 \mathrm{amu}
$$

Furthermore, we can subtract the mass of two electrons from the experimentally measured mass of a helium- 4 atom to find that the mass of a helium- 4 nucleus is 4.00150 amu :

$$
\begin{array}{llr}
\text { Mass of helium-4 atom } & =4.00260 \mathrm{amu} \\
- \text { Mass of } 2 \text { electrons }=-(2)\left(5.486 \times 10^{-4} \mathrm{amu}\right) & =-0.00110 \mathrm{amu} \\
\hline \text { Mass of helium- } 4 \text { nucleus } & =4.00150 \mathrm{amu}
\end{array}
$$

Subtracting the mass of the helium nucleus from the combined mass of its constituent neutrons and protons shows a difference of 0.03038 amu . That is, 0.03038 amu (or $0.03038 \mathrm{~g} / \mathrm{mol}$ ) is lost when two protons and two neutrons combine to form a helium-4 nucleus:

$$
\begin{array}{rlr}
\text { Mass of } 2 \mathrm{n}+2 \mathrm{p} & =4.03188 \mathrm{amu} \\
- \text { Mass of }{ }^{4} \mathrm{He} \text { nucleus } & =-4.00150 \mathrm{amu} \\
\hline \text { Mass difference } & =0.03038 \mathrm{amu} \quad(\text { or } 0.03038 \mathrm{~g} / \mathrm{mol})
\end{array}
$$

The loss in mass that occurs when protons and neutrons combine to form a nucleus is called the mass defect of the nucleus. This lost mass is converted into energy that is released during the nuclear reaction and is thus a direct measure of the binding energy holding the nucleons together. The larger the binding energy, the more stable the nucleus. Using the Einstein equation, we can calculate this binding energy for a helium-4 nucleus:

$$
\begin{aligned}
\Delta E & =\Delta m c^{2} \quad \text { where } c=3.00 \times 10^{8} \mathrm{~m} / \mathrm{s} \\
& =\left(3.038 \times 10^{-5} \mathrm{~kg} / \mathrm{mol}\right)\left(3.00 \times 10^{8} \mathrm{~m} / \mathrm{s}\right)^{2} \\
& =2.73 \times 10^{12} \mathrm{~kg} \cdot \mathrm{~m}^{2} /\left(\mathrm{mol} \cdot \mathrm{~s}^{2}\right) \\
& =2.73 \times 10^{12} \mathrm{~J} / \mathrm{mol}=2.73 \times 10^{9} \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

The binding energy for helium- 4 nuclei is $2.73 \times 10^{9} \mathrm{~kJ} / \mathrm{mol}$. In other words, $2.73 \times 10^{9} \mathrm{~kJ} / \mathrm{mol}$ is released when helium-4 nuclei are formed, and $2.73 \times 10^{9} \mathrm{~kJ} / \mathrm{mol}$ must be supplied to disintegrate helium-4 nuclei into isolated protons and neutrons. This enormous amount of energy is more than 10 million times the energy change associated with a typical chemical process!

To make comparisons among different nuclides easier, binding energies are usually expressed on a per-nucleon basis using electron volts ( eV ) as the energy unit, where $1 \mathrm{eV}=1.60 \times 10^{-19} \mathrm{~J}$ and 1 million electron volts $(1 \mathrm{MeV})=1.60 \times 10^{-13} \mathrm{~J}$. Thus, the helium -4 binding energy is $7.08 \mathrm{MeV} /$ nucleon:

$$
\begin{aligned}
\text { Helium-4 binding energy } & =\left(\frac{2.73 \times 10^{12} \mathrm{~J} / \mathrm{mol}}{6.022 \times 10^{23} \text { nuclei } / \mathrm{mol}}\right)\left(\frac{1 \mathrm{MeV}}{1.60 \times 10^{-13} \mathrm{~J}}\right)\left(\frac{1 \text { nucleus }}{4 \text { nucleons }}\right) \\
& =7.08 \mathrm{MeV} / \text { nucleon }
\end{aligned}
$$

A plot of binding energy per nucleon for the most stable isotope of each element is shown in Figure 22.7. Since a higher binding energy per nucleon corresponds to greater stability, the most stable nuclei are at the top of the curve. Iron-56, with a binding energy of $8.79 \mathrm{MeV} /$ nucleon, is the most stable isotope known. If all the mass in the universe were somehow converted to its most stable form, the universe would become a chunk of iron.


The idea that mass and energy are interconvertible is a potentially disturbing one because it seems to overthrow two of the fundamental principles on which chemistry is based-the law of mass conservation and the law of energy conservation. In fact, what the mass/energy interconversion means is that the two individual laws must be combined. Neither mass nor energy is conserved separately; only the combination of the two is conserved. Every time we do a reaction, whether nuclear or chemical, mass and energy are interconverted, but the combination of the two is conserved. For the energy changes involved in typical chemical reactions, however, the effects are so small that the mass change can't be detected by even the best analytical balance. Worked Example 22.7 illustrates a mass-energy calculation for a chemical reaction.

## Worked Example 22.6

Helium-6 is a radioactive isotope with $t_{1 / 2}=0.861 \mathrm{~s}$. Calculate the mass defect (in $\mathrm{g} / \mathrm{mol}$ ) for the formation of a ${ }^{6} \mathrm{He}$ nucleus, and calculate the binding energy in $\mathrm{MeV} /$ nucleon. Is a ${ }^{6} \mathrm{He}$ nucleus more stable or less stable than a ${ }^{4} \mathrm{He}$ nucleus? (The mass of a ${ }^{6} \mathrm{He}$ atom is 6.01889 amu .)

## Strategy

Find the mass defect by subtracting the mass of the ${ }^{6} \mathrm{He}$ nucleus from the mass of the constituent nucleons, and then use the Einstein equation to find the ${ }^{6} \mathrm{He}$ binding energy.

4 FIGURE 22.7 The binding energy per nucleon for the most stable isotope of each naturally occurring element. Binding energy reaches a maximum of $8.79 \mathrm{MeV} /$ nucleon at ${ }^{56} \mathrm{Fe}$.
As a result, there is an increase in stability when much lighter elements fuse together to yield heavier elements up to ${ }^{56} \mathrm{Fe}$ and when much heavier elements split apart to yield lighter elements down to ${ }^{56} \mathrm{Fe}$, as indicated by the red arrows.

## Solution

First, calculate the total mass of the nucleons $(4 n+2 p)$ :

$$
\begin{aligned}
& \text { Mass of } 4 \text { neutrons }=(4)(1.00866 \mathrm{amu})=4.03464 \mathrm{amu} \\
& \text { Mass of } 2 \text { protons }=(2)(1.00728 \mathrm{amu})=2.01456 \mathrm{amu} \\
& \hline \text { Mass of } 4 \mathrm{n}+2 \mathrm{p}
\end{aligned}
$$

Next, calculate the mass of a ${ }^{6} \mathrm{He}$ nucleus by subtracting the mass of two electrons from the mass of a ${ }^{6} \mathrm{He}$ atom:

$$
\begin{array}{llr}
\text { Mass of helium-6 atom } & =6.01889 \mathrm{amu} \\
- \text { Mass of } 2 \text { electrons }=-(2)\left(5.486 \times 10^{-4} \mathrm{amu}\right) & = & -0.00110 \mathrm{amu} \\
\hline \text { Mass of helium-6 nucleus } & =6.01779 \mathrm{amu}
\end{array}
$$

Then subtract the mass of the ${ }^{6} \mathrm{He}$ nucleus from the mass of the nucleons to find the mass defect:

$$
\begin{aligned}
\text { Mass defect } & =\text { Mass of nucleons }- \text { Mass of nucleus } \\
& =(6.04920 \mathrm{amu})-(6.01779 \mathrm{amu}) \\
& =0.03141 \mathrm{amu}, \text { or } 0.03141 \mathrm{~g} / \mathrm{mol}
\end{aligned}
$$

Now, use the Einstein equation to convert the mass defect into binding energy:

$$
\begin{aligned}
\Delta E=\Delta m c^{2} & =\left(0.03141 \frac{\mathrm{~g}}{\mathrm{~mol}}\right)\left(10^{-3} \frac{\mathrm{~kg}}{\mathrm{~g}}\right)\left(3.00 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2} \\
& =2.83 \times 10^{12} \mathrm{~J} / \mathrm{mol}=2.83 \times 10^{9} \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

This value can be expressed in units of $\mathrm{MeV} /$ nucleon by dividing by Avogadro's number, converting to MeV , and dividing by the number of nucleons:

$$
\left(\frac{2.83 \times 10^{12} \frac{\mathrm{~J}}{\mathrm{~mol}}}{6.022 \times 10^{23} \frac{\text { nuclei }}{\mathrm{mol}}}\right)\left(\frac{1 \mathrm{MeV}}{1.60 \times 10^{-13} \mathrm{~J}}\right)\left(\frac{1 \text { nucleus }}{6 \text { nucleons }}\right)=4.89 \mathrm{MeV} / \text { nucleon }
$$

The binding energy of a radioactive ${ }^{6} \mathrm{He}$ nucleus is $4.89 \mathrm{MeV} /$ nucleon, making it less stable than a ${ }^{4} \mathrm{He}$ nucleus, whose binding energy is $7.08 \mathrm{MeV} /$ nucleon.

## Worked Example 22.7

What is the change in mass (in grams) when 2 mol of hydrogen atoms combine to form 1 mol of hydrogen molecules?

$$
2 \mathrm{H} \longrightarrow \mathrm{H}_{2} \quad \Delta E=-436 \mathrm{~kJ}
$$

## Strategy

The problem asks us to calculate a mass defect $\Delta m$ when the energy change $\Delta E$ is known. To do this, we have to rearrange the Einstein equation to solve for mass, remembering that $1 \mathrm{~J}=1 \mathrm{~kg} \cdot \mathrm{~m}^{2} / \mathrm{s}^{2}$.

## Solution

$$
\begin{aligned}
\Delta m & =\frac{\Delta E}{c^{2}}=\frac{(-436 \mathrm{~kJ})\left(10^{3} \frac{\mathrm{~J}}{\mathrm{~kJ}}\right)\left(\frac{1 \mathrm{~kg} \cdot \mathrm{~m}^{2} / \mathrm{s}^{2}}{1 \mathrm{~J}}\right)}{\left(3.00 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2}} \\
& =-4.84 \times 10^{-12} \mathrm{~kg}=-4.84 \times 10^{-9} \mathrm{~g}
\end{aligned}
$$

The loss in mass accompanying formation of 1 mol of $\mathrm{H}_{2}$ molecules from its constituent atoms is $4.84 \times 10^{-9} \mathrm{~g}$, far too small an amount to be detectable by any balance currently available.

PROBLEM 22.11 Calculate the mass defect (in $\mathrm{g} / \mathrm{mol}$ ) for the formation of an oxygen-16 nucleus, and calculate the binding energy in $\mathrm{MeV} /$ nucleon. The mass of an ${ }^{16} \mathrm{O}$ atom is 15.99492 amu .

- PROBLEM 22.12 What is the mass change (in $\mathrm{g} / \mathrm{mol}$ ) for the thermite reaction of aluminum with iron(III) oxide?

$$
2 \mathrm{Al}(s)+\mathrm{Fe}_{2} \mathrm{O}_{3}(s) \longrightarrow \mathrm{Al}_{2} \mathrm{O}_{3}(s)+2 \mathrm{Fe}(s) \quad \Delta E=-852 \mathrm{~kJ}
$$

## 22.6 | Nuclear Fission and Fusion

A careful look at the plot of atomic number versus binding energy per nucleon in Figure 22.7 leads to some interesting and enormously important conclusions. The fact that binding energy per nucleon begins at a relatively low value for ${ }_{1}^{2} \mathrm{H}$, reaches a maximum at ${ }_{26}^{56} \mathrm{Fe}$, and then gradually tails off implies that both lighter and heavier elements are less stable than midweight elements near iron-56. Very heavy elements can therefore gain stability and release energy if they fragment to yield midweight elements, while very light elements can gain stability and release energy if they fuse together. The two resultant processes-fission for the fragmenting of heavy nuclei and fusion for the joining together of light nuclei-have changed the world since their discovery in the late 1930s and early 1940s.

## Nuclear Fission

Certain nuclei-uranium-233, uranium-235, and plutonium-239, for example-do more than undergo simple radioactive decay; they break into fragments when struck by neutrons. As illustrated in Figure 22.8, an incoming neutron causes the nucleus to split into two smaller pieces of roughly similar size.


The fission of a nucleus does not occur in exactly the same way each time: Nearly 400 different fission pathways have been identified for uranium-235, yielding nearly 800 different fission products. One of the more frequently occurring pathways generates barium-142 and krypton-91, along with two additional neutrons plus the one neutron that initiated the fission:

$$
{ }_{0}^{1} \mathrm{n}+{ }_{92}^{235} \mathrm{U} \longrightarrow{ }_{56}^{142} \mathrm{Ba}+{ }_{36}^{91} \mathrm{Kr}+3{ }_{0}^{1} \mathrm{n}
$$

The three neutrons released by fission of a ${ }^{235} \mathrm{U}$ nucleus can induce three more fissions yielding nine neutrons, which can induce nine more fissions yielding

Ruth Lewin Sime, "Lise Meitner and the Discovery of Fission," J. Chem. Educ., Vol. 66, 1989, 373-378.

Ruth Lewin Sime, "Lise Meitner and the Discovery of Fission," Scientific American, January 1998, 80-85.

FIGURE 22.8 A representation of nuclear fission. A uranium-235 nucleus fragments when struck by a neutron, yielding two smaller nuclei and releasing a large amount of energy.


A An enormous amount of energy is released in the explosion that accompanies an uncontrolled nuclear chain reaction.

Nuclear Power Plant Diagram activity

27 neutrons, and so on indefinitely. The result is a chain reaction that continues to occur even if the external supply of neutrons is cut off. If the sample size is small, many of the neutrons escape before initiating additional fission events, and the chain reaction soon stops. If there is a sufficient amount of ${ }^{235} \mathrm{U}$, though—an amount called the critical mass-enough neutrons remain for the chain reaction to become selfsustaining. Under high-pressure conditions that confine the ${ }^{235} \mathrm{U}$ to a small volume, the chain reaction may even occur so rapidly that a nuclear explosion results. For ${ }^{235} \mathrm{U}$, the critical mass is about 56 kg , although the amount can be reduced to 15 kg by placing a coating of ${ }^{238} \mathrm{U}$ around the ${ }^{235} \mathrm{U}$ to reflect back some of the escaping neutrons.

The amount of energy released during nuclear fission can be calculated as in Worked Example 22.8 by finding the accompanying mass change and then using the Einstein mass-energy relationship discussed in the previous section. When calculating the mass change, it's simplest to use the masses of the atoms corresponding to the relevant nuclei, rather than the masses of the nuclei themselves, because the number of electrons is the same in both reactants and products and thus cancels from the calculation.

## Worked Example 22.8

How much energy (in $\mathrm{kJ} / \mathrm{mol}$ ) is released by the fission of uranium- 235 to form barium-142 and krypton-91? The atomic masses are ${ }^{235} \mathrm{U}$ ( 235.0439 amu ), ${ }^{142} \mathrm{Ba}$ (141.9164 amu), ${ }^{91} \mathrm{Kr}(90.9234 \mathrm{amu})$, and $\mathrm{n}(1.00866 \mathrm{amu})$.

$$
{ }_{0}^{1} \mathrm{n}+{ }_{92}^{235} \mathrm{U} \longrightarrow{ }_{56}^{142} \mathrm{Ba}+{ }_{36}^{91} \mathrm{Kr}+3{ }_{0}^{1} \mathrm{n}
$$

## Strategy

First calculate the mass change by subtracting the masses of the products from the mass of the ${ }^{235} \mathrm{U}$ reactant, and then use the Einstein equation to convert mass to energy.

## SOLUTION

$$
\begin{array}{lll}
\text { Mass of }{ }^{235} \mathrm{U} & & 235.0439 \mathrm{amu} \\
\text {-Mass of }{ }^{142} \mathrm{Ba} & = & -141.9164 \mathrm{amu} \\
\text {-Mass of }{ }^{91} \mathrm{Kr} & = & -90.9234 \mathrm{amu} \\
- \text { Mass of } 2 \mathrm{n}=-(2)(1.00866 \mathrm{amu}) & = & -2.0173 \mathrm{amu} \\
\hline \text { Mass change: } & =0.1868 \mathrm{amu}(\text { or } 0.1868 \mathrm{~g} / \mathrm{mol}) \\
\qquad \begin{aligned}
\Delta E & =\Delta m c^{2} \\
& =\left(0.1868 \frac{\mathrm{~g}}{\mathrm{~mol}}\right)\left(1 \times 10^{-3} \frac{\mathrm{~kg}}{\mathrm{~g}}\right)\left(3.00 \times 10^{8} \frac{\mathrm{~m}}{\mathrm{~s}}\right)^{2} \\
& =1.68 \times 10^{13} \mathrm{~kg} \cdot \mathrm{~m}^{2} /\left(\mathrm{s}^{2} \cdot \mathrm{~mol}\right)=1.68 \times 10^{10} \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
\end{array}
$$

Nuclear fission of ${ }^{235} \mathrm{U}$ releases $1.68 \times 10^{10} \mathrm{~kJ} / \mathrm{mol}$.
PROBLEM 22.13 An alternative pathway for the nuclear fission of ${ }^{235} \mathrm{U}$ produces tellurium-137 and zirconium-97. How much energy (in $\mathrm{kJ} / \mathrm{mol}$ ) is released in this fission pathway?

$$
{ }_{0}^{1} \mathrm{n}+{ }_{92}^{235} \mathrm{U} \longrightarrow{ }_{52}^{137} \mathrm{Te}+{ }_{40}^{97} \mathrm{Zr}+2{ }_{0}^{1} \mathrm{n}
$$

The masses are ${ }^{235} \mathrm{U}(235.0439 \mathrm{amu}),{ }^{137} \mathrm{Te}(136.9254 \mathrm{amu}),{ }^{97} \mathrm{Zr}(96.9110 \mathrm{amu})$, and n (1.008 66 amu ).

## Nuclear Reactors

The same fission process that leads to a nuclear explosion under some conditions can be used to generate electric power when carried out in a controlled manner in a nuclear reactor (Figure 22.9). The principle behind a nuclear reactor is simple:


Uranium fuel is placed in a containment vessel surrounded by circulating coolant, and control rods are added. Made of substances such as boron and cadmium, which absorb and thus regulate the flow of neutrons, the control rods are raised and lowered as necessary to maintain the fission at a barely self-sustainable rate so that overheating is prevented. Energy from the controlled fission heats the circulating coolant, which in turn produces steam to drive a turbine and produce electricity.

Naturally occurring uranium is a mixture of two isotopes. The nonfissionable ${ }^{238} \mathrm{U}$ isotope has a natural abundance of $99.3 \%$, while the fissionable ${ }^{235} \mathrm{U}$ isotope is present only to the extent of $0.7 \%$. The fuel used in nuclear reactors is typically made of compressed pellets of $\mathrm{UO}_{2}$ that have been isotopically enriched to a $3 \%$ concentration of ${ }^{235} \mathrm{U}$ and then encased in zirconium rods. The rods are placed in a pressure vessel filled with water, which acts as a moderator to slow the neutrons so they can be captured more readily. No nuclear explosion can occur in a reactor because the amount and concentration of fissionable fuel is too low and because the fuel is not confined by pressure into a small volume. In a worst-case accident, however, uncontrolled fission could lead to enormous overheating that could melt the reactor and surrounding containment vessel, thereby releasing large amounts of radioactivity to the environment.

Thirty countries around the world now obtain some of their electricity from nuclear energy (Figure 22.10). Lithuania leads with $78 \%$, followed by a number of other European countries that have also made a substantial commitment to the technology. The United States has been more cautious, with only $20 \%$ of its power coming from nuclear plants. Worldwide, 439 nuclear plants were in operation in early 2002, with an additional 32 under construction, most of them in Asia. Approximately $21 \%$ of the world's electrical power is generated by nuclear reactors.

The primary problem holding back future development is the yet unsolved matter of how to dispose of the radioactive wastes generated by the plants. It will take at least 600 years for waste strontium- 90 to decay to safe levels, and at least 20,000 years for plutonium-239 to decay.

## Nuclear Fusion

Just as heavy nuclei such as ${ }^{235} \mathrm{U}$ release energy when they undergo fission, very light nuclei such as the isotopes of hydrogen release enormous amounts of energy when they undergo fusion. In fact, it's just this fusion reaction of hydrogen nuclei to

A FIGURE 22.9 A nuclear power plant. Heat produced in the reactor core is transferred by coolant circulating in a closed loop to a steam generator, and the steam then drives a turbine to generate electricity.

Michael Freemantle, "Ten Years After Chernobyl: Consequences are Still Emerging," Chem. Eng. News, April 29, 1996, 18-28.

10Gregory R. Choppin, "Aspects of Nuclear Waste Disposal of Use in Teaching Basic Chemistry," J. Chem. Educ., Vol. 71, 1994, 826-829.

Torkil H. Jensen, "Fusion-A Potential Power Source," J. Chem. Educ., Vol. 71, 1994, 820-823.

FIGURE 22.10 Percentage of electricity generated by nuclear power in 2001.

The variation in slope of a plot of the binding energy versus mass number shows that a typical fusion process releases far more energy than the fission processes employed in nuclear reactors.

produce helium that powers our sun and other stars. Among the processes thought to occur in the sun are those in the following sequence leading to helium-4:

$$
\begin{aligned}
& { }_{1}^{1} \mathrm{H}+{ }_{1}^{1} \mathrm{H} \longrightarrow{ }_{1}^{2} \mathrm{H}+{ }_{1}^{0} \mathrm{e} \\
& { }_{1}^{1} \mathrm{H}+{ }_{1}^{2} \mathrm{H} \longrightarrow{ }_{2}^{3} \mathrm{He} \\
& { }_{2}^{3} \mathrm{He}+{ }_{2}^{3} \mathrm{He} \longrightarrow{ }_{2}^{4} \mathrm{He}+2{ }_{1}^{1} \mathrm{H} \\
& { }_{2}^{3} \mathrm{He}+{ }_{1}^{1} \mathrm{H} \longrightarrow{ }_{2}^{4} \mathrm{He}+{ }_{1}^{0} \mathrm{e}
\end{aligned}
$$

The main appeal of nuclear fusion as a power source is that the hydrogen isotopes used as fuel are cheap and plentiful and that the fusion products are nonradioactive and nonpolluting. The technical problems that must be solved before achieving a practical and controllable fusion method are staggering, however. Not the least of the problems is that a temperature of approximately 40 million kelvins is needed to initiate the fusion process.

- PROBLEM 22.14 Calculate the amount of energy released (in $\mathrm{kJ} / \mathrm{mol}$ ) for the fusion reaction of ${ }^{1} \mathrm{H}$ and ${ }^{2} \mathrm{H}$ atoms to yield a ${ }^{3} \mathrm{He}$ atom:

$$
{ }_{1}^{1} \mathrm{H}+{ }_{1}^{2} \mathrm{H} \longrightarrow{ }_{2}^{3} \mathrm{He}
$$

The atomic masses are ${ }^{1} \mathrm{H}(1.00783 \mathrm{amu}),{ }^{2} \mathrm{H}(2.01410 \mathrm{amu})$, and ${ }^{3} \mathrm{He}(3.01603 \mathrm{amu})$.

## 22.7 | Nuclear Transmutation

Only about 300 of the more than 3600 known isotopes occur naturally. The remainder have been made by nuclear transmutation, the change of one element into another. Such transmutation is often brought about by bombardment of an atom with a high-energy particle such as a proton, neutron, or $\alpha$ particle. In the ensuing collision between particle and atom, an unstable nucleus is momentarily
created, a nuclear change occurs, and a different element is produced. The first nuclear transmutation was accomplished in 1917 by Ernest Rutherford, who bombarded ${ }^{14} \mathrm{~N}$ nuclei with $\alpha$ particles and found that ${ }^{17} \mathrm{O}$ was produced:

$$
{ }_{7}^{14} \mathrm{~N}+{ }_{2}^{4} \mathrm{He} \longrightarrow{ }_{8}^{17} \mathrm{O}+{ }_{1}^{1} \mathrm{H}
$$

Other nuclear transmutations can lead to the synthesis of entirely new elements never before seen on Earth. In fact, all the transuranium elements-those elements with atomic numbers greater than 92 -have been produced by bombardment reactions. Plutonium, for example, can be made by bombarding uranium-238 with $\alpha$ particles:

$$
{ }_{92}^{238} \mathrm{U}+{ }_{2}^{4} \mathrm{He} \longrightarrow{ }_{94}^{241} \mathrm{Pu}+{ }_{0}^{1} \mathrm{n}
$$

The plutonium-241 that results from uranium-238 bombardment is itself radioactive with a half-life of 14.4 years, decaying by $\beta$ emission to yield americium241. (If the name sounds familiar, it's because americium is used commercially in making smoke detectors.) Americium-241 is also radioactive, decaying by $\alpha$ emission with a half-life of 432 years.

$$
\begin{array}{r}
{ }_{94}^{241} \mathrm{Pu} \longrightarrow{ }_{95}^{241} \mathrm{Am}+{ }_{-1}^{0} \mathrm{e} \\
{ }_{95}^{241} \mathrm{Am} \longrightarrow{ }_{93}^{237} \mathrm{~Np}+{ }_{2}^{4} \mathrm{He}
\end{array}
$$

Still other nuclear transmutations are carried out using neutrons, protons, or other particles for bombardment. The cobalt-60 used in radiation therapy for cancer patients can be prepared by neutron bombardment of iron-58. Iron-58 first absorbs a neutron to yield iron-59, the iron-59 undergoes $\beta$ decay to yield cobalt59 , and the cobalt-59 then absorbs a second neutron to yield cobalt-60:

$$
\begin{aligned}
& { }^{56} \mathrm{Fe}+{ }_{0}^{1} \mathrm{n} \longrightarrow{ }_{26}^{59} \mathrm{Fe} \\
& { }_{29}^{59} \mathrm{Fe} \longrightarrow{ }_{27}^{59} \mathrm{Co}+{ }_{-1}^{0} \mathrm{e} \\
& { }_{27}^{59} \mathrm{Co}+{ }_{0}^{1} \mathrm{n} \longrightarrow{ }_{27}^{60} \mathrm{Co}
\end{aligned}
$$

The overall change can be written as

$$
{ }_{26}^{58} \mathrm{Fe}+2{ }_{0}^{1} \mathrm{n} \longrightarrow{ }_{27}^{60} \mathrm{Co}+{ }_{-1}^{0} \mathrm{e}
$$



The Fermi National Accelerator Laboratory has a particle accelerator 4 mi in circumference that is able to accelerate protons to energies of 1 trillion eV.

## VORKED EXAMPLE 22.9

The element berkelium was first prepared at the University of California at Berkeley in 1949 by $\alpha$ bombardment of ${ }_{95}^{241} \mathrm{Am}$. Two neutrons are also produced during the reaction. What isotope of berkelium results from this transmutation? Write a balanced nuclear equation.

## Strategy and Solution

According to the periodic table, berkelium has $Z=97$. Since the sum of the reactant mass numbers is $241+4=245$ and 2 neutrons are produced, the berkelium isotope must have a mass number of 243 .

$$
{ }_{95}^{241} \mathrm{Am}+{ }_{2}^{4} \mathrm{He} \longrightarrow{ }_{97}^{243} \mathrm{Bk}+2{ }_{0}^{1} \mathrm{n}
$$

- PROBLEM 22.15 Write a balanced nuclear equation for the reaction of argon-40 with a proton:

$$
{ }_{18}^{40} \mathrm{Ar}+{ }_{1}^{1} \mathrm{H} \longrightarrow ?+{ }_{0}^{1} \mathrm{n}
$$

- PROBLEM 22.16 Write a balanced nuclear equation for the reaction of uranium238 with a deuteron $\left({ }_{1}^{2} \mathrm{H}\right)$ :

$$
{ }_{92}^{238} \mathrm{U}+{ }_{1}^{2} \mathrm{H} \longrightarrow ?+2{ }_{0}^{1} \mathrm{n}
$$

## 22.8 | Detecting and Measuring Radioactivity

Radioactive emissions are invisible. We can't see, hear, smell, touch, or taste them, no matter how high the dose. We can, however, detect radiation by measuring its ionizing properties. High-energy radiation of all kinds is usually grouped under the name ionizing radiation because interaction of the radiation with a molecule knocks an electron from the molecule, thereby ionizing it.

$$
\text { Molecule } \xrightarrow[\text { radiation }]{\text { Ionizing }} \text { Ion }+\mathrm{e}^{-}
$$

Ionizing radiation includes not only $\alpha$ particles, $\beta$ particles, and $\gamma$ rays, but also X rays and cosmic rays. X rays, like $\gamma$ rays, are high-energy photons $(\lambda=$ $10^{-8}-10^{-11} \mathrm{~m}$ ) rather than particles; cosmic rays are energetic particles coming from interstellar space. They consist primarily of protons, along with some $\alpha$ and $\beta$ particles.

The simplest device for detecting radiation is the photographic film badge worn by people who routinely work with radioactive materials. Any radiation striking the badge causes it to fog. Perhaps the best-known method for measuring radiation is the Geiger counter, an argon-filled tube containing two electrodes (Figure 22.11). The inner walls of the tube are coated with an electrically conducting material and given a negative charge, and a wire in the center of the tube is given a positive charge. As radiation enters the tube through a thin window, it strikes and ionizes argon atoms, releasing electrons that briefly conduct a tiny electric current between the electrodes. The passage of the current is detected, amplified, and used to produce a clicking sound or to register on a meter. The more radiation that enters the tube, the more frequent the clicks.

This photographic film badge is a common device for monitoring radiation exposure.



The most versatile method for measuring radiation in the laboratory is the scintillation counter, in which a substance called a phosphor, often a sodium iodide crystal containing a small amount of thallium iodide, emits a flash of light when struck by radiation. The number of flashes is counted electronically and converted into an electrical signal.

Radiation intensity is expressed in different ways, depending on what is being measured. Some units measure the number of nuclear decay events; others measure the amount of exposure to radiation or the biological consequences of radiation (Table 22.3).

TABLE 22.3 Units for Measuring Radiation

| Unit | Quantity Measured | Description |
| :---: | :---: | :---: |
| Becquerel (Bq) | Decay events | Amount of sample that undergoes 1 disintegration/s |
| Curie (Ci) | Decay events | Amount of sample that undergoes $3.7 \times 10^{10}$ disintegrations/s |
| Gray (Gy) | Energy absorbed per kilogram of tissue | $1 \mathrm{~Gy}=1 \mathrm{~J} / \mathrm{kg}$ tissue |
| Rad | Energy absorbed per kilogram of tissue | $1 \mathrm{rad}=0.01 \mathrm{~Gy}$ |
| Sievert (Sv) | Tissue damage | $1 \mathrm{~Sv}=1 \mathrm{~J} / \mathrm{kg}$ |
| Rem | Tissue damage | $1 \mathrm{rem}=0.01 \mathrm{~Sv}$ |

FIGURE 22.11 A Geiger counter for measuring radiation. As radiation enters the tube through a thin window, it ionizes argon atoms and produces electrons that conduct a tiny electric current from the negatively charged walls to the positively charged center electrode. The current flow then registers on the meter.


A Radiation is conveniently detected and measured using this scintillation counter, which electronically counts the flashes produced when radiation strikes a phosphor.


- The becquerel $(\mathrm{Bq})$ is the SI unit for measuring the number of nuclear disintegrations occurring per second in a sample: $1 \mathrm{~Bq}=1$ disintegration/s. The curie $(\mathrm{Ci})$ and millicurie $(\mathrm{mCi})$ also measure disintegrations per unit time, but
they are far larger units than the becquerel and are more often used, particularly in medicine and biochemistry. One curie is the decay rate of 1 g of radium, equal to $3.7 \times 10^{10} \mathrm{~Bq}$ :

$$
\begin{aligned}
& 1 \mathrm{~Bq}=1 \text { disintegration } / \mathrm{s} \\
& 1 \mathrm{Ci}=3.7 \times 10^{10} \mathrm{~Bq}=3.7 \times 10^{10} \text { disintegrations } / \mathrm{s}
\end{aligned}
$$

For example, a 1.5 mCi sample of tritium is equal to $5.6 \times 10^{7} \mathrm{~Bq}$, meaning that it undergoes $5.6 \times 10^{7}$ disintegrations/s.

$$
(1.5 \mathrm{mCi})\left(10^{-3} \frac{\mathrm{Ci}}{\mathrm{mCi}}\right)\left(3.7 \times 10^{10} \frac{\mathrm{~Bq}}{\mathrm{Ci}}\right)=5.6 \times 10^{7} \mathrm{~Bq}
$$

- The gray (Gy) is the SI unit for measuring the amount of energy absorbed per kilogram of tissue exposed to a radiation source: $1 \mathrm{~Gy}=1 \mathrm{~J} / \mathrm{kg}$. The rad (radiation absorbed dose) also measures tissue exposure and is more often used in medicine.

$$
1 \mathrm{~Gy}=1 \mathrm{~J} / \mathrm{kg} \quad 1 \mathrm{rad}=0.01 \mathrm{~Gy}
$$

- The sievert (Sv) is the SI unit that measures the amount of tissue damage caused by radiation. It takes into account not just the energy absorbed per kilogram of tissue but also the different biological effects of different kinds of radiation. For example, 1 Gy of $\alpha$ radiation causes 20 times more tissue damage than 1 Gy of $\gamma$ rays, but 1 Sv of $\alpha$ radiation and 1 Sv of $\gamma$ rays cause the same amount of damage. The rem (roentgen equivalent for man) is an analogous non-SI unit that is more frequently used in medicine.

$$
1 \mathrm{rem}=0.01 \mathrm{~Sv}
$$

### 22.9 Biological Effects of Radiation

Rosalyn S. Yalow, "Development and Proliferation of Radioimmunoassay Technology," J. Chem. Educ., Vol. 76, 1999, 767-768.

(1)
Rosalyn S. Yalow, "Radioactivity in the Service of Many," J. Chem. Educ., Vol. 59, 1982, 735-738.

Charles H. Atwood, "How Much Radon is Too Much?" J. Chem. Educ., Vol. 69, 1992, 351-353.

The effects of ionizing radiation on the human body vary with the kind and energy of the radiation, the length of exposure, and whether the radiation is from an external or internal source. When coming from an external source, X rays and $\gamma$ radiation are more harmful than $\alpha$ and $\beta$ particles because they penetrate clothing and skin. When coming from an internal source, however, $\alpha$ and $\beta$ particles are particularly dangerous because all their radiation energy is given up to nearby tissue. Alpha emitters are especially hazardous internally and are almost never used in medical applications.

Because of their relatively large mass, $\alpha$ particles move slowly (up to only one-tenth the speed of light) and can be stopped by a few sheets of paper or by the top layer of skin. Beta particles, because they are much lighter, move at up to nine-tenths the speed of light and have about 100 times the penetrating power of
-

TABLE 22.4 Some Properties of Ionizing Radiation

| Type of <br> Radiation | Energy <br> Range | Penetrating Distance <br> in Water |
| :--- | :--- | :--- |
| $\alpha$ | $3-9 \mathrm{MeV}$ | $0.02-0.04 \mathrm{~mm}$ |
| $\beta$ | $0-3 \mathrm{MeV}$ | $0-4 \mathrm{~mm}$ |
| X | $100 \mathrm{eV}-10 \mathrm{keV}$ | $0.01-1 \mathrm{~cm}$ |
| $\gamma$ | $10 \mathrm{keV}-10 \mathrm{MeV}$ | $1-20 \mathrm{~cm}$ |

* Distances at which one-half of the radiation has been stopped
$\alpha$ particles. A block of wood or heavy protective clothing is necessary to stop $\beta$ radiation, which would otherwise penetrate and burn the skin. Gamma rays and X rays move at the speed of light and have about 1000 times the penetrating power of $\alpha$ particles. A lead block several inches thick is needed to stop $\gamma$ and X radiation, which could otherwise penetrate and damage the body's internal organs. Some properties of different kinds of ionizing radiation are summarized in Table 22.4.

The biological effects of different radiation doses are given in Table 22.5. Although the effects sound fearful, the average radiation dose received annually by most people is only about 120 mrem . About $70 \%$ of this radiation comes from natural sources (rocks and cosmic rays); the remaining $30 \%$ comes from medical procedures such as $X$ rays. The amount due to emissions from nuclear power plants and to fallout from atmospheric testing of nuclear weapons in the 1950s is barely detectable.

| TABLE 22.5 | Biological Effects of Short-Term Radiation on Humans |
| :--- | :--- |
| Dose (rem) | Biological Effects |
| $0-25$ | No detectable effects |
| $25-100$ | Temporary decrease in white blood cell count |
| $100-200$ | Nausea, vomiting, longer-term decrease in white blood cells |
| $200-300$ | Vomiting, diarrhea, loss of appetite, listlessness |
| $300-600$ | Vomiting, diarrhea, hemorrhaging, eventual death in some cases |
| Above 600 | Eventual death in nearly all cases |

### 22.10 Applications of Nuclear Chemistry

## Dating with Radioisotopes

Biblical scrolls are found in a cave near the Dead Sea. Are they authentic? A mummy is discovered in an Egyptian tomb. How old is it? The burned bones of a man are dug up near Lubbock, Texas. How long have humans lived in the area? These and many other questions can be answered by archaeologists using a technique called radiocarbon dating. (The Dead Sea Scrolls are 1900 years old and authentic, the mummy is 3100 years old, and the human remains found in Texas are 9900 years old.)

Radiocarbon dating of archaeological artifacts depends on the slow and constant production of radioactive carbon-14 in the upper atmosphere by neutron bombardment of nitrogen atoms. (The neutrons come from the bombardment of other atoms by cosmic rays.)

$$
{ }_{7}^{14} \mathrm{~N}+{ }_{0}^{1} \mathrm{n} \longrightarrow{ }_{6}^{14} \mathrm{C}+{ }_{1}^{1} \mathrm{H}
$$

Carbon-14 atoms produced in the upper atmosphere combine with oxygen to yield ${ }^{14} \mathrm{CO}_{2}$, which slowly diffuses into the lower atmosphere, where it mixes with ordinary ${ }^{12} \mathrm{CO}_{2}$ and is taken up by plants during photosynthesis. When these plants are eaten, carbon-14 enters the food chain and is ultimately distributed evenly throughout all living organisms.

As long as a plant or animal is living, a dynamic equilibrium exists in which an organism excretes or exhales the same amount of ${ }^{14} \mathrm{C}$ that it takes in. As a result, the ratio of ${ }^{14} \mathrm{C}$ to ${ }^{12} \mathrm{C}$ in the living organism is the same as that in the atmosphereabout 1 part in $10^{12}$. When the plant or animal dies, however, it no longer takes in more ${ }^{14} \mathrm{C}$, and the ${ }^{14} \mathrm{C} /{ }^{12} \mathrm{C}$ ratio in the organism slowly decreases as ${ }^{14} \mathrm{C}$ undergoes radioactive decay by $\beta$ emission, with $t_{1 / 2}=5730$ years.

$$
{ }_{6}^{14} \mathrm{C} \longrightarrow{ }_{7}^{14} \mathrm{~N}+{ }_{-1}^{0} \mathrm{e}
$$



A Radiocarbon dating places the age of this Egyptian mummy at 3100 years.
M. W. Rowe, "Radioactive Dating: A Method for Geochronology," J. Chem. Educ., Vol. 62, 1985, 580-584.
M. W. Rowe, "Archeological Dating," J. Chem. Educ., Vol. 63, 1986, 16-20.

If Kent J. Crippin and Robert D. Cutright, "Modeling Nuclear Decay: A Point of Integration Between Chemistry and Mathematics," J. Chem. Educ., Vol. 75, 1998, 434-436.

Ron DeLorenzo, "California Earthquakes: Predicting the Next Big One Using Radiocarbon Dating," J. Chem. Educ., Vol. 57, 1980, 601.

At 5730 years (one ${ }^{14} \mathrm{C}$ half-life) after the death of the organism, the ${ }^{14} \mathrm{C} /{ }^{12} \mathrm{C}$ ratio has decreased by a factor of 2 ; at 11,460 years after death, the ${ }^{14} \mathrm{C} /{ }^{12} \mathrm{C}$ ratio has decreased by a factor of 4 ; and so on. By measuring the present ${ }^{14} \mathrm{C} /{ }^{12} \mathrm{C}$ ratio in the traces of any once-living organism, archaeologists can determine how long ago the organism died. Human or animal hair from well-preserved remains, charcoal or wood fragments from once-living trees, and cotton or linen from onceliving plants are all useful sources for radiocarbon dating. The technique becomes less accurate as samples get older and the amount of ${ }^{14} \mathrm{C}$ they contain diminishes, but artifacts with an age of 1000-20,000 years can be dated with reasonable accuracy. The outer limit of the technique is about 60,000 years.

Just as radiocarbon measurements allow dating of once-living organisms, similar measurements on other radioisotopes make possible the dating of rocks. Uranium-238, for example, has a half-life of $4.47 \times 10^{9}$ years and decays through the series of events shown previously in Figure 22.6 to yield lead-206. The age of a uranium-containing rock can therefore be determined by measuring the ${ }^{238} \mathrm{U} /{ }^{206} \mathrm{~Pb}$ ratio. Similarly, potassium- 40 has a half-life of $1.28 \times 10^{9}$ years and decays through electron capture and positron emission to yield argon-40. (Both processes yield the same product.)

$$
\begin{aligned}
& { }_{19}^{40} \mathrm{~K}+{ }_{-1}^{0} \mathrm{e} \longrightarrow{ }_{18}^{40} \mathrm{Ar} \\
& { }_{19}^{40} \mathrm{~K} \longrightarrow{ }_{18}^{40} \mathrm{Ar}+{ }_{1}^{0} \mathrm{e}
\end{aligned}
$$

The age of a rock can be found by crushing a sample, measuring the amount of ${ }^{40} \mathrm{Ar}$ gas that escapes, and comparing the amount of ${ }^{40} \mathrm{Ar}$ with the amount of ${ }^{40} \mathrm{~K}$ remaining in the sample. It is through techniques such as these that the age of the earth has been estimated at approximately 4.5 billion years.

## Worked Example 22.10

Radiocarbon measurements made in 1988 on the Shroud of Turin, a religious artifact thought by some to be the burial shroud of Christ, showed a ${ }^{14} \mathrm{C}$ decay rate of 14.2 disintegrations/min per gram of carbon. What age is implied by this result if currently living organisms decay at the rate of 15.3 disintegrations/min per gram of carbon? The half-life of ${ }^{14} \mathrm{C}$ is 5730 years.

## Strategy

As we saw in Worked Example 22.5, the ratio of the decay rate at any time $t$ to the decay rate at time $t=0$ is the same as the ratio of $N$ to $N_{0}$ :

$$
\frac{\text { Decay rate at time } t}{\text { Decay rate at time } t=0}=\frac{k N}{k N_{0}}=\frac{N}{N_{0}}
$$

To date the shroud, we need to calculate the time $t$ that corresponds to the observed decay rate. This can be done by solving for $t$ in the equation

$$
\ln \left(\frac{N}{N_{0}}\right)=(-\ln 2)\left(\frac{t}{t_{1 / 2}}\right)
$$

## SOlUTION

Substituting the proper values into the equation gives

$$
\begin{aligned}
& \ln \left(\frac{14.2}{15.3}\right)=-0.693\left(\frac{t}{5730 \text { years }}\right) \quad \text { or } \quad-0.0746=-0.693\left(\frac{t}{5730 \text { years }}\right) \\
& \text { so } \quad t=\frac{(-0.0746)(5730 \text { years })}{-0.693}=617 \text { years }
\end{aligned}
$$

The Shroud of Turin is approximately 617 years old, indicating that it comes from medieval times.

PROBLEM 22.17 Charcoal found in the Lascaux cave in France, site of many prehistoric cave paintings, was observed to decay at a rate of 2.4 disintegrations $/ \mathrm{min}$ per gram of carbon. What is the age of the charcoal if currently living organisms decay at the rate of 15.3 disintegrations/min per gram of carbon? The half-life of ${ }^{14} \mathrm{C}$ is 5730 years.


4 What is the age of these cave paintings?

## Medical Uses of Radioactivity

The origins of nuclear medicine date to 1901, when the French physician Henri Danlos first used radium in the treatment of a tuberculous skin lesion. Since that time, uses of radioactivity have become a crucial part of modern medical care, both diagnostic and therapeutic. Current nuclear techniques can be grouped into three classes: (1) in vivo procedures, (2) therapeutic procedures, and (3) imaging procedures.

In Vivo Procedures In vivo studies-those that take place inside the body—are carried out to assess the functioning of a particular organ or body system. A radiopharmaceutical agent is administered, and its path in the body-whether it is absorbed, excreted, diluted, or concentrated-is determined by analysis of blood or urine samples.

An example of the many in vivo procedures using radioactive agents is the determination of whole-blood volume by injecting a known quantity of red blood cells labeled with radioactive chromium-51. After a suitable interval to allow the labeled cells to be distributed evenly throughout the body, a blood sample is taken, the amount of dilution of the ${ }^{51} \mathrm{Cr}$ is measured, and the blood volume is calculated. Recall from Section 3.8 that when a concentrated solution is diluted, the amount of solute $\left({ }^{51} \mathrm{Cr}\right.$ in the present instance) remains the same and only the volume changes. That is,

$$
\begin{gathered}
\text { Amount of }{ }^{51} \mathrm{Cr}=C_{0} \times V_{0}=C_{\text {blood }} \times V_{\text {blood }} \\
\text { or } \quad V_{\text {blood }}=\frac{C_{0} V_{0}}{C_{\text {blood }}} \\
\text { where: } \quad C_{0}=\text { Concentration of labeled cells injected }(\mu \mathrm{Ci} / \mathrm{mL}) \\
V_{0}=\text { Volume of labeled cells injected }(\mathrm{mL}) \\
C_{\text {blood }}=\text { Concentration of labeled cells in blood }(\mu \mathrm{Ci} / \mathrm{mL}) \\
V_{\text {blood }}=\text { Blood volume }
\end{gathered}
$$

Therapeutic Procedures Therapeutic procedures-those in which radiation is used to kill diseased tissue-can involve either external or internal sources of radiation. External radiation therapy for the treatment of cancer is often carried out with $\gamma$ rays from a cobalt- 60 source. The highly radioactive source is shielded by a thick lead container and has a small opening directed toward the site of the tumor. By focusing the radiation beam on the tumor and rotating the patient's body, the tumor receives the full exposure while the exposure of surrounding parts of the body is minimized. Nevertheless, sufficient exposure occurs so that most patients suffer some effects of radiation sickness.


A A person's blood volume can be found by injecting a small amount of radioactive chromium-51 and measuring the dilution factor.


A Cancerous tumors can be treated by irradiation with $\gamma$ rays from this cobalt- 60 source.

Mairin B. Brennan, "Positron Emission Tomography Merges Chemistry with Biological Imaging," Chem. Eng. News, February 19, 1996, 26-33.

Marcus E. Raichle, "Visualizing the Mind," Scientific American., April 1994, 64

Timothy J. McCarthy, Sally W. Schwarz, and Michael J. Welch, "Nuclear Medicine and Positron Emission Tomography: An Overview,"J. Chem. Educ., Vol. 71, 1994, 830-836.

Internal radiation therapy is a much more selective technique than external therapy. In the treatment of thyroid disease, for example, iodine-131, a powerful $\beta$ emitter known to localize in the target tissue, is administered internally. Because $\beta$ particles penetrate no farther than several millimeters, the localized ${ }^{131}$ I produces a high radiation dose that destroys only the surrounding diseased tissue.

Imaging Procedures Imaging procedures give diagnostic information about the health of body organs by analyzing the distribution pattern of radioisotopes introduced into the body. A radiopharmaceutical agent that is known to concentrate in a specific tissue or organ is injected into the body, and its distribution pattern is monitored by external radiation detectors. Depending on the disease and the organ, a diseased organ might concentrate more of the radiopharmaceutical than a normal organ and thus show up as a radioactive "hot" spot against a "cold" background. Alternatively, the diseased organ might concentrate less of the radiopharmaceutical than a normal organ and thus show up as a cold spot on a hot background.

The radioisotope most widely used today is technetium-99m, whose short half-life of 6.01 hours minimizes a patient's exposure to harmful effects. Bone scans using Tc-99m, such as that shown in Figure 22.12a, are an important tool in the diagnosis of cancer and other pathological conditions.

Another kind of imaging procedure makes use of a technique called magnetic resonance imaging (MRI). MRI uses no radioisotopes and has no known sideeffects. Instead, MRI uses radio waves to stimulate certain nuclei in the presence of a powerful magnetic field. The stimulated nuclei (normally the hydrogen nuclei in $\mathrm{H}_{2} \mathrm{O}$ molecules) then give off a signal that can be measured, interpreted, and correlated with their environment in the body. Figure 22.12 b shows a brain scan carried out by MRI and indicates the position of a tumor.

FIGURE 22.12 (a) A
bone scan using radioactive technetium-99m. (b) An MRI brain scan, showing the position of a tumor (the large white area at left).


## Interlude The Origin of Chemical Elements

 osmologists tell us that the universe began some 15 billion years ago in an extraordinary event they call the "big bang." Initially, the temperature must have been inconceivably high, but after 1 second, the temperature had dropped to about $10^{10} \mathrm{~K}$ and elementary particles began to form: protons, neutrons, and electrons, as well as positrons and neutrinos-neutral particles with a mass much less than that of an electron. After 3 minutes, the temperature had dropped to $10^{9} \mathrm{~K}$, and protons began fusing with neutrons to form helium nuclei, ${ }_{2}^{4} \mathrm{He}^{2+}$. Matter remained in this form for many millions of years until the expanding universe had cooled to about $10,000 \mathrm{~K}$. Electrons were then able to bind to protons and to helium nuclei, forming stable hydrogen and helium atoms.The attractive force of gravity acting on regions of higher-thanaverage density slowly produced massive local concentrations of matter and ultimately formed billions of galaxies, each with many billions of stars. As the gas clouds of hydrogen and helium condensed under gravitational attraction and stars formed, their temperatures reached $10^{7} \mathrm{~K}$, and their densities reached $100 \mathrm{~g} / \mathrm{cm}^{3}$. Protons and neutrons again fused to yield helium nuclei, generating vast amounts of heat and light-about $6 \times 10^{8} \mathrm{~kJ}$ per mole of prodensaction. tons undergoing fusion.

Most of these early stars probably burned out after a few billion years, but a few were so massive that, as their nuclear fuel diminished, gravitational attraction caused a rapid contraction leading to still higher core temperatures and higher densities-up to $5 \times 10^{8} \mathrm{~K}$ and $5 \times 10^{5} \mathrm{~g} / \mathrm{cm}^{3}$. Much larger nuclei were now formed, including carbon, oxygen, silicon, magnesium, and iron. Ultimately, the stars underwent a gravitational collapse resulting in the synthesis of still-heavier elements and an explosion visible throughout the universe as a supernova.

Matter from exploding supernovas was blown throughout the galaxy,
 forming a new generation of stars and planets. Our own sun and solar system formed only about 4.5 billion years ago from matter released by former supernovas. Except for hydrogen and helium, all the atoms in our bodies, our planet, and our solar system were created more than 5 billion years ago in exploding stars.

PROBLEM 22.18 How do elements heavier than iron arise?

A The instantaneous gravitational collapse of a massive star resulted in this supernova explosion observed in 1987.

Nuclear chemistry is the study of the properties and reactions of atomic nuclei. Nuclear reactions differ from chemical reactions in that they involve a change in an atom's nucleus, often producing a different element. The rate of a nuclear reaction is unaffected by the addition of a catalyst or by a change in temperature or pressure, and the energy change accompanying a nuclear reaction is far greater than that accompanying any chemical reaction. Of the more than 3600 known isotopes, most have been made by nuclear transmutation, the change of one element into another. Such transmutation is often brought about by bombardment of an atom with a highenergy particle such as a proton, neutron, or $\alpha$ particle.

Radioactivity is the spontaneous emission of radiation from an unstable nucleus. Alpha ( $\alpha$ ) radiation consists of helium nuclei, small particles containing two protons and two neutrons $\left({ }_{2}^{4} \mathrm{He}\right)$. Beta ( $\left.\boldsymbol{\beta}\right)$ radiation consists of electrons $\left({ }_{-1}^{0} \mathrm{e}\right)$, and gamma ( $\gamma$ ) radiation consists of high-energy photons that have no mass. Positron emission is the conversion of a proton in the nucleus into a neutron plus an ejected positron, ${ }_{1}^{0} \mathrm{e}$ or $\beta^{+}$, a particle that has the same mass as an electron but an opposite charge. Electron capture is the capture of an inner-shell electron by a proton in the nucleus. The process is accompanied by the emission of $\gamma$ rays and results in the conversion of a proton in the nucleus into a neutron. Every element in the periodic table has at least one radioactive isotope, or radioisotope. Radioactive decay is characterized kinetically by a first-order decay constant and by a half-life, $t_{1 / 2}$, the time required for the
number of radioactive nuclei in a sample to drop to half its initial value.

The stability of a given nucleus is related to its neutron/ proton ratio. Neutrons act as a kind of nuclear glue that holds nuclei together by overcoming proton-proton repulsions. The strength of the forces involved can be measured by calculating an atom's mass defect-the difference in mass between a given nucleus and the total mass of its individual nucleons (protons and neutrons). Applying the Einstein equation $\Delta E=\Delta m c^{2}$ then allows calculation of the nuclear binding energy.

Certain heavy nuclei such as uranium-235 undergo nuclear fission when struck by neutrons, breaking apart into fragment nuclei and releasing enormous amounts of energy. Light nuclei such as the isotopes of hydrogen undergo nuclear fusion when heated to sufficiently high temperatures, forming heavier nuclei and releasing energy.

High-energy radiation of all types- $\alpha$ particles, $\beta$ particles, $\gamma$ rays, X rays, and cosmic rays-is known collectively as ionizing radiation. When ionizing radiation strikes a molecule, it dislodges an electron and leaves an ion. Radiation intensity is expressed in different ways, according to what property is being measured. The becquerel $(\mathrm{Bq})$ and the curie $(\mathrm{Ci})$ measure the number of radioactive disintegrations per second in a sample. The gray (Gy) and the rad measure the amount of radiation absorbed per kilogram of tissue. The sievert (Sv) and the rem measure the amount of tissue damage caused by radiation. Radiation effects become noticeable with a human exposure of 25 rem and become lethal at an exposure above 600 rem.

## Key Words

alpha ( $\boldsymbol{\alpha}$ ) radiation 951
beta ( $\boldsymbol{\beta}$ ) radiation 952
binding energy 962
chain reaction 966
cosmic ray 970
critical mass 966
decay constant 954
decay series 960
electron capture 952
fission 965
fusion 965
gamma $(\gamma)$ radiation 952
ionizing radiation 970
mass defect 962
nuclear chemistry 950
nuclear equation 951
nuclear reaction 950
nuclear transmutation 968
nucleon 950
nuclide 950
positron emission 952
radioactive 951
radioisotope 951
radionuclide 951
transuranium element 958

## Key Concept Summary



## Understanding Key Concepts

Problems 22.1-22.18 appear within the chapter.
22.19 ${ }_{19}^{40} \mathrm{~K}$ decays by positron emission to give ${ }_{18}^{40} \mathrm{Ar}$. If yellow spheres represent ${ }_{19}^{40} \mathrm{~K}$ atoms and blue spheres represent ${ }_{18}^{40} \mathrm{Ar}$ atoms, how many half-lives have passed in the following sample?

22.20 Write the symbol of the isotope represented by the following drawing. Blue spheres represent neutrons, and red spheres represent protons. Do you expect this nuclide to decay by positron emission or $\beta$ emission? Explain.

22.21 Identify the isotopes involved, and tell the type of decay process occurring in the following nuclear reaction:

22.22 Isotope A decays to isotope E through the series of steps shown in the graph. The series has two kinds of processes: one represented by the shorter arrows pointing right and the other represented by the longer arrows pointing left.
(a) What kind of nuclear decay process does each kind of arrow correspond to?
(b) Identify and write the symbol ${ }_{Z}^{A} X$ for each isotope in the decay series:

22.23 What is the half-life of the radionuclide that shows the following decay curve?


## Additional Problems

## Nuclear Reactions and Radioactivity

22.24 Positron emission and electron capture both give a product nuclide whose atomic number is 1 less than the starting nuclide. Explain.
22.25 What is the difference between an $\alpha$ particle and a helium atom?
22.26 Why is an $\alpha$ emitter more hazardous to an organism internally than externally, whereas a $\gamma$ emitter is equally hazardous internally and externally?
22.27 Why do nuclides that are "neutron-rich" emit $\beta$ particles, but nuclides that are "neutron-poor" emit $\alpha$ particles or positrons or undergo electron capture?
22.28 Harmful chemical spills can often be cleaned up by treatment with another chemical. A spill of $\mathrm{H}_{2} \mathrm{SO}_{4}$, for example, can be neutralized by adding $\mathrm{NaHCO}_{3}$. Why can't harmful radioactive wastes from nuclear power plants be cleaned up just as easily?
22.29 The chemical reactions of a ${ }^{24} \mathrm{Na}$ atom and a ${ }^{24} \mathrm{Na}^{+}$ion are completely different, but the nuclear reactions of a ${ }^{24} \mathrm{Na}$ atom and a ${ }^{24} \mathrm{Na}^{+}$ion are identical (both emit $\beta$ particles). Explain.
22.30 Complete and balance the following nuclear equations:
(a) ${ }_{50}^{126} \mathrm{Sn} \rightarrow{ }_{-1}^{0} \mathrm{e}+$ ?
(b) ${ }_{88}^{210} \mathrm{Ra} \rightarrow{ }_{2}^{4} \mathrm{He}+$ ?
(c) ${ }_{37}^{77} \mathrm{Rb} \rightarrow{ }_{1}^{0} \mathrm{e}+$ ?
(d) ${ }_{36}^{76} \mathrm{Kr}+{ }_{-1}^{0} \mathrm{e} \rightarrow$ ?
22.31 Complete and balance the following nuclear equations:
(a) ${ }_{38}^{90} \mathrm{Sr} \rightarrow{ }_{-1}^{0} \mathrm{e}+$ ?
(b) ${ }_{100}^{24} \mathrm{Fm} \rightarrow{ }_{2}^{4} \mathrm{He}+$ ?
(c) ${ }_{25}^{49} \mathrm{Mn} \rightarrow{ }_{1} \mathrm{e}+$ ?
(d) ${ }_{18}^{37} \mathrm{Ar}+{ }_{-1}^{0} \mathrm{e} \rightarrow$ ?
22.32 What particle is produced in each of the following decay reactions?
(a) ${ }_{80}^{188} \mathrm{Hg} \rightarrow{ }_{79}^{188} \mathrm{Au}+$ ?
(b) ${ }_{85}^{218} \mathrm{At} \rightarrow{ }_{83}^{214} \mathrm{Bi}+$ ?
(c) ${ }_{90}^{234} \mathrm{Th} \rightarrow{ }_{91}^{234} \mathrm{~Pa}+$ ?
22.33 What particle is produced in each of the following decay reactions?
(a) ${ }_{11}^{24} \mathrm{Na} \rightarrow{ }_{12}^{24} \mathrm{Mg}+$ ?
(b) ${ }_{60}^{135} \mathrm{Nd} \rightarrow{ }_{59}^{135} \mathrm{Pr}+$ ?
(c) ${ }_{78}^{170} \mathrm{Pt} \rightarrow{ }_{76}^{166} \mathrm{Os}+$ ?
22.34 Write balanced nuclear equations for the following processes:
(a) Alpha emission of ${ }^{162} \mathrm{Re}$
(b) Electron capture of ${ }^{138} \mathrm{Sm}$
(c) Beta emission of ${ }^{188} \mathrm{~W}$
(d) Positron emission of ${ }^{165} \mathrm{Ta}$
22.35 Write balanced nuclear equations for the following processes:
(a) Beta emission of ${ }^{157} \mathrm{Eu}$
(b) Electron capture of ${ }^{126} \mathrm{Ba}$
(c) Alpha emission of ${ }^{146} \mathrm{Sm}$
(d) Positron emission of ${ }^{125} \mathrm{Ba}$
22.36 Of the two isotopes of tungsten, ${ }^{160} \mathrm{~W}$ and ${ }^{185} \mathrm{~W}$, one decays by $\beta$ emission and one decays by $\alpha$ emission. Which is which? Explain.
22.37 Of the two isotopes of iodine, ${ }^{136} \mathrm{I}$ and ${ }^{122} \mathrm{I}$, one decays by $\beta$ emission and one decays by positron emission. Which is which? Explain.
22.38 Americium-241, a radioisotope used in smoke detectors, decays by a series of 12 reactions involving sequential loss of $\alpha, \alpha, \beta, \alpha, \alpha, \beta, \alpha, \alpha, \alpha, \beta, \alpha$, and $\beta$ particles. Identify each intermediate nuclide and the final stable product nucleus.
22.39 Radon-222 decays by a series of three $\alpha$ emissions and two $\beta$ emissions. What is the final stable nuclide?
22.40 Thorium- 232 decays by a 10 -step series, ultimately yielding lead-208. How many $\alpha$ particles and how many $\beta$ particles are emitted?
22.41 How many $\alpha$ particles and how many $\beta$ particles are emitted in the 11 -step decay of ${ }^{235} \mathrm{U}$ into ${ }^{207} \mathrm{~Pb}$ ?

## Radioactive Decay Rates

22.42 What does it mean when we say that the half-life of iron-59 is 44.5 days?
22.43 What is the difference between a half-life and a decay constant, and what is the relationship between them?
22.44 The half-life of indium-111, a radioisotope used in studying the distribution of white blood cells, is $t_{1 / 2}=2.805$ days. What is the decay constant of ${ }^{111} \mathrm{In}$ ?
22.45 What is the decay constant of gallium-67, a radioisotope used for imaging soft-tissue tumors? The half-life of ${ }^{67} \mathrm{Ga}$ is $t_{1 / 2}=78.25 \mathrm{~h}$.
22.46 The decay constant of thallium-201, a radioisotope used for parathyroid imaging, is 0.228 day $^{-1}$. What is the half-life of ${ }^{201} \mathrm{Tl}$ ?
22.47 The decay constant of plutonium-239, a waste product from nuclear reactors, is $2.88 \times 10^{-5}$ year $^{-1}$. What is the half-life of ${ }^{239} \mathrm{Pu}$ ?
22.48 The half-life of ${ }^{241} \mathrm{Am}$ is 432.2 years. What percentage of an ${ }^{241} \mathrm{Am}$ sample remains after 65 days? After 65 years? After 650 years?
22.49 Fluorine-18 has $t_{1 / 2}=109.8 \mathrm{~min}$. What percentage of an ${ }^{18} \mathrm{~F}$ sample remains after 24 min ? After 24 hours? After 24 days?
22.50 How old is a sample of wood whose ${ }^{14} \mathrm{C}$ content is found to be $43 \%$ that of a living tree? The half-life of ${ }^{14} \mathrm{C}$ is 5730 years.
22.51 What is the age of a rock whose ${ }^{40} \mathrm{Ar} /{ }^{40} \mathrm{~K}$ ratio is 1.15 ? The half-life of ${ }^{40} \mathrm{~K}$ is $1.28 \times 10^{9}$ years.
22.52 The decay constant of ${ }^{35} \mathrm{~S}$ is $7.89 \times 10^{-3}$ day $^{-1}$. What percentage of an ${ }^{35}$ S sample remains after 185 days?
22.53 Plutonium-239 has a decay constant of $2.88 \times$ $10^{-5}$ year $^{-1}$. What percentage of a ${ }^{239} \mathrm{Pu}$ sample remains after 1000 years? After 25,000 years? After 100,000 years?
22.54 Polonium-209, an $\alpha$ emitter, has a half-life of 102 years. How many $\alpha$ particles are emitted in 1.0 s from a 1.0 ng sample of ${ }^{209} \mathrm{Po}$ ?
22.55 Chlorine-36 is a $\beta$ emitter, with a half-life of $3.0 \times 10^{5}$ years. How many $\beta$ particles are emitted in 1.0 min from a 5.0 mg sample of ${ }^{36} \mathrm{Cl}$ ? How many curies of radiation does the 5.0 mg sample represent?
22.56 A 1.0 mg sample of ${ }^{79}$ Se decays initially at a rate of $1.5 \times 10^{5}$ disintegrations/s. What is the half-life of ${ }^{79} \mathrm{Se}$ in years?
22.57 What is the half-life (in years) of ${ }^{44} \mathrm{Ti}$ if a 1.0 ng sample decays initially at a rate of $4.8 \times 10^{3}$ disintegrations $/ \mathrm{s}$ ?
22.58 A sample of ${ }^{37} \mathrm{Ar}$ undergoes 8540 disintegrations/min initially but undergoes 6990 disintegrations/min after 10.0 days. What is the half-life of ${ }^{37} \mathrm{Ar}$ in days?
22.59 A sample of ${ }^{28} \mathrm{Mg}$ decays initially at a rate of 53,500 disintegrations $/ \mathrm{min}$, but the decay rate falls to 10,980 disintegrations $/ \mathrm{min}$ after 48.0 hours. What is the half-life of ${ }^{28} \mathrm{Mg}$ in hours?

## Energy Changes During Nuclear Reactions

22.60 Why does a given nucleus have less mass than the sum of its constituent protons and neutrons?
22.61 In an endothermic chemical reaction, do the products have more mass, less mass, or the same mass as the reactants? Explain.
22.62 What is the wavelength (in nm ) of $\gamma$ rays whose energy is 1.50 MeV ?
22.63 What is the frequency (in Hz ) of $X$ rays whose energy is 6.82 keV ?
22.64 Calculate the mass defect (in $\mathrm{g} / \mathrm{mol}$ ) for the following nuclides:
(a) ${ }^{52} \mathrm{Fe}$ (atomic mass $\left.=51.94811 \mathrm{amu}\right)$
(b) ${ }^{92} \mathrm{Mo}$ (atomic mass $=91.90681 \mathrm{amu}$ )
22.65 Calculate the mass defect (in $\mathrm{g} / \mathrm{mol}$ ) for the following nuclides:
(a) ${ }^{32} \mathrm{~S}$ (atomic mass $\left.=31.97207 \mathrm{amu}\right)$
(b) ${ }^{40} \mathrm{Ca}$ (atomic mass $\left.=39.96259 \mathrm{amu}\right)$
22.66 Calculate the binding energy (in $\mathrm{MeV} /$ nucleon) for the following nuclides:
(a) ${ }^{58} \mathrm{Ni}$ (atomic mass $\left.=57.93535 \mathrm{amu}\right)$
(b) ${ }^{84} \mathrm{Kr}$ (atomic mass $\left.=83.91151 \mathrm{amu}\right)$
22.67 Calculate the binding energy (in $\mathrm{MeV} /$ nucleon) for the following nuclides:
(a) ${ }^{63} \mathrm{Cu}$ (atomic mass $=62.93960 \mathrm{amu}$ )
(b) ${ }^{84} \mathrm{Sr}($ atomic mass $=83.91343 \mathrm{amu})$
22.68 What is the energy change $\Delta E$ (in $\mathrm{kJ} / \mathrm{mol}$ ) when an $\alpha$ particle is emitted from ${ }^{174} \mathrm{Ir}$ ? The atomic mass of ${ }^{174} \mathrm{Ir}$ is 173.96666 amu , the atomic mass of ${ }^{170} \mathrm{Re}$ is 169.95804 amu , and the atomic mass of a ${ }^{4} \mathrm{He}$ atom is 4.00260 amu .

$$
{ }_{77}^{174} \mathrm{Ir} \longrightarrow{ }_{75}^{170} \mathrm{Re}+{ }_{2}^{4} \mathrm{He} \quad \Delta E=?
$$

22.69 Magnesium- 28 is a $\beta$ emitter that decays to aluminum28. How much energy is released in $\mathrm{kJ} / \mathrm{mol}$ ? The atomic mass of ${ }^{28} \mathrm{Mg}$ is 27.98388 amu , and the atomic mass of ${ }^{28} \mathrm{Al}$ is 27.98191 amu .
22.70 What is the mass change (in grams) accompanying the formation of $\mathrm{NH}_{3}$ from $\mathrm{H}_{2}$ and $\mathrm{N}_{2}$ ?
$\mathrm{N}_{2}(g)+3 \mathrm{H}_{2}(g) \longrightarrow 2 \mathrm{NH}_{3}(g) \quad \Delta H^{\circ}=-92.2 \mathrm{~kJ}$
22.71 What is the mass change (in grams) accompanying the formation of CO and $\mathrm{H}_{2}$ in the water-gas reaction?
$\mathrm{C}(\mathrm{s})+\mathrm{H}_{2} \mathrm{O}(\mathrm{g}) \longrightarrow \mathrm{CO}(g)+\mathrm{H}_{2}(g) \Delta H^{\circ}=+131 \mathrm{~kJ}$
22.72 A positron has the same mass as an electron $\left(9.109 \times 10^{-31} \mathrm{~kg}\right)$ but an opposite charge. When the two particles encounter each other, annihilation occurs and only $\gamma$ rays are produced. How much energy (in $\mathrm{kJ} / \mathrm{mol}$ ) is produced?
22.73 How much energy is released (in kJ ) in the fusion reaction of ${ }^{2} \mathrm{H}$ to yield 1 mol of ${ }^{3} \mathrm{He}$ ? The atomic mass of ${ }^{2} \mathrm{H}$ is 2.0141 amu , and the atomic mass of ${ }^{3} \mathrm{He}$ is 3.0160 amu .

$$
2{ }_{1}^{2} \mathrm{H} \longrightarrow{ }_{2}^{3} \mathrm{He}+{ }_{0}^{1} \mathrm{n}
$$

## Nuclear Transmutation

22.74 Give the products of the following nuclear reactions:
(a) ${ }_{47}^{109} \mathrm{Ag}+{ }_{2}^{4} \mathrm{He} \rightarrow$ ?
(b) ${ }_{5}^{10} \mathrm{~B}+{ }_{2}^{4} \mathrm{He} \rightarrow$ ? $+{ }_{0}^{1} \mathrm{n}$
22.75 Balance the following equations for the nuclear fission of ${ }^{235} \mathrm{U}$ :
(a) ${ }_{92}^{235} \mathrm{U} \rightarrow{ }_{62}^{160} \mathrm{Sm}+{ }_{30}^{72} \mathrm{Zn}+?{ }_{0}^{1} \mathrm{n}$
(b) ${ }_{92}^{235} \mathrm{U} \rightarrow{ }_{35}^{87} \mathrm{Br}+?+2{ }_{0}^{1} \mathrm{n}$
22.76 Element $109\left({ }_{109}^{266} \mathrm{Mt}\right)$ was prepared in 1982 by bombardment of ${ }^{209} \mathrm{Bi}$ atoms with ${ }^{58} \mathrm{Fe}$ atoms. Identify the other product that must have formed, and write a balanced nuclear equation.
22.77 Molybdenum-99 is formed by neutron bombardment of a naturally occurring isotope. If one neutron is absorbed and no by-products are formed, what is the starting isotope?
22.78 Californium-246 is formed by bombardment of uranium- 238 atoms. If four neutrons are formed as byproducts, what particle is used for the bombardment?
22.79 Balance the following transmutation reactions:
(a) ${ }_{96}^{246} \mathrm{Cm}+{ }_{6}^{12} \mathrm{C} \rightarrow$ ? $+4{ }_{0}^{1} \mathrm{n}$
(b) ${ }_{99}^{253} \mathrm{Es}+? \rightarrow{ }_{101}^{256} \mathrm{Md}+{ }_{0}^{1} \mathrm{n}$
(c) ${ }_{98}^{250} \mathrm{Cf}+{ }_{5}^{11} \mathrm{~B} \rightarrow$ ? $+4{ }_{0}^{1} \mathrm{n}$

## General Problems

22.80 How much energy (in $\mathrm{kJ} / \mathrm{mol}$ ) is released during the overall decay of ${ }^{232} \mathrm{Th}$ to ${ }^{208} \mathrm{~Pb}$ (Problem 22.40)? The relevant masses are: ${ }^{232} \mathrm{Th}=232.038054 \mathrm{amu}$; ${ }^{208} \mathrm{~Pb}=207.976627 \mathrm{amu}$; electron $=5.485799 \times 10^{-4}$ $\mathrm{amu} ; \alpha$ particle $=4.001506 \mathrm{amu}$.
22.81 Potassium ion, $\mathrm{K}^{+}$, is present in most foods and is an essential nutrient in the human body. Potassium-40, however, which has a natural abundance of $0.0117 \%$, is radioactive with $t_{1 / 2}=1.28 \times 10^{9}$ years. What is the decay constant of ${ }^{40} \mathrm{~K}$ ? How many ${ }^{40} \mathrm{~K}^{+}$ions are present in 1.00 g of KCl ? How many disintegrations/s does 1.00 g of KCl undergo?
22.82 How much energy (in $\mathrm{kJ} / \mathrm{mol}$ ) is released during the overall decay process shown in Problem 22.22? The atomic mass of $\mathrm{A}=241.056845 \mathrm{amu}$; atomic mass of $\mathrm{E}=233.039628 \mathrm{amu} ;$ electron mass $=5.485799 \times 10^{-4}$ $\mathrm{amu} ; \alpha$ particle mass $=4.001506 \mathrm{amu}$.
22.83 Fraud in science is rare but does happen occasionally. In 1999, the creation of three superheavy elements (one new) was claimed when ${ }^{208} \mathrm{~Pb}$ was bombarded with ${ }^{86} \mathrm{Kr}$. The claim was subsequently found to be fradulent and was withdrawn. Identify the isotopes $\mathrm{X}, \mathrm{Y}$, and Z that were claimed.

$$
{ }_{82}^{208} \mathrm{~Pb}+{ }_{36}^{86} \mathrm{Kr} \xrightarrow{-\mathrm{n}} \mathrm{X} \xrightarrow{-\alpha} \mathrm{Y} \xrightarrow{-\alpha} \mathrm{Z}
$$

22.84 Chlorine- 34 has a half-life of only 1.53 s . How long does it take for $99.99 \%$ of a ${ }^{34} \mathrm{Cl}$ sample to decay?
22.85 The decay constant for ${ }^{20} \mathrm{~F}$ is $0.063 \mathrm{~s}^{-1}$. How long does it take for $99.99 \%$ of a ${ }^{20} \mathrm{~F}$ sample to decay?
22.86 Calculate the mass defect (in $\mathrm{g} / \mathrm{mol}$ ) and the binding energy (in $\mathrm{MeV} /$ nucleon) for the following nuclides. Which of the two is more stable?
(a) ${ }^{50} \mathrm{Cr}$ (atomic mass $=49.94605 \mathrm{amu}$ )
(b) ${ }^{64} \mathrm{Zn}$ (atomic mass $=63.92915 \mathrm{amu}$ )
22.87 What is the age of a bone fragment that shows an average of 2.9 disintegrations/min per gram of carbon? The carbon in living organisms undergoes an average of 15.3 disintegrations/min per gram, and the half-life of ${ }^{14} \mathrm{C}$ is 5730 years.
22.88 How much energy (in $\mathrm{kJ} / \mathrm{mol}$ ) is released in the fusion reaction of ${ }^{2} \mathrm{H}$ with ${ }^{3} \mathrm{He}$ ?

$$
{ }_{1}^{2} \mathrm{H}+{ }_{2}^{3} \mathrm{He} \longrightarrow{ }_{2}^{4} \mathrm{He}+{ }_{1}^{1} \mathrm{H}
$$

The relevant masses are ${ }^{2} \mathrm{H}(2.0141 \mathrm{amu}),{ }^{3} \mathrm{He}(3.0160$ $\mathrm{amu}),{ }^{4} \mathrm{He}(4.0026 \mathrm{amu})$, and ${ }^{1} \mathrm{H}(1.0078 \mathrm{amu})$.
22.89 The longest half-life yet measured for radioactive decay is the double $\beta$ emission of selenium-82, for which $t_{1 / 2}=1.1 \times 10^{20}$ years .

$$
{ }_{34}^{82} \mathrm{Se} \longrightarrow{ }_{36}^{82} \mathrm{Kr}+2{ }_{-1}^{0} \mathrm{e}
$$

How many disintegrations per day occur initially in a 1.0 mol sample of ${ }^{82} \mathrm{Se}$ ?
22.90 The most abundant isotope of uranium,,$^{238} \mathrm{U}$, does not undergo fission. In a breeder reactor, however, a ${ }^{238} \mathrm{U}$ atom captures a neutron and emits two $\beta$ particles to make a fissionable isotope of plutonium, which can then be used as fuel in a nuclear reactor. Write a balanced nuclear equation.
22.91 It has been estimated that $3.9 \times 10^{23} \mathrm{~kJ} / \mathrm{s}$ is radiated into space by the sun. What is the rate of the sun's mass loss in $\mathrm{kg} / \mathrm{s}$ ?
22.92 In a cancer treatment called boron neutron-capture therapy, a drug containing boron-10 is injected into a patient where it selectively binds to cancer cells. Irradiating the affected area with neutrons then induces the following reaction:

$$
{ }^{10} \mathrm{~B}+{ }^{1} \mathrm{n} \longrightarrow{ }^{4} \mathrm{He}+{ }^{7} \mathrm{Li}+\gamma
$$

The $\alpha$ radiation kills the cancer cells, leaving the surrounding tissue unharmed. The reactants in this nuclear process have essentially no kinetic energy, but the products have a total kinetic energy of 2.31 MeV . What is the energy of the $\gamma$ photon released? Relevant masses are: ${ }^{4} \mathrm{He}$ ( 4.002603 amu ), ${ }^{7} \mathrm{Li}(7.016004 \mathrm{amu}),{ }^{10} \mathrm{~B}(10.012937 \mathrm{amu})$, $\mathrm{e}^{-}(0.0005486 \mathrm{amu}), \mathrm{n}(1.008665 \mathrm{amu})$.
22.93 Neptunium-237 decays by a series of steps to bismuth209. How many $\alpha$ and $\beta$ particles are produced by this decay process?
22.94 The radioactive nuclide ${ }^{100} \mathrm{Tc}$ decays to form the stable nuclide ${ }^{100} \mathrm{Mo}$.
(a) There are two possible pathways for this decay. Write balanced equations for both.
(b) Only one of the pathways is observed. Calculate the energy released by both pathways, and explain why only one is observed. Relevant masses are: ${ }^{100} \mathrm{Tc}(99.907657 \mathrm{amu}),{ }^{100} \mathrm{Mo}$ (99.907 48 amu ), $\mathrm{e}^{-}$ ( 0.0005486 amu ).
22.95 The nuclide ${ }^{226} \mathrm{Ac}$ can decay by any of three different nuclear processes: $\alpha$ emission, $\beta$ emission, or electron capture.
(a) Write a balanced nuclear equation for the decay of ${ }^{226} \mathrm{Ac}$ by each decay mode.
(b) For the decay of ${ }^{226} \mathrm{Ac}$ by all processes combined, the first-order rate constant is $k=0.556 \mathrm{~d}^{-1}$. How many days are required for $80.0 \%$ of a sample of ${ }^{226}$ Ac to decay?

## Multi-Concept Problems

22.96 A small sample of wood from an archeological site in Clovis, New Mexico, was burned in $\mathrm{O}_{2}$, and the $\mathrm{CO}_{2}$ produced was bubbled through a solution of $\mathrm{Ba}(\mathrm{OH})_{2}$ to produce a precipitate of $\mathrm{BaCO}_{3}$. When the $\mathrm{BaCO}_{3}$ was collected by filtration, a 1.000 g sample was found to have a radioactivity of $4.0 \times 10^{-3} \mathrm{~Bq}$. The half-life of ${ }^{14} \mathrm{C}$ is 5730 y , and living organisms have a radioactivity due to ${ }^{14} \mathrm{C}$ of 15.3 disintegrations/min per gram of carbon. What is the age of the Clovis site?
22.97 Polonium-210, a naturally occurring radioisotope, is an $\alpha$ emitter, with $t_{1 / 2}=138 \mathrm{~d}$. Assume that a sample of ${ }^{210}$ Po with a mass of 0.700 mg was placed in a 250.0 mL flask, which was evacuated, sealed, and allowed to sit undisturbed. What would the pressure be inside the flask (in mm Hg ) at $20^{\circ} \mathrm{C}$ after 365 days if all the $\alpha$ particles emitted had become helium atoms?
22.98 A blood-volume determination was carried out on a patient by injection with 20.0 mL of blood that had been radioactively labeled with Cr -51 to an activity of $4.10 \mu \mathrm{Ci} / \mathrm{mL}$. After a brief period to allow for mixing in the body, blood was drawn from the patient for analysis. Unfortunately, a mix-up in the laboratory prevented an immediate analysis, and it was not until 17.0 days later that a scintillation measurement on the blood was made. The radiation level was then determined to be $0.00935 \mu \mathrm{Ci} / \mathrm{mL}$. If ${ }^{51} \mathrm{Cr}$ has $t_{1 / 2}=27.7$ days, what is the volume of blood in the patient?
22.99 Imagine that you have a 0.00750 M aqueous $\mathrm{MgCl}_{2}$ solution, prepared so that it contains a small amount of radioactive ${ }^{28} \mathrm{Mg}$. The half-life of ${ }^{28} \mathrm{Mg}$ is 20.91 h , and the initial activity of the $\mathrm{MgCl}_{2}$ solution is $0.112 \mu \mathrm{Ci} / \mathrm{mL}$. Assume that 20.00 mL of this $\mathrm{MgCl}_{2}$ solution is added to 15.00 mL of 0.01250 M aqueous $\mathrm{Na}_{2} \mathrm{CO}_{3}$ solution and that the resultant precipitate is then removed by filtration to give a clear filtrate. After a long break to go for a run, you find that the activity of the filtrate measured 2.40 h after beginning the experiment is $0.029 \mu \mathrm{Ci} / \mathrm{mL}$. What are the molar concentrations of $\mathrm{Mg}^{2+}$ and $\mathrm{CO}_{3}{ }^{2-}$ in the filtrate, and what is the solubility product constant of $\mathrm{MgCO}_{3}$ ?

## eMedia Problems

22.100 The following questions refer to the Half-Life activity in eChapter 22.3.
(a) How many half-lives are required for $96.875 \%$ of a sample to decompose?
(b) Assuming that each line on the $x$-axis represents 10.0 minutes, after how much time will $25.0 \%$ of the original sample remain?
(c) Assuming that the original mass of the sample was 13.5 g and that each line on the $x$-axis represents 10.0 minutes, at what time will the mass of the sample be 0.211 g ?
22.101 ${ }^{238} \mathrm{U}$ has a half-life of $4.47 \times 10^{9}$ years. Use the Radioactive Decay activity (eChapter 22.3) to determine the half-life of ${ }^{235} \mathrm{U}$. Considering that the atomic mass of uranium is greater than 238, which isotope do you expect to be more abundant in nature? Comment on the apparent relationship between half-life and natural abundance of these two isotopes.
22.102 Determine the half-life of ${ }^{232} \mathrm{Th}$ to 3 significant figures using the Radioactive Decay activity (eChapter 22.3). What percentage of a 20.00 kg sample of ${ }^{232} \mathrm{Th}$ would remain after $5.05 \times 10^{9}$ years?
22.103 Use the Decay Series activity in eChapter 22.4 to write balanced equations for the following decay processes.
(a) The decomposition of ${ }^{230} \mathrm{Th}$ by alpha decay.
(b) The decomposition of ${ }^{234} \mathrm{~Pa}$ by beta decay.
(c) The decomposition of ${ }^{214} \mathrm{Bi}$ to ${ }^{214} \mathrm{Po}$.
(d) The decomposition of ${ }^{210} \mathrm{Po}$ to ${ }^{206} \mathrm{~Pb}$.
22.104 The water in the Nuclear Power Plant Diagram activity (eChapter 22.6) is located in 3 sections of the power plant, and the water in each section is physically separated from water in the other sections. What is the function/purpose of the water in each section? Why must the water be separated?

## Chapter



## Organic Chemistry

## From the very beginning of chemical studies in the mid-1700s, people noticed that substances from plants and animals were more difficult

 to purify and work with than those from minerals. To express this difference, the term organic chemistry was used to mean the study of compounds from living organisms, while inorganic chemistry was used for the study of compounds from nonliving sources. Today we know that there are no fundamentaldifferences between organic

Flamingos owe their color to organic chemicals in their diet. Without these compounds, the feathers eventually turn white.

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■ Interlude-Natural or Synthetic?
and inorganic compounds-the same principles apply to both. The only common characteristic of compounds from living sources is that all contain the element carbon. Thus, organic chemistry is now defined as the study of carbon compounds.

Why is carbon special, and why do chemists still treat organic chemistry as a separate branch of science? The answers to these questions involve the ability of carbon atoms to bond together, forming long chains and rings. Of all the elements, only carbon is able to form such an immense array of compounds, from methane, with one carbon atom, to deoxyribonucleic acid (DNA), with tens of billions of carbon atoms. More than 19 million organic compounds have been made, and thousands of new ones are made each week in chemical laboratories throughout the world.

## 23.1 | The Nature of Organic Molecules

Let's review what we've seen in earlier chapters about organic molecules:

- Carbon is tetravalent (Section 7.5); it has four outer-shell electrons $\left(1 s^{2} 2 s^{2} 2 \boldsymbol{p}^{\mathbf{2}}\right)$ and forms four bonds. In methane, for instance, carbon is bonded to four hydrogen atoms:

- Organic molecules have covalent bonds (Section 7.1). In ethane, for instance, all bonds result from the sharing of two electrons, either between $C$ and $C$ or between C and H :

- Organic molecules have polar covalent bonds when carbon bonds to an element on the right or left side of the periodic table (Section 7.4). In chloromethane, the electronegative chlorine atom attracts electrons more strongly than carbon does, polarizing the $\mathrm{C}-\mathrm{Cl}$ bond so that carbon has a partial positive charge, $\delta+$. In methyllithium, the lithium attracts electrons less strongly than carbon does, polarizing the carbon-lithium bond so that carbon has a partial negative charge, $\delta$-. In electrostatic potential maps, the chloromethane carbon thus appears blue (electron-poor), while the methyllithium carbon appears red (electron-rich).


Chloromethane, $\mathrm{CH}_{3} \mathrm{Cl}$ (electron-poor carbon)


H


Methyllithium, $\mathrm{CH}_{3} \mathrm{Li}$ (electron-rich carbon)

- Carbon can form multiple covalent bonds by sharing more than two electrons with a neighboring atom (Section 7.5). In ethylene, the two carbon atoms share four electrons in a double bond. In acetylene, the two carbons share six electrons in a triple bond:

- Organic molecules have specific three-dimensional shapes, which can be predicted by the VSEPR model (Section 7.9). When carbon is bonded to four atoms, as in methane, the bonds are oriented toward the four corners of a tetrahedron with carbon in the center and with $\mathrm{H}-\mathrm{C}-\mathrm{H}$ angles near 109.5



When carbon bonds to three atoms, as in ethylene, the bonds are at angles of approximately $120^{\circ}$ to one another. When carbon bonds to two atoms, as in acetylene, the bonds are at angles of $180^{\circ}$.



$$
\begin{gathered}
\mathrm{H}-\mathrm{C} \equiv \mathrm{C}-\mathrm{H} \\
\text { Acetylene }\left(180^{\circ} \text { angles }\right)
\end{gathered}
$$

- Carbon uses hybrid atomic orbitals for bonding (Sections 7.11 and 7.12). A carbon that bonds to four atoms uses $s p^{3}$ orbitals, formed by the combination of an atomic $s$ orbital with three atomic $p$ orbitals. These $s p^{3}$ orbitals point toward the corners of a tetrahedron, accounting for the observed geometry of carbon.

Doubly bonded carbons are $s p^{2}$-hybridized. Carbon has three $s p^{2}$ hybrid orbitals, which lie in a plane and point toward the corners of an equilateral triangle, and one unhybridized $p$ orbital, which is oriented at a $90^{\circ}$ angle to the plane of the $s p^{2}$ hybrids. When two $s p^{2}$-hybridized carbon atoms approach each other with $s p^{2}$ orbitals aligned head-on for sigma bonding, the unhybridized $p$ orbitals on each carbon overlap to form a pi bond, resulting in a net carbon-carbon double bond.

Triply bonded carbons are $s p$-hybridized. Carbon has two $s p$ hybrid orbitals, which are $180^{\circ}$ away from each other, and two unhybridized $p$ orbitals, which are oriented $90^{\circ}$ from the $s p$ hybrids and $90^{\circ}$ from each other. When two $s p$-hybridized carbon atoms approach each other with $s p$ orbitals aligned head-on for sigma bonding, the $p$ orbitals on each carbon overlap to form two pi bonds, resulting in a net carbon-carbon triple bond.


For $\sigma$ bond formation carbon uses $s p^{3}$ hybrid orbitals in tetrahedral molecules, $s p^{2}$ hybrid orbitals in trigonal planar molecules, and $s p$ hybrid orbitals in linear molecules. These molecules generally also have zero, one, and two $\pi$ bonds, respectively.

Covalent bonding gives organic compounds properties that are quite different from those of ionic compounds. Intermolecular forces between individual organic molecules are relatively weak, and organic compounds therefore have lower melting and boiling points than do ionic compounds. In fact, many simple organic compounds are liquid at room temperature. In addition, most organic compounds are insoluble in water and don't conduct electricity. Only a few small polar organic molecules such as glucose, acetic acid, and ethyl alcohol dissolve in water.

### 23.2 Alkanes and Their Isomers

Why are there so many organic compounds? The answer is that a relatively small number of atoms can bond together in a great many ways. Take molecules that contain only carbon and hydrogen (hydrocarbons) and have only single bonds. Such compounds belong to the family of organic molecules called saturated hydrocarbons, or alkanes.

The paraffin wax coating that makes these apples so shiny is a mixture of alkanes.


If you imagine ways that one carbon and four hydrogens can combine, only methane, $\mathrm{CH}_{4}$, is possible. If you imagine ways that two carbons and six hydrogens can combine, only ethane, $\mathrm{C}_{2} \mathrm{H}_{6}$, is possible; and if you imagine the combination of three carbons with eight hydrogens, only propane, $\mathrm{C}_{3} \mathrm{H}_{8}$, is possible.

An alkane is a hydrocarbon in which each carbon atom is bonded to four other carbon or hydrogen atoms. Because each carbon atom is bonded to its maximum number of atoms and cannot bond to additional atoms, the alkane is said to be saturated.

Raymond B. Seymour, "Alkanes: Abundant, Pervasive, Important, and Essential," J. Chem. Educ., Vol. 66, 1989, 59-63.



Methane, $\mathrm{CH}_{4}$



Ethane, $\mathrm{C}_{2} \mathrm{H}_{6}$



Propane, $\mathrm{C}_{3} \mathrm{H}_{8}$

When larger numbers of carbons and hydrogens combine, though, more than one structure can result. There are two ways in which molecules with the formula $\mathrm{C}_{4} \mathrm{H}_{10}$ can be formed: Either the four carbons can be in a row, or they can be in a branched arrangement. Similarly, there are three ways in which molecules with the formula $\mathrm{C}_{5} \mathrm{H}_{12}$ can result, and even more ways for larger alkanes. Compounds with all their carbons connected in a row are called straight-chain alkanes, and those with a branching connection of carbons are called branched-chain alkanes.



Compounds like the two different $\mathrm{C}_{4} \mathrm{H}_{10}$ molecules and the three different $\mathrm{C}_{5} \mathrm{H}_{12}$ molecules, which have the same molecular formula but different structures, are called isomers (Section 20.8). The number of possible alkane isomers grows rapidly as the number of carbon atoms increases, from five isomers for $\mathrm{C}_{6} \mathrm{H}_{14}$ to more than $6 \times 10^{13}$ isomers for $\mathrm{C}_{40} \mathrm{H}_{82}$ !

It's important to realize that different isomers are different chemical compounds. They have different structures, different chemical properties, and different physical properties, such as melting point and boiling point. For example, ethyl alcohol (ethanol, or grain alcohol) and dimethyl ether both have the formula $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$, yet ethyl alcohol is a liquid with a boiling point of $78.5^{\circ} \mathrm{C}$, whereas dimethyl ether is a gas with a boiling point of $-23^{\circ} \mathrm{C}$.

A. Haudrechy, "A Simple Method of Drawing Stereoisomers from Complicated Symmetrical Structures," J. Chem. Educ., Vol. 77, 2000, 864-866.
$\mathrm{C}-\mathrm{H}$ and most $\mathrm{C}-\mathrm{C}$ bonds are not shown in condensed structures.



Ethyl alcohol, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$



Dimethyl ether, $\mathrm{C}_{2} \mathrm{H}_{6} \mathrm{O}$

- PROBLEM 23.1 Draw the straight-chain isomer with the formula $\mathrm{C}_{7} \mathrm{H}_{16}$.
- PROBLEM 23.2 Draw the five alkane isomers with the formula $\mathrm{C}_{6} \mathrm{H}_{14}$.


## 23.3 | Drawing Organic Structures

It's both awkward and time-consuming to draw all the bonds and all the atoms in an organic molecule, even for a relatively small one like $\mathrm{C}_{4} \mathrm{H}_{10}$. Thus, a shorthand way of drawing condensed structures is often used. In condensed structures, carbon-hydrogen and most carbon-carbon single bonds aren't shown; rather, they're "understood." If a carbon atom has three hydrogens bonded to it, we write $\mathrm{CH}_{3}$; if the carbon has two hydrogens bonded to it, we write $\mathrm{CH}_{2}$; and so on. For example, the four-carbon, straight-chain alkane (called butane) and its branched-chain isomer (called 2-methylpropane, or isobutane) can be written in the following way:


Note that the horizontal bonds between carbons aren't shown-the $\mathrm{CH}_{3}$ and $\mathrm{CH}_{2}$ units are simply placed next to each other-but the vertical bond in 2-methylpropane is shown for clarity.

## Worked Key Concept Example 23.1

Give the formula of the following compound, and convert the model into a condensed structure:


## Strategy and Solution

The compound has 7 carbons and 16 hydrogens: $\mathrm{C}_{7} \mathrm{H}_{16}$. Its condensed structure is


- PROBLEM 23.3 Draw the three isomers of $\mathrm{C}_{5} \mathrm{H}_{12}$ as condensed structures.
- KEY CONCEPT PROBLEM 23.4 Give the formula of the following molecular model, and convert the model into a condensed structure.



### 23.4 The Shapes of Organic Molecules

The condensed structure of an organic molecule implies nothing about threedimensional shape; it only indicates the connections among atoms. Thus, a molecule can be arbitrarily drawn in many different ways. The branched-chain alkane called 2-methylbutane, for instance, might be represented by any of the following structures. All have four carbons connected in a row, with a $-\mathrm{CH}_{3}$ branch on the second carbon from the end.


$\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right)_{2}$


Some representations of 2-methylbutane
In fact, 2-methylbutane has no one single shape because rotation occurs around carbon-carbon single bonds. The two parts of a molecule joined by a carbon-carbon single bond are free to spin around the bond, giving rise to an infinite number of possible three-dimensional structures. Thus, a large sample of 2-methylbutane contains a great many molecules that are constantly changing their shape. At any given instant, though, most of the molecules have an extended, zigzag shape, which is slightly more stable than other possibilities. The same is true for other alkanes.


An electron-dot structure does not give the shape of a molecule. The shape is defined by applying the VSEPR model to each carbon, nitrogen, and oxygen atom present in the molecule.

3D models of n-Pentane, Isopentane, and Neopentane

Worked Example 23.2
The following condensed structures have the same formula, $\mathrm{C}_{8} \mathrm{H}_{18}$. Which of them represent the same molecule?
(a)

(b)



## Strategy

Pay attention to the order of connection between atoms. Don't get confused by the apparent differences caused by writing a structure right-to-left versus left-to-right.

## Solution

Structure (a) has a straight chain of six carbons with $-\mathrm{CH}_{3}$ branches on the second and fourth carbons from the end. Structure (b) also has a straight chain of six carbons with $-\mathrm{CH}_{3}$ branches on the second and fourth carbons from the end and is therefore identical to (a). The only difference between (a) and (b) is that one is written "forward" and one is written "backward." Structure (c) has a straight chain of six carbons with $-\mathrm{CH}_{3}$ branches on the second and fifth carbons from the end, so it is an isomer of (a) and (b).

- PROBLEM 23.5 Which of the following structures are identical?



-KEY CONCEPT PROBLEM 23.6 Are the following two structures identical?

and



## 23.5 | Naming Alkanes

In earlier times, when relatively few pure organic chemicals were known, new compounds were named at the whim of their discoverer. Thus, urea is a crystalline substance first isolated from urine, and the barbiturates are a group of tranquilizing agents named by their discoverer in honor of his friend Barbara. As more and more compounds became known, however, the need for a systematic method of naming organic compounds became apparent.

The system of naming now used was devised by the International Union of Pure and Applied Chemistry, abbreviated IUPAC. In the IUPAC system, a chemical name has three parts: prefix, parent, and suffix. The parent name tells how many carbon atoms are present in the longest continuous chain; the suffix identifies what family the molecule belongs to; and the prefix (if needed) specifies the location of various substituent groups attached to the parent chain:


Straight-chain alkanes are named by counting the number of carbon atoms in the chain and adding the suffix -ane. With the exception of the first four com-pounds-methane, ethane, propane, and butane-whose names have historical origins, the alkanes are named from Greek numbers according to the number of carbons present. Thus, pentane is the five-carbon alkane, hexane is the six-carbon alkane, and so on, as shown in Table 23.1.

| TABLE 23.1 | Names of Straight-Chain Alkanes |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of <br> Carbons | Structure | Name | Number of <br> Carbons | Structure | Name |
| 1 | $\mathrm{CH}_{4}$ | Methane | 6 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Hexane |
| 2 | $\mathrm{CH}_{3} \mathrm{CH}_{3}$ | Ethane | 7 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Heptane |
| 3 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Propane | 8 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Octane |
| 4 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Butane | 9 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Nonane |
| 5 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Pentane | 10 | $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CH}_{3}$ | Decane |

Branched-chain alkanes are named by following four steps:
Step 1. Name the main chain. Find the longest continuous chain of carbons in the molecule, and use the name of that chain as the parent name. The longest chain may not always be obvious from the manner of writing; you may have to "turn corners" to find it:


Named as hexane, not as a pentane, because the longest chain has six carbons.

If you prefer, you can redraw the structure so that the longest chain is on one line:


Step 2. Number the carbon atoms in the main chain. Beginning at the end nearer the first branch point, number each carbon atom in the parent chain:


Step 3. Identify and number the branching substituent. Assign a number to each branching substituent group on the parent chain according to its point of attachment.


The main chain is a hexane. There is a $-\mathrm{CH}_{3}$ substituent group connected to C 3 of the chain.

If there are two substituent groups on the same carbon, assign the same number to both. There must always be as many numbers in the name as there are substituents.


The main chain is hexane. There are two substituents, a $-\mathrm{CH}_{3}$ and a $-\mathrm{CH}_{2} \mathrm{CH}_{3}$, both connected to C 3 of the chain.

The $-\mathrm{CH}_{3}$ and $-\mathrm{CH}_{2} \mathrm{CH}_{3}$ substituents that branch off the main chain in this compound are called alkyl groups. You can think of an alkyl group as the part of an alkane that remains when a hydrogen is removed. For example, removal of a hydrogen from methane, $\mathrm{CH}_{4}$, gives the methyl group, $-\mathrm{CH}_{3}$, and removal of a hydrogen from ethane, $\mathrm{CH}_{3} \mathrm{CH}_{3}$, gives the ethyl group, $-\mathrm{CH}_{2} \mathrm{CH}_{3}$. Alkyl groups are named by replacing the -ane ending of the parent alkane with an -yl ending.


Methane


A methyl group


Ethane


An ethyl group

Step 4. Write the name as a single word. Use hyphens to separate the different prefixes, and use commas to separate numbers when there are more than one. If two or more different substituent groups are present, list them in alphabetical order. If two or more identical substituents are present, use one of the prefixes di-, tri-, tetra-, and so forth, but don't use these numerical prefixes for alphabetizing purposes. That is, a prefix like "dimethyl" is listed alphabetically under " m " rather than under " $d$ ". Look at the following examples to see how names are written:




3-Methylhexane-a six-carbon main chain with a 3-methyl substituent

3-Ethyl-3-methylhexane-a six-carbon main chain with 3-ethyl and 3-methyl substituents

3,3-Dimethylhexane-a six-carbon main chain with two 3-methyl substituents

## More About Alkyl Groups

It doesn't matter which hydrogen is removed from $\mathrm{CH}_{4}$ to form a methyl group or which hydrogen is removed from $\mathrm{CH}_{3} \mathrm{CH}_{3}$ to form an ethyl group because all the hydrogen atoms in each molecule are equivalent. The eight hydrogens in $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{3}$, however, are not all equivalent. Propane has two "kinds" of hydro-gens-six on the end carbons and two on the middle carbon. Depending on which kind of hydrogen is removed, two different propyl groups result. Removing one of the six hydrogens attached to an end carbon yields a straight-chain group called propyl, and removing one of the two hydrogens attached to the middle carbon yields a branched-chain group called isopropyl.

Similarly, there are four different kinds of butyl groups. Two (butyl and secbutyl) are derived from straight-chain butane, and two (isobutyl and tert-butyl) are derived from branched-chain isobutane. The prefixes sec- (for secondary) and tert- (for tertiary) refer to the number of other carbon atoms attached to the branching carbon. There are two other carbons attached to the branch point in a sec-butyl group and three other carbons attached to the branch point in a tert-butyl group.


Keep in mind that alkyl groups themselves are not stable compounds and that the "removal" of a hydrogen from an alkane is just a useful way of looking at things, not a chemical reaction. Alkyl groups are simply parts of molecules that help us to name compounds.

## Worked Example 23.3

What is the IUPAC name of the following alkane?


## Strategy

Follow the steps outlined in the text: First, identify and number the longest continuous chain. Then identify the substituents and write the name.

## Solution

The molecule has a chain of eight carbons (octane) with two methyl substituents. Numbering from the end nearer the first methyl substituent indicates that the methyls are at C2 and C6, giving the name 2,6-dimethyloctane. The numbers are separated by a comma and are set off from the rest of the name by a hyphen.


2,6-Dimethyloctane

## Worked Example 23.4

Draw the structure of 3-isopropyl-2-methylhexane.

## Strategy and Solution

First, look at the parent name (hexane) and draw its carbon structure:

$$
\mathrm{C}-\mathrm{C}-\mathrm{C}-\mathrm{C}-\mathrm{C}-\mathrm{C} \text { Hexane }
$$

Next, find the substituents (3-isopropyl and 2-methyl) and place them on the proper carbons:


Finally, add hydrogens to complete the structure:
$\mathrm{CH}_{3} \mathrm{CHCH}_{3}$


- PROBLEM 23.7 What are the IUPAC names of the following alkanes?
(a) The three isomers of $\mathrm{C}_{5} \mathrm{H}_{12}$
(b)




PROBLEM 23.8 Draw condensed structures corresponding to the following IUPAC names:
(a) 3,4-Dimethylnonane
(b) 3-Ethyl-4,4-dimethylheptane
(c) 2,2-Dimethyl-4-propyloctane
(d) 2,2,4-Trimethylpentane
-KEY CONCEPT PROBLEM 23.9 What is the IUPAC name of the following alkane?


### 23.6 Cycloalkanes

The compounds we've been dealing with thus far have all been open-chain, or acyclic, alkanes. Cycloalkanes, which contain rings of carbon atoms, are also well known and are widespread throughout nature. Compounds of all ring sizes from 3 through 30 carbons and beyond have been prepared. The four simplest cycloalkanes having three carbons (cyclopropane), four carbons (cyclobutane), five carbons (cyclopentane), and six carbons (cyclohexane) are shown at the top of the next page.


Even condensed structures are awkward for cyclic molecules, and a streamlined way of drawing structures is often used in which cycloalkanes are represented by polygons. A triangle represents cyclopropane, a square represents cyclobutane, and so on. Carbon and hydrogen atoms aren't shown explicitly in these structures. A carbon atom is simply understood to be at every junction of lines, and the proper number of hydrogen atoms needed to give each carbon four bonds is supplied mentally. Methylcyclohexane, for instance, looks like this:


As you might expect, the $\mathrm{C}-\mathrm{C}$ bonds in cyclopropane and cyclobutane are considerably distorted from the ideal $109.5^{\circ}$ value. Cyclopropane, for example, has the shape of an equilateral triangle, with $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angles of $60^{\circ}$. As a result, the bonds in threeand four-membered rings are weaker than normal, and the molecules are more reactive than other alkanes. Cyclopentane, cyclohexane, and larger cycloalkanes, however, pucker into shapes that allow bond angles to be near their normal tetrahedral value, as shown in the computer-generated models at the beginning of this section.

Substituted cycloalkanes are named using the cycloalkane as the parent name and identifying the positions on the ring where substituents are attached. Start numbering at the group that has alphabetical priority, and proceed in the direction that gives the second substituent the lower possible number. For example,


1-Ethyl-3-methylcyclohexane

Not 1-methyl-3-ethylcyclohexane or 1-ethyl-5-methylcyclohexane or 1-methyl-5-ethylcyclohexane

## Worked Example 23.5

What is the IUPAC name of the following cycloalkane?

-
Although cycloalkanes are usually drawn as planar polygons, most are not planar but puckered.

and Cyclohexane

## Strategy

First, identify the parent cycloalkane (cyclopentane) and the two substituents (a methyl group and an isopropyl group). Then, number the ring beginning at the group having alphabetical priority (isopropyl rather than methyl), and proceed in a direction that gives the second group the lower possible number.

## Solution



- PROBLEM 23.10 Give IUPAC names for the following cycloalkanes:
(a)

(b)

(c)

- PROBLEM 23.11 Draw structures corresponding to the following IUPAC names. Use polygons for the rings.
(a) 1,1-Dimethylcyclobutane
(b) 1-tert-Butyl-2-methylcyclopentane
(c) 1,3,5-Trimethylcycloheptane


## 23.7 | Reactions of Alkanes

Alkanes have relatively low chemical reactivity and are inert to acids, bases, and most other common laboratory reagents. They do, however, react with oxygen and with halogens under appropriate conditions. The chemical reaction of alkanes with oxygen occurs during combustion in an engine or furnace when the alkane is burned as fuel. Carbon dioxide and water are formed as products, and a large amount of heat is released. For example, methane, the main component of natural gas, reacts with oxygen to release 890 kJ per mole of methane burned:

$$
\mathrm{CH}_{4}(g)+2 \mathrm{O}_{2}(g) \longrightarrow \mathrm{CO}_{2}(g)+2 \mathrm{H}_{2} \mathrm{O}(l) \quad \Delta H^{\circ}=-890 \mathrm{~kJ}
$$

Propane (the LP gas used in campers and rural homes), gasoline (a mixture of $\mathrm{C}_{5}-\mathrm{C}_{11}$ alkanes), kerosene (a mixture of $\mathrm{C}_{11}-\mathrm{C}_{14}$ alkanes), and other alkanes burn similarly.

Methane gas is burned off from these oil wells.


The reaction of alkanes with $\mathrm{Cl}_{2}$ or $\mathrm{Br}_{2}$ occurs when a mixture of the two reactants is irradiated with ultraviolet light, denoted by $h \nu$. Depending on the relative amounts of the two reactants and on the time allowed for the reaction, a
sequential substitution of the alkane hydrogen atoms by halogen occurs, leading to a mixture of halogenated products. Methane, for example, reacts with chlorine to yield a mixture of chloromethane $\left(\mathrm{CH}_{3} \mathrm{Cl}\right)$, dichloromethane (methylene chloride; $\mathrm{CH}_{2} \mathrm{Cl}_{2}$ ), trichloromethane (chloroform; $\mathrm{CHCl}_{3}$ ), and tetrachloromethane (carbon tetrachloride; $\mathrm{CCl}_{4}$ ):


- PROBLEM 23.12 Draw all the monochloro substitution products $\left(\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{Cl}\right)$ you would expect to obtain from chlorination of 2-methylbutane.


### 23.8 Families of Organic Molecules: <br> Functional Groups

Chemists have learned through experience that organic compounds can be classified into families according to their structural features and that the chemical behavior of family members is often predictable. The structural features that make it possible to class compounds together are called functional groups. A functional group is an atom or group of atoms within a molecule that has a characteristic chemical behavior. A given functional group undergoes the same kinds of reactions in every molecule it's a part of. Look at the carbon-carbon double-bond functional group, for example. Ethylene $\left(\mathrm{C}_{2} \mathrm{H}_{4}\right)$, the simplest compound with a double bond, undergoes reactions that are remarkably similar to those of menthene $\left(\mathrm{C}_{10} \mathrm{H}_{16}\right)$, a much larger and more complex molecule. Both, for example, react with $\mathrm{Br}_{2}$ to give products in which a Br atom has added to each of the double-bond carbons (Figure 23.1).


- FIGURE 23.1 The reactions of ethylene and menthene with bromine. In both molecules, electrostatic potential maps show similar polarity patterns for the carbon-carbon double bond functional group. Bromine therefore reacts with both in the same way, regardless of the size and complexity of the remainder of the molecule.





The example shown in Figure 23.1 is typical: The chemistry of an organic molecule, regardless of its size and complexity, is largely determined by the functional groups it contains. Table 23.2 lists some of the most common functional groups and gives

TABLE 23.1 Some Important Families of Organic Molecules

| Family Name | Functional Group Structure | Simple Example | Name | Name Ending |
| :---: | :---: | :---: | :---: | :---: |
| Alkane | (contains only $\mathrm{C}-\mathrm{H}$ and C - C single bonds) | $\mathrm{CH}_{3} \mathrm{CH}_{3}$ | Ethane | -ane |
| Alkene |  | $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}$ | Ethene <br> (Ethylene) | -ene |
| Alkyne | $-\mathrm{C} \equiv \mathrm{C}-$ | $\mathrm{H}-\mathrm{C} \equiv \mathrm{C}-\mathrm{H}$ | Ethyne <br> (Acetylene) | -yne |
| Arene (aromatic) |  |  | Benzene | None |
| Alcohol |  | $\mathrm{CH}_{3} \mathrm{OH}$ | Methanol | -ol |
| Ether |  | $\mathrm{CH}_{3} \mathrm{OCH}_{3}$ | Dimethyl ether | ether |
| Amine |  | $\mathrm{CH}_{3} \mathrm{NH}_{2}$ | Methylamine | -amine |
| Aldehyde |  |  | Ethanal (Acetaldehyde) | -al |
| Ketone |  |  | Propanone (Acetone) | -one |
| Carboxylic acid |  |  | Ethanoic acid (Acetic acid) | -oic acid |
| Ester |  |  | Methyl ethanoate (Methyl acetate) | -oate |
| Amide |  |  | Ethanamide (Acetamide) | -amide |

[^25]examples of their occurrence. Some functional groups, such as alkenes, alkynes, and aromatic rings, have only carbon-carbon double or triple bonds; others contain single bonds to oxygen, nitrogen, or halogen atoms; and still others have carbon-oxygen double bonds.

- PROBLEM 23.13 Locate and identify the functional groups in the following molecules:
(a) Lactic acid, from sour milk
(b) Styrene, used to make polystyrene


- PROBLEM 23.14 Propose structures for molecules that fit the following descriptions:
(a) $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}$, containing an aldehyde functional group
(b) $\mathrm{C}_{3} \mathrm{H}_{6} \mathrm{O}_{2}$, containing a carboxylic acid functional group


## 23.9 | Alkenes and Alkynes

In contrast to alkanes, which have only single bonds, alkenes and alkynes have multiple bonds: Alkenes are hydrocarbons that contain a carbon-carbon double bond, and alkynes are hydrocarbons that contain a carbon-carbon triple bond. Both groups of compounds are unsaturated, meaning that they have fewer hydrogens per carbon than the related alkanes. Ethylene $\left(\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}\right)$, for example, has the formula $\mathrm{C}_{2} \mathrm{H}_{4}$, whereas ethane $\left(\mathrm{CH}_{3} \mathrm{CH}_{3}\right)$ has the formula $\mathrm{C}_{2} \mathrm{H}_{6}$.

Alkenes are named by counting the longest chain of carbons that contains the double bond and adding the suffix -ene. Thus, ethylene, the simplest alkene, is followed by propene, butene, pentene, hexene, and so on. Note that ethylene should properly be called ethene, but the name ethylene has been used for so long that it is universally accepted. Similarly, the name propylene is often used for propene.


3D models of Ethane, Ethene, Ethyne, Benzene, Ethanol, Dimethyl Ether, Ethylamine, Ethanal, Diethyl Ketone, Ethanoic Acid, Ethyl Acetate, and Acetamide

To emphasize the role of a functional group in the chemistry of a molecule, it is sometimes useful to represent nonreacting portions of the molecule with the letter R. For example, both $\mathrm{CH}_{3} \mathrm{OH}$ and $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}$ are represented by the general formula ROH , because the chemistry of both depends primarily on the -OH group and little or not at all on the nature of $R$.

Isomers are possible for butene and higher alkenes, depending on the position of the double bond in the chain, which must be specified by a numerical prefix. Numbering starts from the chain end nearer the double bond, and only the first of the double-bond carbons is cited. If a substituent is present on the chain, its identity is noted and its position of attachment is given. If the double bond is

3D models of cisand trans-2-Butene

In an alkene, the doublebonded carbon atoms and atoms attached to them all lie in the same plane.


FIGURE 23.2 Rotation around a carbon-carbon double bond requires a large amount of energy because $p$ orbital overlap is destroyed. Cis-trans alkene isomers are stable and do not interchange as a result of this barrier to rotation.
equidistant from both ends of the chain, numbering starts from the end nearer the substituent.

(numbered to give double bond the lower number)

(numbered to give substituent the lower number when the double bond is equidistant from both ends)

In addition to the alkene isomers that exist because of double-bond position, alkene isomers can also exist because of double-bond geometry. For instance, there are two geometrical, or cis-trans isomers, of 2-butene, which differ in their geometry about the double bond. The cis isomer has its two $-\mathrm{CH}_{3}$ groups on the same side of the double bond, and the trans isomer has its two $-\mathrm{CH}_{3}$ groups on opposite sides. Like other kinds of isomers we've discussed, the individual cis and trans isomers of an alkene are different substances with different physical properties and different (although often similar) chemical behavior. cis-2-Butene boils at $4^{\circ} \mathrm{C}$, for example, but trans-2butene boils at $0.9^{\circ} \mathrm{C}$.

cis-2-Butene (methyl groups on the same side)

(Top view)

(Top view)


(Side view)

trans-2-Butene (methyl groups on opposite sides)

(Side view)

Cis-trans isomerism in alkenes arises because the electronic structure of the carbon-carbon double bond makes bond rotation energetically unfavorable at normal temperatures. Were it to occur, rotation would break the pi part of the double bond by disrupting the sideways overlap of two parallel $p$ orbitals (Figure 23.2). In fact, an energy input of $240 \mathrm{~kJ} / \mathrm{mol}$ is needed to cause bond rotation.


Alkynes are similar in many respects to alkenes and are named using the suffix -yne. The simplest alkyne, $\mathrm{HC} \equiv \mathrm{CH}$, is often called by its alternative name acetylene rather than by its systematic name ethyne.


As with alkenes, isomers are possible for butyne and higher alkynes, depending on the position of the triple bond in the chain. Unlike the alkenes, however, no cis-trans isomers are possible for alkynes because of their linear geometry.

## Worked Example 23.6

Draw the structure of cis-3-heptene.

## Strategy

The name 3-heptene indicates that the molecule has seven carbons (hept-) and has a double bond between carbons 3 and 4 . The prefix cis- indicates that the two alkyl groups attached to the double-bond carbons lie on the same side of the double bond.

## Solution



- PROBLEM 23.15 Give IUPAC names for the following alkenes and alkynes:
(a)

(b)

(c)

- PROBLEM 23.16 Draw structures corresponding to the following IUPAC names:
(a) 2,2-Dimethyl-3-hexene
(b) 4-Isopropyl-2-heptyne
(c) trans-3-Heptene


### 23.10 Reactions of Alkenes and Alkynes

The most important transformations of alkenes and alkynes are addition reactions. That is, a reagent we might write in a general way as $\mathrm{X}-\mathrm{Y}$ adds to the multiple bond of the unsaturated reactant to yield a saturated product. Alkenes and alkynes react similarly, but we'll look only at alkenes because they're more common.


## An addition reaction

Addition of Hydrogen Alkenes react with hydrogen gas in the presence of a platinum or palladium catalyst to yield the corresponding alkane product. For example,

Testing for Unsaturated Hydrocarbons with Bromine movie

This addition of hydrogen to an alkene, often called hydrogenation, is used commercially to convert unsaturated vegetable oils to the saturated fats used in margarine and cooking fats.


Addition of $\mathrm{Cl}_{2}$ and $\mathrm{Br}_{2}$ Alkenes react with the halogens $\mathrm{Cl}_{2}$ and $\mathrm{Br}_{2}$ to give dihaloalkane addition products, a process called halogenation. For example,


Approximately 10 million tons of 1,2-dichloroethane are manufactured each year in the United States by the reaction of ethylene with chlorine. The process is the first step in making PVC [poly(vinyl chloride)] plastics.
Addition of Water Alkenes don't react with pure water, but in the presence of a strong acid catalyst such as sulfuric acid, a hydration reaction takes place to yield an alcohol. An -H from water adds to one carbon, and an -OH adds to the other. For example, nearly 300 million gallons of ethyl alcohol (ethanol) are produced each year in the United States by the acid-catalyzed addition of water to ethylene:


- PROBLEM 23.17 Show the products of the reaction of 2-butene with the following:
(a) $\mathrm{H}_{2}, \mathrm{Pd}$ catalyst
(b) $\mathrm{Br}_{2}$
(c) $\mathrm{H}_{2} \mathrm{O}, \mathrm{H}_{2} \mathrm{SO}_{4}$ catalyst
- PROBLEM 23.18 The reaction of 2-pentene with $\mathrm{H}_{2} \mathrm{O}$ in the presence of $\mathrm{H}_{2} \mathrm{SO}_{4}$ yields a mixture of two alcohol products. Draw their structures.
- KEY CONCEPT PROBLEM 23.19 Draw the structure of the alcohol you would expect to obtain by acid-catalyzed reaction of the following cyclic alkene with $\mathrm{H}_{2} \mathrm{O}$ :



### 23.11 Aromatic Compounds and Their Reactions

In the early days of organic chemistry, the word aromatic was used to describe certain fragrant substances from fruits, trees, and other natural sources. Chemists soon realized, however, that substances grouped as aromatic behaved in a chemically different manner from most other organic compounds. Today, the term aromatic refers to the class of compounds that can be represented as having a sixmembered ring with three double bonds. Benzene is the simplest aromatic compound, but aspirin, the steroid sex hormone estradiol, and many other important compounds also contain aromatic rings.

( -
Benzene is a flat, symmetrical molecule that is often represented as a sixmembered ring with three double bonds. The problem with this representation, however, is that it gives the wrong impression about benzene's chemical reactivity. Because benzene appears to have three double bonds, we might expect it to react with $\mathrm{H}_{2}, \mathrm{Br}_{2}$, and $\mathrm{H}_{2} \mathrm{O}$ to give the same kinds of addition products that alkenes do. In fact, though, benzene and other aromatic compounds are much less reactive than alkenes and don't normally undergo addition reactions.

Benzene's relative lack of reactivity is a consequence of its electronic structure. As shown by the orbital picture in Figure 23.3b, each of the six carbons in benzene is $s p^{2}$-hybridized and has a $p$ orbital perpendicular to the ring. When these $p$ orbitals overlap to form pi bonds, there are two possibilities, shown in Figure 23.3c.

(a)

(b)

(c)

Neither of the two equivalent structures in Figure 23.3c is correct by itself. Rather, each represents one resonance form of the true benzene structure, which is a resonance hybrid of the two. (For a review of resonance, you might want to reread Section 7.7). Benzene is stable because its six pi electrons are spread equally around the entire ring. The six electrons aren't confined to specific double bonds in the normal way, so benzene doesn't react to give addition products in the normal way. Such an idea is hard to show using lines for covalent bonds, so chemists sometimes represent the six electrons as a circle inside the six-membered ring. In this book, though, we'll indicate aromatic rings by showing just one of the individual resonance structures because it's easier to keep track of electrons that way.


Benzaldehyde, a close structural relative of benzene, is an aromatic compound responsible for the odor of cherries.
© FIGURE 23.3 Some representations of benzene: (a) an electrostatic potential map; (b) an orbital picture; and (c) two equivalent resonance structures, which differ only in the positions of the double bonds.


Aromatic compounds undergo substitution reactions, whereas alkenes undergo addition reactions.

© The dyes used to add the bright colors to clothing are made by a process that begins with an aromatic nitration reaction.

Substituted aromatic compounds are named using the suffix -benzene. Thus, $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{Br}$ is bromobenzene, $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CH}_{3}$ is methylbenzene (also called toluene), $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NO}_{2}$ is nitrobenzene, and so on. Disubstituted aromatic compounds are named using one of the prefixes ortho-, meta-, or para-. An ortho- or o-disubstituted benzene has its two substituents in a 1,2 relationship on the ring; a meta- or $m$ disubstituted benzene has its two substituents in a 1,3 relationship; and a para- or $p$-disubstituted benzene has its substituents in a 1,4 relationship. When the benzene ring itself is a substituent, the name phenyl (pronounced fen-nil) is used.


Unlike alkenes, which undergo addition reactions, aromatic compounds usually undergo substitution reactions. That is, a group Y substitutes for one of the hydrogen atoms on the aromatic ring without changing the ring itself. It doesn't matter which of the six ring hydrogens in benzene is replaced, because all six are equivalent.


Nitration Substitution of a nitro group $\left(-\mathrm{NO}_{2}\right)$ for a ring hydrogen occurs when benzene reacts with nitric acid in the presence of sulfuric acid as catalyst. Nitration of aromatic rings is a key step in the synthesis of explosives such as TNT (trinitrotoluene) and many important pharmaceutical agents. Nitrobenzene itself is a starting material for preparing many of the brightly colored dyes used in clothing.


Halogenation Substitution of a bromine or chlorine for a ring hydrogen occurs when benzene reacts with $\mathrm{Br}_{2}$ or $\mathrm{Cl}_{2}$ in the presence of $\mathrm{FeBr}_{3}$ or $\mathrm{FeCl}_{3}$ as catalyst. The chlorination of an aromatic ring is a step used in the synthesis of numerous pharmaceutical agents, such as the tranquilizer Valium.




Sulfonation Substitution of a sulfonic acid group $\left(-\mathrm{SO}_{3} \mathrm{H}\right)$ for a ring hydrogen occurs when benzene reacts with concentrated sulfuric acid and sulfur trioxide. Aromatic-ring sulfonation is a key step in the synthesis of such compounds as aspirin and the sulfa-drug family of antibiotics.


- PROBLEM 23.20 Draw structures corresponding to the following names:
(a) $o$-Dibromobenzene
(b) $p$-Chloronitrobenzene
(c) $m$-Diethylbenzene
- PROBLEM 23.21 Write the products from reaction of the following reagents with $p$-dimethylbenzene (also called $p$-xylene):
(a) $\mathrm{Br}_{2}, \mathrm{FeBr}_{3}$
(b) $\mathrm{HNO}_{3}, \mathrm{H}_{2} \mathrm{SO}_{4}$
(c) $\mathrm{SO}_{3}, \mathrm{H}_{2} \mathrm{SO}_{4}$
- PROBLEM 23.22 Reaction of $\mathrm{Br}_{2} / \mathrm{FeBr}_{3}$ with toluene (methylbenzene) can lead to a mixture of three substitution products. Show the structure of each.


### 23.12 Alcohols, Ethers, and Amines

## Alcohols

Alcohols can be viewed either as derivatives of water, in which one of the hydrogens is replaced by an organic substituent, or as derivatives of alkanes, in which one of the hydrogens is replaced by a hydroxyl group ( -OH ).


Like water, alcohols form hydrogen bonds (Section 10.2), which affect many of their chemical and physical properties. Alcohols are generally higher-boiling than alkanes of similar size, and simple alcohols are often soluble in water because of their ability to form hydrogen bonds to the solvent (Figure 23.4).



Nonbonded electrons are usually not shown in condensed structures. Atoms in organic molecules (except hydrogen) generally obey the octet rule, so any atom with fewer than four bonds must have a number of nonbonded electron pairs equal to four minus the number of bonds. For example, the oxygen in an alcohol has $4-2=2$ nonbonded electron pairs.

4 FIGURE 23.4 Alcohols, like water, form intermolecular hydrogen bonds. As a result, alcohols are relatively high boiling and are often soluble in water.
$\underset{3}{\underset{2}{\mathrm{C}_{3}} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{OH}}+{ }^{\text {1-Propanol }}$




2-Methyl-2-propanol

Cyclohexanol

Alcohols are named by identifying the point of attachment of the -OH group to the hydrocarbon chain and using the suffix -ol to replace the terminal -e in the alkane name. Numbering of the chain begins at the end nearer the-OH group. For example,

Alcohols are among the most important and commonly encountered of all organic chemicals. Methanol $\left(\mathrm{CH}_{3} \mathrm{OH}\right)$, the simplest member of the family, was once known as wood alcohol because it was prepared by heating wood in the absence of air. Approximately 1.6 billion gallons of methanol are manufactured each year in the United States by catalytic reduction of carbon monoxide with hydrogen gas:

$$
\mathrm{CO}+2 \mathrm{H}_{2} \frac{400^{\circ} \mathrm{C}}{\mathrm{ZnO} / \mathrm{Cr}_{2} \mathrm{O}_{3} \text { catalyst }} \mathrm{CH}_{3} \mathrm{OH}
$$



Although toxic to humans, causing blindness in low doses ( 15 mL ) and death in larger amounts ( $100-200 \mathrm{~mL}$ ), methanol is an important industrial starting material for preparing formaldehyde $\left(\mathrm{CH}_{2} \mathrm{O}\right)$, acetic acid $\left(\mathrm{CH}_{3} \mathrm{CO}_{2} \mathrm{H}\right)$, and other chemicals.

Ethanol $\left(\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OH}\right)$ is one of the oldest known pure organic chemicals. Its production by fermentation of grains and sugars and its subsequent purification by distillation go back at least as far as the twelfth century A.D. Sometimes called grain alcohol, ethanol is the "alcohol" present in all wines (10-13\%), beers (3-5\%), and distilled liquors ( $35-90 \%$ ). Fermentation is carried out by adding yeast to an aqueous sugar solution and allowing enzymes in the yeast to break down carbohydrates into ethanol and $\mathrm{CO}_{2}$ :



Only about 5\% of the ethanol produced industrially comes from fermentation. Most is obtained by acid-catalyzed addition of water to ethylene (Section 23.10).

2-Propanol $\left[\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHOH}\right]$, commonly called isopropyl alcohol or rubbing alcohol, is used primarily as a solvent. It is prepared industrially by addition of water to propene:



Still other important alcohols include 1,2-ethanediol (ethylene glycol), 1,2,3propanetriol (glycerol), and the aromatic compound phenol. Ethylene glycol is the principal constituent of automobile antifreeze, glycerol is used as a moisturizing agent in many foods and cosmetics, and phenol is used for preparing nylon, epoxy adhesives, and heat-setting resins.

$\mathrm{HOCH}_{2} \mathrm{CH}_{2} \mathrm{OH}$

1,2-Ethanediol (Ethylene glycol)


1,2,3-Propanetriol (Glycerol)



Phenol

## Ethers

Ethers can be viewed as derivatives of water in which both hydrogens are replaced by organic substituents. They are fairly inert chemically and so are often used as reaction solvents. Diethyl ether, the most common member of the ether family, was used for many years as a surgical anesthetic agent but has now been replaced by safer nonflammable alternatives.

## $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{OCH}_{2} \mathrm{CH}_{3}$ <br> Diethyl ether



## Amines

Amines are organic derivatives of ammonia in the same way that alcohols and ethers are organic derivatives of water. That is, one or more of the ammonia hydrogens is replaced in amines by an organic substituent. As the following examples indicate, the suffix -amine is used in naming these compounds:


Ammonia


Methylamine




Trimethylamine


Benzeneamine (Aniline)

Like ammonia, amines are bases because they can use the lone pair of electrons on nitrogen to accept $\mathrm{H}^{+}$from an acid and give ammonium salts (Section 15.12). Because they're ionic, ammonium salts are much more soluble in water than are neutral amines. Thus, a water-insoluble amine such as

Glycerol is a good moisturizing agent because it attracts water molecules, which hydrogen bond with glycerol's three -OH groups.
-

-


A The characteristic aroma of ripe fish is due to methylamine, $\mathrm{CH}_{3} \mathrm{NH}_{2}$.

Ethylamine 3D model

FIGURE 23.5 Carbonyl compounds can be classified into two categories. Aldehydes and ketones are less polar, while carboxylic acids, esters, and amides are more polar.
triethylamine dissolves readily in water when converted to its ammonium salt by reaction with HCl .


This increase in water solubility on conversion of an amine to its protonated salt has enormous practical consequences in drug delivery. Many important amine-containing drugs, such as morphine (a painkiller) and tetracycline (an antibiotic), are insoluble in aqueous body fluids and are thus difficult to deliver to the appropriate site within the body. Converting these drugs to their ammonium salts, however, increases their solubility to the point where delivery through the bloodstream becomes possible.

- PROBLEM 23.23 Write the structures of the ammonium salts produced by reaction of the following amines with HCl :


(b)

$$
\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}
$$

### 23.13 Aldehydes and Ketones

Look back at the functional groups listed in Table 23.2 and you'll see that many of them have a carbon-oxygen double bond ( $\mathrm{C}=\mathrm{O}$ ), called a carbonyl group (pronounced car-bo-neel). Carbonyl-containing compounds are everywhere. Carbohydrates, fats, proteins, and nucleic acids all contain carbonyl groups; most pharmaceutical agents contain carbonyl groups; and many of the synthetic polymers used for clothing and other applications contain carbonyl groups.

As shown by the electrostatic potential maps in Figure 23.5, the $\mathrm{C}=\mathrm{O}$ bond in carbonyl compounds is polar because the electronegative oxygen atom attracts electrons from the carbon atom. Nevertheless, some carbonyl compounds are more polar than others because of what else is bonded to the carbonyl carbon atom.

It's useful to classify carbonyl compounds into two categories, based on the nature of the groups bonded to the $\mathrm{C}=\mathrm{O}$ and on the chemical consequences that



Ketone



Carboxylic acid


Ester


Amide
result. In one category are aldehydes and ketones. In the other are carboxylic acids, esters, and amides. In aldehydes and ketones, the carbonyl carbon is bonded to atoms (H and C) that are not strongly electronegative and thus contribute no additional polarity to the molecule. In carboxylic acids, esters, and amides, however, the carbonyl carbon is bonded to an atom ( O or N ) that is strongly electronegative, giving these compounds even greater polarity and greater chemical reactivity (Figure 23.5).

Aldehydes, which have a hydrogen atom bonded to the carbonyl group, and ketones, which have two carbon atoms bonded to the carbonyl group, are used throughout chemistry and biology. For example, an aqueous solution of formaldehyde (properly named methanal) is used under the name formalin as a biological sterilant and preservative. Formaldehyde is also used in the chemical industry as a starting material for the manufacture of the plastics Bakelite and melamine, as a component of the adhesives used to bind plywood, and as a part of the foam insulation used in houses. Note that formaldehyde differs from other aldehydes in having two hydrogens attached to the carbonyl group rather than one. Acetone (properly named propanone) is perhaps the most widely used of all organic solvents. You might have seen cans of acetone sold in paint stores for generalpurpose cleanup work. When naming these groups of compounds, use the suffix -al for aldehydes and use the suffix -one for ketones.

|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Formaldehyde (Methanal) | Acetaldehyde (Ethanal) | Acetone <br> (Propanone) | 2-Butanone | Cyclohexanone |

Aldehyde and ketone functional groups are also present in many biologically important compounds. Glucose and most other sugars contain aldehyde groups, for instance. Testosterone and many other steroid hormones contain ketone groups.


Glucose-a pentahydroxyhexanal


Testosterone-a steroid hormone

The industrial preparation of simple aldehydes and ketones usually involves an oxidation reaction of the related alcohol. Thus, formaldehyde is prepared by oxidation of methanol, and acetone is prepared by oxidation of 2-propanol.


-

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "The Disappearing Coffee Cup," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), p. 98. A polystyrene coffee cup is dissolved in acetone.


Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Making Canned Heat," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 111-112. Stearic acid is saponified to produce a solid fuelcanned heat.

Ellin Doyle, "Trans Fatty Acids," J. Chem. Educ., Vol. 74 1997, 1030-1032.

### 23.14 Carboxylic Acids, Esters, and Amides

Carboxylic acids, esters, and amides have their carbonyl groups bonded to an atom ( O or N ) that strongly attracts electrons. All three families undergo carbonylgroup substitution reactions, in which a group we can represent as $-Y$ substitutes for the $-\mathrm{OH},-\mathrm{OC}$, or -N group of the carbonyl reactant.


A carboxylic acid


An ester




A carbonyl-group substitution reaction

## Carboxylic Acids

Carboxylic acids, which contain the $-\stackrel{\|}{\mathrm{C}}-\mathrm{OH}$ functional group, occur widely throughout the plant and animal kingdoms. Acetic acid (ethanoic acid), for example, is the principal organic constituent of vinegar, and butanoic acid is responsible for the odor of rancid butter. In addition, long-chain carboxylic acids such as stearic acid are components of all animal fats and vegetable oils. Although many carboxylic acids have common names-acetic acid instead of ethanoic acid, for instance-systematic names are derived by replacing the final $-e$ of the corresponding alkane with -oic acid.


Acetic acid (Ethanoic acid)


Butanoic acid


Benzoic acid


As their name implies, carboxylic acids are acidic-they dissociate slightly in aqueous solution to give $\mathrm{H}_{3} \mathrm{O}^{+}$and a carboxylate anion. Carboxylic acids are much weaker than inorganic acids like HCl or $\mathrm{H}_{2} \mathrm{SO}_{4}$, however. The $K_{\mathrm{a}}$ of acetic acid, for example, is $1.78 \times 10^{-5}\left(\mathrm{p} K_{\mathrm{a}}=4.75\right)$, meaning that only about $1 \%$ of acetic acid molecules dissociate in a 1.0 M aqueous solution. Note in the following electrostatic potential map of acetic acid that the acidic-OH hydrogen is positively polarized (blue).


One of the most important chemical transformations of carboxylic acids is their acid-catalyzed reaction with an alcohol to yield an ester. Acetic acid, for example, reacts with ethanol in the presence of $\mathrm{H}_{2} \mathrm{SO}_{4}$ to yield ethyl acetate, a widely used solvent. The reaction is a typical carbonyl-group substitution, with $-\mathrm{OCH}_{2} \mathrm{CH}_{3}$ from the alcohol replacing -OH from the acid.


## Esters

Esters, which contain the $-\stackrel{\text { O }}{\mathrm{C}}-\mathrm{O}-\mathrm{C}$ functional group, have many uses in medicine, industry, and living systems. In medicine, a number of important pharmaceutical agents, including aspirin and the local anesthetic benzocaine, are esters. In industry, polyesters such as Dacron and Mylar are used to make synthetic fibers and films. In nature, many simple esters are responsible for the fragrant odors of fruits and flowers. For example, pentyl acetate is found in bananas, and octyl acetate is found in oranges.
Michele Clarke, Ann Brown, Dianne N. Epp, Mary Gallup, Jeffrey R. Wilson, and Judith A. Wuerthele, "Ester, What's in My Food?" J. Chem. Educ., Vol. 63, 1986, 1050-1051.


Aspirin


Benzocaine



A The odor of these bananas is due to pentyl acetate, a simple ester.

$\sqrt{ }$
This hydrolysis reaction can be considered the reverse of the carbonyl substitution reaction: carboxylic acid + alcohol $\rightarrow$ ester + water.

The most important reaction of esters is their conversion by a carbonyl-group substitution reaction into carboxylic acids. Both in the laboratory and in the body, esters undergo a reaction with water-a hydrolysis-that splits the ester molecule into a carboxylic acid and an alcohol. The net effect is a substitution of -OC by -OH . Although the reaction is slow in pure water, it is catalyzed by both acid and base. Base-catalyzed ester hydrolysis is often called saponification, from the Latin word sapo meaning "soap." Soap, in fact, is a mixture of sodium salts of long-chain carboxylic acids and is produced by hydrolysis with aqueous NaOH of the naturally occurring esters in animal fat.


Since esters are derived from carboxylic acids and alcohols, they are named by first identifying the alcohol-related part and then the acid-related part, using the -ate ending. Ethyl acetate, for example, is the ester derived from ethanol and acetic acid.

## Amides

Amides are compounds with the $-{ }^{\|}-\mathrm{N}$ functional group. Without amides, there would be no life. As we'll see in the next chapter, the amide bond between nitrogen and a carbonyl-group carbon is the fundamental link used by organisms for forming proteins. In addition, some synthetic polymers such as nylon contain amide groups, and important pharmaceutical agents such as acetaminophen, the aspirin substitute found in Tylenol and Excedrin, are amides.


Repeating unit of nylon 66


Acetaminophen

Unlike amines, which also contain nitrogen (Section 23.12), amides are neutral rather than basic. Amides do not act as proton acceptors and do not form ammonium salts when treated with acid. The neighboring carbonyl group causes the unshared pair of electrons on nitrogen to be held tightly, thus preventing the electrons from bonding to $\mathrm{H}^{+}$.

Although better methods are normally used, amides can be prepared by the reaction of a carboxylic acid with ammonia or an amine, just as esters are prepared by the reaction of a carboxylic acid with an alcohol. In both cases, water is a by-product, and the - OH part of the carboxylic acid is replaced. Amides are named by first citing the $N$-alkyl group on the amine part ( $N$ because the group is attached to nitrogen) and then identifying the carboxylic acid part using the -amide ending.


Amides undergo an acid- or base-catalyzed hydrolysis reaction with water in the same way that esters do. Just as an ester yields a carboxylic acid and an alcohol, an amide yields a carboxylic acid and an amine (or ammonia). The net effect is a substitution of -N by -OH . This hydrolysis of amides is the key process that occurs in the stomach during digestion of proteins.


## Worked Example 23.7

Give the systematic names of the following compounds:
(a)

(b)


## Strategy

First identify the alcohol-derived or amine-derived part, and then assign the name.

## Solution

(a) This ester is derived from propyl alcohol and butanoic acid. It's name is propyl butanoate.

(b) This amide is derived from dimethylamine and benzoic acid. It's name is $\mathrm{N}, \mathrm{N}$-dimethylbenzamide.


## Worked Example 23.8

Write the products of the following reactions:
(a)

(b)


## Strategy

The reaction of a carboxylic acid with an alcohol yields an ester plus water, and the reaction of an amide with water yields a carboxylic acid and an amine (or ammonia). Write the reagents to show how $\mathrm{H}_{2} \mathrm{O}$ is removed, and then connect the remaining fragments to complete the substitution reaction.
(a)

(b)


- PROBLEM 23.24 Draw structures corresponding to the following names:

Synthesis of Nylon 610 movie
(a) 4-Methylpentanoic acid
(b) Isopropyl benzoate
(c) N -Ethylpropanamide

PROBLEM 23.25 Write the products of the following reactions:
(a)

(b)


- KEY CONCEPT PROBLEM 23.26 Draw the structure of the ester you would obtain by acid-catalyzed reaction of the following carboxylic acid with 2-propanol:



### 23.15 Synthetic Polymers

Polymers are large molecules formed by the repetitive bonding together of many smaller molecules, called monomers. As we'll see in the next chapter, biological polymers occur throughout nature. Cellulose and starch are polymers built from small sugar monomers, proteins are polymers built from amino acid monomers, and nucleic acids are polymers built from nucleotide monomers. The basic idea is the same, but synthetic polymers are much less complex than biopolymers because the starting monomer units are usually smaller and simpler.

TABLE 23.3 Some Alkene Polymers and Their Uses

| Monomer Name | Structure | Polymer Name | Uses |
| :--- | :--- | :--- | :--- |
| Ethylene | $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}$ | Polyethylene | Packaging, bottles |
| Propylene | $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}-\mathrm{CH}_{3}$ | Polypropylene | Bottles, rope, pails <br> medical tubing |
| Vinyl chloride | $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}-\mathrm{Cl}$ | Poly(vinyl chloride) | Insulation, plastic pipe |
| Styrene | $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}$ | Polystyrene | Foams and molded plastics |
| Acrylonitrile | $\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}-\mathrm{C}=\mathrm{N}$ | Orlon, Acrilan | Fibers, outdoor carpeting |

Many simple alkenes called vinyl monomers undergo polymer-forming (polymerization) reactions: Ethylene yields polyethylene, propylene (propene) yields polypropylene, styrene yields polystyrene, and so forth. The polymer molecules that result may have anywhere from a few hundred to many thousand monomer units incorporated into a long chain. Some commercially important polymers are listed in Table 23.3.

where S represents a substituent, such as $\mathrm{H}, \mathrm{CH}_{3}, \mathrm{Cl}, \mathrm{OH}$, or phenyl
The fundamental process in alkene polymerization is a double-bond addition reaction similar to those discussed in Section 23.10. A species called an initiator, In•, first adds to the double bond of an alkene, yielding a reactive intermediate that in turn adds to a second alkene molecule to produce another reactive intermediate, and so on.


A second kind of polymerization process occurs when molecules with two functional groups react. We've seen, for example, that a carboxylic acid reacts with an amine to yield an amide (Section 23.14). If a molecule with two carboxylic acid groups reacts with a molecule having two amino groups, an initial reaction joins the two molecules together, and further reactions then link more and more

$\Delta$ Climbing ropes are made of Perlon, one of the many varieties of nylon.
molecules together until a giant polyamide chain results. Nylon 66, one of the most important such polymers, is prepared by heating adipic acid (hexanedioic acid) with 1,6 -hexanediamine at $280^{\circ} \mathrm{C}$.


Nylons have many uses, both in engineering applications and in fibers. High impact strength and resistance to abrasion make nylon an excellent material for bearings and gears. High tensile strength makes it suitable as fibers for a range of applications from clothing to mountaineering ropes to carpets.

Just as diacids and diamines react to give polyamides, diacids and dialcohols react to give polyesters. The most industrially important polyester, made from reaction of terephthalic acid (1,4-benzenedicarboxylic acid) with ethylene glycol (1,2ethanediol), is used under the trade name Dacron to make clothing fiber and under the name Mylar to make plastic film and recording tape.


Ethylene glycol
(1,2-Ethanediol)



PROBLEM 23.27 Identify the monomer units used to make the following polymers:
(a)

(b)


## Interlude Natural or Synthetic?

 rior to the development of the chemical industry in the late nineteenth and early twentieth centuries, only substances from natural sources were available for treating our diseases, dying our clothes, cleansing and perfuming our bodies, and so forth. Extracts of the opium poppy, for instance, have been used since the seventeenth century for the relief of pain. The prized purple dye called Tyrian purple, obtained from a Middle Eastern mollusk, has been known since antiquity. Oils distilled from bergamot, sweet bay, rose, and lavender, have been employed for centuries in making perfume.Many of these so-called natural products were first used without any knowledge of their chemical composition. As organic chemistry developed, though, chemists learned how to work out the structures of the compounds in natural products. The disease-curing properties of limes and other citrus fruits, for example, were known for centuries but the chemical structure of vitamin C, the active ingredient, was not determined until 1933. Today there is a revival of interest in folk remedies, and a large effort is being made to identify medicinally important chemical compounds found in plants.


Once a structure is known, organic chemists try to synthesize the compound in the laboratory. If the starting materials are inexpensive and the synthesis process is simple enough, it may become more economical to manufacture a compound than to isolate it from a plant or bacterium. In the case of vitamin C , a complete synthesis was achieved in 1933, and it is now much cheaper to synthesize it from glucose than to extract it from citrus or other natural sources. Worldwide, more than 80 million pounds are synthesized each year.

But is the "synthetic" vitamin C as good as the "natural" one? Some people still demand vitamins only from natural sources, assuming that natural is somehow better. Although eating an orange is probably better than taking a tablet, the difference lies in the many other substances present in the orange. The vitamin C itself is exactly the same, just as the NaCl produced by reacting sodium and chlorine in the laboratory is exactly the same as the NaCl found in the ocean. Natural and synthetic compounds are identical in all ways; neither is better than the other.

- PROBLEM 23.28 Identify the functional groups present in vitamin C.

Organic chemistry is the study of carbon compounds. The more than 19 million known organic compounds can be organized into families according to the functional groups they contain. A functional group is an atom or group of atoms within a molecule that has characteristic chemical behavior and undergoes the same kinds of reactions in every molecule it's a part of.

The simplest compounds are the saturated hydrocarbons, or alkanes, which contain only carbon and hydrogen and have only single bonds. Straight-chain alkanes have all their carbons connected in a row, branched-chain alkanes have a branched connection of atoms in their chain, and cycloalkanes have a ring of carbon atoms. Isomerism is possible in alkanes having four or more carbons. Straight-chain alkanes are named in the IUPAC system by adding the family ending -ane to the Greek number that tells how many carbon atoms are present. Branched-chain alkanes are named by identifying the longest continuous chain of carbon atoms and then telling what alkyl groups are present as branches off the main chain. Alkanes are chemically rather inert, although they undergo combustion with oxygen and undergo a substitution reaction with chlorine.

Alkenes are hydrocarbons that contain a carbon-carbon double bond, and alkynes are hydrocarbons that contain a carbon-carbon triple bond. Cis-trans isomers are possible for substituted alkenes because of the lack of rotation about the carbon-carbon double bond. The cis isomer has two substituents on the same side of the double bond, and the trans isomer has two substituents on opposite sides. The most
important transformations of alkenes and alkynes are addition reactions, in which a substance adds to the multiple bond to yield a saturated product.

Aromatic compounds are often represented as having a six-membered ring with three double bonds. These compounds usually undergo substitution reactions, in which a group substitutes for one of the hydrogen atoms on the aromatic ring. Alcohols and ethers can be thought of as derivatives of water in which one or both of the hydrogens are replaced by an organic substituent. Similarly, amines are derivatives of ammonia in which one or more of the ammonia hydrogens are replaced by an organic substituent. Amines are bases and can be protonated by acids to yield ammonium salts.

Compounds that contain a carbonyl group, $\mathrm{C}=\mathrm{O}$, can be classified into two categories: In aldehydes and ketones, the carbonyl-group carbon is bonded to atoms (H and C) that don't attract electrons strongly. In carboxylic acids, esters, and amides, the carbonyl-group carbon is bonded to an atom ( O or N ) that does attract electrons strongly. As a result, these three families of compounds undergo carbonylgroup substitution reactions, in which a group $-Y$ substitutes for the $-\mathrm{OH},-\mathrm{OC}$, or -N group of the carbonyl reactant.

Polymers are large molecules formed when many smaller monomers bond together. Alkene polymers such as polyethylene result from the polymerization of simple alkenes. Nylons and polyesters result from the sequential reaction of two difunctional molecules.

## Key Words

addition reaction 1003
alcohol 1007
aldehyde 1011
alkane 988
alkene 1001
alkyl group 994
alkyne 1001
amide 1014
amine 1009
aromatic 1005

## branched-chain alkane

 989carbonyl group 1010
carboxylate anion 1012
carboxylic acid 1012
cis-trans isomers 1002
condensed structure 990
cycloalkane 996
ester 1013
ether 1009
functional group 999
halogenation 1004
hydration 1004
hydrocarbon 988
hydrogenation 1004
ketone 1011
monomer 1016
organic chemistry 986
polymer 1016
saturated hydrocarbon 988
straight-chain alkane 989
substitution reaction
1006
unsaturated 1001
vinyl monomer 1017

Key Concept Summary


## Understanding Key Concepts

Problems 23.1-23.28 appear within the chapter.
23.29 Convert the following model into a condensed structure, and draw the structures of two isomeric compounds.

23.30 Convert each of the following models into a condensed formula:

(a)

(b)
23.31 Convert each of the following models into a chemical structure:

(a)

(b)
23.32 Identify the functional groups in each of the following compounds:

(a)

(b)
23.33 Give systematic names for the following compounds:
-

(a)

(b)
23.34 The following structure represents a segment of an alkene polymer. Identify the monomer from which the polymer was made.

23.35 Identify the carboxylic acid and alcohol from which the following ester was made:
-

23.36 Draw two isomers of the following compound:

23.37 Draw three resonance forms for naphthalene, showing the positions of the double bonds.


## Additional Problems

## Functional Groups and Isomers

23.38 What are functional groups, and why are they important?
23.39 Describe the structure of the functional group in each of the following families:
(a) Alkene
(b) Alcohol
(c) Ester
(d) Amine
23.40 Propose structures for molecules that meet the following descriptions:
(a) A ketone with the formula $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}$
(b) An ester with the formula $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$
(c) A compound with formula $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NO}_{2}$ that is both an amine and a carboxylic acid
23.41 Write structures for each of the following molecular formulas. You may have to use rings and/or multiple bonds in some instances.
(a) $\mathrm{C}_{2} \mathrm{H}_{7} \mathrm{~N}$
(b) $\mathrm{C}_{4} \mathrm{H}_{8}$
(c) $\mathrm{C}_{2} \mathrm{H}_{4} \mathrm{O}$
(d) $\mathrm{CH}_{2} \mathrm{O}_{2}$
23.42 There are three isomers with the formula $\mathrm{C}_{3} \mathrm{H}_{8} \mathrm{O}$. Draw their structures.
23.43 Write as many isomers as you can that fit the following descriptions:
(a) Alcohols with formula $\mathrm{C}_{4} \mathrm{H}_{10} \mathrm{O}$
(b) Amines with formula $\mathrm{C}_{3} \mathrm{H}_{9} \mathrm{~N}$
(c) Ketones with formula $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}$
(d) Aldehydes with formula $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}$
23.44 Identify the functional groups in the following (O) molecules:
(a)

(b)


Estrone, a female sex hormone
23.45 Identify the functional groups in cocaine.
(O)


Cocaine

## Alkanes

23.46 What is the difference between a straight-chain alkane and a branched-chain alkane?
23.47 What is the difference between an alkane and an alkyl group?
23.48 What kind of hybrid orbitals does carbon use in forming alkanes?
23.49 Why are alkanes said to be saturated?
23.50 If someone reported the preparation of a compound with the formula $\mathrm{C}_{3} \mathrm{H}_{9}$, most chemists would be skeptical. Why?
23.51 What is wrong with each of the following structures?
(a) $\mathrm{CH}_{3}=\mathrm{CHCH}_{2} \mathrm{CH}_{2} \mathrm{OH}$
(b)

(c) $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{C} \equiv \mathrm{CH}_{2} \mathrm{CH}_{3}$
23.52 What are the IUPAC names of the following alkanes?
(a)

(b)

(c)

(d)

23.53 The following compound, known commonly as isooctane, is used as a reference substance for determining the octane rating of gasoline. What is the IUPAC name of isooctane?

23.54 Write condensed structures for each of the following compounds:
(a) 3-Ethylhexane
(b) 2,2,3-Trimethylpentane
(c) 3-Ethyl-3,4-dimethylheptane
(d) 5-Isopropyl-2-methyloctane
23.55 Draw structures corresponding to the following IUPAC names:
(a) Cyclooctane
(b) 1,1-Dimethylcyclopentane
(c) 1,2,3,4-Tetramethylcyclobutane
(d) 4-Ethyl-1,1-dimethylcyclohexane
23.56 Give IUPAC names for each of the following cycloalkanes:
(a)


b)

23.57 The following names are incorrect. What is wrong with each, and what are the correct names?
(a)


4-Ethyl-4-methylpentane
(b)


5-Ethyl-3-methylhexane
(c)

23.58 Give IUPAC names for each of the five isomers with the formula $\mathrm{C}_{6} \mathrm{H}_{14}$.
23.59 Draw structures and give IUPAC names for the nine isomers of $\mathrm{C}_{7} \mathrm{H}_{16}$.
23.60 Write the formulas of all monochlorinated substitution products that might result from a substitution reaction of the following substances with $\mathrm{Cl}_{2}$ :
(a) Hexane
(b) 3-Methylpentane
(c) Methylcyclohexane
23.61 Which of the following reactions is likely to have a higher yield? Explain.
(a)

(b)


## Alkenes, Alkynes, and Aromatic Compounds

23.62 What kind of hybrid orbitals does carbon use in forming the following?
(a) Double bonds
(b) Triple bonds
(c) Aromatic rings
23.63 Why are alkenes, alkynes, and aromatic compounds said to be unsaturated?
23.64 Not all compounds that smell nice are called "aromatic," and not all compounds called "aromatic" smell nice. Explain.
23.65 What is meant by the term addition reaction?
23.66 Write structural formulas for compounds that meet the following descriptions:
(a) An alkene with five carbons
(b) An alkyne with four carbons
(c) A substituted aromatic compound with eight carbons
23.67 How many dienes (compounds with two double bonds) are there with the formula $\mathrm{C}_{5} \mathrm{H}_{8}$ ? Draw structures of as many as you can.
23.68 Give IUPAC names for the following compounds:
(a)

(b)

(c)

(d)

(e)

23.69 Draw structures corresponding to the following IUPAC names:
(a) cis-2-Hexene
(b) 2-Methyl-3-hexene
(c) 2-Methyl-1,3-butadiene
23.70 Ignoring cis-trans isomers, there are five alkenes with the formula $\mathrm{C}_{5} \mathrm{H}_{10}$. Draw structures for as many as you can, and give their IUPAC names. Which can exist as cis-trans isomers?
23.71 There are three alkynes with the formula $\mathrm{C}_{5} \mathrm{H}_{8}$. Draw and name them.
23.72 Which of the following compounds are capable of cis-trans isomerism?
(a) 1-Hexene
(b) 2-Hexene
(c) 3-Hexene
23.73 Which of the following compounds are capable of cis-trans isomerism?
(a)

(b)

(c) $\mathrm{CH}_{3} \mathrm{CH}=\mathrm{CHCHCH} \mathrm{CH}_{3}$
23.74 Draw structures of the following compounds, indicating the cis or trans geometry of the double bond if necessary:
(a) cis-3-Heptene
(b) cis-4-Methyl-2-pentene
(c) trans-2,5-Dimethyl-3-hexene
23.75 The following names are incorrect by IUPAC rules. Draw the structures represented and give the correct names.
(a) 2-Methyl-4-hexene
(b) 5,5-Dimethyl-3-hexyne
(c) 2-Butyl-1-propene
(d) 1,5-Diethylbenzene
23.76 Why is cis-trans isomerism possible for alkenes but not for alkanes or alkynes?
23.77 Why do you suppose small-ring cycloalkenes such as cyclohexene don't exist as cis-trans isomers?
23.78 Write equations for the reaction of 2,3-dimethyl-2butene with each of the following reagents:
(a) $\mathrm{H}_{2}$ and Pd catalyst
(b) $\mathrm{Br}_{2}$
(c) $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{H}_{2} \mathrm{SO}_{4}$ catalyst
23.79 Write equations for the reaction of 2-methyl-2-butene with the reagents given in Problem 23.78.
23.80 Write equations for the reaction of $p$-dichlorobenzene with the following reagents:
(a) $\mathrm{Br}_{2}$ and $\mathrm{FeBr}_{3}$ catalyst
(b) $\mathrm{HNO}_{3}$ and $\mathrm{H}_{2} \mathrm{SO}_{4}$ catalyst
(c) $\mathrm{H}_{2} \mathrm{SO}_{4}$ and $\mathrm{SO}_{3}$
(d) $\mathrm{Cl}_{2}$ and $\mathrm{FeCl}_{3}$ catalyst
23.81 Benzene and other aromatic compounds don't normally react with hydrogen in the presence of a palladium catalyst. If very high pressures ( 200 atm ) and high temperatures are used, however, benzene will add three molecules of $\mathrm{H}_{2}$ to give an addition product. What is a likely structure for the product?

## Alcohols, Amines, and Carbonyl Compounds

23.82 Draw structures corresponding to the following names:
(a) 2,4-Dimethyl-2-pentanol
(b) 2,2-Dimethylcyclohexanol
(c) 5,5-Diethyl-1-heptanol
(d) 3-Ethyl-3-hexanol
23.83 Draw structures corresponding to the following names:
(a) Propylamine
(b) Diethylamine
(c) N -Methylpropylamine
23.84 Assume that you have samples of quinine (an amine) and menthol (an alcohol). What simple chemical test could you do to distinguish between them?
23.85 Assume that you're given samples of pentanoic acid and methyl butanoate, both of which have the formula $\mathrm{C}_{5} \mathrm{H}_{10} \mathrm{O}_{2}$. Describe how you can tell them apart.
23.86 What is the structural difference between an aldehyde and a ketone?
23.87 How do aldehydes and ketones differ from carboxylic acids, esters, and amides?
23.88 How are industrially important ketones and aldehydes usually prepared?
23.89 What general kind of reaction do carboxylic acids, esters, and amides undergo?
23.90 Identify the kinds of carbonyl groups in the following molecules (aldehyde, amide, ester, or ketone):
(a)

(b) $\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CH}_{2} \mathrm{CHO}$
(c)

(d)

(e)

23.91 Draw and name compounds that meet the following descriptions:
(a) Three different amides with the formula $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{NO}$
(b) Three different esters with the formula $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{2}$
23.92 Write the equation for the dissociation of benzoic acid in water. If the $K_{\mathrm{a}}$ of benzoic acid is $6.5 \times 10^{-5}$, what is its percent dissociation in a 1.0 M solution?
23.93 Assume that you have a sample of acetic acid $\left(\mathrm{p} K_{\mathrm{a}}=4.75\right)$ dissolved in water.
(a) Draw the structure of the major species present in the water solution.
(b) Now assume that aqueous HCl is added to the acetic acid solution until pH 2 is reached. Draw the structure of the major species present.
(c) Finally, assume that aqueous NaOH is added to the acetic acid solution until pH 12 is reached. Draw the structure of the major species present.
23.94 Give the IUPAC names of the following compounds:
(a)

(b)

(c)

23.95 Give the IUPAC names of the following compounds:
(a)

(b)

(c)

23.96 Draw structures corresponding to the following IUPAC names:
(a) Methyl pentanoate
(b) Isopropyl 2-methylbutanoate
(c) Cyclohexyl acetate
23.97 Draw structures corresponding to the following IUPAC names:
(a) 3-Methylpentanamide
(b) N-Phenylacetamide
(c) N -Ethyl- N -methylbenzamide
23.98 Write equations showing how you could prepare each of the esters in Problem 23.96 from the appropriate alcohols and carboxylic acids.
23.99 Write equations showing how you could prepare each of the amides in Problem 23.97 from the appropriate amines and carboxylic acids.
23.100 Novocaine, a local anesthetic, has the following structure. Identify the functional groups present in novocaine, and show the structures of the alcohol and carboxylic acid you would use to prepare it.


Novocaine
23.101 Ordinary soap is a mixture of the sodium or potassium salts of long-chain carboxylic acids that arise from saponification of animal fat. Draw the structures of soap molecules produced in the following reaction:


## Polymers

23.102 What is the difference between a monomer and a polymer?
23.103 What is the difference between a polymer like polyethylene and a polymer like nylon?
23.104 Show the structure of poly(vinyl chloride) by drawing several repeating units. Vinyl chloride is $\mathrm{H}_{2} \mathrm{C}=\mathrm{CHCl}$.
23.105 Show the structures of the polymers you would obtain from the following monomers:
(a) $\mathrm{F}_{2} \mathrm{C}=\mathrm{CF}_{2}$ gives Teflon
(b) $\mathrm{H}_{2} \mathrm{C}=\mathrm{CHCO}_{2} \mathrm{CH}_{3}$ gives Lucite
23.106 Show the monomer units you would use to prepare the following alkene polymers:
(a)

(b)

(c)

23.107 What monomer unit is used to prepare poly(methyl cyanoacrylate), also known as "superglue"?


Poly(methyl cyanoacrylate)
23.108 Kevlar, a nylon polymer prepared by the reaction of 1,4-benzenedicarboxylic acid (terephthalic acid) with $p$-diaminobenzene, is so strong that it's used to make bulletproof vests. Draw the structure of a segment of Kevlar.
23.109 Draw the structure of a segment of the polyester that results from the reaction of ethylene glycol $\left(\mathrm{HOCH}_{2} \mathrm{CH}_{2} \mathrm{OH}\right)$ with butanedioic acid $\left(\mathrm{HO}_{2} \mathrm{CCH}_{2} \mathrm{CH}_{2} \mathrm{CO}_{2} \mathrm{H}\right)$.

## General Problems

23.110 Draw structural formulas for the following compounds:
(a) 2-Methylheptane
(b) 4-Ethyl-2-methylhexane
(c) 4-Ethyl-3,4-dimethyloctane
(d) 2,4,4-Trimethylheptane
(e) 1,1-Dimethylcyclopentane
(f) 4-Isopropyl-3-methylheptane
23.111 Give IUPAC names for the following alkanes:
(a)

(b)

(c)

(d)

23.112 Assume that you have two unlabeled bottles, one with cyclohexane and one with cyclohexene. How could you tell them apart by doing chemical reactions?
23.113 Assume you have two unlabeled bottles, one with cyclohexene and one with benzene. How could you tell them apart by doing chemical reactions?
23.114 Write the products of the following reactions:
(a)

(b)

(c)

23.115 Show the structure of the nylon polymer that results from heating 6-aminohexanoic acid.


6-Aminohexanoic acid

## Multi-Concept Problems

23.116 Fumaric acid is an organic substance widely used as a food additive. Its elemental composition is $41.4 \%$ C, $3.5 \% \mathrm{H}$, and $55.1 \% \mathrm{O}$. A solution made by dissolving 0.1500 g of fumaric acid in water and diluting to a volume of 100.0 mL gave rise to an osmotic pressure of 240.3 mm Hg at 298 K . On titration of a sample weighing $0.573 \mathrm{~g}, 94.1 \mathrm{~mL}$ of 0.105 M NaOH was required to reach an equivalence point. Fumaric acid reacts with 1 mol of HCl to give an addition product and with 1 mol of $\mathrm{H}_{2}$ to give a reduction product.
(a) What is the empirical formula of fumaric acid?
(b) What is the molecular mass of fumaric acid?
(c) Draw three possible structures for fumaric acid.
(d) If fumaric acid contains a trans double bond, which of your structures is correct?
23.117 When 0.0552 g of an unknown liquid containing only $\mathrm{C}, \mathrm{H}$, and O was subjected to combustion analysis, 0.1213 g of $\mathrm{CO}_{2}$ and 0.0661 g of $\mathrm{H}_{2} \mathrm{O}$ were formed.
(a) Calculate a formula for the unknown, and write a balanced equation for the combustion reaction.
(b) Is the formula you calculated an empirical formula or a molecular formula? Explain.
(c) Draw three possible structures for the compound, and identify the functional groups in each.
(d) Reaction of the compound with $\mathrm{CrO}_{3}$ yields acetone. Which of the three structures you drew in part (c) is most likely to be correct?
(e) Combustion of 5.000 g of the compound releases 166.9 kJ of heat. Look up $\Delta H_{\mathrm{f}}{ }^{\circ}$ values for $\mathrm{CO}_{2}(g)$ and $\mathrm{H}_{2} \mathrm{O}(l)$ in Appendix B, and calculate $\Delta H_{\mathrm{f}}{ }^{\circ}$ for the compound.
23.118 Reaction of methyl propanoate $\left(\mathrm{CH}_{3} \mathrm{CH}_{2} \mathrm{CO}_{2} \mathrm{CH}_{3}\right)$ with ammonia gives methanol plus a second product with the formula $\mathrm{C}_{3} \mathrm{H}_{7} \mathrm{NO}$.
(a) Propose a structure, and give a name for the second product.
(b) Draw two resonance structures for the product.
(c) Predict the geometry around the three carbon atoms and the nitrogen atom in the product according to VSEPR theory.
(d) Experimentally, the nitrogen atom in the product is found to be trigonal planar, with bond angles near $120^{\circ}$. How does this result compare with your prediction? Sketch a $p$-orbital picture of the product, and account for the experimental geometry.

## eMedia Problems

23.119 Use the Boiling Points activity (eChapter 23.2) to get the boiling points of the first six straight-chain alkanes (methane, ethane, propane, butane, pentane, and hexane) and the corresponding alcohols derived by replacing one of the $\mathrm{CH}_{3}$ hydrogens at the end of each chain with an OH group.
(a) For a given number of carbons, which has the higher boiling point, the alkane or the alcohol? Explain this observation in terms of intermolecular forces.
(b) Does the difference in boiling point for an alkane and its corresponding alcohol increase or decrease with increasing number of carbons?
(c) Using your answer from part (b), describe how the relative importance of hydrogen bonding and London dispersion forces changes with increasing length of a carbon chain. Which type of interaction contributes more significantly to the overall intermolecular forces for small molecules, and which for large molecules?
23.120 Determine the boiling points of at least five different alcohols and their corresponding amines using the Boiling Points activity (eChapter 23.2).
(a) Based on the boiling points, which functional group, OH or $\mathrm{NH}_{2}$, appears to exhibit more significant hydrogen bonding?
(b) Draw electron-dot structures of alcohol and amine functional groups. Use the electron-dot structures to explain the observation that one group exhibits more significant hydrogen bonding than the other.
23.121 From the 3D Models of $n$-pentane, isopentane, and neopentane (eChapter 23.4) draw expanded and condensed structures for each molecule. Name these molecules using proper IIUPAC nomenclature.
23.122 Draw structural formulas from all of the 3D Models of the examples of the families of organic molecules in $e$ Chapter 23.8. Circle the functional group in each of the molecules. Which families do you expect to exhibit hydrogen bonding?
23.123 Look at the Styrene Monomer 3D Model (eChapter 23.15) and draw the structural formula for styrene. Name the functional group on the monomer. Draw the structural formula for a segment of the polymer containing 3 styrene monomers.
23.124 Watch the Synthesis of Nylon 610 movie (eChapter 23.15) and complete the following equation for the polymerization process by drawing structural formulas for the reactants and for a segment of the polymer product. Include the formula for the other product.

$$
\mathrm{ClCO}\left(\mathrm{CH}_{2}\right)_{8} \mathrm{COCl}+\mathrm{NH}_{2}(\mathrm{CH})_{6} \mathrm{NH}_{2}
$$

## Chapter

## Biochemistry



The ultimate goal of chemistry is to understand the world around us on a molecular level, and a knowledge of biochemistry-the chemistry of living organisms-is a crucial
part of that goal. In this chapter, we'll look at the main classes of biomolecules: proteins, carbohydrates, lipids, and nucleic acids. First, though, we'll take a brief look at biochemical energetics to see where biochemical energy comes from and how it is used by organisms.

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### 24.1 Biochemical Energy

All living things do mechanical work. Microorganisms engulf food, plants bend toward the sun, animals move about. Organisms also do the chemical work of synthesizing biomolecules needed for energy storage, growth, and repair. Even individual cells do work when they move molecules and ions across cell membranes.

In animals, it is the energy extracted from food and released in the exquisitely interconnected reactions of metabolism that allows work to be done. All animals are powered by the cellular oxidation of biomolecules containing mainly carbon, hydrogen, and oxygen. The end products of this biological oxidation are carbon dioxide, water, and energy, just as they are when an organic fuel such as methane is burned with oxygen in a furnace.

$$
\mathrm{C}, \mathrm{H}, \mathrm{O}(\text { food molecules })+\mathrm{O}_{2} \longrightarrow \mathrm{CO}_{2}+\mathrm{H}_{2} \mathrm{O}+\text { Energy }
$$

The energy used by the vast majority of living organisms comes ultimately from the sun. Photosynthesis in plants converts sunlight to potential energy stored mainly in the chemical bonds of carbohydrates. Plant-eating animals use some of this energy for living and store the rest of it, mainly in the chemical bonds of fats. Other animals, including humans, then eat plants and smaller animals and make use of the chemical energy these organisms have stored.

The energy used by almost all living organisms ultimately comes from the sun. Plants use solar energy for the photosynthesis of glucose from $\mathrm{CO}_{2}$, and animals then eat the plants.


The sum of the many organic reactions that take place in cells is called metabolism. These reactions usually occur in long sequences, which may be either linear or cyclic. In a linear sequence, the product of one reaction serves as the starting material for the next. In a cyclic sequence, a series of reactions regenerates the first reactant and produces other products along the way.



Those reaction sequences that break molecules apart are known collectively as catabolism, while those that put building blocks back together to assemble larger molecules are known as anabolism. Catabolic reactions generally release energy that is used to power living organisms, whereas anabolic reactions generally absorb energy. The overall picture of catabolism and energy production can be roughly divided into the four stages shown in Figure 24.1.
degraded in cells to yield acetyl CoA.

Stage 3
Acetyl CoA is oxidized in the citric-acid cycle to yield $\mathrm{CO}_{2}$ and reduced coenzymes.

## Stage 4

The reduced coenzymes produced in stage 3 are oxidized by the electron-transport chain, and the energy released is used to make ATP.




Reduced coenzymes


Oxidized coenzymes

+ ATP

The first stage of catabolism, digestion, takes place in the stomach and small intestine when bulk food is broken down into small molecules such as simple sugars, long-chain carboxylic acids (called fatty acids), and amino acids. In stage 2, these small molecules are further degraded in cells to yield two-carbon acetyl groups $\mathrm{CH}_{3} \mathrm{C}=\mathrm{O}$ attached to a large carrier molecule called coenzyme $A$. The resultant compound, acetyl coenzyme $A$ (acetyl CoA), is an intermediate in the breakdown of all the main classes of food molecules.

Acetyl groups are oxidized in the third stage of catabolism, the citric acid cycle, to yield carbon dioxide and water. This stage releases a great deal of energy that is used in stage 4, the electron-transport chain, to make molecules of adenosine triphosphate (ATP). ATP, the final product of food catabolism, plays a pivotal role in the production of biological energy. As the crucial molecule for driving many metabolic reactions, ATP has been called the "energy currency of the living cell." Catabolic reactions "pay off" in ATP by synthesizing it from adenosine diphosphate (ADP) plus hydrogen phosphate ion, $\mathrm{HPO}_{4}{ }^{2-}$. Anabolic reactions "spend" ATP by transferring a phosphate group to other molecules, thereby regenerating ADP. The entire process of energy production revolves around the ATP $\rightleftharpoons$ ADP interconversion.
< FIGURE 24.1 An overview of catabolic pathways in the four stages of food degradation and the production of biochemical energy.

v
Oxidation of an organic molecule usually involves an increase in the number of carbon-oxygen bonds. When the acetyl group is oxidized to carbon dioxide, the number of carbonoxygen bonds increases from one double bond to two double bonds.



Although we say that energy is stored in bonds and released when the bonds are broken, in actuality bond breaking requires energy. Energy is released when new bonds are formed that are stronger than the bonds broken.

VTo reinforce the importance of functional groups, point out the functional groups present in molecules discussed in this chapter, for example, the aldehyde and alcohol groups in glucose.

VThis is a reaction between an alcohol $(\mathrm{R}-\mathrm{OH})$ and an acid $\left(\mathrm{HPO}_{4}{ }^{2-}\right)$ to produce an ester (a phosphate ester). Note that glucose 6-phosphate has a phosphate group attached to $\mathrm{C}_{6}$, where $\mathrm{C}_{1}$ is the aldehyde carbon.

Because the primary metabolic function of ATP is to drive reactions, biochemists often refer to it as a "high-energy molecule" or an "energy storehouse." These terms don't mean that ATP is somehow different from other compounds; they mean only that ATP releases a large amount of energy when its $\mathrm{P}-\mathrm{O}-\mathrm{P}$ (phosphoric anhydride) bonds are broken and a phosphate group is transferred.

What does the body do with ATP? Recall from Sections 8.14 and 17.7 that a chemical reaction is favorable, or spontaneous, if the free-energy change $(\Delta G)$ for the process is negative. Conversely, a reaction is unfavorable if the free-energy change is positive. The change in free energy depends on two factors: the release or absorption of heat $(\Delta H)$ and the increase or decrease in entropy $(\Delta S)$. The larger the amount of heat released and the greater the increase in entropy, the more favorable the reaction.

$$
\Delta G=\Delta H-T \Delta S
$$

Reactions in living organisms are no different from reactions in laboratory flasks. Both follow the same laws, and both have the same kinds of energy requirements. For any biochemical reaction to occur spontaneously, $\Delta G$ must be negative. For example, oxidation of 1 mol of glucose, the principal source of energy for animals, has $\Delta G^{\circ}=-2870 \mathrm{~kJ}$.


Glucose $\left(\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}\right)$
Reactions in which the free-energy change is positive can also occur, but such reactions can't be spontaneous. An example is the conversion of glucose to glucose-6-phosphate, an important step in the breakdown of dietary carbohydrates.


What usually happens when an energetically unfavorable reaction occurs is that it is "coupled" to an energetically favorable reaction so that the overall freeenergy change for the combined reactions is favorable. For example, the reaction of glucose with hydrogen phosphate ion $\left(\mathrm{HPO}_{4}{ }^{2-}\right)$ to yield glucose-6-phosphate plus water does not take place spontaneously because it is energetically unfavorable by 13.8 kJ . When ATP is involved, however, the reaction of ATP with water to yield ADP plus hydrogen phosphate ion is energetically favorable by about 30.5 kJ . Thus, if the two reactions are coupled, the overall process for the synthesis of glucose-6-phosphate is favorable by about 16.7 kJ . That is, the free-energy change for the reaction of ATP with water is so favorable that it can "drive" the unfavorable reaction of glucose with hydrogen phosphate ion.

| Glucose $+\mathrm{HPO}_{4}{ }^{2-} \longrightarrow$ Glucose-6-phosphate $+\mathrm{H}_{2} \mathrm{O}$ | $\Delta G^{\circ}=+13.8 \mathrm{~kJ}$ |
| ---: | :--- |
| ATP $+\mathrm{H}_{2} \mathrm{O} \longrightarrow \mathrm{ADP}+\mathrm{HPO}_{4}{ }^{2-}+\mathrm{H}^{+}$ | $\Delta G^{\circ}=-30.5 \mathrm{~kJ}$ |
| Net: Glucose $+\mathrm{ATP} \longrightarrow$ Glucose-6-phosphate $+\mathrm{ADP}+\mathrm{H}^{+}$ | $\Delta G^{\circ}=-16.7 \mathrm{~kJ}$ |

This is an application of Hess's law, discussed in Chapter 8.

It's this ability to drive otherwise unfavorable reactions that makes ATP so useful. In fact, most of the thousands of reactions going on in your body every minute are somehow coupled to ATP. It's no exaggeration to say that the transfer of a phosphate group from ATP is the single most important chemical reaction in making life possible.

- PROBLEM 24.1 One of the steps in fat metabolism is the reaction of glycerol $\left[\mathrm{HOCH}_{2}-\mathrm{CH}(\mathrm{OH})-\mathrm{CH}_{2} \mathrm{OH}\right]$ with ATP to yield glycerol-1-phosphate. Draw the structure of glycerol-1-phosphate.


### 24.2 Amino Acids and Peptides

Taken from the Greek proteios, meaning "primary," the name protein aptly describes a group of biological molecules that are of primary importance to all living organisms. Approximately $50 \%$ of the body's dry weight is protein, and almost all the reactions that occur in the body are catalyzed by proteins. In fact, a human body contains over 100,000 different kinds of proteins.

Proteins have many different biological functions. Some, such as the keratin in skin, hair, and fingernails, serve a structural purpose. Others, such as the insulin that controls glucose metabolism, act as hormones-chemical messengers that coordinate the activities of different cells in an organism. And still other proteins, such as DNA polymerase, are enzymes, the biological catalysts that carry out body chemistry. All proteins are biological polymers made up of many amino acid molecules linked together to form a long chain. As their name implies, amino acids contain two functional groups, a basic amino group $\left(-\mathrm{NH}_{2}\right)$ and an acidic $-\mathrm{CO}_{2} \mathrm{H}$ group. Alanine is one of the simplest examples.


Alanine—an amino acid

Two or more amino acids can link together by forming amide bonds (Section 23.14), usually called peptide bonds. A dipeptide results when two amino acids link together by formation of a peptide bond between the $-\mathrm{NH}_{2}$ group of one and the $-\mathrm{CO}_{2} \mathrm{H}$ group of the other. Similarly, a tripeptide results when three amino acids link together with two peptide bonds, and so on. Short chains of up to 100 amino acids are usually called polypeptides, while the term protein is reserved for longer chains.


- Bird feathers are made largely of the protein keratin.

$\sqrt{ }$Although written as $-\mathrm{CO}_{2} \mathrm{H}$, there is no bond between the two oxygen atoms. Since carbon must have four bonds, $-\mathrm{CO}_{2} \mathrm{H}$ is actually a shorthand notation for

$$
\stackrel{\mathrm{O}}{\|}-\stackrel{\text { ® }}{\mathrm{C}}-\mathrm{OH}
$$

The formation of the peptide bond from reaction of the acid group on one amino acid with the amine group on a second amino acid is a carbonyl-group substitution reaction, discussed in Chapter 23. The peptide bond is part of the amide group formed by this reaction.



A FIGURE 24.2 Structures of the $20 \alpha$-amino acids found in proteins. Fifteen of the 20 have neutral side chains, two have acidic side chains, and three have basic side chains. The names of the 10 essential amino acids are highlighted.

Twenty different amino acids are commonly found in proteins, as shown in Figure 24.2. Each amino acid is referred to by a three-letter shorthand code, such as Ala (alanine), Gly (glycine), Pro (proline), and so on. All 20 are called alpha-$(\boldsymbol{\alpha}-)$ amino acids because the amino group in each is connected to the carbon atom alpha to (next to) the carboxylic acid group. Nineteen of the 20 have an $-\mathrm{NH}_{2}$ amino group, and one (proline) has an $-\mathrm{NH}-$ amino group as part of a ring.

The 20 amino acids differ only in the nature of the group attached to the $\alpha$ carbon. Usually called the side chain, this group can be symbolized in a general way by the letter R. (In a broader context, the symbol R is used throughout organic chemistry to refer to an organic fragment of unspecified structure.) Our bodies can synthesize only 10 of the 20 amino acids. The remaining 10, highlighted in Figure 24.2, are called essential amino acids because they must be obtained from the diet.


The 20 common amino acids are classified as neutral, basic, or acidic, depending on the structure of their side chains. Fifteen of the 20 have neutral side chains. Two (aspartic acid and glutamic acid) have an additional carboxylic acid group in their side chains and are classified as acidic amino acids. Three (lysine, arginine, and histidine) have an additional amine function in their side chains and are classified as basic amino acids. The 15 neutral amino acids can be further divided into those with nonpolar side chains and those with polar functional groups such as amide or hydroxyl groups. Nonpolar side chains are often described as hydrophobic (water fearing) because they are not attracted to water, while polar side chains are described as hydrophilic (water loving) because they are attracted to water.

## Worked Example 24.1

Identify the following amino acid, and tell from the electrostatic potential map whether its side chain is acidic, basic, neutral nonpolar, or neutral polar.


## Strategy

Identify the amino acid by looking at Figure 24.2, and predict its polarity by looking for electron-rich (red) or electron-poor (blue) regions in the side chain.

## Solution

The amino acid is leucine. It is nonpolar because it contains a hydrocarbon side chain that has neither electron-rich nor electron-poor groups.

PROBLEM 24.2 Which common amino acids contain an aromatic (benzene-like) ring? Which contain sulfur? Which are alcohols? Which have alkyl-group side chains?


3D models of Glycine, Alanine, Phenylalanine, Tryptophan, Serine,
Glutamine, Aspartic Acid, and Lysine

$\sqrt{ }$All $20 \alpha$-amino acids found in proteins have an amine group and a side chain, R , on the carbon adjacent to the carboxylic acid group.


A Corn is particularly low in lysine, one of the essential amino acids.

The side chains of neutral amino acids are hydrophilic if $R$ is polar (for example, if $\mathrm{R}=-\mathrm{CH}_{2} \mathrm{OH}$ ), and hydrophobic if $R$ is nonpolar (for example, if $\mathrm{R}=-\mathrm{H})$.

PROBLEM 24.3 Draw alanine using wedges and dashes to show the tetrahedral geometry of its $\alpha$ carbon.

- KEY CONCEPT PROBLEM 24.4 Identify the following amino acid, and tell from the electrostatic potential map whether its side chain is acidic, basic, neutral nonpolar, or neutral polar.



### 24.3 Amino Acids and Molecular Handedness

We saw in Section 20.9 that certain molecules lack a plane of symmetry and are therefore chiral. When held up to a mirror, a chiral molecule is not identical to its reflected image. Instead, the molecule and its mirror image have a right-hand/lefthand relationship. Compare alanine and propane, for example (Figure 24.3). An alanine molecule is chiral; it has no symmetry plane and can exist in two forms-a "right-handed" form called D-alanine (from dextro, Latin for "right") and a "lefthanded" form called L-alanine (from levo, Latin for "left"). Propane, however, is achiral. It has a symmetry plane cutting through the three carbons and thus exists in only a single form.

A FIGURE 24.3 Alanine (2-aminopropanoic acid) has no symmetry plane; the two "halves" of the molecule are not mirror images. Thus, alanine can exist in two formsa "right-handed" form and a "left-handed" form. Propane, however, has a symmetry plane and is achiral.

Why are some organic molecules chiral while others are not? The answer has to do with the three-dimensional nature of organic molecules. We've seen that carbon forms four bonds that are oriented toward the four corners of a regular tetrahedron. Whenever a carbon atom is bonded to four different atoms or groups of atoms, chirality results. If a carbon is bonded to two or more of the same groups, however, no chirality is possible. In alanine, for example, carbon 2 is bonded to four different groups: a $-\mathrm{CO}_{2} \mathrm{H}$ group, an -H atom, an $-\mathrm{NH}_{2}$ group, and a $-\mathrm{CH}_{3}$ group. Thus, alanine is chiral. In propane, however, each of the carbons is bonded to at least two groups-the - H atoms-that are identical. Thus, propane is achiral.


As mentioned in Section 20.9, the two mirror-image forms of a chiral molecule are called enantiomers, or optical isomers. The mirror-image relationship of the enantiomers of a molecule with four different groups on a chiral carbon atom is shown in Figure 24.4.


4 FIGURE 24.4 A molecule with a carbon atom that is bonded to four different groups is chiral and is not identical to its mirror image. It thus exists in two enantiomeric forms.


Of the 20 common amino acids, 19 are chiral because they have four different groups bonded to their $\alpha$ carbons, $-\mathrm{H},-\mathrm{NH}_{2},-\mathrm{CO}_{2} \mathrm{H}$, and -R (the side chain). Only glycine, $\mathrm{H}_{2} \mathrm{NCH}_{2} \mathrm{CO}_{2} \mathrm{H}$, is achiral. Even though the naturally occurring chiral $\alpha$-amino acids can exist as pairs of enantiomers, only L-amino acids are found in proteins. When drawn with the $-\mathrm{CO}_{2} \mathrm{H}$ group at the top and the side-chain R group at the bottom, an L-amino acid has its $-\mathrm{NH}_{2}$ group coming out of the plane of the paper on the left side of the structure:


## Worked Example 24.2

Lactic acid can be isolated from sour milk. Is lactic acid chiral?


## Strategy

To find out if lactic acid is chiral, list the groups attached to each carbon, and see if any carbon is attached to four different groups.

## Solution

Groups on carbon 1

1. -OH
2. $=\mathrm{O}$
3. $-\mathrm{CH}(\mathrm{OH}) \mathrm{CH}_{3}$

Groups on carbon 2

1. $-\mathrm{CO}_{2} \mathrm{H}$
2. -OH
3. -H
4. $-\mathrm{CH}_{3}$

Groups on carbon 3

1. $-\mathrm{CH}(\mathrm{OH}) \mathrm{CO}_{2} \mathrm{H}$
2. -H
3. -H
4. -H

Of the three carbons, carbon 2 has four different groups, so lactic acid is chiral.

- PROBLEM 24.5 Which of the following objects are chiral?
(a) A glove
(b) A baseball
(c) A screw
(d) A nail
- PROBLEM 24.6 2-Aminopropane is an achiral molecule, but 2-aminobutane is chiral. Explain.
- PROBLEM 24.7 Which of the following molecules are chiral?
(a) 3-Chloropentane
(b) 2-Chloropentane
(c)

- PROBLEM 24.8 Two of the 20 common amino acids have two chiral carbon atoms in their structures. Identify them.

KEY CONCEPT PROBLEM 24.9 Two of the following three molecules are identical, and one is the enantiomer of the other two. Which one is the enantiomer?

Proteins and Amino Acids movie


### 24.4 Proteins

Proteins are amino acid polymers in which the individual amino acids, often called residues, are linked together by peptide (amide) bonds. The repeating chain of amide linkages to which the side chains are attached is called the backbone.
-


A segment of a protein backbone. The side-chain R groups of the individual amino acids are substituents on the backbone.

Since amino acids can be assembled in any order, depending on which $-\mathrm{CO}_{2} \mathrm{H}$ group joins with which $-\mathrm{NH}_{2}$ group, the number of possible isomeric peptides increases rapidly as the number of amino acid residues increases. There are six
ways in which three different amino acids can be joined, more than 40,000 ways in which the eight amino acids present in the blood pressure-regulating hormone angiotensin II can be joined (Figure 24.5), and a staggering number of ways in which the 1800 amino acids in myosin, the major component of muscle filaments, can be arranged.

FIGURE 24.5 The structure of angiotensin II, an octapeptide in blood plasma that regulates blood pressure.


No matter how long the chain, all noncyclic proteins have an N -terminal amino acid with a free $-\mathrm{NH}_{2}$ group on one end and a C-terminal amino acid with a free $-\mathrm{CO}_{2} \mathrm{H}$ group on the other end. By convention, a protein is written with the N-terminal residue on the left and the C-terminal residue on the right, and its name is indicated with the three-letter abbreviations listed in Figure 24.2. Thus, angiotensin II (Figure 24.5) is abbreviated Asp-Arg-Val-Tyr-Ile-His-Pro-Phe.

Proteins are classified according to their three-dimensional shape as either fibrous or globular. Fibrous proteins, such as collagen and the keratins, consist of polypeptide chains arranged side by side in long filaments. Because these proteins are tough and insoluble in water, they are used in nature for structural materials like skin, tendons, hair, ligaments, and muscle. Globular proteins, by contrast, are usually coiled into compact, nearly spherical shapes, as seen in the computer-generated picture of the digestive enzyme pepsin in Figure 24.6. Most of the 2000 or so known enzymes present inside cells are globular proteins.

Another way to classify proteins is according to biological function. As indicated in Table 24.1, proteins have a remarkable diversity of roles.

TABLE 24.1 Some Biological Functions of Proteins

| Type | Function | Example |
| :--- | :--- | :--- |
| Enzymes | Catalyze biological processes | Pepsin |
| Hormones | Regulate body processes | Insulin |
| Storage proteins | Store nutrients | Ferritin |
| Transport proteins | Transport oxygen and other | Hemoglobin |
|  | substances through the body |  |
| Structural proteins | Form an organism's structure | Collagen |
| Protective proteins | Help fight infection | Antibodies |
| Contractile proteins | Form muscles | Actin, myosin |
| Toxic proteins | Serve as a defense for the plant | Snake venoms |
|  | or animal |  |

Proteins are always drawn as $\mathrm{H}_{2} \mathrm{~N}-$ (amino acid sequence) $-\mathrm{CO}_{2} \mathrm{H}$ and named according to the left-to-right sequence of the amino acids.


A FIGURE 24.6 A computergenerated view of the enzyme pepsin, a typical globular protein.
C. M. Drain and Barry B. Corden, "Reversible Oxygenation of Oxygen Transport Proteins, "J. Chem. Educ., Vol. 64, 1987, 441-443.

## Worked Example 24.3

Draw the structure of the dipeptide Ala-Ser.

## Strategy

First, look up the names and structures of the two amino acids, Ala (alanine) and Ser (serine). Since alanine is N-terminal and serine is C-terminal, Ala-Ser must have an amide bond between the alanine $-\mathrm{CO}_{2} \mathrm{H}$ and the serine $-\mathrm{NH}_{2}$.
Solution

Proteins and Amino Acids movie

$\square$Primary structure is the amino acid sequence, which controls the shape of the protein and the role the protein serves in the body.

©Secondary structure is due to hydrogen bonding between amino acids, which folds the protein into an $\alpha$-helix or a $\beta$-pleated sheet.


- PROBLEM 24.10 Use the three-letter shorthand notations to name the two isomeric dipeptides that can be made from valine and cysteine. Draw both structures.
- PROBLEM 24.11 Name the six tripeptides that contain valine, tyrosine, and glycine.


### 24.5 Levels of Protein Structure

With molecular masses of up to one-half million amu, many proteins are so large that the word structure takes on a broader meaning with these immense molecules than it does with simple organic molecules. In fact, chemists usually speak about four levels of structure when describing proteins. The primary structure of a protein specifies the sequence in which the various amino acids are linked together. Secondary structure refers to how segments of the protein chain are oriented into a regular pattern. Tertiary structure refers to how the entire protein chain is coiled and folded into a specific three-dimensional shape, and quaternary structure refers to how several protein chains can aggregate to form a larger unit.

## Primary Structure

Primary structure is the most fundamental of the four structural levels because it is the protein's amino acid sequence that determines its overall shape and function. So crucial is primary structure to function that the change of only one amino acid out of several hundred can drastically alter biological properties. The disease sickle-cell anemia, for example, is caused by a genetic defect in blood hemoglobin whereby valine is substituted for glutamic acid at only one position in a chain of 146 amino acids.

## Secondary Protein Structure

When looking at the primary structure of a protein like angiotensin II in Figure 24.5, you might get the idea that the molecule is long and threadlike. In fact, though, most proteins fold in such a way that segments of the protein chain orient into regular patterns, called secondary structures. There are two common kinds of patterns: the alpha-helix and the beta-pleated sheet.

Keratin, a fibrous protein found in wool, hair, fingernails, and feathers, wraps into a helical coil, much like the cord on a telephone (Figure 24.7). Called an alpha$(\boldsymbol{\alpha} \boldsymbol{-})$ helix, this secondary structure is stabilized by the formation of hydrogen bonds (Section 10.2) between the $\mathrm{N}-\mathrm{H}$ group of one amino acid and the $\mathrm{C}=\mathrm{O}$ group of another amino acid four residues away. Each turn of the helix contains 3.6 amino acid residues, with a distance between turns of 0.54 nm .


Fibroin, the fibrous protein found in silk, has a secondary structure called a beta- ( $\boldsymbol{\beta}$-) pleated sheet, in which a polypeptide chain doubles back on itself after a hairpin bend. The two sections of the chain on either side of the bend line up in a parallel arrangement held together by hydrogen bonds (Figure 24.8). Although not as common as the $\alpha$-helix, small pleated-sheet regions are often found in proteins.


4 FIGURE 24.7 The $\alpha$-helical secondary structure of keratin. The amino acid backbone winds in a spiral, much like that of a telephone cord.


- Sheep's wool is made largely of keratin, a fibrous protein with an $\alpha$-helical secondary structure.


A Silk is made of fibroin, a fibrous protein with a pleatedsheet secondary structure.

4 FIGURE 24.8 The $\beta$-pleated-sheet secondary structure of silk fibroin. The amino acid side chains, shown in green, are above and below the rough plane of the sheet. (Dotted lines indicate hydrogen bonds between chains.)


- The muscles of sea mammals contain myoglobin, a globular protein that stores oxygen.

Hemoglobin 3D model

## Tertiary Protein Structure

Secondary protein structures result primarily from hydrogen bonding between amide linkages along the protein backbone, but higher levels of structure result primarily from interactions of side-chain R groups in the protein. Myoglobin, for example, is a globular protein found in the skeletal muscles of sea mammals, where it stores oxygen needed to sustain the animals during long dives. With a single chain of 153 amino acid residues, myoglobin consists of eight straight segments, each of which adopts an $\alpha$-helical secondary structure. These helical sections then fold up further to form a compact, nearly spherical, tertiary structure (Figure 24.9).

© FIGURE 24.9 Secondary and tertiary structure of myoglobin, a globular protein found in the muscles of sea mammals. Myoglobin has eight helical sections.

The most important force stabilizing a protein's tertiary structure results from the hydrophobic interactions of hydrocarbon side chains on amino acids. Those amino acids with neutral, nonpolar side chains have a strong tendency to congregate on the hydrocarbonlike interior of a protein molecule, away from the aqueous medium. Those amino acids with polar side chains, by contrast, are usually found on the exterior of the protein where they can be solvated by water. Also important for stabilizing a protein's tertiary structure are disulfide bridges (covalent S-S bonds formed between nearby cysteine residues), salt bridges (ionic attractions between positively and negatively charged sites on the protein), and hydrogen bonds between nearby amino acids.


## 24.6 | Enzymes

Enzymes are large proteins that act as catalysts for biological reactions. A catalyst, as we saw in Section 12.12, is an agent that speeds up the rate of a chemical reaction without itself undergoing change. For example, sulfuric acid catalyzes the reaction of a carboxylic acid with an alcohol to yield an ester (Section 23.14).

Enzymes, too, catalyze reactions that might otherwise occur very slowly, but they differ from catalysts like sulfuric acid in two important respects. First, enzymes are much larger, more complicated molecules than simple inorganic catalysts. Second, enzymes are far more specific in their action. Sulfuric acid catalyzes the reaction of nearly every carboxylic acid with nearly every alcohol, but enzymes often catalyze only a single reaction of a single compound, called the enzyme's substrate. For example, the enzyme amylase found in human digestive systems is able to catalyze the breakdown of starch to yield glucose but has no effect on cellulose, even though starch and cellulose are structurally similar. Thus, humans can digest potatoes (starch) but not grass (cellulose).

$$
\begin{aligned}
\text { Starch }+\mathrm{H}_{2} \mathrm{O} \\
\text { Cellulose }+\mathrm{H}_{2} \mathrm{O} \xrightarrow{\text { Amylase }} \text { Many glucose molecules } \\
\text { No reaction }
\end{aligned}
$$

The catalytic activity of an enzyme is measured by its turnover number, which is defined as the number of substrate molecules acted on by one molecule of enzyme per second. As indicated in Table 24.2, enzymes vary greatly in their turnover number. Most enzymes have values in the 1-20,000 range, but carbonic anhydrase, which catalyzes the reaction of $\mathrm{CO}_{2}$ with water to yield bicarbonate ion, acts on 600,000 substrate molecules per second.

In addition to their protein part, many enzymes contain small, nonprotein parts called cofactors. In such enzymes, the protein part is called an apoenzyme, and the entire assembly of apoenzyme plus cofactor is called a holoenzyme. Only holoenzymes are active as catalysts; neither apoenzyme nor cofactor alone can catalyze a reaction.
Holoenzyme = Apoenzyme + Cofactor

An enzyme cofactor can be either an inorganic ion (usually a metal cation) or a small organic molecule called a coenzyme. In fact, the requirement of many enzymes for metal-ion cofactors is the main reason behind our dietary need for trace minerals. Iron, zinc, copper, manganese, molybdenum, cobalt, nickel, and selenium are all essential trace elements that function as enzyme cofactors. A large number of different organic molecules also serve as coenzymes. Often, although not always, the coenzyme is a vitamin. Thiamine (vitamin $B_{1}$ ), for example, is a coenzyme required in the metabolism of carbohydrates.


Thiamine (vitamin $\mathrm{B}_{1}$ ); an enzyme cofactor

## How Enzymes Work: The Lock-and-Key Model

According to the lock-and-key model, an enzyme is pictured as a large, irregularly shaped molecule with a cleft, or crevice, in its middle. Inside the crevice is an active site, a small region with the shape and chemical composition necessary to bind the substrate and catalyze the appropriate reaction. In other words, the active site acts like a lock into which only a specific key can fit (Figure 24.10). An enzyme's active site is lined by various acidic, basic, and neutral amino acid side chains, all properly positioned for maximum interaction with the substrate.

Enzyme-catalyzed reactions begin when the substrate migrates into the active site to form an enzyme-substrate complex. No covalent bonds are formed; the enzyme and substrate are held together by hydrogen bonds and by

TABLE 24.2 Turnover Numbers of
Some Enzymes

| Enzyme | Turnover <br> Number <br> $\left(\mathbf{s}^{\mathbf{- 1}}\right)$ |
| :--- | ---: |
| Carbonic anhydrase | 600,000 |
| Acetylcholinesterase | 25,000 |
| $\beta$-Amylase | 18,000 |
| Penicillinase | 2,000 |
| DNA polymerase I | 15 |



Hexose Kinase 3D models

FIGURE 24.10 According to the lock-and-key model, an enzyme is a large, threedimensional molecule containing a crevice with an active site. Only a substrate whose shape and structure are complementary to those of the active site can fit into the enzyme. The active site of the enzyme hexose kinase is visible as the cleft on the left in this computergenerated structure, as is the fit of the substrate (yellow) in the active site.

weak intermolecular attractions between functional groups. With enzyme and substrate thus held together in a precisely defined arrangement, the appropriately positioned functional groups in the active site carry out a chemical reaction on the substrate molecule, and enzyme plus product then separate:

$$
\underset{\text { Enzyme }}{\mathrm{E}}+\underset{\text { Substrate }}{\mathrm{S}} \underset{\text { Complex }}{\mathrm{E}-\mathrm{S}} \longrightarrow \underset{\text { Enzyme }}{\mathrm{E}}+\underset{\text { Product }}{\mathrm{P}}
$$

As an example of enzyme action, look in Figure 24.11 at the enzyme hexose kinase, which catalyzes the reaction of adenosine triphosphate (ATP) with glucose to yield glucose-6-phosphate and adenosine diphosphate (ADP). The enzyme first binds a molecule of ATP cofactor at a position near the active site, and glucose then bonds to the active site with its C6 hydroxyl group held rigidly in position next to the ATP molecule. Reaction ensues, and the two products are released from the enzyme.



Compare the enzyme-catalyzed reaction shown in Figure 24.11 with the same reaction in the absence of enzyme. Without enzyme present, the two reactants would spend most of their time surrounded by solvent molecules, far away from each other and only occasionally bumping together. With an enzyme present, however, the two reactants are forced into close contact. Enzymes act as catalysts because of their ability to bring reactants together, hold them at the exact distance and with the exact orientation necessary for reaction, and provide acidic or basic sites as required.

## 24.7 | Carbohydrates

Carbohydrates occur in every living organism. The starch in food and the cellulose in grass are nearly pure carbohydrate. Modified carbohydrates form part of the coating around all living cells, and other carbohydrates are found in the DNA that carries genetic information from one generation to the next.

The word carbohydrate was used originally to describe glucose, which has the formula $\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}$ and was once thought to be a "hydrate of carbon," $\mathrm{C}_{6}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}$. Although this view was soon abandoned, the word persisted and is now used to refer to a large class of polyhydroxylated aldehydes and ketones. Glucose, for example, is a six-carbon aldehyde with five hydroxyl groups.


Glucose-a pentahydroxy aldehyde
Carbohydrates are classified as either simple or complex. Simple sugars, or monosaccharides, are carbohydrates such as glucose and fructose that can't be broken down into smaller molecules by hydrolysis with aqueous acid. Complex carbohydrates, or polysaccharides, are compounds such as cellulose and starch that are made of many simple sugars linked together. On hydrolysis, polysaccharides are cleaved to yield many molecules of simple sugars.

Monosaccharides are further classified as either aldoses or ketoses. An aldose contains an aldehyde carbonyl group; a ketose contains a ketone carbonyl group (Section 23.13). The -ose suffix indicates a sugar, and the number of carbon atoms in the sugar is specified by using one of the prefixes tri-, tetr-, pent-, or hex-. Thus, glucose is an aldohexose (a six-carbon aldehyde sugar), fructose is a ketohexose (a six-carbon ketone sugar), and ribose is an aldopentose (a five-carbon aldehyde sugar). Most commonly occurring sugars are either aldopentoses or aldohexoses.


Fructose-a ketohexose


Ribose-an aldopentose

- PROBLEM 24.12 Classify each of the following monosaccharides:
(a)

(b)

(c)



### 24.8 Handedness of Carbohydrates

We saw in Section 24.3 that compounds are chiral if they have a carbon atom bonded to four different atoms or groups of atoms. Such compounds lack a plane of symmetry and can exist as a pair of enantiomers in either a "right-handed" D form or a "left-handed" L form. For instance, the simple triose glyceraldehyde is

7] Charles L. Bering, "The Biochemistry of Brewing," J. Chem. Educ., Vol. 65, 1988, 519-521.


$\nabla$
A carbohydrate contains many hydroxyl groups and either an aldehyde or ketone functional group. A simple carbohydrate (monosaccharide or sugar) is an aldose if it contains an aldehyde group, or a ketose if it contains a ketone group.

Common sugars have five or six carbon atoms.

Robert S. Shallenberger and Wanda J. Wienen, "Carbohydrate Stereochemistry," J. Chem. Educ., Vol. 66, 1989, 67-73.

Phillip S. Beauchamp,
"Absolutely Simple Stereochemistry," J. Chem. Educ., Vol. 61, 1984, 666-667.

Chirality of D-Glyceraldehyde activity
chiral because it has four different groups bonded to C 2 : $-\mathrm{CHO},-\mathrm{H},-\mathrm{OH}$, and $-\mathrm{CH}_{2} \mathrm{OH}$. Of the two enantiomers, only D-glyceraldehyde occurs naturally.



Groups bonded to C2
1.- CHO
2.-H
3.- OH
4. $-\mathrm{CH}_{2} \mathrm{OH}$

D-Glyceraldehyde

Glyceraldehyde has only one chiral carbon atom and can exist as two enantiomers, but other sugars have two, three, four, or even more chiral carbons. In general, a compound with $n$ chiral carbon atoms has a maximum of $2^{n}$ possible isomeric forms. Glucose, for example, has four chiral carbon atoms, so a total of $2^{4}=16$ isomers are possible, differing in the spatial arrangements of the substituents around the chiral carbon atoms.


- PROBLEM 24.13 Draw tetrahedral representations of the two glyceraldehyde enantiomers using wedged, dashed, and normal lines to show three-dimensionality.
- PROBLEM 24.14 Ribose has three chiral carbon atoms. What is the maximum number of isomers?
- KEY CONCEPT PROBLEM 24.15 Classify the following monosaccharide, and identify each chiral carbon in its structure.



## 24.9 | Cyclic Structures of Monosaccharides

Glucose and other monosaccharides are often shown for convenience as having open-chain structures. They actually exist, however, primarily as cyclic molecules in which an -OH group near the bottom of the chain adds to the carbonyl group near the top of the chain to form a ring. In glucose itself, ring formation occurs between the -OH group on C 5 and the $\mathrm{C}=\mathrm{O}$ group at C 1 (Figure 24.12).


Curl around

## Form ring

/




FIGURE 24.12 The cyclic $\alpha$ and $\beta$ forms of D-glucose that result from ring formation between the -OH group at C 5 and the $\mathrm{C}=\mathrm{O}$ group at C 1 . The $\alpha$ form has the-OH group at C 1 on the bottom side of the ring; the $\beta$ form has the -OH group on the top.

Note that two cyclic forms of glucose can result from ring formation, depending on whether the newly formed -OH group at C 1 is on the bottom or top side of the ring. The ordinary crystalline glucose you might take from a bottle is entirely the cyclic $\alpha$ form, in which the $\mathrm{C} 1-\mathrm{OH}$ group is on the bottom side of the ring. At equilibrium in water solution, however, all three forms are present in the proportion $0.02 \%$ open-chain form, $36 \% \alpha$ form, and $64 \% \beta$ form.

### 24.10 Some Common Disaccharides and Polysaccharides

## Lactose

Lactose, or milk sugar, is the major carbohydrate present in mammalian milk. Human milk, for example, is about $7 \%$ lactose. Structurally, lactose is a disaccharide whose hydrolysis with aqueous acid yields one molecule of glucose and one molecule of another monosaccharide called galactose. The two sugars are bonded together by what is called a 1,4 link-a bridging oxygen atom between C 1 of $\beta$-galactose and C4 of $\beta$-glucose.


James M. Garrett, "Brand the Name with the Linkage of the Same," J. Chem. Educ., Vol. 61, 1984, 665.

## Sucrose

Sucrose, or plain table sugar, is probably the most common pure organic chemical in the world. Although sucrose is found in many plants, sugar beets ( $20 \%$ by mass) and sugar cane ( $15 \%$ by mass) are the most common sources. Hydrolysis of sucrose yields one molecule of glucose and one molecule of fructose. The 1:1 mixture of glucose and fructose that results, often called invert sugar, is commonly used as a food additive.

$\beta$-Fructose

## Cellulose and Starch

Cellulose 3D model

Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "A Variation of the Starch-Iodine Clock Reaction," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 147-148.

Cellulose, the fibrous substance that forms the structural material in grasses, leaves, and stems, consists of several thousand $\beta$-glucose molecules joined together by 1,4 links to form an immense polysaccharide.


Starch, like cellulose, is also a polymer of glucose. Unlike cellulose, though, starch is edible. Indeed, the starch in such vegetables as beans, rice, and potatoes is an essential part of the human diet. Structurally, starch differs from cellulose in that it contains $\alpha$ - rather than $\beta$-glucose units. Starch is also more structurally complex than cellulose and is of two types: amylose and amylopectin. Amylose, which accounts for about $20 \%$ of starch, consists of several hundred to 1000 $\alpha$-glucose units joined together in a long chain by 1,4 links (Figure 24.13a). Amylopectin, which accounts for about $80 \%$ of starch, is much larger than amylose (up to 100,000 glucose units per molecule) and has branches approximately every 25 units along its chain. A glucose molecule at a branch point uses two of its hydroxyl groups (those at C4 and C6) to form links to two other sugars (Figure 24.13b).

Starch molecules are digested in the stomach by enzymes called $\alpha$-glycosidases, which break down the polysaccharide chain and release individual glucose molecules. As is usually the case with enzyme-catalyzed reactions, $\alpha$-glycosidases are

(a) Amylose

(b) Amylopectin
highly specific in their action. They hydrolyze only the links between $\alpha$ units while leaving the links between $\beta$ units untouched. Thus, starch is easily digested but cellulose is not.

## Glycogen

Glycogen, sometimes called animal starch, serves the same food storage role in animals that starch serves in plants. After we eat starch and the body breaks it down into simple glucose units, some of the glucose is used immediately as fuel and some is stored in the body as glycogen for later use. Structurally, glycogen is similar to amylopectin in being a long polymer of $\alpha$-glucose units with branch points in its chain. Glycogen has many more branches than amylopectin, however, and is much larger-up to 1 million glucose units per glycogen molecule.

### 24.11 Lipids

Lipids are less well known to most people than are proteins or carbohydrates, yet they are just as essential to life. Lipids have many important biological roles, serving as sources of fuel storage, as protective coatings around many plants and insects, and as major components of the membranes that surround every living cell.

Chemically, a lipid is a naturally occurring organic molecule that dissolves in a nonpolar organic solvent when a sample of plant or animal tissue is crushed or ground. Because they're defined by solubility—a physical property—rather than by chemical structure, it's not surprising that there are a great many different kinds of lipids (Figure 24.14). Note that all the lipids in Figure 24.14 contain large hydrocarbon portions, which accounts for their solubility behavior.

## Fats and Oils

Animal fats and vegetable oils are the most plentiful lipids in nature. Although they appear physically different-animal fats like butter and lard are usually solid, whereas vegetable oils like corn and peanut oil are liquid-their structures

4 FIGURE 24.13 Glucose polymers in starch. (a) Amylose consists of linear chains of $\alpha$-glucose units linked by 1,4 bonds. (b) Amylopectin has branch points about every 25 sugars in the chain. A glucose unit at a branch point uses two of its hydroxyls (at C4 and C6) to form 1,4 and 1,6 links to two other sugars.

$\triangle$ Glycogen provides the stored energy that lets these marathoners finish the race.

$\sqrt{ }$Remember from Chapter 23 that alcohol + acid $\rightarrow$ ester + water. In fats and oils, glycerol is the alcohol, and the acids are fatty acids that contain long hydrocarbon chains, 12 to 22 carbon atoms long. Lipids with unsaturated fatty acid groups tend to be oils; those with saturated fatty acid groups tend to be solids.
-



An animal fat or vegetable oil


$\mathrm{PGF}_{2 \alpha}$-a prostaglandin

A FIGURE 24.14 Structures of some representative lipids isolated from plant and animal tissue by extraction with nonpolar organic solvents. All have large hydrocarbon portions.
are similar. All fats and oils are triacylglycerols, or triglycerides, esters of glycerol (1,2,3-propanetriol) with three long-chain carboxylic acids called fatty acids. The fatty acids are usually unbranched and have an even number of carbon atoms in the range 12-22.

As shown by the triacylglycerol structure in Figure 24.14, the three fatty acids of a given molecule need not be the same. Furthermore, the fat or oil from a given source is a complex mixture of many different triacylglycerols. Table 24.3 shows the structures of some commonly occurring fatty acids, and Table 24.4 lists the composition of several fats and oils. Note that vegetable oils are largely unsaturated but animal fats contain a high percentage of saturated fatty acids.

TABLE 24.3 Structures of Some Common Fatty Acids
\(\left.$$
\begin{array}{llll} & \begin{array}{l}\text { No. of } \\
\text { Carbons }\end{array}
$$ \& \begin{array}{l}No. of <br>
Double <br>

Bonds\end{array} \& Structure\end{array}\right]\)| Melting |
| :--- |
| Point ( ${ }^{\circ} \mathbf{C}$ ) |

TABLE 24.4 Approximate Composition of Some Common Fats and Oils

|  | $\begin{array}{c}\text { Saturated } \\ \text { Fatty Acids (\%) }\end{array}$ |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | \(\left.\begin{array}{c}Unsaturated <br>

Fatty Acids (\%)\end{array}\right)\)

About 40 different fatty acids occur naturally. Palmitic acid $\left(\mathrm{C}_{16}\right)$ and stearic $\operatorname{acid}\left(\mathrm{C}_{18}\right)$ are the most abundant saturated acids; oleic and linoleic acids (both $\mathrm{C}_{18}$ ) are the most abundant unsaturated ones. Oleic acid is monounsaturated because it has only one double bond, but linoleic and linolenic acids are polyunsaturated fatty acids (called PUFAs) because they have more than one carbon-carbon double bond. Although the reasons are not yet clear, it appears that a diet rich in saturated fats leads to a higher level of blood cholesterol and consequent higher risk of heart attack than a diet rich in unsaturated fats.

The data in Table 24.3 show that unsaturated fatty acids generally have lower melting points than their saturated counterparts, a trend that's also true for triacylglycerols. Since vegetable oils have a higher proportion of unsaturated fatty acids than do animal fats, they have lower melting points and appear as liquids rather than solids. This behavior arises because the carbon-carbon double bonds in unsaturated vegetable oils introduce bends and kinks into the hydrocarbon chains, making it difficult for the chains to nestle closely together in crystals.

The carbon-carbon double bonds in vegetable oils can be hydrogenated to yield saturated fats in the same way that any alkene can react with hydrogen to yield an alkane (Section 23.10). By carefully controlling the extent of hydrogenation, the final product can have any desired consistency. Margarine, for example, is prepared so that only about two-thirds of the double bonds present in the starting vegetable oil are hydrogenated.


- PROBLEM 24.16 Show the structure of glyceryl trioleate, a fat molecule whose components are glycerol and three oleic acid units.



## Steroids

A steroid is a lipid whose structure is based on the tetracyclic (four-ring) system shown in the following examples. Three of the rings are six-membered, while the fourth is five-membered. Steroids have many diverse roles throughout both the plant and animal kingdoms. Some steroids, such as digitoxigenin, isolated from the purple foxglove Digitalis purpurea, are used in medicine as heart stimulants. Others, such as hydrocortisone, are hormones, and still others have a variety of different physiological functions.
-



Hydrocortisone
The purple foxglove, a common backyard plant, contains the steroidal heart stimulant digitoxigenin.


Cholesterol 3D model

Cholesterol, an unsaturated alcohol whose structure is shown in Figure 24.14, is the most abundant animal steroid. It has been estimated that a 60 kg ( 130 lb ) person has a total of about 175 g of cholesterol distributed throughout the body. Much of this cholesterol is bonded through ester links to fatty acids, but some is found as the free alcohol. Gallstones, for example, are nearly pure cholesterol.

Cholesterol serves two important functions in the body. First, it is a minor component of cell membranes, where it helps to keep the membranes fluid. Second, it serves as the body's starting material for the synthesis of all other steroids, including the sex hormones. Although news reports sometimes make cholesterol sound dangerous, there would be no life without it. The human body obtains its cholesterol both by synthesis in the liver and by ingestion of food. Even on a strict no-cholesterol diet, an adult is able to synthesize approximately 800 mg per day.

## $24.12 \mid$ Nucleic Acids

How does a seed "know" what kind of plant to become? How does a fertilized ovum know how to grow into a human being? How does a cell know what part of the body it's in so that it can carry out the right reactions? The answers to such questions involve the biological molecules called nucleic acids. Deoxyribonucleic acid (DNA) and ribonucleic acid (RNA) are the chemical carriers of an organism's genetic information. Coded in an organism's DNA is all the information that determines the nature of the organism and all the directions that are needed for producing the thousands of different proteins required by the organism.

Just as proteins are polymers made of amino acid units, nucleic acids are polymers made up of nucleotide units linked together to form a long chain. Each nucleotide is composed of a nucleoside plus phosphoric acid, $\mathrm{H}_{3} \mathrm{PO}_{4}$, and each nucleoside is composed of an aldopentose sugar plus an amine base.


The sugar component in RNA is ribose, and the sugar in DNA is 2-deoxyribose (2-deoxy means that oxygen is missing from C 2 of ribose).


Four different cyclic amine bases occur in DNA: adenine, guanine, cytosine, and thymine. Adenine, guanine, and cytosine also occur in RNA, but thymine is replaced in RNA by a related base called uracil.


Adenine (A)
DNA
RNA


Guanine (G) DNA RNA


Cytosine (C)
DNA
RNA


Thymine (T) DNA

In both DNA and RNA, the cyclic amine base is bonded to $\mathrm{C1}^{\prime}$ of the sugar, and the phosphoric acid is bonded to the $\mathrm{C}^{\prime}$ ' sugar position. Thus, nucleosides and nucleotides have the general structures shown in Figure 24.15. (In discussions of RNA and DNA, numbers with a prime superscript refer to positions on the sugar component of a nucleotide; numbers without a prime refer to positions on the cyclic amine base.)

## Maureen M. Julian, "Rosalind

 Franklin: From Coal to DNA to Plant Viruses," J. Chem. Educ., Vol. 60, 1983, 660-662.


Uracil (U) RNA

3D models of Adenine, Guanine, Cytosine, Thymine, and Uracil

FIGURE 24.15 General structures of (a) a nucleoside and (b) a nucleotide. When $Y=H$, the sugar is deoxyribose; when $\mathrm{Y}=\mathrm{OH}$, the sugar is ribose.

FIGURE 24.16 Generalized structure of a nucleic acid.

(a) A nucleoside

(b) A nucleotide

Nucleotides join together in nucleic acids by forming a phosphate ester bond between the phosphate group at the $5^{\prime}$ end of one nucleotide and the hydroxyl group on the sugar component at the $3^{\prime}$ end of another nucleotide (Figure 24.16).


Just as the structure of a protein depends on its sequence of individual amino acids, the structure of a nucleic acid depends on its sequence of individual nucleotides. To carry the analogy further, just as a protein has a polyamide backbone with different side chains attached to it, a nucleic acid has an alternating sugar-phosphate backbone with different amine base side chains attached.


The sequence of nucleotides is described by starting at the $5^{\prime}$ phosphate end and identifying the bases in order. Abbreviations are used for each nucleotide: A for adenosine, G for guanosine, C for cytidine, T for thymidine, and U for uracil. Thus, a typical DNA sequence might be written as -T-A-G-G-C-T-.

## Worked Example 24.4

Draw the full structure of the DNA dinucleotide C-T.

## Solution



- PROBLEM 24.17 Draw the full structure of the DNA dinucleotide A-G.
- PROBLEM 24.18 Draw the full structure of the RNA dinucleotide U-A.

KEY CONCEPT PROBLEM 24.19 Identify the following bases, and tell whether each is found in DNA, RNA, or both.


### 24.13 Base Pairing in DNA: The Watson-Crick Model

Molecules of DNA isolated from different tissues of the same species have the same proportions of nucleotides, but molecules from different species can have quite different proportions. For example, human DNA contains about 30\% each of A and T and about $20 \%$ each of G and C, but the bacterium Clostridium perfringens contains about $37 \%$ each of A and T and only $13 \%$ each of G and C. Note that in both cases, the bases occur in pairs. Adenine and thymine are usually present in equal amounts, as are guanine and cytosine. Why should this be?

According to the Watson-Crick model, DNA consists of two polynucleotide strands coiled around each other in a double helix. The sugar-phosphate backbone is on the outside of the helix, and the amine bases are on the inside, so that a base on one strand points directly in toward a base on the second strand. The two strands run in opposite directions and are held together by hydrogen bonds between pairs of bases. Adenine and thymine form two strong hydrogen bonds to each other, but not to $G$ or $C ; G$ and $C$ form three strong hydrogen bonds to each other, but not to A or T (Figure 24.17).
(O)
A. B. Wolbarst, "DNAmonic," J. Chem. Educ., Vol. 56, 1979,

Michael F. Bruist, Wayne L. Smith, and Galen Mell, "A Simple Demonstration of How Internuclear Forces Make DNA Helical," J. Chem. Educ., Vol. 75, 1998, 53-55

$\nabla$The double-helix structure is a result of hydrogen bonding between pairs of bases, one located on one polynucleotide strand and a complementary base located on the second polynucleotide strand. The sequence of bases on one strand requires a specific, complementary sequence on the second strand.

3D models of the A-T Base Pair, the G-C Base Pair, and DNA



G


C

## Strategy

© FIGURE 24.17 Hydrogen bonding between base pairs in the DNA double helix. Electrostatic potential maps show that the faces of the bases are relatively neutral (green), while the edges have positive (blue) and negative (red) regions. Pairing A with T and G with C brings together oppositely charged regions.

The two strands of the DNA double helix aren't identical; rather, they're complementary. Whenever a G base occurs in one strand, a $C$ base occurs opposite it in the other strand. When an A base occurs in one strand, a T base occurs in the other strand. This complementary pairing of bases explains why A and T are always found in equal amounts, as are G and C. Figure 24.18 illustrates this base pairing, showing how the two complementary strands coil into the double helix. X-ray measurements show that the DNA double helix is 2.0 nm wide, that there are exactly 10 base pairs in each full turn, and that each turn is 3.4 nm high.

## Worked Example 24.5

What sequence of bases on one strand of DNA is complementary to the sequence G-C-A-T-T-A-T on another strand?

Since A and G form complementary pairs with T and C, respectively, go through the given sequence replacing $A$ with $T, G$ with $C, T$ with $A$, and $C$ with $G$

A FIGURE 24.18 The coil of the sugar-phosphate backbone is visible on the outside of the DNA double helix in this computer-generated structure, while the hydrogen-bonded pairs of amine bases lie flat on the inside.

$$
\begin{array}{ll}
\text { Original: } & \text { G-C-A-T-T-A-T } \\
\text { Complement: } & \text { C-G-T-A-A-T-A }
\end{array}
$$

- PROBLEM 24.20 What sequence of bases on one strand of DNA is complementary to the following sequence on another strand?


### 24.14 Nucleic Acids and Heredity

Most DNA of higher organisms, both plant and animal, is found in the nucleus of cells in the form of threadlike strands that are coated with proteins and wound into complex assemblies called chromosomes. Each chromosome is made up of several thousand genes, where a gene is a segment of a DNA chain that contains the instructions necessary to make a specific protein. By decoding the right genes at the right time, an organism uses genetic information to synthesize the thousands of proteins needed for living. Thus, the function of DNA is to act as a storage medium for an organism's genetic information. The function of RNA is to read, decode, and use the information received from DNA to make proteins.

Three main processes take place in the transfer and use of genetic information: Replication is the means by which identical copies of DNA are made, forming additional molecules and preserving genetic information for passing on to offspring. Transcription is the means by which information in the DNA is transferred to and decoded by RNA. Translation is the means by which RNA uses the information to build proteins.


## Replication

DNA replication is an enzyme-catalyzed process that begins with a partial unwinding of the double helix. As the DNA strands separate and bases are exposed, new nucleotides line up on each strand in a complementary manner, A to $T$ and $C$ to $G$, and two new strands begin to grow. Each new strand is complementary to its old template strand, and two new, identical DNA double helixes are produced (Figure 24.19).

FIGURE 24.19 DNA replication. A portion of the DNA double helix unwinds, and complementary nucleotides line up for linking to yield two new DNA molecules. Each of the new DNA molecules contains one of the original strands and one new strand.

-

The magnitude of the replication process is extraordinary. The nucleus of a human cell contains 46 chromosomes ( 23 pairs), each of which consists of one large DNA molecule. Each chromosome, in turn, is made up of several thousand genes, and the sum of all genes in a human cell (the genome) is approximately 3 billion base pairs. This immense base sequence is faithfully copied during replication, with an error occurring only about once each 10 billion100 billion bases.

FIGURE 24.20 Transcription of DNA to synthesize RNA. A small portion of the DNA double helix unwinds, and one of the two DNA strands acts as a template on which ribonucleotides line up. The RNA produced is complementary to the DNA strand from which it is transcribed.

Protein Synthesis movie

FIGURE 24.21 Protein biosynthesis. Messenger RNA is read by tRNA that contains complementary three-base sequences. Transfer RNA then assembles the proper amino acids ( $\mathrm{AA}_{1}, \mathrm{AA}_{2}$, and so on) into position for incorporation into the peptide.

## Transcription

The genetic instructions contained in DNA are transcribed into RNA when a small portion of the DNA double helix unwinds and one of the two DNA strands acts as a template for complementary ribonucleotides to line up, a process similar to that of DNA replication (Figure 24.20). The only difference is that uracil (U) rather than thymine lines up opposite adenine. Once completed, the RNA molecule separates from the DNA template, and the DNA rewinds to its stable doublehelix conformation.


## Translation

Protein biosynthesis is directed by a special kind of RNA called messenger RNA, or $m R N A$, and takes place on knobby protuberances within a cell called ribosomes. The specific ribonucleotide sequence in mRNA acts like a long coded sentence to specify the order in which different amino acid residues are to be joined. Each of the estimated 100,000 proteins in the human body is synthesized from a different mRNA that has been transcribed from a specific gene segment on DNA.

Each "word" along the mRNA chain consists of a series of three ribonucleotides that is specific for a given amino acid. For example, the series cytosine-uracil-guanine (C-U-G) on mRNA is a three-letter word directing that the amino acid leucine be incorporated into the growing protein. The words are read by another kind of RNA called transfer $R N A$, or $t R N A$. Each of the 60 or so different tRNAs contains a complementary base sequence that allows it to recognize a three-letter word on mRNA and act as a carrier to bring a specific amino acid into place for transfer to the growing peptide chain (Figure 24.21). When synthesis of the protein is completed, a "stop" word signals the end, and the protein is released from the ribosome.


## Worked Example 24.6

What RNA base sequence is complementary to the following DNA base sequence?

## G-C-C-T-A-A-G-T-G

## Strategy

Go through the DNA sequence replacing $A$ with $U, G$ with $C, T$ with $A$, and $C$ with $G$.

## Solution

| Original DNA: | G-C-C-T-A-A-G-T-G |
| :--- | :--- |
| Complementary RNA: | C-G-G-A-U-U-C-A-C |

- PROBLEM 24.21 Show how uracil can form strong hydrogen bonds to adenine.
- PROBLEM 24.22 What RNA sequence is complementary to the following DNA sequence?

C-G-T-G-A-T-T-A-C-A

PROBLEM 24.23 From what DNA sequence was the following RNA sequence transcribed?

```
U-G-C-A-U-C-G-A-G-U
```


## Interlude DNA Fingerprinting

 whether Hemings. DNA fingerprinting evidence obtained in 1998 is not conclusive but suggests obtained well may have.
eing a criminal is a lot harder now than it was in the good old days, and part of the reason is the development of DNA fingerprinting. DNA fingerprinting arose from the discovery in 1984 that human genes contain short, repeating sequences of noncoding DNA, called short tandem repeat (STR) loci. The base sequences in these STR loci are slightly different for every individual (except identical twins), so a pattern unique to each person can be obtained by determining the sequences.

Perhaps the most common and well-publicized use of DNA fingerprinting is that carried out by crime laboratories to link suspects to biological evidence-blood, hair follicles, skin, semen, or even items of clothing-found at a crime scene. Thousands of court cases have now been decided based on DNA evidence.

Forensic laboratories in the United States have agreed on 13 core STR loci that are most accurate for identification of an individual. Based on these 13 loci, a Combined DNA Index System (CODIS) has been established to serve as a registry of convicted offenders. If the profile of sequences from a known individual and the profile from DNA obtained at a crime scene match, the probability is approximately 82 billion to 1 that the DNA is from the same individual. In paternity cases, where the DNA of father and offspring are related but not fully identical, the identity of the father can be established with a probability of 100,000 to 1 .

Even after several generations have passed, paternity can still be implied by DNA analysis of the $Y$ chromosome of direct male-line descendants. The most well-known such case is that of Thomas Jefferson, who is thought to have fathered a child by his slave Sally Hemings. Although Jefferson himself has no male-line descendants, DNA analysis of the male-line descendants of Jefferson's paternal uncle showed the same $Y$ chromosome as a male-line descendant of Eston Hemings, youngest son of Sally Hemings.

Among its many other applications, DNA fingerprinting is widely used for the diagnosis of genetic disorders. Cystic fibrosis, hemophilia, Huntington's disease, Tay-Sachs disease, and sickle-cell anemia are among the many diseases that can be detected, enabling early treatment of an affected child. In addition, the U.S. Department of Defense now requires blood and saliva samples from all military personnel. The samples are stored, and DNA is extracted should the need for identification of a casualty arise.

- PROBLEM 24.24 What characteristic of human DNA makes fingerprinting possible?

Fats, carbohydrates, and proteins are metabolized in the body to yield acetyl CoA, which is further degraded in the citric acid cycle to yield two molecules of $\mathrm{CO}_{2}$ plus a large amount of energy. The energy output of the various steps in the citric acid cycle is coupled to the electron-transport chain, a series of enzyme-catalyzed reactions whose ultimate purpose is to synthesize adenosine triphosphate (ATP).

Proteins are large biomolecules consisting of $\boldsymbol{\alpha}$-amino acids linked together by amide, or peptide, bonds. Twenty amino acids are commonly found in proteins, and all except glycine have a handedness. In general, any carbon atom bonded to four different groups has a handedness and is said to be chiral. Proteins can be classified either by shape or biological function. Fibrous proteins are tough, threadlike, and water insoluble; globular proteins are compact, water soluble, and mobile within cells. Some proteins are enzymes, some are hormones, and some are structural or transport agents.

A protein's primary structure is its amino acid sequence. Its secondary structure is the orientation of segments of the protein chain into a regular pattern, such as an $\boldsymbol{\alpha}$-helix or a $\boldsymbol{\beta}$-pleated sheet. Its tertiary structure is the three-dimensional shape into which the entire protein molecule is coiled.

Enzymes are large proteins that function as biological catalysts and whose specificity is due to a lock-and-key fit between enzyme and substrate. Enzymes contain a crevice, inside which is an active site, a small three-dimensional region of the enzyme with the specific shape necessary to bind the proper substrate.

Carbohydrates are polyhydroxy aldehydes and ketones. Simple carbohydrates such as glucose can't be hydrolyzed to smaller molecules; complex carbohydrates such as starch and
cellulose contain many simple sugars linked together. Monosaccharides such as glucose exist as a mixture of an open-chain form and two cyclic forms called the $\alpha$ form and the $\beta$ form. Disaccharides such as sucrose contain two simple sugars joined by a linking oxygen atom.

Lipids are the naturally occurring organic molecules that dissolve in a nonpolar solvent. There are a great many different kinds of lipids. Animal fats and vegetable oils are triacylglycerols-esters of glycerol with three long-chain fatty acids. The fatty acids are unbranched, have an even number of carbon atoms, and may be either saturated or unsaturated.

Deoxyribonucleic acid (DNA) and ribonucleic acid (RNA) are the chemical carriers of an organism's genetic information. Nucleic acids are made up of many individual building blocks, called nucleotides, linked together to form a long chain. Each nucleotide consists of a cyclic amine base linked to C1 of a sugar, with the sugar in turn linked to phosphoric acid. The sugar component in RNA is ribose; the sugar in DNA is 2-deoxyribose. The bases in DNA are adenine (A), guanine (G), cytosine (C), and thymine ( T ); the bases in RNA are adenine, guanine, cytosine, and uracil (U). Molecules of DNA consist of two complementary polynucleotide strands held together by hydrogen bonds between bases on the two strands and coiled into a double helix. Adenine and thymine form hydrogen bonds only to each other, as do cytosine and guanine.

Three processes take place in the transfer of genetic information: Replication is the process by which identical copies of DNA are made and genetic information is preserved. Transcription is the process by which messenger RNA is produced. Translation is the process by which mRNA directs protein synthesis.

## Key Words

active site 1045
adenosine triphosphate (ATP) 1033
alpha- ( $\alpha$-) amino acid 1037
alpha- ( $\alpha$-) helix 1042
anabolism 1032
beta- ( $\beta$-) pleated sheet 1043
biochemistry 1031
C-terminal amino acid 1041
carbohydrate 1047
catabolism 1032
chromosome 1059
coenzyme 1045
cofactor 1045
deoxyribonucleic acid
(DNA) 1055
enzyme 1044
fatty acid 1052
gene 1059
lipid 1051
lock-and-key model 1045
metabolism 1032
monosaccharide 1047
$\mathbf{N}$-terminal amino acid 1041
nucleic acid 1055
nucleoside 1055
nucleotide 1055
peptide bond 1035
polypeptide 1035
polysaccharide 1047
primary structure 1042
protein 1035
quaternary structure 1042
replication 1059
ribonucleic acid (RNA) 1055
secondary structure 1042
steroid 1054
substrate 1045
tertiary structure 1042
transcription 1059
translation 1059
triacylglycerol 1052
Watson-Crick model 1057

## Key Concept Summary

- 



## 1 <br> Understanding Key Concepts

Problems 24.1-24.24 appear within the chapter.
24.25 Identify the following amino acids, and tell whether each is acidic, basic, or neutral.
(O)

(a)

(b)
24.26 Identify the following amino acids:
©

24.27 Does the following model represent a D-amino acid or an L-amino acid? Identify it.
\%

24.28 Is the following model of glucose in the $\alpha$ form or the $\beta$ $\%$

24.29 The following model represents D-ribose in its openchain form. Is ribose an aldose or a ketose? How many chiral carbon atoms does ribose have?

24.30 Identify the following dipeptide:
(O)

24.31 Identify the following amine bases found in nucleic acids:

(a)

(b)

## Additional Problems

## Amino Acids, Peptides, and Proteins

24.32 What does the prefix " $\alpha$ " mean when referring to $\alpha$-amino acids?
24.33 Why are the naturally occurring amino acids called L-amino acids?
24.34 What amino acids do the following abbreviations stand for?
(a) Ser
(b) Thr
(c) Pro
(d) Phe
(e) Cys
24.35 Name and draw the structures of amino acids that fit the following descriptions:
(a) Contains an isopropyl group
(b) Contains an alcohol group
(c) Contains a thiol (-SH) group
(d) Contains an aromatic ring
24.36 Much of the chemistry of amino acids is the familiar chemistry of carboxylic acid and amine functional groups. What products would you expect to obtain from the following reactions of glycine?


24.37 Aspartame, marketed under the trade name NutraSweet for use as a nonnutritive sweetener, is the methyl ester of a simple dipeptide. Identify the two amino acids present in aspartame, and show all the products of digestion, assuming that both amide and ester bonds are hydrolyzed in the stomach.

24.39 Look at the structure of angiotensin II in Figure 24.5, and identify both the N -terminal and C -terminal amino acids.
24.40 What is meant by the following terms as they apply to proteins?
(a) Primary structure
(b) Secondary structure
(c) Tertiary structure
24.41 What is the difference between fibrous and globular proteins?
24.42 What kinds of intramolecular interactions are important in stabilizing a protein's tertiary structure?
24.43 What kind of bonding stabilizes helical and $\beta$-pleated-sheet secondary protein structures?
24.44 Why is cysteine such an important amino acid for defining the tertiary structure of proteins?
24.45 Which of the following amino acids are most likely to be found on the outside of a globular protein, and which on the inside? Explain.
(a) Valine
(b) Leucine
(c) Aspartic acid
(d) Asparagine
24.46 Use the three-letter abbreviations to name all tripeptides containing methionine, isoleucine, and lysine.
24.47 How many tetrapeptides containing alanine, serine, leucine, and glutamic acid do you think there are? Use the three-letter abbreviations to name three.
24.48 Write structural formulas for the two dipeptides containing phenylalanine and glutamic acid.
24.49 Write the structural formula of Asp-Met-Pro-Gly.

## Molecular Handedness

24.50 Which of the following objects are chiral?
(a) A shoe
(b) A bed
(c) A lightbulb
(d) A flowerpot
24.51 Give two examples of chiral objects and two examples of achiral objects.
24.38 Identify the amino acids present in the following hexapeptide:

24.52 Which of the following compounds are chiral?
(a) 2,4-Dimethylheptane
(b) 5-Ethyl-3,3-dimethylheptane
24.53 Draw chiral molecules that meet the following descriptions:
(a) A chloroalkane, $\mathrm{C}_{5} \mathrm{H}_{11} \mathrm{Cl}$
(b) An alcohol, $\mathrm{C}_{6} \mathrm{H}_{14} \mathrm{O}$
(c) An alkene, $\mathrm{C}_{6} \mathrm{H}_{12}$
(d) An alkane, $\mathrm{C}_{8} \mathrm{H}_{18}$
24.54 There are eight alcohols with the formula $\mathrm{C}_{5} \mathrm{H}_{12} \mathrm{O}$. Draw them, and tell which are chiral.
24.55 Propose structures for compounds that meet the following descriptions:
(a) A chiral alcohol with four carbons
(b) A chiral aldehyde
(c) A compound with two chiral centers

## Carbohydrates

24.56 What is the structural difference between an aldose and a ketose?
24.57 Classify each of the following carbohydrates by indicating the nature of its carbonyl group and the number of carbon atoms present. For example, glucose is an aldohexose.
(a)

(b)

(c)

24.58 Starch and cellulose are both polymers of glucose. What is the main structural difference between them, and what different roles do they serve in nature?
24.59 Starch and glycogen are both $\alpha$-linked polymers of glucose. What is the structural difference between them, and what different roles do they serve in nature?
24.60 Write the open-chain structure of a ketotetrose.
24.61 Write the open-chain structure of a four-carbon deoxy sugar.
24.62 D-Mannose, an aldohexose found in orange peels, has the following structure in open-chain form. Coil mannose around, and draw it in cyclic $\alpha$ and $\beta$ forms.

24.63 Draw D-galactose in its cyclic $\alpha$ and $\beta$ forms.

24.64 Show two D-mannose molecules (Problem 24.62) attached by an $\alpha-1,4$ link.
24.65 Show two D-galactose molecules (Problem 24.63) attached by a $\beta-1,4$ link.

## Lipids

24.66 What is a fatty acid?
24.67 What does it mean to say that fats and oils are triacylglycerols?
24.68 Draw the structure of glycerol myristate, a fat made from glycerol and three myristic acid molecules (see Table 24.3).
24.69 Spermaceti, a fragrant substance isolated from sperm whales, was a common ingredient in cosmetics until its use was banned in 1976 to protect the whales from extinction. Chemically, spermaceti is cetyl palmitate, the ester of palmitic acid (see Table 24.3) with cetyl alcohol (the straight-chain $\mathrm{C}_{16}$ alcohol). Show the structure of spermaceti.
24.70 There are two isomeric fat molecules whose components are glycerol, one palmitic acid, and two stearic acids (see Table 24.3). Draw the structures of both, and explain how they differ.
24.71 One of the two molecules you drew in Problem 24.70 is chiral. Which molecule is chiral, and why?
24.72 Draw the structures of all products you would obtain by reaction of the following lipid with aqueous KOH . What are the names of the products?

24.73 Draw the structure of the product you would obtain on hydrogenation of the lipid in Problem 24.72. What is its name? Would the product have a higher or lower melting point than the original lipid? Why?
24.74 What products would you obtain by treating oleic acid with the following reagents?
(a) $\mathrm{Br}_{2}$
(b) $\mathrm{H}_{2}$, Pd catalyst
(c) $\mathrm{CH}_{3} \mathrm{OH}, \mathrm{HCl}$ catalyst
24.75 Look up the structure of linoleic acid in Table 24.3, and draw all potential products of its reaction with 2 mol of HCl .

## Nucleic Acids

24.76 What is a nucleotide, and what three kinds of components does it contain?
24.77 What are the names of the sugars in DNA and RNA, and how do they differ?
24.78 Where in the cell is most DNA found?
24.79 What is meant by the following terms as they apply to nucleic acids?
(a) Base pairing
(b) Replication
(c) Translation
(d) Transcription
24.80 What is the difference between a gene and a chromosome?
24.81 What genetic information does a single gene contain?
24.82 Show by drawing structures how the phosphate and sugar components of a nucleic acid are joined.
24.83 Show by drawing structures how the sugar and amine base components of a nucleic acid are joined.
24.84 Draw the complete structure of deoxycytidine 5'-phosphate, one of the four deoxyribonucleotides.
24.85 Draw the complete structure of guanosine 5'-phosphate, one of the four ribonucleotides.
24.86 If the sequence T-A-C-C-G-A appeared on one strand of DNA, what sequence would appear opposite it on the other strand?
24.87 What sequence would appear on the mRNA molecule transcribed from the DNA in Problem 24.86?
24.88 Human insulin is composed of two polypeptide chains. One chain contains 21 amino acids, and the other contains 30 amino acids. How many nucleotides are present in the DNA to code for each chain?
24.89 The DNA from sea urchins contains about $32 \% \mathrm{~A}$ and about $18 \% \mathrm{G}$. What percentages of T and C would you expect in sea urchin DNA? Explain.

## General Problems

24.90 One of the constituents of the carnauba wax used in floor and furniture polish is an ester of a $C_{32}$ straightchain alcohol with a $\mathrm{C}_{20}$ straight-chain carboxylic acid. Draw the structure of this ester.
24.91 Cytochrome $c$ is an important enzyme found in the cells of all aerobic organisms. Elemental analysis of cytochrome $c$ shows that it contains $0.43 \%$ iron. What is the minimum molecular mass of this enzyme?
24.92 The catabolism of glucose to yield carbon dioxide and water has $\Delta G^{\circ}=-2870 \mathrm{~kJ} / \mathrm{mol}$. What is the value of $\Delta G^{\circ}$ for the photosynthesis of glucose from carbon dioxide and water in green plants?
24.93 The endorphins are a group of naturally occurring neuroproteins that act in a manner similar to morphine to control pain. Research has shown that the biologically active part of the endorphin molecule is a simple pentapeptide called an enkephalin, with the structure Tyr-Gly-Gly-PheMet. Draw the complete structure of this enkephalin.
24.94 Write full structures for the following peptides, and indicate the positions of the amide bonds:
(a) Val-Phe-Cys
(b) Glu-Pro-Ile-Leu
24.95 The $\alpha$-helical segments of myoglobin and other proteins stop when a proline residue is encountered in the chain. Why is proline never encountered in a protein $\alpha$-helix?
24.96 Jojoba wax, used in candles and cosmetics, is partially composed of the ester of stearic acid and a straightchain $\mathrm{C}_{22}$ alcohol. Draw the structure of this ester.
24.97 Write representative structures for the following:
(a) A fat
(b) A vegetable oil
(c) A steroid
24.98 What DNA sequence is complementary to the following sequence?

## A-G-T-T-C-A-T-C-G

24.99 Protonation of the side chain in arginine occurs on the double-bonded nitrogen atom. Draw three resonance structures of the protonated product.

## Multi-Concept Problems

24.100 The relative degree of unsaturation in a fat or oil is expressed as an iodine number. Olive oil, for instance, is highly unsaturated and has an iodine number of 172, while butter is much less unsaturated and has an iodine number of 37 . Defined as the number of grams of $I_{2}$ absorbed per 100 grams of fat, the iodine number is based on the fact that the carbon-carbon double bonds in fats and oils undergo an addition reaction with $\mathrm{I}_{2}$. The larger the number of double bonds, the larger the amount of $I_{2}$ that reacts.


To determine an iodine number, a known amount of fat is treated with a known amount of $I_{2}$. When the reaction is complete (about 1 h ), the amount of excess $\mathrm{I}_{2}$ remaining is determined by titration with $\mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ according to the equation

$$
2 \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}(a q)+\mathrm{I}_{2}(a q) \longrightarrow \mathrm{Na}_{2} \mathrm{~S}_{4} \mathrm{O}_{6}(a q)+2 \mathrm{Nal}(a q)
$$

Knowing both the amount of $\mathrm{I}_{2}$ originally added and the amount remaining after reaction, the iodine number can be calculated.

Assume that 0.500 g of human milk fat is allowed to react with 25.0 mL of $0.200 \mathrm{M} \mathrm{I}_{2}$ solution and that 81.99 mL of $0.100 \mathrm{M} \mathrm{Na}_{2} \mathrm{~S}_{2} \mathrm{O}_{3}$ is required for complete reaction with the excess $\mathrm{I}_{2}$.
(a) What amount (in grams) of $\mathrm{I}_{2}$ was added initially?
(b) How many grams of $\mathrm{I}_{2}$ reacted with the milk fat, and how many grams were in excess?
(c) What is the iodine number of human milk fat?
(d) Assuming a molecular mass of 800 amu , how many double bonds does an average molecule of milk fat contain?
24.101 The protonated form of a neutral amino acid such as alanine is a diprotic acid, $\mathrm{H}_{2} \mathrm{~A}^{+}$, with two acid dissociation constants, one for the $-\mathrm{NH}_{3}{ }^{+}$group and one for the $-\mathrm{CO}_{2} \mathrm{H}$ group.

(a) Which group is more acidic, the $-\mathrm{NH}_{3}{ }^{+}$or the $-\mathrm{CO}_{2} \mathrm{H}$ ?
(b) What percentage of each form-protonated $\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right)$, neutral (HA), and deprotonated ( $\mathrm{A}^{-}$) -is present in aqueous solution at $\mathrm{pH}=4.00$ ?
(c) What percentage of each form-protonated $\left(\mathrm{H}_{2} \mathrm{~A}^{+}\right)$, neutral (HA), and deprotonated ( $\mathrm{A}^{-}$) -is present in aqueous solution at $\mathrm{pH}=8.50$ ?
(d) At what pH is the neutral form present in maximum amount?

## eMedia Problems

24.102 Watch the Chirality movie (eChapter 24.3), and answer the following questions:
(a) What conditions are required for a carbon in a molecule to be chiral?
(b) How many chiral carbons are there in the structure in Problem 24.7(c)?
24.103 Choose 2 of the amino acids from the 3D Models in eChapter 24.2, and draw structural formulas. Draw the structural formula for the dipeptide formed by a condensation reaction between the two. What would be the other product?
24.104 View the 3D Models of L-alanine and D-alanine in eChapter 24.3. Draw structural formulas for each molecule showing the chiral nature of the isomers. Identify the functional groups on the central carbon.
24.105 Watch the Energy and Enzymes movie (eChapter 24.6) and answer the following questions:
(a) What is meant by the term inhibition?
(b) Name two different ways that enzyme inhibition can occur.
24.106 Choose one of the 3D Models of amine bases in eChapter 24.12, and draw the structural formula. Use the structure you have drawn along with the sugar ribose to write out the first three reaction steps represented in the Nucleic Acid activity to demonstrate the formation a nucleotide.


[^0]:    Original quantity $\times$ Conversion factor $=$ Equivalent quantity

[^1]:    *The atomic mass unit (amu) is defined in Section 2.6.

[^2]:    $\mathrm{ClO}^{-}$Hypochlorite ion (less oxygen than chlorite)
    $\mathrm{ClO}_{2}^{-}$Chlorite ion
    $\mathrm{ClO}_{3}{ }^{-}$Chlorate ion
    $\mathrm{ClO}_{4}^{-}$Perchlorate ion (more oxygen than chlorate)

[^3]:    3.9 Solution Stoichiometry
    3.10 Titration
    3.11 Percent Composition and Empirical Formulas
    3.12 Determining Empirical Formulas: Elemental Analysis
    3.13 Determining Molecular Masses: Mass Spectrometry

    - Interlude—Did Ben Franklin Have Avogadro's Number? A Ballpark Calculation

[^4]:    $\square$The number of significant figures in the answer to any calculation should be limited only by the number of significant digits in measured quantities. When selecting an atomic mass for use in a calculation, use one more significant figure than is found in the least precise measured quantity involved in the calculation.

[^5]:    Richard A. Kjonas, "An analogy for Solubility: Marbles and Magnets," J. Chem. Educ., Vol. 61, 1984, 765.

    V
    A functional definition of insoluble is that some of the compound remains in the solid state when about $10^{-3} \mathrm{~mol}$ of the compound is placed in contact with one liter of water. It does not mean that none of the compound dissolves.

[^6]:    REDUCING AGENT

    - Causes reduction
    - Loses one or more electrons
    - Undergoes oxidation
    - Oxidation number of atom increases
    oxidizing agent - Causes oxidation
    - Gains one or more electrons
    - Undergoes reduction
    - Oxidation number of atom decreases

[^7]:    N. C. Thomas and R. Brown, "A Spectacular Demonstration of Flame Tests," J. Chem. Educ., Vol. 69, 1992, 326. Brightly-colored flashes of light resulting from the ignition of cellulose nitrate impregnated with salts of sodium, potassium, strontium, and barium ions demonstrate light emission from these energetically excited ions.

[^8]:    Pedro L. Muino, "Introducing the Uncertainty Principle Using Diffraction of Light Waves," J. Chem. Educ., Vol. 77, 2000, 1025-1027.

[^9]:    *Some books and reference sources adopt the opposite sign convention for electron affinity, giving it a positive value and defining it as the energy absorbed when an anion loses an electron.

[^10]:    *The standard pressure, listed here and in most other books as 1 atm, has been redefined to be 1 bar, which is equal to 0.986923 atm . The difference is small, however, and has little effect on the accuracy of existing thermodynamic measurements.

[^11]:    *Barium hydroxide octahydrate, $\mathrm{Ba}(\mathrm{OH})_{2} \cdot 8 \mathrm{H}_{2} \mathrm{O}$, is a crystalline compound that contains eight water molecules clustered around the barium atom. We'll learn more about hydrates in Section 14.15.

[^12]:    v
    Atmospheric pressure is measured with a barometer; the pressure of any gas is measured with a manometer. If gas pressure $>$ atmospheric pressure, $P_{\text {gas }}=P_{\text {atm }}+\Delta h_{\text {mercury; }}$ if gas pressure $<$ atmospheric pressure, $P_{\text {gas }}=P_{\text {atm }}-\Delta h_{\text {mercury }}$.

[^13]:    Rick Broniec, "Boyle's Law and the Monster Marshmallow," J. Chem. Educ., Vol. 59, 1982, 974.

[^14]:    Charles' law The volume of an ideal gas varies directly with absolute temperature. That is, $V$ divided by $T$ is constant when $n$ and $P$ are held constant.

    $$
    V \propto T \quad \text { or } \quad V / T=k \text { at constant } n \text { and } P
    $$

[^15]:    Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Nonadditivity of Volumes," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), p. 14. The volume of a solution of two miscible liquids is shown to not equal the sum of the volumes of the individual liquids before mixing.

[^16]:    Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Making Hydrogen Gas from an Acid and a Base," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 33-34. Hydrogen gas is produced in flasks and collected in balloons.

[^17]:    * The proton that is transferred to water when the acid dissociates is shown in color. $\quad{ }^{\dagger} \mathrm{p} K_{\mathrm{a}}=-\log K_{\mathrm{a}}$.

[^18]:    Lee R. Summerlin, Christie L. Borgford, and Julie B. Ealy, "Colorful Complex Ions in Ammonia," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 75-76.
    $\left\{\begin{array}{l}\text { Lee R. Summerlin, Christie L. } \\ \text { Borgford, and Julie B. Ealy, }\end{array}\right.$ Borgford, and Julie B. Ealy, "Green and Blue Copper Complexes," Chemical Demonstrations, A Sourcebook for Teachers, Vol. 2 (American Chemical Society, Washington, DC, 1988), pp. 71-72.

[^19]:    Bassam Z. Shakhashiri, "Acidic and Basic Properties of
    Oxides," Chemical Demonstrations, A Handbook for Teachers of Chemistry, Vol. 3 (The University of Wisconsin Press, Madison, 1989) pp. 109-113.

[^20]:    The Nernst equation relates the concentration of any chemical species, including $\mathrm{H}^{+}$, to cell potential. This relationship is utilized in a pH meter which measures a cell potential and displays its value in terms of pH .

[^21]:    *Diamond
    ${ }^{\dagger}$ White Sn

[^22]:    *Electrical conductivity relative to an arbitrary value of 100 for silver
    ${ }^{\dagger}$ Ionization energy

[^23]:    * The elastic modulus, measured in units of pressure ( 1 gigapascal $=1 \mathrm{GPa}=10^{9} \mathrm{~Pa}$ ) indicates the stiffness of a material when it is subjected to a load. The larger the value, the stiffer the material.
    ${ }^{\dagger}$ Numbers on the Mohs hardness scale range from 1 for talc, a very soft material, to 10 for diamond, the hardest known substance.

[^24]:    Energy changes for nuclear reactions are on the order of a million times greater than energy changes for chemical reactions.

[^25]:    *The bonds whose connections aren't specified are assumed to be attached to carbon or hydrogen atoms in the rest of the molecule.

